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CSE 13s

Writeup

The worst case and average time complexity for bubble sort is $O(n^2)$, the time complexity of shell sort depends on the gap sequence but is generally around $O(n \log^2 n)$, and the time complexity of quick sort is $O(n \log n)$ during best case and $O(n^2)$ during worst case.

```
Bubble Sort
15 elements, 138 moves, 90 compares
  34732749    42067670    104268822    134750049    989854347
  1128740088  1176217884  1256702424  1611961436  1703689917
  1857327504  2028658157  2040620901  2068323909  2146508390
Shell Sort
15 elements, 162 moves, 82 compares
  34732749    42067670    104268822    134750049    989854347
  1128740088  1176217884  1256702424  1611961436  1703689917
  1857327504  2028658157  2040620901  2068323909  2146508390
Quick Sort (Stack)
15 elements, 42 moves, 113 compares
Max stack size: 0
  34732749    42067670    104268822    134750049    989854347
  1128740088  1176217884  1256702424  1611961436  1703689917
  1857327504  2028658157  2040620901  2068323909  2146508390
Quick Sort (Queue)
15 elements, 42 moves, 113 compares
Max stack size: 0
  34732749    42067670    104268822    134750049    989854347
  1128740088  1176217884  1256702424  1611961436  1703689917
  1857327504  2028658157  2040620901  2068323909  2146508390
```

This is somewhat reflected in this image because the quick sorts have a lot fewer moves than shell and bubble which makes sense because its best case time complexity is better as well although there are more comparisons.

```

Bubble Sort
100 elements, 7470 moves, 4905 compares
    8032304    34732749    42067670    56499902    57831606
    62698132    73647806    75442881    104268822    134750049
    243082246    256731966    281272176    297461283    334122749
Shell Sort
100 elements, 3038 moves, 1583 compares
    8032304    34732749    42067670    56499902    57831606
    62698132    73647806    75442881    104268822    134750049
    243082246    256731966    281272176    297461283    334122749
Quick Sort (Stack)
100 elements, 468 moves, 951 compares
Max stack size: 0
    8032304    34732749    42067670    56499902    57831606
    62698132    73647806    75442881    104268822    134750049
    243082246    256731966    281272176    297461283    334122749
Quick Sort (Queue)
100 elements, 468 moves, 951 compares
Max stack size: 0
    8032304    34732749    42067670    56499902    57831606
    62698132    73647806    75442881    104268822    134750049
    243082246    256731966    281272176    297461283    334122749

```

If we increase the amount of elements in the array as shown in the image above the quick sort makes drastically fewer moves and comparisons to the bubble and shell sort which shows how the algorithm affects the time complexity. This also shows how if you have an array with not many elements it could be just as fast to use shell or bubble sort, but if you have a large array then quick sort is more efficient in terms of moves and comparisons. Regrettably this program was started very last minute and it is reflected in the quality of this writeup which is being submitted mere minutes before the deadline, lesson learned.