

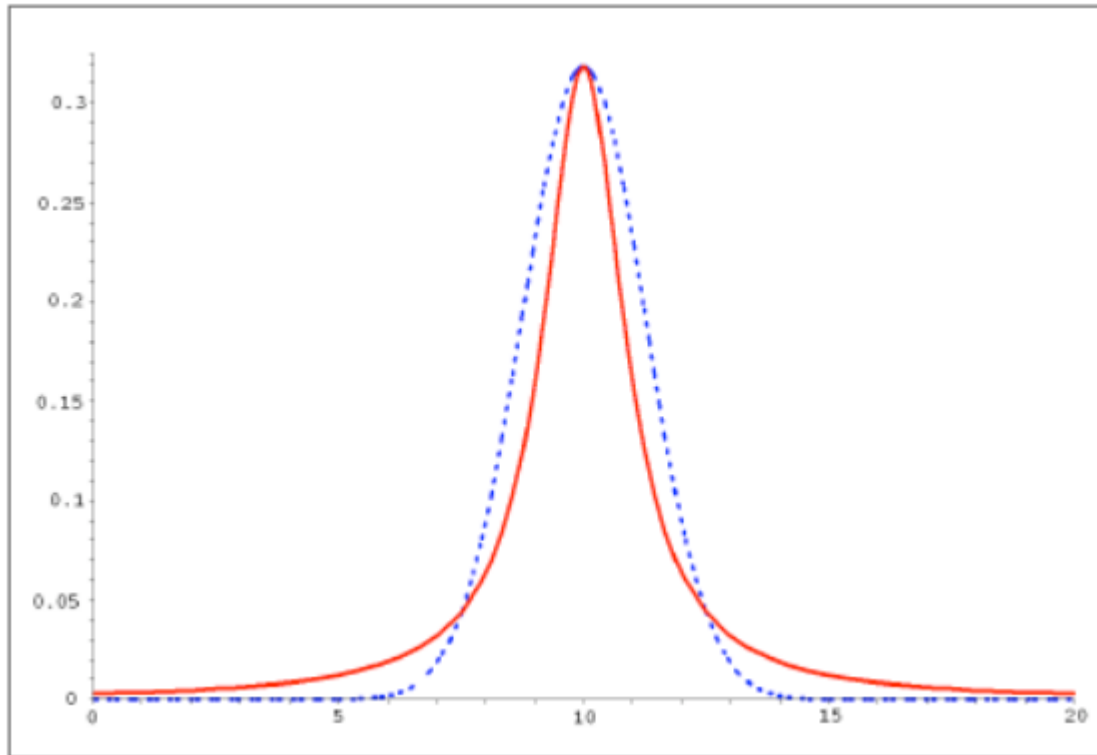
The t -test

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Multivariate statistics @ ELTE

The t distribution

- Determine if a sample is from the hypothetical population



Mean (μ) – the location of the peak
Variance (σ) – the width of the peak
Degrees of freedom (ν) – the $n - 1$

The significance of the t -test

- In the Cauchy the Mean and the variance is undefined
- When $\nu > 2$ the mean is defined but the variance depends on ν
- The smaller the n the larger the sample variance and the larger the variance of the t distribution
- Introducing the effect of sampling and uncertainty

t -test assumptions

- Derive from the definition:
 - Decide if a sample's mean is from a given population with given variance and mean and of family gaussian
- Normality assumption : it must be approximated well with a t distribution
- Variance assumption : we are not testing it in the t test so it is assumed to be equal

The Bayesian *t*-test

- *T*-Test – $P(\text{Data}|\text{hypothesis})$ is our data is from the expected population?
- *Bayes*: $P(\text{Hypothesis}|\text{data})$ is it likely to be that population if I collected this data?
 - *Uncertainty already introduced*
 - *B.E.S.T. test: Reallocate probability \rightarrow Approximate the parameter values*
 - *The Priors have little effect on the Posterior here*
 - *MCMC – potential parameter values, These are approximations*
 - *It return an interval too (95%) to give a more stable estimate*