

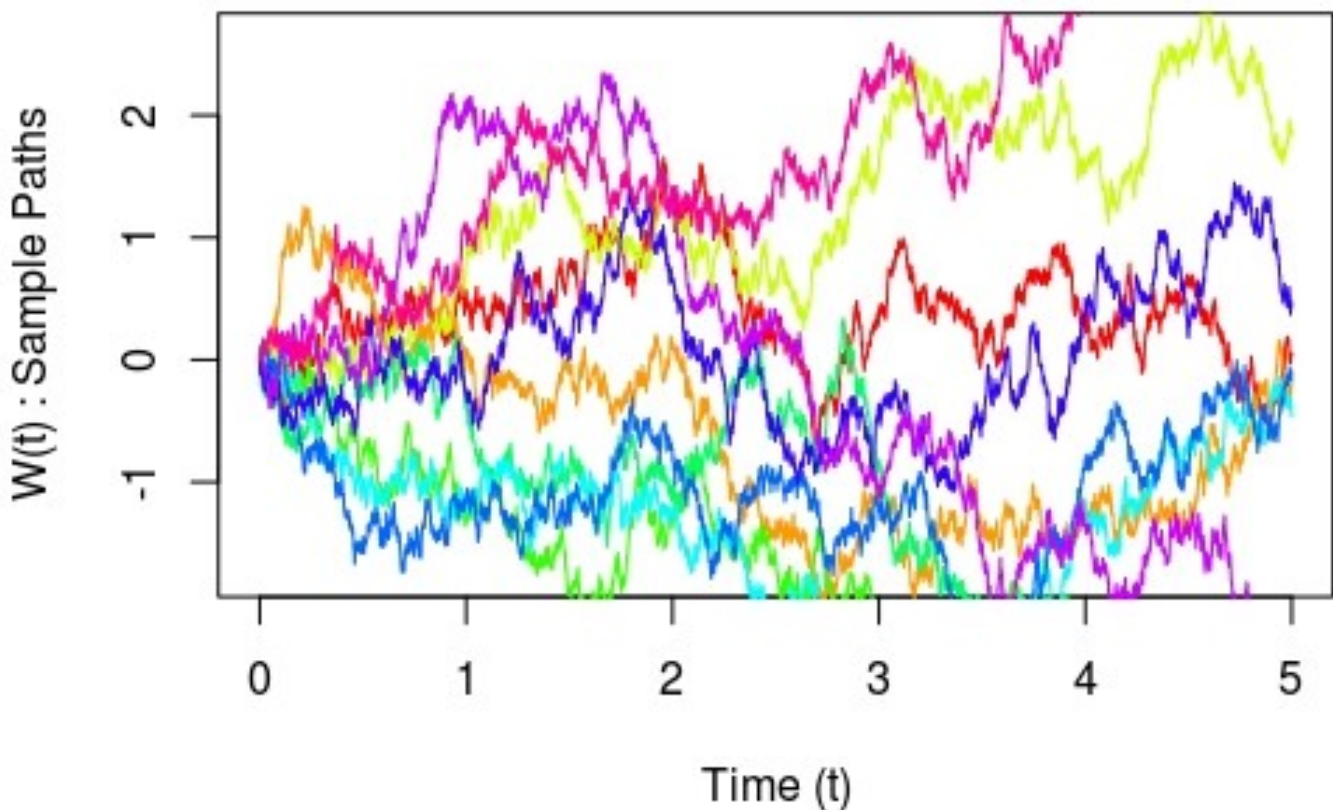
LAB 09

◆ Question 1

10 sample paths for the standard Brownian Motion in the time interval $[0,5]$ were generated and following values were obtained in one of the sample run of the program:

$$\text{Exp}[W(2)] = 0.1632837$$

$$\text{Exp}[W(5)] = -0.3610785$$

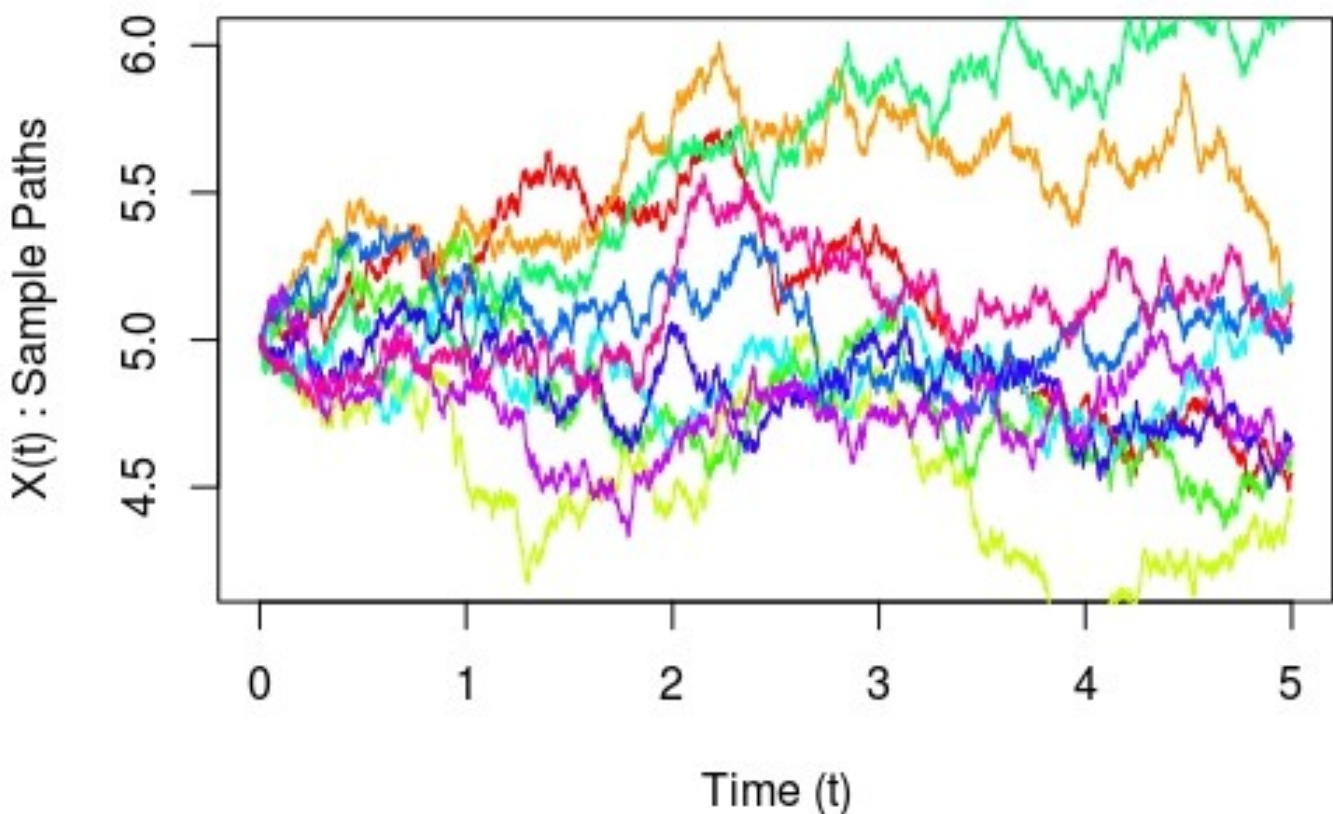


Generated Sample paths of standard Brownian Motion

◆ Question 2

10 sample paths for the Brownian motion $X \sim (\text{BM}(\mu, \sigma^2))$ in the time interval $[0, 5]$ were generated using $X(0)=5$, $\mu=0.06$ and $\sigma=0.3$ and following values were obtained in one of the sample run of the program:

$$\begin{aligned}\text{Exp}[X(2)] &= 5.064602 \\ \text{Exp}[X(5)] &= 4.94676\end{aligned}$$



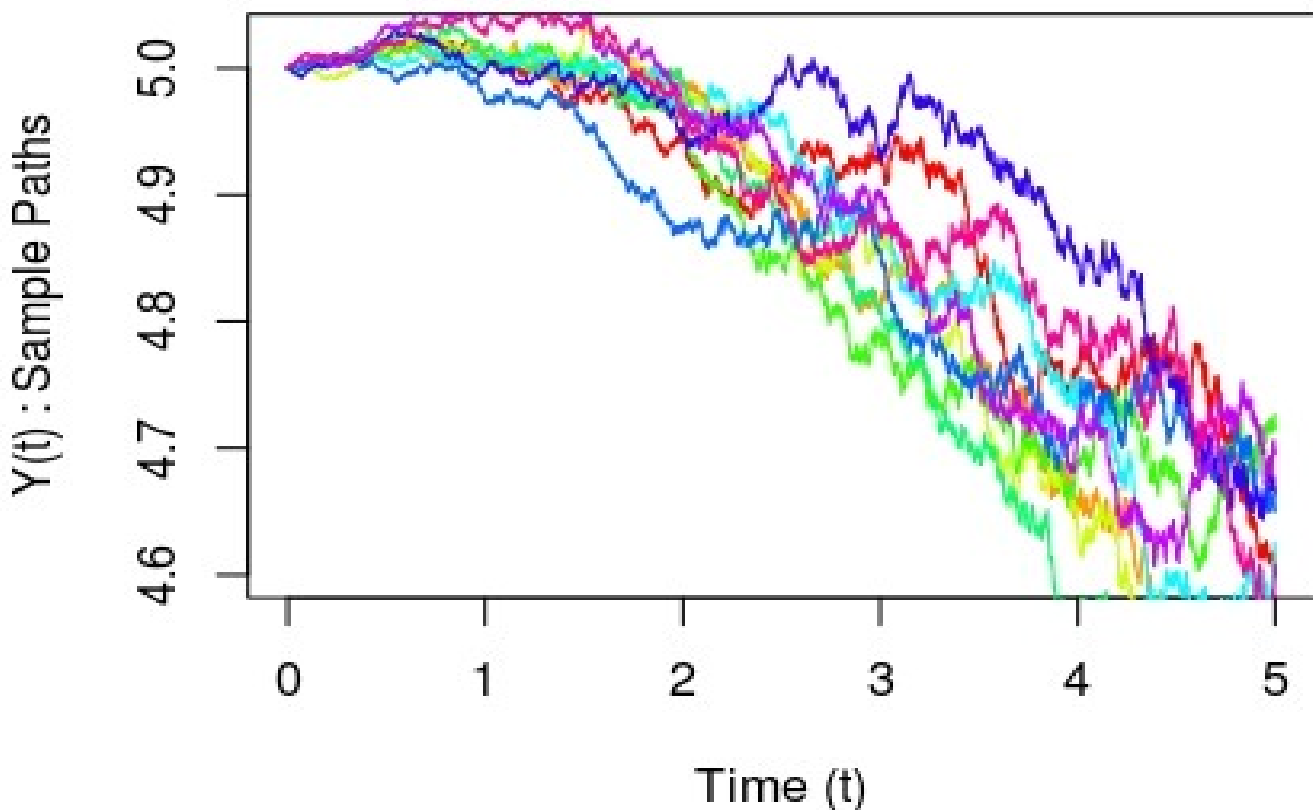
Generated Sample paths of Brownian motion ($\text{BM}(\mu, \sigma^2)$)

◆ Question 3

10 sample paths for the Brownian motion $Y \sim (\text{BM}(\mu, \sigma^2))$ in the time interval $[0, 5]$ were generated using $Y(0)=5$, $\mu(t) = 0.0325 - 0.05t$, $\sigma(t) = 0.012 + 0.0138t + 0.00125t^2$ and Euler's approximations and following values were obtained in one of the sample run of the program :

$$\text{Exp}[Y(2)] = 4.957307$$

$$\text{Exp}[Y(5)] = 4.581593$$



Generated Sample paths of Brownian motion ($\text{BM}(\mu, \sigma^2)$)