Multilevel Models, Equations, Syntax & English

true

2022-12-29

| model | equation | Stata | English |
|---|---|---|--|
| Intercept Only | $y = \beta_0 + e_{ij}$ | mixed y | We estimated the mean of [outcome] |
| $ \begin{array}{c} \text{Intercept Independent} \\ \text{Variable(s)} \end{array} $ | $y = \beta_0 + \beta_1 x + e_{ij} \ y = \beta_0 + \beta_1 x + \beta_2 z + e_{ij}$ | mixed y x mixed y x z | We estimated the relationship of [independent variable(s)] with [outcome] |
| Intercept Random variation of the intercept | $y = \beta_0 + e_{ij} + u_{0j}$ | mixed y groupid: | We estimated the mean of [outcome]. We allowed the intercept of the model to vary by [groupid]. |
| Unconditional intraclass correlation coefficient (ICC) | $\frac{var(u_{0j})}{var(u_{0j}) + var(e_{ij})}$ | mixed y groupid: estat icc | XX% of the variation in [outcome] was explained by clustering of participants in [groupid] |
| Intercept Independent variable(s) Random variation of the intercept | $y = \beta_0 + \beta_1 x + e_{ij} + u_{0j} \ y = \beta_0 + \beta_1 x + \beta_2 z + e_{ij} + u_{0j}$ | mixed y x groupid: mixed y x z groupid: | We estimated the relationship of [independent variable(s)] with [outcome]. We allowed the intercept of the model to vary by group. |

| model | equation | Stata | English |
|--|---|------------------------------------|---|
| Intercept Independent variable Random intercept Random slope | $y = \beta_0 + \beta_1 x + e_{ij} + u_{0j} + u_{1j} x$ | mixed y x groupid: x | We estimated the relationship of [independent variable] with [outcome]. We allowed the intercept of the model to vary by group. We also allowed the relationship of [independent variable] with [outcome] to vary by group. |
| We can estimate multilevel models with more than 1 random slope. | $y = \beta_0 + \beta_1 x + \beta_2 z + e_{ij} + u_{0j} + u_{1j} x + u_{2j} z$ | mixed y x z /// groupid: x z | |