Multilevel Multilingual

Multilevel Models in Stata, R and Julia

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1 Multilevel Multilingual

"This curious world which we inhabit is more wonderful than it is convenient..." (Thoreau, 1975)

"Mathematics is my secret. My secret weakness. I feel like a stubborn, helpless fool in the middle of a problem. Trapped and crazed. Also, thrilled." (Schanen, 2021)

1.1 Introduction

Below, I describe the use of Stata (StataCorp, 2023), R (Bates et al., 2015; R Core Team, 2023), and Julia (Bates, 2024; Bezanson et al., 2017) to estimate multilevel models.

All of these software packages can estimate multilevel models and can visualize relationships in the data. However, there are substantial differences between the different packages: Stata is proprietary for cost software, which is very well documented and very intuitive. While it costs money to purchase Stata, the price is often very reasonable for academic and educational use. R is free open source software which is less intuitive, but there are many excellent resources for learning R. There is often a cost associated with purchasing books and other materials for learning R, which sometimes feels like it offsets the fact that R is free. Julia is newer open source software, also free, and ostensibly much faster than either Stata or R, which may be an important advantage when running multilevel models with very large data sets. At this point in time, both Stata and R feel much more stable than Julia which is still evolving software.

While any of these software packages can be used for learning and estimating multilevel models, I will offer my own opinion—based upon 15 years of teaching multilevel models at the doctoral level—that Stata offers the quickest pathway for learning the basic and advanced uses of multilevel models. I also believe the intuitive nature of Stata syntax contributes to accurate and replicable work in this area.

Table 1.1: Software for Multilevel Modeling

Software	Cost	Ease of Use
Stata	some cost	learning curve, but very intuitive for both multilevel modeling and graphing.

Software	Cost	Ease of Use
R	free	learning curve: intuitive for multilevel modeling; but steeper learning curve for graphing (ggplot).
Julia	free	steep learning curve in general: steep learning curve for multilevel modeling; and very steep learning curve for graphing. Graphics libraries are very much under development and in flux.

Results Will Vary Somewhat

Estimating multilevel models is a complex endeavor. The software details of how this is accomplished are beyond the purview of this book. Suffice it to say that across different software packages there will be differences in estimation routines, resulting in some numerical differences in the results provided by different software packages. Substantively speaking, however, results should agree across software.

Multi-Line Commands

Sometimes I have written commands out over multiple lines. I have done this for especially long commands, but have also sometimes done this simply for the sake of clarity. The different software packages have different approaches to multi-line commands.

- 1. By default, Stata ends a command at the end of a line. If you are going to write a multi-line command you should use the /// line continuation characters.
- 2. R is the software that most naturally can be written using multiple lines, as R commands are usually clearly encased in parentheses (()) or continued with + signs.
- 3. Like Stata, Julia expects commands to end at the end of a line. If you are going to write a mult-line command, all commands except for the last line should end in a character that clearly indicates continuation, like a + sign. An alternative is to encase the entire Julia command in an outer set of parentheses (()).

Running Statistical Packages in Quarto

I used Quarto (Allaire et al., 2024) (https://quarto.org/) to create this Appendix. Quarto is a programming and publishing environment that can run multiple programming languages, including Stata, R and Julia, and that can write to multiple output formats including HTML, PDF, and MS Word. To run Stata, I used the Statamarkdown library (Hemken, 2023) in R to connect Stata to Quarto. Quarto has a built in connection to R, and runs R without issue. To run Julia, I used the $\tt JuliaCall$ library (Li, 2019) in R to connect Quarto to Julia.

Of course, each of these programs can be run by itself, if you have them installed on your computer.

1.2 The Data

i Datasets

The examples use the simulated_multilevel_data.dta and simulated_multilevel_longitudinal_data.dta files.

Here is a direct link to download the cross-sectional data.

Here is a direct link to download the longitudinal data.

Table 1.2: Sample of Simulated Multilevel Data

Table 1.2: Table continues below

country	HDI	family	id	identity	intervention	physical_punishment
1	69	1	1.1	1	0	3
1	69	2	1.2	1	1	2
1	69	3	1.3	0	1	3
1	69	4	1.4	1	0	0
1	69	5	1.5	1	0	4
1	69	6	1.6	0	1	5

Table 1.3: Sample of Simulated Multilevel Data

warmth	outcome
3	57.47
1	50.1
2	52.92
5	60.17
4	55.05
3	49.81

1.3 An Introduction To Equations and Syntax

To explain statistical syntax for each software, I consider the general case of a multilevel model with dependent variable y, independent variables x and z, clustering variable group, and a random slope for x. i is the index for the person, while j is the index for the group.

$$y = \beta_0 + \beta_1 x_{ij} + \beta_2 z_{ij} + u_{0j} + u_{1j} \times x_{ij} + e_{ij}$$
(1.1)

1.3.1 Stata

In Stata mixed, the syntax for a multilevel model of the form described in Equation 1.1 is:

```
mixed y x z || group: x
```

1.3.2 R

In R lme4, the syntax for a multilevel model of the form described in Equation 1.1 is:

```
library(lme4)

lmer(y ~ x + z + (1 + x || group), data = ...)
```

1.3.3 Julia

In Julia MixedModels, the syntax for a multilevel model of the form described in Equation 1.1 is:

```
using MixedModels
fit(MixedModel, @formula(y ~ x + z + (1 + x | group)), data)
```

2 Statistical Workflows

2.1 Statistical Software Is Best Run Using a Script

Many statistical workflows—whatever the statistical package being used—follow the same conceptual pattern.

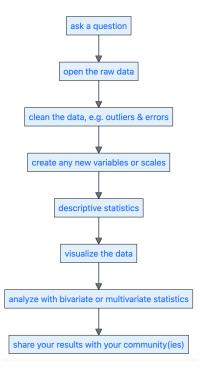


Figure 2.1: A Common Statistical Workflow

Increasingly, we want to think about workflows that are

- documentable, transparent, and auditable: We have a record of what we did if we want to double check our work, clarify a result, or develop a new project with a similar process. We, or others, can find the inevitable errors in our work, and correct them.
- replicable: Others can replicate our findings with the same or new data.

• scalable: We are developing a process that can be as easily used with thousands or millions of rows of data as it can with ten rows of data. We are developing a process that can be easily repeated if we are constantly getting new or updated data, e.g. getting new data every week, or every month.

2.2 Scripts

For most statistical workflows, we will often want to write a script or code. Data analysis scripts can be stored in a Quarto document (Allaire et al., 2024) as they are in this Appendix, or every statistical package has its own unique format for storing scripts as a text file: in Stata, scripts are stored in .do files; in R, scripts are stored in .R files, and in Julia, scripts are stored in .jl files.

2.3 Script Flow

A good practice when writing a script, is to have a script that begins with the raw data, moves through any necessary re-coding or cleaning of the data, generates descriptive statistics, generates the appropriate multivariate results, and then generates any necessary visualizations.

2.4 Storing Statistical Data

It is usually best to store quantitative data in a statistical format such as R (.Rdata), or Stata (.dta), or even a text format such as .csv. Spreadsheets are likely to be a bad tool for storing quantitative data.

2.5 It Is Possible To Use Multiple Statistical Packages

While this Appendix focuses on the use of each individual statistical package on its own, it is certainly possible to use multiple statistical packages as part of the same workflow. For example, one might employ Stata to carry out data management tasks, and then possibly use R to run a multilevel model with a more complicated multilevel structure, such as a cross-classified model, or Julia to more quickly run a model with a large data.

2.6 Good Statistical Workflows Require Safe Workspaces

It is also *very important* to be aware that good complex workflows are *highly iterative* and *highly collaborative*. Good complex workflows require a *safe workspace* in which team members feel free to admit their own errors, and help with others' mistakes in a non-judgmental fashion. Such a *safe environment* is necessary to build an environment where the *overall error rate* is low.

2.7 Good Statistical Workflows Require Patience And Can Be Psychologically Demanding

Developing a good documented and auditable workflow that is implemented in code requires a lot of patience, and often, **many iterations**. Working through these many iterations can be psychologically demanding. It is important to remember that careful attention to getting the details right early in the research process, while sometimes tiring and frustrating, will pay large dividends later on when the research is reviewed, presented, published and read.

3 Descriptive Statistics

3.1 Descriptive Statistics

3.1.1 Stata

```
use simulated_multilevel_data.dta // use data
```

We use summarize for *continuous* variables, and tabulate for *categorical* variables.

```
summarize outcome warmth physical_punishment HDI
tabulate identity
tabulate intervention
```

Variable	0bs	Mean	Std. dev.	Min	Max
outcome	3,000	52.43327	6.530996	29.60798	74.83553
warmth	3,000	3.521667	1.888399	0	7
physical_p~t	3,000	2.478667	1.360942	0	5
HDI	3,000	64.76667	17.24562	33	87

hypothetica l identity group variable	Freq.	Percent	Cum.
0 1	1,507 1,493	50.23 49.77	50.23
Total	3.000	100.00	

recieved				
interventio				
n	 +	Freq.	Percent	Cum.
0		1,547	51.57	51.57
1		1,453	48.43	100.00
Total	+ 	3,000	100.00	

3.1.2 R

```
library(haven) # read data in Stata format

df <- read_dta("simulated_multilevel_data.dta")</pre>
```

R's descriptive statistics functions rely heavily on whether a variable is a *numeric* variable, or a *factor* variable. Below, I convert two variables to factors (factor) before using summary¹ to generate descriptive statistics.

```
df$country <- factor(df$country)

df$identity <- factor(df$identity)

df$intervention <- factor(df$intervention)

summary(df)</pre>
```

country	HDI	family	id	identity
1 : 100	Min. :33.00	Min. : 1.00	Length:3000	0:1507
2 : 100	1st Qu.:53.00	1st Qu.: 25.75	Class :character	1:1493
3 : 100	Median :70.00	Median : 50.50	Mode :character	
4 : 100	Mean :64.77	Mean : 50.50		
5 : 100	3rd Qu.:81.00	3rd Qu.: 75.25		
6 : 100	Max. :87.00	Max. :100.00		
(Other):2400				
intervention	physical_punishme	ent warmth	outcome	
0:1547	Min. :0.000	Min. :0.000	Min. :29.61	
1:1453	1st Qu.:2.000	1st Qu.:2.000	1st Qu.:48.02	

¹skimr is an excellent new alternative library for generating descriptive statistics in R.

```
Median :2.000Median :4.000Median :52.45Mean :2.479Mean :3.522Mean :52.433rd Qu.:3.0003rd Qu.:5.0003rd Qu.:56.86Max. :5.000Max. :7.000Max. :74.84
```

3.1.3 Julia

```
using Tables, MixedModels, MixedModelsExtras, StatFiles, DataFrames, CategoricalArrays, Data
df = DataFrame(load("simulated_multilevel_data.dta"))
```

Similarly to R, Julia relies on the idea of variable type. I use transform to convert the appropriate variables to categorical variables.

```
@transform!(df, :country = categorical(:country))
@transform!(df, :identity = categorical(:identity))
@transform!(df, :intervention = categorical(:intervention))
```

```
describe(df) # descriptive statistics
```

9×7 Da	9×7 DataFrame						
Row	variable	mean	min	median	max	nmissing	eltype
	Symbol	Union	Any	Union	Any	Int64	Union
1	country		1.0		30.0	0	Union{
2	HDI	64.7667	33.0	70.0	87.0	0	Union{
3	family	50.5	1.0	50.5	100.0	0	Union{
4	id		1.1		9.99	0	Union{
5	identity		0.0		1.0	0	Union{
6	intervention		0.0		1.0	0	Union{
7	physical_punishment	2.47867	0.0	2.0	5.0	0	Union{
8	warmth	3.52167	0.0	4.0	7.0	0	Union{
9	outcome	52.4333	29.608	52.449	74.8355	0	Union{
						1 colum	n omitted

3.2 Interpretation

Examining descriptive statistics is an important first step in any analysis. It is important to examine your descriptive statistics before skipping ahead to more sophisticated analyses, such as multilevel models.

In examining the descriptive statistics for this data, we get a sense of the data.

- outcome has a mean of approximately 52 and ranges from approximately 30 to 75.
- warmth and physical punishment are both variables that represent the number of times that parents use each of these forms of discipline in a week. The average of the former is about 3.5, while the average of the latter is about 2.5.
- HDI, the Human Development Index has an average of about 65, and a wide range.
- identity is a categorical variable for a hypothetical identity group, and has values of 0 and 1.
- intervention is also a categorical variable, and has values of 0 and 1.

4 Unconditional Models

4.1 Two Level Model

An *unconditional* multilevel model is a model with no independent variables. One should always run an unconditional model as the first step of a multilevel model in order to get a sense of the way that variation is apportioned in the model across the different levels.

4.1.1 The Equation

$$outcome_{ij} = \beta_0 + u_{0j} + e_{ij} \tag{4.1}$$

The Intraclass Correlation Coefficient (ICC) is given by:

$$ICC = \frac{var(u_{0j})}{var(u_{0j}) + var(e_{ij})}$$

$$\tag{4.2}$$

In a two level multilevel model, the ICC provides a measure of the proportion of variation attributable to Level 2.

4.1.2 Run Models

4.1.2.1 Stata

```
use simulated_multilevel_data.dta // use data
mixed outcome || country: // unconditional model
estat icc // ICC
```

Performing gradient-based optimization: Iteration 0: Log likelihood = -9802.8371 Iteration 1: Log likelihood = -9802.8371 Computing standard errors ... Mixed-effects ML regression Number of obs = 3,000Group variable: country Number of groups = 30 Obs per group: min = 100avg = 100.0max = 100Wald chi2(0) Log likelihood = -9802.8371Prob > chi2 outcome | Coefficient Std. err. z P>|z| [95% conf. interval] ______ _cons | 52.43327 .3451217 151.93 0.000 51.75685 Random-effects parameters | Estimate Std. err. [95% conf. interval] ______ country: Identity var(_cons) | 3.178658 .9226737 1.799552 5.614658 ______ var(Residual) | 39.46106 1.024013 37.50421 _____ LR test vs. linear model: chibar2(01) = 166.31 Prob >= chibar2 = 0.0000 Intraclass correlation -----Level | ICC Std. err. [95% conf. interval] ----country | .0745469 .0201254 .0434963 .1248696

Performing EM optimization ...

4.1.2.2 R

```
library(haven)
df <- read_dta("simulated_multilevel_data.dta")</pre>
library(lme4) # estimate multilevel models
fit0 <- lmer(outcome ~ (1 | country),</pre>
            data = df) # unconditional model
summary(fit0)
Linear mixed model fit by REML ['lmerMod']
Formula: outcome ~ (1 | country)
  Data: df
REML criterion at convergence: 19605.9
Scaled residuals:
   Min 1Q Median
                           3Q
                                   Max
-3.3844 -0.6655 -0.0086 0.6725 3.6626
Random effects:
 Groups Name
                     Variance Std.Dev.
 country (Intercept) 3.302 1.817
 Residual
                     39.461
                              6.282
Number of obs: 3000, groups: country, 30
Fixed effects:
           Estimate Std. Error t value
(Intercept) 52.433 0.351 149.4
library(performance)
performance::icc(fit0) # ICC
# Intraclass Correlation Coefficient
    Adjusted ICC: 0.077
```

Unadjusted ICC: 0.077

4.1.2.3 Julia

```
using Tables, MixedModels, MixedModelsExtras,
StatFiles, DataFrames, CategoricalArrays, DataFramesMeta
df = DataFrame(load("simulated_multilevel_data.dta"))
@transform!(df, :country = categorical(:country))
m0 = fit(MixedModel,
         @formula(outcome ~ (1 | country)), df) # unconditional model
Linear mixed model fit by maximum likelihood
 outcome ~ 1 + (1 | country)
          -2 logLik
                          AIC
                                    AICc
                                                BIC
   logLik
 -9802.8371 19605.6742 19611.6742 19611.6822 19629.6933
Variance components:
            Column
                     Variance Std.Dev.
country
         (Intercept)
                       3.17863 1.78287
Residual
                      39.46106 6.28180
 Number of obs: 3000; levels of grouping factors: 30
 Fixed-effects parameters:
               Coef. Std. Error
                                       z Pr(>|z|)
(Intercept) 52.4333
                        0.345121 151.93
                                            <1e-99
icc(m0) # ICC
```

```
0.07454637475695493
```

4.1.3 Interpretation

In each case, the software finds that nearly 8% of the variation in the outcome is explainable by the clustering of the observations in each country.

4.2 Three Level Model

4.2.1 The Equation

$$outcome_{ij} = \beta_0 + u_{0j} + v_{0i} + e_{ij}$$
 (4.3)

As discussed in the main text, in a three level model, there are two intraclass correlation coefficients (StataCorp, 2023). The formulas for the Intraclass Correlation Coefficient (ICC) are given by (StataCorp, 2023):

$$ICC = \frac{var(u_{0j})}{var(u_{0j}) + var(v_{0i}) + var(e_{ij})}$$

$$(4.4)$$

Following StataCorp (2023), Equation 4.4 is the correlation of responses for person-timepoints from the same country but different persons.

$$ICC = \frac{var(u_{0j}) + var(v_{0i})}{var(u_{0j}) + var(v_{0i}) + var(e_{ij})}$$
(4.5)

Again, closely following StataCorp (2023), Equation 4.5 is the correlation of responses for person-timepoints from the same country and same person.

4.2.2 Run Models

4.2.2.1 Stata

```
use simulated_multilevel_longitudinal_data.dta // use data
mixed outcome || country: || id: // unconditional model
estat icc // ICC
```

Performing EM optimization ...

Performing gradient-based optimization: Iteration 0: Log likelihood = -29058.266 Iteration 1: Log likelihood = -29058.259 Iteration 2: Log likelihood = -29058.259

${\tt Mixed-effects}\ {\tt ML}\ {\tt regression}$

Number of obs = 9,000

Grouping information

Group variable	 	No. of groups	Obser Minimum	vations per Average	group Maximum
country id	 	30 3,000	300 3	300.0	300

Random-effects parameters | Estimate Std. err. [95% conf. interval]

country: Identity | var(_cons) | 3.232092 .8891367 1.885043 5.54174

id: Identity | var(_cons) | 11.72403 .5747501 10.64996 12.90641

Note: LR test is conservative and provided only for reference.

Intraclass correlation

Level | ICC Std. err. [95% conf. interval]

country | .0748336 .0190847 .0450028 .1219141 id|country | .3462837 .0171461 .3134867 .3806097

4.2.2.2 R

In R, the ICC for a three level model is easiest to estimate "by hand".

```
library(haven)
dfL <- read_dta("simulated_multilevel_longitudinal_data.dta")</pre>
library(lme4) # estimate multilevel models
fit0L <- lmer(outcome ~ (1 | country/id),</pre>
            data = dfL) # unconditional model
summary(fit0L)
Linear mixed model fit by REML ['lmerMod']
Formula: outcome ~ (1 | country/id)
  Data: dfL
REML criterion at convergence: 58116.8
Scaled residuals:
            1Q Median 3Q
                                   Max
-3.7858 -0.6059 -0.0062 0.6017 3.4348
Random effects:
 Groups
        Name Variance Std.Dev.
 id:country (Intercept) 11.724 3.424
 country (Intercept) 3.351 1.830
 Residual
                       28.234 5.314
Number of obs: 9000, groups: id:country, 3000; country, 30
Fixed effects:
           Estimate Std. Error t value
(Intercept) 53.3777 0.3446 154.9
```

```
3.351 / (11.724 + 3.351 + 28.234)
[1] 0.07737422
(3.351 + 11.724) / (11.724 + 3.351 + 28.234)
[1] 0.3480801
4.2.2.3 Julia
In Julia, the ICC for a three level model is also easiest to estimate "by hand".
using Tables, MixedModels, StatFiles, DataFrames, CategoricalArrays, DataFramesMeta
dfL = DataFrame(load("simulated_multilevel_longitudinal_data.dta"))
@transform!(dfL, :country = categorical(:country))
mOL = fit(MixedModel, @formula(outcome ~
                                  (1 | country) +
                                  (1 | id)), dfL)
Linear mixed model fit by maximum likelihood
 outcome ~ 1 + (1 | country) + (1 | id)
    logLik
             -2 logLik
                            AIC
                                         AICc
                                                     BIC
 -29058.2592 58116.5184 58124.5184 58124.5229 58152.9384
Variance components:
            Column
                     Variance Std.Dev.
id
         (Intercept) 11.72401 3.42403
country (Intercept)
                       3.23190 1.79775
Residual
                      28.23426 5.31359
 Number of obs: 9000; levels of grouping factors: 3000, 30
  Fixed-effects parameters:
               Coef. Std. Error
                                        z Pr(>|z|)
```

<1e-99

0.338785 157.56

(Intercept) 53.3777

```
3.23190 / (11.72401 + 3.23190 + 28.23426)
```

0.07482952718176382

```
(3.23190 + 11.72401) / (11.72401 + 3.23190 + 28.23426)
```

0.34628041519632824

4.2.3 Interpretation

Each software suggests that almost 8% of the variation in the outcome is within time points for different individuals within the same country, while almost 35% of the variation in the outcome is within time points for the same individual within the same country.

5 Cross Sectional Multilevel Models

5.1 The Equation

Recall the general model of Equation 1.1, and the syntax outlined in Section 1.3. Below in Equation 5.1, we consider a more substantive example.

$$outcome_{ij} = \beta_0 + \beta_1 warmth_{ij} +$$
(5.1)

 β_2 physical punishment_{ij}+

$$\beta_3 \mathrm{identity}_{ij} + \beta_4 \mathrm{intervention}_{ij} + \beta_5 \mathrm{HDI}_j +$$

$$u_{0j} + u_{1j} \times \text{warmth}_{ij} + e_{ij}$$

5.2 Correlated and Uncorrelated Random Effects

Consider the covariance matrix of random effects (e.g. u_{0j} and u_{1j}). In Equation 5.2 the covariances of the random effects are constrained to be zero.

$$\begin{bmatrix} var(u_{0j}) & 0\\ 0 & var(u_{1j}) \end{bmatrix}$$
 (5.2)

As discussed in the Chapter on multilevel models with cross-sectional data, however, one can consider a multilevel model in which the random effects are correlated, as is the case in Equation 5.3.

$$\begin{bmatrix} var(u_{0j}) & cov(u_{0j}, u_{1j}) \\ cov(u_{0j}, u_{1j}) & var(u_{1j}) \end{bmatrix}$$

$$(5.3)$$

Procedures for estimating models with uncorrelated and correlated random effects are detailed below (Bates et al., 2015; Bates, 2024; StataCorp, 2023).

Table 5.1: Correlated and Uncorrelated Random Effects

Software	Uncorrelated Random Effects	Correlated Random Effects
Stata R	default separate random effects from grouping variable with	add option: , cov(uns) separate random effects from grouping variable with
Julia	separate terms for each random effect e.g. (1 group) + (0 + x group)	separate random effects from grouping variable with .

All models in the examples below are run with uncorrelated random effects, but could just as easily be run with *correlated* random effects.

5.3 Run Models



△ Continuous and Categorical Variables

Statistically-as noted in the main text-it is important to be clear on whether independent variables in one's model are continuous or categorical. Continuous variables can be entered straightforwardly into statistical syntax. Categorical variables, on the other hand usually require specific attention in statistical software. In Stata, categorical variables are indicated in a statistical model by prefixing them with an i.. In R, categorical variables are distinguished by making them into factors e.g. x <- factor(x). In Julia, categorical variables are created by using the Otransform syntax detailed below.

5.3.1 Stata

5.3.1.1 Get The Data

use simulated_multilevel_data.dta

5.3.1.2 Run The Model

mixed outcome warmth physical_punishment i.identity i.intervention HDI $\mid\mid$ /// country: warmth

Performing EM optimization ...

 ${\tt Performing\ gradient-based\ optimization:}$

Iteration 0: Log likelihood = -9626.6279
Iteration 1: Log likelihood = -9626.607
Iteration 2: Log likelihood = -9626.607

Computing standard errors ...

Mixed-effects ML regression

Group variable: country

Number of obs = 3,000

Number of groups = 30

Obs per group:

min = 100 avg = 100.0

max = 100 Wald chi2(5) = 334.14

Log likelihood = -9626.607 Prob > chi2 = 0.0000

 outcome
 Coefficient
 Std. err.
 z
 P>|z|
 [95% conf. interval]

 warmth
 .8345368
 .0637213
 13.10
 0.000
 .7096453
 .9594282

 physical_punishment
 -.9916657
 .0797906
 -12.43
 0.000
 -1.148052
 -.8352791

 1.identity
 -.3004767
 .2170295
 -1.38
 0.166
 -.7258466
 .1248933

 1.intervention
 .6396427
 .2174519
 2.94
 0.003
 .2134448
 1.065841

 HDI
 -.003228
 .0199257
 -0.16
 0.871
 -.0422817
 .0358256

 _cons
 51.99991
 1.371257
 37.92
 0.000
 49.3123
 54.68753

Random-effects parameters | Estimate Std. err. [95% conf. interval]

country: Independent | var(warmth) | .0227504 .0257784 .0024689 .2096436

var(_cons) | 2.963975 .9737647 1.556777 5.643163

var(Residual) | 34.97499 .9097109 33.23668 36.80422

LR test vs. linear model: chi2(2) = 205.74

Prob > chi2 = 0.0000

Note: LR test is conservative and provided only for reference.

5.3.2 R

5.3.2.1 Get The Data

```
library(haven)
df <- read_dta("simulated_multilevel_data.dta")</pre>
```

5.3.2.2 Change Some Variables To Categorical

```
df$identity <- factor(df$identity)</pre>
df$intervention <- factor(df$intervention)</pre>
```

5.3.2.3 Run The Model



Caution

lme4 does not directly provide p values in results, because of some disagreement over exactly how these p values should be calculated. Therefore, in this Appendix, I also call library lmerTest to provide p values for lme4 results.



? Tip

R prefers to use scientific notation when possible. I find that the use of scientific notation can be confusing in reading results. I turn off scientific notation by setting a penalty for its use: options(scipen = 999).

```
library(lme4)
library(lmerTest)
```

```
options(scipen = 999)
fit1 <- lmer(outcome ~ warmth + physical_punishment +</pre>
              identity + intervention + HDI +
               (1 + warmth || country),
            data = df
summary(fit1)
Linear mixed model fit by REML. t-tests use Satterthwaite's method [
lmerModLmerTest]
Formula: outcome ~ warmth + physical punishment + identity + intervention +
    HDI + (1 + warmth || country)
  Data: df
REML criterion at convergence: 19268.8
Scaled residuals:
    Min
            1Q Median
                            3Q
                                   Max
-3.9774 -0.6563 0.0186 0.6645 3.6730
Random effects:
 Groups
          Name
                      Variance Std.Dev.
 country
           (Intercept) 3.19120 1.786
 country.1 warmth
                       0.02464 0.157
                      35.01779 5.918
 Residual
Number of obs: 3000, groups: country, 30
Fixed effects:
                      Estimate Std. Error
                                                    df t value
(Intercept)
                     52.011324 1.414976
                                             30.293141 36.758
warmth
                      0.834562 0.064250 41.896457 12.989
physical_punishment -0.991893 0.079845 2968.012381 -12.423
identity1
                     -0.300354 0.217179 2970.108153 -1.383
intervention1
                      0.639060 0.217603 2971.186718 2.937
HDT
                     -0.003394 0.020598
                                             27.592814 -0.165
                               Pr(>|t|)
                   < 0.00000000000000000000 ***
(Intercept)
                    0.00000000000000277 ***
warmth
physical_punishment < 0.000000000000000 ***
```

0.16678

identity1

5.3.3 Julia

5.3.3.1 Get The Data

```
using Tables, MixedModels, StatFiles, DataFrames, CategoricalArrays, DataFramesMeta
df = DataFrame(load("simulated_multilevel_data.dta"))
```

5.3.3.2 Change Some Variables To Categorical

```
@transform!(df, :country = categorical(:country))
@transform!(df, :identity = categorical(:identity))
@transform!(df, :intervention = categorical(:intervention))
```

5.3.3.3 Run The Model

```
Linear mixed model fit by maximum likelihood
outcome ~ 1 + warmth + physical_punishment + identity + intervention + HDI + (1 | country)
logLik -2 logLik AIC AICc BIC
-9626.6070 19253.2140 19271.2140 19271.2742 19325.2713
```

Variance components:

Column Variance Std.Dev. Corr

country (Intercept) 2.963849 1.721583

warmth 0.022756 0.150852

Residual 34.974984 5.913965

Number of obs: 3000; levels of grouping factors: 30

Fixed-effects parameters:

	Coef.	Std. Error	z	Pr(> z)
(Intercept)	51.9999	1.37124	37.92	<1e-99
warmth	0.834537	0.0637228	13.10	<1e-38
physical_punishment	-0.991665	0.0797906	-12.43	<1e-34
identity: 1.0	-0.300475	0.217029	-1.38	0.1662
intervention: 1.0	0.639641	0.217452	2.94	0.0033
HDI	-0.0032286	0.0199255	-0.16	0.8713

5.4 Interpretation

Models suggest that parental warmth is associated with increases in the beneficial outcome, while physical punishment is associated with decreases in the beneficial outcome. The intervention is associated with increases in the outcome. There is insufficient evidence that either identity group or the Human Development Index are associated with the outcome.

6 Longitudinal Multilevel Models

6.1 The Data

The data employed in these examples are a longitudinal extension of the data described in Section 1.2.

6.2 The Equation

outcome
$$_{itj} = \beta_0 + \beta_1$$
parental warmth $_{itj} + \beta_2$ physical punishment $_{itj} + \beta_3$ time $_{itj} +$ (6.1)
$$\beta_4 \text{identity}_{itj} + \beta_5 \text{intervention}_{itj} + \beta_6 \text{HDI}_j +$$

$$u_{0j} + u_{1j} \times \text{parental warmth}_{itj} +$$

$$v_{0ij} + v_{1ij} \times \text{time}_{itj} + e_{itj}$$

6.3 Growth Trajectories

Remember, following the discussion in the main text, that in longitudinal multilevel models, the variable for *time* assumes an important role as we are often thinking of a *growth trajectory* over time.

As discussed in the main text, think about a model where *identity* is a (1/0) variable for membership in one of two groups:

$$\text{outcome} = \beta_0 + \beta_t \\ \text{time} + \beta_{\text{identity}} \\ \text{identity} + \beta_{\text{interaction}} \\ \text{identity} \\ \times \\ \text{time} + u_{0i} + e_{it}$$

Then, each identity group has its own intercept and time trajectory:

Table 6.1: Slope and Intercept for Each Group

Group	Intercept	Slope (Time Trajectory)
0	β_0	eta_t
1	$\beta_0 + \beta_{\text{identity}}$	$eta_t + eta_{ ext{interaction}}$

Main Effects and Interactions

Thus, again following the main text, in longitudinal multilevel models, main effects modify the intercept of the time trajectory, while interactions with time, modify the slope of the time trajectory. Below, we run models with main effects only, then models with main effects, and interactions with time.

6.4 Run Models



Warning

Remember that we are estimating a model in which time points are nested inside families, who are in turn nested inside countries. For each software package, it is accordingly important to specify the way in which different levels of the data are nested. Pay careful attention to the syntax examples below with regard to id and country

6.4.1 Stata

6.4.1.1 Get The Data

use simulated_multilevel_longitudinal_data.dta

6.4.1.2 Run The Models

6.4.1.2.1 Main Effects Only

mixed outcome t warmth physical_punishment i.identity i.intervention HDI || /// country: warmth || id: t

Performing EM optimization ...

Performing gradient-based optimization:

Iteration 0: Log likelihood = -28523.49
Iteration 1: Log likelihood = -28499.987
Iteration 2: Log likelihood = -28499.739
Iteration 3: Log likelihood = -28499.604
Iteration 4: Log likelihood = -28499.603

Computing standard errors ...

 ${\tt Mixed-effects}\ {\tt ML}\ {\tt regression}$

Number of obs = 9,000

Grouping information

	No. of	Obser	vations per	group
Group variable	groups	Minimum	Average	Maximum
country	30	300	300.0	300
id		3	3.0	3

Log likelihood = -28499.603

Wald chi2(6) = 1096.15Prob > chi2 = 0.0000

outcome	Coefficient		z	P> z	[95% conf.	interval]
t	.943864	.0658716	14.33	0.000	.814758	1.07297
warmth	.9134959	.0423732	21.56	0.000	.830446	.9965459
physical_punishment	-1.007897	.0497622	-20.25	0.000	-1.105429	9103647
1.identity	1276926	.1515835	-0.84	0.400	4247908	.1694057
1.intervention	.8589966	.1519095	5.65	0.000	.5612596	1.156734
HDI	0005657	.0196437	-0.03	0.977	0390666	.0379352
_cons	50.46724	1.338318	37.71	0.000	47.84418	53.09029

Random-effects parameters	 	Estimate	Std. err.	[95% conf.	interval]
country: Independent					
<pre>var(warmth)</pre>		.0107586	.0127845	.0010478	.1104703
<pre>var(_cons)</pre>		3.167085	.9146761	1.798154	5.578181

id: Independent | var(t) | 3.58e-09 7.06e-07 3.5e-177 3.7e+159 | var(_cons) | 8.387275 .4724188 7.510631 9.366242 | var(Residual) | 26.02733 .4753701 25.11211 26.97592 | LR test vs. linear model: chi2(4) = 1247.03 | Prob > chi2 = 0.0000

Note: LR test is conservative and provided only for reference.

6.4.1.2.2 Interactions With Time

mixed outcome c.t##(c.warmth c.physical_punishment i.identity i.intervention c.HDI) || count

Performing EM optimization ...

Performing gradient-based optimization:

Iteration 0: Log likelihood = -28522.21
Iteration 1: Log likelihood = -28498.677
Iteration 2: Log likelihood = -28498.468
Iteration 3: Log likelihood = -28498.31
Iteration 4: Log likelihood = -28498.309

Computing standard errors ...

Mixed-effects ML regression

Number of obs = 9,000

Grouping information

Group variable	No. of groups	Obser Minimum	vations per Average	group Maximum
country	30	300 3	300.0	300

Wald chi2(11) = 1100.25Prob > chi2 = 0.0000

Log likelihood = -28498.309

outcome	Coefficient	Std. err.	z	P> z	[95% conf.	interval]
t l	.7582075	.326177	2.32	0.020	.1189123	1.397503
warmth	.8170757	.082662	9.88	0.000	.6550611	.9790903
$physical_punishment \mid$	-1.009031	.1112932	-9.07	0.000	-1.227162	7909007
1.identity $ $	2387167	.3039964	-0.79	0.432	8345387	.3571053
1.intervention $ $.6607606	.3044503	2.17	0.030	.064049	1.257472
HDI	.0013614	.0210842	0.06	0.949	0399628	.0426856
I						
c.t#c.warmth	.0483637	.0356074	1.36	0.174	0214255	.1181529
I						
c.t#						
c.physical_punishment	.0005421	.0494354	0.01	0.991	0963496	.0974338
I						
identity#c.t						
1 I	.0554389	.1317444	0.42	0.674	2027754	.3136532
I						
intervention#c.t						
1	.0992811	. 131925	0.75	0.452	1592872	.3578493
I						
c.t#c.HDI	0009551	.0038216	-0.25	0.803	0084453	.0065352
I						
_cons	50.83632	1.483548	34.27	0.000	47.92862	53.74402

Random-effects parameters	Estimate	Std. err.	[95% conf.	_
country: Independent	l			
var(warmth)	.0106014	.0127458	.0010046	.1118779
var(_cons)		.9153355	1.80009	5.582753
id: Independent				
var(t)	9.47e-10	2.07e-07	1.5e-195	6.0e+176
-	8.39189	.4724106	7.515234	9.370809
var(Residual)		.4751602	25.10101	26.964
LR test vs. linear model: chi	2(4) = 1247.84	4	Prob > chi	2 = 0.0000

Note: LR test is conservative and provided only for reference.

6.4.2 R

6.4.2.1 Get The Data

```
library(haven)
dfL <- read_dta("simulated_multilevel_longitudinal_data.dta")</pre>
```

6.4.2.2 Change Some Variables To Categorical

```
dfL$identity <- factor(dfL$identity)</pre>
dfL$intervention <- factor(dfL$intervention)</pre>
```

6.4.2.3 Run The Models



Caution

lme4 does not directly provide p values in results, because of some disagreement over exactly how these p values should be calculated. Therefore, in this Appendix, I also call library lmerTest to provide p values for lme4 results.



🕊 Tip

R prefers to use scientific notation when possible. I find that the use of scientific notation can be confusing in reading results. I turn off scientific notation by setting a penalty for its use: options(scipen = 999).

6.4.2.3.1 Main Effects Only

```
library(lme4)
library(lmerTest)
options(scipen = 999)
fit2A <- lmer(outcome ~ t + warmth + physical_punishment +</pre>
```

```
identity + intervention + HDI +
               (1 | country/id),
            data = dfL)
summary(fit2A)
Linear mixed model fit by REML. t-tests use Satterthwaite's method [
lmerModLmerTest]
Formula:
outcome ~ t + warmth + physical punishment + identity + intervention +
    HDI + (1 | country/id)
   Data: dfL
REML criterion at convergence: 57022.7
Scaled residuals:
    Min
            1Q Median
                            3Q
                                   Max
-3.6850 -0.6094 -0.0035 0.6133 3.6792
Random effects:
 Groups
           Name
                       Variance Std.Dev.
 id:country (Intercept) 8.438
                                2.905
          (Intercept) 3.675
                                1.917
 country
 Residual
                       26.036 5.103
Number of obs: 9000, groups: id:country, 3000; country, 30
Fixed effects:
                                  Std. Error
                       Estimate
                                                       df t value
(Intercept)
                     50.3842343 1.4139114
                                               29.8246912 35.635
                      0.9433806
                                   0.0658755 5998.3764548 14.321
t
warmth
                      0.9140307 0.0379336 4745.3497493 24.096
                     -1.0087537
physical_punishment
                                   0.0497972 6483.6771808 -20.257
identity1
                     -0.1319548
                                   0.1517350 2968.7828107 -0.870
intervention1
                      0.8591494
                                   0.1520510 2971.8111995 5.650
HDI
                      0.0007909
                                   0.0207656
                                               28.0001855 0.038
                               Pr(>|t|)
(Intercept)
                   < 0.000000000000000 ***
                   < 0.00000000000000000000 ***
t
                   < 0.000000000000000 ***
physical_punishment < 0.000000000000000 ***</pre>
identity1
                                  0.385
```

0.000000175 ***

intervention1

```
HDI
                                   0.970
___
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Correlation of Fixed Effects:
           (Intr) t
                          warmth physc_ idntt1 intrv1
           -0.092
           -0.091 -0.002
warmth
physcl_pnsh -0.092 -0.007 -0.012
          -0.051 0.000 -0.013 -0.003
identity1
interventn1 -0.058 0.000 0.039 0.019 -0.018
HDI
           -0.951 0.000 -0.004 0.005 0.000 0.002
6.4.2.3.2 Interactions With Time
fit2B <- lmer(outcome ~ t *(warmth + physical_punishment +</pre>
               identity + intervention + HDI) +
               (1 | country/id),
             data = dfL
summary(fit2B)
Linear mixed model fit by REML. t-tests use Satterthwaite's method [
lmerModLmerTest]
Formula:
outcome ~ t * (warmth + physical_punishment + identity + intervention +
    HDI) + (1 | country/id)
   Data: dfL
REML criterion at convergence: 57042.8
Scaled residuals:
    Min
             1Q Median
                             3Q
                                    Max
-3.7118 -0.6092 -0.0024 0.6150 3.6779
Random effects:
 Groups
                        Variance Std.Dev.
            Name
 id:country (Intercept) 8.436
                                 2.905
 country
            (Intercept) 3.675
                               1.917
                                 5.104
 Residual
                        26.046
Number of obs: 9000, groups: id:country, 3000; country, 30
```

Fixed effects:

```
Estimate
                                    Std. Error
                                                         df t value
(Intercept)
                       50.7590272
                                     1.5518360
                                                 43.2608620 32.709
                                                              2.315
t
                        0.7552909
                                     0.3263028 6176.7440549
                                     0.0805355 8274.9995422 10.146
warmth
                        0.8170912
physical punishment
                       -1.0097729
                                     0.1113557 8084.6084915 -9.068
identity1
                       -0.2446453
                                     0.3041604 8695.8966197 -0.804
intervention1
                        0.6604671
                                     0.3046286 8697.0843430
                                                              2.168
HDT
                        0.0026692
                                     0.0221295
                                                 36.1037733
                                                              0.121
                                     0.0356217 6404.8723333
t:warmth
                        0.0486211
                                                              1.365
                                     0.0494590 6753.0158441
                                                              0.010
t:physical_punishment
                        0.0004964
                        0.0563140
                                     0.1318043 5993.4518022
                                                              0.427
t:identity1
                                     0.1319917 5994.1433001
t:intervention1
                        0.0995037
                                                              0.754
t:HDI
                       -0.0009379
                                     0.0038233 5993.9090880 -0.245
                                Pr(>|t|)
(Intercept)
                     0.0207 *
                     <0.000000000000000000002 ***
warmth
                     <0.0000000000000000 ***
physical_punishment
identity1
                                  0.4212
intervention1
                                  0.0302 *
HDT
                                  0.9047
t:warmth
                                  0.1723
t:physical_punishment
                                  0.9920
t:identity1
                                  0.6692
                                  0.4510
t:intervention1
t:HDI
                                  0.8062
___
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Correlation of Fixed Effects:
            (Intr) t
                         warmth physc_ idntt1 intrv1 HDI
                                                           t:wrmt t:phy_
           -0.421
t.
warmth
           -0.178 0.331
physcl pnsh -0.190 0.360 -0.005
identity1
           -0.093 0.166 -0.013 -0.002
interventn1 -0.107 0.192 0.039 0.019 -0.017
HDI
           -0.925 0.264 -0.007 0.012 -0.001 0.003
t:warmth
            0.158 -0.377 -0.882 0.001 0.011 -0.035 0.006
t:physcl_pn 0.170 -0.402 0.004 -0.894 -0.001 -0.017 -0.010 -0.003
t:identity1 0.081 -0.192 0.011 0.000 -0.867 0.014 0.001 -0.013 0.002
t:intrvntn1 0.093 -0.222 -0.035 -0.017 0.014 -0.867 -0.003 0.041 0.019
```

6.4.3 Julia

6.4.3.1 Get The Data

```
using Tables, MixedModels, StatFiles, DataFrames, CategoricalArrays, DataFramesMeta

dfL = DataFrame(load("simulated_multilevel_longitudinal_data.dta"))
```

6.4.3.2 Change Some Variables To Categorical

```
@transform!(dfL, :country = categorical(:country))
@transform!(dfL, :identity = categorical(:identity))
@transform!(dfL, :intervention = categorical(:intervention))
```

6.4.3.3 Run The Models

6.4.3.3.1 Main Effects Only

```
(1 | country) +
  (0 + warmth | country) +
  (1 | id)), dfL)
```

```
Linear mixed model fit by maximum likelihood
outcome ~ 1 + t + warmth + physical_punishment + identity + intervention + HDI + (1 | counts
logLik -2 logLik AIC AICc BIC
-28499.6031 56999.2063 57021.2063 57021.2356 57099.3610
```

Variance components:

Column Variance Std.Dev. Corr.

id (Intercept) 8.387214 2.896069

country (Intercept) 3.167143 1.779647

warmth 0.010762 0.103739 .

Residual 26.027363 5.101702

Number of obs: 9000; levels of grouping factors: 3000, 30

Fixed-effects parameters:

	Coef.	Std. Error	Z	Pr(> z)
(Intercept)	50.4673	1.33833	37.71	<1e-99
t	0.943864	0.0658717	14.33	<1e-45
warmth	0.913496	0.0423744	21.56	<1e-99
physical_punishment	-1.0079	0.0497622	-20.25	<1e-90
identity: 1.0	-0.127692	0.151583	-0.84	0.3996
intervention: 1.0	0.858997	0.151909	5.65	<1e-07
HDI	-0.000566026	0.0196439	-0.03	0.9770

6.4.3.3.2 Interactions With Time

Linear mixed model fit by maximum likelihood

```
outcome ~ 1 + t + warmth + physical_punishment + identity + intervention + HDI + t & warmth logLik -2 logLik AIC AICc BIC -28498.3091 56996.6182 57028.6182 57028.6788 57142.2979
```

Variance components:

Column Variance Std.Dev. Corr.

id (Intercept) 8.391746 2.896851

country (Intercept) 3.170032 1.780458

warmth 0.010609 0.102999 .

Residual 26.015906 5.100579

Number of obs: 9000; levels of grouping factors: 3000, 30

Fixed-effects parameters:

	Coef.	Std. Error	z	Pr(> z)
(Intercept)	50.8364	1.48355	34.27	<1e-99
t	0.758209	0.326177	2.32	0.0201
warmth	0.817076	0.0826636	9.88	<1e-22
physical_punishment	-1.00903	0.111293	-9.07	<1e-18
identity: 1.0	-0.238714	0.303996	-0.79	0.4323
intervention: 1.0	0.660761	0.30445	2.17	0.0300
HDI	0.00136065	0.0210842	0.06	0.9485
t & warmth	0.0483635	0.0356074	1.36	0.1744
t & physical_punishment	0.000542203	0.0494355	0.01	0.9912
t & identity: 1.0	0.0554385	0.131745	0.42	0.6739
t & intervention: 1.0	0.0992809	0.131925	0.75	0.4517
t & HDI	-0.000955067	0.00382162	-0.25	0.8027

6.5 Interpretation

The main effects only model suggests that time is associated with increases in the outcome. In the main effects model, main effects other than time, indicate whether a particular variable is associated with higher or lower intercepts of the time trajectory, at the beginning of the study time. Warmth is again associated with increases in the outcome, while physical punishment is associated with decreases in the outcome. Identity is again not associated with the outcome, while the intervention is associated with higher levels of the outcome. The Human Development Index is again not associated with the outcome.

The second model adds interactions with time to the first model. Results are largely similar to the prior model. However, here we not only examine whether main effects other than time

are associated with higher or lower time trajectories, but also whether particular variables are associated with differences in the slope of the time trajectory. In this case, we find insufficient evidence that any independent variable is associated with changes in the slope of the time trajectory.

• Which Interactions To Test?

In this example—for the sake of illustration—I test the interaction of every independent variable with time. In many cases, it may make sense to test only only one or two interactions of time with particular variables of key interest. Also, after finding, as I did in this model, that none of the interactions of other independent variables with time are significant, I might report the model with interactions, or might report only the results of the model with only main effects.

It may be illustrative to imagine how we would interpret the results had a particular interaction term been statistically significant. Let us consider one of the interaction terms with the largest coefficient, intervention#time. The interaction of the intervention with time is positive. Had this coefficient been statistically significant, it would have indicated that the intervention was associated with more rapid increases in the outcome over time in addition to the fact that the intervention is associated with higher initial levels of the outcome.

7 Reshaping Data

7.1 Introduction

Cross-sectional analyses (Chapter 5) make use of data in *wide* format: every row is a person, or family, and every person, or family, has a single row of data.

Longitudinal analyses (Chapter 6) make use of *long* data: every row is a person-timepoint, or family-timepoint, and every person, or family, has multiple rows of data.

Data therefore sometimes need to be *reshaped*, most often from *wide* format to *long* format. Almost any software that is capable of estimating multilevel models is capable of reshaping data.

Below, I detail the procedure for reshaping data in Stata and R.

7.2 Data in Wide Format

Note

The data below are in wide format.

Every individual in the data set has a *single row of data*. Every row in the data set is an *individual* or *family*.

Table 7.1: Data in Wide Format

Table 7.1: Table continues below

id	$physical_punishment 1$	warmth1	outcome1	$physical_punishment 2$
1.1	3	3	57.47	3
1.10	2	0	62.9	3
1.100	2	5	62.71	1
1.11	4	4	55.61	2
1.12	5	4	41.15	5
1.13	4	5	63.66	3

Table 7.2: Data in Wide Format

Table 7.2: Table continues below

warmth2	outcome2	physical_punishment3	warmth3	outcome3	country	HDI
4	55.06	1	2	58.77	1	69
0	56.67	2	0	68.22	1	69
4	51.58	2	5	55.51	1	69
5	50.9	3	3	48.02	1	69
5	45.4	3	4	55.86	1	69
3	64.81	3	3	58.3	1	69

Table 7.3: Data in Wide Format

family	identity	intervention
1	1	0
10	1	0
100	1	1
11	1	1
12	0	0
13	0	1

7.3 Data Management

Because reshaping your data dramatically changes the structure of your data...

- 1. It is a good idea to have your raw data saved in a location where it will not be changed, and can be retrieved again if the reshape command does not work correctly, or if you simply want to modify your reshaping data workflow.(CF Section 2.3)
- 2. Usually we want to work with only a *subset* of your data, to keep only the data in which we are interested.
 - In Stata, the command to keep only variables of interest would be: keep y x z t.
 - In R, one option would be to use the subset function: mysubset <- subset(mydata, select = c(y, x, z, t))

7.4 Reshaping Data From Wide To Long

Usually, we are most interested in reshaping data from wide to long.

7.4.1 Stata

In Stata, I only list variables that vary over time, or are *time varying*. Stata assumes that variables that are *not listed* do *not vary over time*, or are *time invariant*.

Notice also that our *time varying* data are in the *stub-time* format, e.g. warmth1, warmth2, physical_punishment1 physical_punishment2, etc. Because the variables are named in this way, Stata knows to use the *stub* (e.g. warmth) as the variable name, and the numeric value, (e.g. 1, 2, 3) as the timepoint.

The id variable, whatever it is named, has to uniquely identify the observations. A useful Stata command here is isid, e.g. isid id. If your id variable is not unique, it is often due to missing values. drop if id == . usually solves the problem (assuming that your id variable is indeed named id, and not something else).

```
use simulated_multilevel_longitudinal_data_WIDE.dta, clear
describe
reshape long outcome physical_punishment warmth, i(id) j(wave)
```

Contains data from simulated_multilevel_longitudinal_data_WIDE.dta

Observations: 3,000

Variables: 15 3 Jul 2024 14:29

Variable name	Storage type	Display format	Value label	Variable label
id	str7	%9s		unique country family id
physical_pun:	i~1 float	%9.0g		1 physical_punishment
warmth1	float	%9.0g		1 warmth
outcome1	float	%9.0g		1 outcome
physical_pun:	i~2 float	%9.0g		2 physical_punishment
warmth2	float	%9.0g		2 warmth
outcome2	float	%9.0g		2 outcome
physical_pun	i~3 float	%9.0g		3 physical_punishment
warmth3	float	%9.0g		3 warmth
outcome3	float	%9.0g		3 outcome
country	float	%9.0g		country id
HDI	float	%9.0g		Human Development Index
family	float	%9.0g		family id
identity	float	%9.0g		hypothetical identity group variable

```
intervention float %9.0g
                                           recieved intervention
Sorted by: id
(j = 1 2 3)
Data
                                 Wide -> Long
                               3,000
Number of observations
                                        ->
                                            9,000
Number of variables
                                  15
                                        -> 10
j variable (3 values)
                                        ->
                                            wave
xij variables:
            outcome1 outcome2 outcome3
                                        ->
                                             outcome
physical_punishment1 physical_punishment2 physical_punishment3->physical_punishment
               warmth1 warmth2 warmth3
                                            warmth
```

7.4.2 R

In R, I only list variables that vary over time, or are time varying.

Notice also that our *time varying* data are in the *stub-time* format, e.g. warmth1, warmth2, physical_punishment1 physical_punishment2, etc. In order to facilitate reshaping the data, it is helpful in R to insert an underscore (_) to separate the *stub* from the *time* variable.

```
library(dplyr) # data wrangling
library(tidyr) # tidy (reshape data)
```

```
# rename variables with "_" separator

df <- simulated_multilevel_longitudinal_data_WIDE %>%
    rename(outcome_1 = outcome1,
        outcome_2 = outcome2,
        outcome_3 = outcome3,
        physical_punishment_1 = physical_punishment1,
        physical_punishment_2 = physical_punishment2,
        physical_punishment_3 = physical_punishment3,
        warmth_1 = warmth1,
        warmth_2 = warmth2,
        warmth_3 = warmth3)
```

7.5 Data in Long Format

Note

The data below are in long format.

Every individual/family in the data set has a multiple rows of data. Every row in the data set is an individual-timepoint or family-timepoint.

Table 7.4: Data in Long Format

Table 7.4: Table continues below

country	HDI	family	id	identity	intervention	\mathbf{t}
1	69	1	1.1	1	0	1
1	69	1	1.1	1	0	2
1	69	1	1.1	1	0	3
1	69	2	1.2	1	1	1
1	69	2	1.2	1	1	2
1	69	2	1.2	1	1	3

Table 7.5: Data in Long Format

physical_punishment	warmth	outcome
3	3	57.47
3	4	55.06
1	2	58.77
2	1	50.1
3	0	53.31
3	1	49.79

References

- Allaire, J. J., Teague, C., Scheidegger, C., Xie, Y., & Dervieux, C. (2024). Quarto (Version 1.4). https://doi.org/10.5281/zenodo.5960048
- Bates, D. (2024). MixedModels.jl Documentation. https://juliastats.org/MixedModels.jl/stable/
- Bates, D., Mächler, M., Bolker, B., & Walker, S. (2015). Fitting linear mixed-effects models using lme4. *Journal of Statistical Software*, 67(1), 1–48. https://doi.org/10.18637/jss.v067.i01
- Bezanson, J., Edelman, A., Karpinski, S., & Shah, V. B. (2017). Julia: A fresh approach to numerical computing. SIAM Review, 59(1), 65–98. https://doi.org/10.1137/141000671
- Hemken, D. (2023). Statamarkdown: 'Stata' markdown. https://CRAN.R-project.org/package=Statamarkdown
- Li, C. (2019). JuliaCall: An R package for seamless integration between R and Julia. The Journal of Open Source Software, 4(35), 1284. https://doi.org/10.21105/joss.01284
- R Core Team. (2023). R: A language and environment for statistical computing. R Foundation for Statistical Computing. https://www.R-project.org/
- Schanen, J. (2021). *Math person (Strogatz Prize entry)*. National Museum of Mathematics. StataCorp. (2023). *Stata 18 mixed effects reference manual*. Stata Press.
- Thoreau, H. D. (1975). The commercial spirit of modern times [1837]. In J. J. Moldenhauer, E. Moser, & A. C. Kern (Eds.), *Early essays and miscellanies*. Princeton University Press.