Multilevel Structure

true

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Contents

1 Call The Libraries

```r
library(ggplot2) # beautiful graphs

# library(gganimate) # animated ggplots

library(lme4) # MLM

# library(pander) # nice tables

library(sjPlot) # nice tables for MLM
```

2 Simulate Some Data

```r
e <- rnorm(10, 0, 1) # error

# group 1

group1 <- rep(1, 10)

x1 <- seq(1,10)
```

```r
y1 <- 10 + -1 * x1 + e

# group 2

group2 <- rep(2, 10)

x2 <- seq(11, 20)

y2 <- 30 + -1 * x2 + e

# group 3

group3 <- rep(3, 10)

x3 <- seq(21, 30)

y3 <- 50 + -1 * x3 + e

# combine into a dataframe

x <- c(x1, x2, x3)

y <- c(y1, y2, y3)

group <- factor(c(group1, group2, group3))

mydata <- data.frame(x, y, group)
```

3 Graphs

3.1 A "Naive" Graph

This "naive" graph is unaware of the grouped nature of the data.
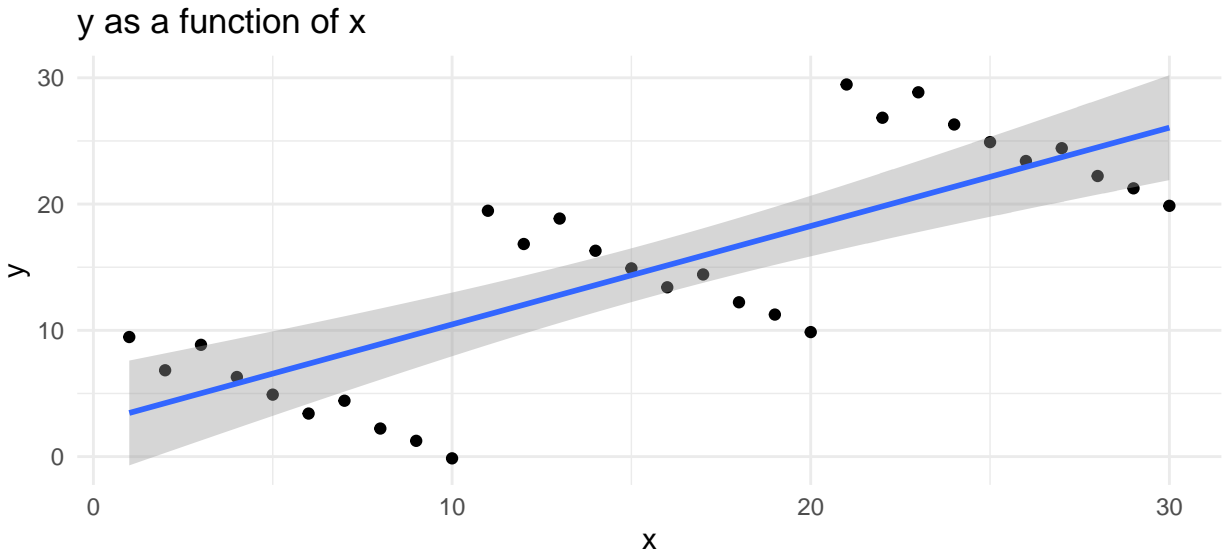
```r
library(ggplot2)

p0 <- ggplot(mydata,
             aes(x = x,
                 y = y)) +
  geom_point() +
  geom_smooth(method = "lm") +
  labs(title = "y as a function of x") +
  theme_minimal()

p0 # replay
```
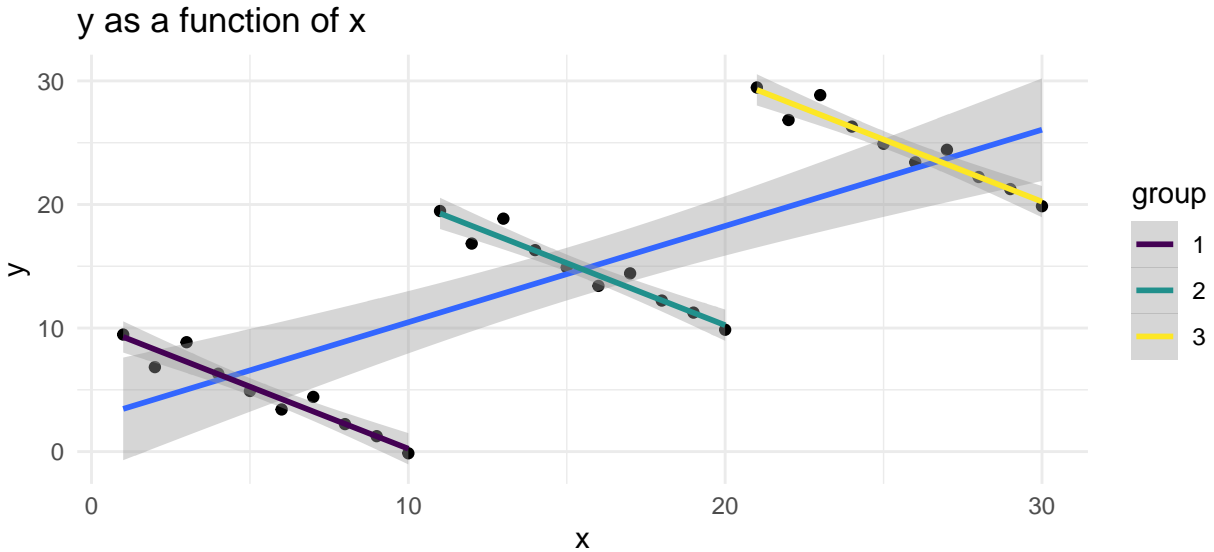
y as a function of x

3.2 An "Aware" Graph

This "aware" graph is aware of the grouped nature of the data.

```
p0 + geom_smooth(aes(color = group), method = "lm") + scale_color_viridis_d()
```


y as a function of x

4 Regressions

4.1 OLS

The OLS model with only x as a covariate is not aware of the grouped structure of the data, and the coefficient for x reflects this.

```r
myOLS <- lm(y ~ x, data = mydata)

sjPlot::tab_model(myOLS,
                  show.se = TRUE,
                  show.ci = FALSE,
                  show.stat = TRUE)
```

y

Predictors

Estimates

std. Error

Statistic

p

(Intercept)

2.68

2.13

1.26

0.219

x

0.78

0.12

6.49

<0.001

Observations

30

R2 / R2 adjusted

0.601 / 0.587

4.2 MLM

The multilevel model is aware of the grouped structure of the data, and the coefficient for x reflects this.

```r
myMLM <- lmer(y ~ x + (1 | group), data = mydata)

sjPlot::tab_model(myMLM,
                  show.se = TRUE,
                  show.ci = FALSE,
                  show.stat = TRUE)
```

y				
Predictors	Estimates	std. Error	Statistic	p
(Intercept)	30.29	11.60	2.61	0.015
x	-1.00	0.06	-17.59	<0.001

Random Effects	
σ²	0.80
τ₀₀ group	401.07
ICC	1.00
N group	3
Observations	30
Marginal R2 / Conditional R2	0.162 / 0.998