

Machine learning on electrophysiology EEG/MEG signals

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with

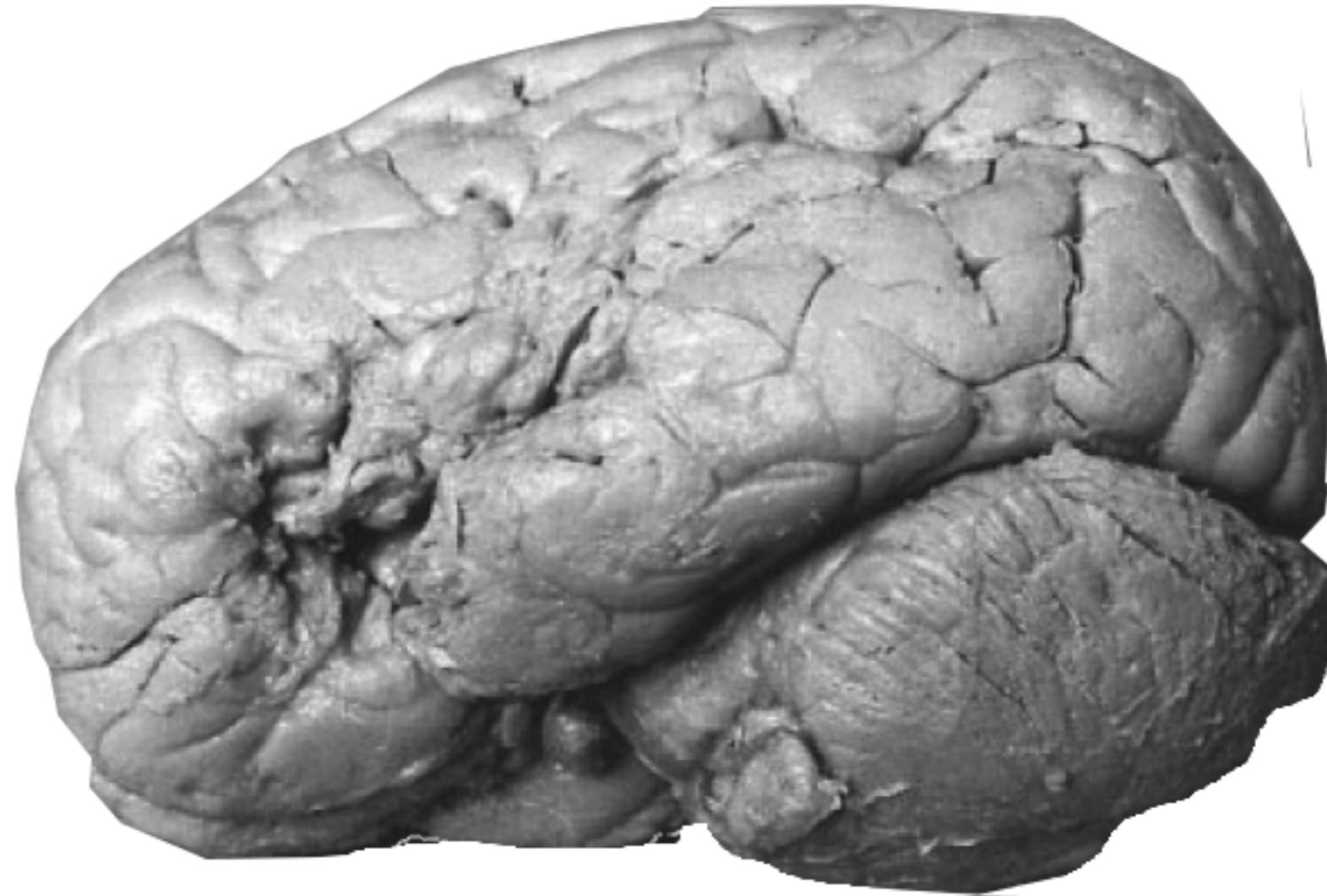
MNE

<http://mne.tools>

scikit
learn

<https://scikit-learn.org>

Before imaging the brain...



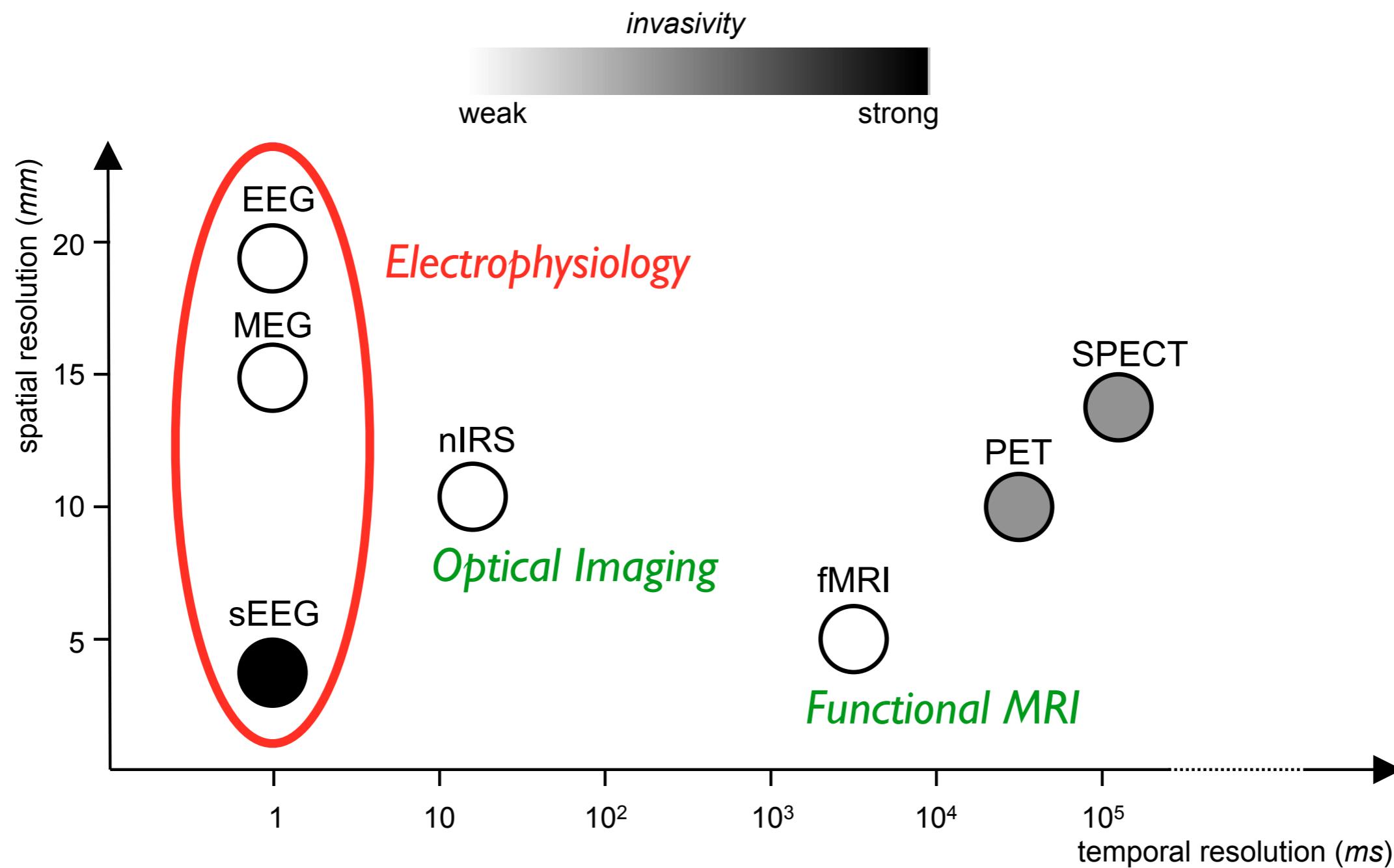
Mr Le Borgne's brain preserved in museum Dupuytren in Paris

Mr Le Borgne, a.k.a “Tan”, could not speak

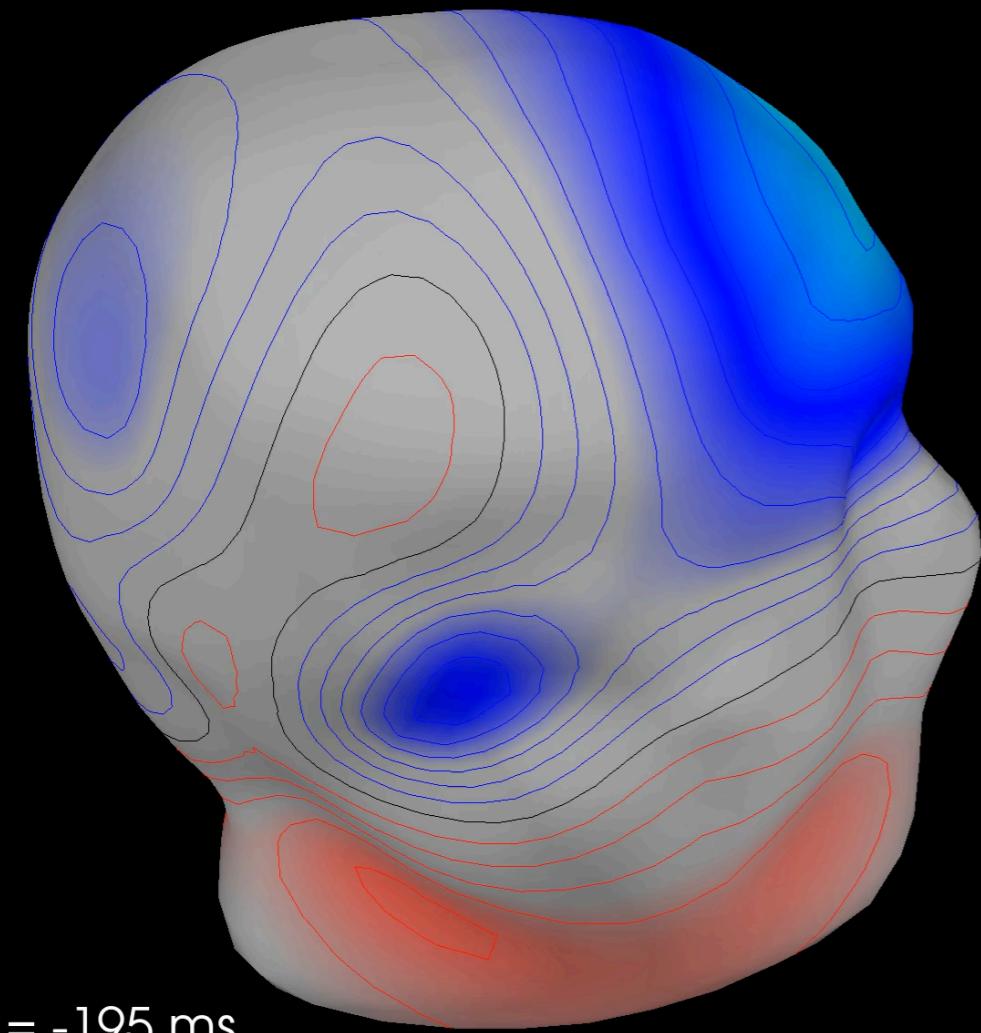
He allowed the French neurologist **Paul Broca** to understand
the functional role of the so-called “Broca’s area”

Functional neuroimaging

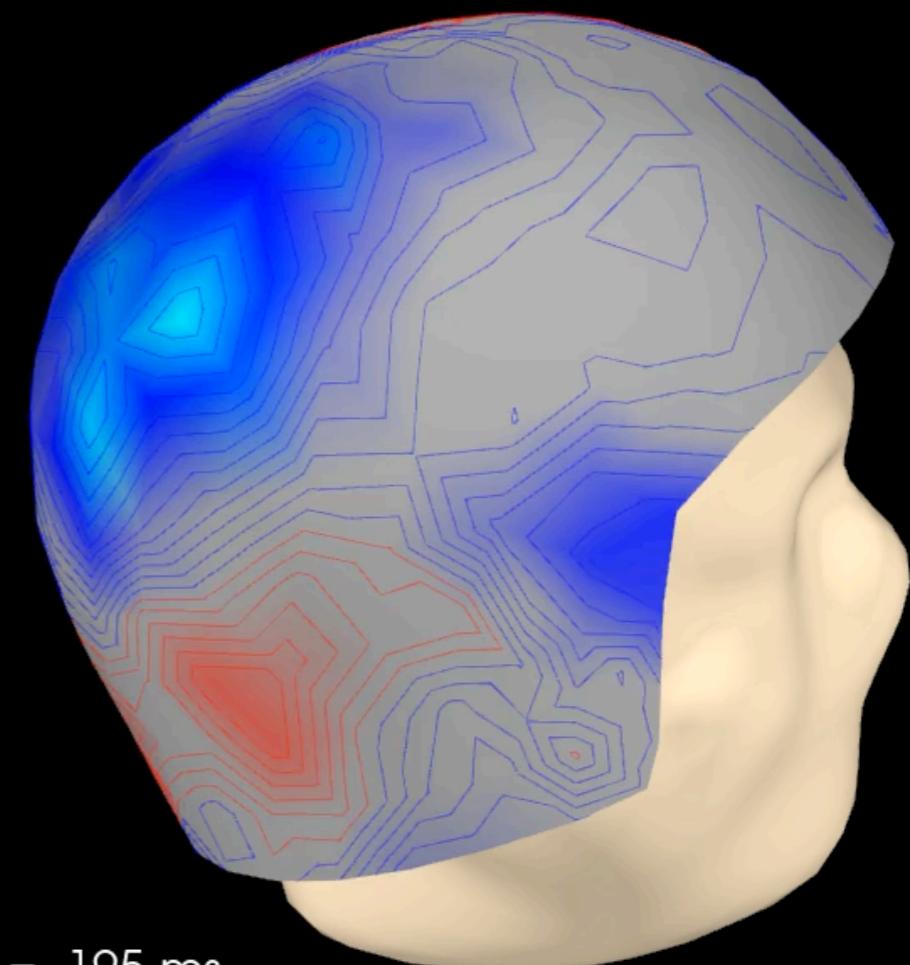
It's the study of the **brain activity** through **functional imaging devices**



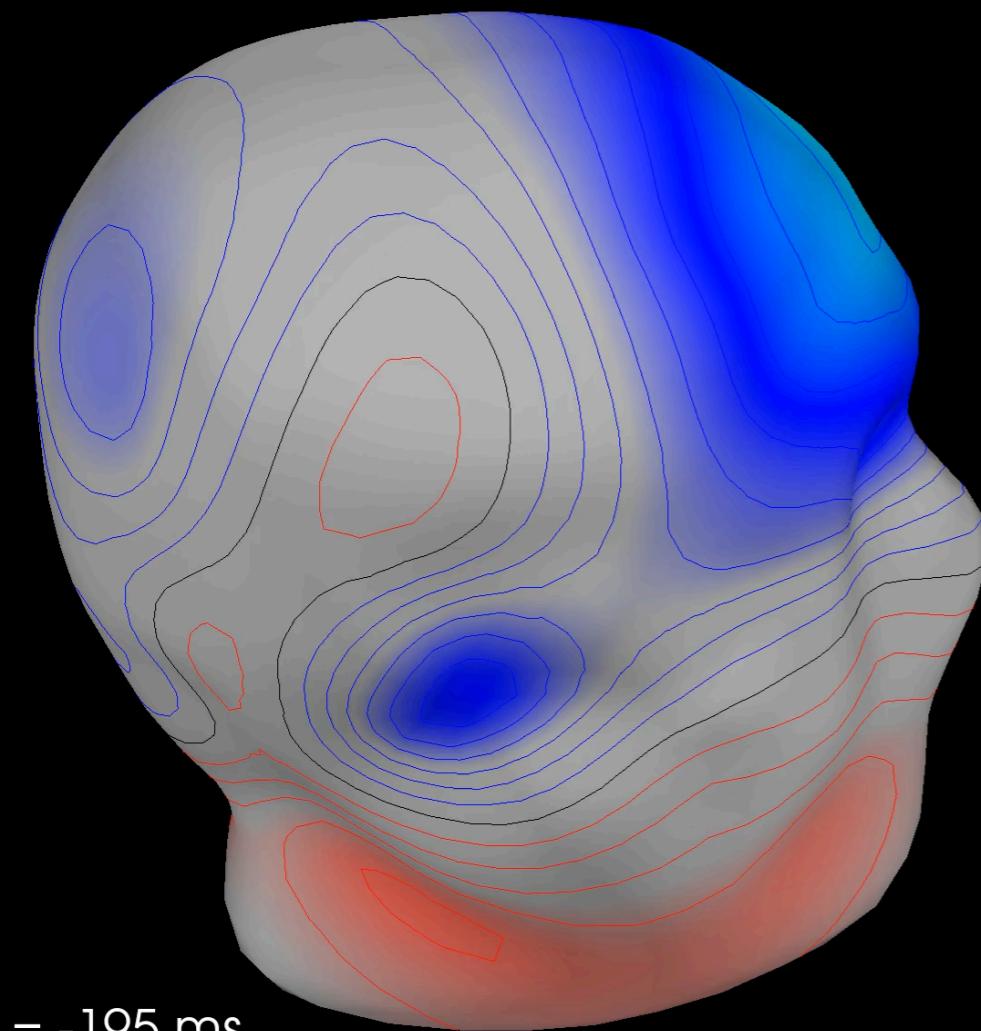
Electroencephalography (EEG)
Electric Potential [V]



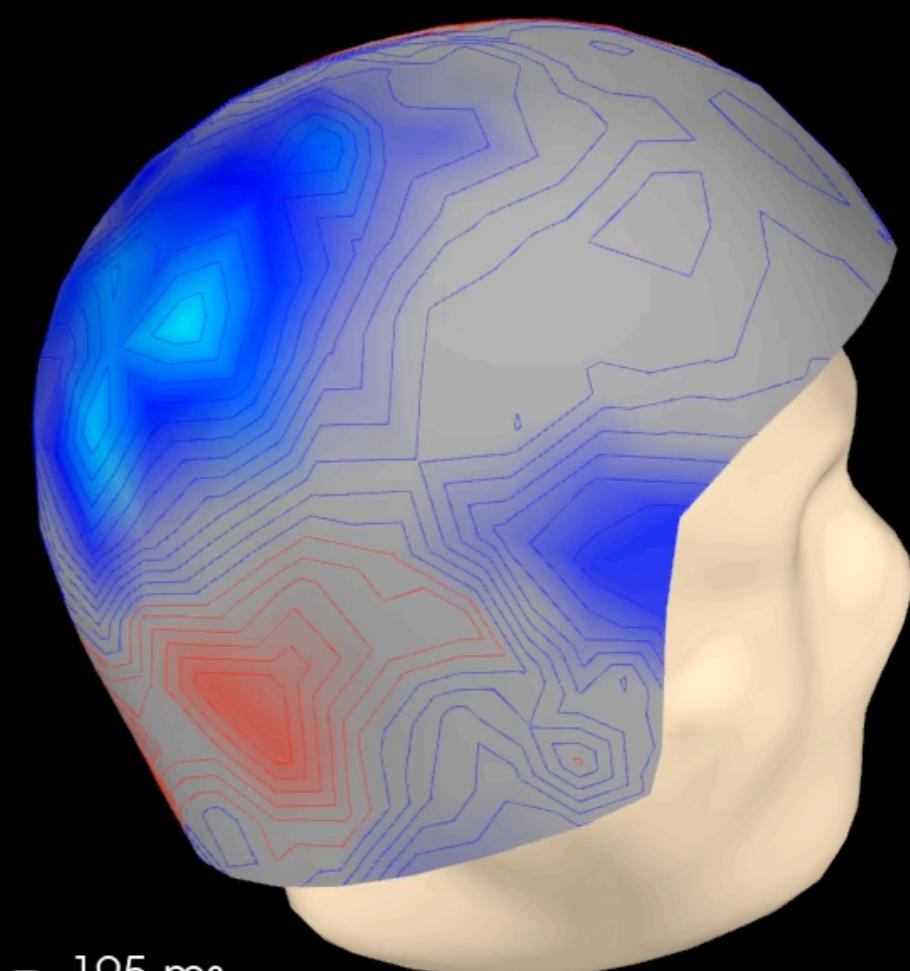
Magnetoencephalography (MEG)
Magnetic field [T]



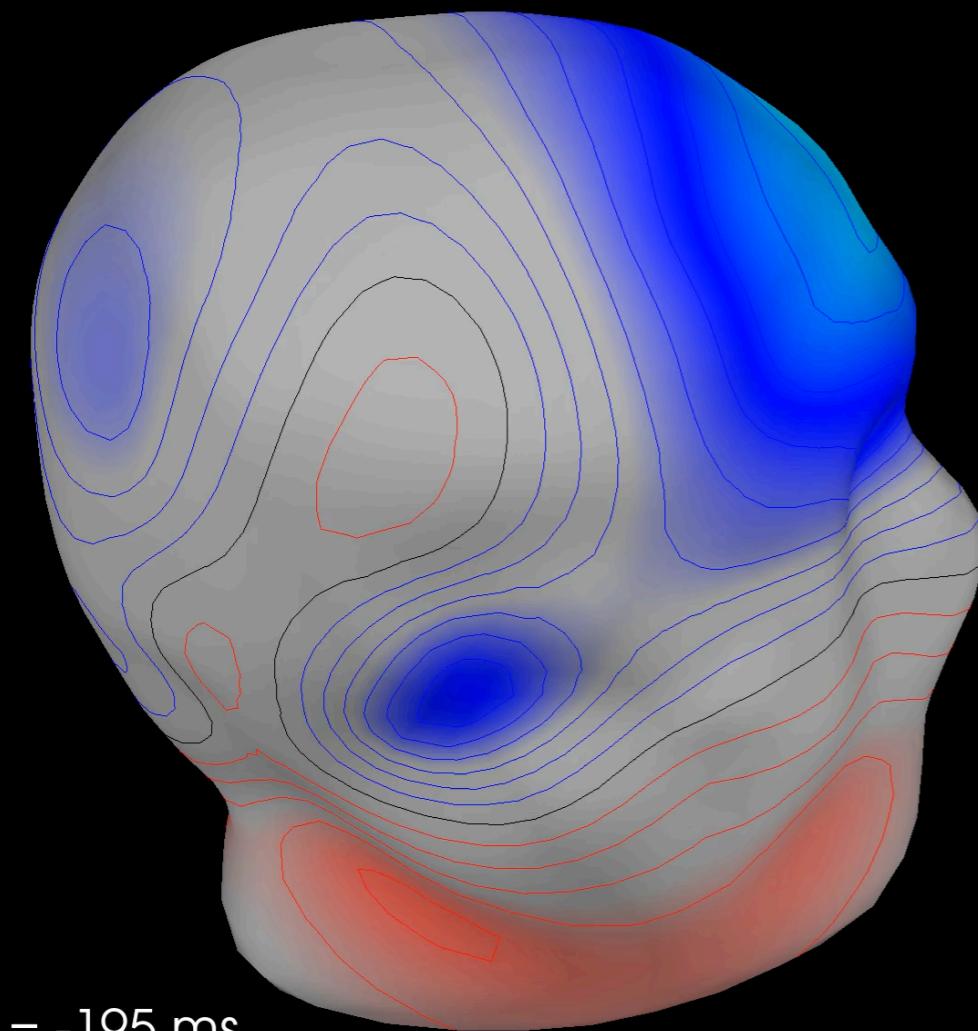
Electroencephalography (EEG)
Electric Potential [V]



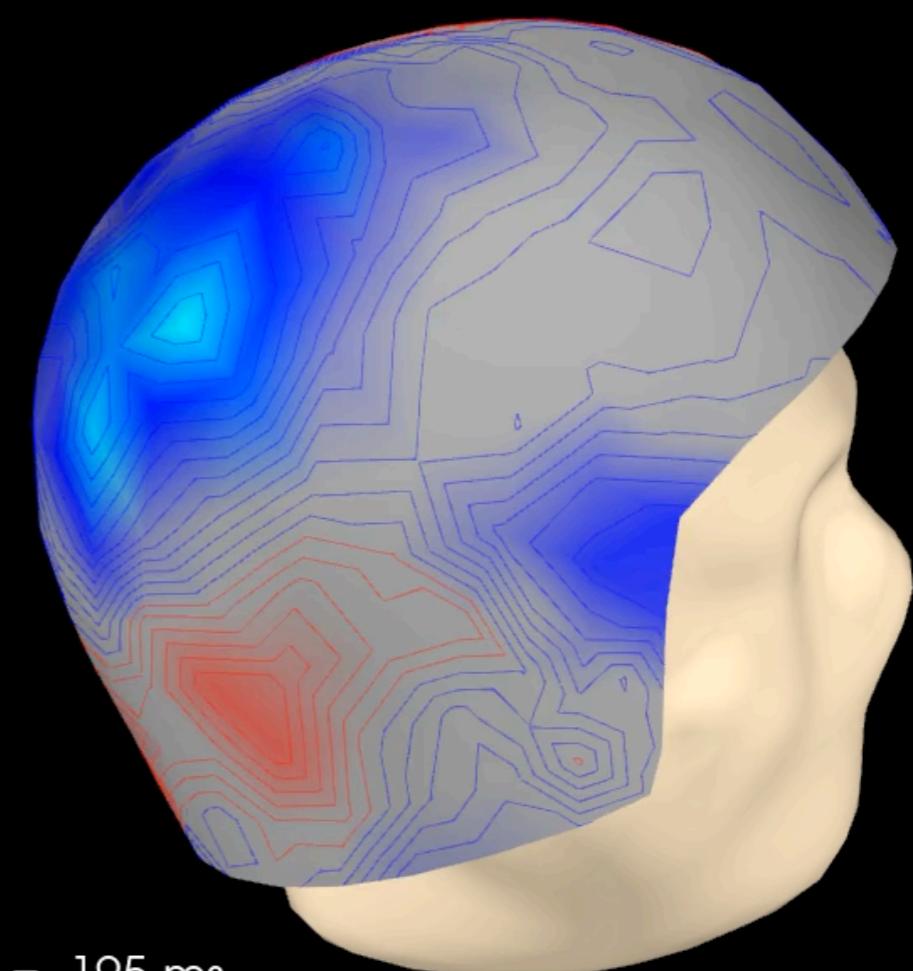
Magnetoencephalography (MEG)
Magnetic field [T]

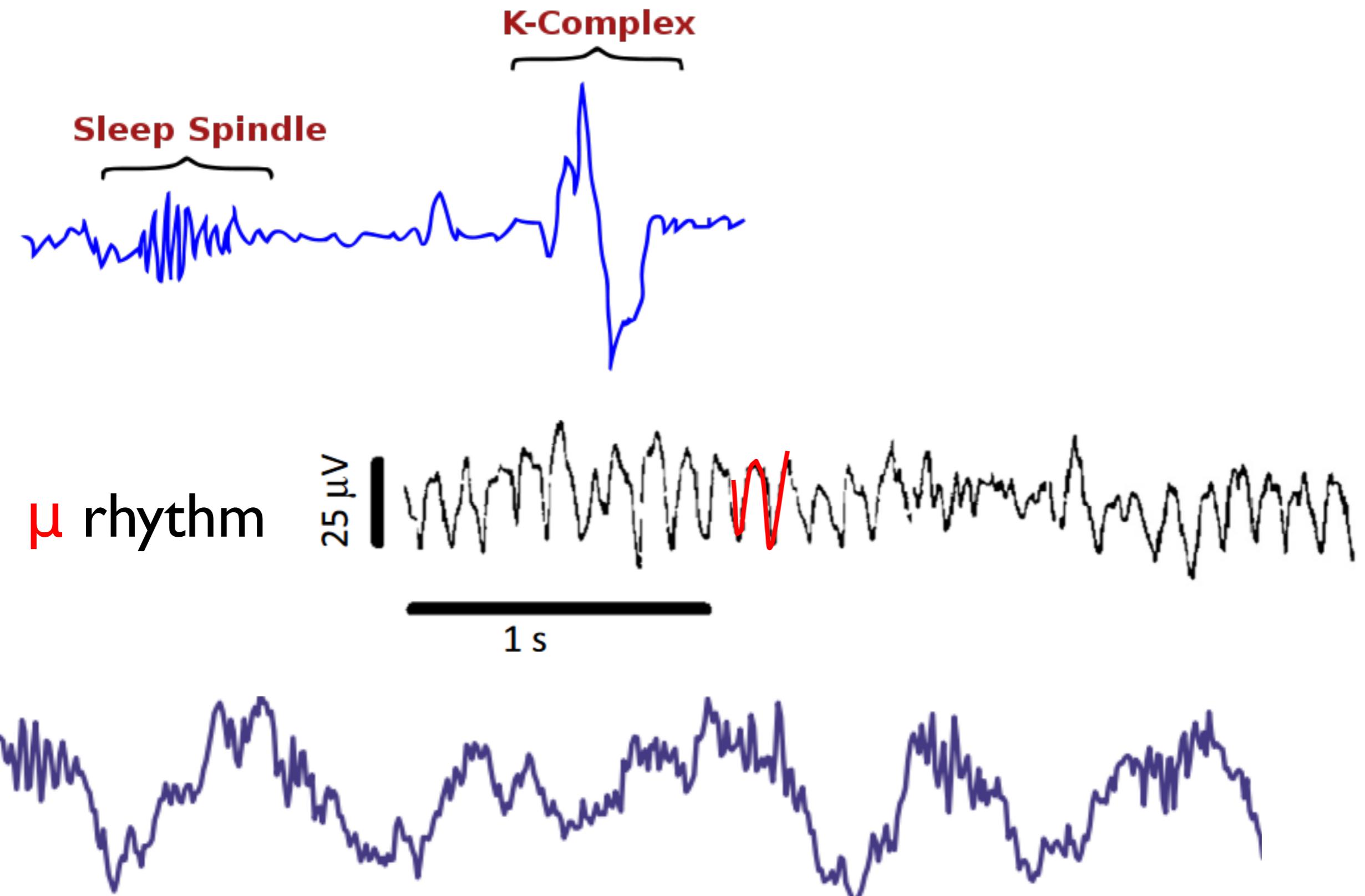


Electroencephalography (EEG)
Electric Potential [V]

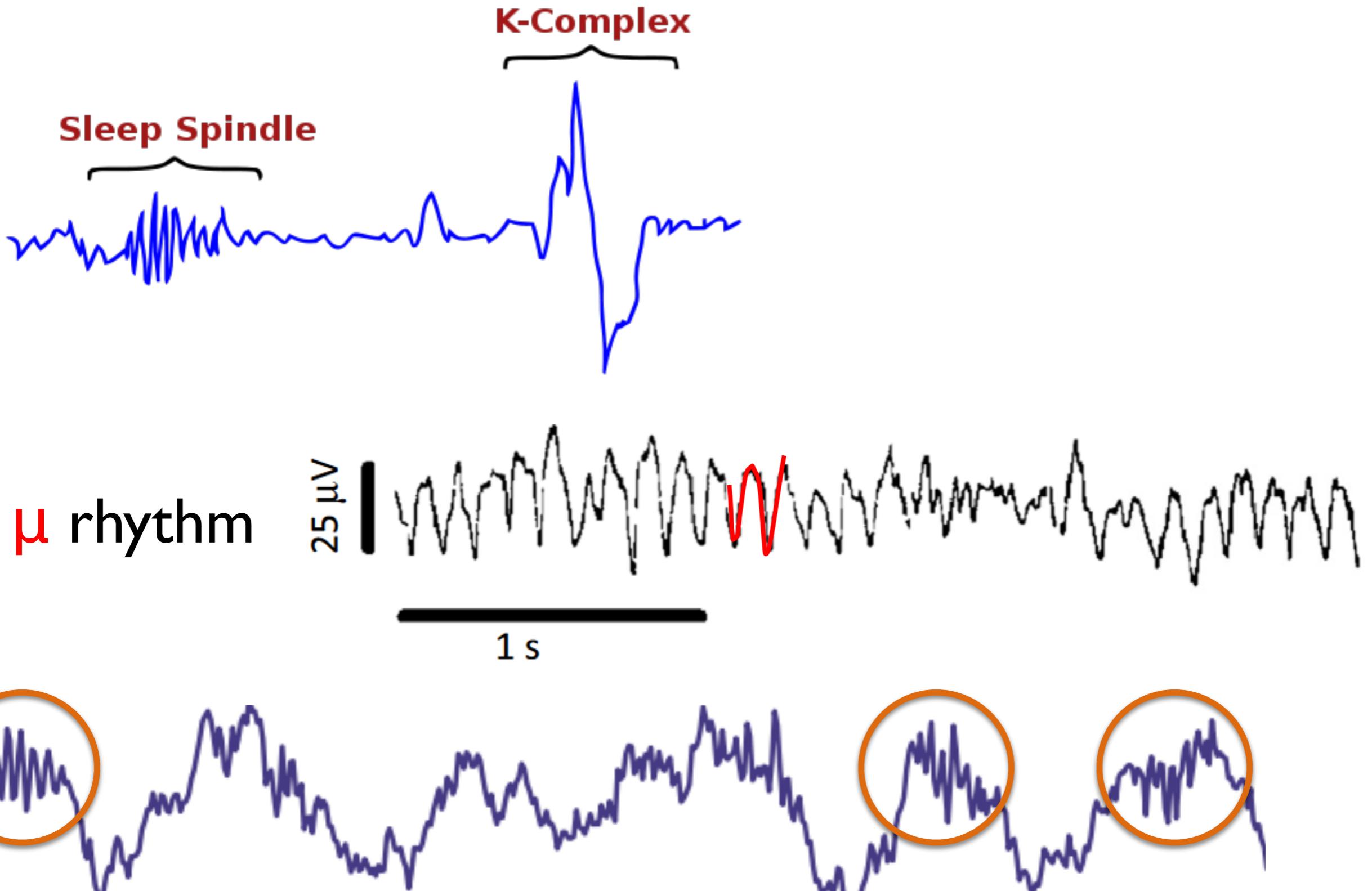


Magnetoencephalography (MEG)
Magnetic field [T]

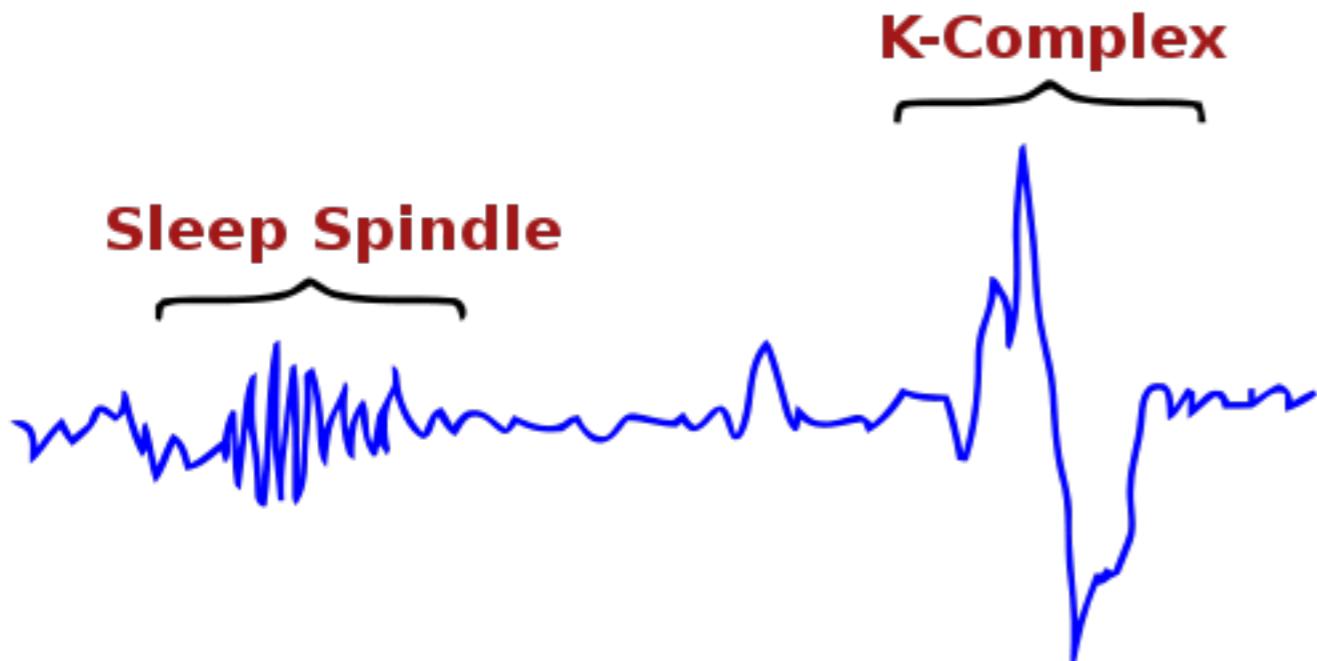




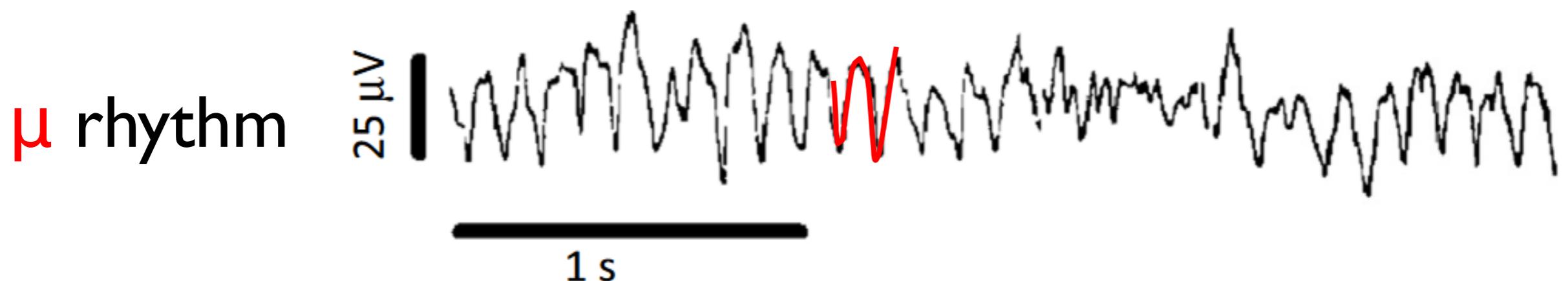
[T. Dupré la Tour, L. Tallot, L. Grabot, V. Doyère, V. van Wassenhove, Y. Grenier, A. Gramfort,
(2017) PLOS Computational biology]



CFC: High frequency bursts coupled with slow waves



Neural signals exhibit diverse and complex morphologies



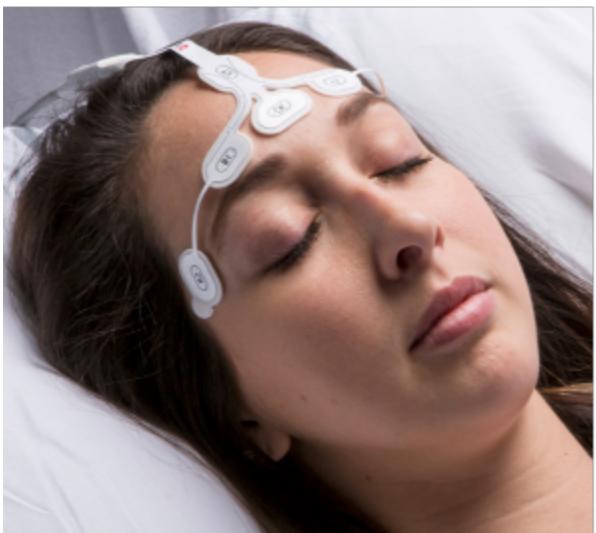
CFC: High frequency bursts coupled with slow waves



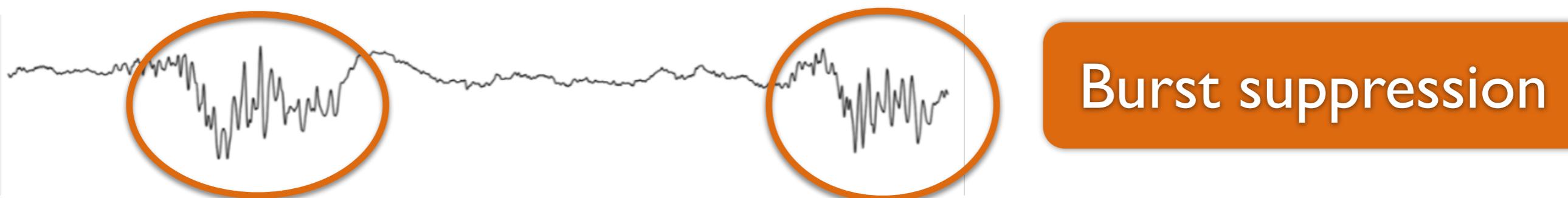
(abnormal) EEG during general anaesthesia (GA)



Burst suppression



(abnormal) EEG during general anaesthesia (GA)



Burst suppression

Propofol

Sevoflurane

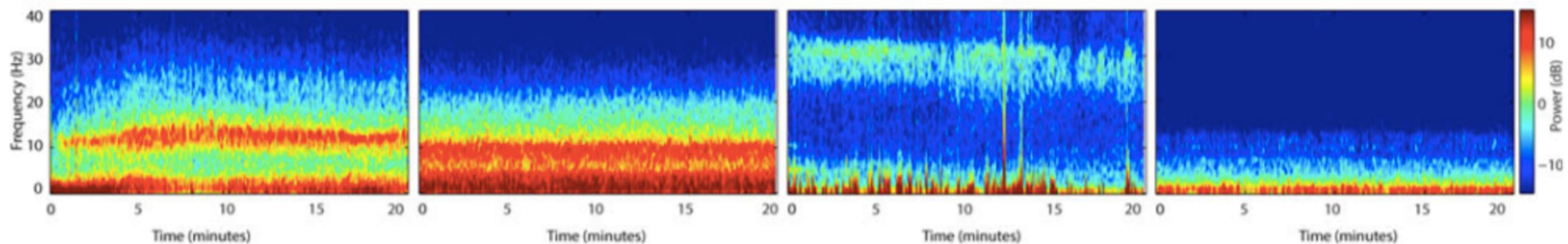
Ketamine

Dexmedetomidine

A



B



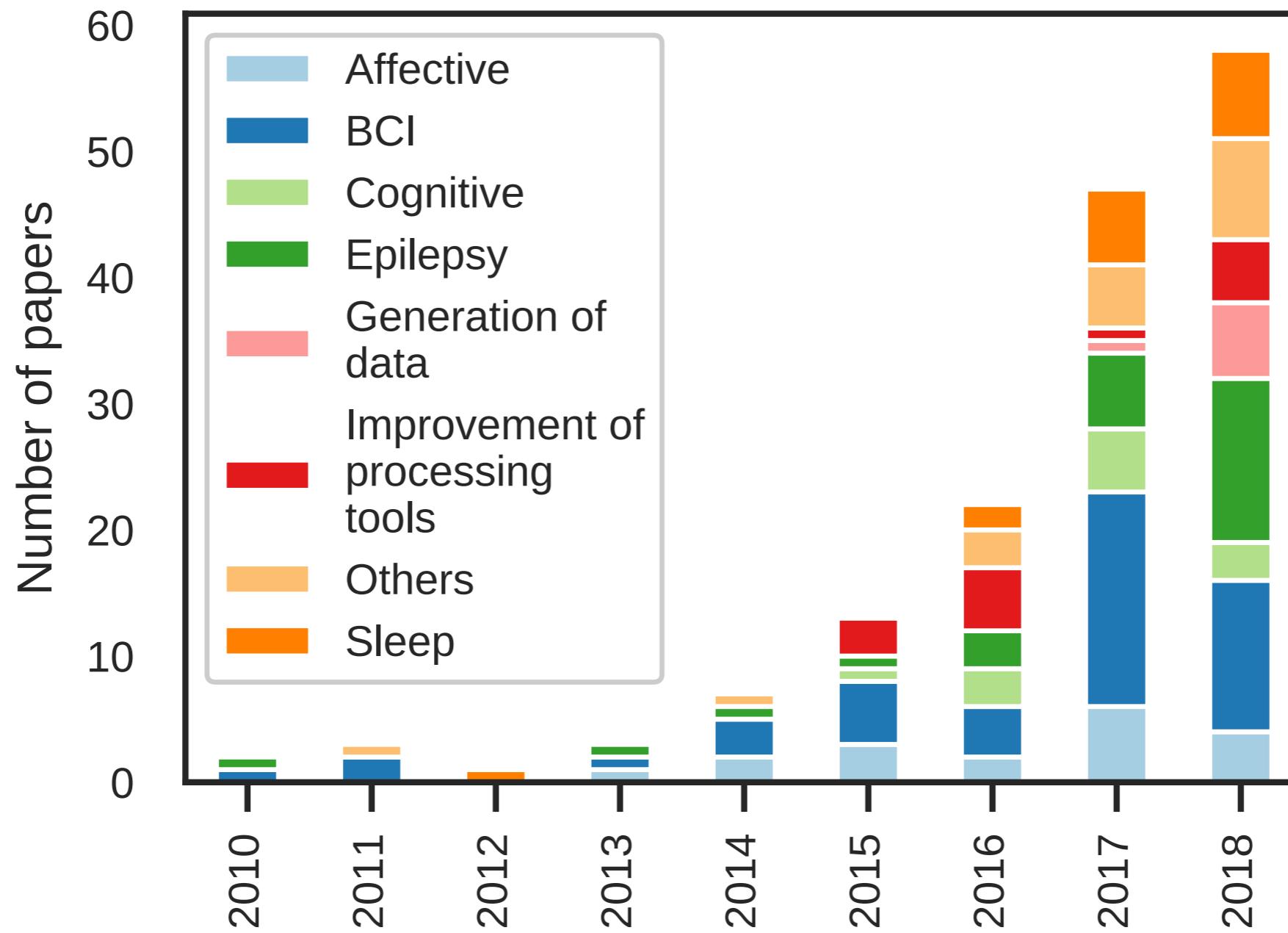
GABAergic Inhibition

GABAergic Inhibition + others

NMDA Inhibition

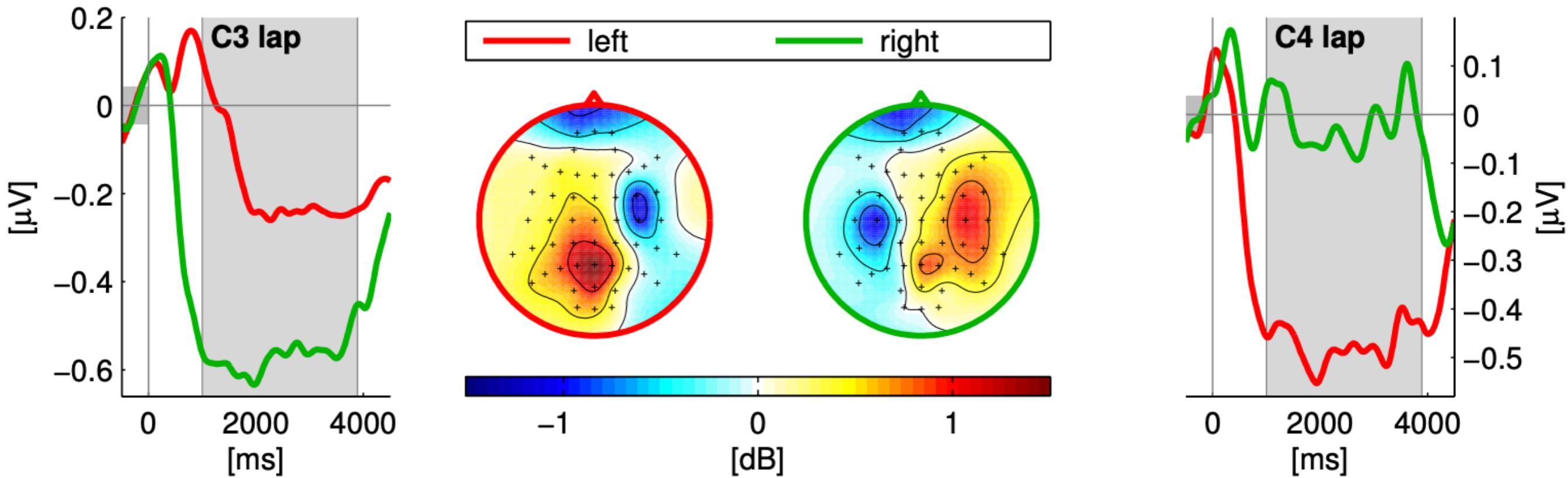
α_2 Adrenergic-mediated Inhibition

Deep Learning papers on EEG



[Deep learning-based electroencephalography analysis: a systematic review
Roy, Y., Banville, H., Albuquerque, I., Gramfort, A., Falk, T. and Faubert, J. (2019)
Journal of Neural Engineering 16: (051001).]

Example: Motor Imagery



Event-Related Desynchronization (ERD) during motor imagery of the left and the right hand. Averaged signal Hilbert enveloppe between 9 and 13Hz on C3 and C4 (After Laplace / Current Source Density transform)

[Blankertz et al. 2008]

Example: P300 Speller



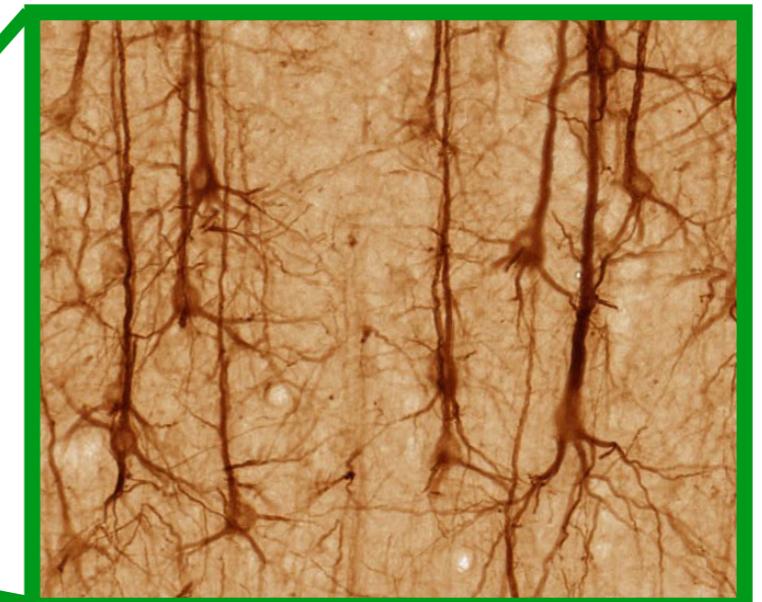
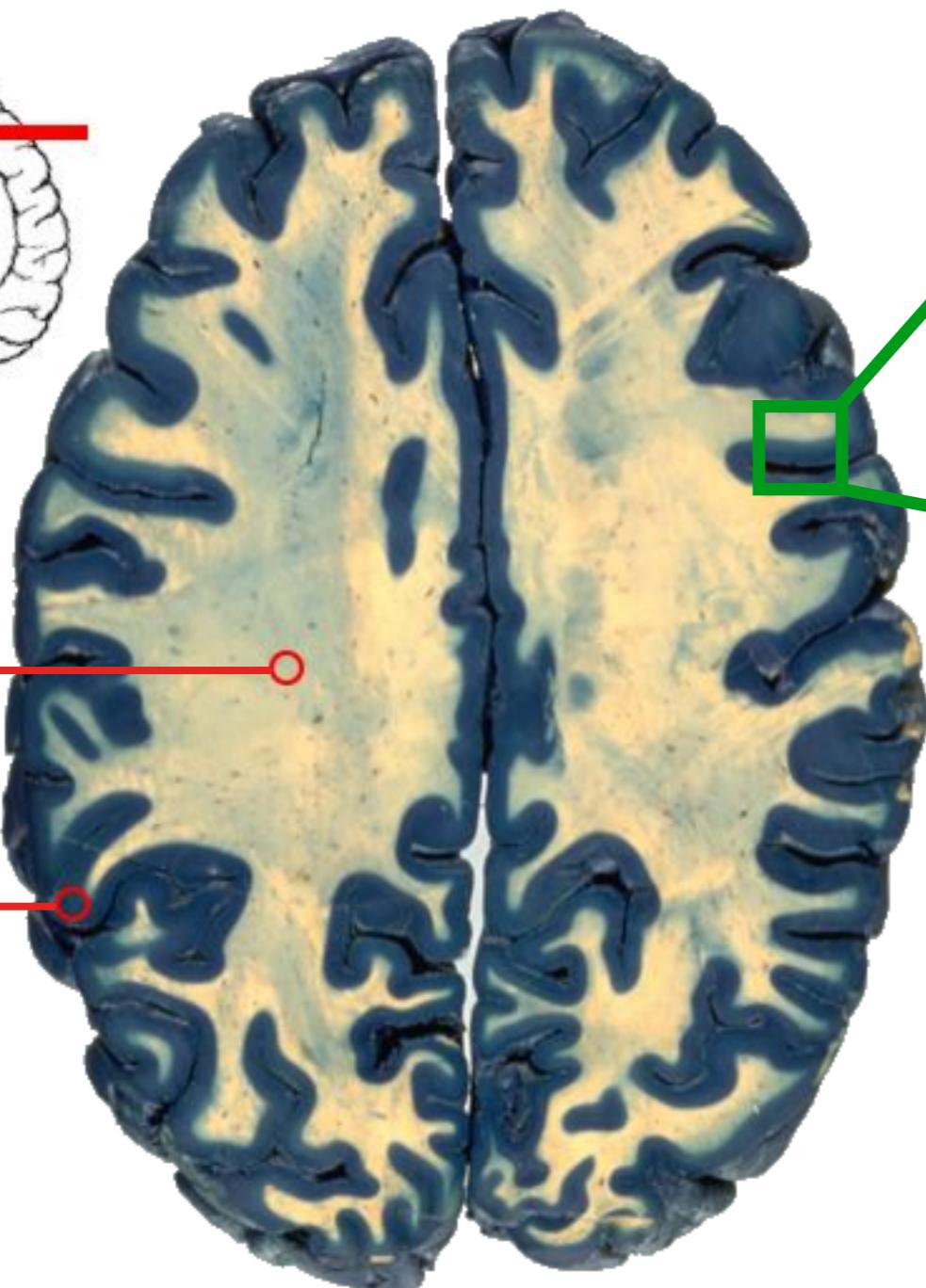
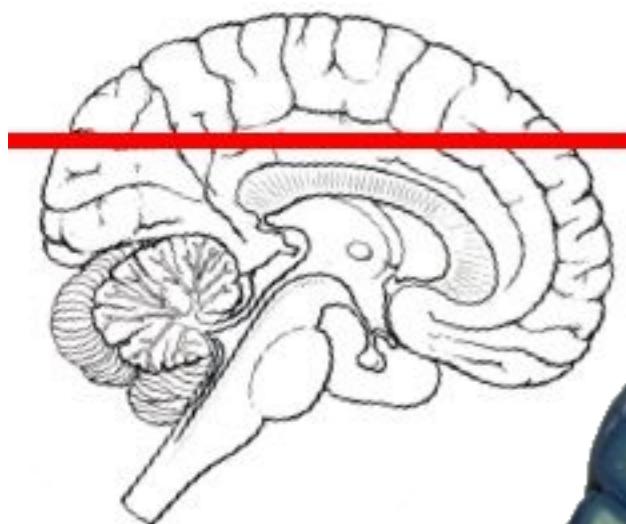
https://www.youtube.com/watch?v=1WzU_8_qA6w

inria

Part I: Electrophysiology: Origin of the signals

Brain anatomy

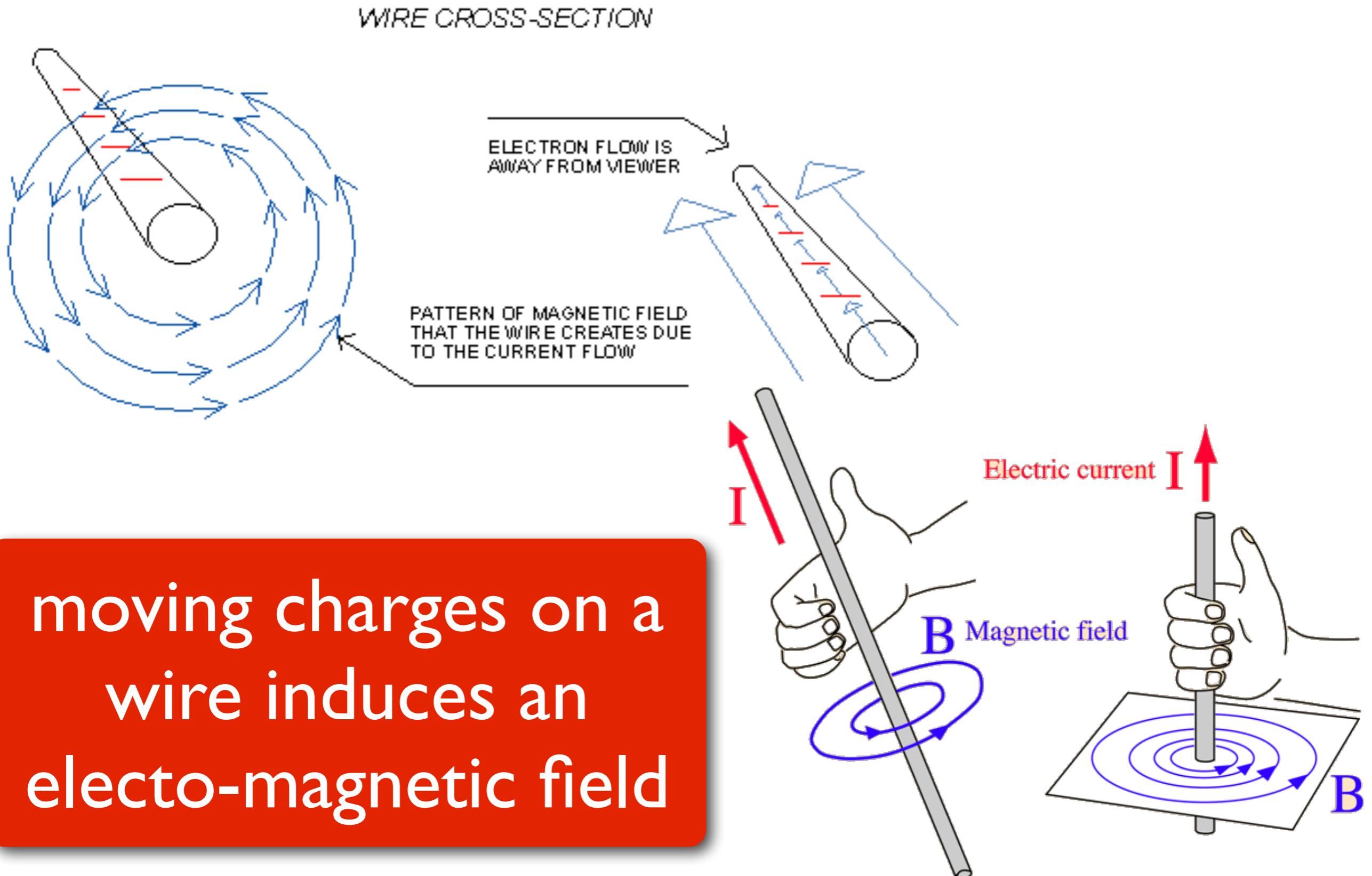
Axial slice



Neurons
in the gray matter

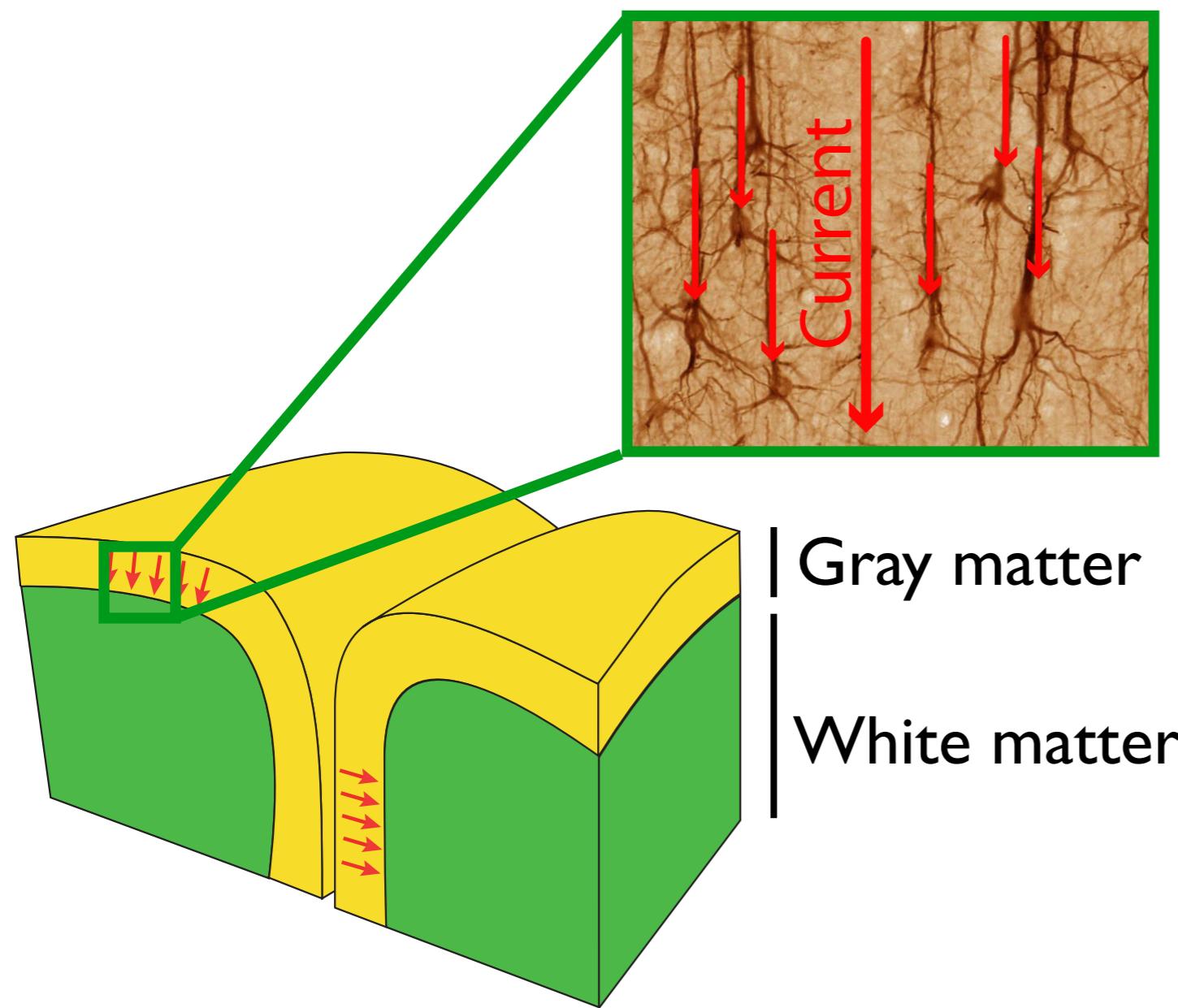
Source: dartmouth.edu

Background on electromagnetism



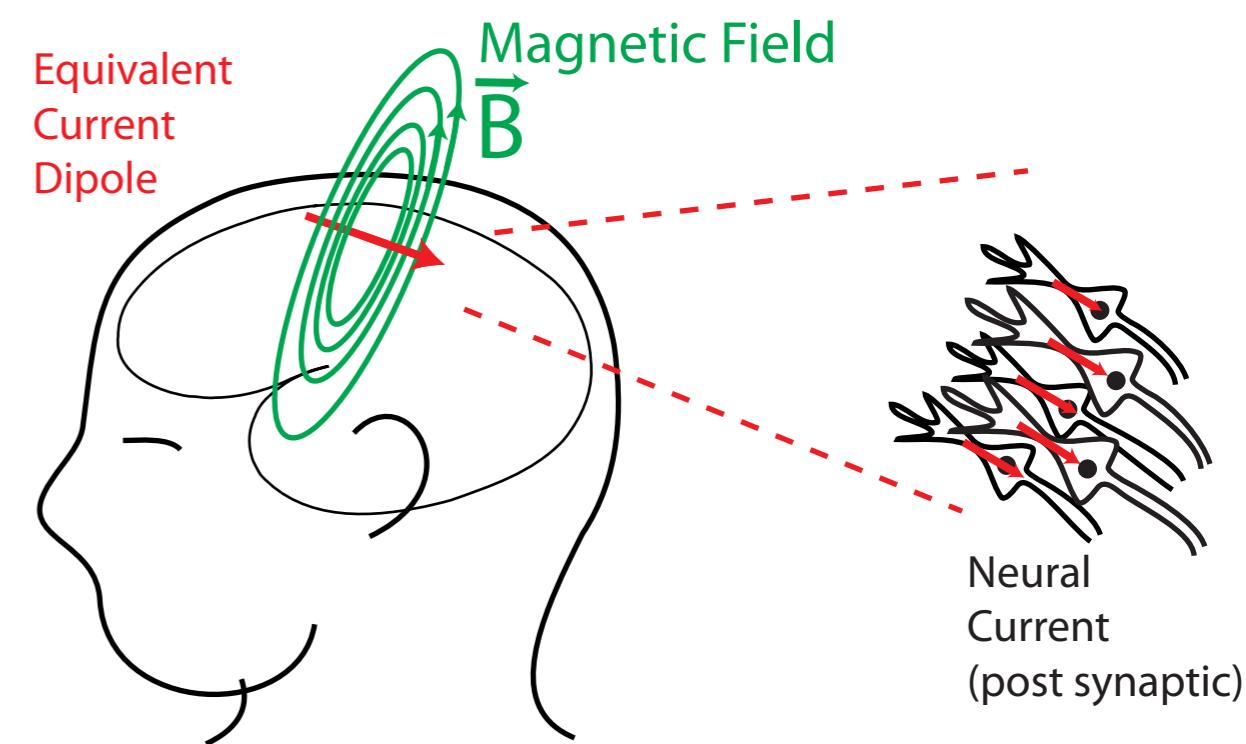
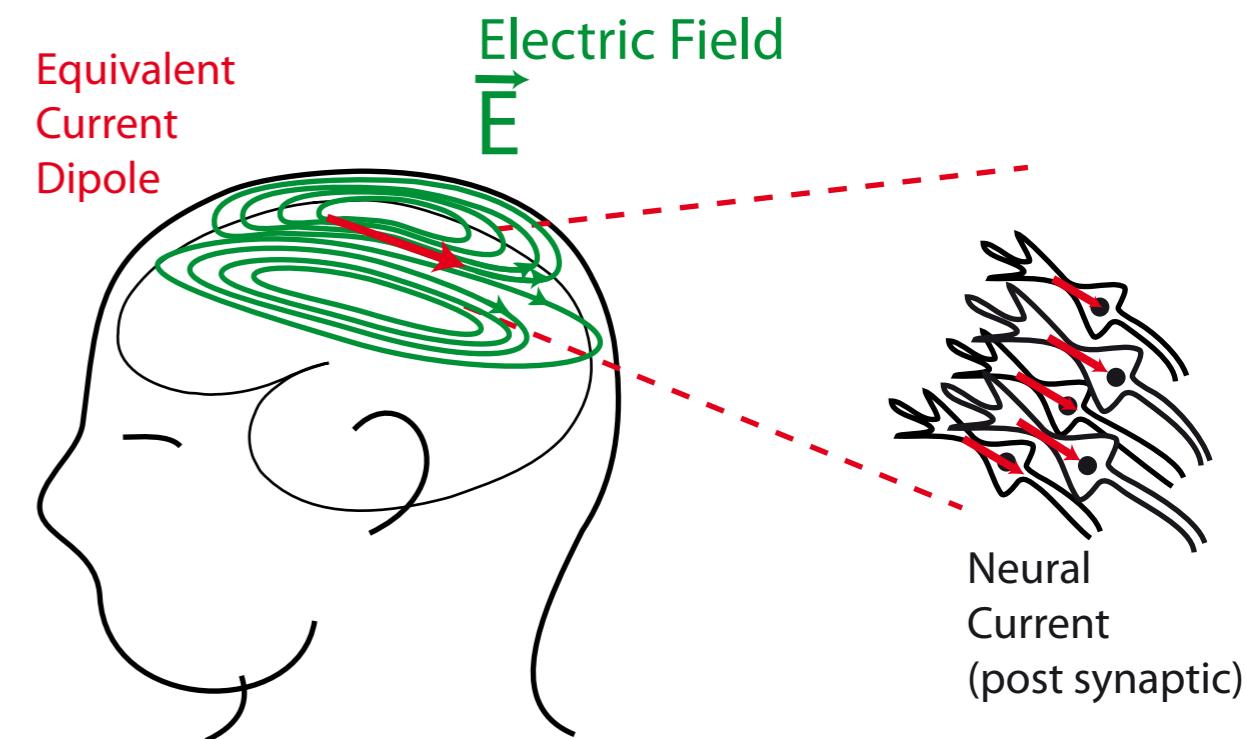
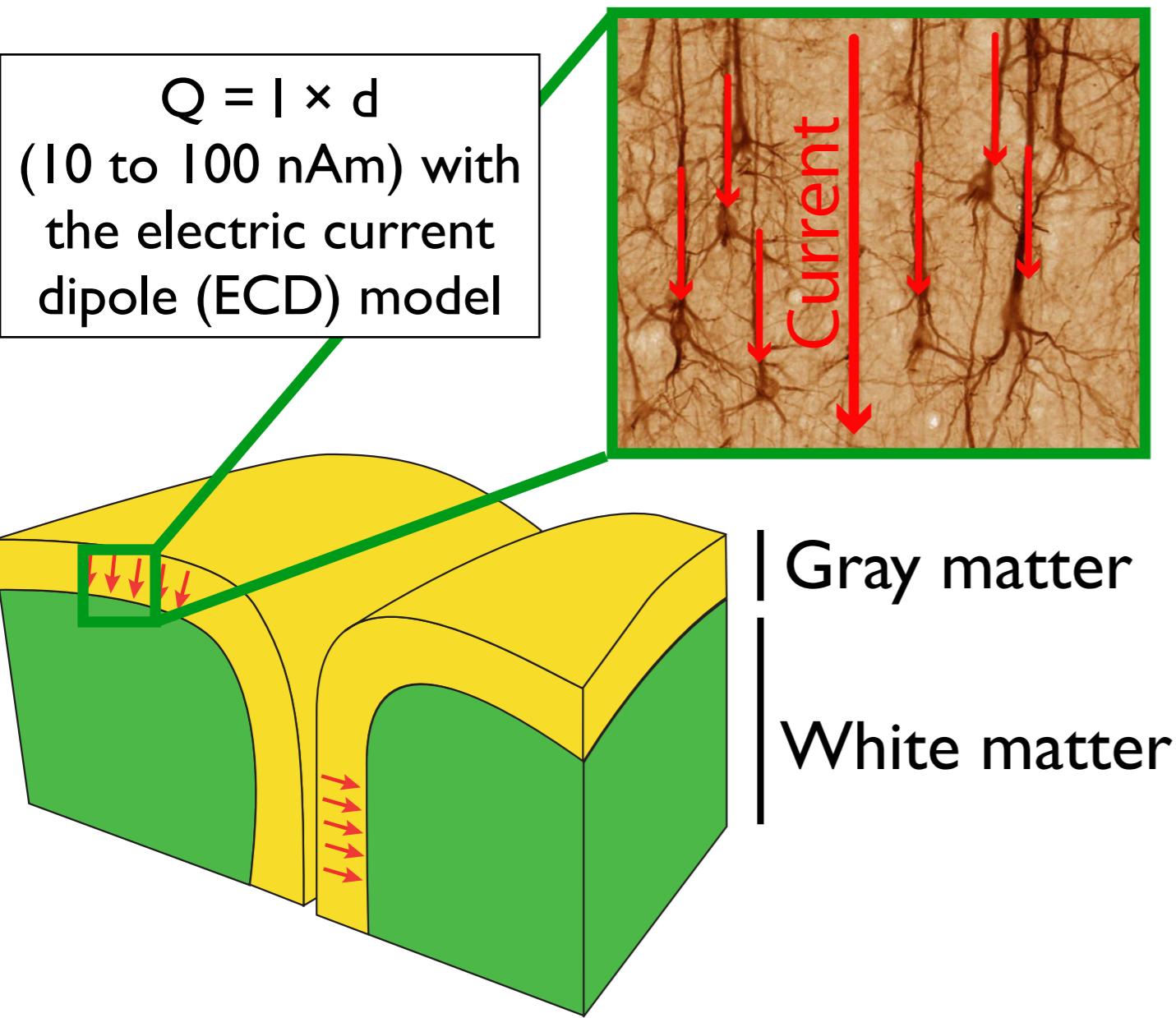
Neurons as current generators

Large cortical pyramidal cells organized in macro-assemblies with their **dendrites** **normally oriented to the local cortical surface**

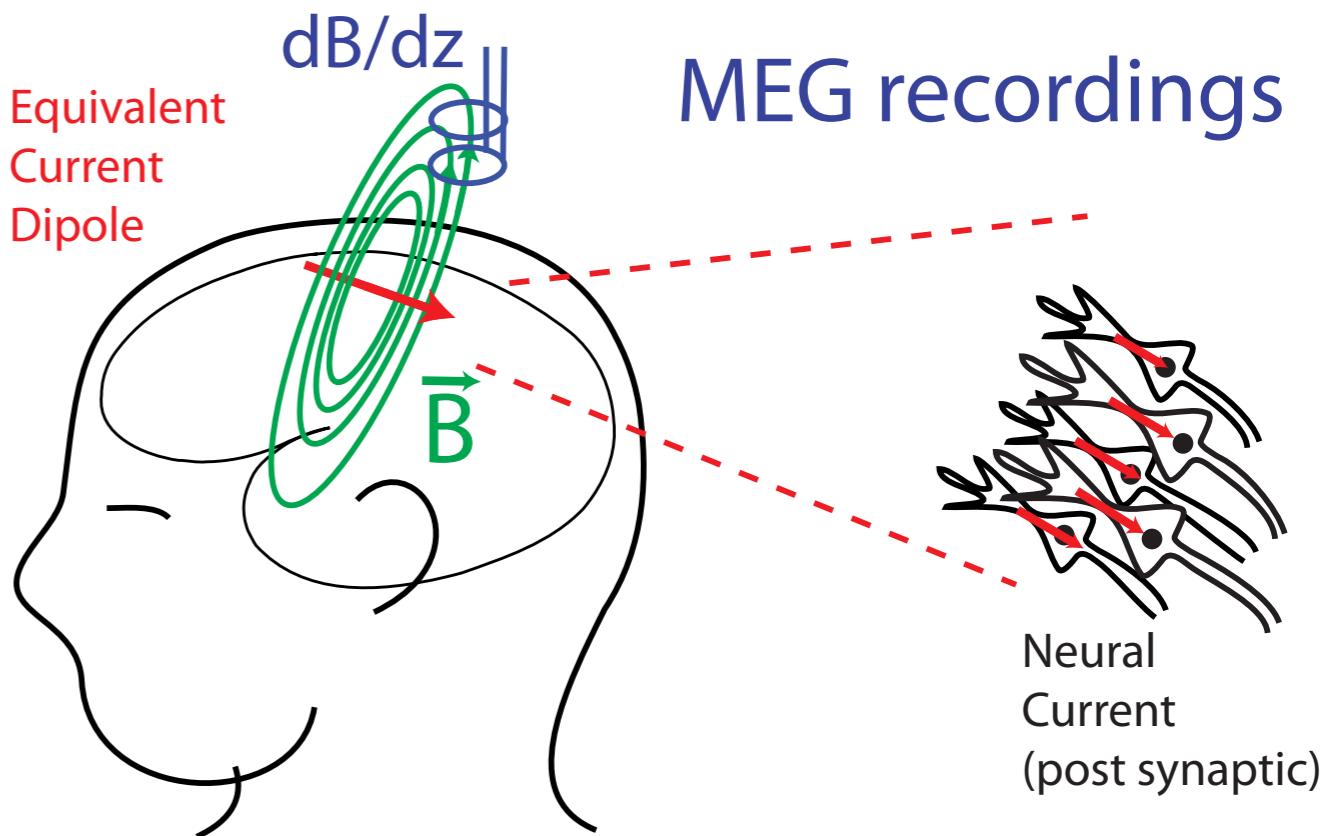
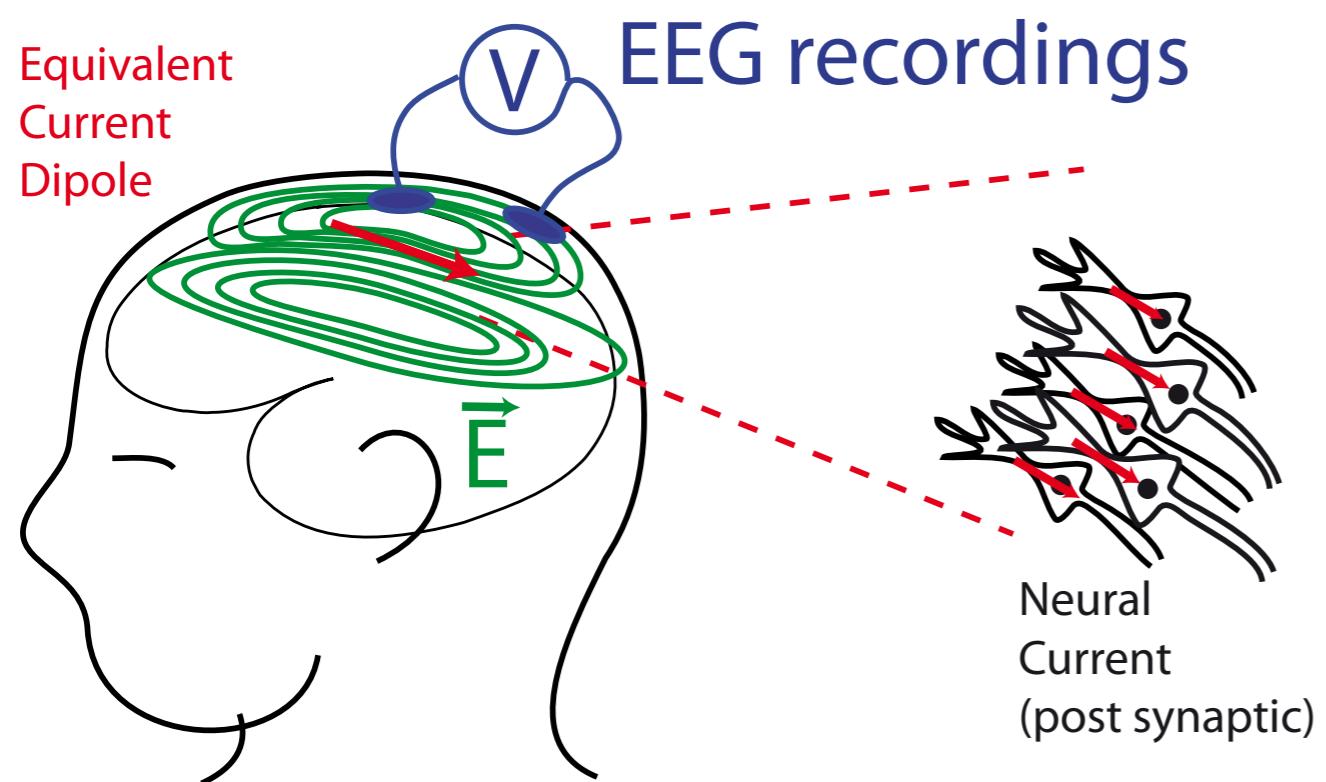


Neurons as current generators

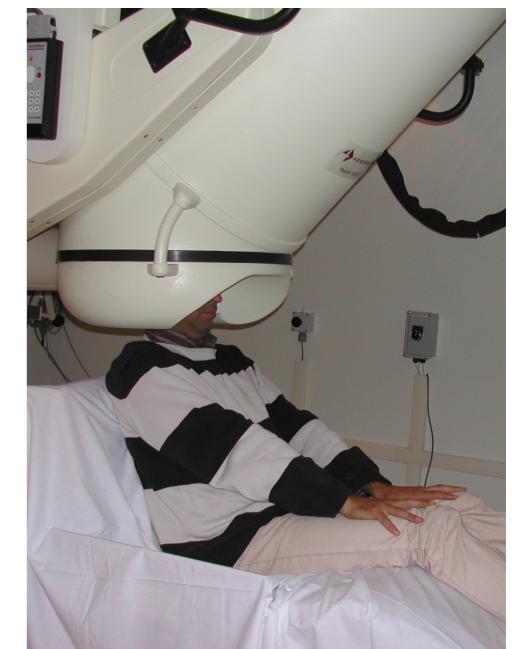
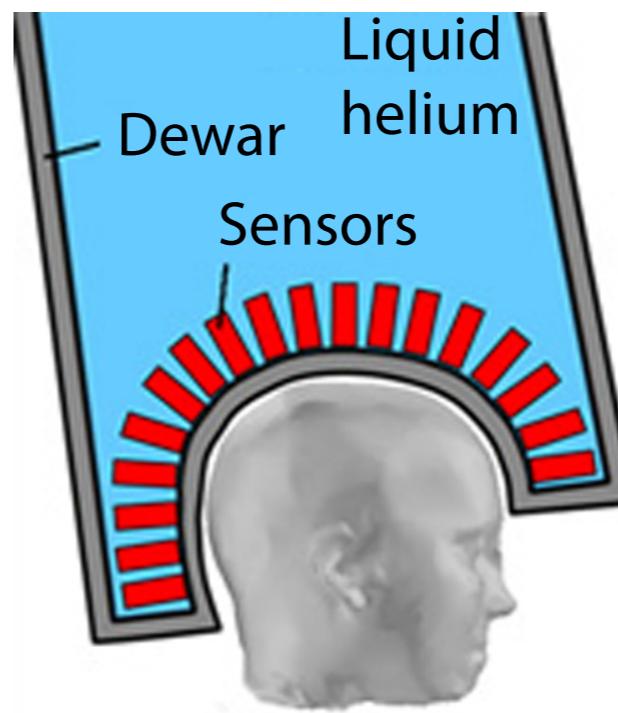
Large cortical pyramidal cells organized in macro-assemblies with their **dendrites** **normally oriented to the local cortical surface**



EEG & MEG systems

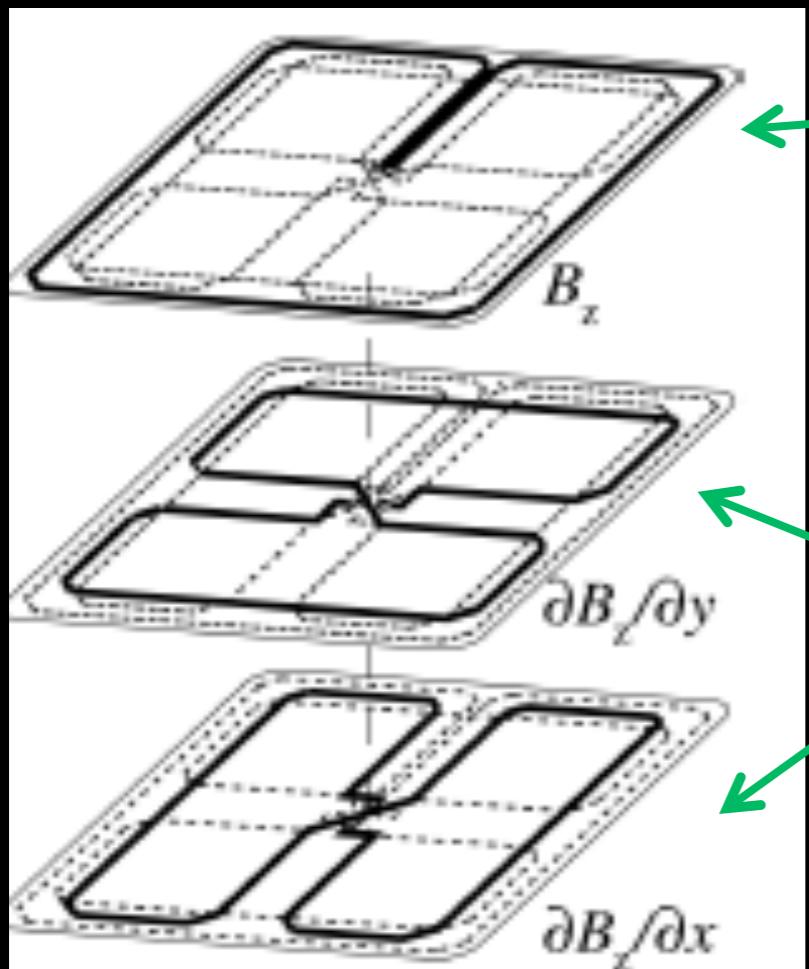


First EEG
recordings
in 1929
by H. Berger



Hôpital La Timone
Marseille, France

MEG sensors



Magnetometer

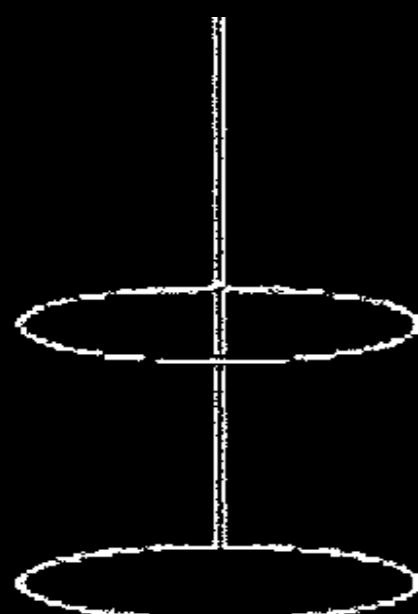
- General magnetic fields
- Very sensitive overall, **noisy**

Planar Gradiometer

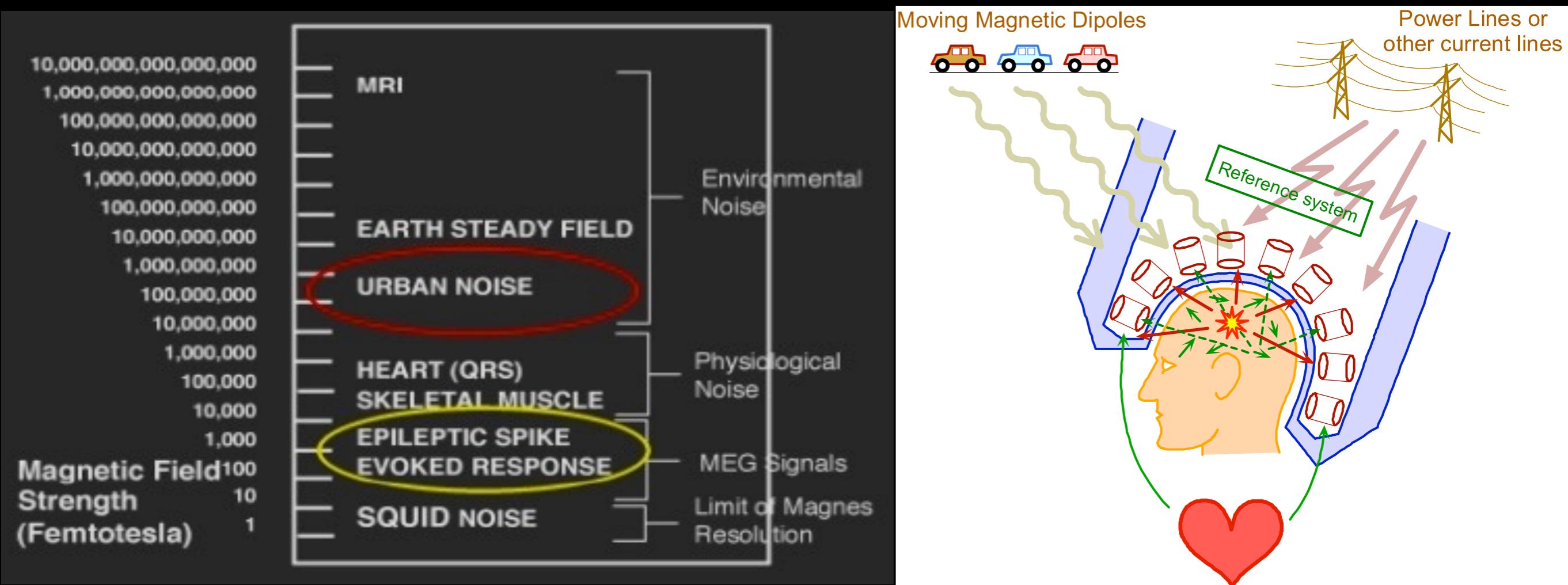
- Focal magnetic fields
- Most sensitive to fields directly underneath

Axial Gradiometer

- Focal magnetic fields
- Most sensitive to fields directly underneath it



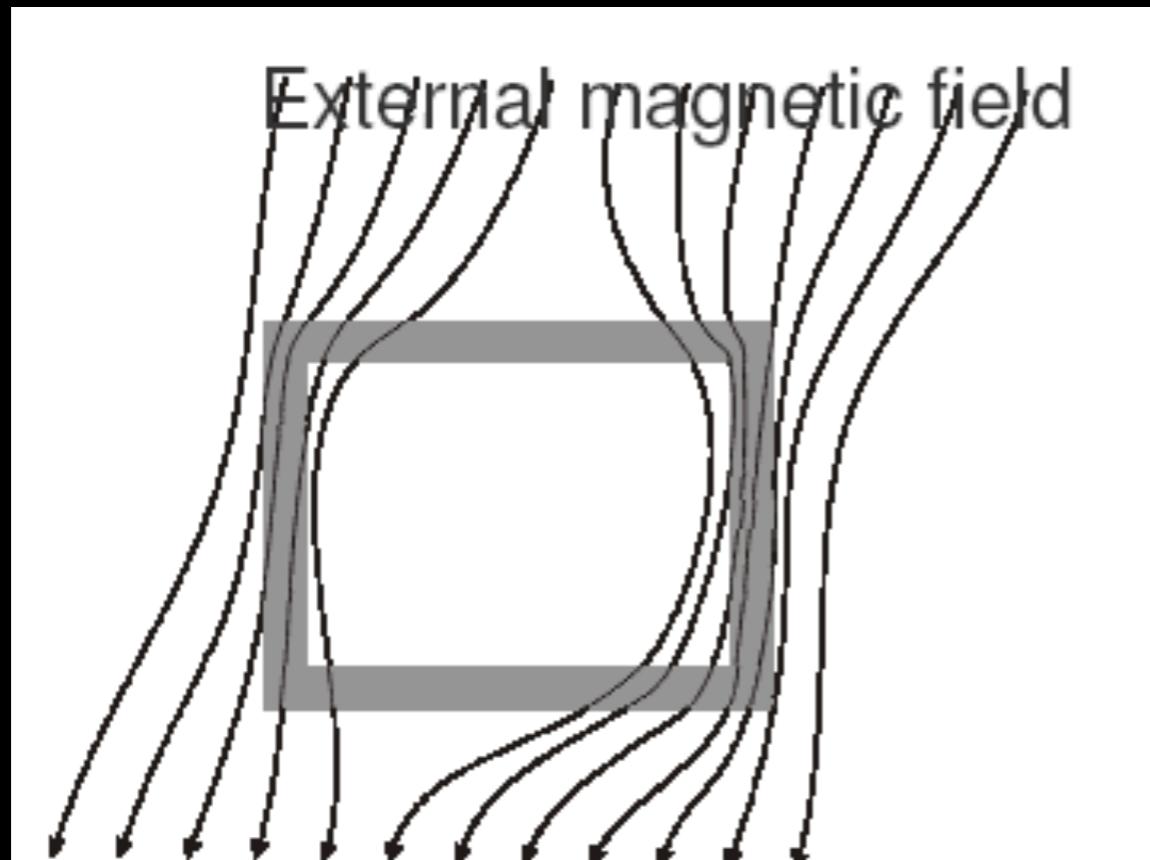
Magnetic shielding

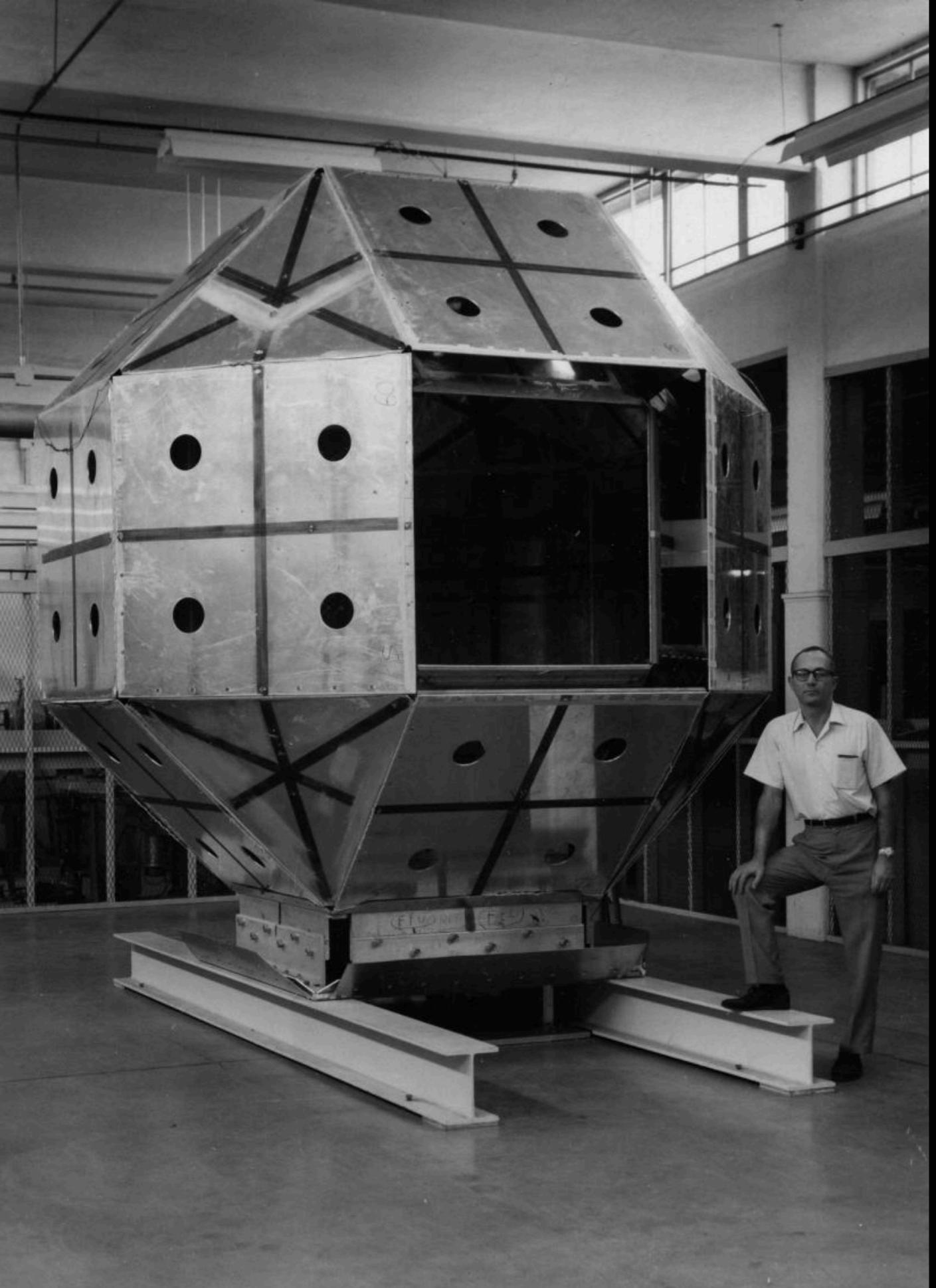


Hence the importance of shielding...

Magnetic shielding

Magnetically Shielded Room (MSR)





In late 1969, David Cohen and James Zimmerman ushered in a new era of biomagnetism when they measured the magnetic field from a human heart using a superconducting quantum interference device, or SQUID. The first use of a SQUID with a human subject, the experiment threw open the doors to medical applications of the technology, the possibilities of which researchers are still exploring today.

Cohen 1971

First unaveraged MEG recording

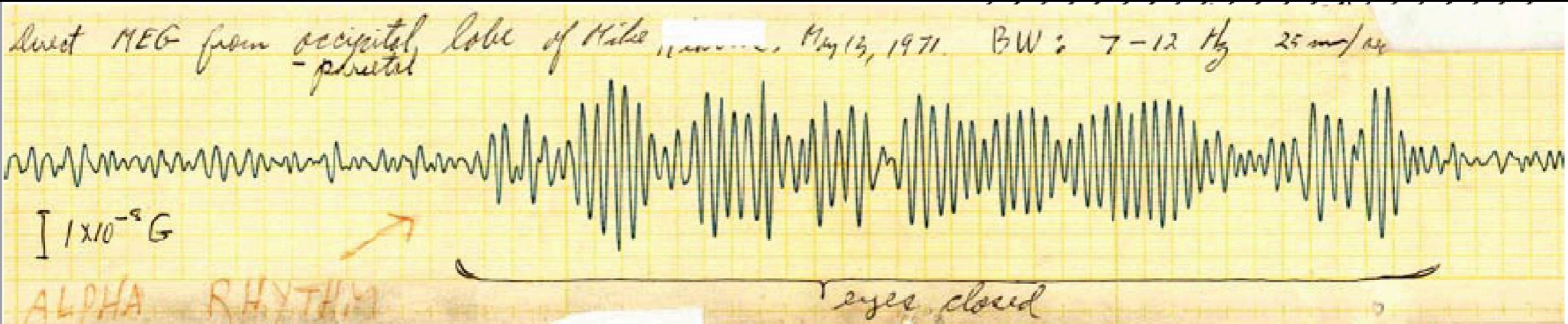
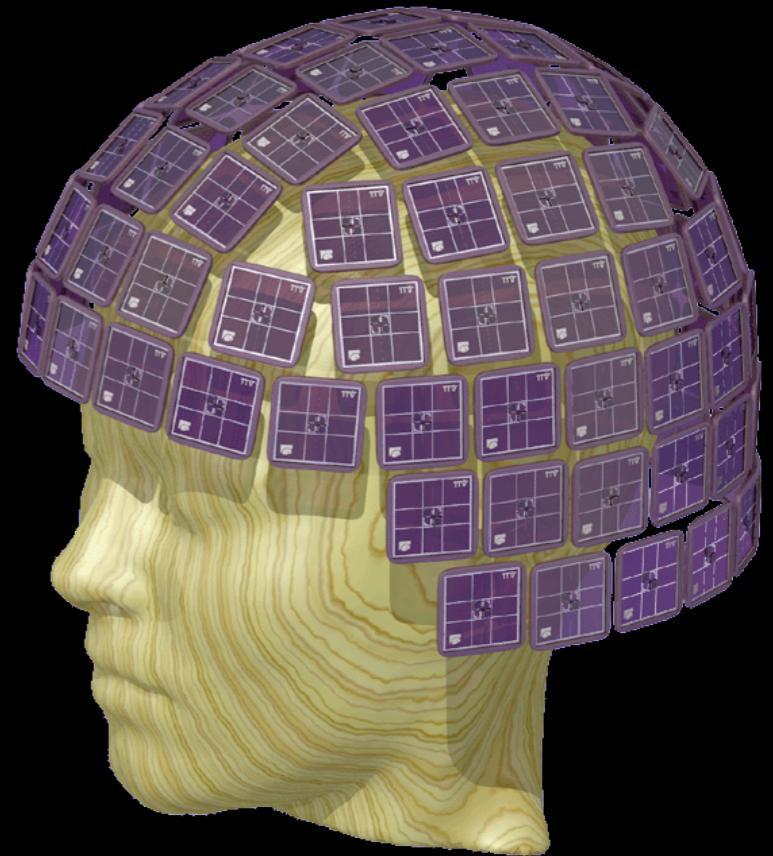


Figure 3. First MEG measured with a SQUID, in the MIT shielded room (May, 1971), using an early commercial SQUID. The subjects eyes were open at the beginning of the trace, then closed, resulting in the large alpha rhythm, then open again. The MEG was now as clear as the conventional EEG.

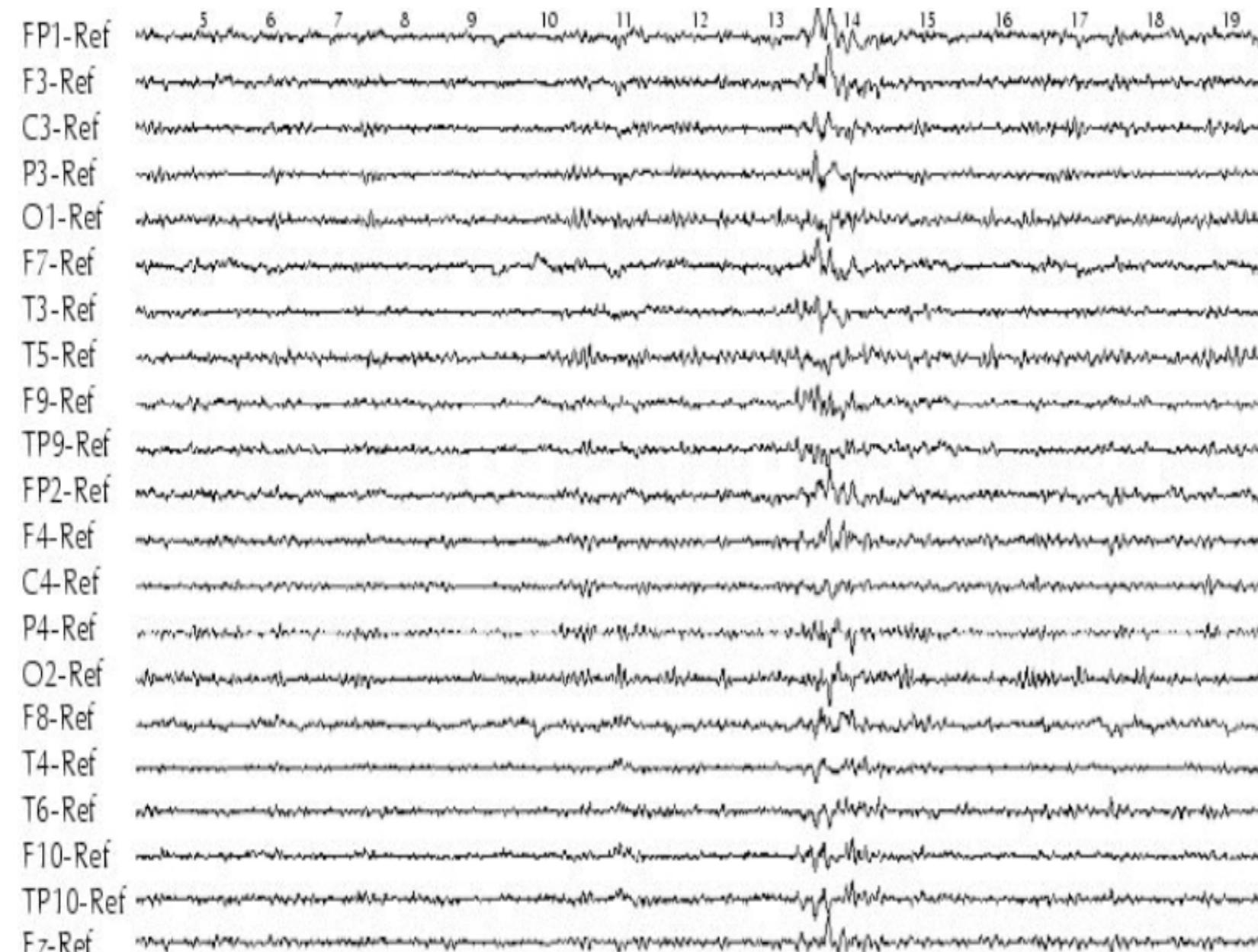
A machine (Neuromag vectorview)



No Magnet
Quiet
Machine makes no noise
Participant can sit or lay down
Can record 128 EEG simultaneously



M/EEG Measurements



Sample EEG measurements

EEG :

- ≈ 100 sensors

MEG :

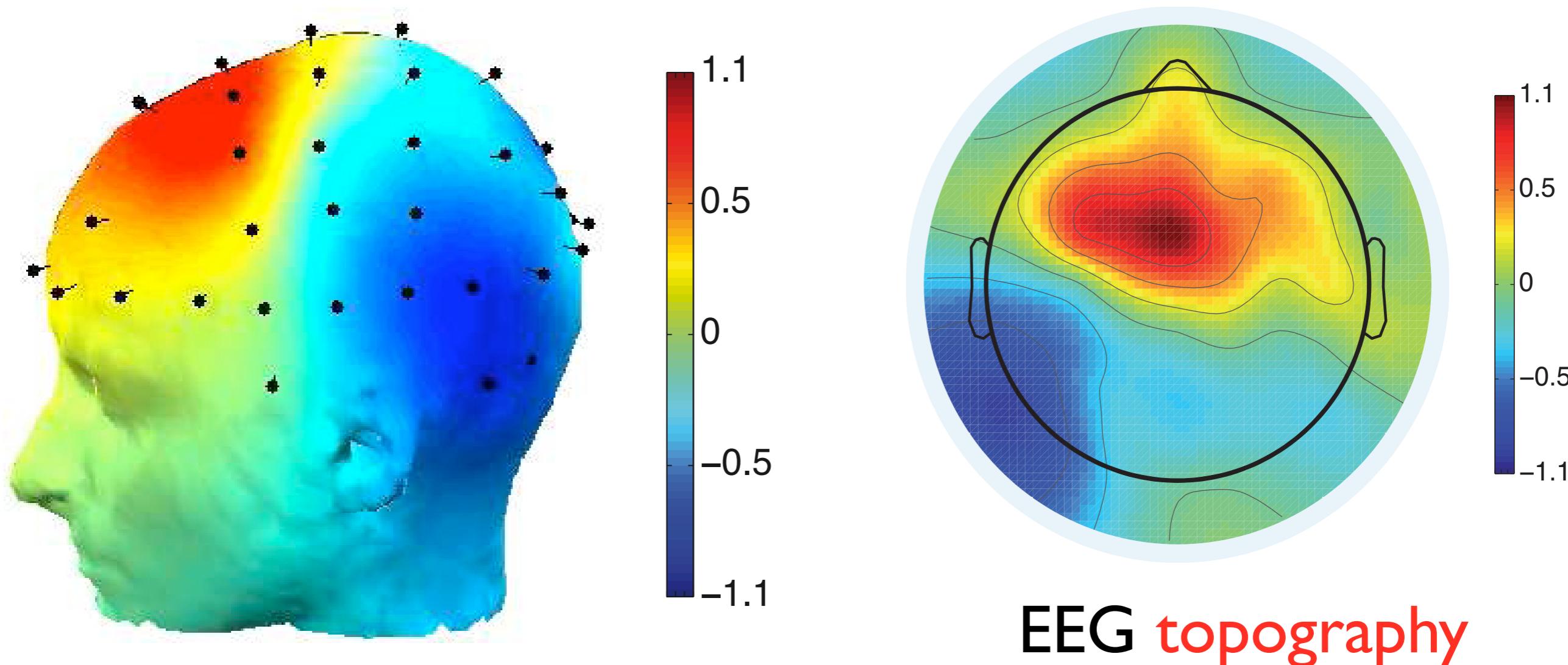
- ≈ 150 to 300 sensors

Sampling between 250
and 1000 Hz

High temporal
resolution but what
about spatial
resolution?

M/EEG Measurements

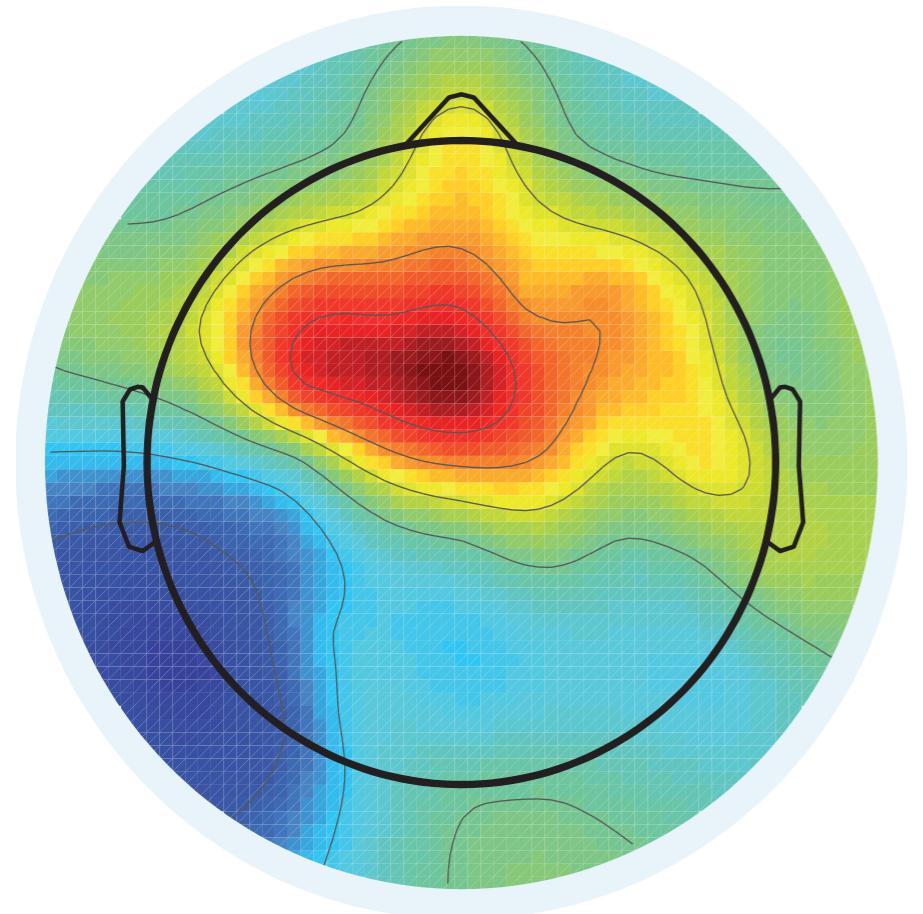
At **each time instant** EEG sensors measure a potential field



Remark: Such a smooth potential field confirms the presence of
current generators within the head

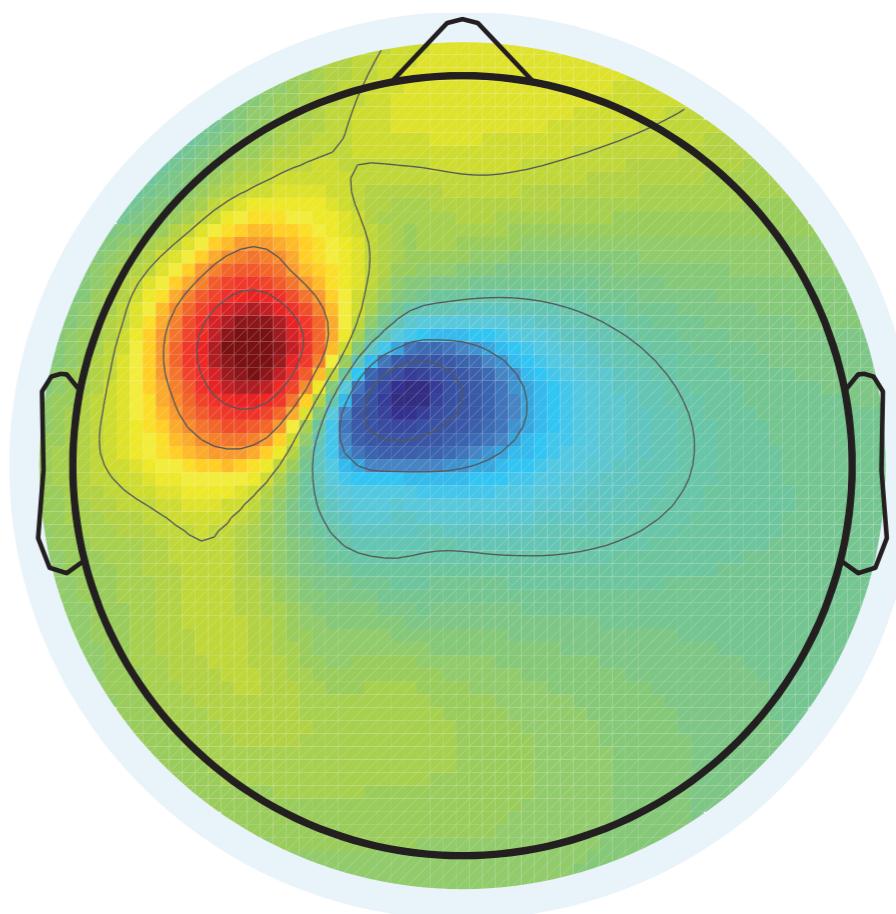
M/EEG Measurements

EEG topography



vs.

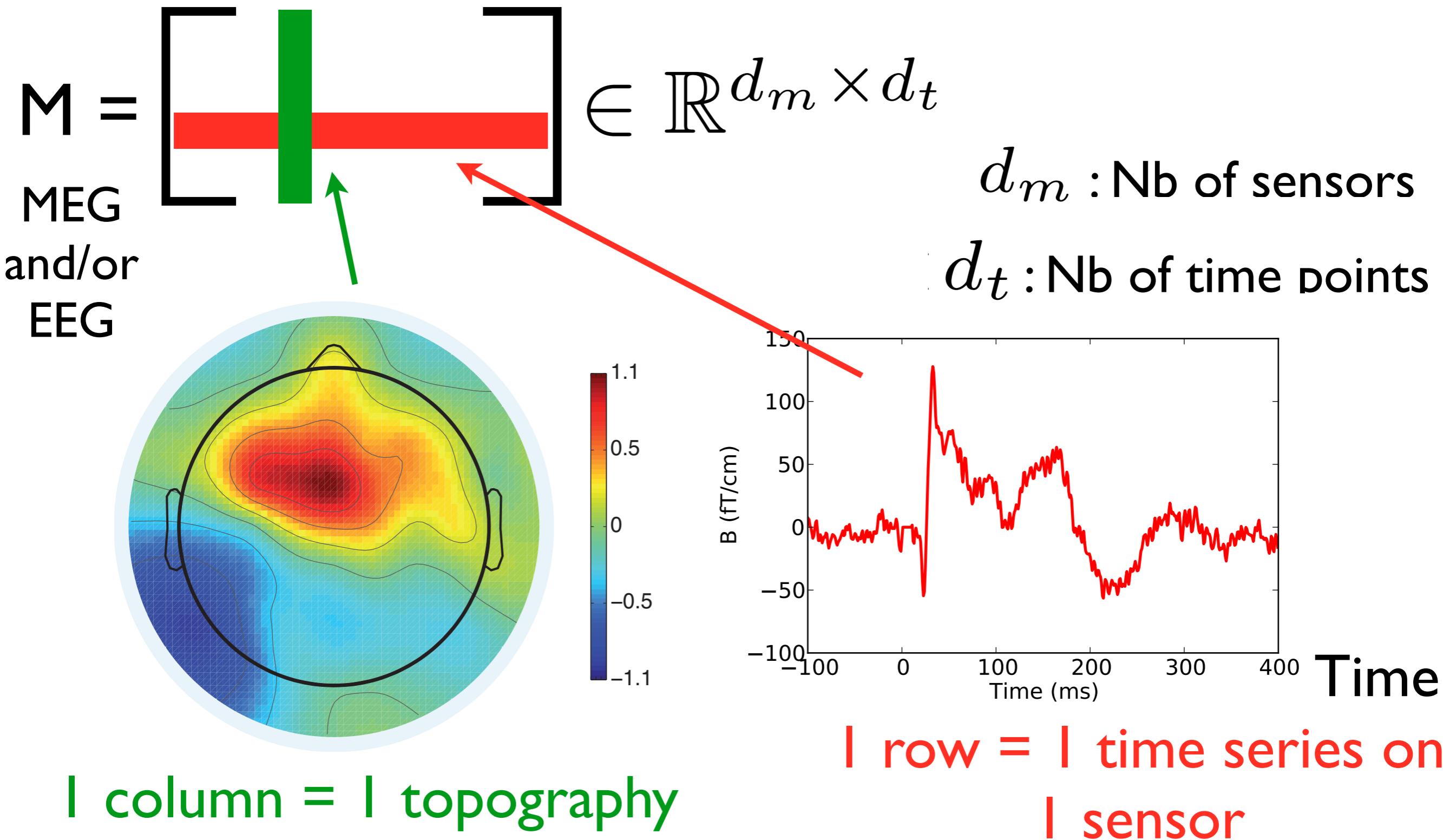
MEG topography



*CTF system with 151
axial gradiometers*

MEG topography exhibits also a dipolar field but MEG has a **better spatial resolution**

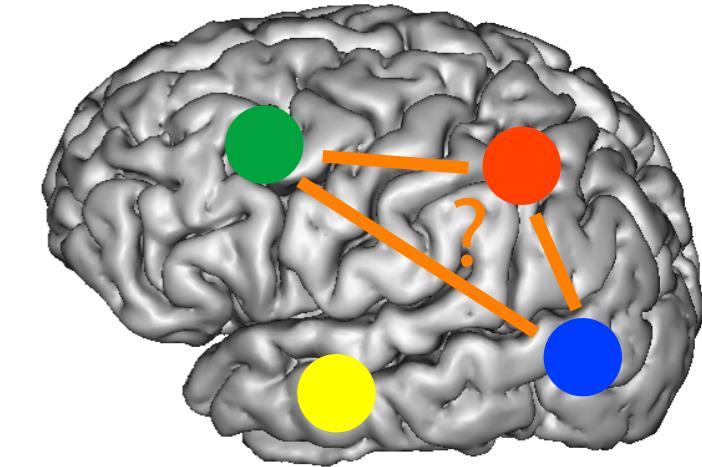
M/EEG Measurements: Notation



What can you do with M/EEG?

I. Cognitive studies

- **Which areas** are activated during a given cognitive task? **When** are they active? **What is common** in a population of subjects?



2. Therapy (Epilepsy)

- Where is the location of the **origin of epileptic seizures?**
- Will my **patient be able to talk** if I remove this area of the cortex?



Source: life.com

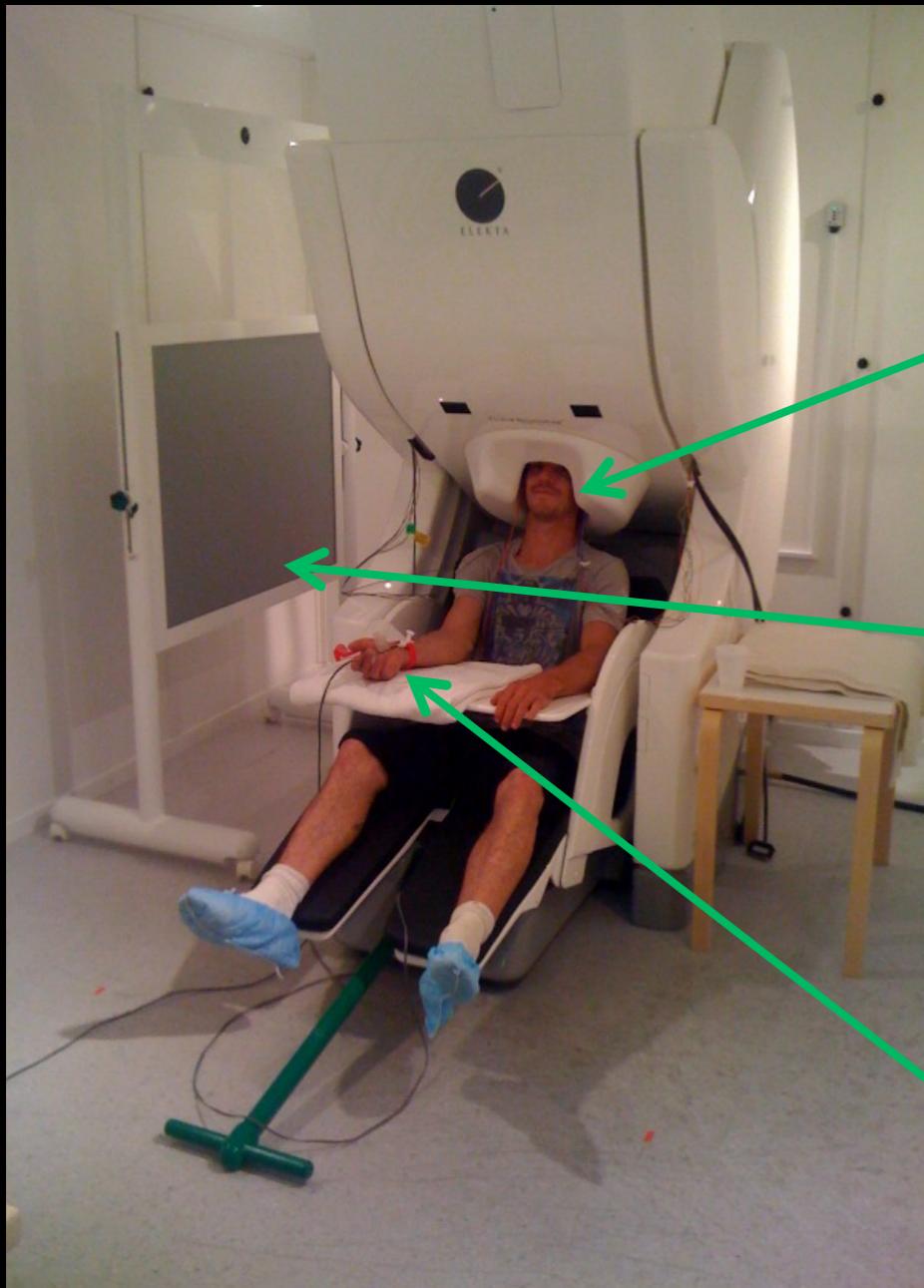
3. Brain computer interfaces (BCI)

- How to extract in **real time** the signal of interest from EEG measurements in order to **control a computer?**



Source: nih.gov

Data acquisition examples



Earphones

Presentation Screen
(moved to front!)

Electrical Stimulator

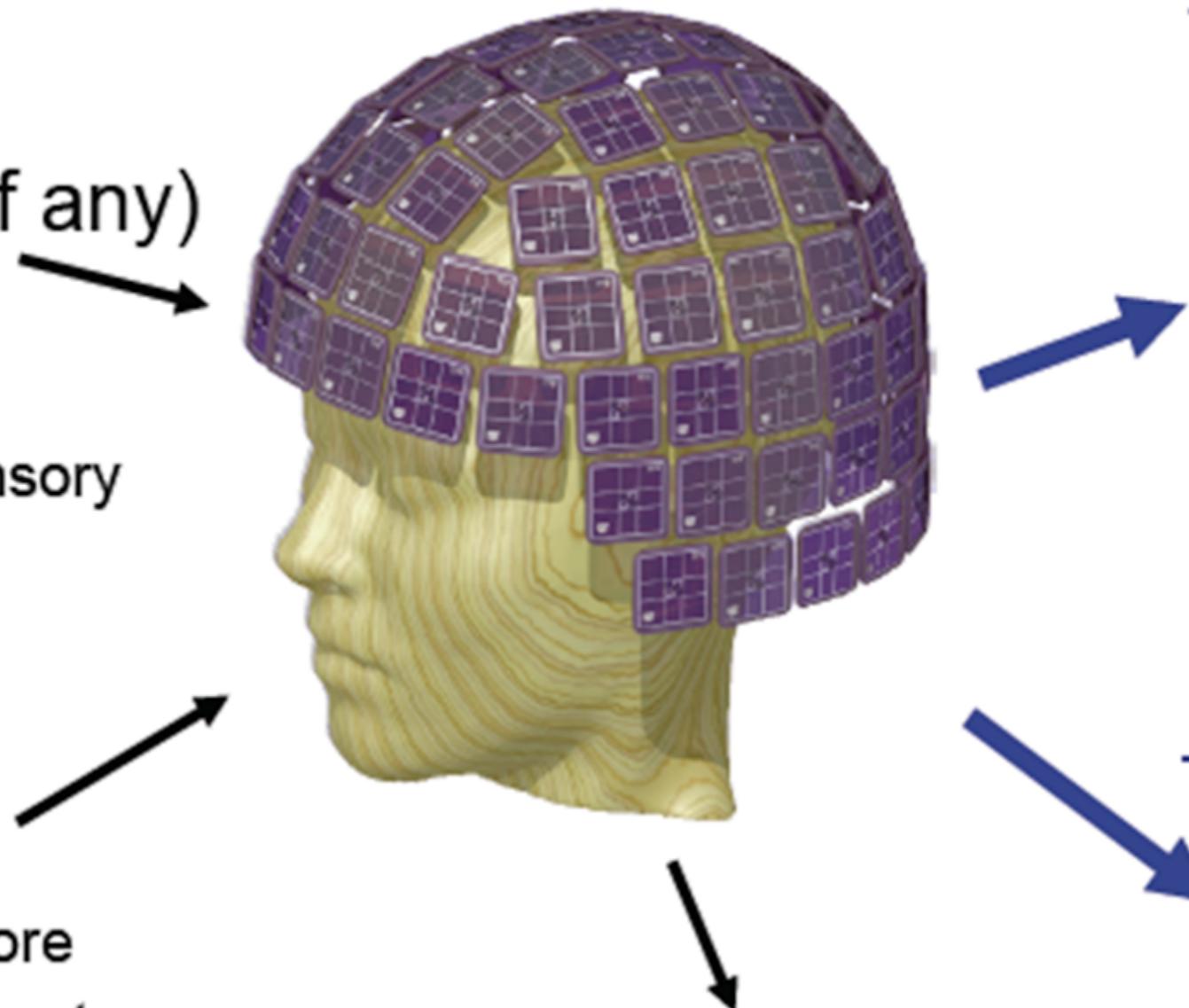
Also:
Button Pads
Button Gloves
Manual Tapper

Stimulus delivered
by E-Prime,
PsychToolBox, etc.

Data acquisition examples

Stimuli (if any)

- auditory
- visual
- somatosensory



Task

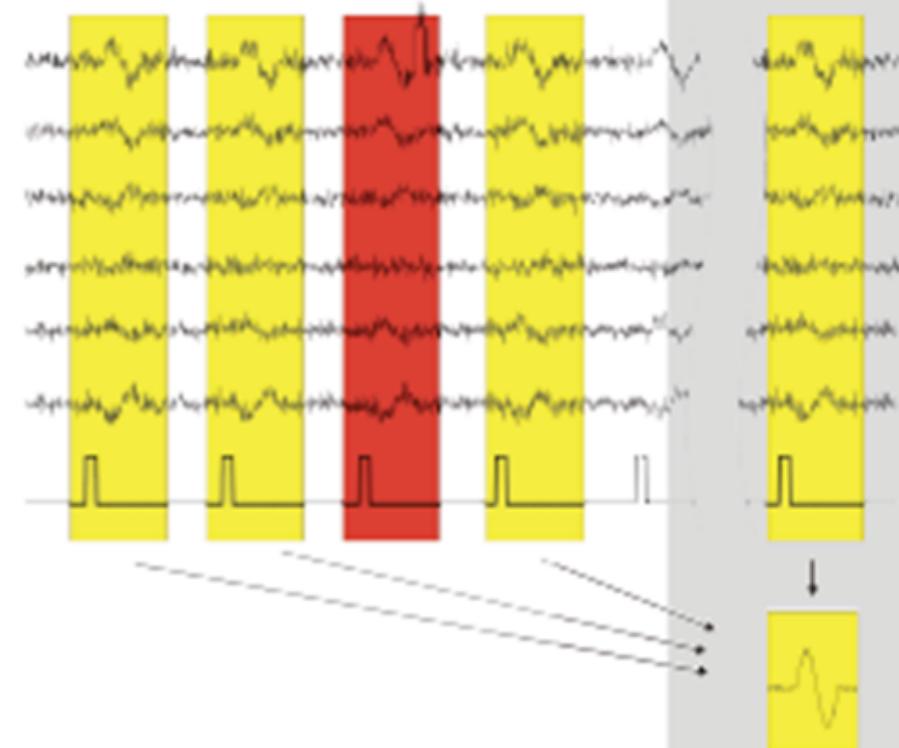
- attend/ignore
- detect + react

Behavioral responses

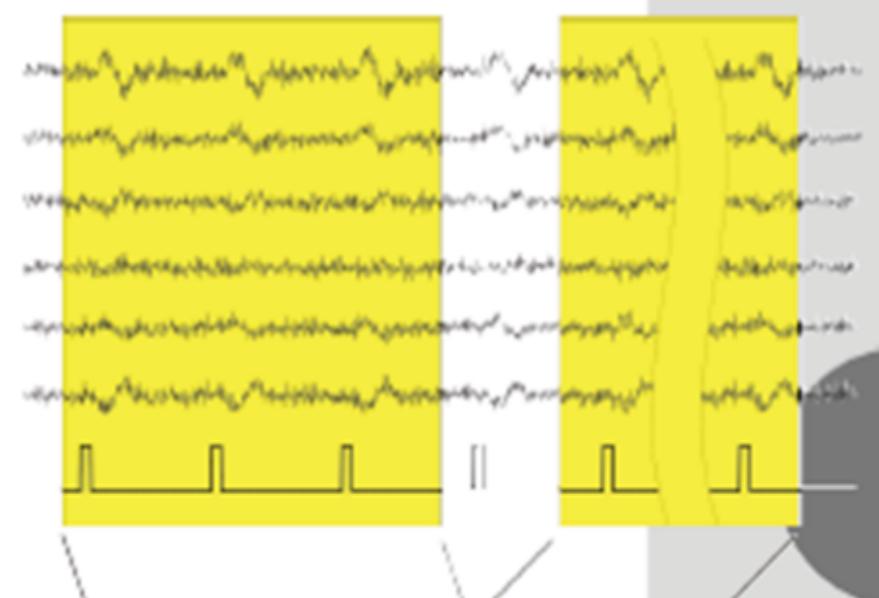
- limb/finger movement
- speech

MEG/EEG

- evoked responses

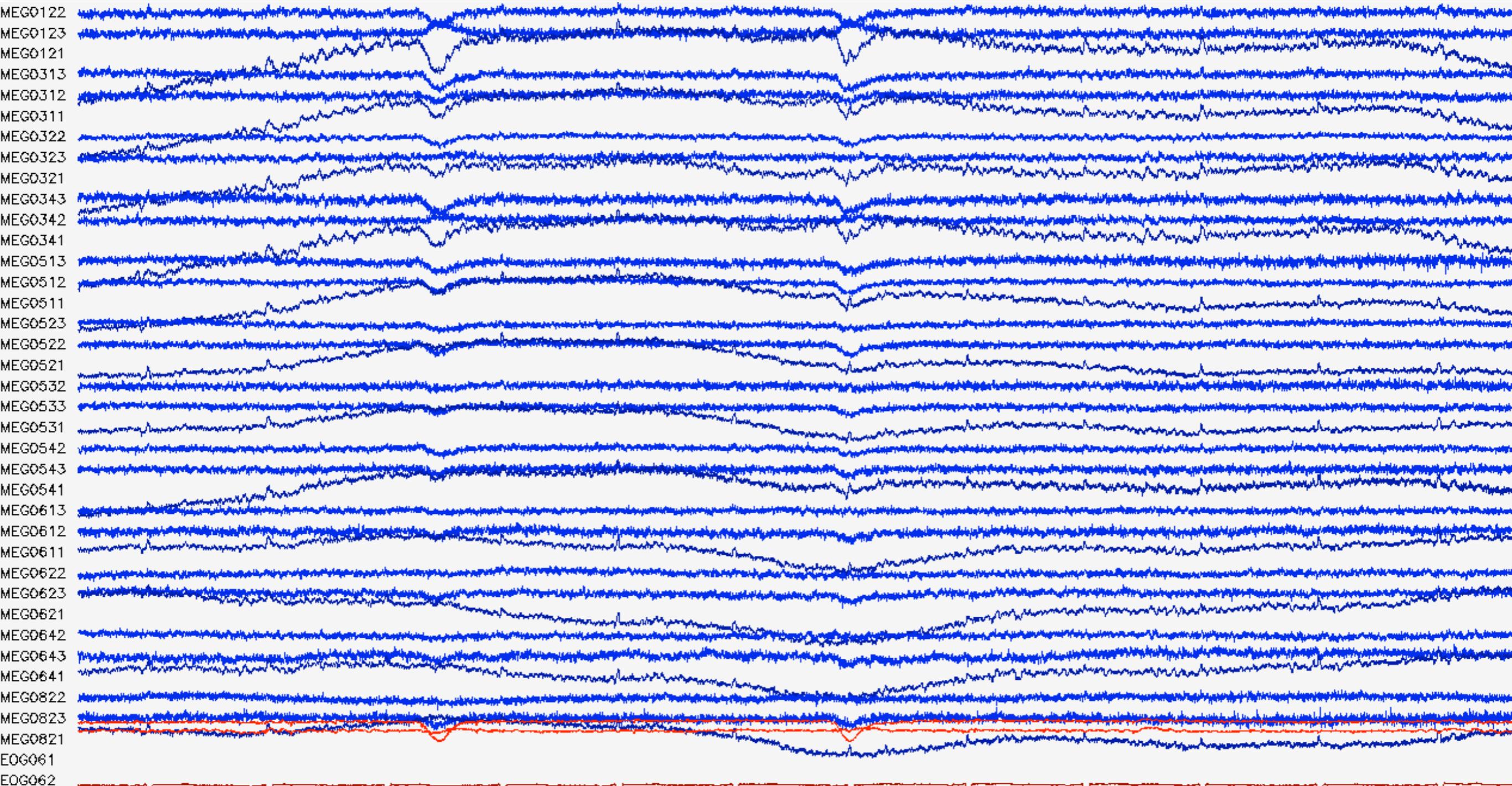


- spontaneous data



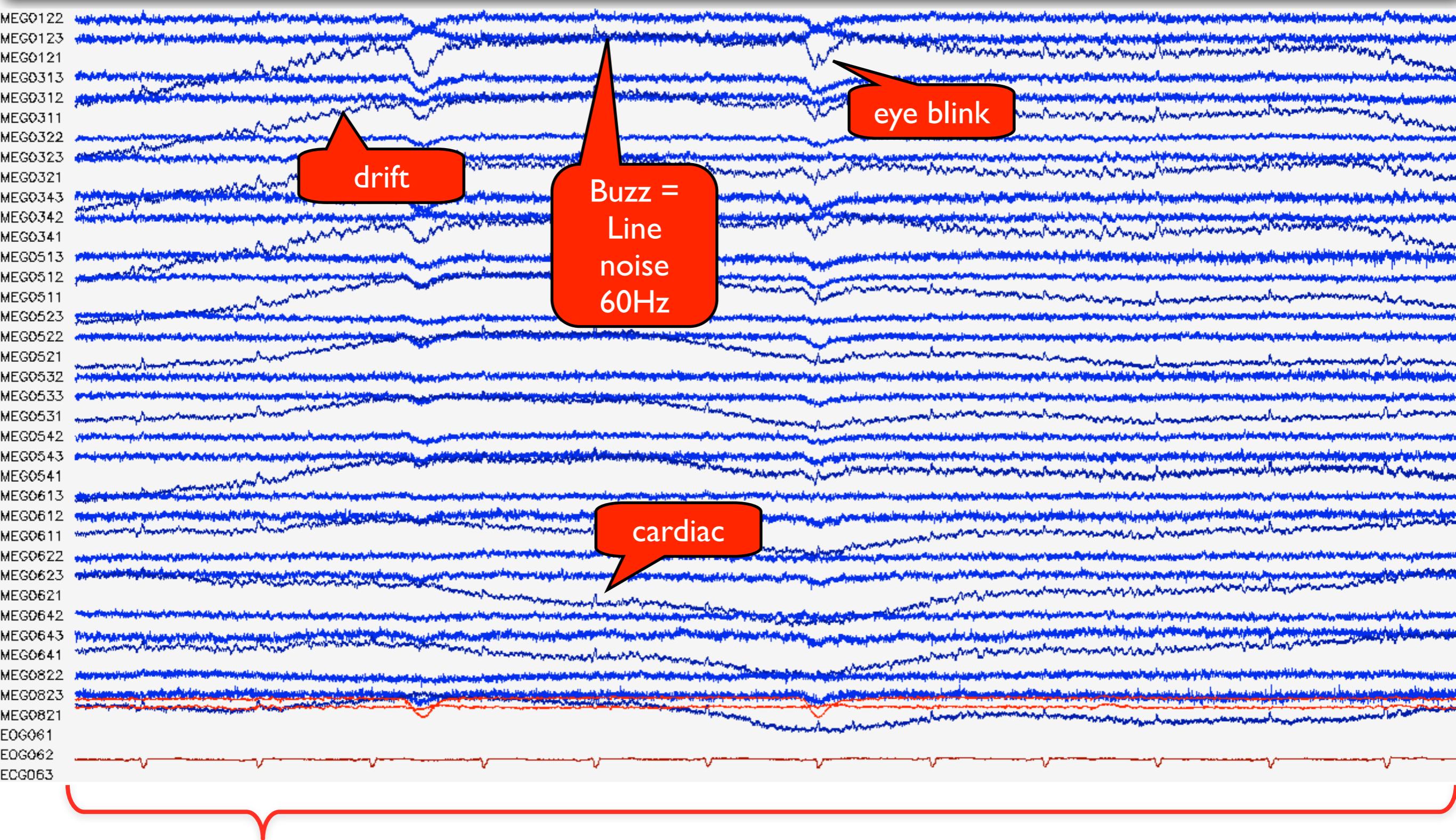
Preprocessing

Raw continuous data

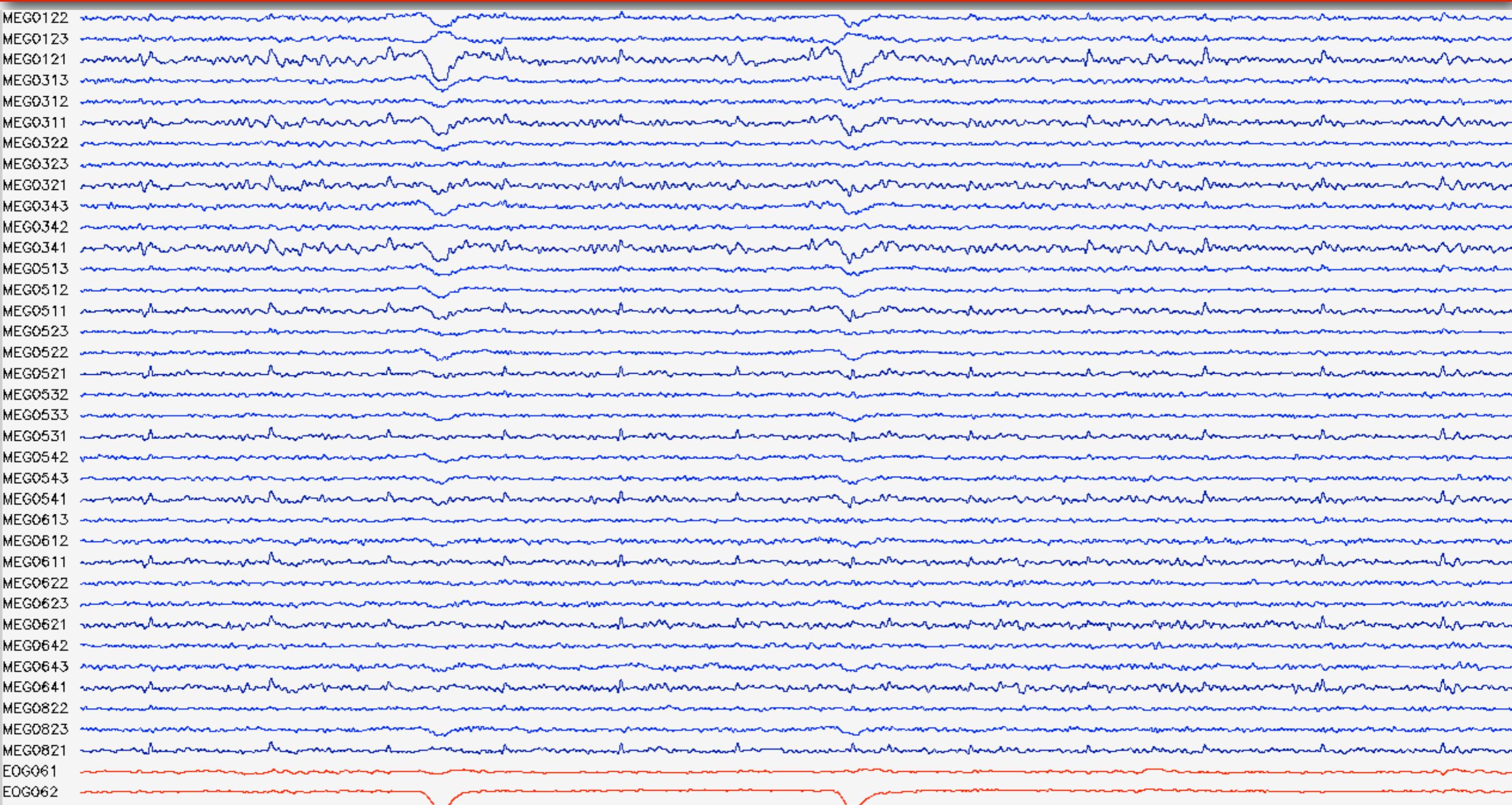


Time frame: 10 seconds

Artifacts



Filtered 1-40Hz



Time frame: 10 seconds

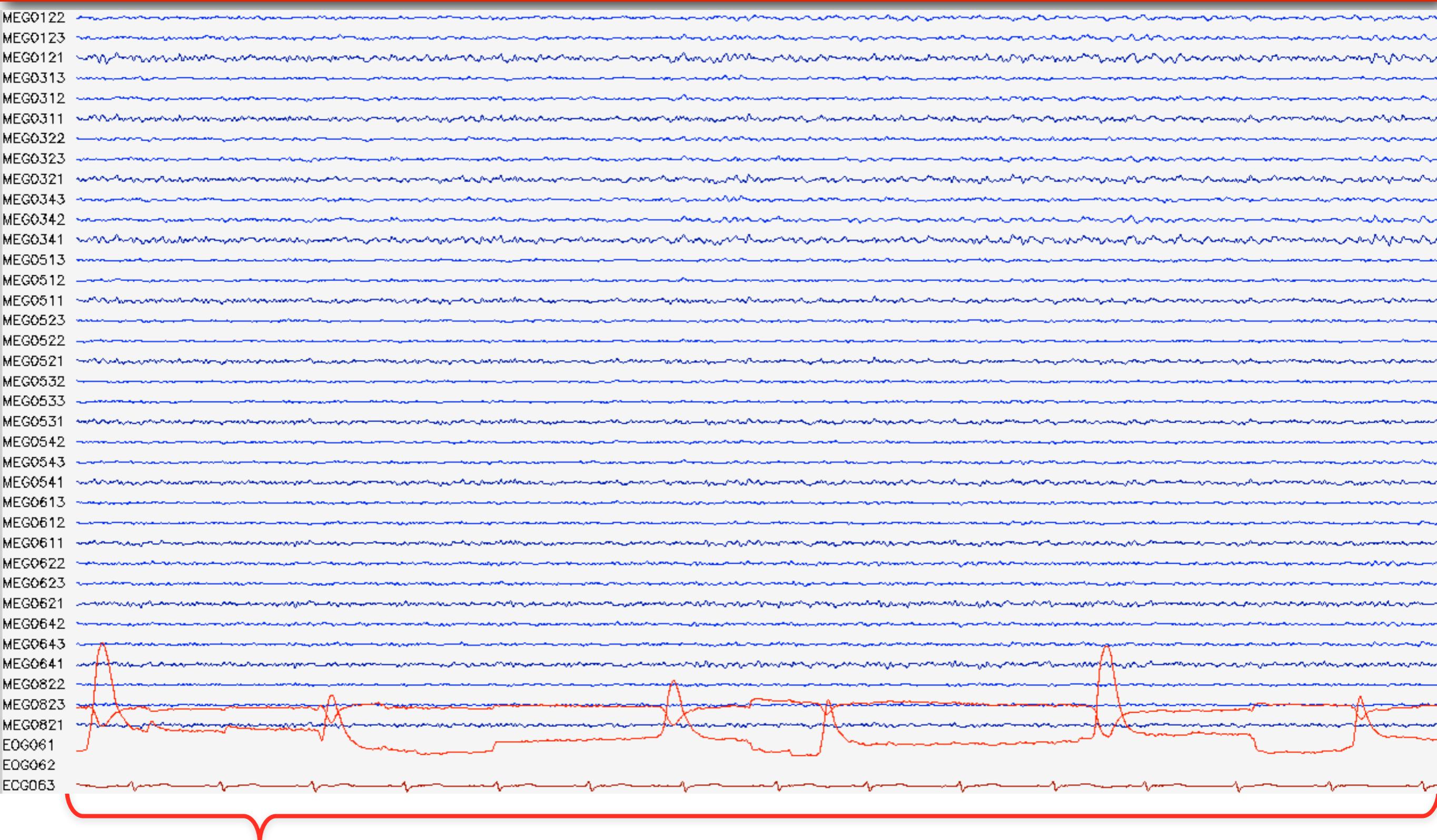
Artifact correction

- Signal Space Projections (SSP)
- Independent component analysis (ICA)
- ...

https://mne.tools/dev/auto_tutorials/preprocessing/plot_45_projectors_background.html

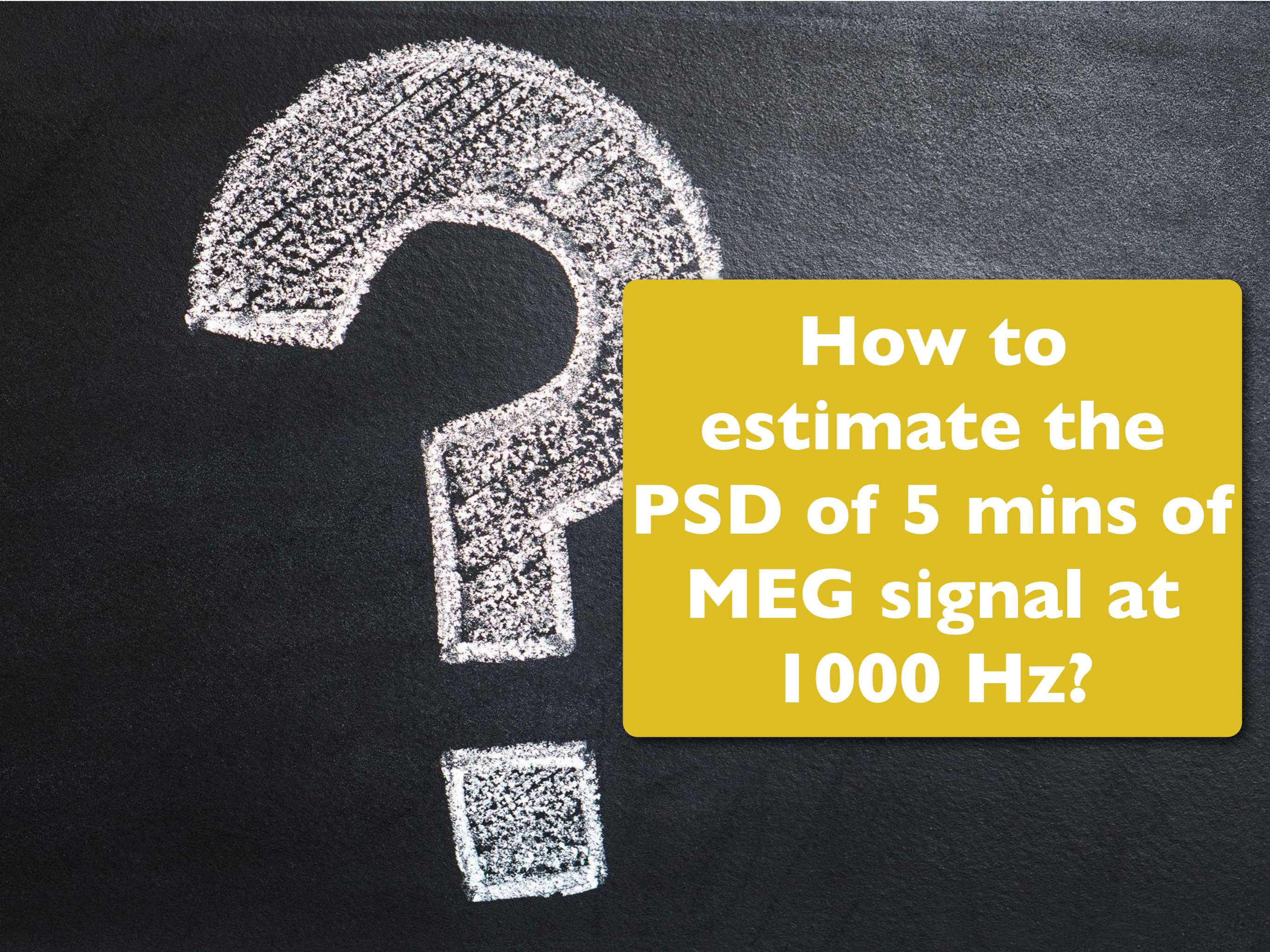
https://mne.tools/dev/auto_tutorials/discussions/plot_background_ica.html

To get clean data...



Time frame: 10 seconds

Power Spectra estimation

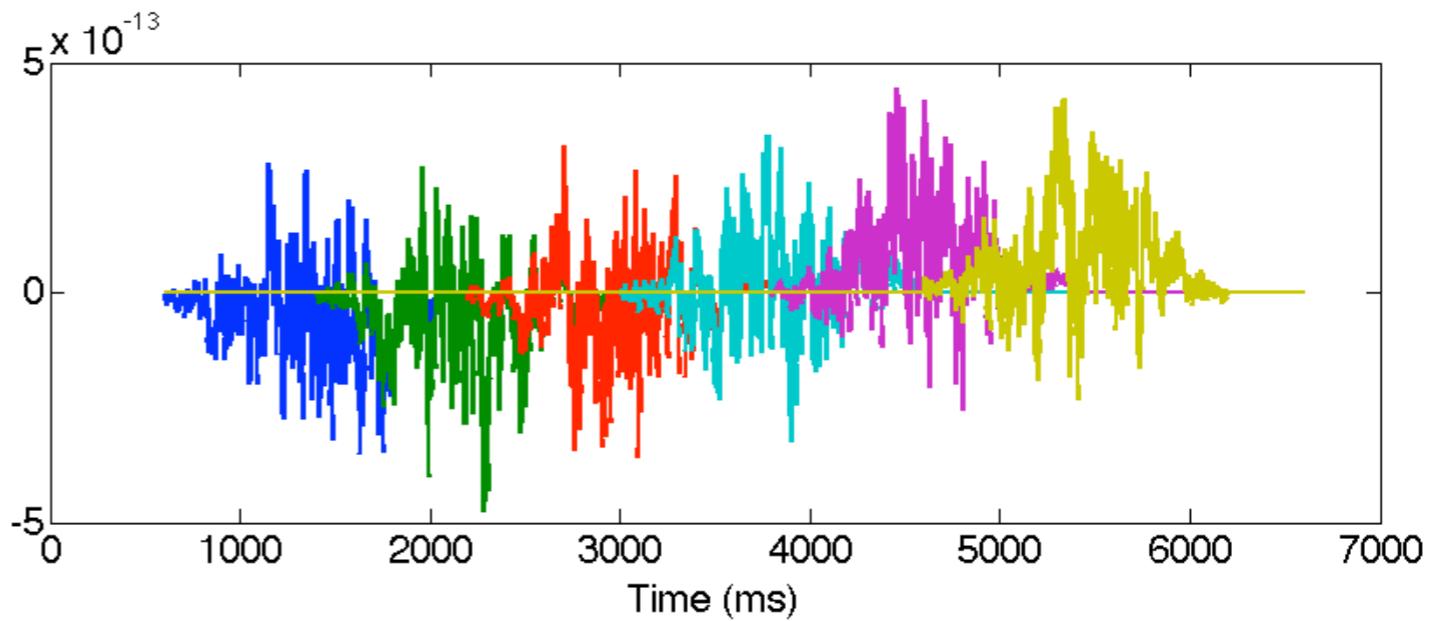


**How to
estimate the
PSD of 5 mins of
MEG signal at
1000 Hz?**

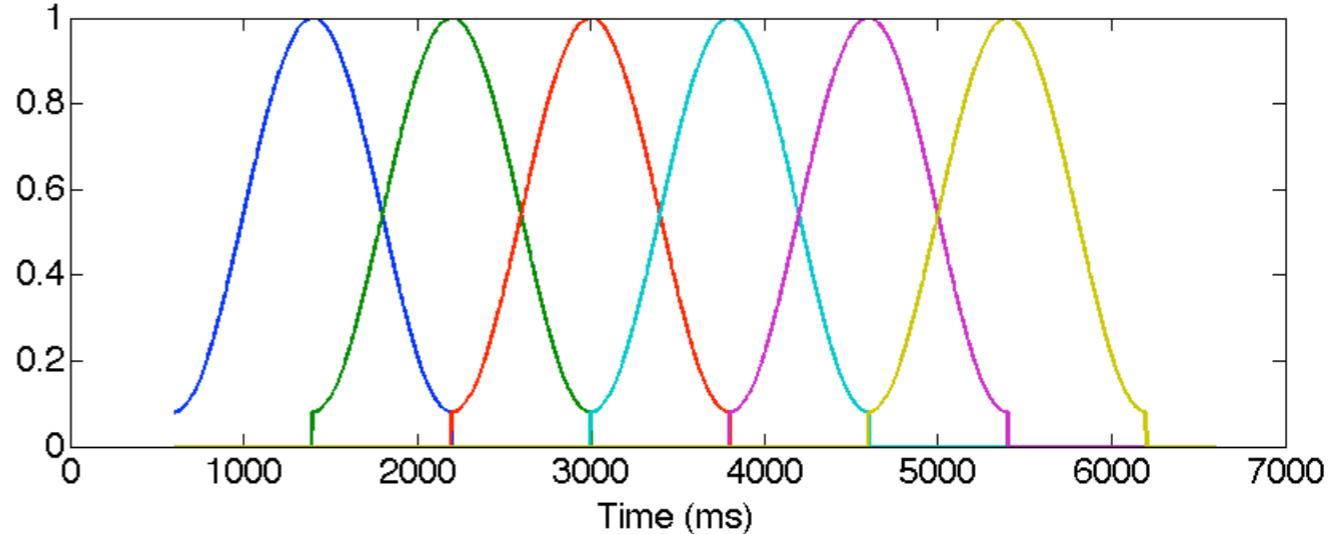
Power Spectrum Density

On raw data (typically > 5 minutes)

Approach: Sliding-
Overlapping windows



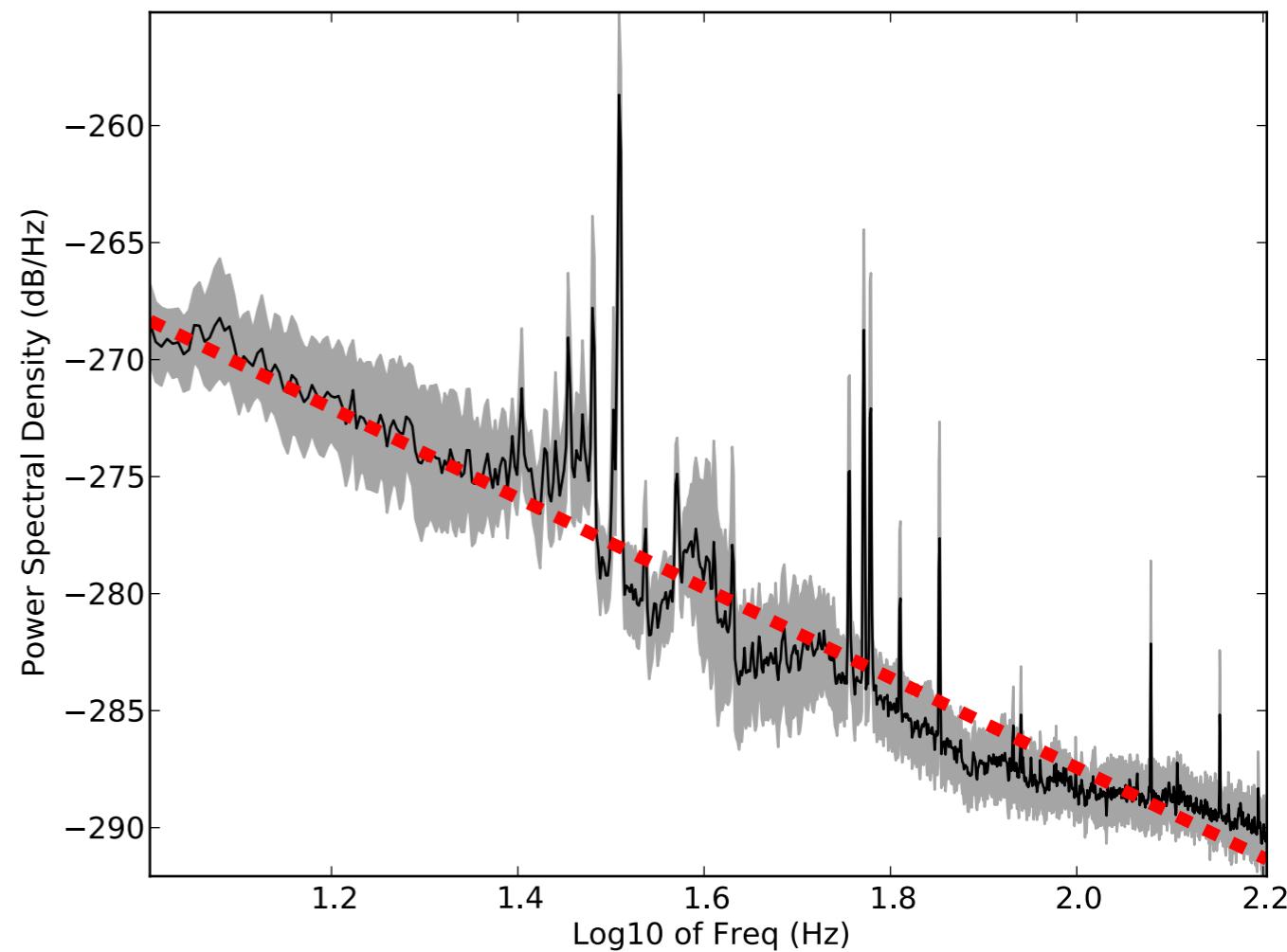
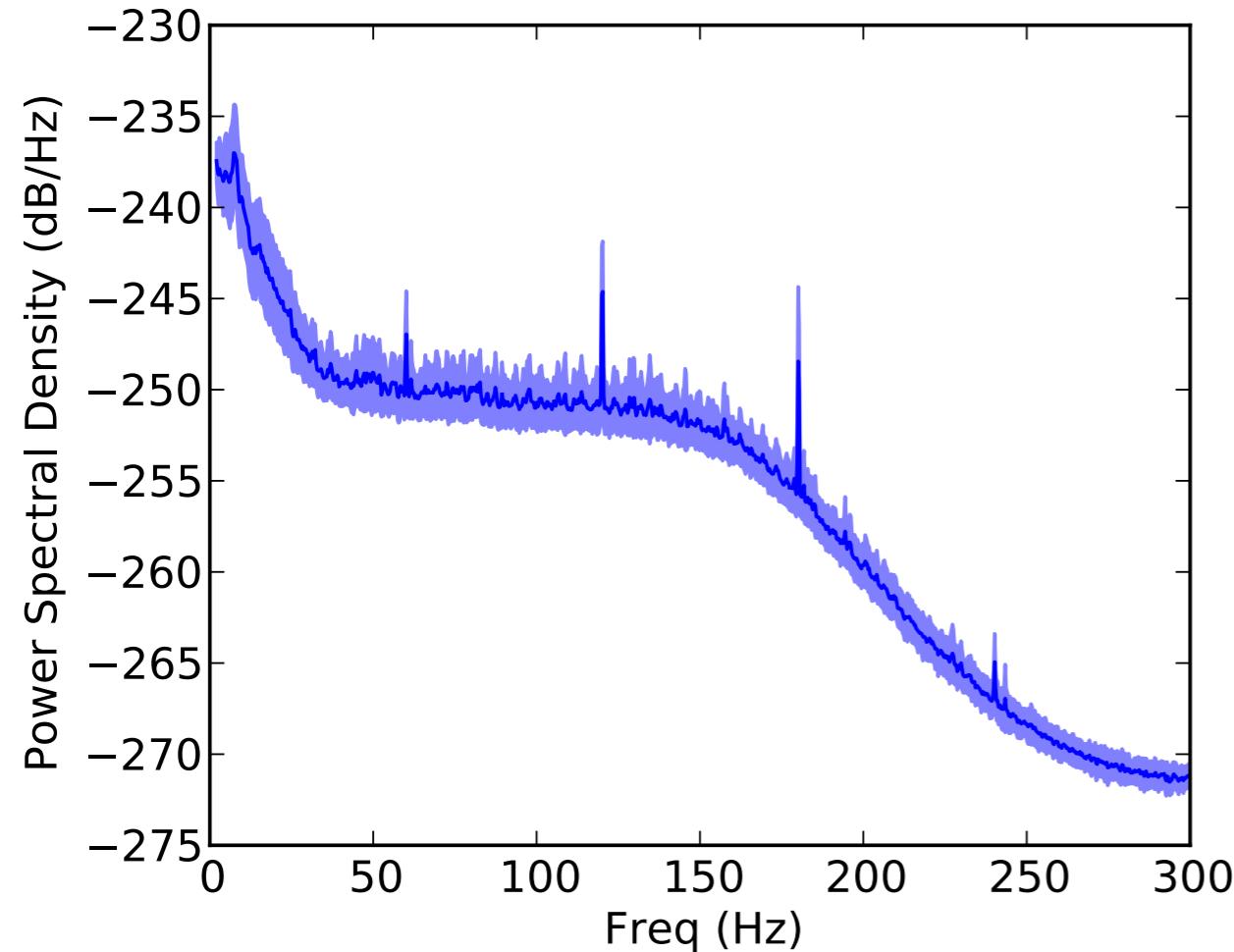
Pro: Presence of artifacts at some time instants so the windows can be discarded



Welch, P.D, "The Use of Fast Fourier Transform for the Estimation of Power Spectra: A Method Based on Time Averaging Over Short, Modified Periodograms," IEEE Trans. Audio Electroacoustics, Vol. AU-15 (June 1967), pp.70-73.

Power Spectrum Density

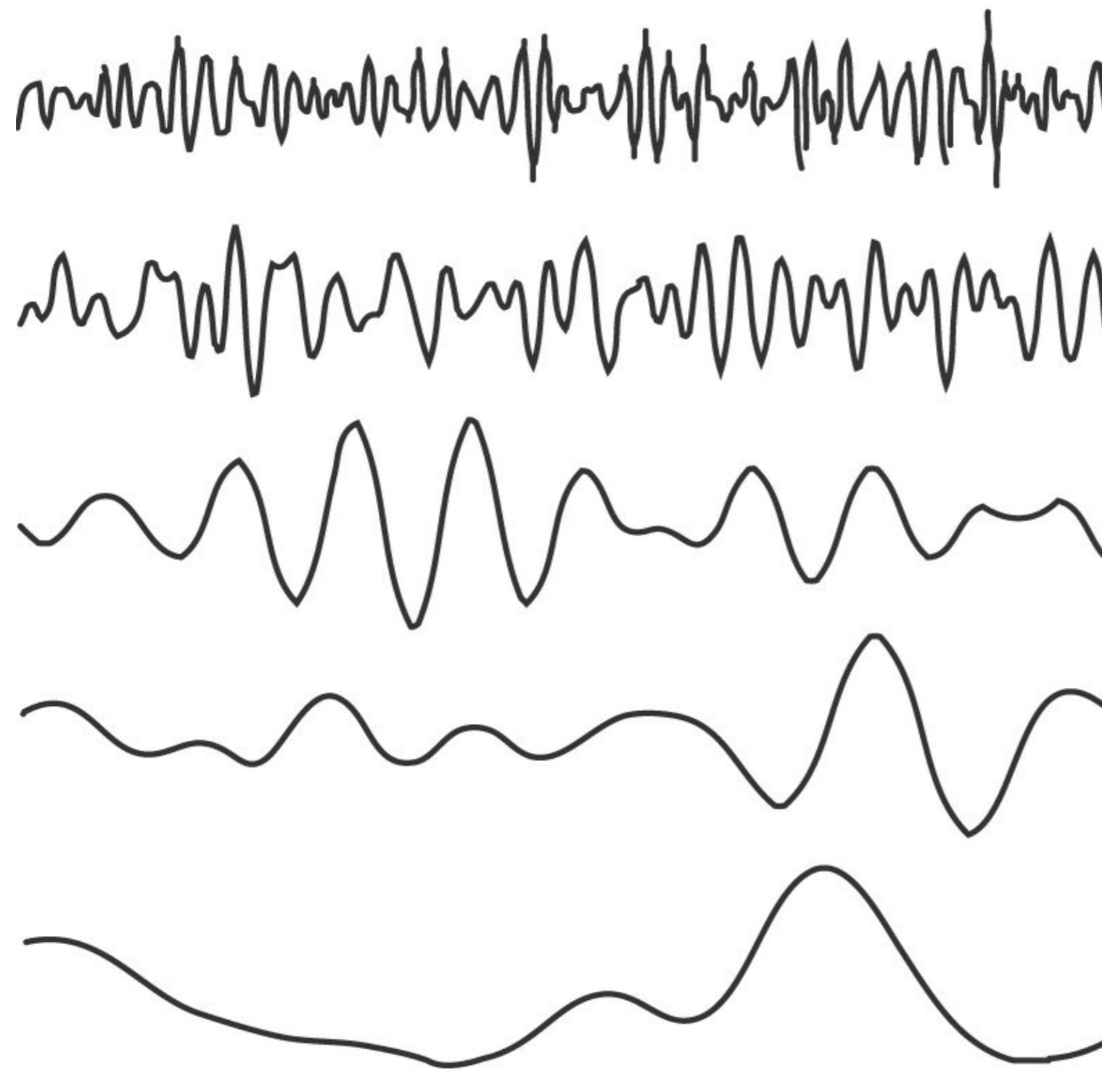
On raw data (typically > 5 minutes)



Presence of peaks
that are artifacts

I/f PSD

“Textbook” brain rythms



Gamma
(> 25 Hz)

Beta
(12-25 Hz)

Alpha
(8-12 Hz)

Theta
(4-8 Hz)

Delta
(1-4 Hz)

Part 2: Machine learning on EEG/MEG (a.k.a. decoding)

Encoding and Decoding Neuronal Dynamics: Methodological Framework to Uncover the Algorithms of Cognition

Jean-Rémi King, Laura Gwilliams, Chris Holdgraf, Jona Sassenhagen,
Alexandre Barachant, Denis Engemann, Eric Larson, Alexandre Gramfort

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Encoding and Decoding Neuronal Dynamics: Methodological Framework to Uncover the Algorithms
of Cognition. 2018. hal-01848442

<https://hal.archives-ouvertes.fr/hal-01848442/document>

Journal of Neural Engineering

TOPICAL REVIEW • OPEN ACCESS

Deep learning-based electroencephalography analysis: a systematic review

Yannick Roy^{1,5}  ID, Hubert Banville^{2,3,5}, Isabela Albuquerque⁴, Alexandre Gramfort², Tiago H Falk⁴ and Jocelyn Faubert¹

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[Journal of Neural Engineering](#), [Volume 16](#), [Number 5](#)



Article PDF

Figures ▾

References ▾

<https://arxiv.org/abs/1901.05498>

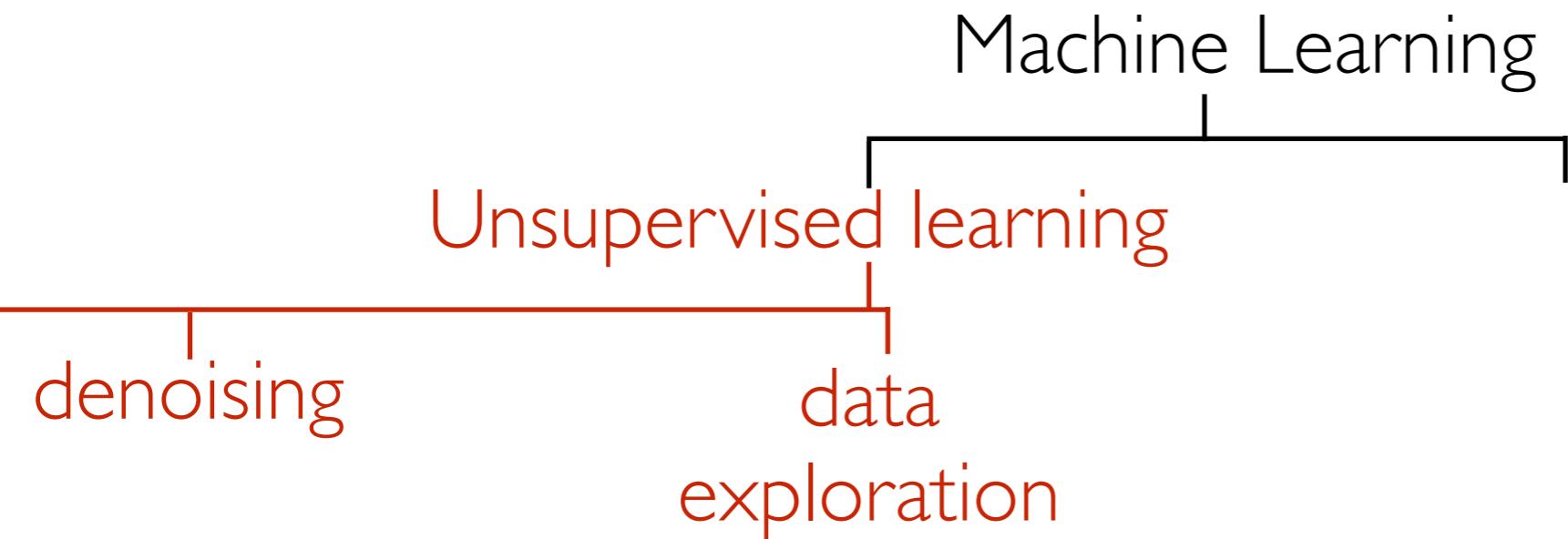
Machine Learning on EEG/MEG

“big picture”



Machine Learning on EEG/MEG

“big picture”

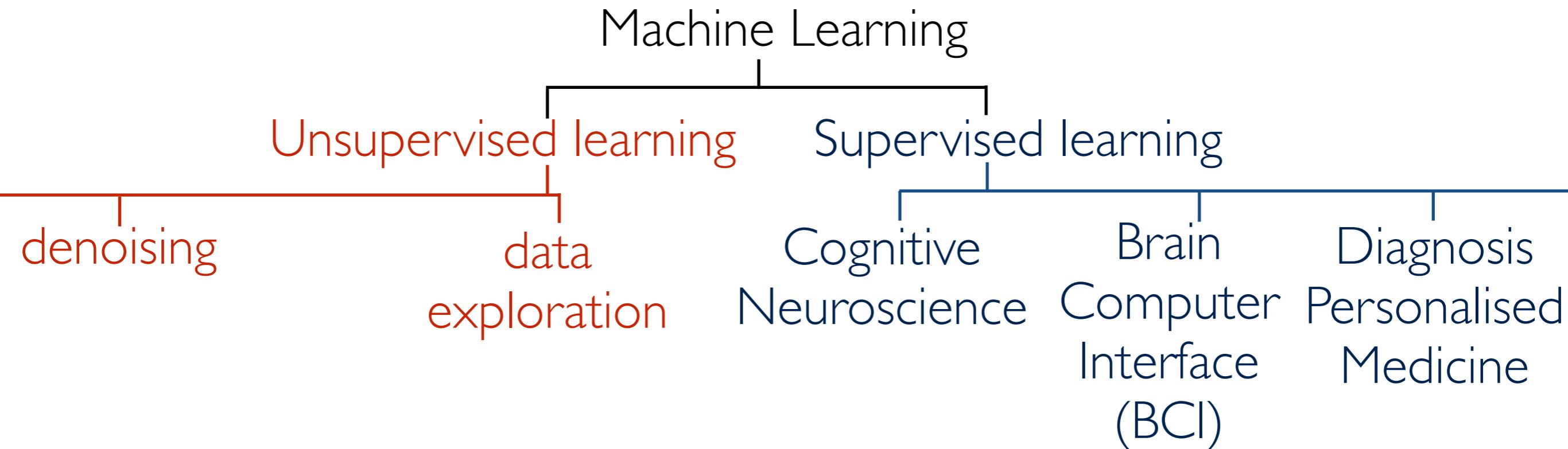


Methods:

Principal Component Analysis (PCA)
Independent Component Analysis (ICA)
Convolutional Sparse Coding (CSC)
Spatio-Spectral Decomposition (SSD)
etc.

Machine Learning on EEG/MEG

“big picture”



Methods:

Principal Component Analysis (PCA)
Independent Component Analysis (ICA)
Convolutional Sparse Coding (CSC)
Spatio-Spectral Decomposition (SSD)
etc.

Methods:

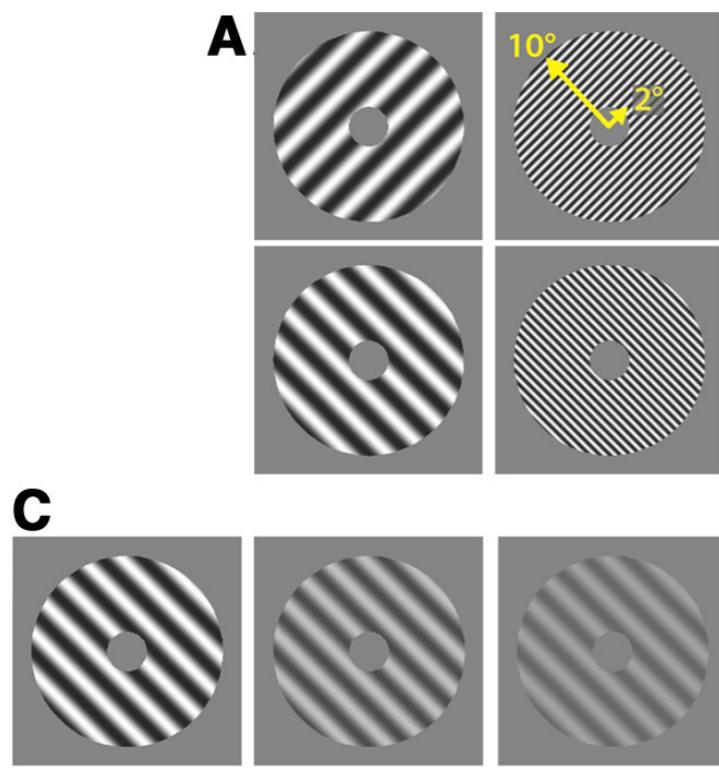
Linear Discriminant Analysis (LDA)
Logistic Regression (LR),
Support Vector Machine (SVM)
Common Spatial Filters (CSP)
Convolutional Neural Network (CNN)
Riemann on covariance matrices,
Random Forest, etc.

Outline

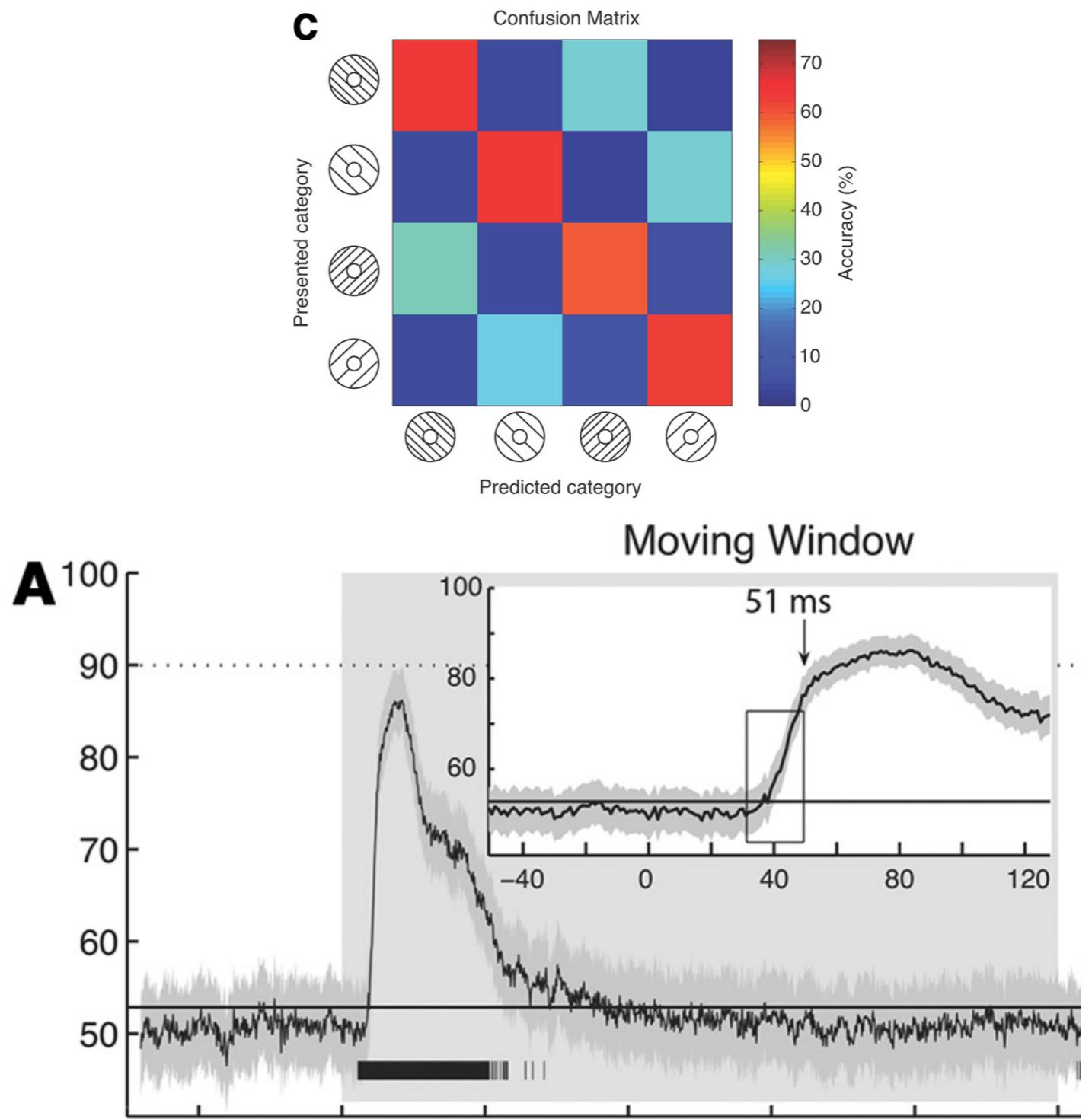
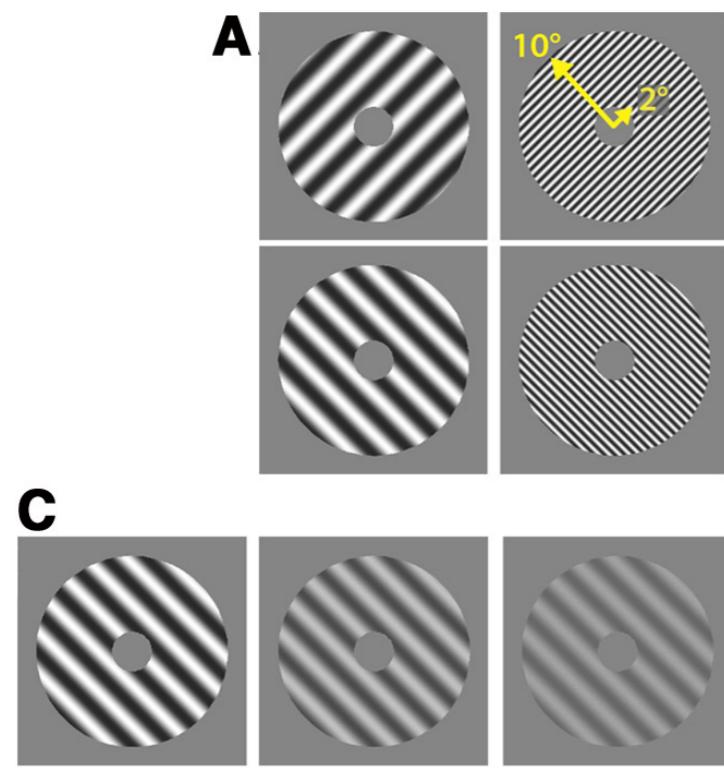
- Examples of EEG/MEG papers you can replicate with  MNE
MEG + EEG ANALYSIS & VISUALIZATION
- Evoked vs. Induced activity
- ML on EEG/MEG: Encoding vs. Decoding
- Why doing machine learning on EEG/MEG?
- Algorithms
 - Background on linear models
 - Algorithms for evoked activity (Time decoding, xDAWN)
 - Algorithms for induced activity (CSP, Riemann)
- How to run cross-validation right !
- Choosing your metric



Examples of ML on EEG and MEG



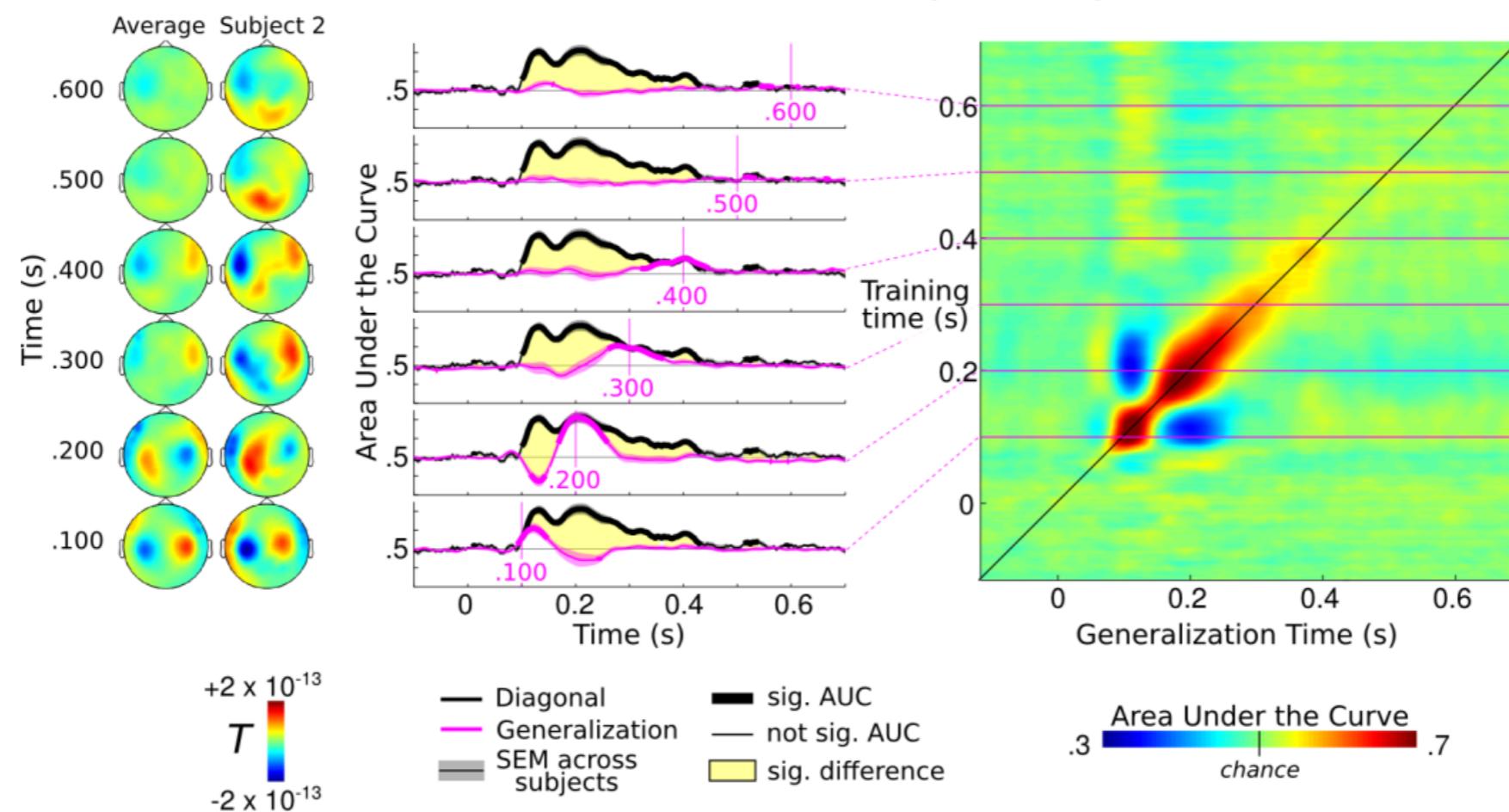
[Ramkumar, Jas, Pannasch, Hari, Parkkonen, J. Neuroscience (2013)]



“Time-resolved classifiers using a 20 ms moving window exceeded chance level at 51 ms (the later edge of the window) for spatial frequency, 65 ms for orientation, and 98 ms for rotation direction.”

[Ramkumar, Jas, Pannasch, Hari, Parkkonen, J. Neuroscience (2013)]

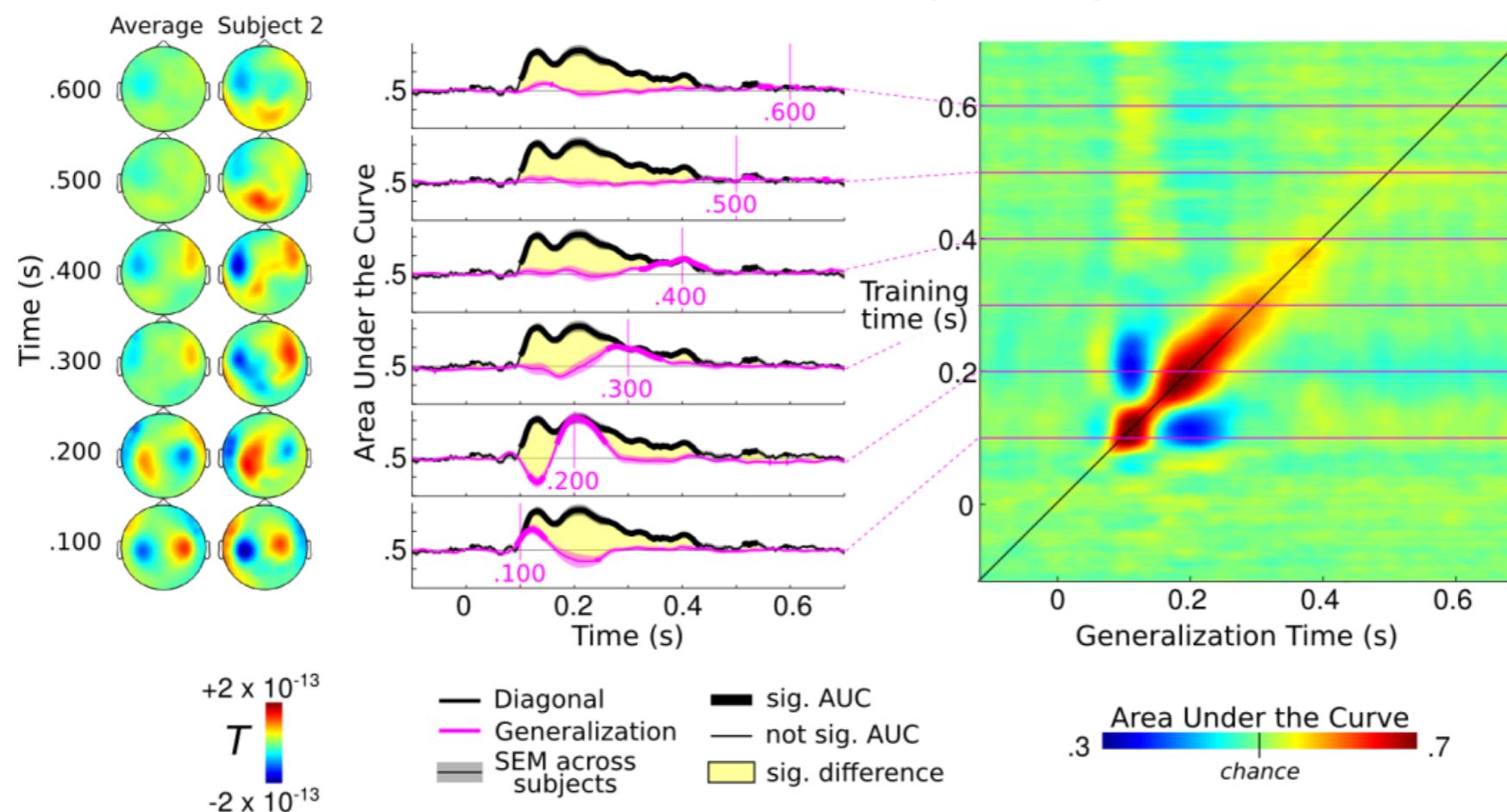
Local Auditory Novelty



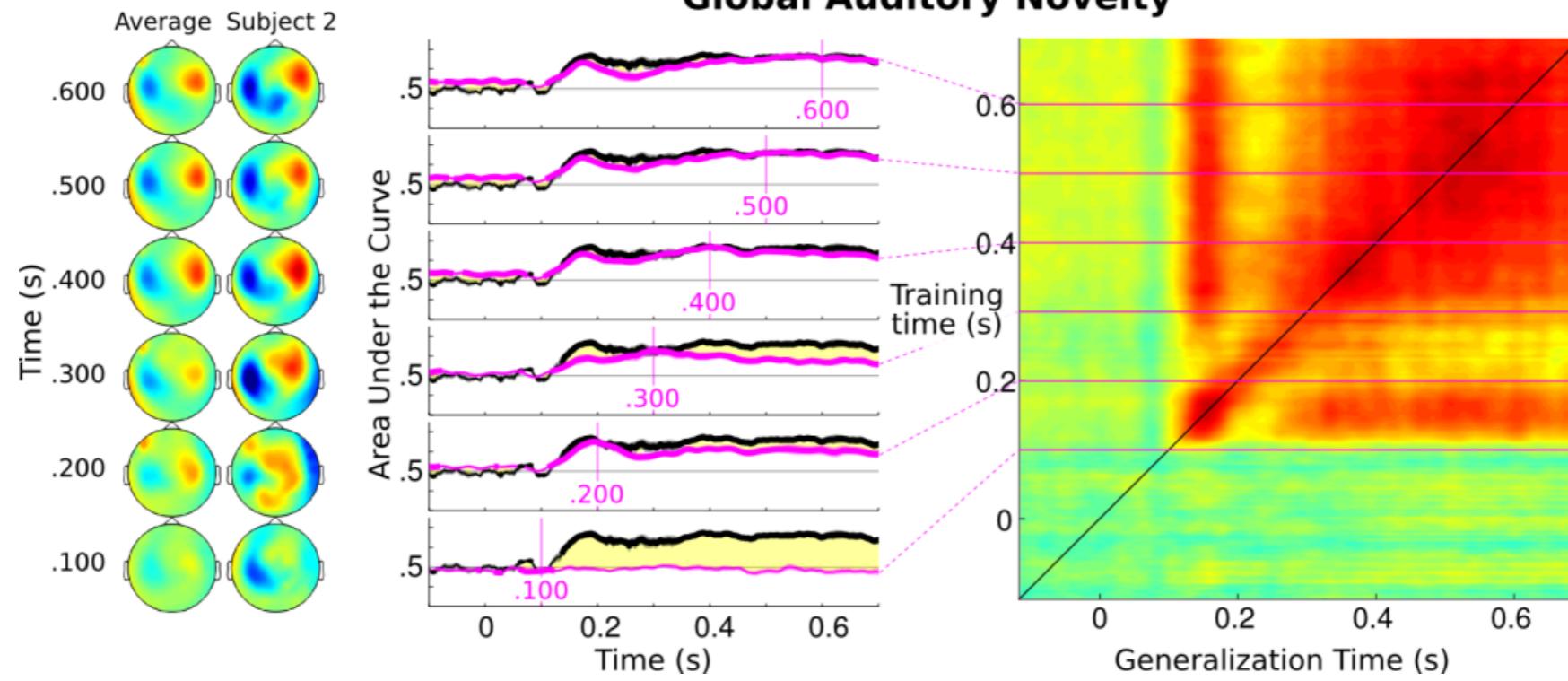
[King, Gramfort, Schurger, Naccache, Dehaene (2014) PLoS One]

<https://mne.tools/stable/generated/mne.decoding.GeneralizingEstimator.html>

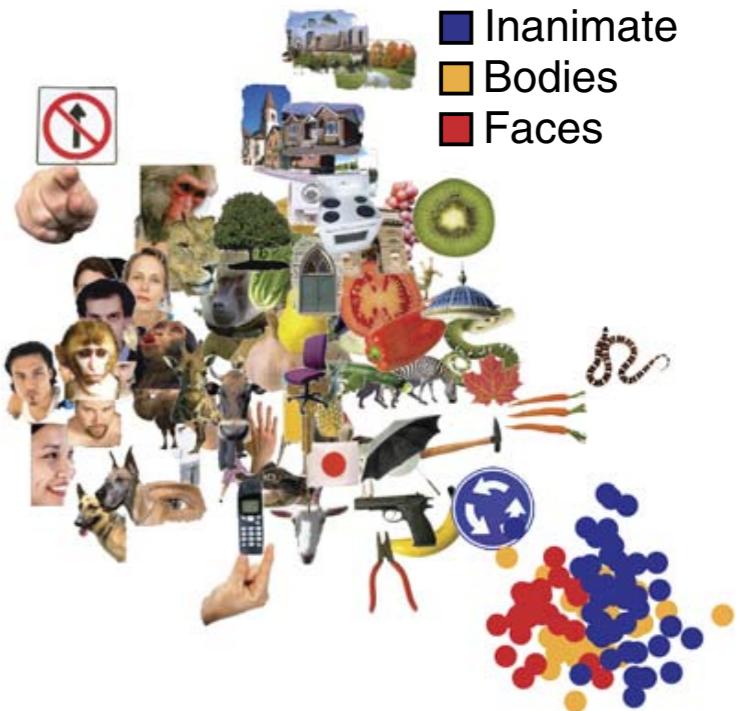
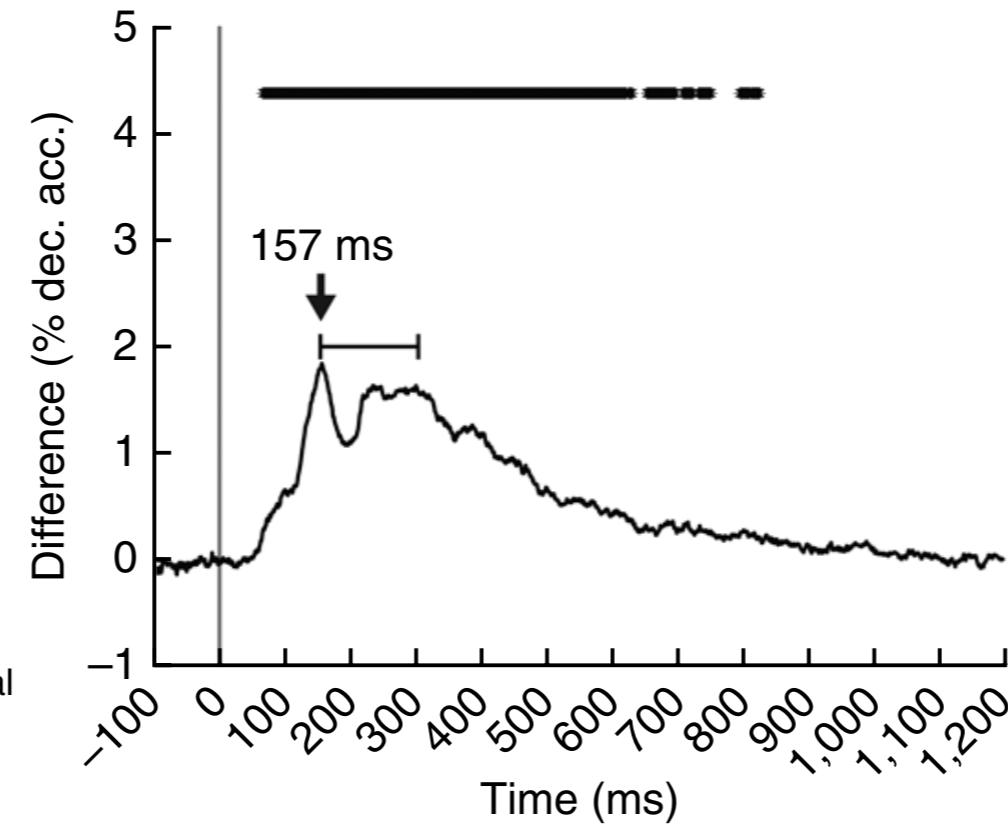
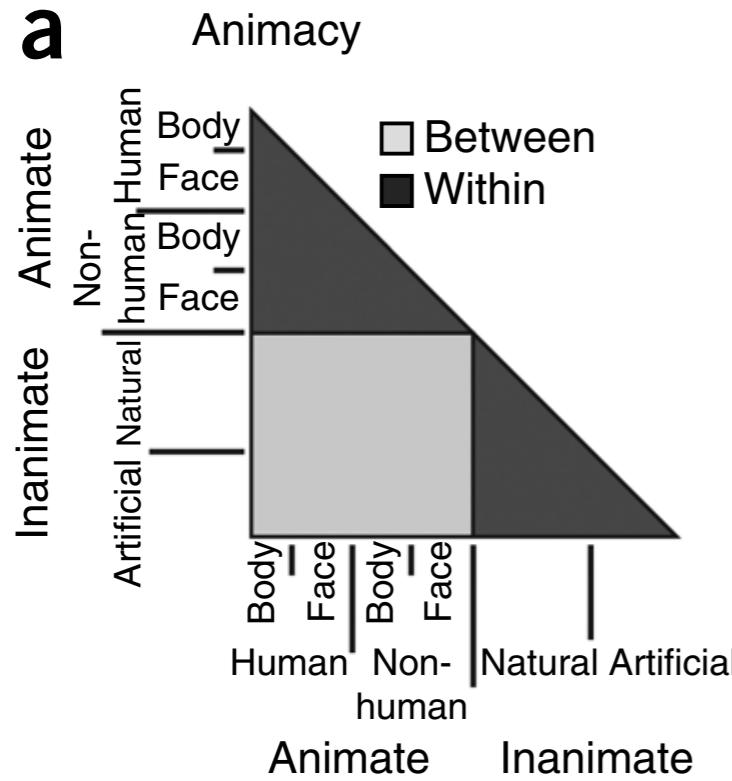
Local Auditory Novelty



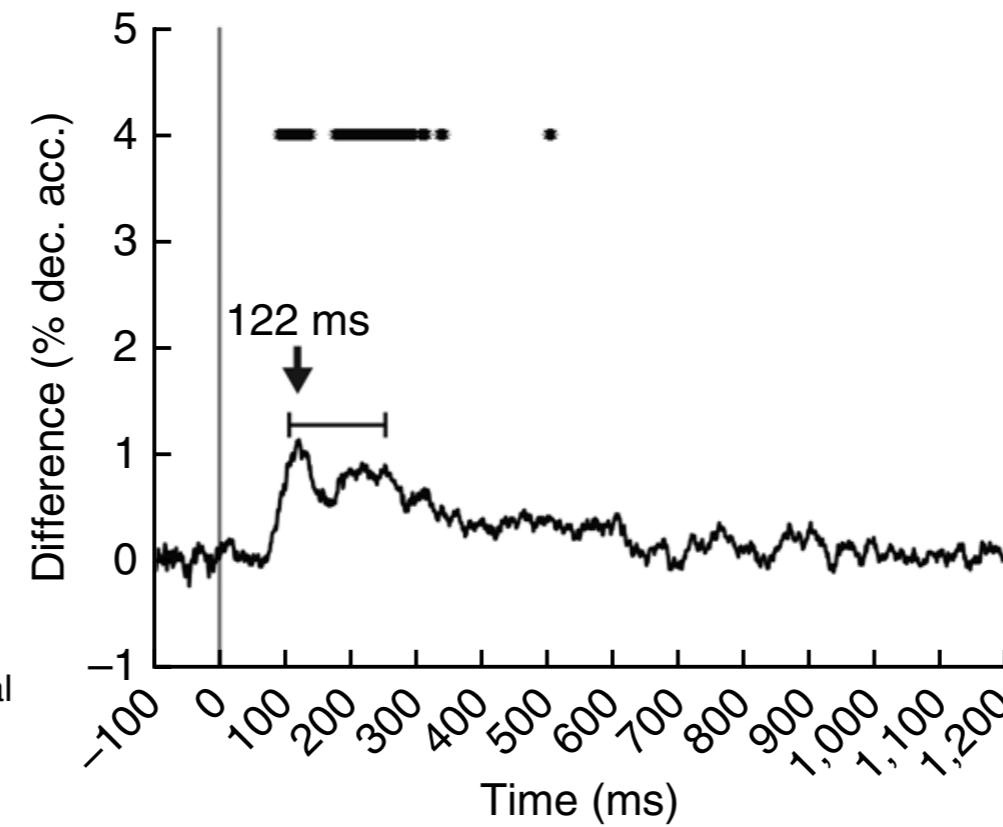
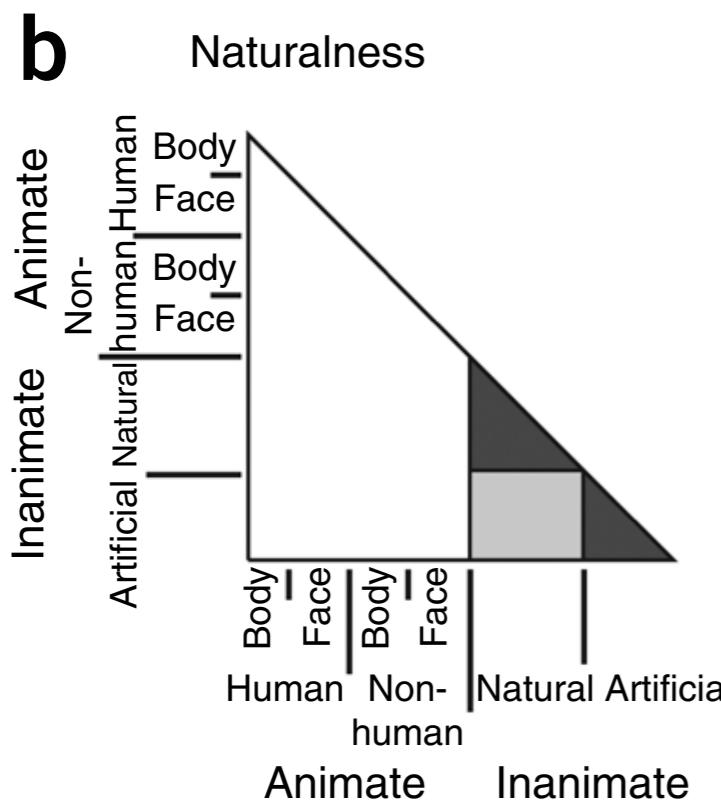
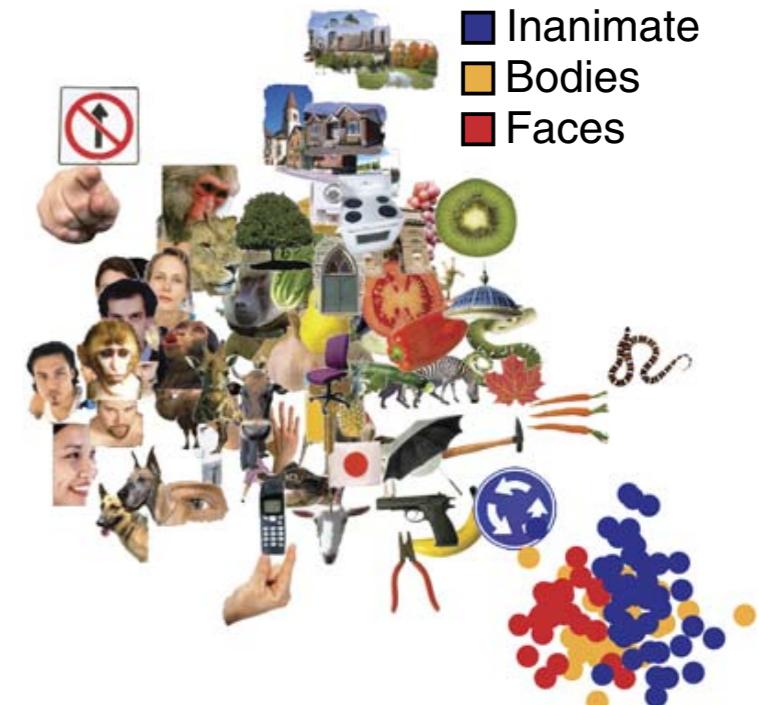
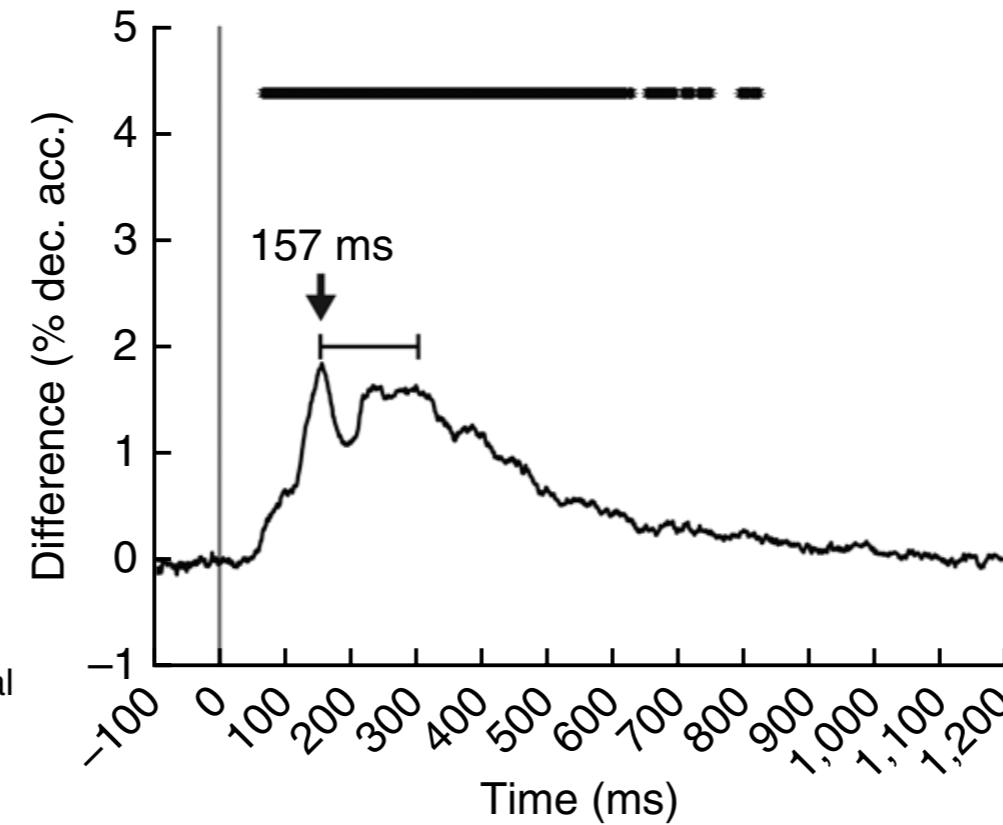
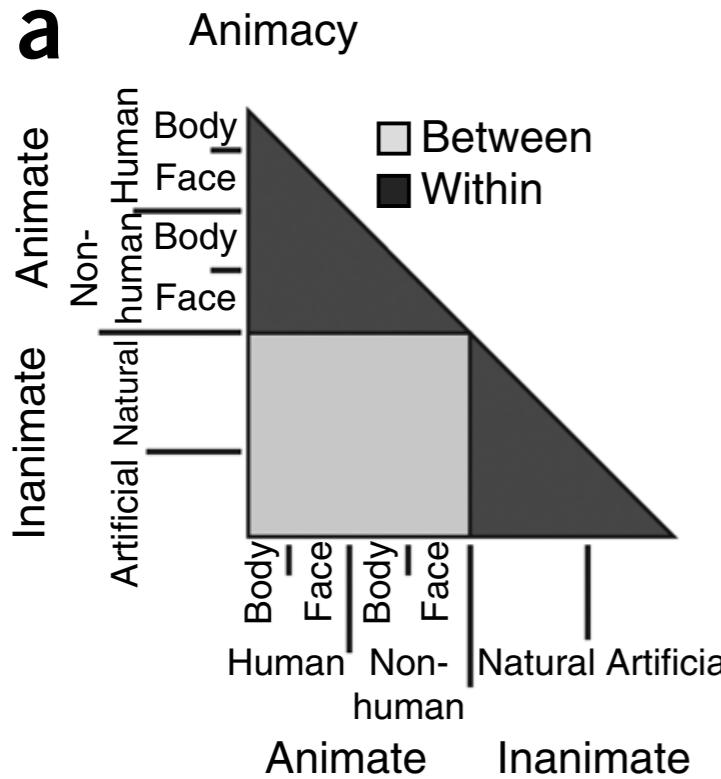
Global Auditory Novelty



[King, Gramfort, Schurger, Naccache, Dehaene (2014) PLoS One]

a

[*Resolving human object recognition in space and time, Cichy, Pantazis & Oliva, Nat Neuro 2014*]



[*Resolving human object recognition in space and time, Cichy, Pantazis & Oliva, Nat Neuro 2014*]

J Neurophysiol. 2012 Jan 1; 107(1): 78–89.
Published online 2011 Oct 5. doi: [10.1152/jn.00297.2011](https://doi.org/10.1152/jn.00297.2011)

PMCID: PMC3570829
PMID: [21975452](https://pubmed.ncbi.nlm.nih.gov/21975452/)

Neural coding of continuous speech in auditory cortex during monaural and dichotic listening

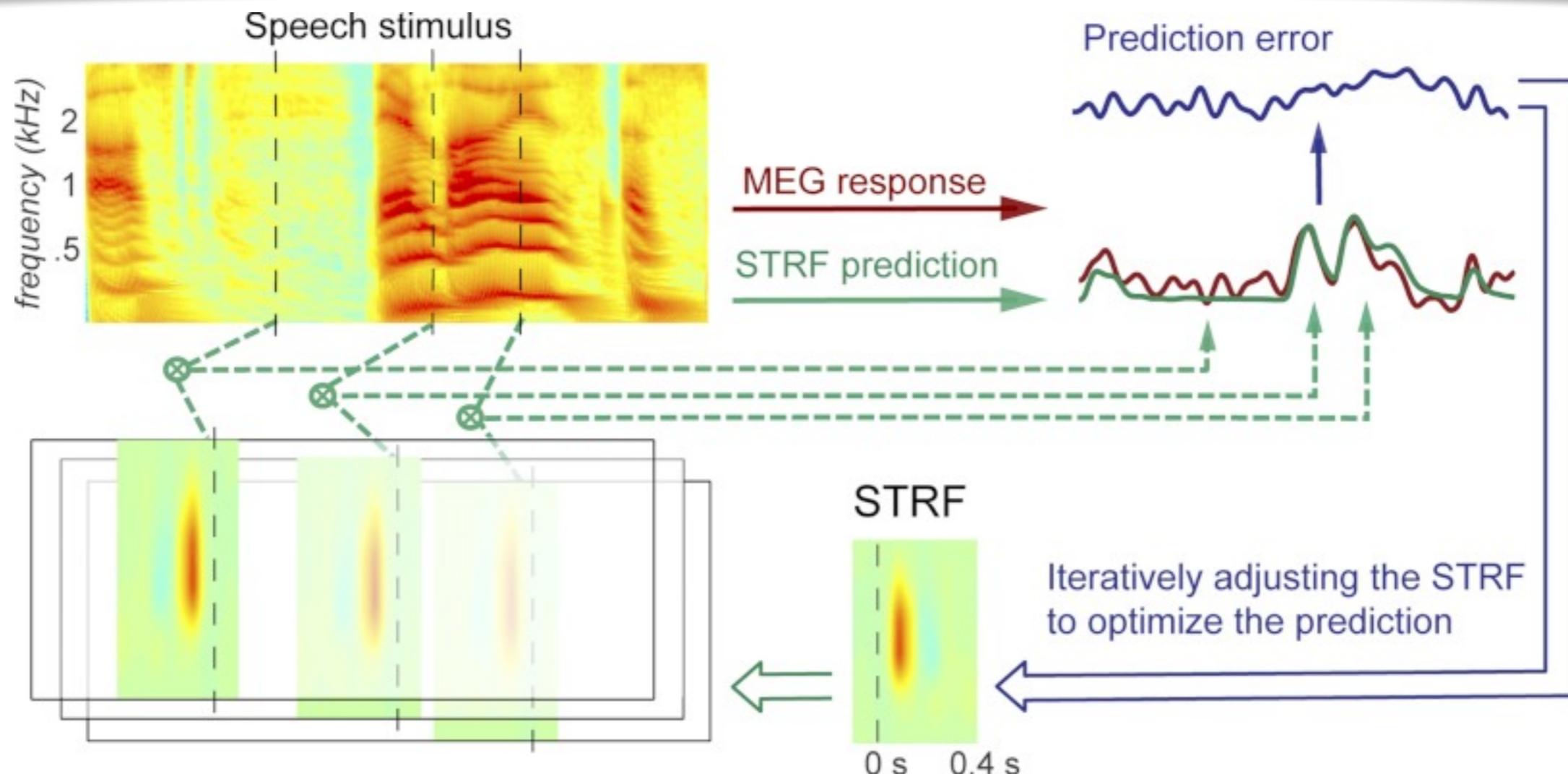
Nai Ding¹ and Jonathan Z. Simon^{1,2}

¹Department of Electrical and Computer Engineering and

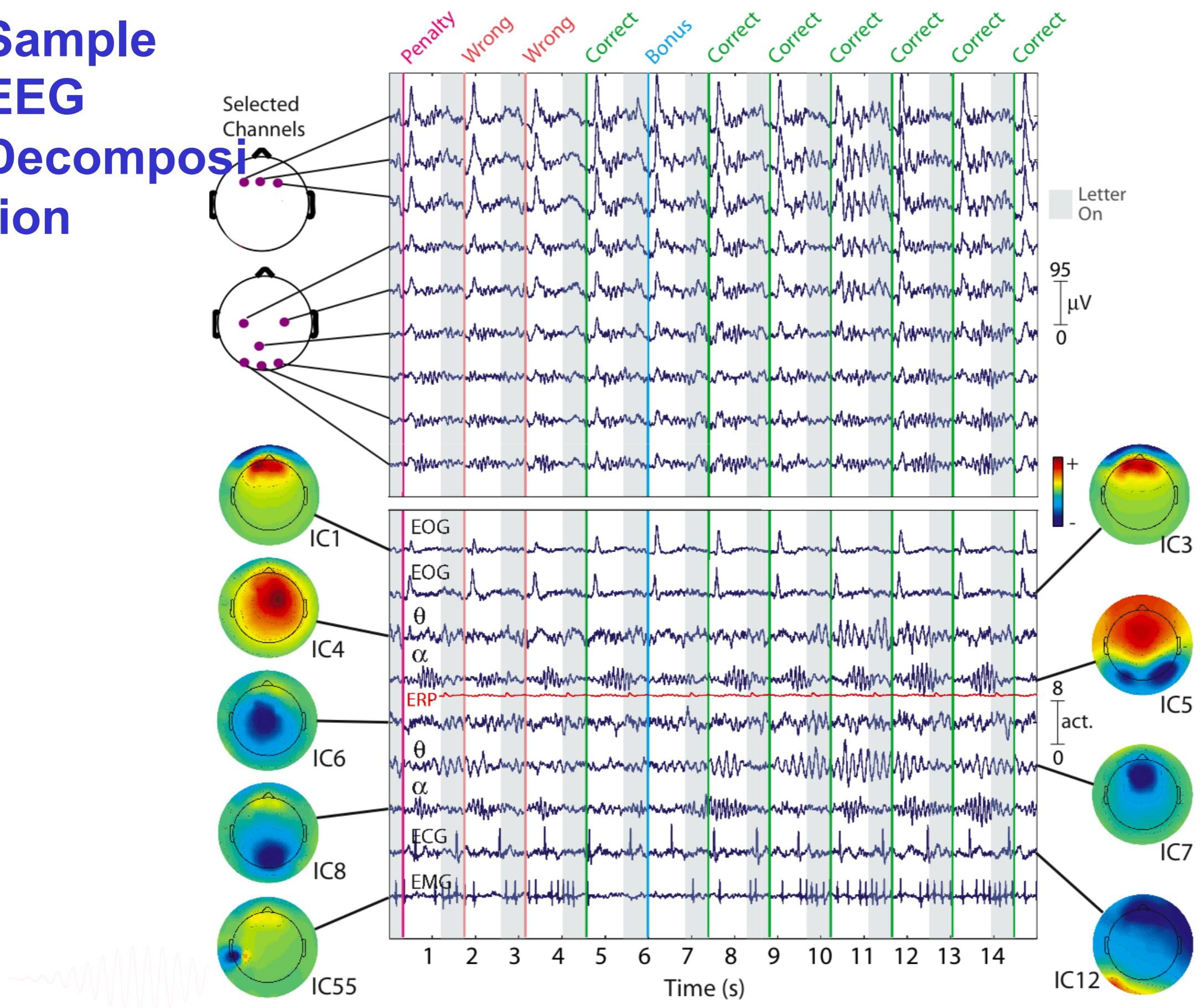
²Department of Biology, University of Maryland, College Park, Maryland

✉ Corresponding author.

Address for reprint requests and other correspondence: J. Z. Simon, Univ. of Maryland, College Park, MD 20742 (e-mail: jzsimon@umd.edu).

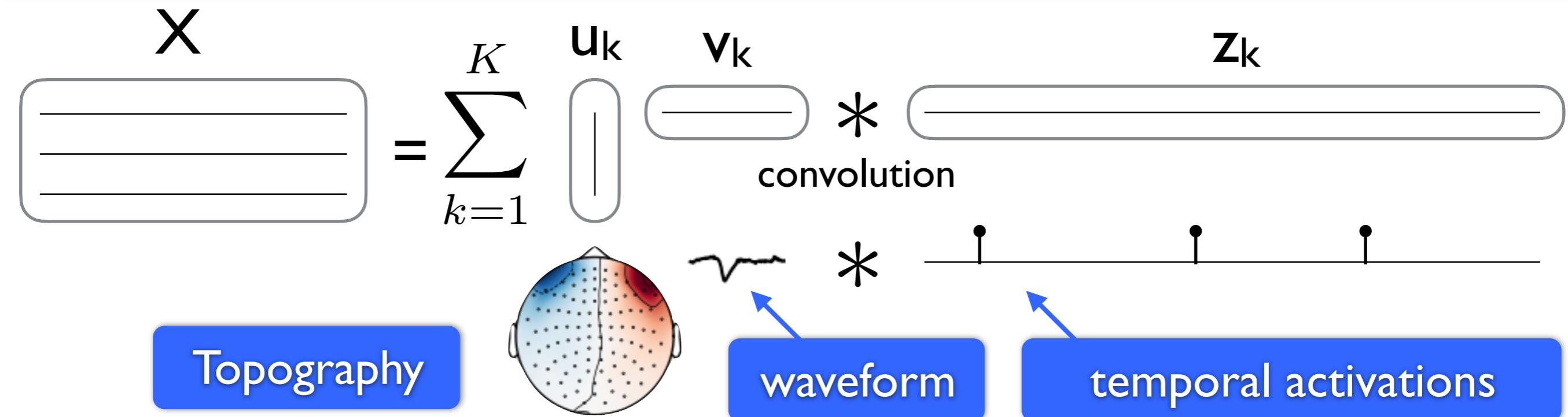


Sample EEG Decomposi tion



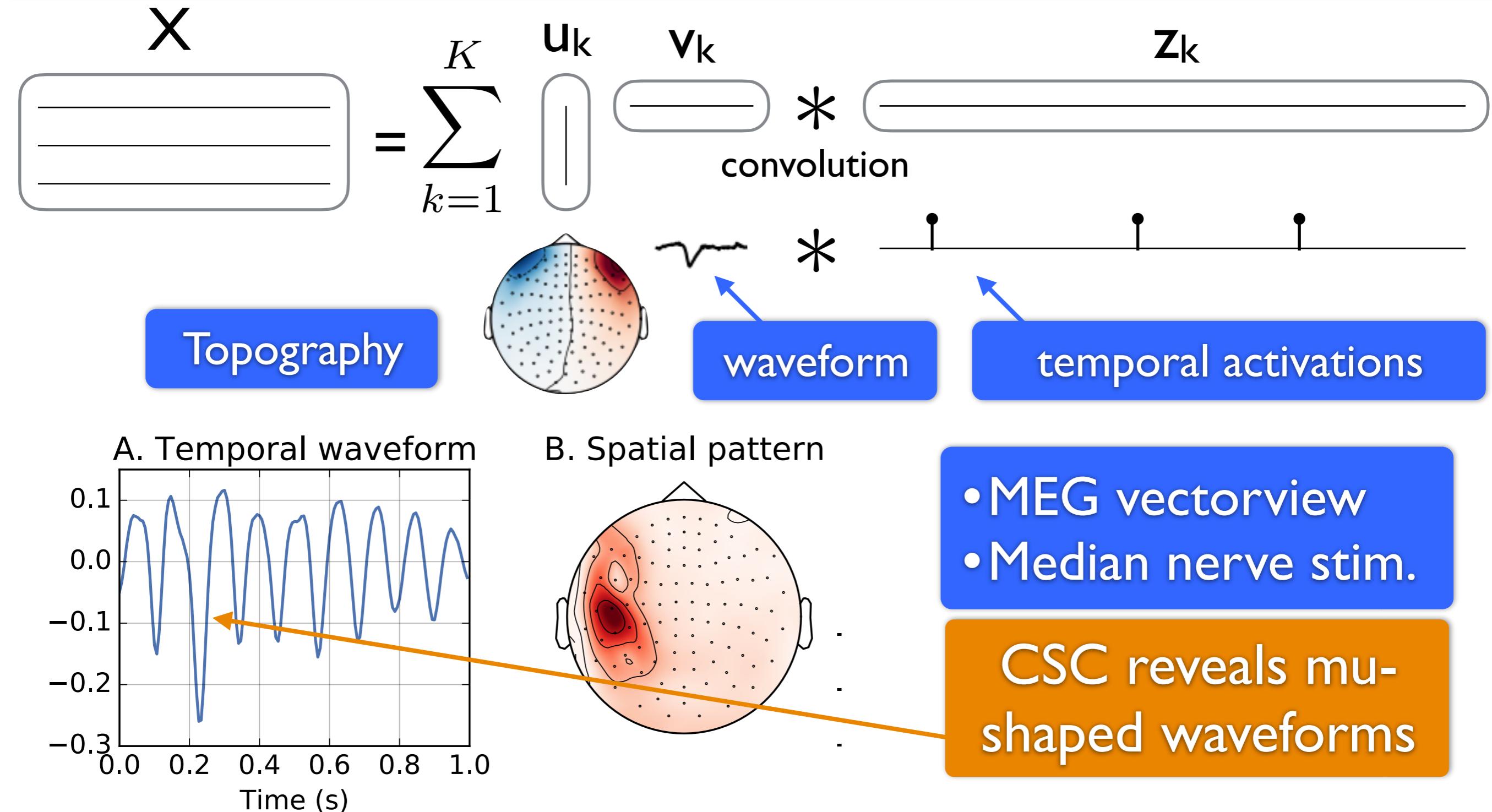
[Makeig et al. 1996, Jung et al. 1998, Jung et al. 1999 etc.]

Convolutional Sparse Coding



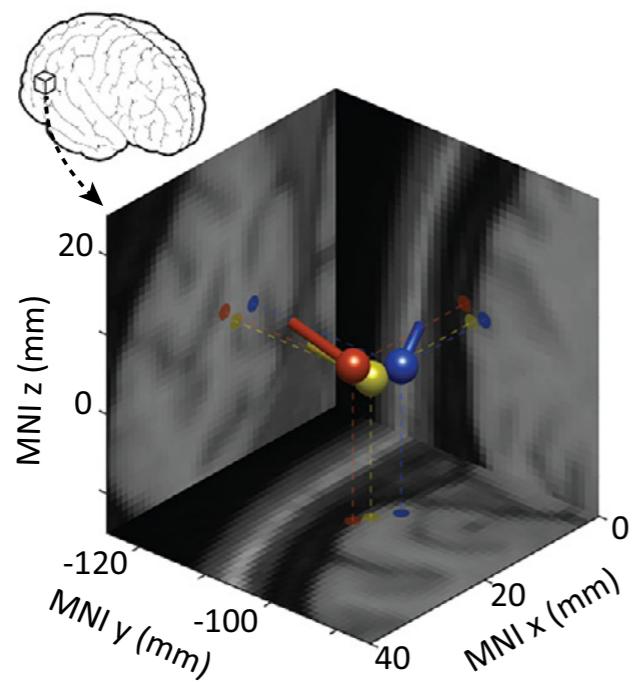
[*Multivariate Convolutional Sparse Coding for Electromagnetic Brain Signals, (2018), T. Dupré la Tour, T. Moreau, M. Jas, A. Gramfort, Proc. NeurIPS Conf.*]

Convolutional Sparse Coding

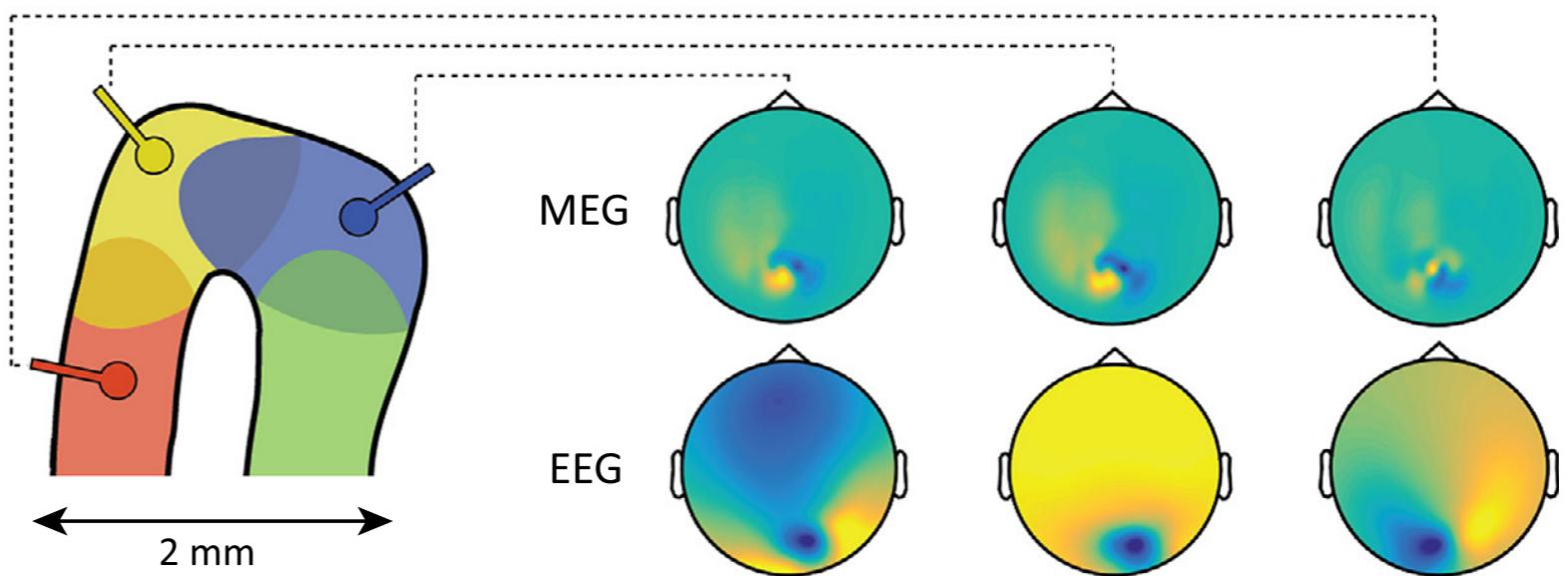


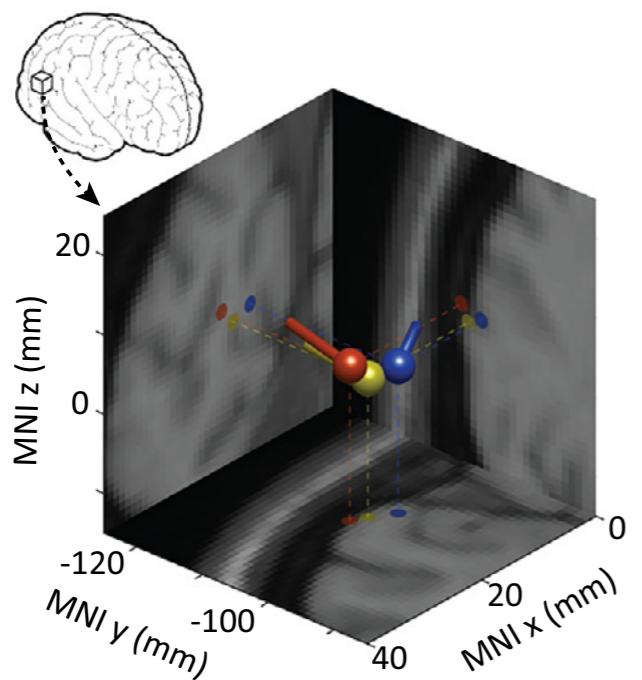
[*Multivariate Convolutional Sparse Coding for Electromagnetic Brain Signals, (2018), T. Dupré la Tour, T. Moreau, M. Jas, A. Gramfort, Proc. NeurIPS Conf.*]

Why it works

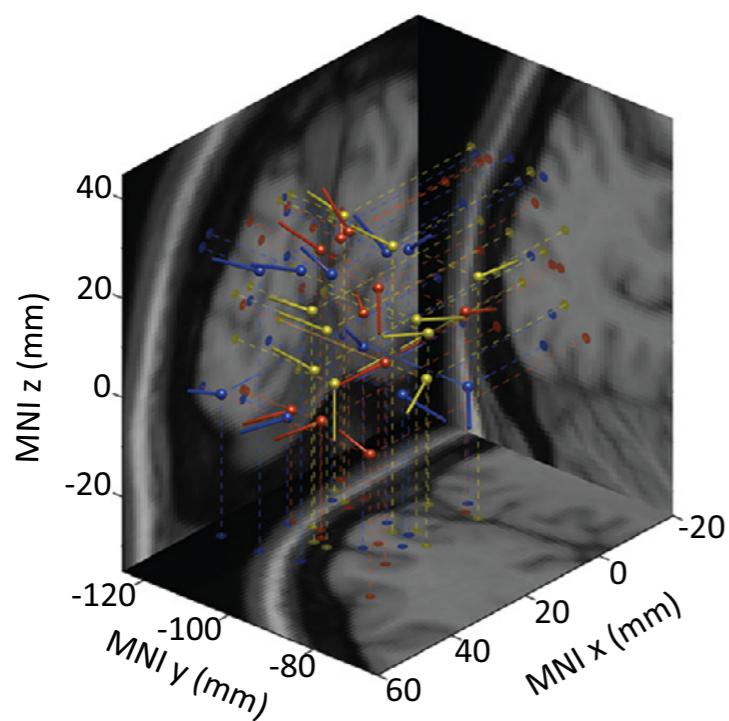
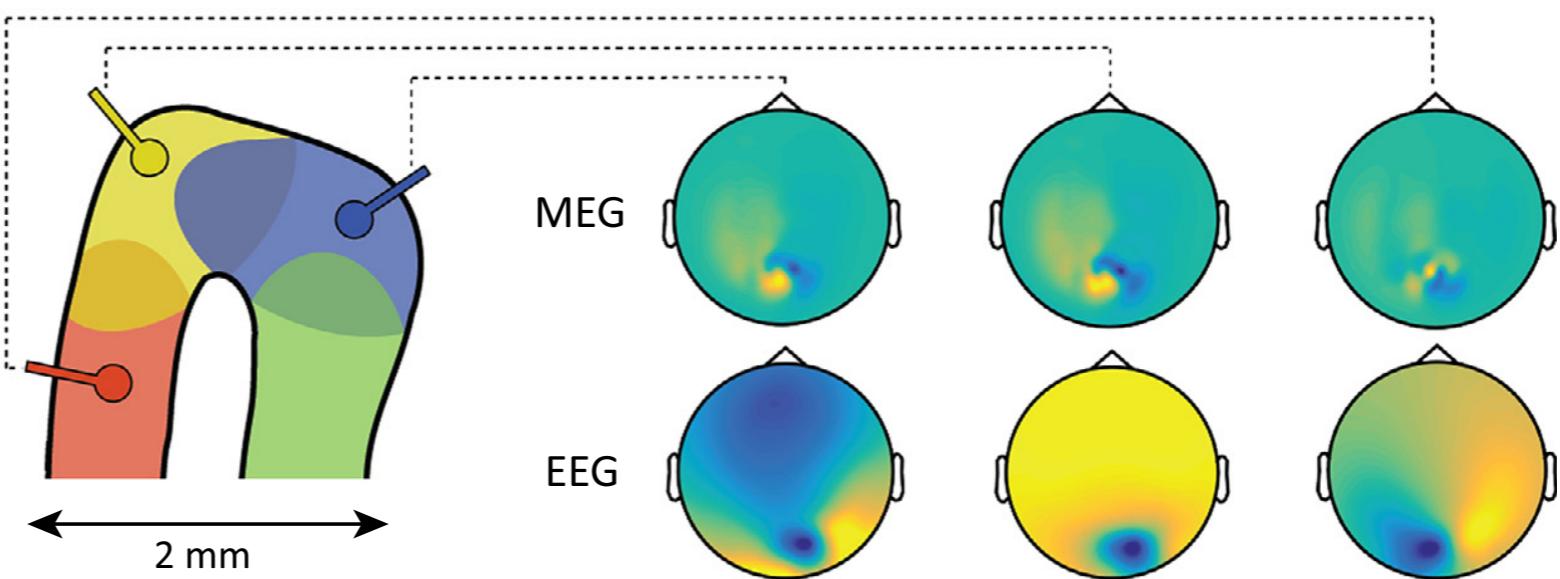


(i) Example for three orientation-specific dipoles

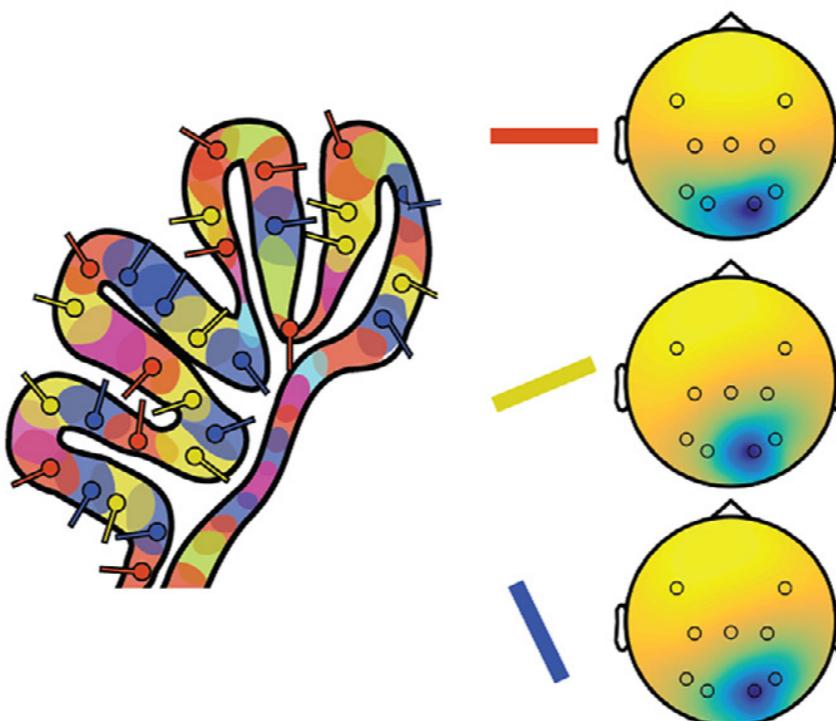




(i) Example for three orientation-specific dipoles



(ii) Example for many orientation-specific dipoles



New research suggests that magnetoencephalography (MEG) contains rich spatial information for decoding neural states. Even small differences in the angle of neighbouring dipoles generate subtle, but statistically separable field patterns. This implies MEG (and electroencephalography: EEG) is ideal for decoding neural states with high-temporal resolution in the human brain.

Multivariate models boost SNR

Consider 2 EEG signals such that:

$$x_1(t) = 2s(t) + n(t)$$

$$x_2(t) = s(t) + n(t)$$

where $s(t)$ is the source and $n(t)$ the additive noise, which is common.

Multivariate models boost SNR

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$$x_1(t) = 2s(t) + n(t)$$

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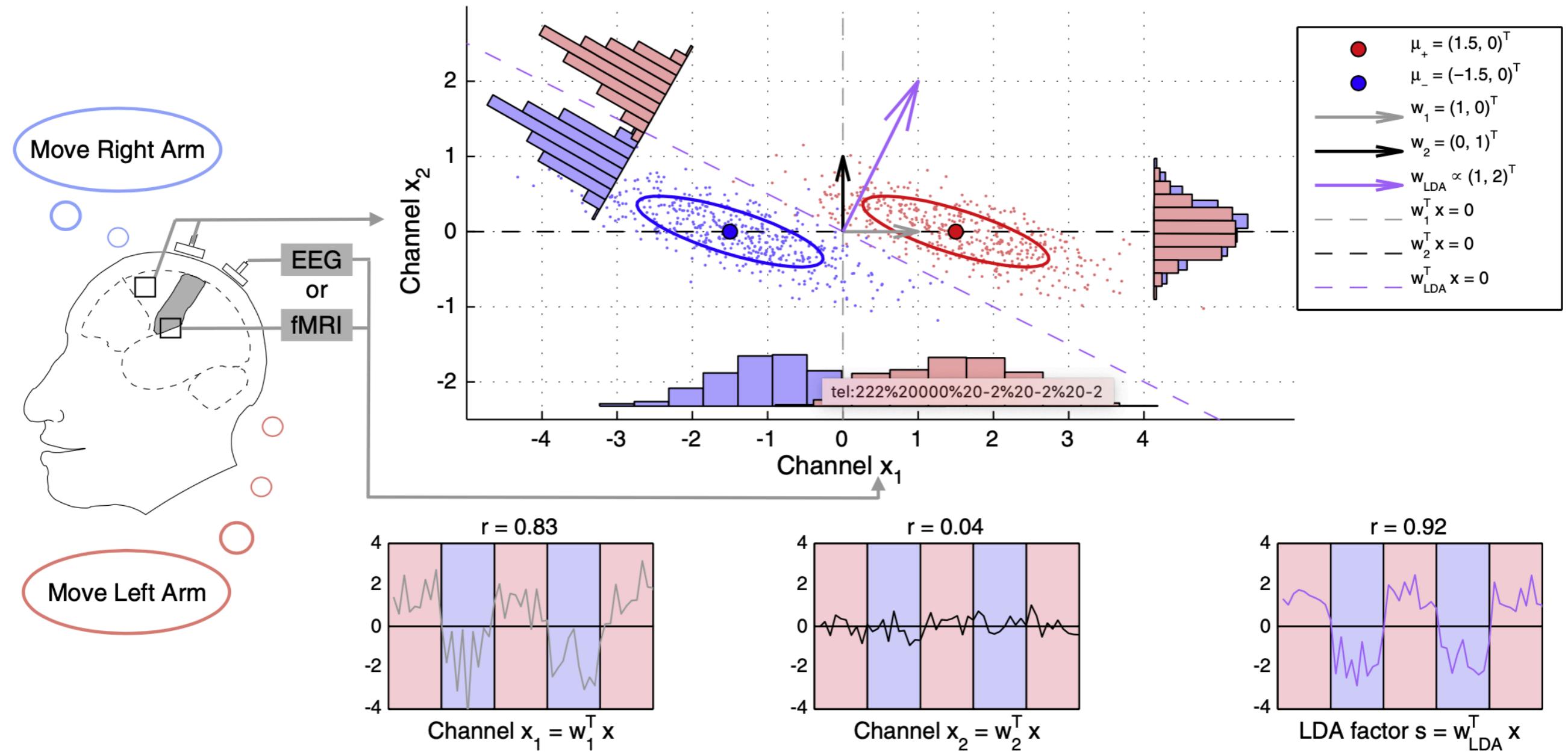
This implies that:

$$x_1(t) - x_2(t) = s(t)$$

Only signal remains !

**THM: By subtracting the signals
one can improve the SNR even if noise is huge**

Multivariate models boost SNR



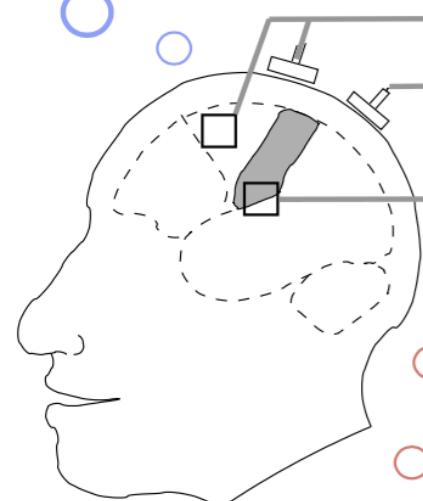
[Haufe et al. (2014) On the interpretation of weight vectors of linear models in multivariate neuroimaging, *NeuroImage*]

MNE
MEG + EEG ANALYSIS & VISUALIZATION

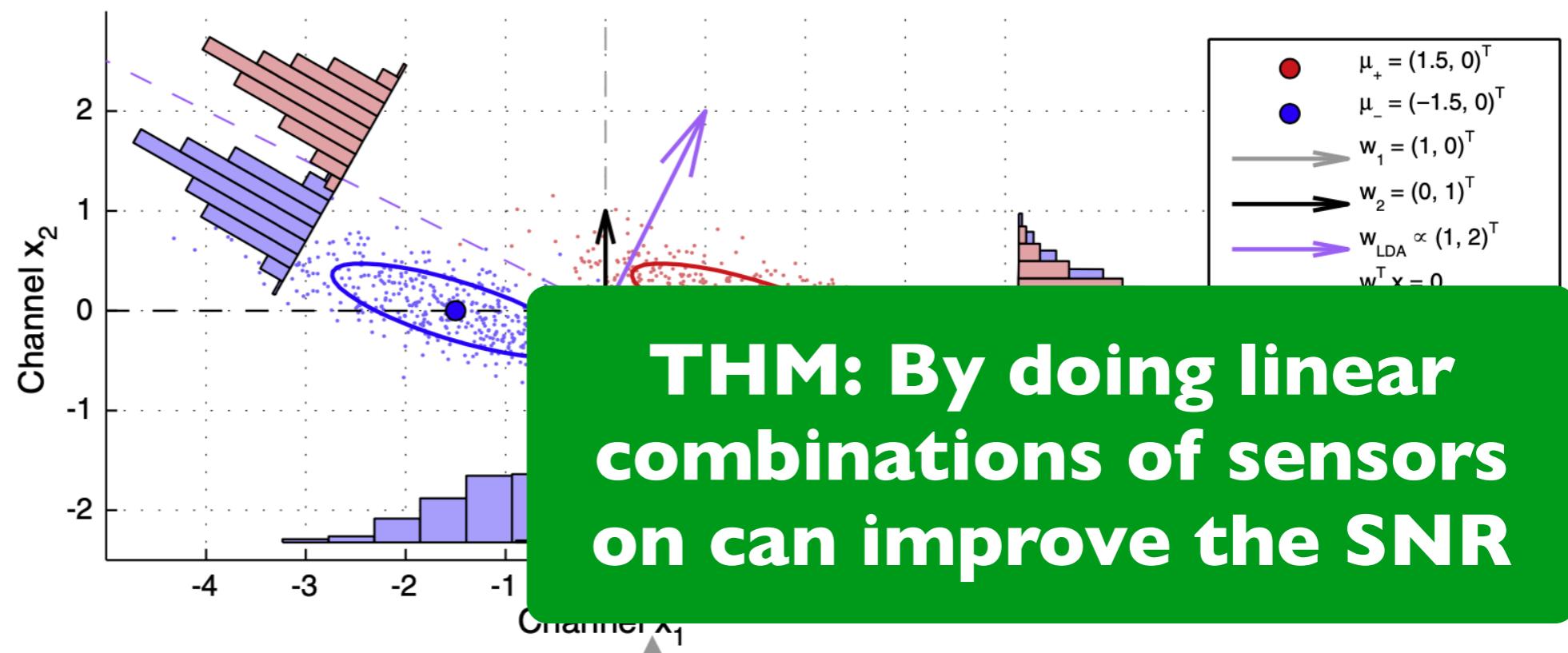
https://mne.tools/stable/auto_examples/decoding/plot_linear_model_patterns.html

Multivariate models boost SNR

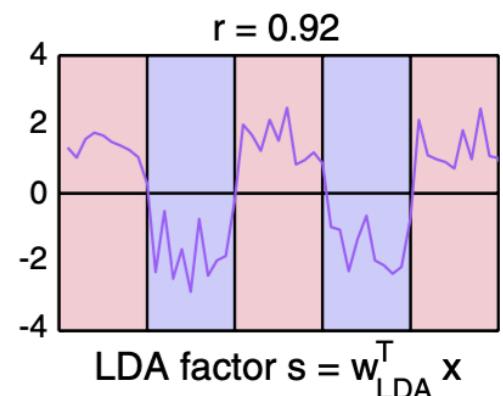
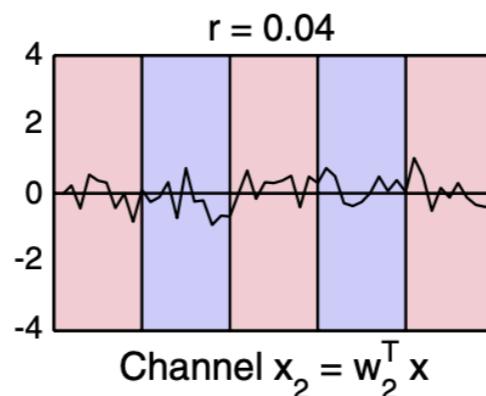
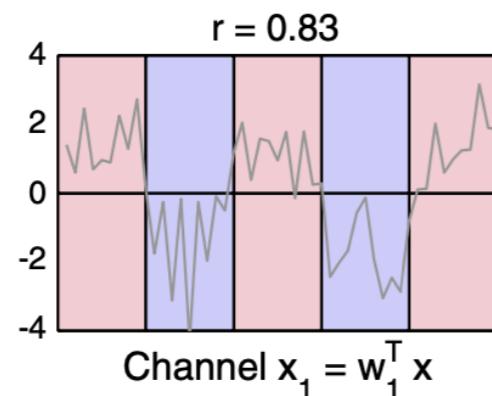
Move Right Arm



EEG
or
fMRI



Move Left Arm



[Haufe et al. (2014) On the interpretation of weight vectors of linear models in multivariate neuroimaging, NeuroImage]

MNE
MEG + EEG ANALYSIS & VISUALIZATION

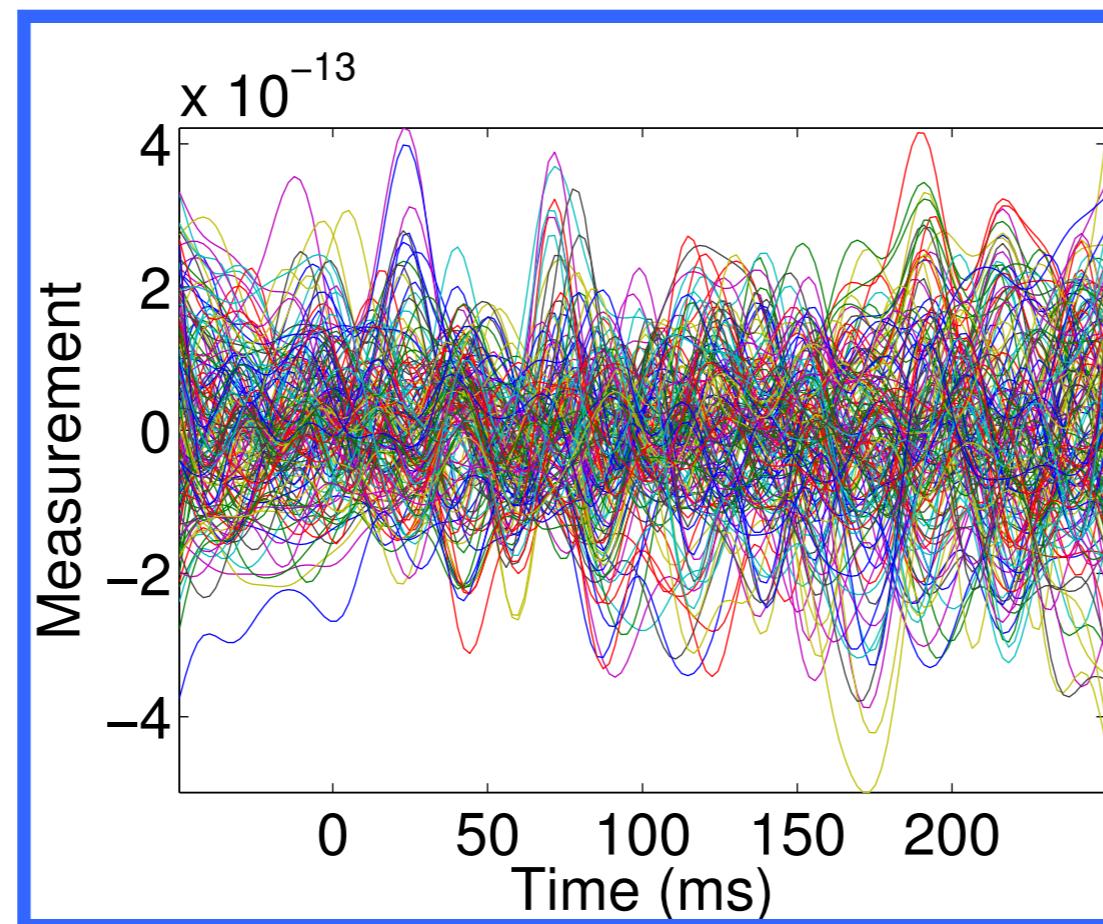
https://mne.tools/stable/auto_examples/decoding/plot_linear_model_patterns.html

Induced and Evoked M/EEG activity

requires different ML approaches

Evoked activity

Evoked activity is revealed by trial averaging:

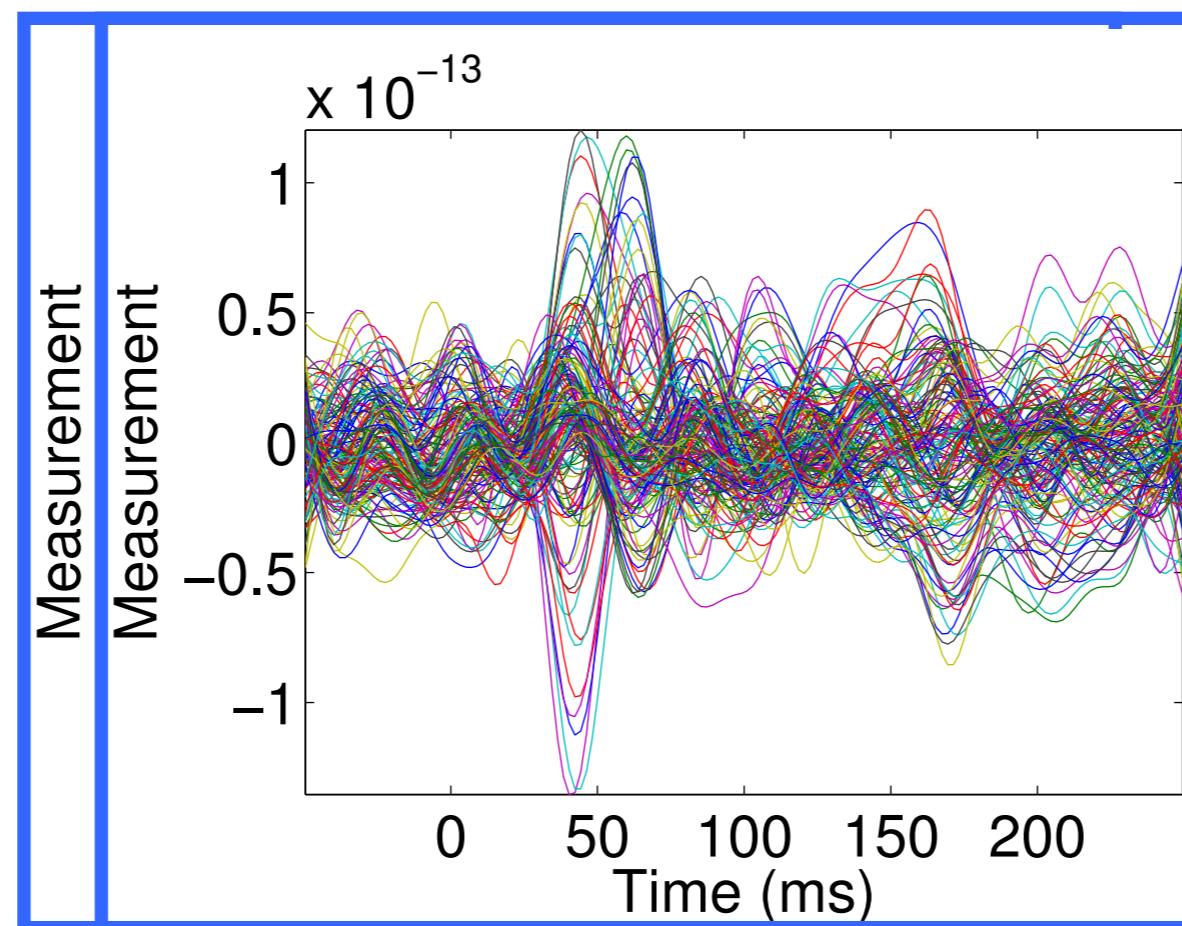


Signal
on
151
MEG
Channels

| trial

Evoked activity

Evoked activity is revealed by trial averaging:

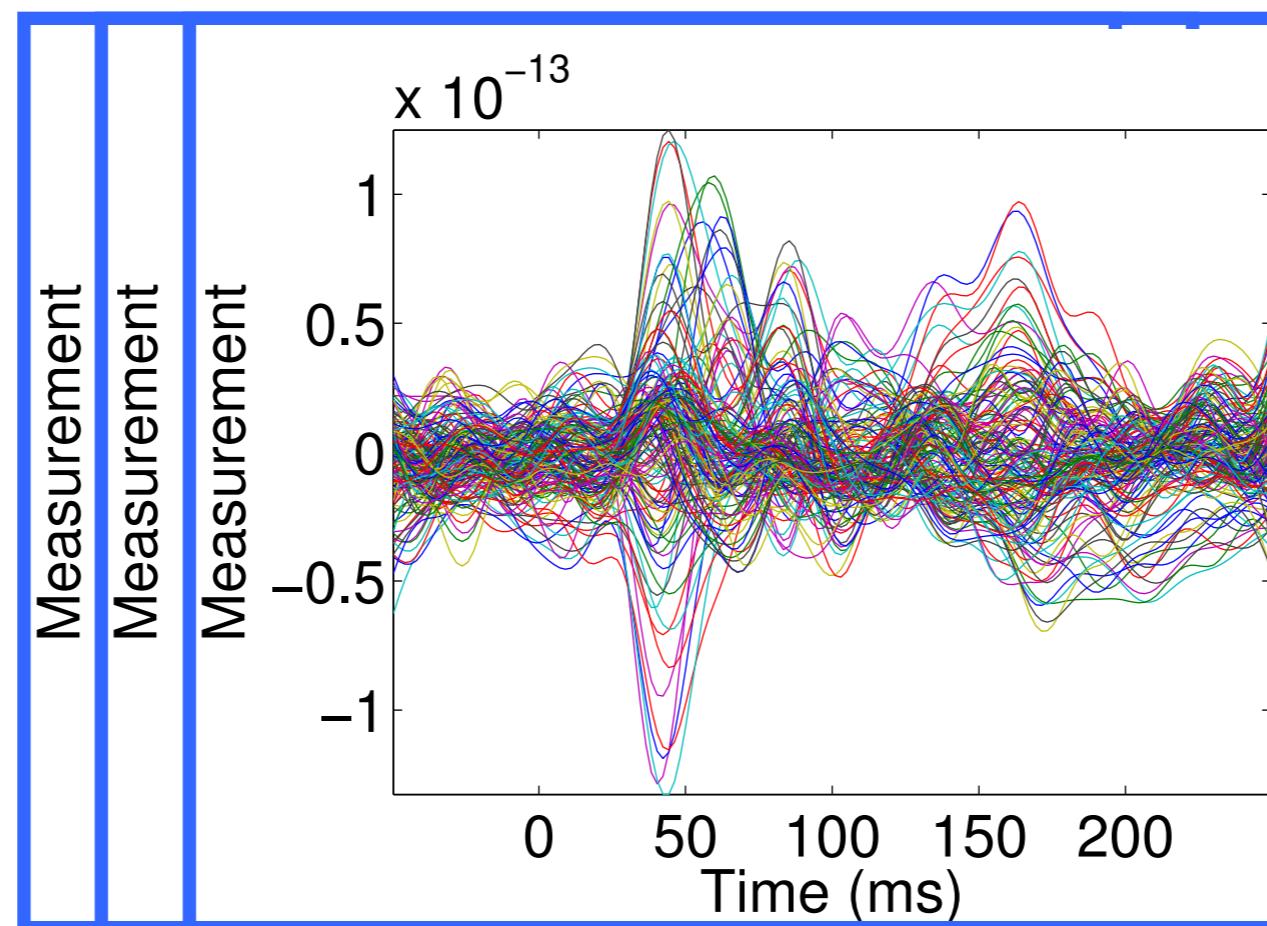


50 trials

Signal
on
151
MEG
Channels

Evoked activity

Evoked activity is revealed by trial averaging:

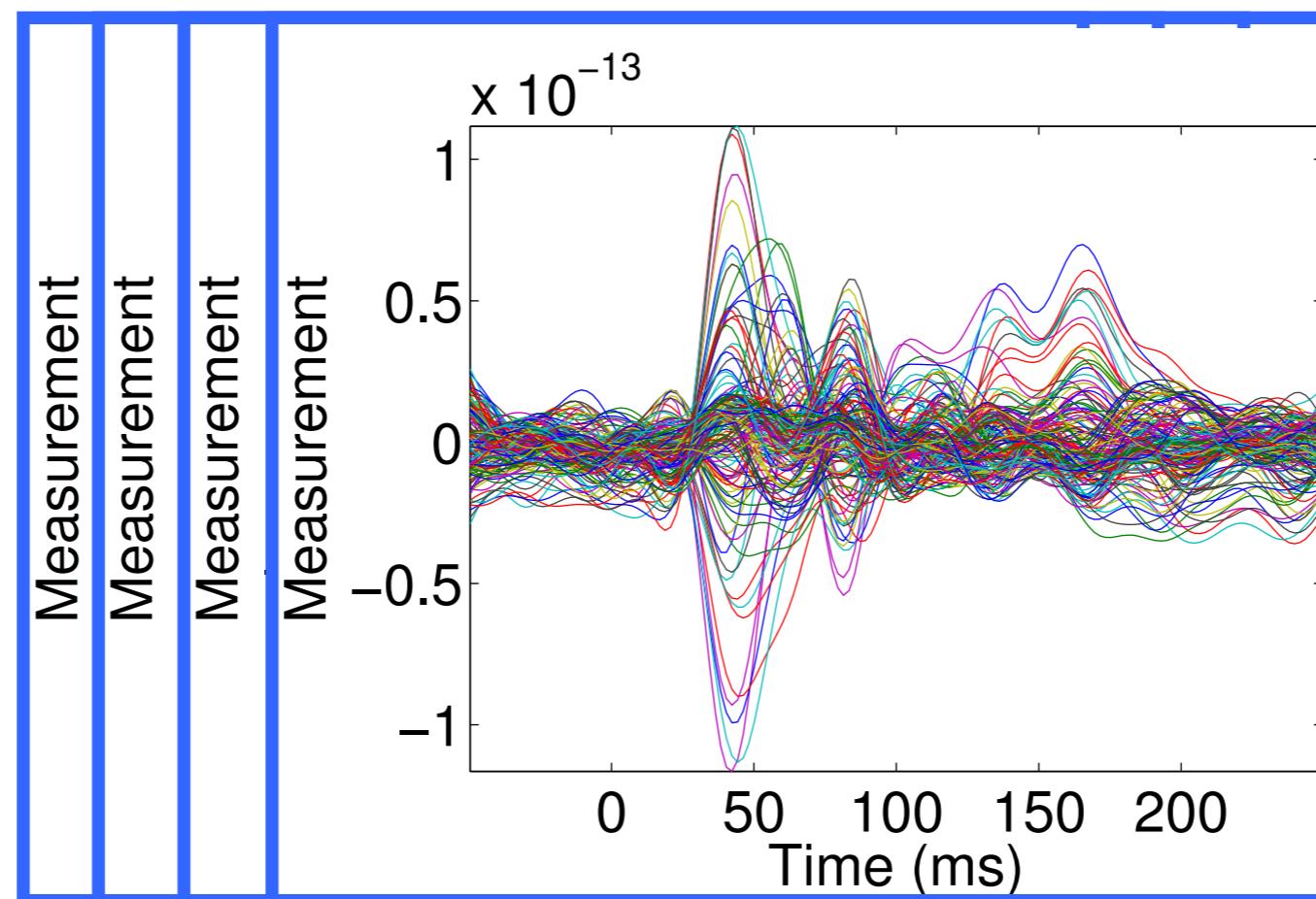


100 trials

Signal
on
151
MEG
Channels

Evoked activity

Evoked activity is revealed by trial averaging:

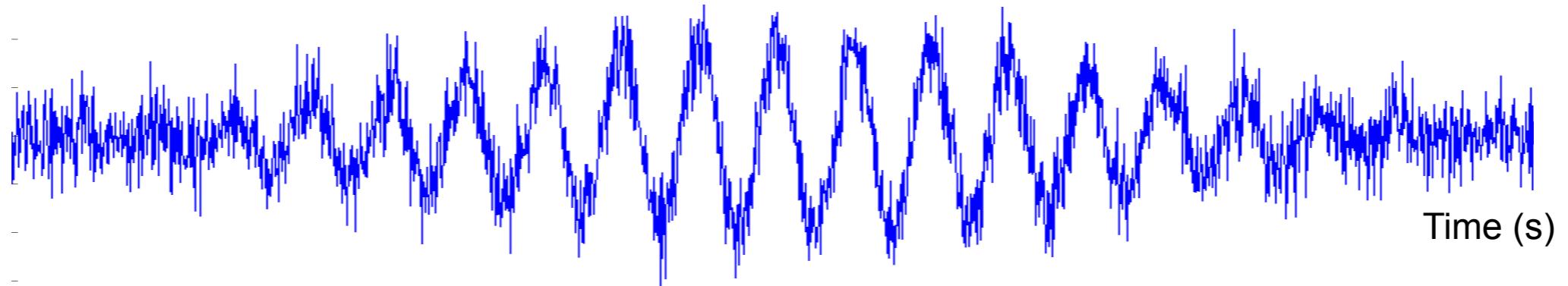


400 trials

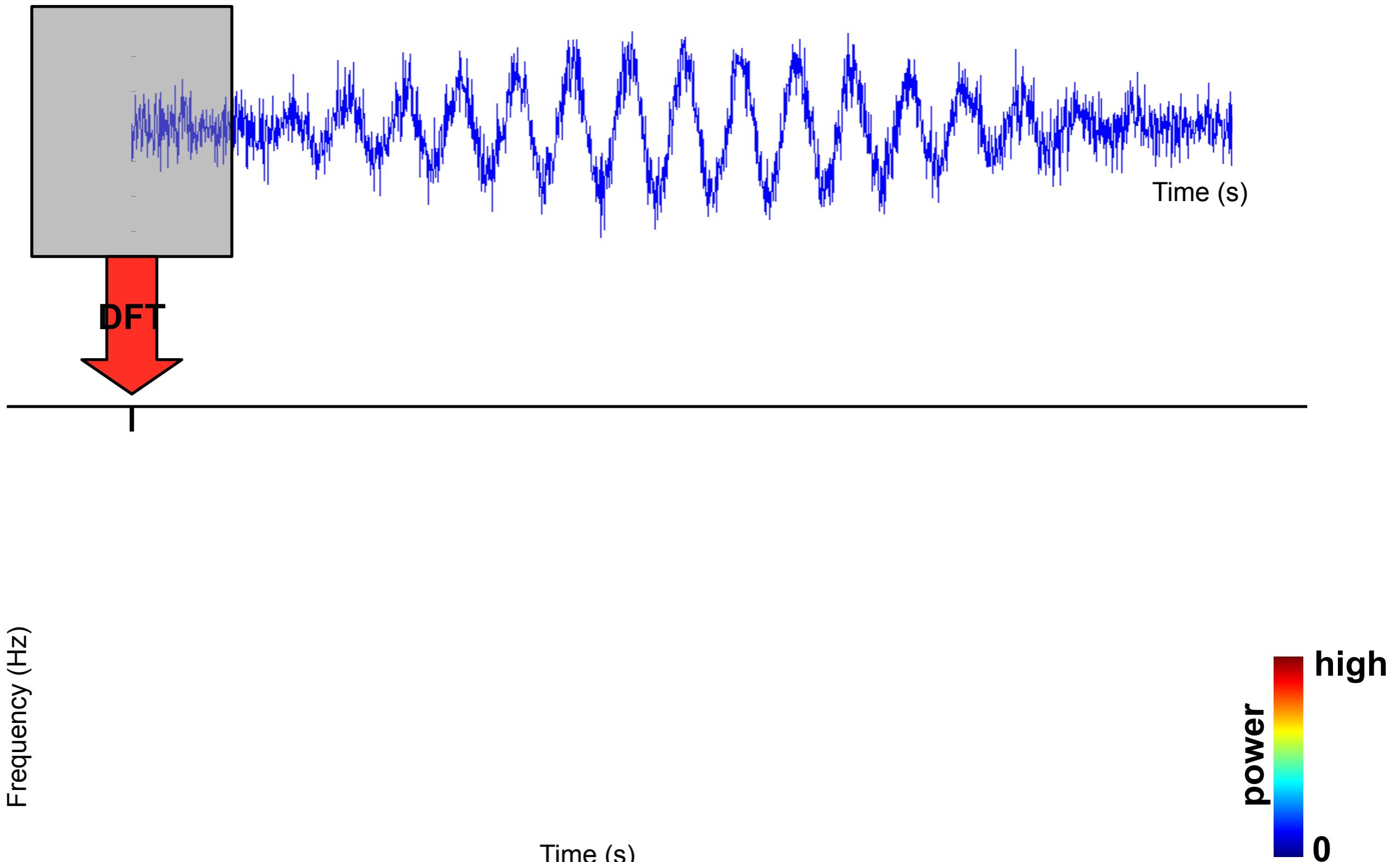
Signal
on
151
MEG
Channels

BUT: Does not work if the phase/latency are different over trials

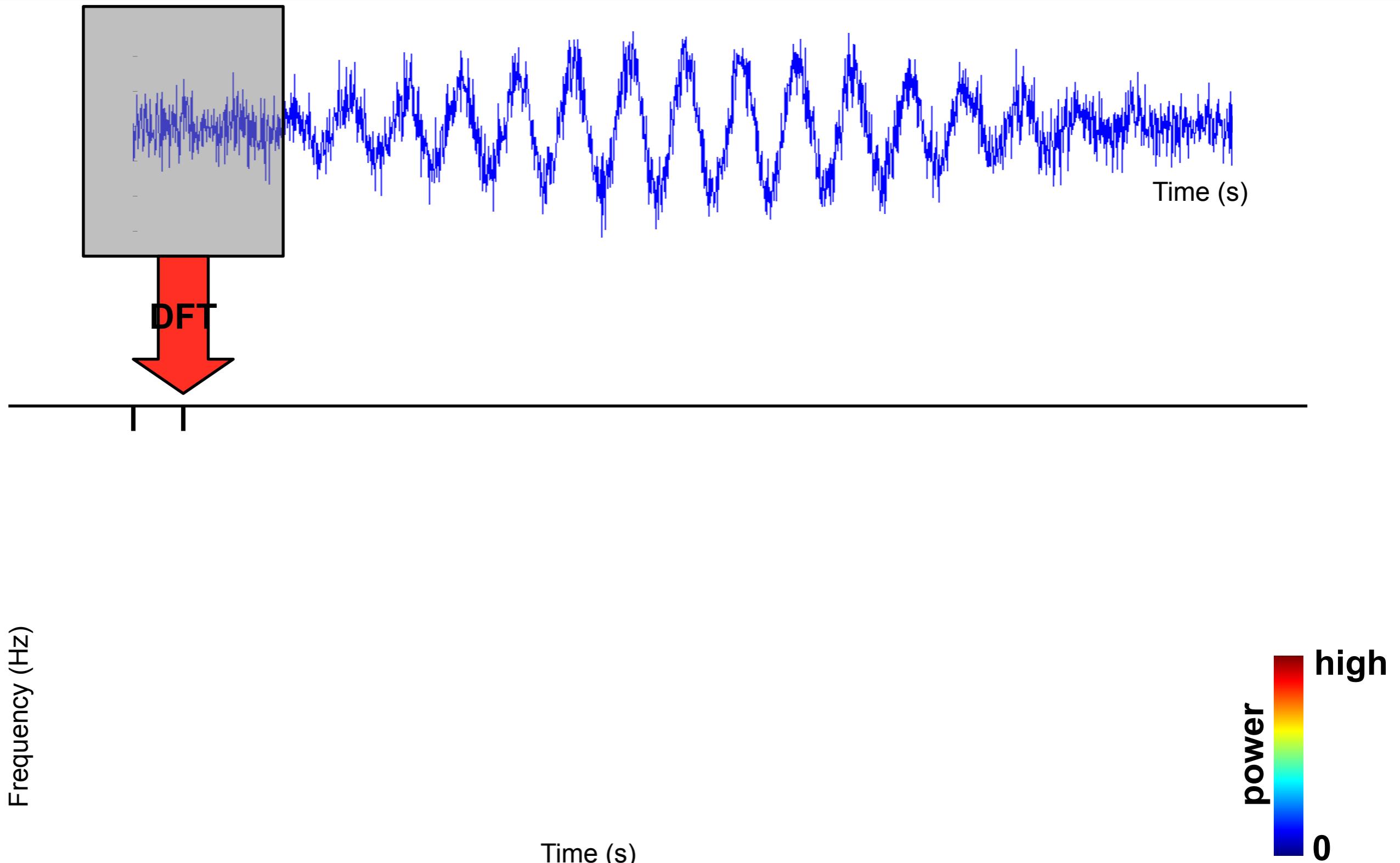
Time frequency analysis



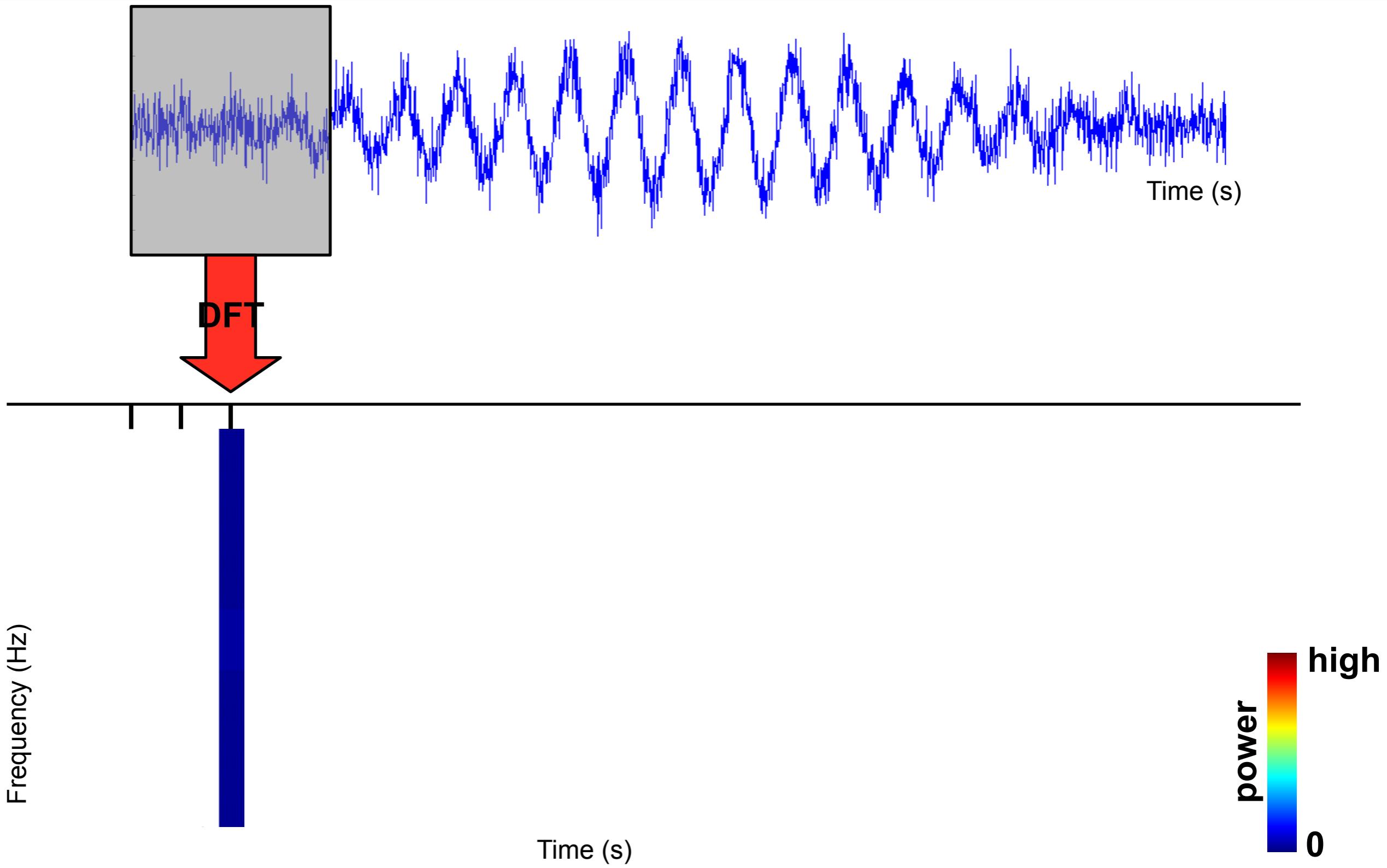
Time frequency analysis



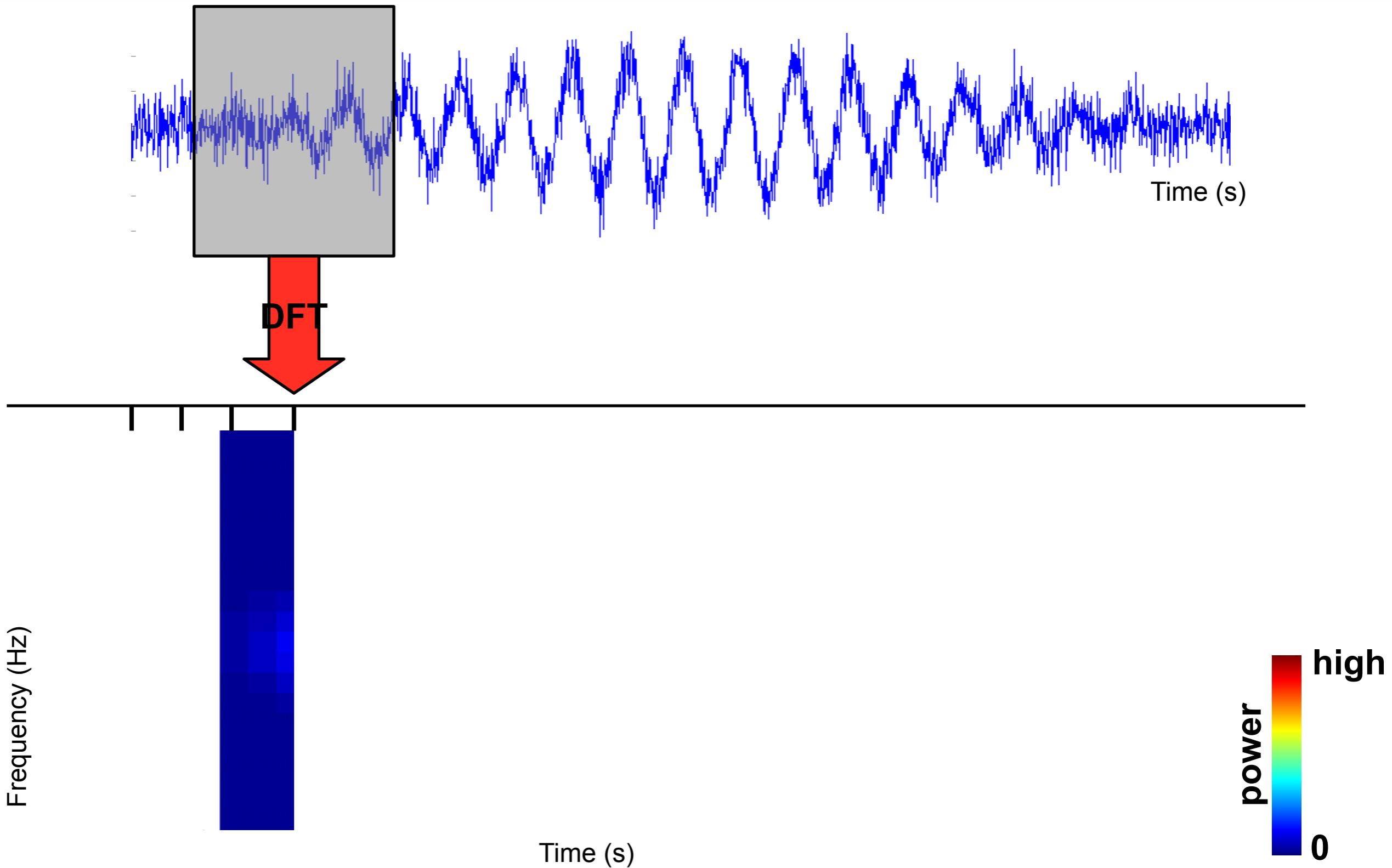
Time frequency analysis



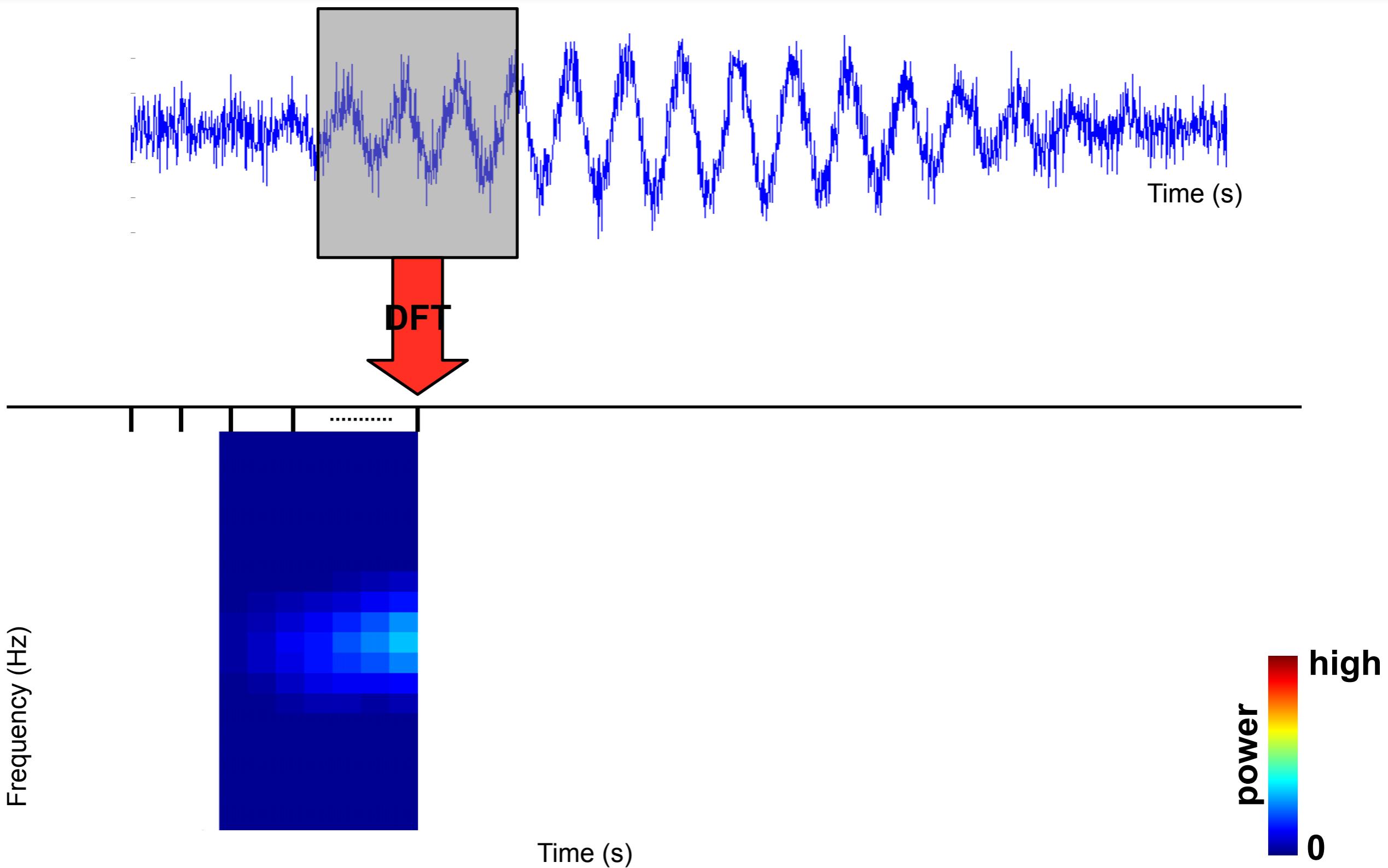
Time frequency analysis



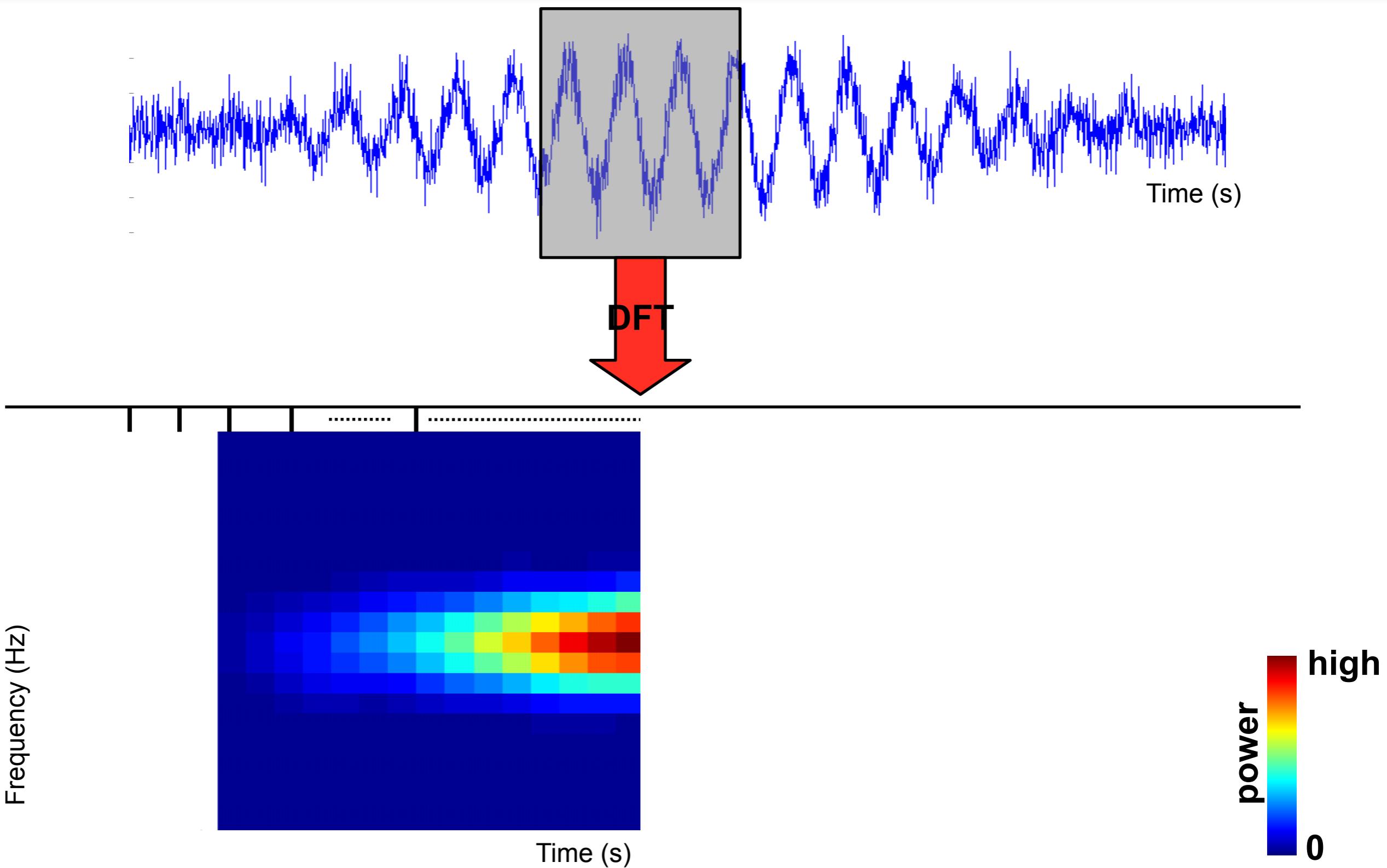
Time frequency analysis



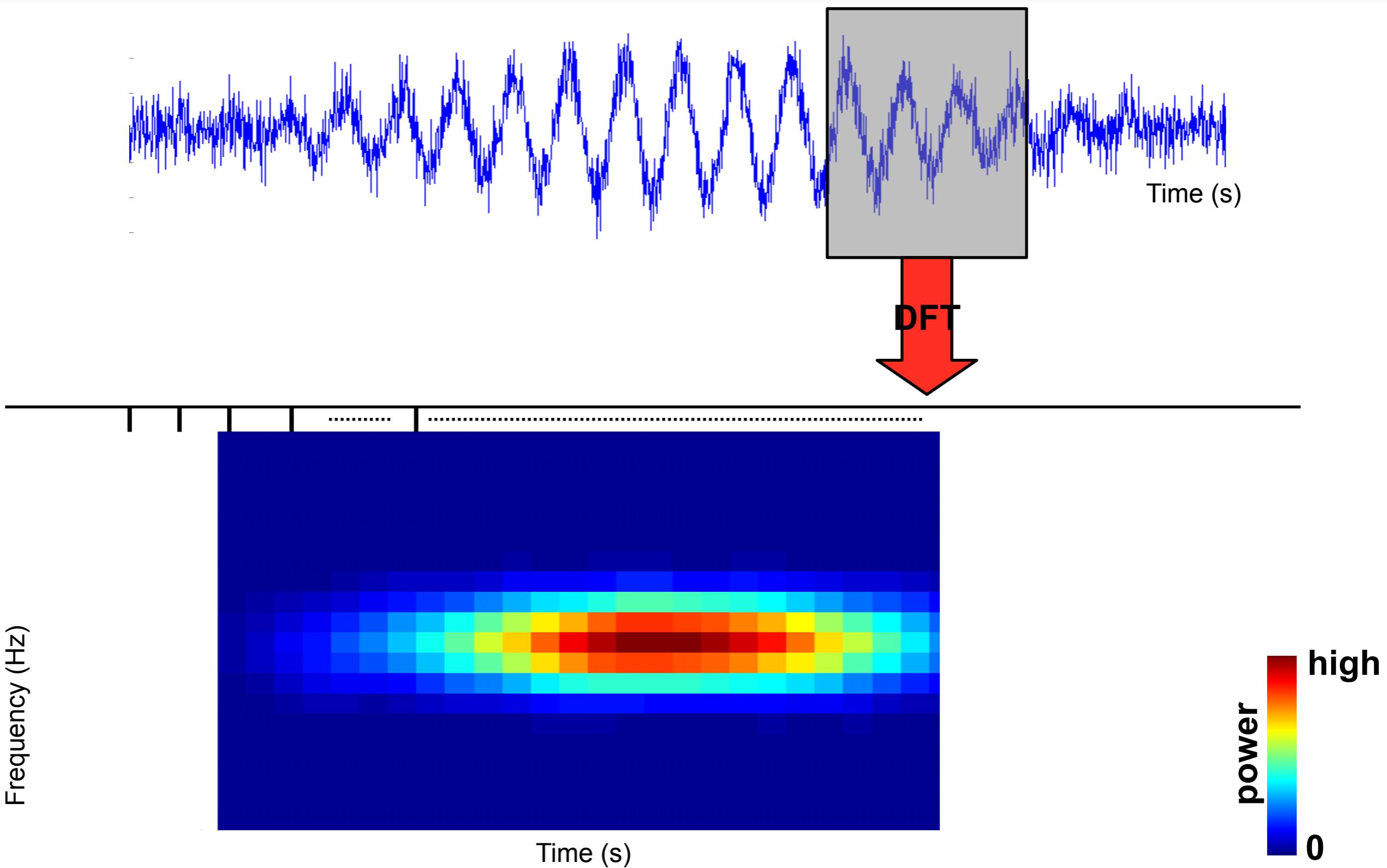
Time frequency analysis



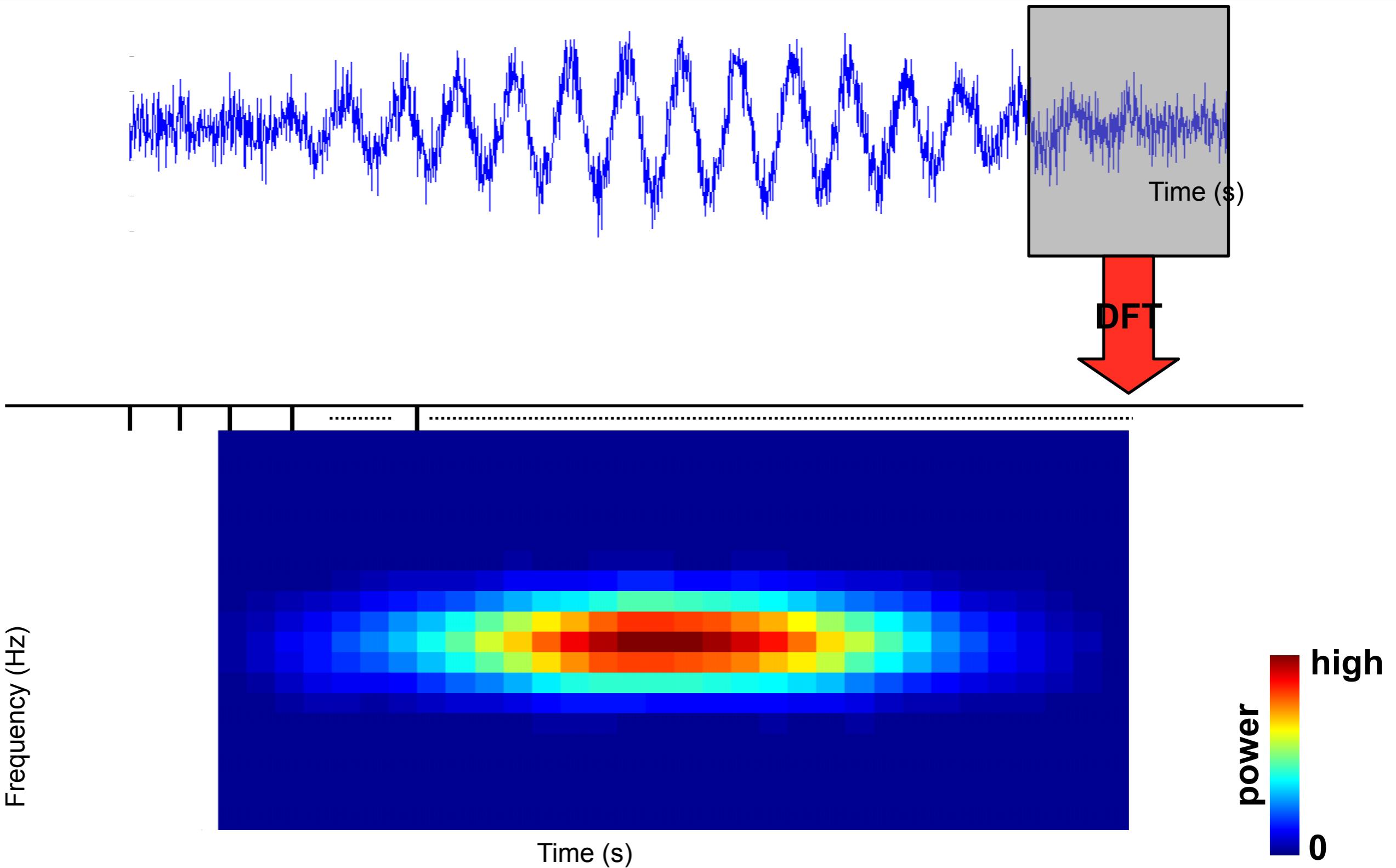
Time frequency analysis



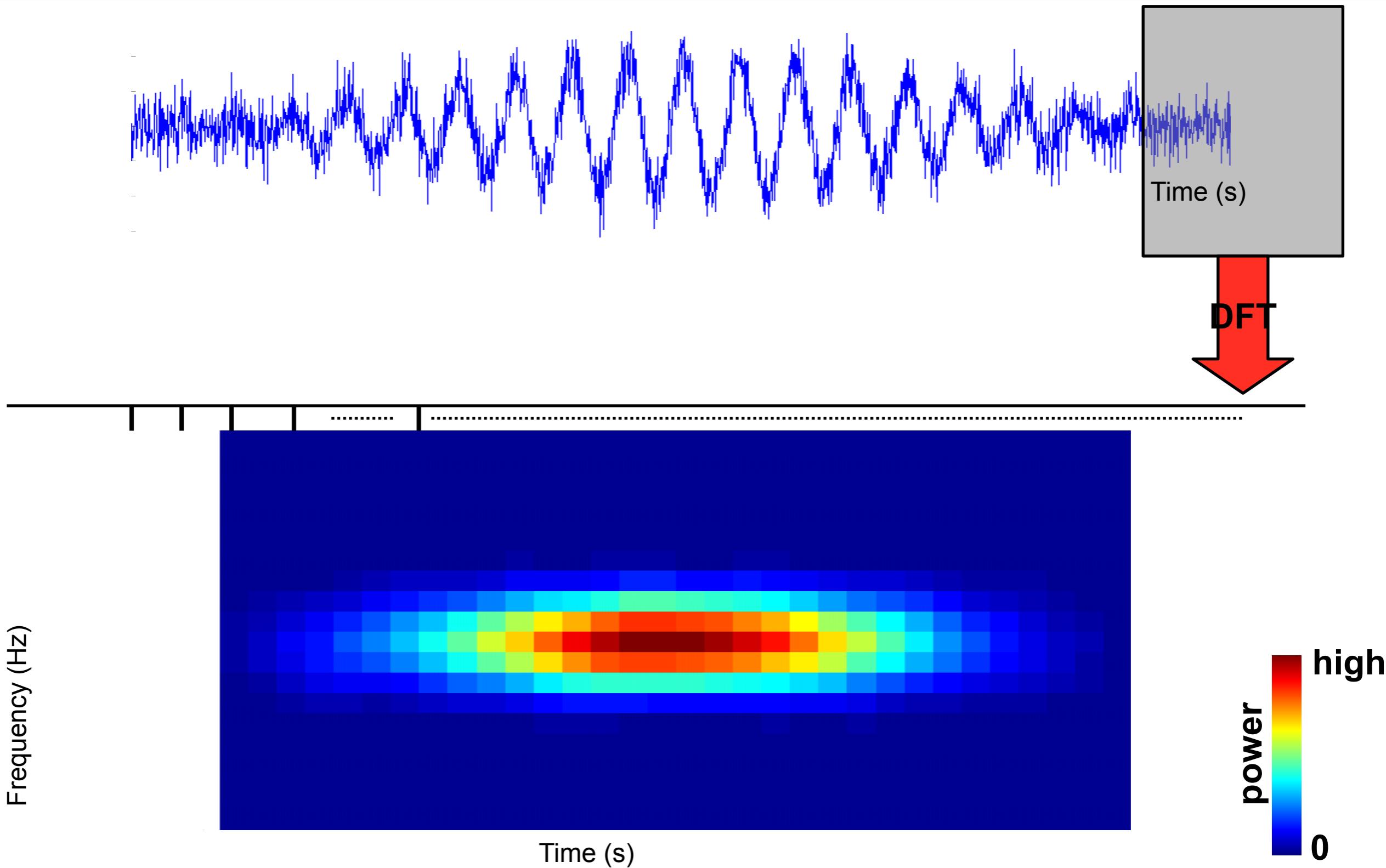
Time frequency analysis



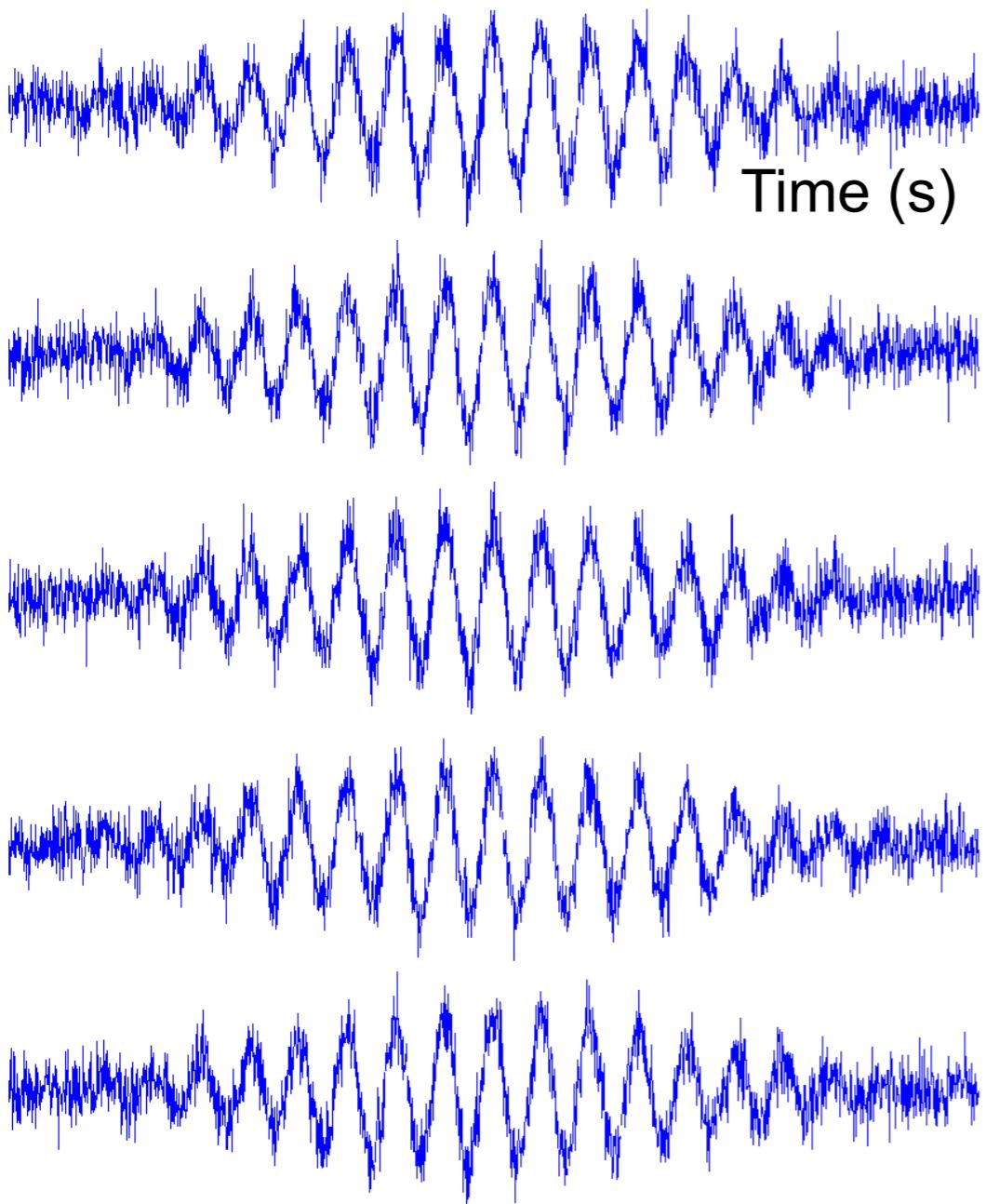
Time frequency analysis



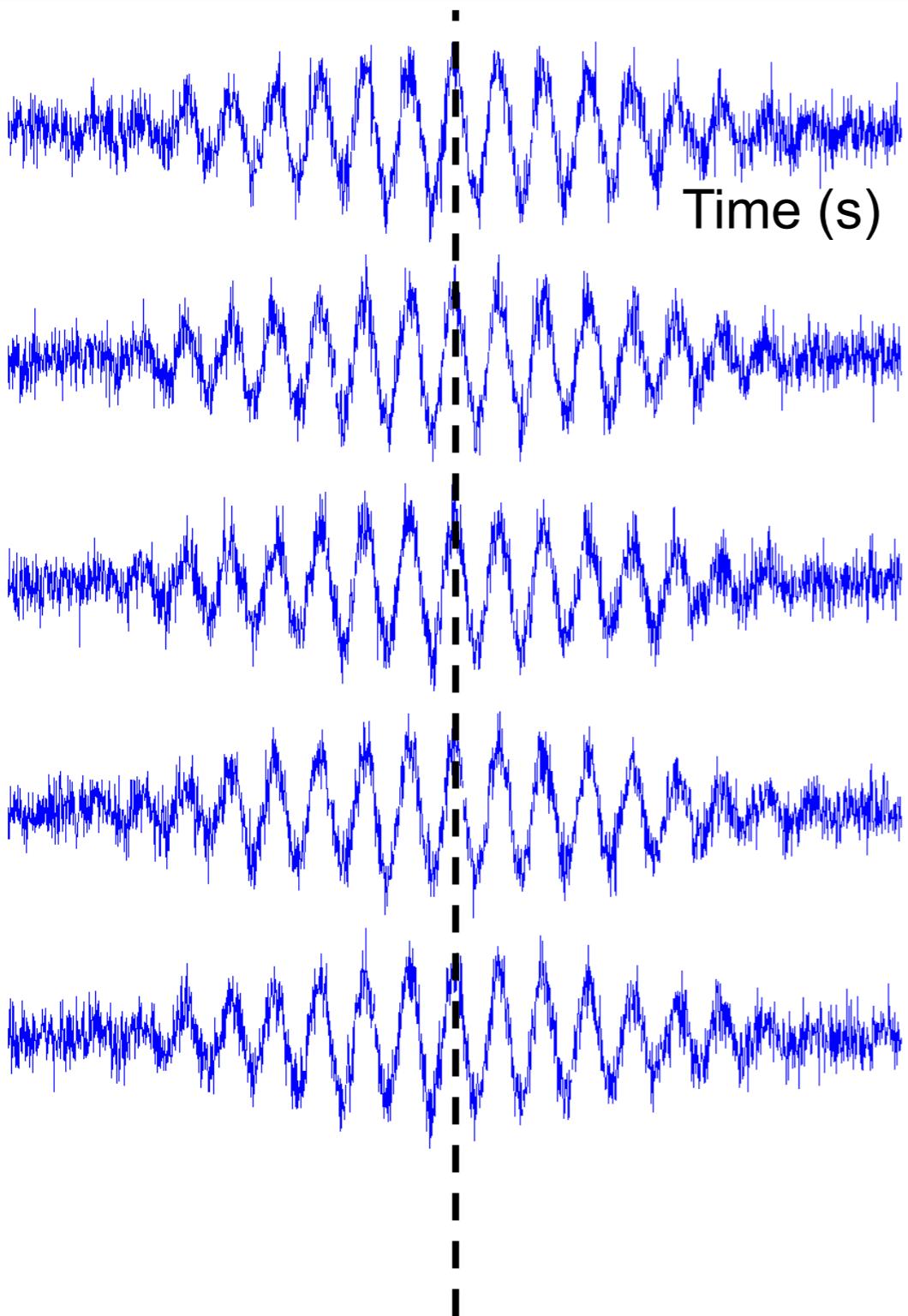
Time frequency analysis



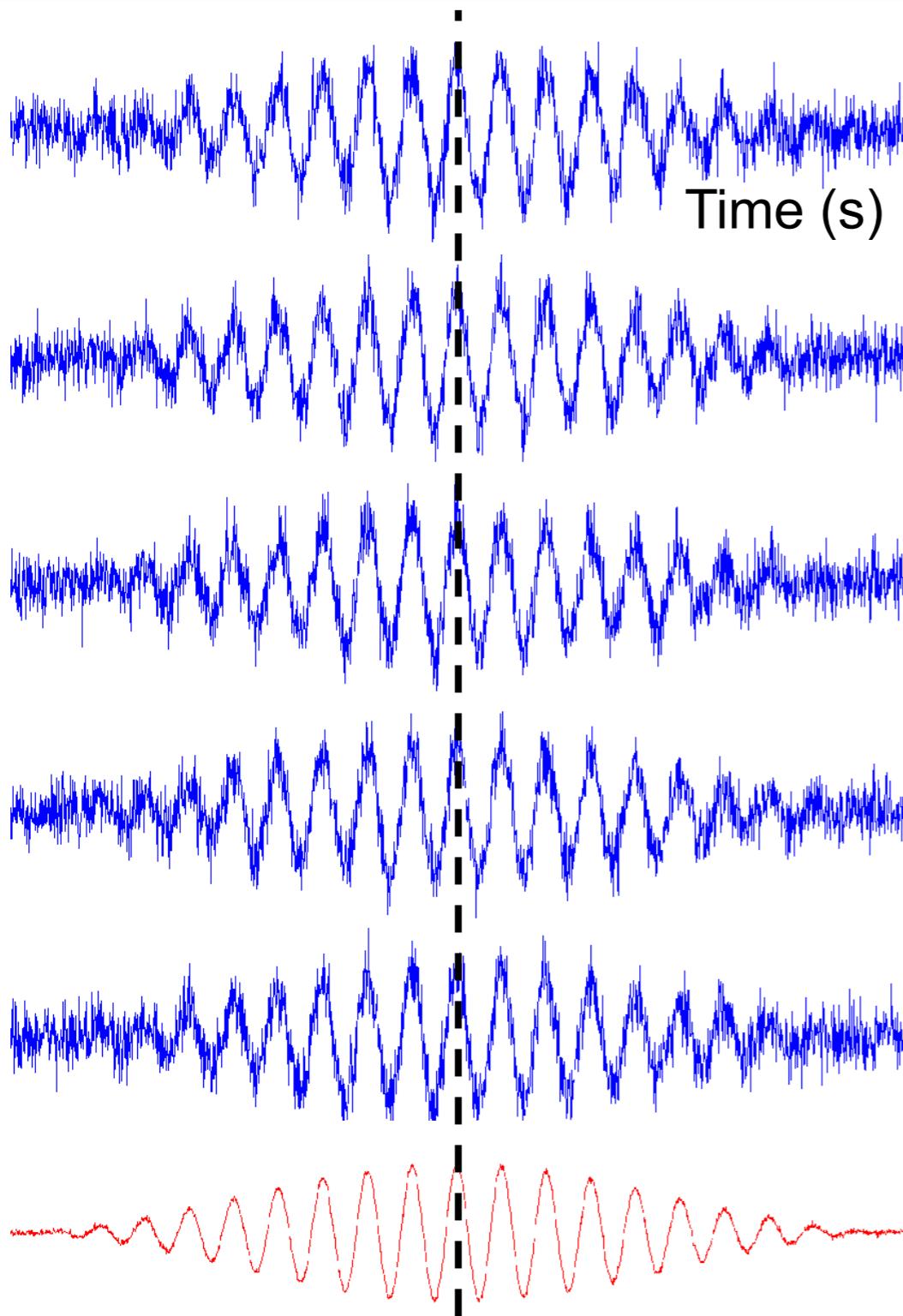
Evoked vs. induced activity



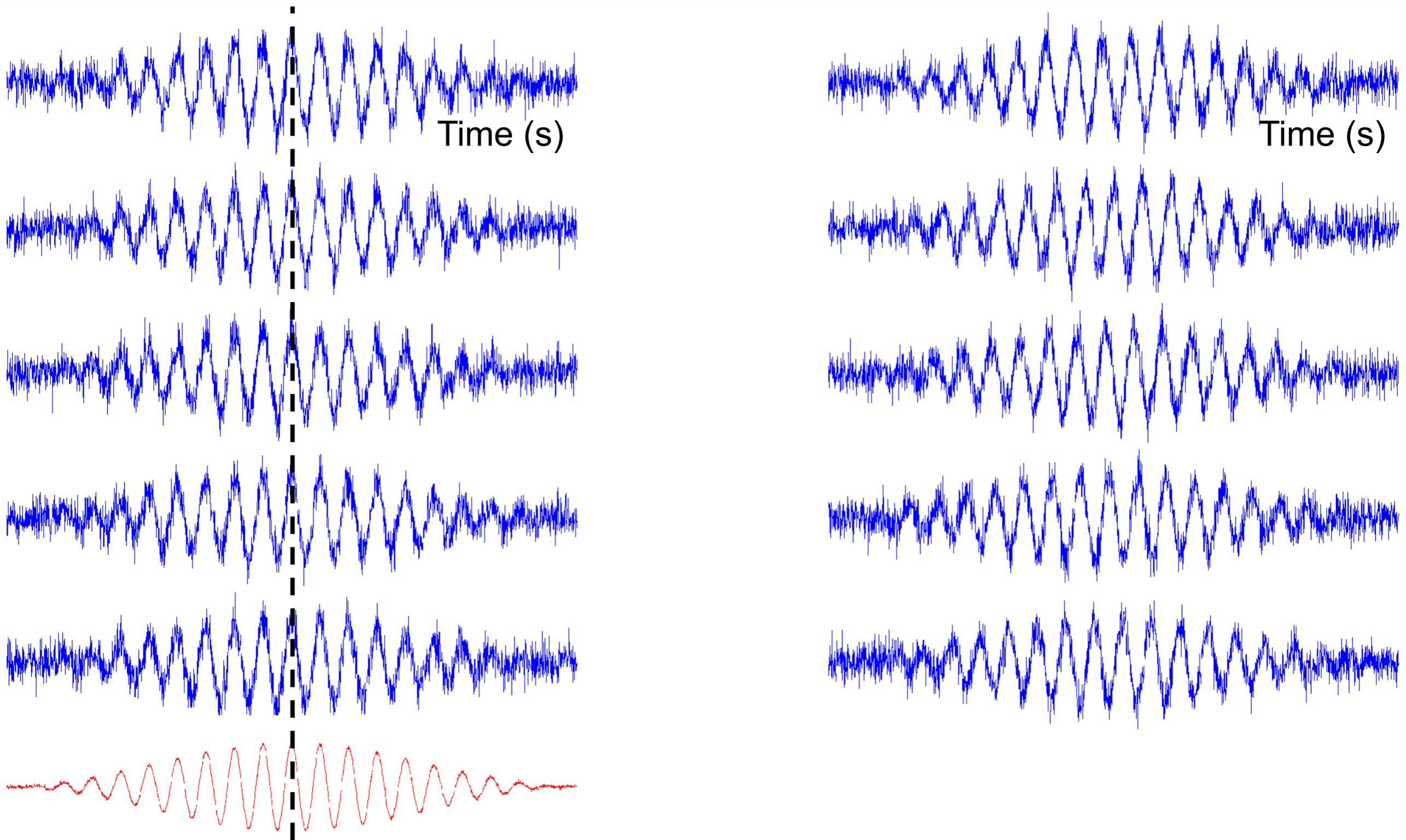
Evoked vs. induced activity



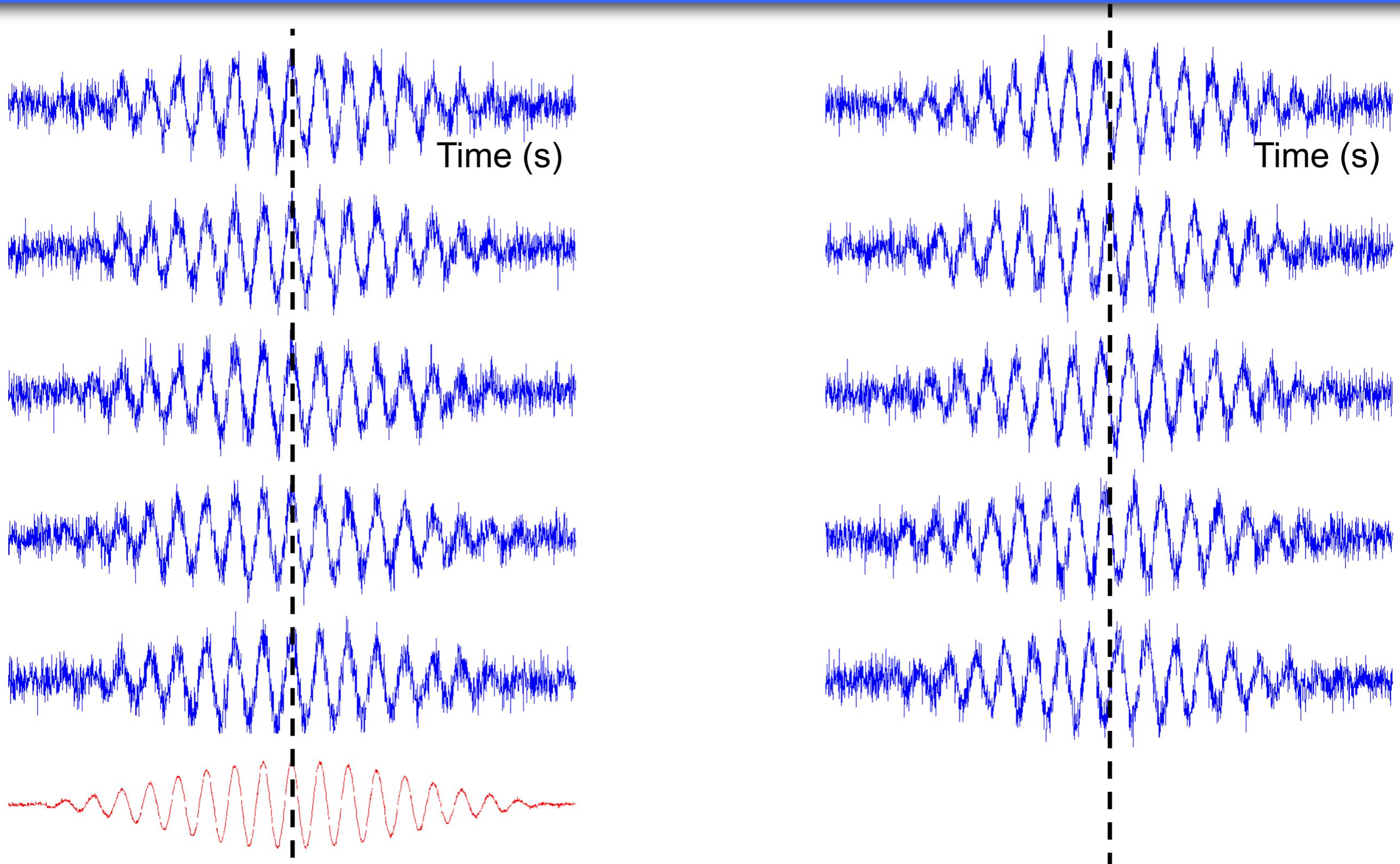
Evoked vs. induced activity



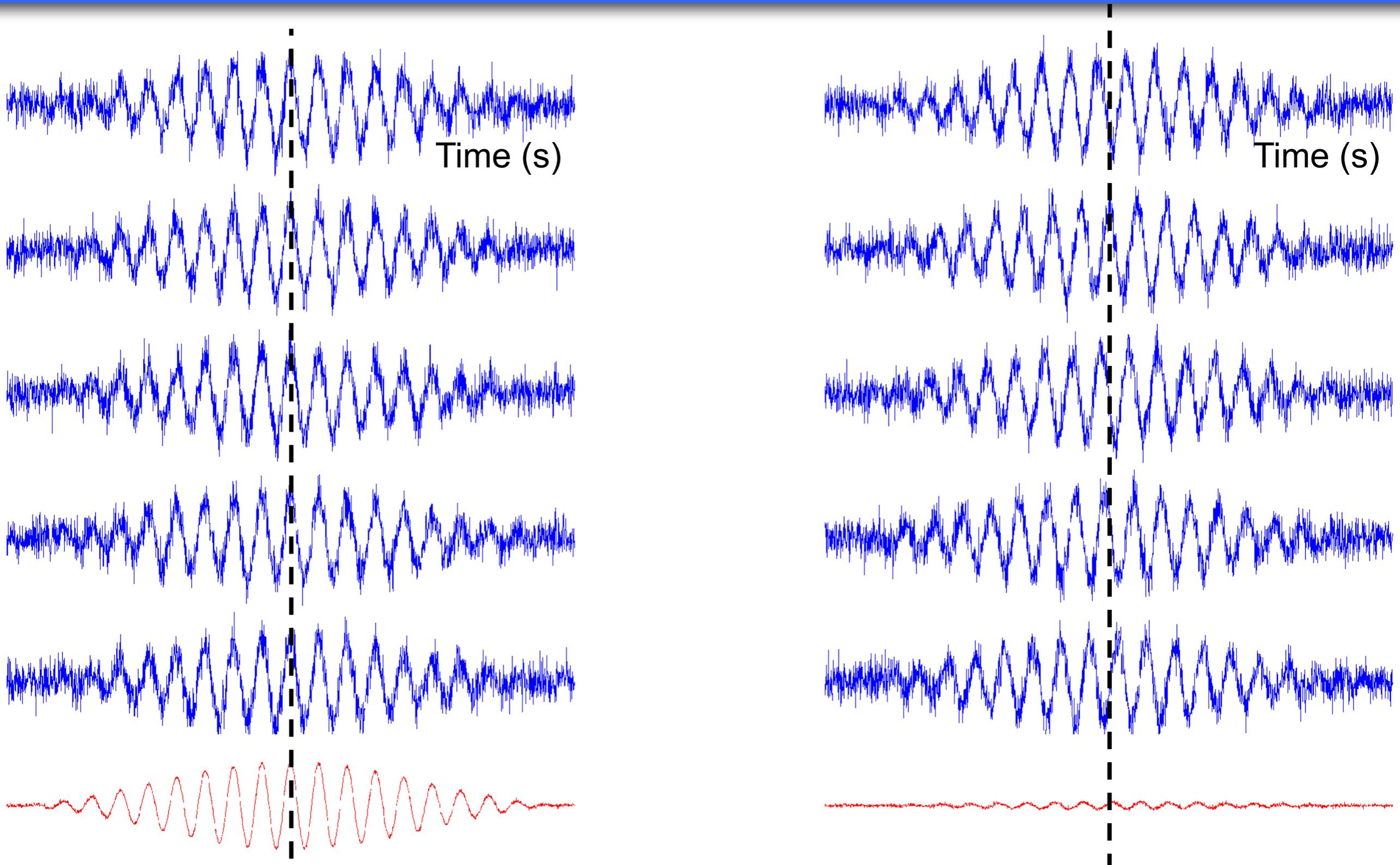
Evoked vs. induced activity



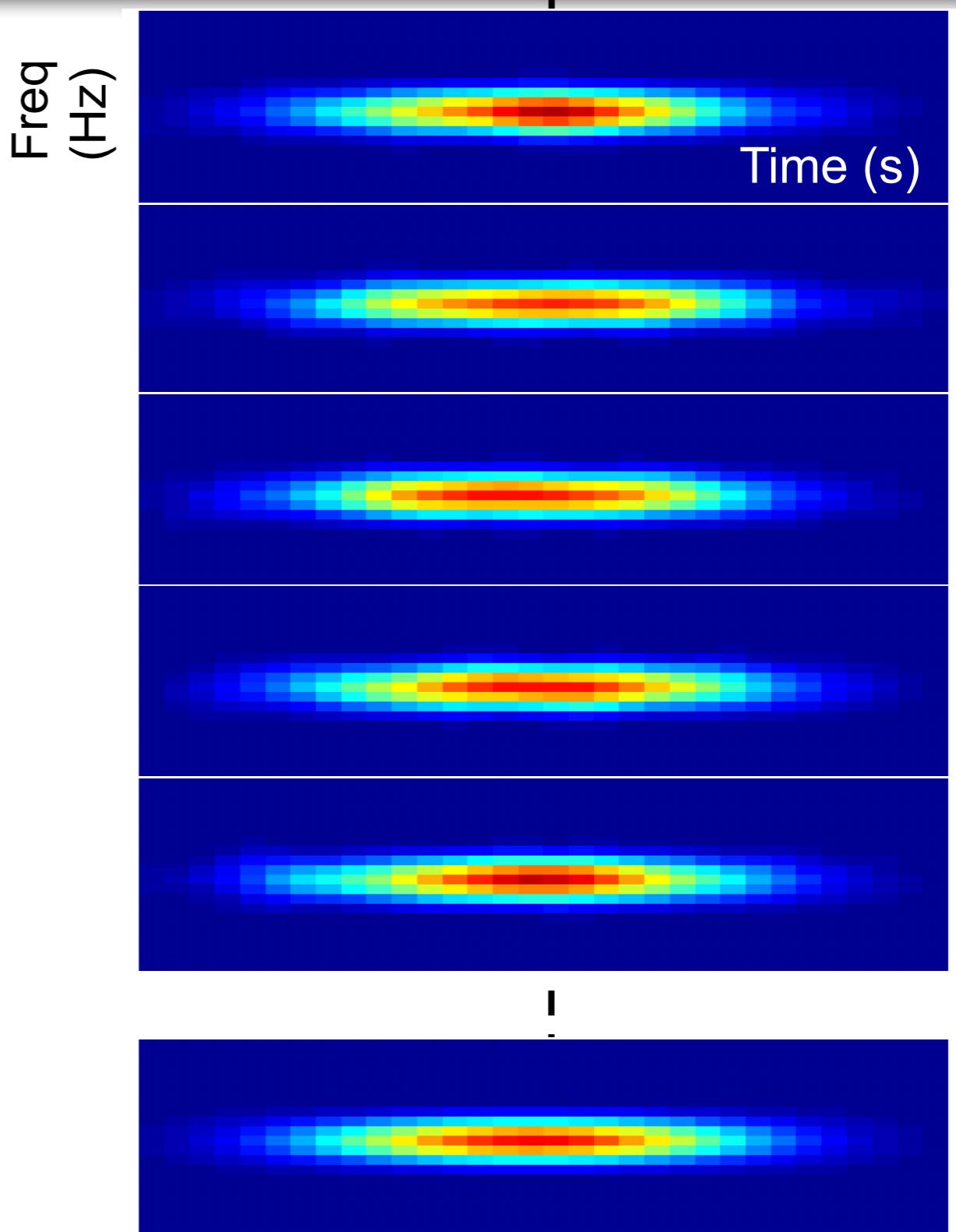
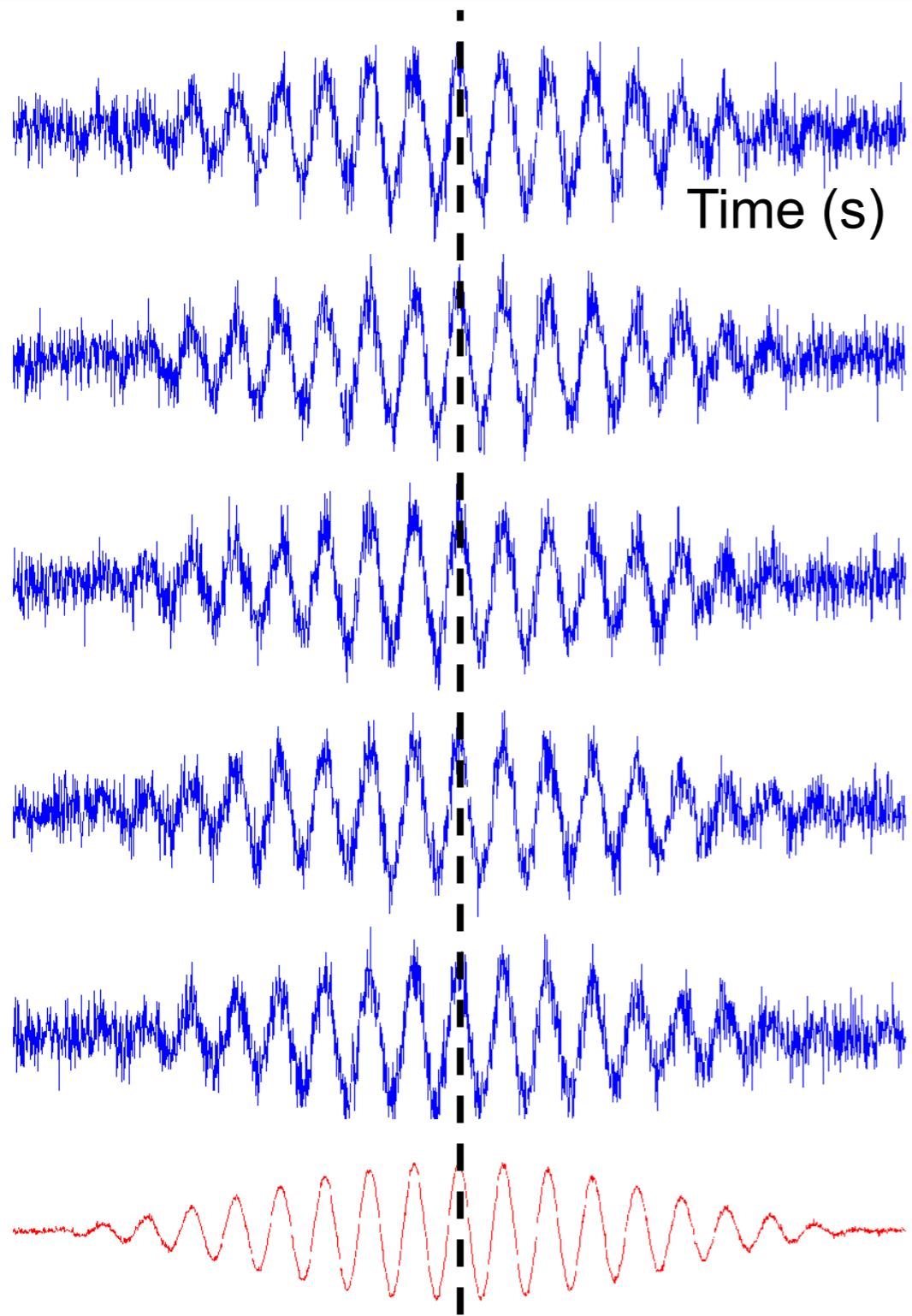
Evoked vs. induced activity



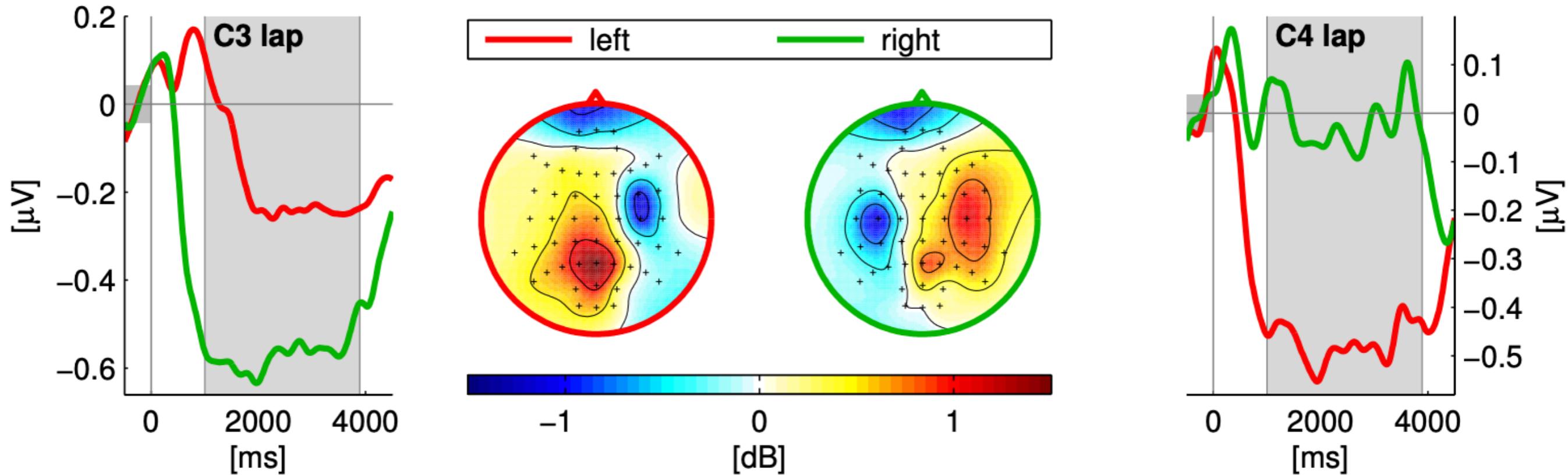
Evoked vs. induced activity



Evoked vs. induced activity



Example of induced: Motor Imagery



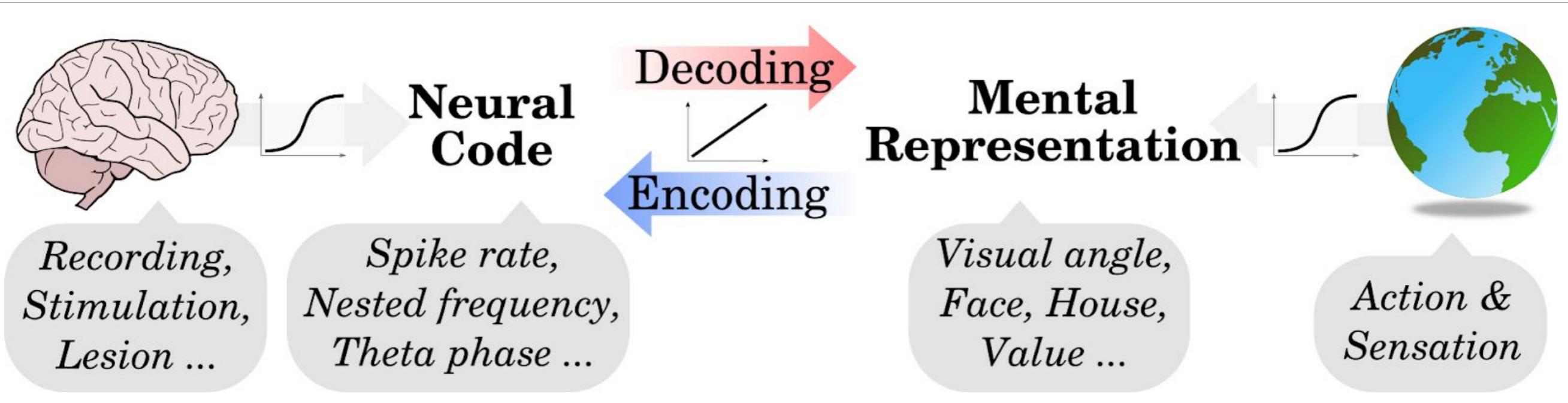
Event-Related Desynchronization (ERD) during motor imagery of the left and the right hand. Averaged signal Hilbert enveloppe between 9 and 13Hz on C3 and C4 (After Laplace / Current Source Density transform)

[Blankertz et al. 2008]

Decoding vs. Encoding

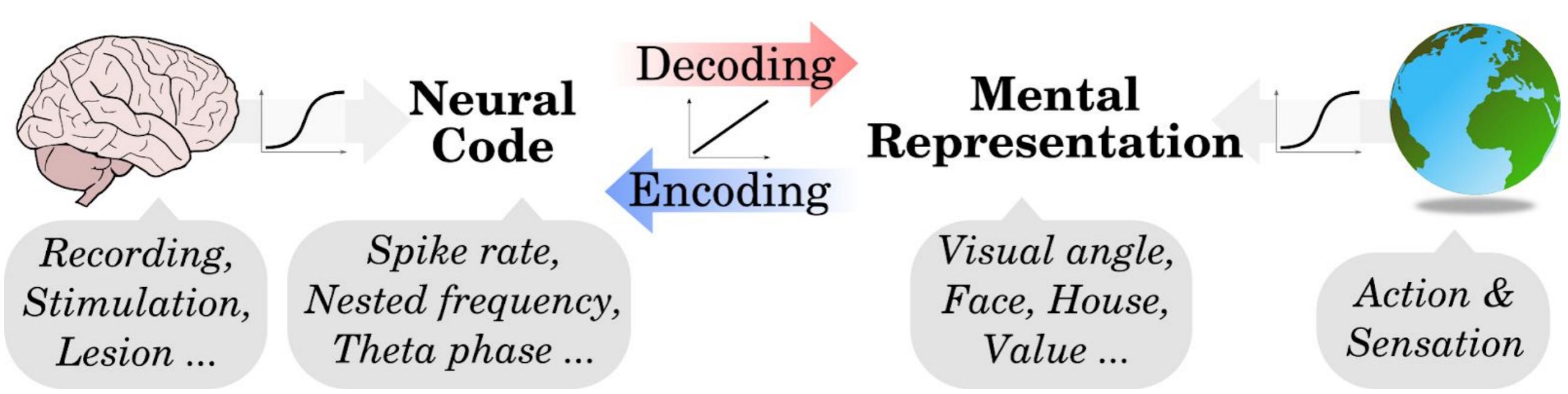
... introducing some maths notations

Neural code & mental representations



[Encoding and Decoding Neuronal Dynamics: Methodological Framework to Uncover the Algorithms of Cognition, King et al. 2019]

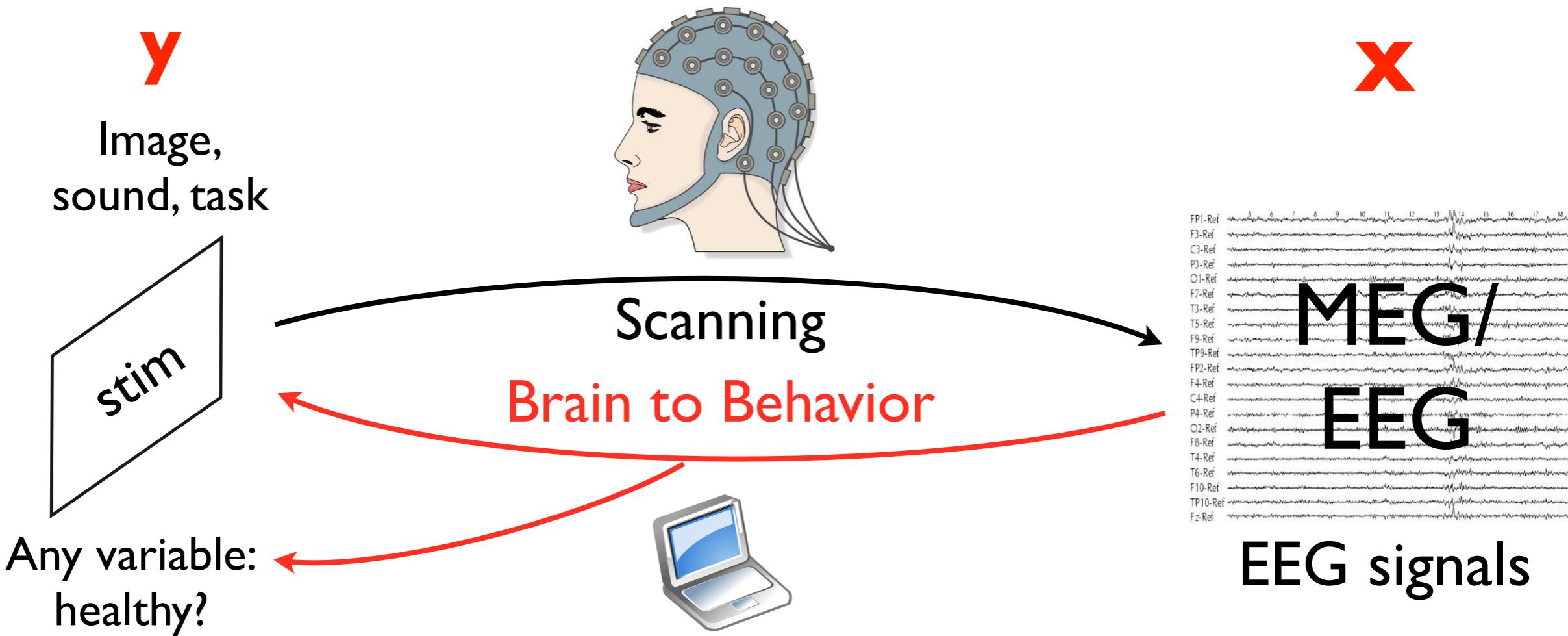
Neural code & mental representations



Decoding predicts experimental factors (e.g. the speed of a hand movement, the luminance of an flashed image etc) from specific features of brain activity (e.g. spike rate, electric field etc), whereas encoding predicts the reverse.

[Encoding and Decoding Neuronal Dynamics: Methodological Framework to Uncover the Algorithms of Cognition, King et al. 2019]

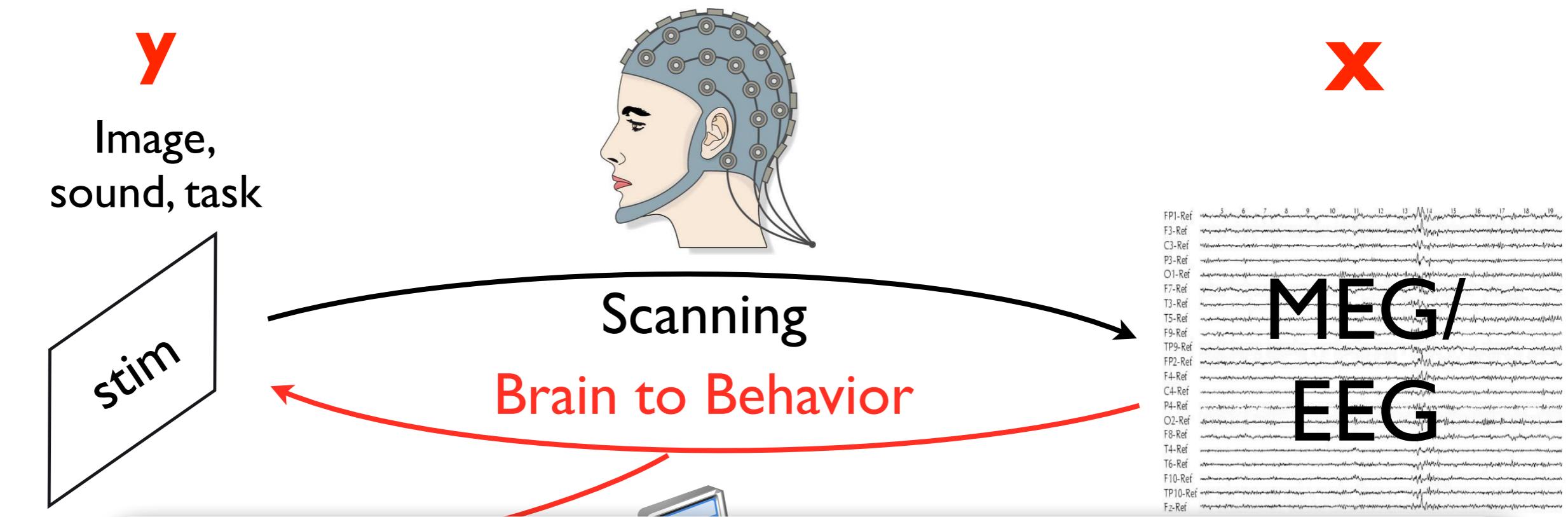
Decoding



Challenge: Predict a behavioral variable from the EEG/MEG data

Objective: Predict y given X or learn a function $f : X \rightarrow y$

Decoding



$$x_i \in \mathbb{R}^P$$

: vector of features for sample i

$$y_i \in \mathbb{R}$$

: target to predict for sample i

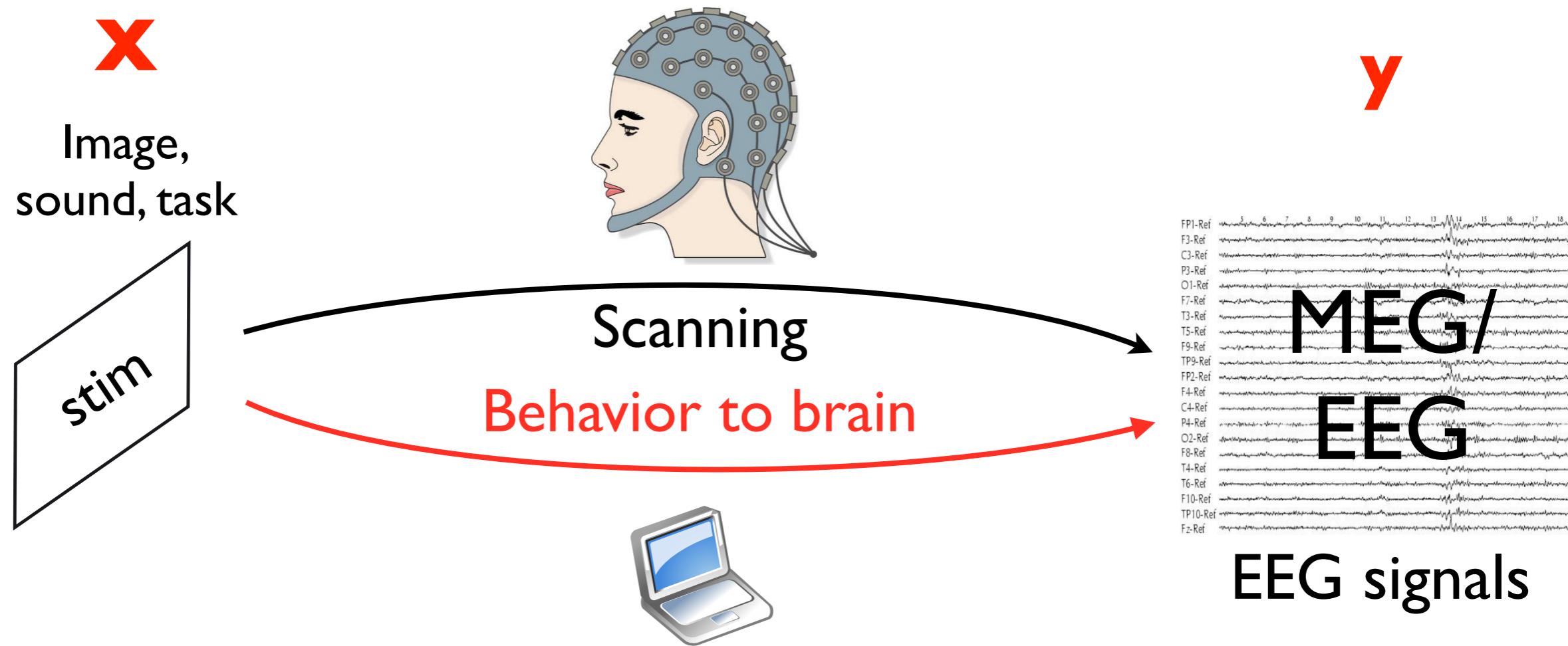
$$f : \mathbb{R}^P \rightarrow \mathbb{R}$$

: prediction function (to learn)

Challeng

Objectiv

Encoding

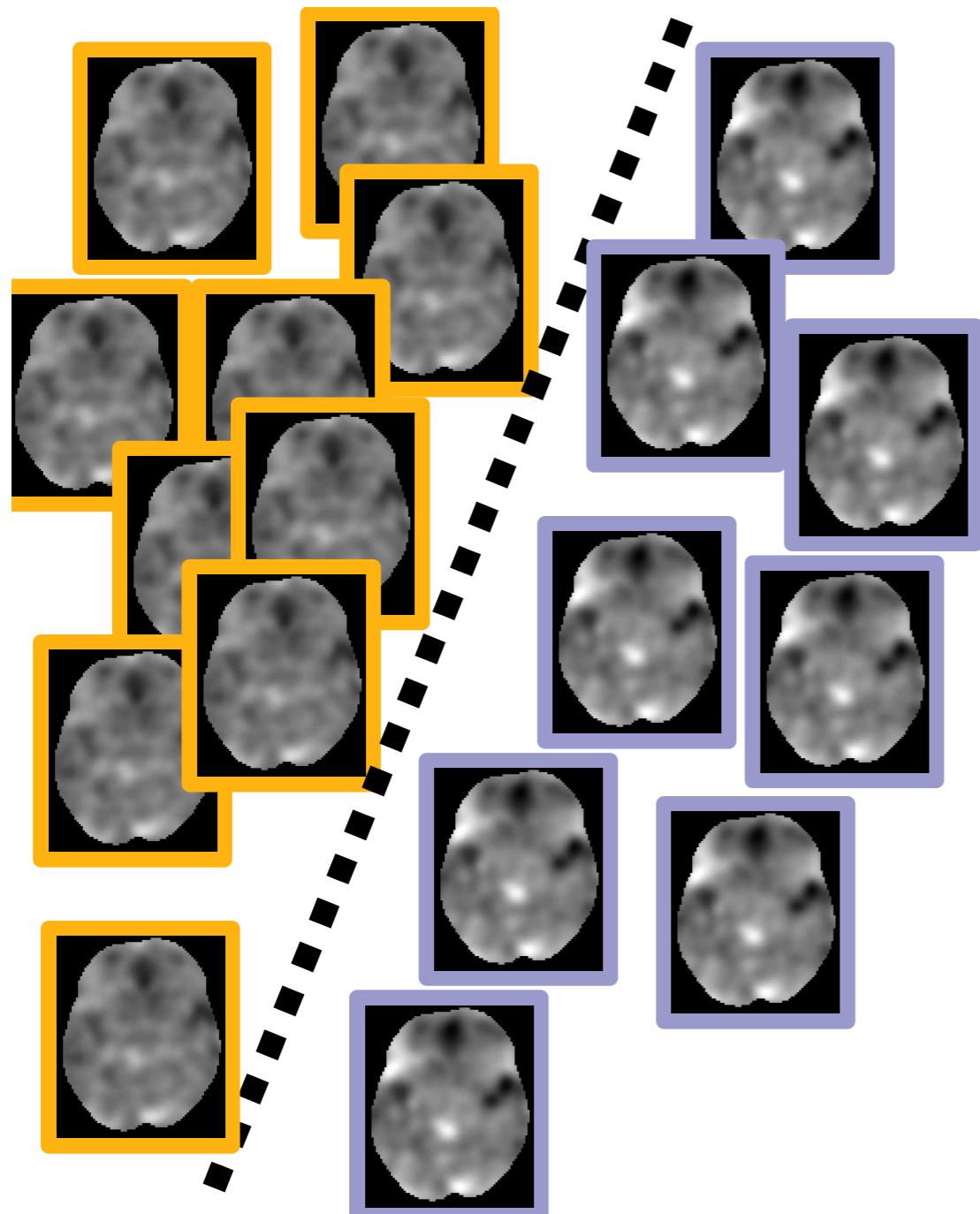


Challenge: Predict a EEG/MEG data from behavioral variable / stimuli

Objective: Predict **y** given **X** or learn a function $f : X \rightarrow y$

Algorithms

101 Classification example



The **objective** is to be able to **predict** ■ or ■ given a brain activation map



Patient vs. Controls

Faces vs. Houses

...

vs.

...

|

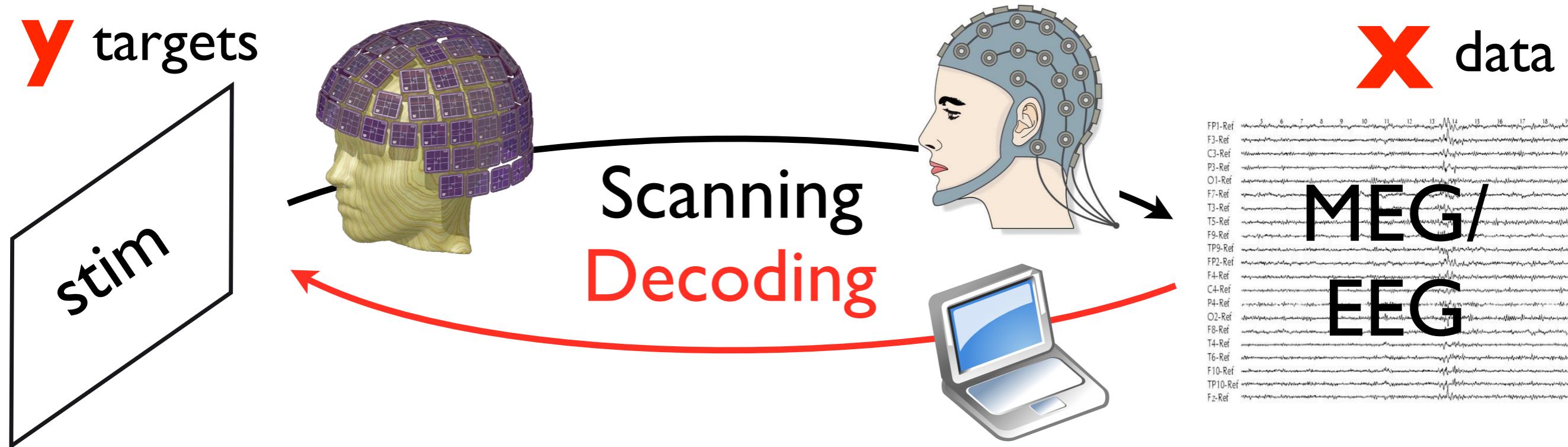
vs.

-|

ie. $y = \{-1, 1\}$

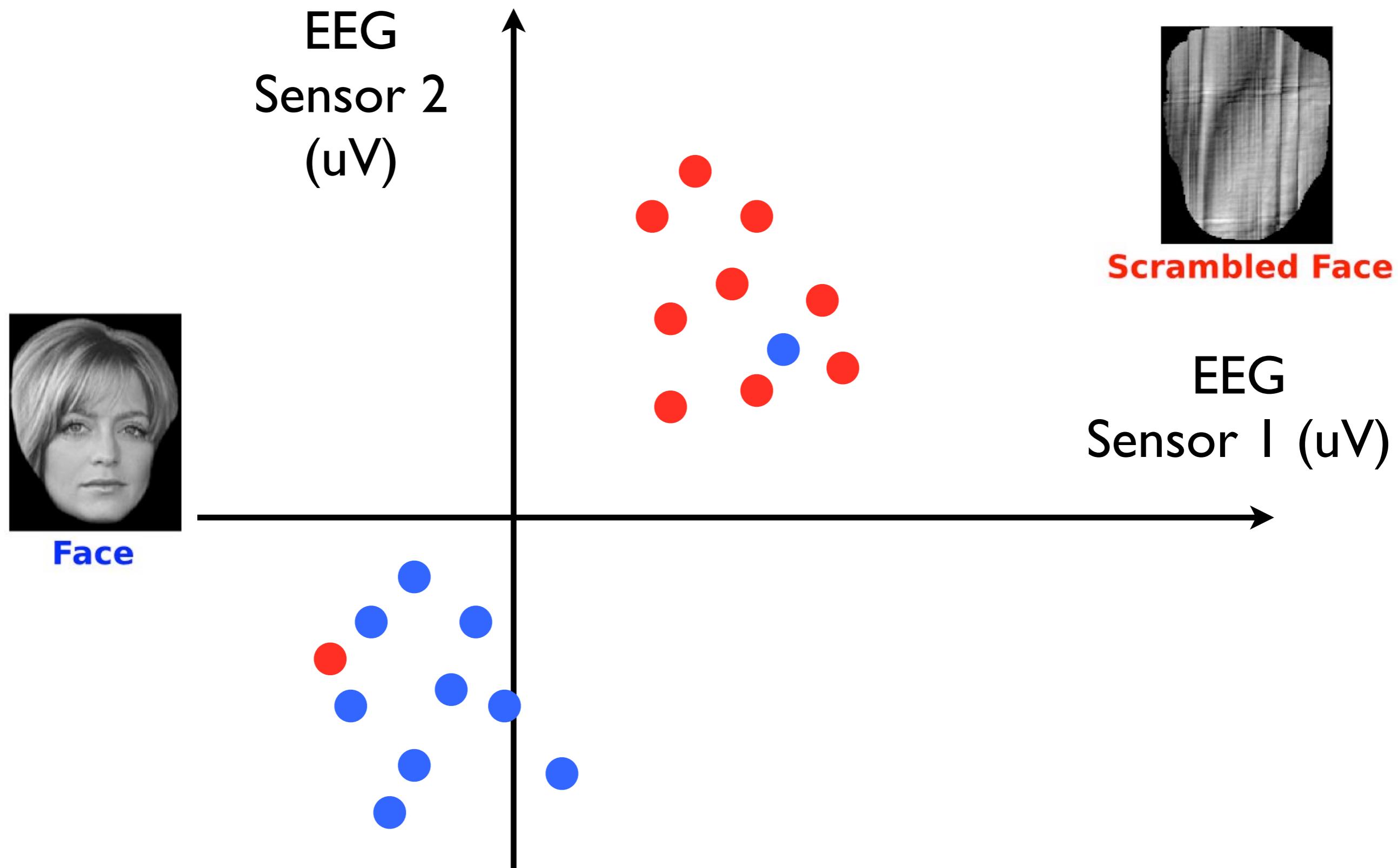
objective: Predict $y = \{-1, 1\}$ given $x \in \mathbb{R}^p$

My first “decoder”

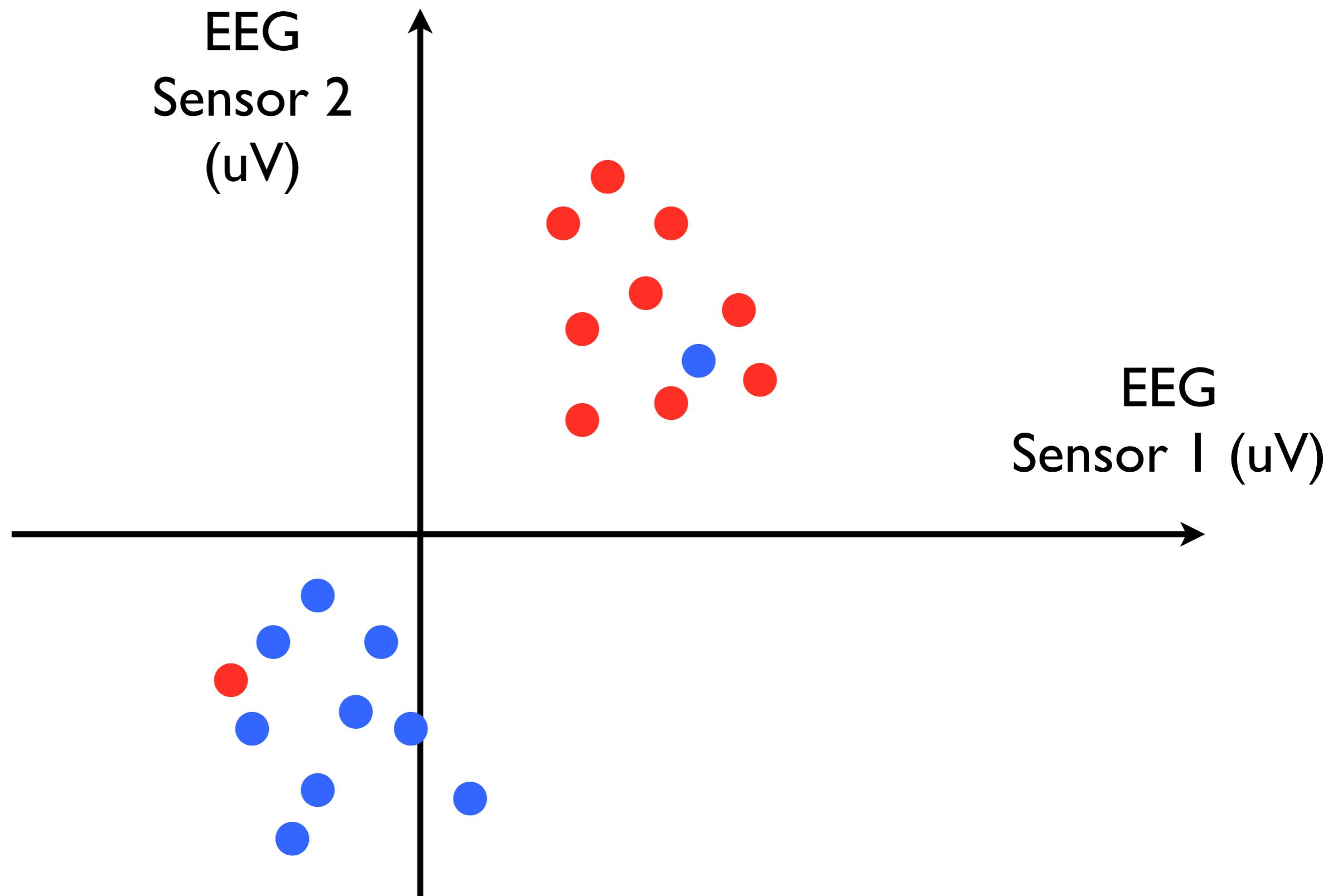


- Visual paradigm with 2 conditions: **faces or scrambled faces**
- **Questions:**
 - Can we learn from M/EEG signals to predict on a single trial if the subject saw a face or a scrambled face?
 - When does this happen? How is it encoded in the brain?
 - How to link “neural codes” to “mental representations”?

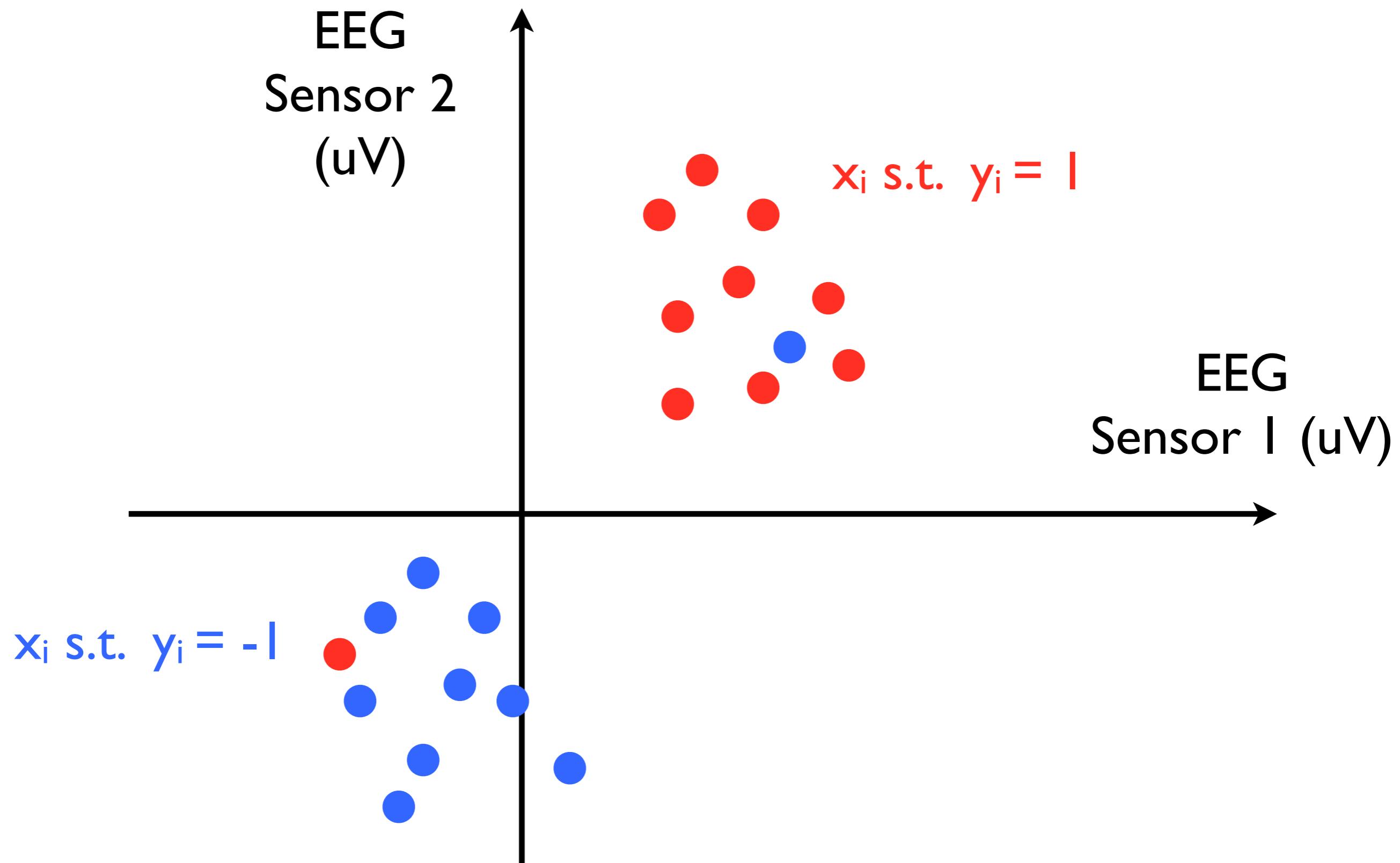
A simple decoder with 2 sensors



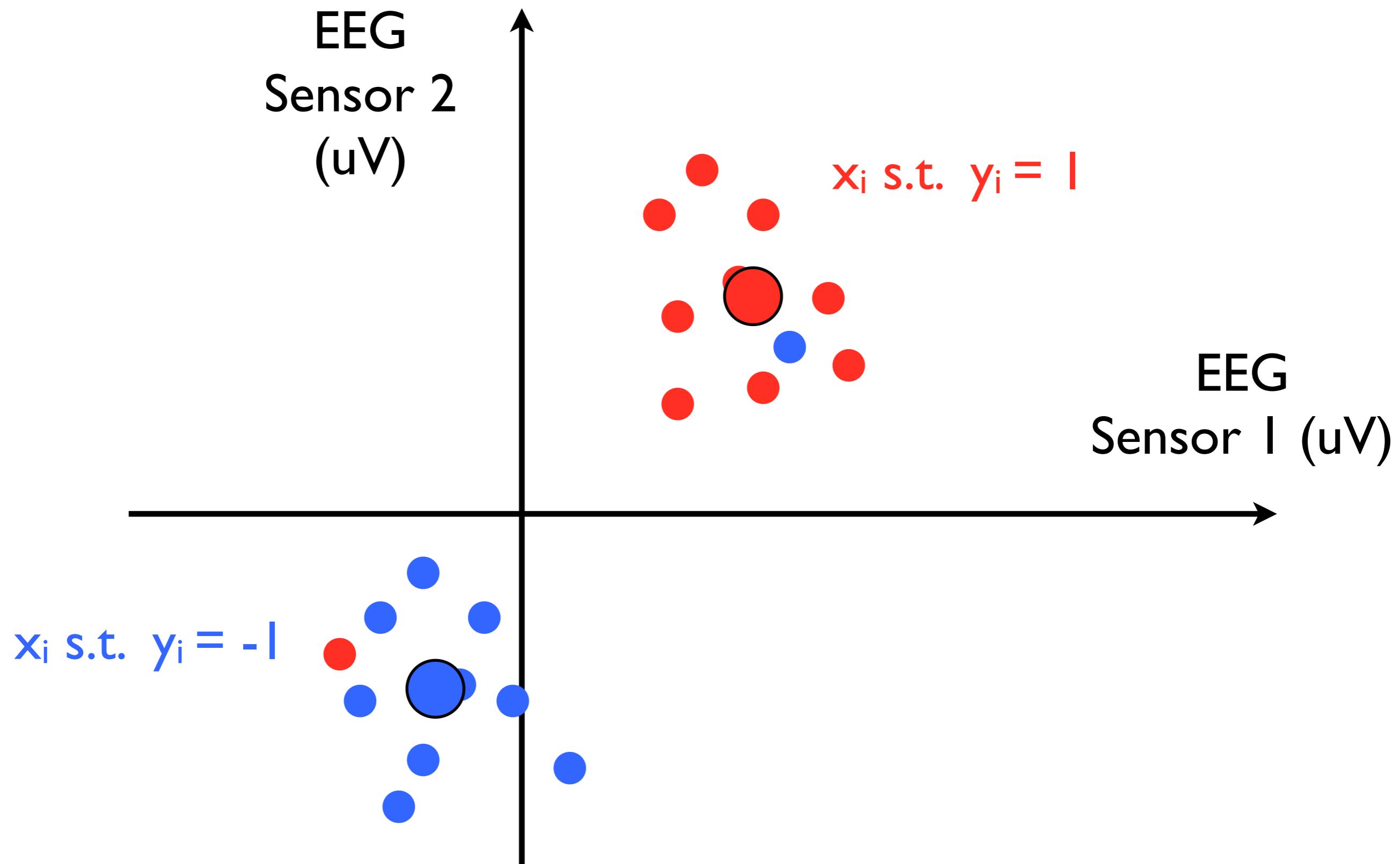
A simple decoder with 2 sensors



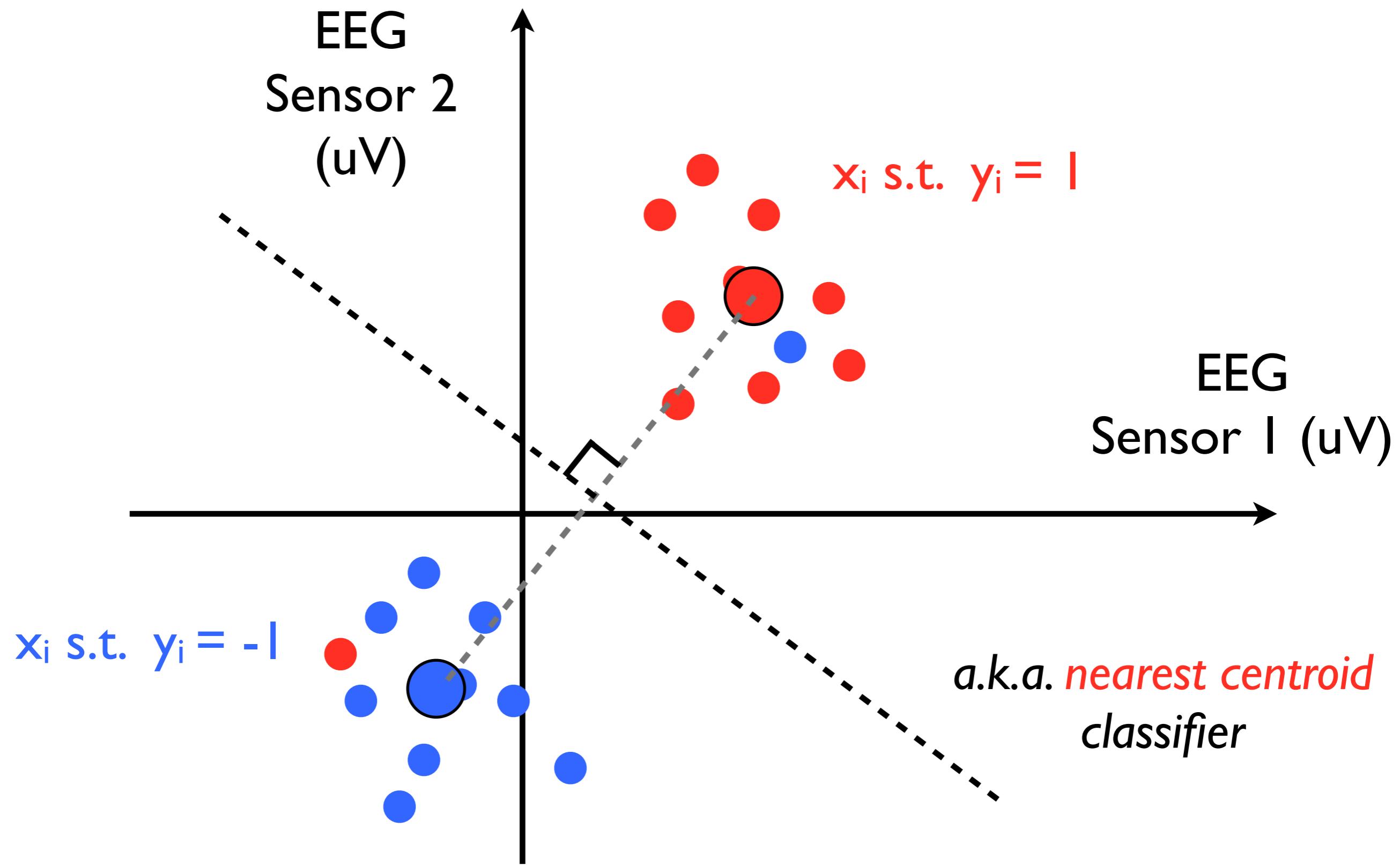
A simple decoder with 2 sensors



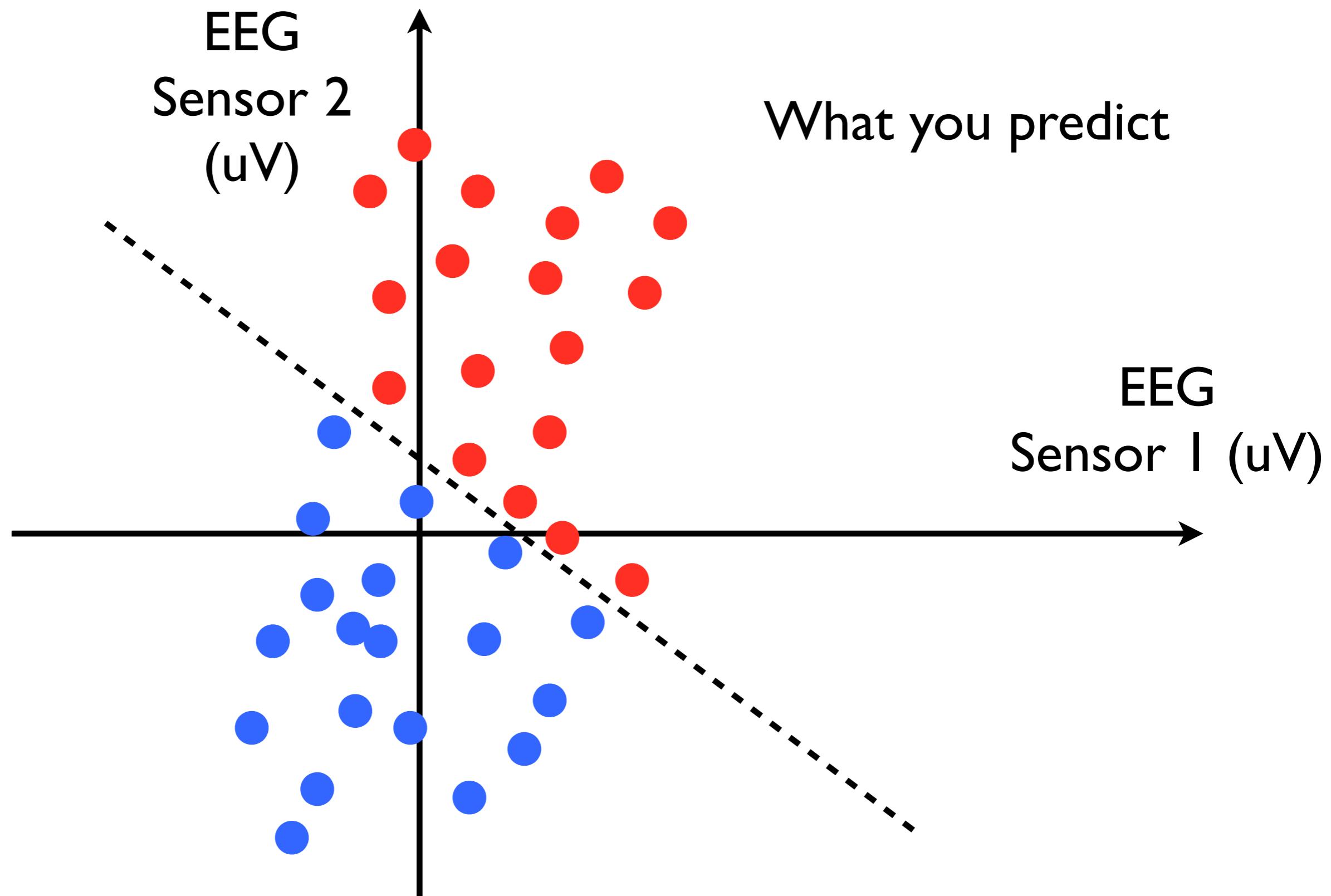
A simple decoder with 2 sensors



A simple decoder with 2 sensors



Testing my first “decoder”



Testing my first “decoder”



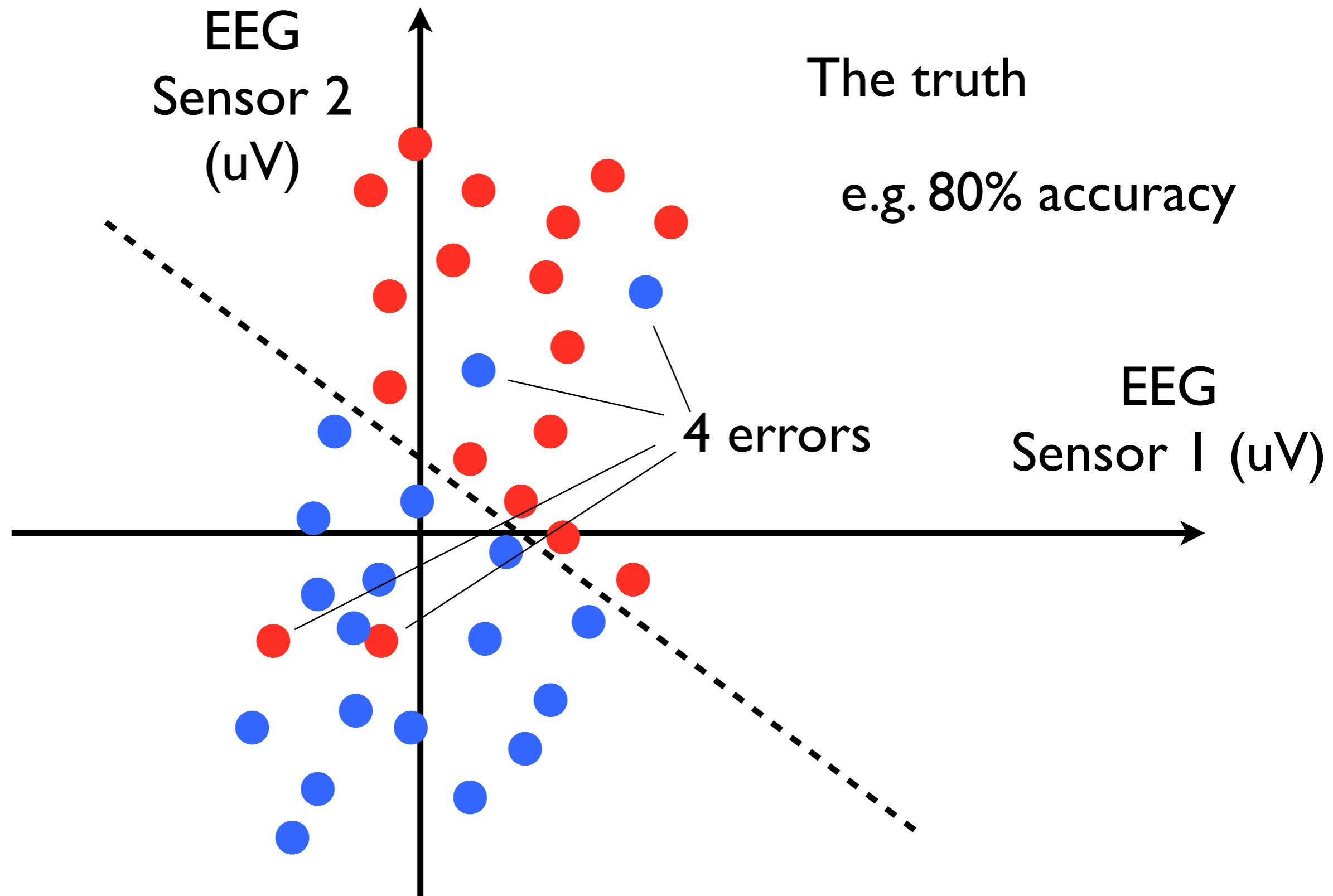
It is a linear model

$$y_i = \text{sign}\left(\sum_{j=1}^P \beta_j x_{ij} + \beta_0\right) = \text{sign}(\beta^\top x_i + \beta_0)$$

$x_i \in \mathbb{R}^P$: vector of features (here 2)

$\beta \in \mathbb{R}^P, \beta_0 \in \mathbb{R}$: model parameters to estimate

Testing my first “decoder”



Logistic regression

Hypothesis (grounded in the LDA generative model):

$$\log \left(\frac{\text{Prob}(y = 1|x)}{\text{Prob}(y = -1|x)} \right) = \beta^\top x + \beta_0$$

Logistic regression

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$$\log \left(\frac{\text{Prob}(y = 1|x)}{\text{Prob}(y = -1|x)} \right) = \beta^\top x + \beta_0$$

Inference my maximum likelihood:

$$\hat{\beta}, \hat{\beta}_0 = \arg \min_{\beta, \beta_0} \frac{1}{N} \sum_{i=1}^N \log(1 + \exp(-y_i(\beta^\top x_i + \beta_0)))$$

Logistic regression

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$+ \lambda \Omega(\beta)$ Regularization

Logistic regression

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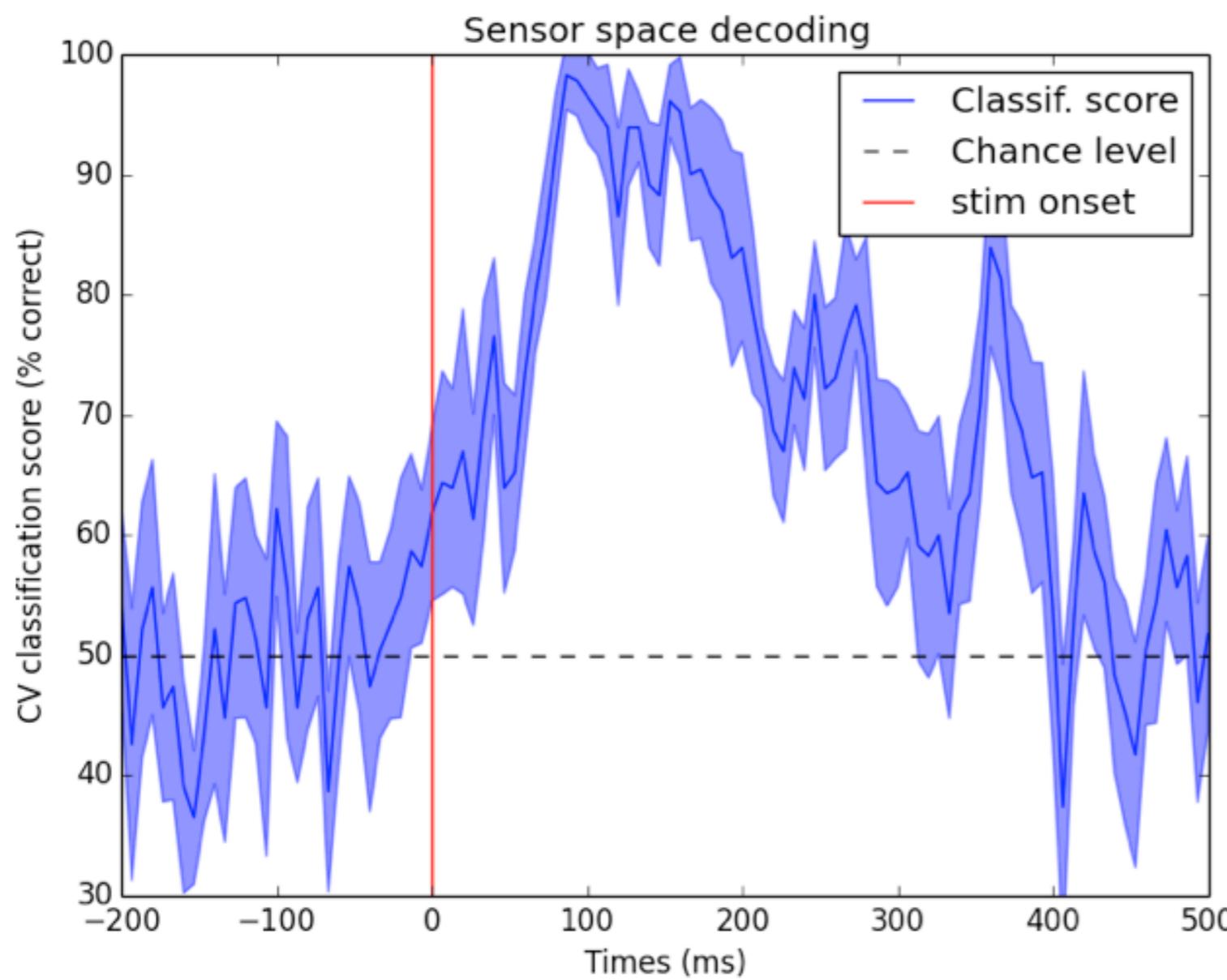
$+ \lambda \Omega(\beta)$ Regularization

Example: $\Omega(\beta) = \frac{1}{2} \|\beta\|_2^2$ Hyperparameter: λ

Decoding evoked
MEG/EEG activity

Decoding over time with MEG/EEG

- **IDEA:** Run a cross-validation loop at each time point



Condition 1 (auditory tone in left ear) vs. condition 2 (visual flash in left hemifield)

- 50 epochs per class
- no baseline
- band pass between 2Hz and 40Hz
- Linear SVM ($C=1$)
- Monte-carlo cross-val.



https://mne.tools/stable/auto_tutorials/machine-learning/plot_sensors_decoding.html

Decoding induced
MEG/EEG activity

Covariance

$S_i \in \mathbb{R}^{C \times T}$: MEG/EEG signals

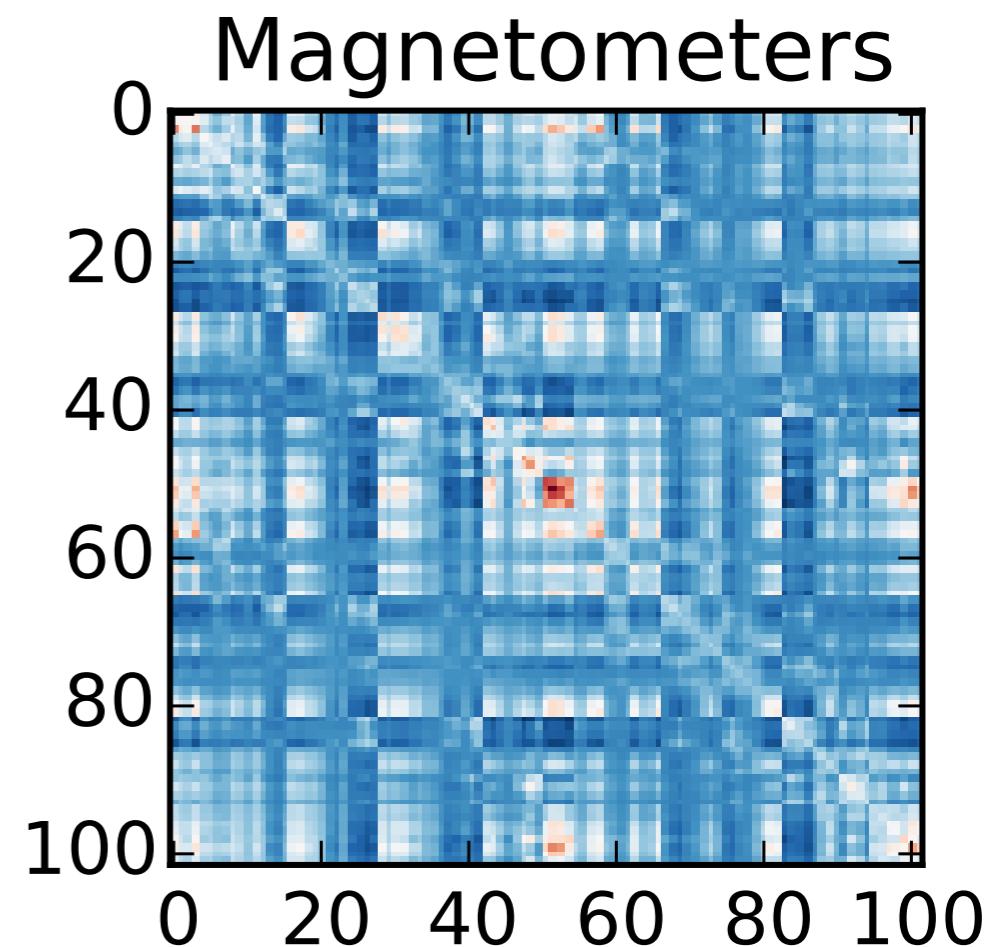
C : number of channels

T : number of time samples

Definition [Covariance]:

$$\Sigma_i = \frac{S_i S_i^\top}{T} \in \mathbb{S}_+^C \subset \mathbb{R}^{C \times C}$$

Set of non-negative
symmetric matrices



Remark: Estimation
of cov. requires care

[Engemann & Gramfort,
Neuroimage 2017]

Common Spatial Pattern (CSP)

The model:

$$w_j \in \mathbb{R}^C \text{ : Spatial filter}$$

$$x_{ij} = \log(w_j^\top \Sigma_i w_j) \text{ : Feature construction}$$

$$y_i = \text{sign}\left(\sum_{j=1}^P \beta_j \log(w_j^\top \Sigma_i w_j) + \beta_0\right) \text{ : Linear model}$$

[Koles 1991, Blankertz et al. 2008 etc.]

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How do you estimate filters?

[Koles 1991, Blankertz et al. 2008 etc.]

Common Spatial Pattern (CSP)

$$\Sigma^c = \frac{1}{N_c} \sum_{i/y_i=c} \Sigma_i \quad c \in \{-1, 1\}$$

Estimate per class covariance

[Koles 1991, Blankertz et al. 2008 etc.]

https://mne.tools/dev/auto_examples/decoding/plot_decoding_csp_eeg.html

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Solve generalized eigenvalue problem:

$$w \in \mathbb{R}^C, \mu \in \mathbb{R} \quad \text{s.t.} \quad \Sigma^1 w = \mu \left(\sum_{c \in \{-1, 1\}} \Sigma^c \right) w$$

[Koles 1991, Blankertz et al. 2008 etc.]

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Properties:

$$W^\top \Sigma^c W = \Lambda^c \quad \Lambda^c = \text{diag}(\lambda_1^c, \dots, \lambda_C^c) \quad \sum_{c \in \{1, -1\}} \Lambda^c = I$$

[Koles 1991, Blankertz et al. 2008 etc.]

https://mne.tools/dev/auto_examples/decoding/plot_decoding_csp_eeg.html

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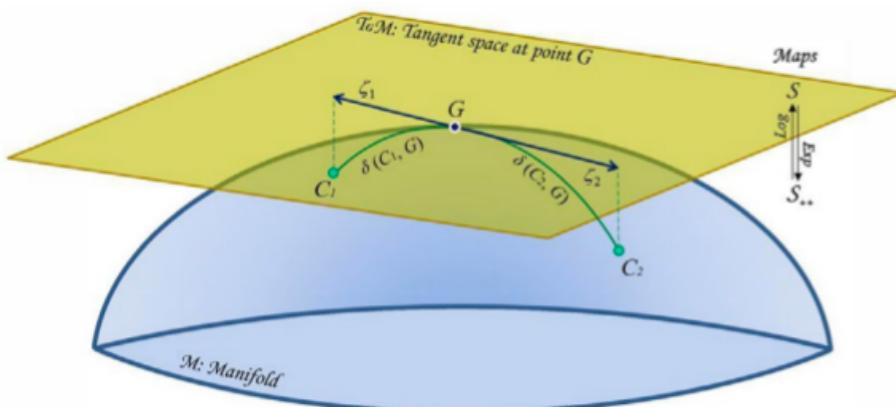
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Since $\lambda_j^1 + \lambda_j^{-1} = 1$, a high value for λ_j^1 means that the filter output based on filter w_j yields a high variance for input signals in class 1 and a low variance for signals in class -1 (and vice versa).

[Koles 1991, Blankertz et al. 2008 etc.]

Riemann

- Summarise a trial by a covariance
- Classification where samples are covariances
- Covariances live a curved manifold $\mathbb{S}_+^C \neq \mathbb{R}^{2C}$



Def. [Geometric distance]:

$$d_G(\Sigma_1, \Sigma_2) = \left\| \log(\Sigma_1^{-\frac{1}{2}} \Sigma_2 \Sigma_1^{-\frac{1}{2}}) \right\|_F$$
$$= \left[\sum_{i=1}^C \log^2 \lambda_k \right]^{\frac{1}{2}}$$

[Barachant et al. 2013, Bhatia 2007, Absil et al. 2009]

Nearest Centroid with Riemann

The algorithm:

- Compute centroid for each class

$$\bar{\Sigma}^c = \arg \min_{\Sigma \in \mathbb{S}_{++}^C} \sum_{i/y_i=c} d_G(\Sigma_i, \Sigma)^2 \quad \text{“Fréchet Mean”}$$

- Prediction rule:

$$f(\Sigma_i) = \arg \min_{c \in \{1, -1\}} d_G(\Sigma_i, \bar{\Sigma}^c)$$

Remark: Called “Minimum Distance to Mean” (MDM) by Barachant

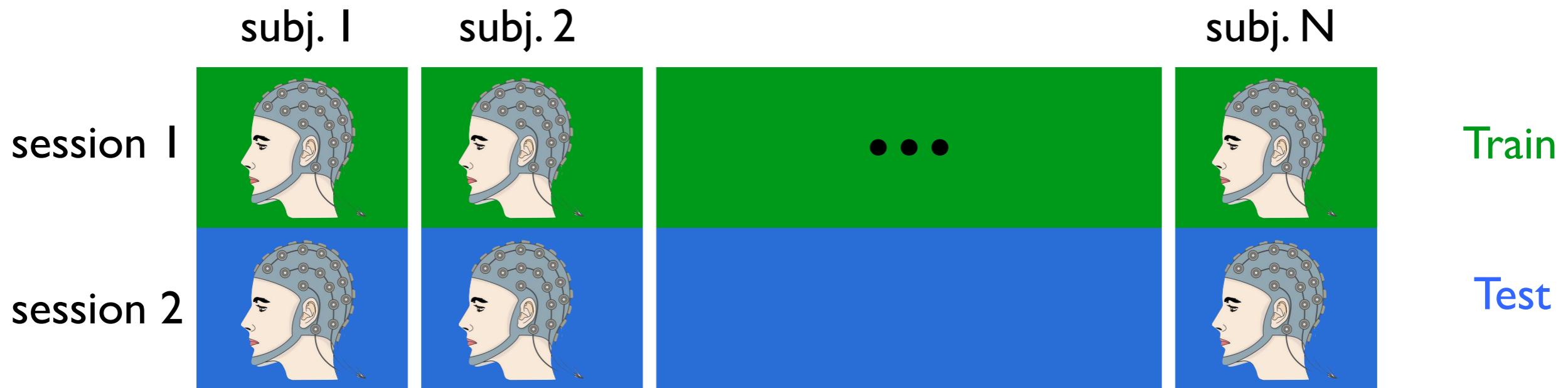
[Barachant et al. LVA ICA 2010, Barachant et al. 2013]

<http://pyriemann.readthedocs.io/en/latest/>

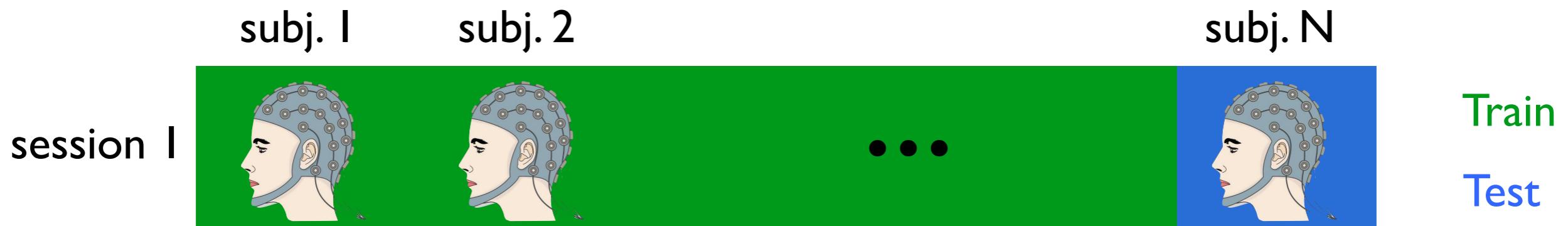
Cross-validation
done right !

2 setups in neuroimaging

- **Intra-subject decoding:** learn and predict on the same subject



- **Inter-subject decoding:** learn and predict on different subjects



In both cases left-out samples are independent

Training vs. Test vs. Validation error

Full dataset

Training vs. Test vs. Validation error

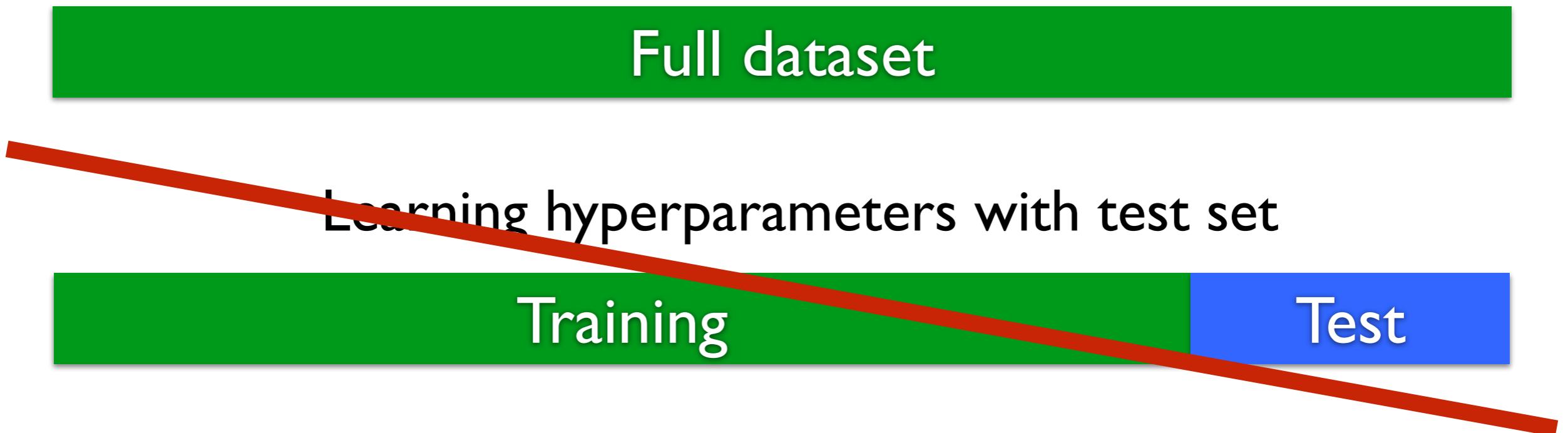
Full dataset

Learning hyperparameters with test set

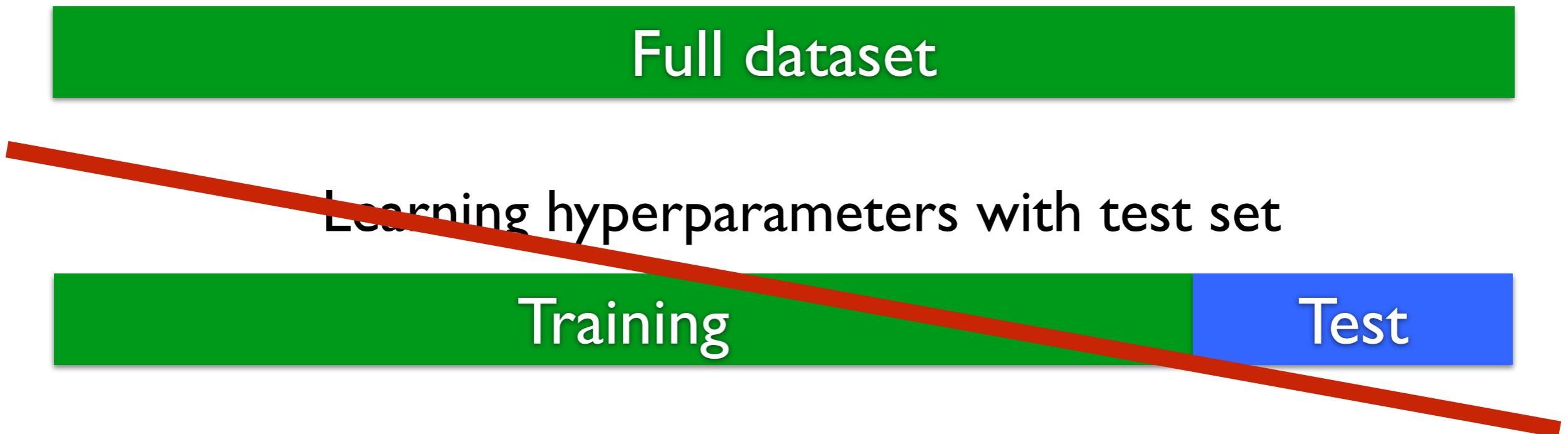
Training

Test

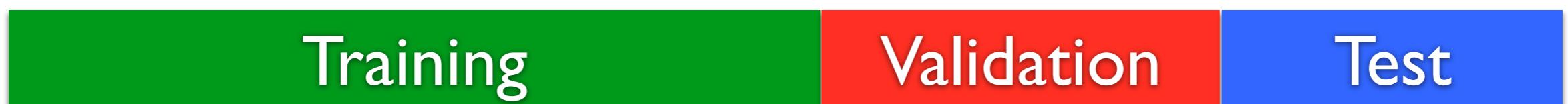
Training vs. Test vs. Validation error



Training vs. Test vs. Validation error



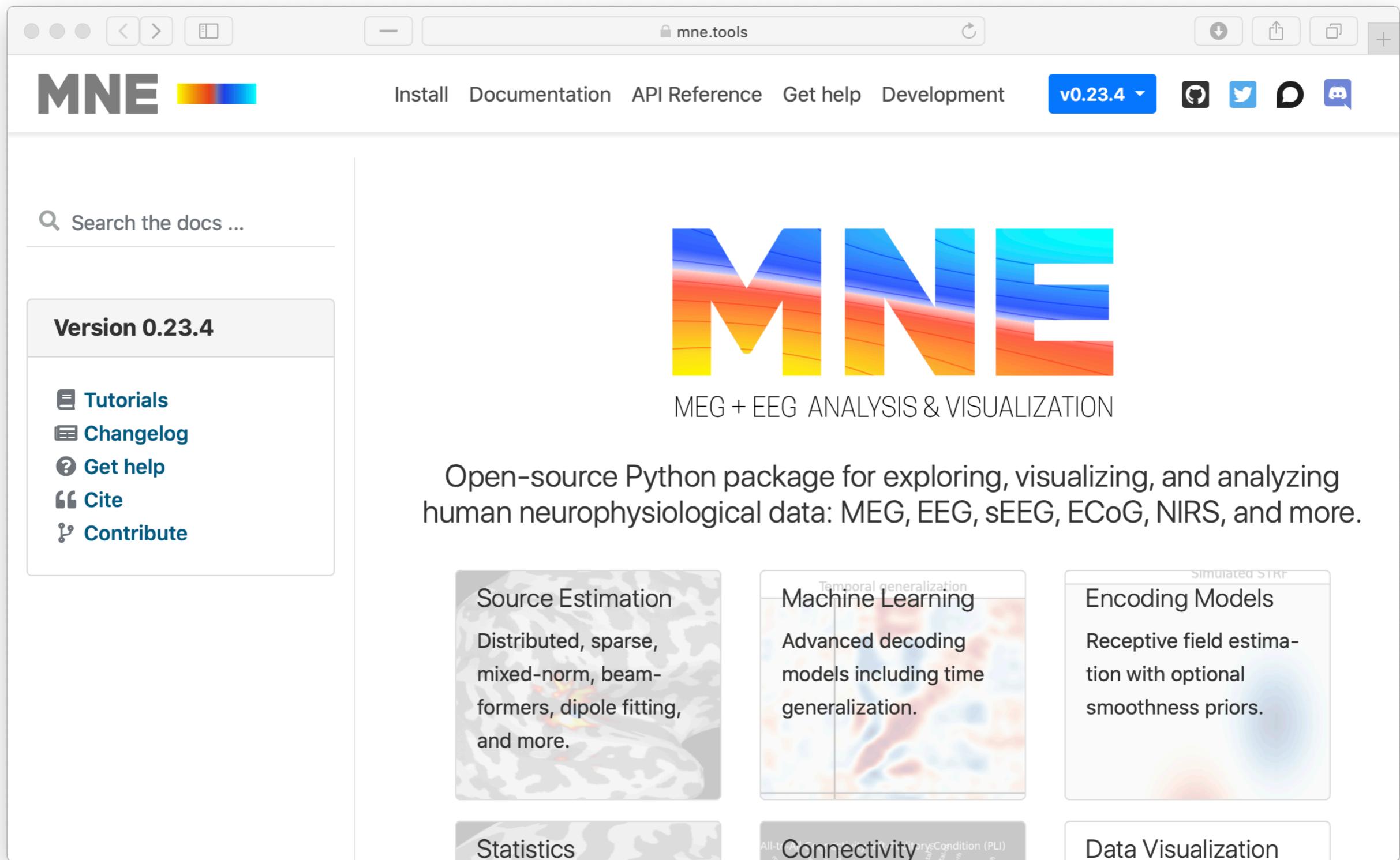
Learning hyperparameters with validation set and use test for test !



**To reliably assess the performance of your model
don't optimize hyperparameters on test set**

MNE quick info

http://mne.tools



The screenshot shows the MNE (Magnetic Resonance Imaging) website homepage. At the top, there is a navigation bar with links for 'Install', 'Documentation', 'API Reference', 'Get help', and 'Development'. A dropdown menu shows 'v0.23.4'. Below the navigation bar is a search bar with the placeholder 'Search the docs ...'. To the left, a sidebar displays 'Version 0.23.4' and links to 'Tutorials', 'Changelog', 'Get help', 'Cite', and 'Contribute'. The main content area features a large 'MNE' logo with a colorful, wavy background. Below the logo, the text 'MEG + EEG ANALYSIS & VISUALIZATION' is displayed. A descriptive paragraph states: 'Open-source Python package for exploring, visualizing, and analyzing human neurophysiological data: MEG, EEG, sEEG, ECoG, NIRS, and more.' Three callout boxes highlight 'Source Estimation', 'Machine Learning', and 'Encoding Models'. At the bottom, there are buttons for 'Statistics', 'Connectivity', and 'Data Visualization'.

mne.tools

Install Documentation API Reference Get help Development v0.23.4

Search the docs ...

Version 0.23.4

Tutorials Changelog Get help Cite Contribute

MNE

MEG + EEG ANALYSIS & VISUALIZATION

Open-source Python package for exploring, visualizing, and analyzing human neurophysiological data: MEG, EEG, sEEG, ECoG, NIRS, and more.

Source Estimation
Distributed, sparse, mixed-norm, beam-formers, dipole fitting, and more.

Machine Learning
Advanced decoding models including time generalization.

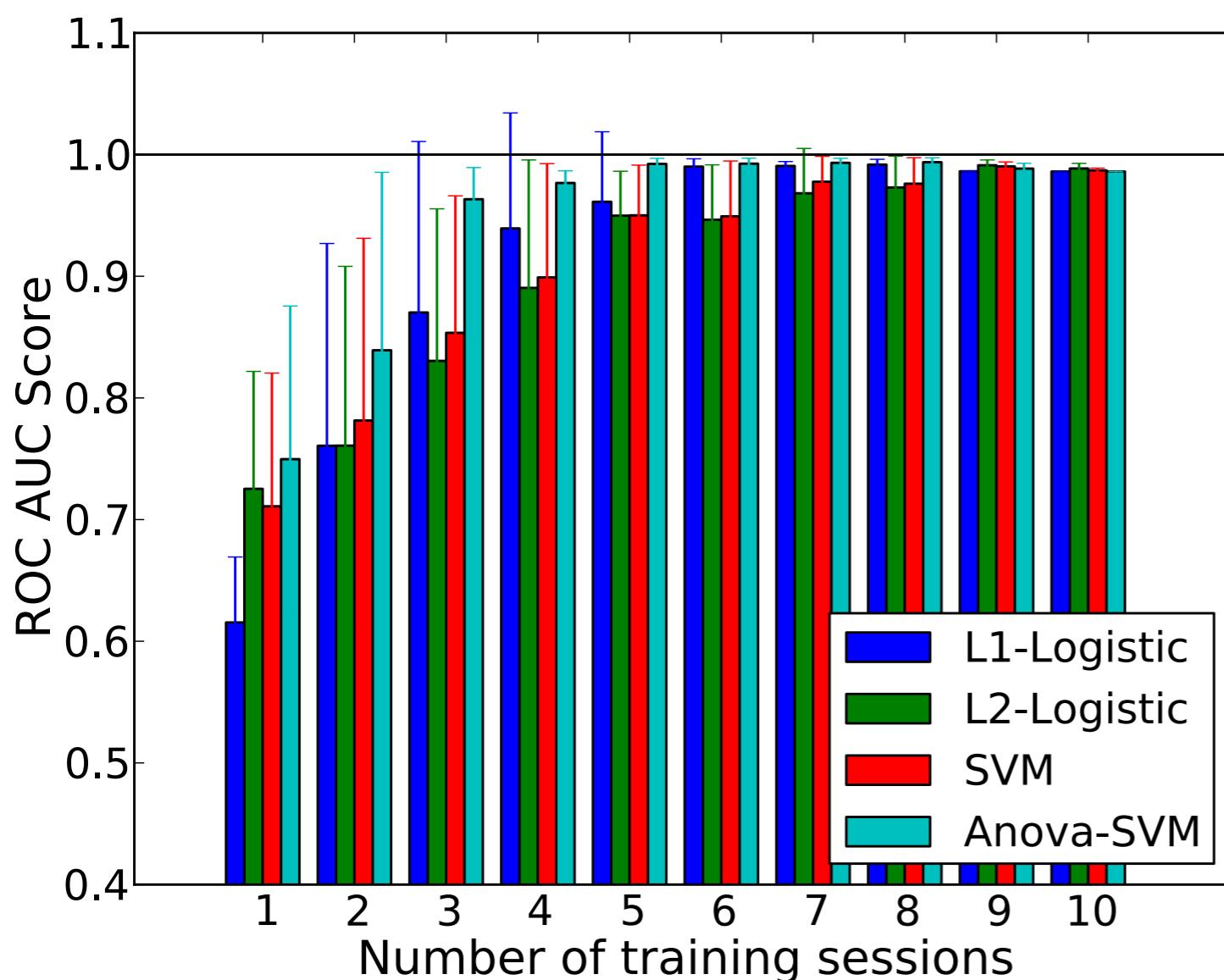
Encoding Models
Receptive field estimation with optional smoothness priors.

Statistics Connectivity Data Visualization

MNE software for processing MEG and EEG data, A. Gramfort, M. Luessi, E. Larson, D. Engemann, D. Strohmeier, C. Brodbeck, L. Parkkonen, M. Hämäläinen, Neuroimage 2013

Conclusion

Why more data is better?

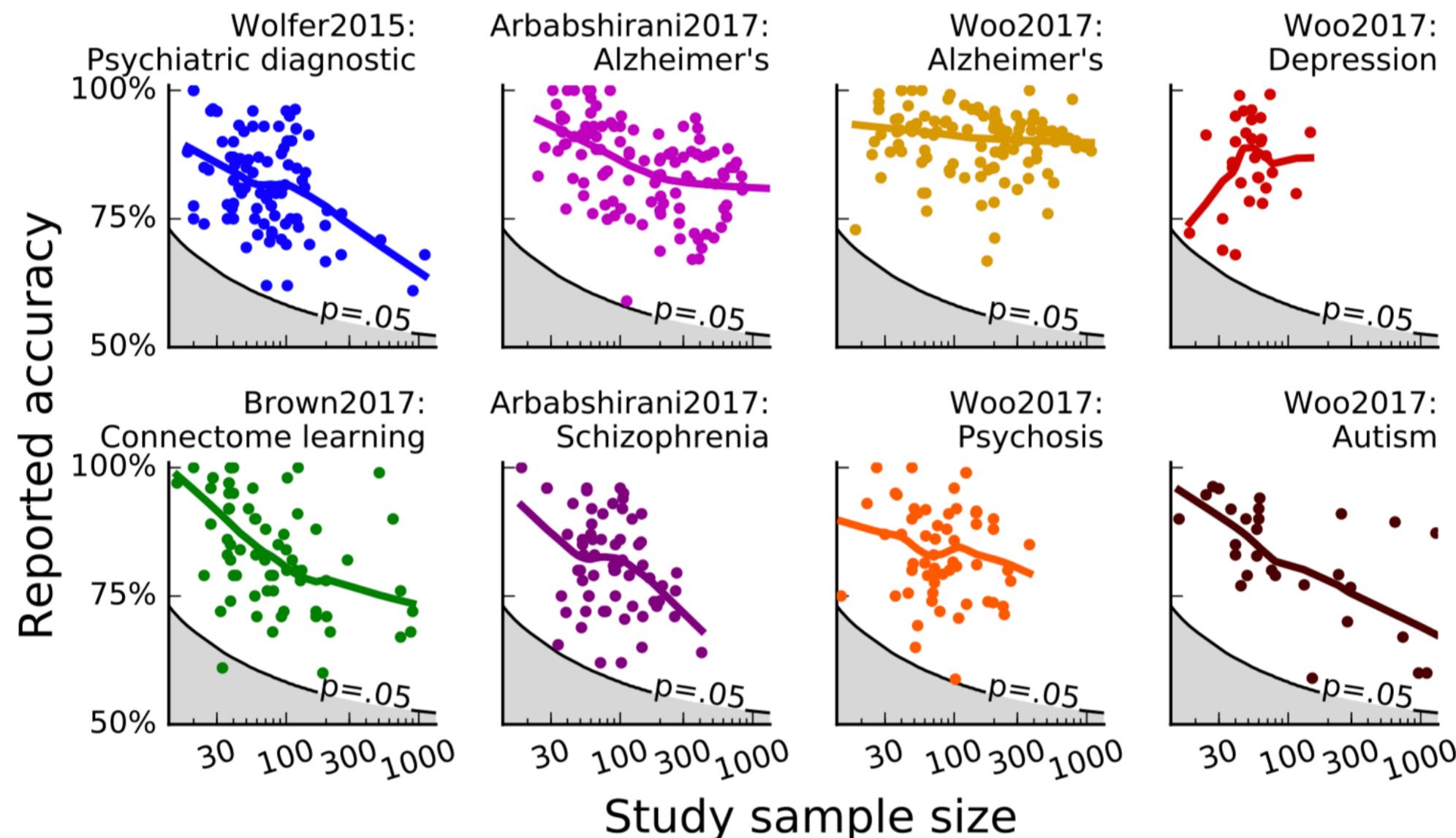


- 5 subjects
- 12 sessions (more than 1000 scans)
- Binary classification
- Test of 2 left-out sessions
- The more data the better
- Almost no noise

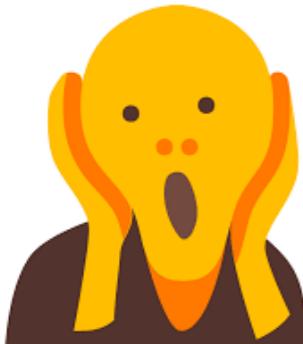
Data from [Haxby et al. 2001]

Figure from [Gramfort et al. 2011]

Cross-validation failure !!!



Prediction accuracy should increase with sample size
and not the opposite...



[Varoquaux 2017, Neuroimage]

Now hands on!

To install the bare minimum for this tutorial:

```
pip install mne
```

To install everything using conda (or mamba):

```
conda install mamba -n base -c conda-forge  
mamba install mne
```

For more complete install see:

<https://mne.tools/stable/install/index.html>

Thanks !

Contact

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GitHub : @agramfort



Twitter : @agramfort



Support

ERC SLAB, ANR THALAMEEG ANR-14-NEUC-0002-01
NIH R01 MH106174, ANR Chaire IA BrAIN

Inria



anr

"An approximate answer to the right problem is worth a good deal more than an exact answer to an approximate problem. ~ John Tukey"

