$$=egin{bmatrix} rac{\partial \langle q_1|A_1
angle}{\partial \mathbf{r}_{11}} & \dots & rac{\partial \langle q_{n_{ ext{feat}}}|A_1
angle}{\partial \mathbf{r}_{11}} & \dots & rac{\partial \langle q_{n_{ ext{feat}}}|A_1
angle}{\partial \mathbf{r}_{21}} & rac{\partial \langle q_{n_{ ext{feat}}}|A_1
angle}{\partial \mathbf{r}_{21}} & \dots & rac{\partial \langle q_{n_{ ext{feat}}}|A_1
angle & \mathbf{r}_{21} & \mathbf{r}_{21} \end{pmatrix}$$

 $\partial \mathbf{r}_{31}$ 

 $\mathbf{J}_1 \in \mathbb{R}^{3n_{ ext{atoms}},n_{ ext{feat}}}$