

Every surface of an object receives a certain amount of radiations, this flux we call to be the Incident radiation. If we consider the surface  $d_i$  be a diffuse surface, the Incident radiation  $G$  correspond to:

$$G = \pi I_i$$

The incident radiation on a surface then splits in three parts: one is absorbed, one is reflected and one is transmitted. So every surface has specific proprieties called absorptivity, reflectivity and transmissivity. They all derive from the Incident radiation following those formulas:

$$\text{Absorptivity} = \frac{\text{Absorbed radiation}}{\text{Incident radiation}} = \frac{G_{abs}}{G}$$

$$\text{Reflectivity} = \frac{\text{Reflected radiation}}{\text{Incident radiation}} = \frac{G_{ref}}{G}$$

$$\text{Transmissivity} = \frac{\text{Transmitted radiation}}{\text{Incident radiation}} = \frac{G_{tr}}{G}$$

A black body is an idealized body that does not transmit any part of the incoming radiation. For studying the radiative proprieties of objects, its useful compare them to a black body, which is a perfect absorber/emitter of energy.

Emissivity is quantity that makes a straight comparison and state how much a surface behaves closely to a black body. More precisely Emissivity means the ratio of the radiation emitted by the surface at a given temperature to the radiation emitted by a blackbody at the same temperature. We assume the emissivity of a black body is  $\epsilon = 1$  while in a real surface is  $0 < \epsilon < 1$ .

The emissivity of a surface varies also with direction and wavelength. A diffuse surface is an idealized surface where the emissivity doesn't depend on the direction. The emissivity of a surface at a specified wavelength is called spectral emissivity ( $\epsilon_\lambda$ ) The emissivity in a specified direction is called directional emissivity ( $\epsilon_\theta$ )

There is a relationship between the absorptivity ( $\alpha$ ) and emissivity ( $\epsilon$ ): the **Kirchhoff's Law** says: the total hemispherical emissivity of a surface at temperature  $T$  is equal to its total hemispherical absorptivity for radiation coming from a blackbody at the same temperature.

$$G_{abs} = \alpha G = \alpha \sigma T^4 = E_{emit} = \epsilon \sigma T^4$$

The transmission of energy between two surfaces depends on their proprieties, the temperatures the view factor. The view factor is a quantity that describes only the geometrical condition of the two surfaces: it depends on their Areas, their distances and orientation.

$$F_{12} = F_{A_1 \rightarrow A_2} = \frac{\dot{Q}_{A_1 \rightarrow A_2}}{\dot{Q}_{A_1}} = \frac{1}{A_1} \int_{A_2} \int_{A_1} \frac{\cos \theta_1 \cos \theta_2}{\pi r^2} dA_1 dA_2$$

The reciprocity law says that the view factor doesn't change whether it is considered from the surface 1 to surface 2 or from surface 2 to surface 1

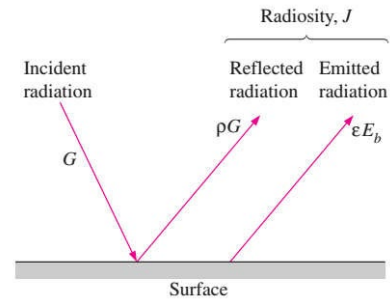
$$A_1 F_{12} = A_2 F_{21}$$

The heat exchange between two black surfaces ( $\epsilon = 1$ ) is given by the difference between the radiation leaving the entire surface 1 to the surface 2 and the radiation leaving all the surface 2 to the surface 1.

$$\dot{Q}_{1 \rightarrow 2} = A_1 E_{b1} F_{1-2} - A_{21} E_{b2} F_{2-1} \quad \text{With the reciprocity law: } \dot{Q}_{1 \rightarrow 2} = A_1 F_{12} \sigma (T_1^4 - T_2^4)$$

The heat exchange between two diffuse gray surfaces is given by the difference between the radiosity leaving the surface one and the radiosity leaving the surface 2

$$\dot{Q}_i = A_i \left( J_i - \frac{J_i - \epsilon_i E_{bi}}{1 - \epsilon_i} \right) = \frac{A_i \epsilon_i}{1 - \epsilon_i} (E_{bi} - J_i)$$



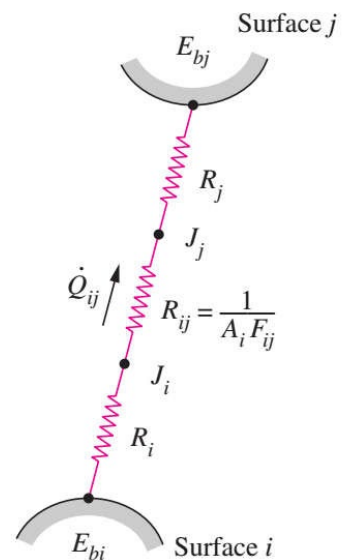
Where we know that  $J_i = \epsilon_i E_{bi} + (1 - \epsilon_i) G_{bi}$

Electric analogy: The heat transfer between two surfaces can be seen as a succession of different resistances.

$$\dot{Q}_{1 \rightarrow 2} = A_1 J_1 F_{1-2} - A_2 J_2 F_{2-1}$$

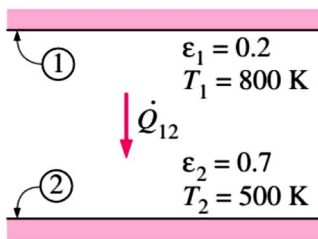
$$\dot{Q}_{i \rightarrow j} = \frac{J_i - J_j}{R_{i \rightarrow j}}$$

$$R_{i \rightarrow j} = \frac{1}{A_i F_{i \rightarrow j}}$$



### **Exercise:**

Calculate the heat exchange between the two parallel plates:



$$\dot{Q}_{12} = \frac{A\sigma(T_1^4 - T_2^4)}{\frac{1}{\epsilon_1} + \frac{1}{\epsilon_2} - 1}$$

$$\dot{Q}_{12} = A \frac{5.670 \cdot 10^{-8} \cdot (800^4 - 500^4)}{\frac{1}{0.2} + \frac{1}{0.7} - 1} = A \frac{19680,57}{5.4286} = \mathbf{3625,35 \times A \quad [W]}$$

With the two emissivities of the plates are 0.1:

$$\dot{Q}_{12} = A \times \frac{5.670 \cdot 10^{-8} \cdot (800^4 - 500^4)}{\frac{1}{0.1} + \frac{1}{0.1} - 1} = A \times \frac{19680,57}{19} = \mathbf{1035,82 \times A \quad [W]}$$

With the same area and variation of temperature, increasing the emissivity it also increases the heat exchange between the two parallel plates