

# Chapter 6

## Non holonomic vehicles

Low and high level vehicle control depends on the vehicle structure. Planning and control execution of trajectories by non holonomic vehicles require the study of their kinematics model and environment conditions.

Autonomous maneuvering on non holonomic vehicles for moving in a structured dynamic environment is studied by Paromtchick, Garnier and Laugier. The problem faced up is the autonomous maneuvering for lane following, changing and parallel parking. Motion generation and vehicle control is split in three phases: localization, planning and execution. The vehicle kinematics determine the constraints to define possible trajectories based on the mission and range measurement of environmental objects.

Khatib, Jaouni, Chatila and Laumond proposed a dynamic path structure that they call a deformable structure to deal with environment changing conditions. The goal is to define a methodology linking planning and execution taking into consideration the vehicle structure. The work is an evolution of the method called elastic band that has been adapted from holonomic to non holonomic robots. The method considers distance to obstacles and uses convex potential functions to increase reactivity to deal with environment changes.

The paper of Lamiriaux and Laumond addresses the problem of parametrizing a path with respect to time to generate a trajectory for a mobile robot towing a trailer. They present a numerical algorithm where they introduce the movement constraints for velocity and acceleration. The motion planning and control system is based on three main steps: non-holonomic path planning, trajectory computation that is the main objective of the paper, and feedback control.

# Autonomous maneuvers of a nonholonomic vehicle

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**Abstract:** Maneuvers of a nonholonomic vehicle in a structured dynamic environment are considered. The paper focuses on motion generation and control methods to autonomously perform lane following/changing and parallel parking maneuvers. Lane following/changing involves the tracking of a nominal trajectory in the traffic lane, and the generation and tracking of local lane-changing trajectories, for instance, for obstacle avoidance. Parallel parking involves a controlled sequence of motions, in order to localize a sufficient parking space, obtain a convenient start location for the vehicle and perform a parallel parking maneuver. The methods developed are tested on an automatic electric vehicle.

## 1. Introduction

The autonomous maneuvering of nonholonomic vehicles in dynamic environments is being studied by many research teams. The state-of-the-art of this domain reflects approaches of various complexity. A generalized approach involves planning a global path within an available map of the environment. Because of the computational costs, global planning is usually performed off-line. The subsequent following of the planned nominal trajectory involves reactive capabilities, in order to avoid collisions with unexpected obstacles. These two behaviors (trajectory following and obstacle avoidance) are in conflict, their simultaneous operation can lead to an oscillatory motion of the vehicle. However, if a nominal trajectory which is obstructed by an obstacle can be modified locally to avoid the obstacle and then return to the nominal trajectory, the oscillations can be eliminated. This issue is studied in the present paper using the example of lane following/changing maneuvers in a traffic environment.

A practical approach to motion generation and control for autonomous parallel parking in a traffic environment is also considered. Its key idea is to carry out a “Localization-Planning-Execution” cycle until a specified “parked” location of the vehicle relative to its environment is reached. The approach is based on range measurements to environmental objects around the vehicle. Feasible controls (steering angle and locomotion velocity) that correspond to a nominal trajectory leading to the “parked” location are planned and executed in real time. Once the motion has been carried out, the sensor data is used to decide whether the “parked” location has been reached and the parking maneuver is completed. This research work contributes to the French PRAXITELE

programme that aims to develop a new urban transportation system based on a fleet of electric computer-driven vehicles [1]. At present, several experimental vehicles have been designed and their autonomous abilities are being developed.

A kinematic model of such a vehicle with front wheel steering is shown in Fig. 1. The vehicle's coordinates are denoted as a configuration  $q = (x, y, \theta)^T$  relative to some reference coordinate system where  $x = x(t)$  and  $y = y(t)$  are the coordinates of the midpoint of the rear wheel axle,  $\theta = \theta(t)$  is the orientation of the vehicle, and  $t$  is time. The motion of the vehicle is described by the equations

$$\begin{cases} \dot{x} = v \cos \phi \cos \theta, \\ \dot{y} = v \cos \phi \sin \theta, \\ \dot{\theta} = \frac{v}{L} \sin \phi, \end{cases} \quad (1)$$

where  $\phi = \phi(t)$  is the steering angle,  $v = v(t)$  is the locomotion velocity of the midpoint of the front wheel axle, and  $L$  is the wheel base. The steering angle and locomotion velocity are two control commands  $(\phi, v)$ . Equations (1) correspond to a system with nonholonomic constraints because they involve the derivatives of the coordinates of the vehicle and are non-integrable [2]. Equations (1) are valid for a vehicle moving on flat ground with a pure rolling contact without slippage between the wheels and the ground. This purely kinematic

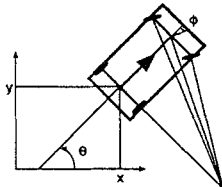


Figure 1. Kinematic model of a vehicle with front wheel steering

model of the vehicle is adequate to control low-speed motions, e.g. during parallel parking or lane following/changing in areas where only low-speed motions are allowed. For the high-speed motions, the dynamics of the vehicle must also be considered.

The notion "automatic vehicle" means that the vehicle is equipped with: (1) - a sensor unit to measure relative distances between the vehicle and environmental objects, (2) - a servo unit for low-level control of the steering angle and locomotion velocity, (3) - a control unit that processes data from the sensor and servo units and "drives" the vehicle by issuing appropriate servo commands. The sensor unit uses range sensors to measure relative distances between the vehicle and environmental objects. The servo unit consists of a steering wheel servo-system, a locomotion servo-system for forward and backward motions, and a brake servo-system to slow down and stop the vehicle. The microcomputer-based control unit monitors the current steering angle, locomotion velocity, travelled distance, coordinates of the vehicle and range data from the environment, calculates an appropriate local trajectory and issues the required servo commands.

## 2. Lane Following/Changing

Autonomous lane following is performed by tracking a nominal trajectory delivered by a global off-line path planner. In the case of unforeseen obstacles, the nominal trajectory is modified on-line, in order to avoid collisions. The modified trajectory has to satisfy temporal motion constraints and avoid collisions. In our earlier experiments, the trajectory following and obstacle avoidance behaviors were decoupled and considered independently, followed by a fuzzy behavior merging process. However, experiments showed that this produced oscillations of the effective motion of the vehicle during obstacle avoidance [3]. To remove these oscillations, a local trajectory is generated that avoids collisions with obstacles detected on the nominal trajectory. The local trajectory also allows the vehicle to catch up with the nominal trajectory (i.e. geometrical path and velocity profile along this path) after the obstacle avoidance. The major difference with the previous behavior-based approach is that the vehicle always follows a specific trajectory.

### 2.1. Lane Following

A method of trajectory following for a nonholonomic vehicle was described in [4]. This method guarantees the stable tracking of a feasible trajectory when the vehicle's control commands are:

$$\dot{\theta} = \dot{\theta}_{ref} + v_{R,ref}(k_y y_e + k_\theta \sin \theta_e), \quad (2)$$

$$v_R = v_{R,ref} \cos \theta_e + k_x x_e, \quad (3)$$

where  $q_e = (x_e, y_e, \theta_e)^T$  represents the error configuration between the reference configuration  $q_{ref}$  and the current configuration  $q$  of the vehicle ( $q_e = q_{ref} - q$ ),  $\dot{\theta}_{ref}$  and  $v_{R,ref}$  are the reference velocities,  $v_R = v \cos \phi$  is the control command for the locomotion velocity of the midpoint of the rear wheel axle,  $k_x, k_y, k_\theta$  are positive constants, and  $\phi = \arctan\left(\frac{\dot{\theta} L}{v_{R,ref}}\right)$ .

### 2.2. Lane Changing

Lane changing is carried out by generating and following a local trajectory. Such maneuvers are performed when the preplanned nominal trajectory would collide with an unforeseen obstacle. When an obstacle is detected, the nominal trajectory is translated to one side as shown in Fig. 2, in order to avoid collisions with the obstacle. The algorithm for collision avoidance involves the following iterations:

1. Generate a local trajectory which connects the nominal one with a collision-free local trajectory "parallel" to it (i.e. a parallel translation of the nominal trajectory).
2. Follow the local trajectory until the obstacle is overtaken.
3. Generate a local trajectory which connects the "parallel" trajectory with the nominal one.
4. Follow the local trajectory to catch up with the nominal one.

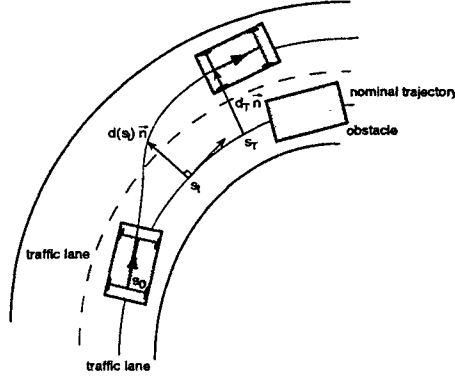


Figure 2. Translation of the nominal trajectory

A feasible trajectory for lane changing is obtained as a quintic polynomial

$$d(s) = d_T \left( 10 \left( \frac{s}{s_T} \right)^3 - 15 \left( \frac{s}{s_T} \right)^4 + 6 \left( \frac{s}{s_T} \right)^5 \right), \quad (4)$$

where  $d_T$  is a distance between the two traffic lanes,  $s_T$  is a length of the nominal trajectory which is necessary to complete the lane changing maneuver, and  $s = s_t$  is a length of the nominal trajectory since the start of the lane changing maneuver [5]. The distance  $d_T$  is supposed to be known. The minimal value of  $s_T$  is estimated as

$$s_{T,min} = \frac{\pi \sqrt{k d_T}}{2 C_{max}}, \quad (5)$$

where  $C_{max}$  stands for the maximum allowed curvature:

$$C_{max} = \min \left\{ \frac{\tan(\phi_{max})}{L}, \frac{\gamma_{max}}{v_{R,ref}^2} \right\}, \quad (6)$$

$\gamma_{max}$  is the maximum allowed lateral acceleration, and  $k > 1$  is an empirical constant (e.g.  $k = 1.17$  in our experiments).

When an obstacle is detected, a value  $s_{T,min}$  is calculated according to (5) and compared with a distance between the vehicle and the obstacle. A decision is made, either to perform a lane changing maneuver or to slow down and possibly stop the vehicle. For the lane changing maneuver, the translation of the nominal trajectory is computed: at each instant  $t$  since the start of the maneuver, the reference position  $p_{ref}$  is translated along the vector  $d(s_t) \cdot \vec{n}$  where  $\vec{n}$  represents the unit normal vector to the velocity vector along the nominal trajectory. The reference orientation  $\theta_{ref}$  is converted into  $\theta_{ref} + \arctan \left( \frac{\partial d}{\partial s}(s_t) \right)$ , and the reference velocity  $v_{R,ref}$  is obtained as

$$v_{R,ref}(t) = \frac{dist(p_{ref}(t), p_{ref}(t + \Delta t))}{\Delta t}, \quad (7)$$

where  $dist$  stands for the euclidean distance.

### 3. Parallel Parking

Autonomous parallel parking involves localizing a sufficient space (parking bay), obtaining a convenient start location for the vehicle relative to the bay, and performing a parallel parking maneuver. During localization the vehicle moves slowly along the traffic lane. Range data allows a local map of the environment alongside the vehicle to be built. Free spaces are detected, their borders are localized, and their orientation is calculated. The dimensions of the bay are compared with those of the vehicle and a decision on suitability for parking is made.

Drivers know from experience that before the parking maneuver starts, the vehicle must be oriented near parallel to the parking bay and it must also reach a convenient start position in front of the bay. A start location for parallel parking is shown in Fig. 3 where an automatic vehicle A1 is in a traffic lane. The parking lane with parked vehicles B1, B2 and a parking bay between them is on the right hand side of the vehicle A1. L1 and L2 are respectively the length and width of A1, and D1 and D2 are the distances available for longitudinal and lateral displacements of A1 within the bay. D3 and D4 are the longitudinal and lateral displacements of the corner A13 of A1 relative to the corner B24 of B2. The distances D1, D2, D3 and D4 are computed by the

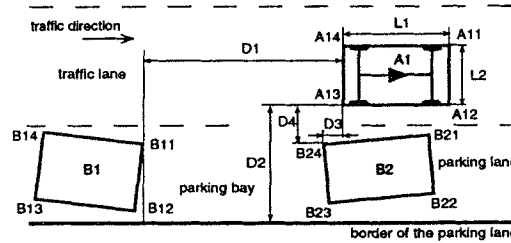


Figure 3. Start location for parallel parking

control unit from data obtained by the sensor and servo units. The control unit compares the length (D1-D3) and width (D2-D4) of the parking bay with the length L1 and width L2 of A1, where L1 and L2 include sufficient clearance for the vehicle to move around. If  $(D1-D3) > L1$  and  $(D2-D4) > L2$ , the parking bay is sufficient for parallel parking.

During parallel parking, iterative low-speed backwards-and-forwards motions with coordinated control of the steering angle and locomotion velocity are performed to produce a lateral displacement of the vehicle into the parking bay. The number of such motions depends on the distances D1, D2, D3, D4 and the necessary parking "depth" which depends on the width L2 of the vehicle A1. The start and end orientations of the vehicle are the same for each iterative motion  $i = 1, \dots, N$ .

For the  $i$ -th iterative motion (but omitting the index " $i$ "), let the start coordinates of the vehicle be  $x_0 = x(0)$ ,  $y_0 = y(0)$ ,  $\theta_0 = \theta(0)$  and the end coordinates be  $x_T = x(T)$ ,  $y_T = y(T)$ ,  $\theta_T = \theta(T)$ , where  $T$  is duration of the

motion. The "parallel parking" condition means that

$$\theta_0 - \delta_\theta < \theta_T < \theta_0 + \delta_\theta, \quad (8)$$

where  $\delta_\theta > 0$  is a small admissible error in orientation of the vehicle.

The following control commands of the steering angle  $\phi$  and locomotion velocity  $v$  provide the parallel parking maneuver [6]:

$$\phi(t) = \phi_{max} k_\phi A(t), \quad 0 \leq t \leq T, \quad (9)$$

$$v(t) = v_{max} k_v B(t), \quad 0 \leq t \leq T, \quad (10)$$

where  $\phi_{max} > 0$  and  $v_{max} > 0$  are the admissible magnitudes of the steering angle and locomotion velocity respectively,  $k_\phi = \pm 1$  corresponds to a right side (+1) or left side (-1) parking bay relative to the traffic lane,  $k_v = \pm 1$  corresponds to forward (+1) or backward (-1) motion,

$$A(t) = \begin{cases} 1, & 0 \leq t < t', \\ \cos \frac{\pi(t-t')}{T^*}, & t' \leq t \leq T-t', \\ -1, & T-t' < t \leq T, \end{cases} \quad (11)$$

$$B(t) = 0.5 \left( 1 - \cos \frac{4\pi t}{T} \right), \quad 0 \leq t \leq T, \quad (12)$$

where  $t' = \frac{T-T^*}{2}$ ,  $T^* < T$ .

The commands (9) and (10) are open-loop in the  $(x, y, \theta)$ -coordinates. The steering wheel servo-system and locomotion servo-system must execute the commands (9) and (10), in order to provide the desired  $(x, y)$ -path and orientation  $\theta$  of the vehicle. The resulting accuracy of the motion in the  $(x, y, \theta)$ -coordinates depends on the accuracy of these servo-systems. Possible errors are compensated by subsequent iterative motions.

For each pair of successive motions  $(i, i+1)$ , the coefficient  $k_v$  in (10) has to satisfy the equation  $k_{v,i+1} = -k_{v,i}$  that alternates between forward and backward directions. Between successive motions, when the velocity is null, the steering wheels turn to the opposite side in order to obtain a suitable steering angle  $\phi_{max}$  or  $-\phi_{max}$  to start the next iterative motion.

In this way, the form of the commands (9) and (10) is defined by (11) and (12) respectively. In order to evaluate (9)-(12) for the parallel parking maneuver, the durations  $T^*$  and  $T$ , the magnitudes  $\phi_{max}$  and  $v_{max}$  must be known.

The value of  $T^*$  is lower-bounded by the kinematic and dynamic constraints of the steering wheel servo-system. When the control command (9) is applied, the lower bound of  $T^*$  is

$$T_{min}^* = \pi \max \left\{ \frac{\phi_{max}}{\dot{\phi}_{max}}, \sqrt{\frac{\phi_{max}}{\ddot{\phi}_{max}}} \right\}, \quad (13)$$

where  $\dot{\phi}_{max}$  and  $\ddot{\phi}_{max}$  are the maximal admissible steering rate and acceleration respectively for the steering wheel servo-system. The value of  $T_{min}^*$  gives

duration of the full turn of the steering wheels from  $-\phi_{max}$  to  $\phi_{max}$  or vice versa, i.e. one can choose  $T^* = T_{min}^*$ .

The value of  $T$  is lower-bounded by the constraints on the velocity  $v_{max}$  and acceleration  $\dot{v}_{max}$  and by the condition  $T^* < T$ . When the control command (10) is applied, the lower bound of  $T$  is

$$T_{min} = \max \left\{ \frac{2\pi v'(D1)}{\dot{v}_{max}}, T^* \right\}, \quad (14)$$

where the empirically-obtained function  $v'(D1) \leq v_{max}$  serves to provide a smooth motion of the vehicle when the available distance D1 is small.

The computation of  $T$  and  $\phi_{max}$  aims to obtain the maximal values such that the following “longitudinal” and “lateral” conditions are still satisfied:

$$|(x_T - x_0) \cos \theta_0 + (y_T - y_0) \sin \theta_0| < D1, \quad (15)$$

$$|(x_0 - x_T) \sin \theta_0 + (y_T - y_0) \cos \theta_0| < D2. \quad (16)$$

Using the maximal values of  $T$  and  $\phi_{max}$  assures that the longitudinal and, especially, lateral displacement of the vehicle is maximal within the available free parking space. The computation is carried out on the basis of the model (1) when the commands (9) and (10) are applied. In this computation, the value of  $v_{max}$  must correspond to a safety requirement for parking maneuvers (e.g.  $v_{max} = 0.75 \text{ m/s}$  was found empirically).

At each iteration  $i$  the parallel parking algorithm is summarized as follows:

1. Obtain available longitudinal and lateral displacements D1 and D2 respectively by processing the sensor data.
2. Search for maximal values  $T$  and  $\phi_{max}$  by evaluating the model (1) with controls (9), (10) so that conditions (15), (16) are still satisfied.
3. Steer the vehicle by controls (9), (10) while processing the range data for collision avoidance.
4. Obtain the vehicle's location relative to environmental objects at the parking bay. If the “parked” location is reached, stop; else, go to step 1.

When the vehicle A1 moves backwards into the parking bay from the start location shown in Fig. 3, the corner A12 (front right corner of the vehicle) must not collide with the corner B24 (front left corner of the bay). The start location must ensure that the subsequent motions will be collision-free with objects limiting the bay. To obtain a convenient start location, the vehicle has to stop at a distance D3 that will ensure a desired minimal safety distance D5 between the vehicle and the nearest corner of the bay during the subsequent backward motion. The relation between the distances D1, D2, D3, D4 and D5 is described by a function

$$\mathcal{F}(D1, D2, D3, D4, D5) = 0. \quad (17)$$



This function can not be expressed in closed form, but it can be estimated for a given type of vehicle by using the model (1) when the commands (9) and (10) are applied. The computations are carried out off-line and stored in a look-up table which is used on-line, to obtain an estimate of  $D_3$  corresponding to a desired minimal safety distance  $D_5$  for given  $D_1$ ,  $D_2$  and  $D_4$  [7].

When the necessary parking "depth" has been reached, some clearance between the vehicle and the parked ones is provided, i.e. the vehicle moves forwards or backwards so as to be in the middle of the parking bay between the two parked vehicles.

#### 4. Experiments

The developed methods have been tested on an experimental automatic vehicle designed on the base of a LIGIER electric car. This is a four-wheeled vehicle with the front driven and steering wheels. The vehicle can either be driven as a car, or it can move autonomously. To allow autonomous motions, the vehicle is equipped with a control unit based on a Motorola VME162-CPU board and a transputer net. The sensor unit of the vehicle consists of ultrasonic range sensors (Polaroid 9000) and a linear CCD-camera. The steering wheel servo-system is equipped with a direct current motor and an optical encoder to measure the steering angle. The locomotion servo-system of the vehicle is equipped with 12 kW asynchronous motor and two optical encoders at the rear wheels to provide data on locomotion velocity of the vehicle. The vehicle also has an hydraulic braking servo-system. The developed steering and velocity control is implemented using ORCCAD software [8] running on a SUN workstation. The compiled code is transmitted via Ethernet to the VME162-CPU board.

An example of our experimental setup for lane following/changing on a circular road is shown in Fig. 4. The LIGIER vehicle has to follow a nominal trajectory along the circular traffic lane where another vehicle is moving at a lower velocity in front of LIGIER, as shown in Fig. 4a. When the obstacle is detected, a local trajectory for a lane change to the right is generated to avoid collisions, and LIGIER performs the lane changing maneuver, as illustrated in Fig. 4b. Then, LIGIER moves in parallel to its nominal trajectory until the obstacle is overtaken. Further, a new local trajectory for a lane change to the left is generated, and LIGIER performs the lane changing maneuver to return to its nominal trajectory, as shown in Fig. 4c. Finally, LIGIER continues to follow its nominal trajectory, as illustrated in Fig. 4d.

An example of the control commands of the steering angle and locomotion velocity during the lane following/changing maneuvers on a circular road is shown in Fig. 5. The corresponding motion of the vehicle is depicted in Fig. 6 where the nominal circular trajectory and the local one are plotted. The vehicle performs a lane change to the right, moves in parallel to the nominal trajectory and performs a lane change to the left to catch up with its nominal trajectory. The locomotion velocity of the vehicle is increased when it moves along the local trajectory: as it is illustrated in Fig. 6, the duration of the motion along the local trajectory equals the duration of the motion along the nominal trajectory without the lane changing maneuvers.

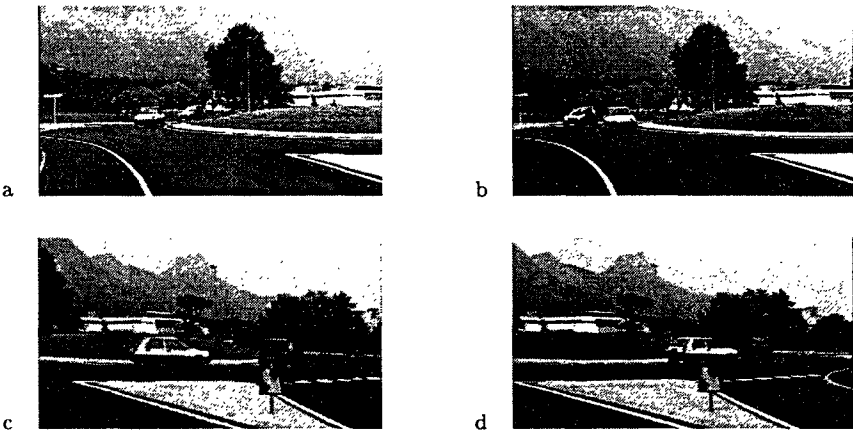


Figure 4. Sequence of motions for lane following/changing on a circular road: a - following the nominal trajectory, b - lane changing to the right and overtaking, c - lane changing to the left, d - continuing with the nominal trajectory

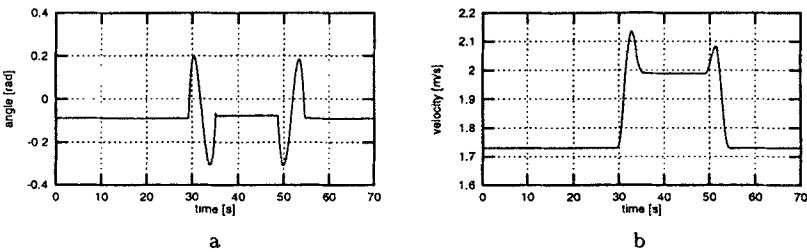


Figure 5. Control commands during lane following/changing: a - steering angle, b - locomotion velocity

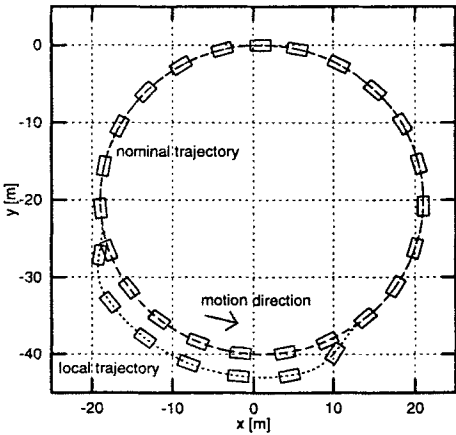


Figure 6. Lane following/changing on a circular road

An example of our experimental setup for autonomous parallel parking in a street is shown in Fig. 7. Autonomous parking can be carried out in an environment where there are moving obstacles, e.g. a pedestrian and another vehicle. As shown in Fig. 7a, the parking bay is in front of LIGIER at its right side between the two vehicles. Initially, LIGIER was driven to a position near the bay, the driver started the autonomous parking and left the vehicle. Then, LIGIER moves forwards autonomously in order to localize the parking bay, obtain a convenient start location and perform a parallel parking maneuver. When during this motion a pedestrian crosses the street in a dangerous proximity to the vehicle, as shown in Fig. 7a, this moving obstacle is detected, LIGIER slows down and stops to avoid the collision. When the way is free, LIGIER continues its forward motion. Range data is used to detect the parking bay. A decision to carry out the parking maneuver is made and a convenient start position for the initial backward movement is obtained, as shown in Fig. 7b. Then, LIGIER moves backwards into the bay, as shown in Fig. 7c. During this backward motion, the front human-driven vehicle starts to move backwards, reducing the length of the bay. The change in the environment is detected and taken into account. The range data shows that the necessary "depth" in the bay has not been reached, so further iterative motions are carried out until it has been reached. Then, LIGIER moves to the middle between the rear and front vehicles, as shown in Fig. 7d. The parallel parking maneuver is completed.

An example of the control commands (9) and (10) for parallel parking into a bay situated at the right side of the vehicle is shown in Fig. 8. The corresponding motion of the vehicle is depicted in Fig. 9 where the motion of the corners of the vehicle and the midpoint of the rear wheel axle is plotted. The available distances are  $D1=4.9\text{ m}$ ,  $D2=2.7\text{ m}$  relative to the start location of the vehicle. The lateral distance  $D4=0.6\text{ m}$  was measured by the sensor unit. The longitudinal distance  $D3=0.8\text{ m}$  was estimated so as to ensure the minimal safety distance  $D5=0.2\text{ m}$ . In this case, five iterative motions are performed to park the vehicle. As seen in Fig. 8 and Fig. 9, the durations  $T$  of the iterative motions, magnitudes of the steering angle  $\phi_{max}$  and locomotion velocity  $v_{max}$  correspond to the available displacements  $D1$  and  $D2$  within the parking bay (e.g. the values of  $T$ ,  $\phi_{max}$  and  $v_{max}$  differ for the first and last iterative motion).

The developed methods of motion generation and control for the lane following/changing and parallel parking maneuvers were tested. Because the vehicle is equipped with very simple ultrasonic sensors, only low-speed motions were allowed during the experiments. Also, small vertical objects such as posts can not be detected reliably. The execution of the maneuvers was found to be quite sensitive to the calibration of the steering wheel servo-system. To avoid accumulation of errors when computing the position and orientation of the vehicle during the lane following/changing maneuvers, landmarks were to be used. In the future, the experimental vehicle will be equipped with a more advanced sensor system.

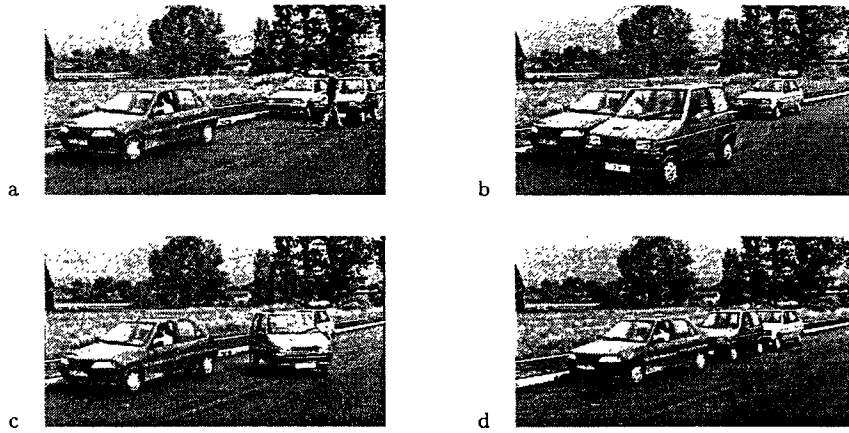


Figure 7. Sequence of motions for parallel parking: a - autonomous motion to localize a parking bay, b - obtaining a convenient start location, c - backward motion into the bay, d - parallel parking is completed

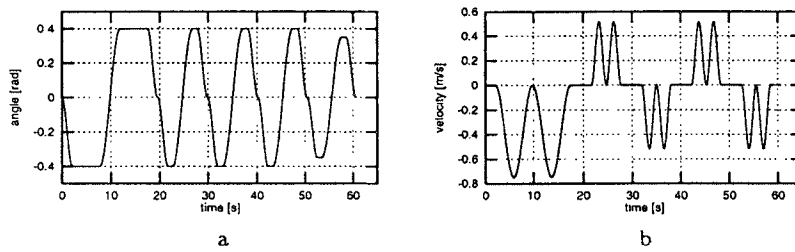


Figure 8. Control commands for parallel parking when backward and forward motions are performed: a - steering angle, b - locomotion velocity

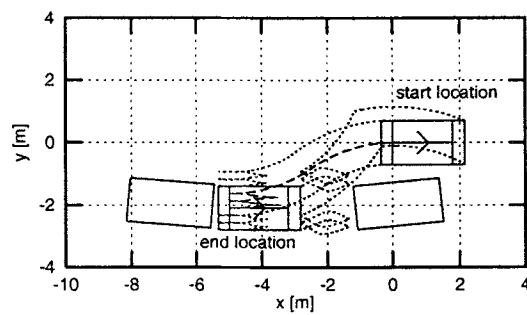


Figure 9. Parallel parking when backward and forward motions are performed

## 5. Conclusion

Motion generation and control methods to perform autonomous lane following/changing and parallel parking maneuvers were developed. Autonomous maneuvers were considered for a nonholonomic vehicle within a structured dynamic environment. The vehicle's constraints were taken into account to obtain feasible trajectories and control commands for the vehicle. The methods developed were implemented on an automatic electric vehicle and experimentally verified. The results obtained show the effectiveness of the developed methods of motion generation and control for autonomous maneuvers.

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