# Multilevel Multilingual

Multilevel Models in Stata, R and Julia

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# 1 Multilevel Multilingual

#### 1.1 Introduction

Below, I describe the use of Stata, R, and Julia to estimate multilevel models.

#### Results Will Vary Somewhat

Estimating multilevel models is a complex endeavor. The software details of how this is accomplished are beyond the purview of this book. Suffice it to say that across different software packages there will be differences in estimation routines, resulting in some numerical differences in the results provided by different software packages. Substantively speaking, however, results should agree across software.

#### Multi-Line Commands

Sometimes I have written commands out over multiple lines. I have done this for especially long commands, but have also sometimes done this simply for the sake of clarity. The different software packages have different approaches to multi-line commands.

- 1. By default, Stata ends a command at the end of a line. If you are going to write a multi-line command you should use the /// line continuation characters.
- 2. R is the software that most naturally can be written using multiple lines, as R commands are usually clearly encased in parentheses (()) or continued with + signs.
- 3. Like Stata, Julia expects commands to end at the end of a line. If you are going to write a mult-line command, all commands except for the last line should end in a character that clearly indicates continuation, like a + sign. An alternative is to encase the entire Julia command in an outer set of parentheses (()).

#### 1.2 The Data

The examples use the simulated\_multilevel\_data.dta file from Multilevel Thinking. Here is a direct link to download the data.

Table 1.1: Sample of Simulated Multilevel Data

country	HDI	family	id	group	physical_punishment	warmth	outcome
1	69	1	1.1	2	2	3	59.18
1	69	2	1.2	2	4	0	61.54
1	69	3	1.3	1	4	4	51.87
1	69	4	1.4	2	0	6	51.71
1	69	5	1.5	2	3	2	55.88
1	69	6	1.6	1	5	3	60.78

### 1.3 An Introduction To Equations and Syntax

To explain statistical syntax for each software, I consider the general case of a multilevel model with dependent variable y, independent variables x and z, clustering variable group, and a random slope for x. i is the index for the person, while j is the index for the group.

$$y = \beta_0 + \beta_1 x_{ij} + \beta_2 z_{ij} + u_{0j} + u_{1j} \times x_{ij} + e_{ij}$$
(1.1)

#### 1.3.1 Stata

In Stata mixed, the syntax for a multilevel model of the form described in Equation 1.1 is:

```
mixed y x || group: x
```

#### 1.3.2 R

In R lme4, the general syntax for a multilevel model of the form described in Equation 1.1 is:

```
library(lme4)

lmer(y ~ x + z + (1 + x || group), data = ...)
```

## 1.3.3 Julia

In Julia MixedModels, the general syntax for a multilevel model of the form described in Equation 1.1 is:

```
using MixedModels
fit(MixedModel, @formula(y ~ x + z + (1 + x | group)), data)
```

# 2 Descriptive Statistics

## 2.1 Descriptive Statistics

#### 2.1.1 Stata

```
use simulated_multilevel_data.dta // use data
```

We use summarize for *continuous* variables, and tabulate for *categorical* variables.

```
summarize outcome warmth physical_punishment HDI
tabulate group
```

Variable	0bs	Mean	Std. dev.	Min	Max
outcome	3,000	53.46757	6.65179	33.39014	76.75101
warmth	3,000	3.524333	1.889956	0	7
physical_p~t	3,000	2.494667	1.380075	0	5
HDI	3,000	64.76667	17.24562	33	87

arbitrary   group   variable	Freq.	Percent	Cum.
1   2	1,507 1,493	50.23 49.77	50.23
Total	3,000	100.00	

#### 2.1.2 R

```
library(haven) # read data in Stata format

df <- read_dta("simulated_multilevel_data.dta")</pre>
```

R's descriptive statistics functions rely heavily on whether a variable is a *numeric* variable, or a *factor* variable. Below, I convert two variables to factors (factor) before using summary<sup>1</sup> to generate descriptive statistics.

```
df$country <- factor(df$country)

df$group <- factor(df$group)

summary(df)</pre>
```

```
country
                    HDI
                                   family
                                                     id
                                                                   group
1
       : 100
               Min.
                      :33.00
                               Min.
                                     : 1.00
                                                Length:3000
                                                                   1:1507
2
       : 100
                               1st Qu.: 25.75
                                                                   2:1493
              1st Qu.:53.00
                                                Class : character
3
       : 100
              Median :70.00
                               Median : 50.50
                                                Mode :character
4
       : 100
               Mean
                      :64.77
                               Mean
                                      : 50.50
5
                               3rd Qu.: 75.25
       : 100
               3rd Qu.:81.00
6
       : 100
                     :87.00
                                      :100.00
               Max.
                               Max.
(Other):2400
physical_punishment
                        warmth
                                       outcome
       :0.000
                           :0.000
Min.
                    Min.
                                    Min.
                                           :33.39
1st Qu.:2.000
                    1st Qu.:2.000
                                    1st Qu.:48.78
Median :3.000
                   Median:4.000
                                    Median :53.64
Mean
     :2.495
                   Mean :3.524
                                    Mean :53.47
3rd Qu.:3.250
                    3rd Qu.:5.000
                                    3rd Qu.:58.06
Max.
      :5.000
                    Max. :7.000
                                    Max.
                                          :76.75
```

#### 2.1.3 Julia

```
using Tables, MixedModels, MixedModelsExtras, StatFiles, DataFrames, CategoricalArrays, Data

df = DataFrame(load("simulated_multilevel_data.dta"))
```

<sup>&</sup>lt;sup>1</sup>skimr is an excellent new alternative library for generating descriptive statistics in R.

Similarly to R, Julia relies on the idea of *variable type*. I use transform to convert the appropriate variables to *categorical* variables.

```
@transform!(df, :country = categorical(:country))
@transform!(df, :group = categorical(:group))
```

```
describe(df) # descriptive statistics
```

8×7 DataFrame										
Row	variable	mean	min	median	max	nmissing	eltyp			
	Symbol	Union	Any	Union	Any	Int64	Union			
1	country		1.0		30.0	0	Union			
2	HDI	64.7667	33.0	70.0	87.0	0	Union			
3	family	50.5	1.0	50.5	100.0	0	Union			
4	id		1.1		9.99	0	Union			
5	group		1.0		2.0	0	Union			
6	physical_punishment	2.49467	0.0	3.0	5.0	0	Union			
7	warmth	3.52433	0.0	4.0	7.0	0	Union			
8	outcome	53.4676	33.3901	53.6426	76.751	0	Union			

# 3 Unconditional Model

An *unconditional* multilevel model is a model with no independent variables. One should always run an unconditional model as the first step of a multilevel model in order to get a sense of the way that variation is apportioned in the model across the different levels.

#### 3.1 The Equation

$$outcome_{ij} = \beta_0 + u_{0j} + e_{ij} \tag{3.1}$$

The Intraclass Correlation Coefficient (ICC) is given by:

$$ICC = \frac{var(u_{0j})}{var(u_{0j}) + var(e_{ij})}$$

$$(3.2)$$

In a two level multilevel model, the ICC provides a measure of the amount of variation attributable to Level 2.

#### 3.2 Run Models

#### 3.2.1 Stata

```
use simulated_multilevel_data.dta // use data
```

```
mixed outcome || country: // unconditional model
```

Performing EM optimization ...

Performing gradient-based optimization: Iteration 0: Log likelihood = -9856.1548 Iteration 1: Log likelihood = -9856.1548

```
Computing standard errors ...
Mixed-effects ML regression
                                  Number of obs = 3,000
Group variable: country
                                  Number of groups = 30
                                  Obs per group:
                                          min = 100
                                          avg = 100.0
                                          max = 100
                                  Wald chi2(0)
                                  Prob > chi2
Log likelihood = -9856.1548
   outcome | Coefficient Std. err. z P>|z| [95% conf. interval]
______
    _cons | 53.46757 .3539097 151.08 0.000
                                    52.77392
_____
 Random-effects parameters | Estimate Std. err. [95% conf. interval]
______
country: Identity
           var(_cons) | 3.348734 .9702594 1.897816 5.908906
         var(Residual) | 40.88284 1.060908
                                    38.8555
LR test vs. linear model: chibar2(01) = 169.64
                                 Prob \geq chibar2 = 0.0000
estat icc // ICC
Intraclass correlation
______
                       ICC Std. err.
              Level |
                                    [95% conf. interval]
______
             country | .0757091 .0203761 .0442419 .1265931
```

3.2.2 R

```
library(haven)
df <- read_dta("simulated_multilevel_data.dta")</pre>
library(lme4) # estimate multilevel models
fit0 <- lmer(outcome ~ (1 | country),</pre>
            data = df) # unconditional model
summary(fit0)
Linear mixed model fit by REML ['lmerMod']
Formula: outcome ~ (1 | country)
  Data: df
REML criterion at convergence: 19712.5
Scaled residuals:
              1Q Median
     Min
                                ЗQ
                                        Max
-2.97650 -0.68006 0.00936 0.67580 3.03510
Random effects:
 Groups Name Variance Std.Dev.
 country (Intercept) 3.478 1.865
 Residual
                    40.883 6.394
Number of obs: 3000, groups: country, 30
Fixed effects:
           Estimate Std. Error t value
(Intercept) 53.47 0.36 148.5
library(performance)
performance::icc(fit0) # ICC
# Intraclass Correlation Coefficient
```

Adjusted ICC: 0.078 Unadjusted ICC: 0.078

#### 3.2.3 Julia

```
using Tables, MixedModels, MixedModelsExtras,
StatFiles, DataFrames, CategoricalArrays, DataFramesMeta
df = DataFrame(load("simulated_multilevel_data.dta"))
@transform!(df, :country = categorical(:country))
m0 = fit(MixedModel,
         @formula(outcome ~ (1 | country)), df) # unconditional model
Linear mixed model fit by maximum likelihood
 outcome ~ 1 + (1 | country)
   logLik -2 logLik
                         AIC
                                   AICc
                                               BIC
 -9856.1548 19712.3097 19718.3097 19718.3177 19736.3288
Variance components:
           Column
                   Variance Std.Dev.
                      3.34871 1.82995
country (Intercept)
Residual
                     40.88285 6.39397
 Number of obs: 3000; levels of grouping factors: 30
 Fixed-effects parameters:
              Coef. Std. Error
                                    z Pr(>|z|)
(Intercept) 53.4676 0.353908 151.08
                                           <1e-99
icc(m0) # ICC
```

# 4 Cross Sectional Multilevel Models

### 4.1 The Equation

Recall the general model of Equation 1.1, and the syntax outlined in Section 1.3. Below in Equation 4.1, we consider a more substantive example.

```
\text{outcome}_{ij} = \beta_0 + \beta_1 \text{warmth}_{ij} + \beta_2 \text{physical punishment}_{ij} + \beta_3 \text{group}_{ij} + \beta_4 \text{HDI}_{ij} + u_{0j} + u_{1j} \times \text{warmth}_{ij} + e_{ij} \tag{4.1}
```

### 4.2 Run Models

#### 4.2.1 Stata

#### 4.2.1.1 Get The Data

```
use simulated_multilevel_data.dta
```

#### 4.2.1.2 Graph

```
twoway scatter outcome warmth, ///
   xtitle("warmth") ytitle("outcome") ///
   title("Outcome by Parental Warmth")

quietly graph export scatter.png, replace
```

#### 4.2.1.3 Run The Model

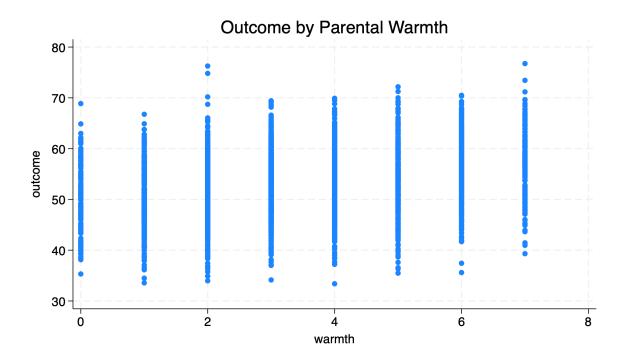


Figure 4.1: Outcome by Parental Warmth (Stata)

### mixed outcome warmth physical\_punishment group HDI || country: warmth

#### Performing EM optimization ...

Performing gradient-based optimization:
Iteration 0: Log likelihood = -9668.198
Iteration 1: Log likelihood = -9667.9551
Iteration 2: Log likelihood = -9667.9534
Iteration 3: Log likelihood = -9667.9533
Iteration 4: Log likelihood = -9667.9532

#### Computing standard errors ...

Mixed-effects ML regression	Number of obs $= 3,000$
Group variable: country	Number of groups = 30
	Obs per group:
	min = 100
	avg = 100.0
	max = 100
	Wald chi2(4) = $401.26$
Log likelihood = -9667.9532	Prob > chi2 = 0.0000

outcome	   -+-	Coefficient		z	P> z		interval]
warmth physical_punishment group HDI cons	İ	.96164478453802 1.084344 .010557 49.87963	.0581825 .0798155 .2200539 .0204522	16.53 -10.59 4.93 0.52 34.72	0.000 0.000 0.000 0.606 0.000	.8476091 -1.001816 .6530461 0295286 47.06392	1.075686889448 1.515642 .0506426 52.69534

Estimate	Std. err.	[95% conf.	interval]
1.83e-06	.0000173	1.76e-14	190.9774
3.370262	.9633726	1.924651	5.901676
36.01906	.9346936	34.23291	37.89842
	1.83e-06 3.370262	1.83e-06 .0000173 3.370262 .9633726	1.83e-06 .0000173 1.76e-14 3.370262 .9633726 1.924651

```
LR test vs. linear model: chi2(2) = 198.01 Prob > chi2 = 0.0000
```

Note: LR test is conservative and provided only for reference.

#### 4.2.2 R

### 4.2.2.1 Get The Data

```
library(haven)

df <- read_dta("simulated_multilevel_data.dta")</pre>
```

#### 4.2.2.2 Graph

```
library(ggplot2)

ggplot(df,
    aes(x = warmth,
        y = outcome)) +
    geom_point() +
    labs(title = "Outcome by Parental Warmth")
```

#### Outcome by Parental Warmth

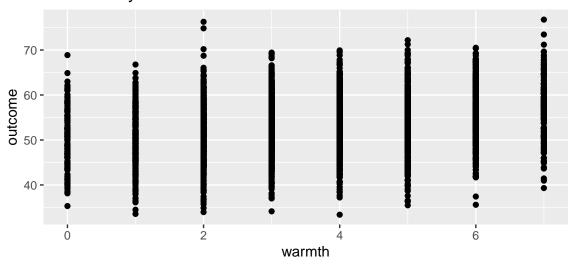


Figure 4.2: Outcome by Parental Warmth (R)

#### 4.2.2.3 Run The Model

```
group + HDI +
               (1 + warmth || country),
             data = df)
summary(fit1)
Linear mixed model fit by REML ['lmerMod']
Formula: outcome ~ warmth + physical_punishment + group + HDI + ((1 |
    country) + (0 + warmth | country))
   Data: df
REML criterion at convergence: 19350.3
Scaled residuals:
             1Q Median
                             3Q
                                    Max
-3.4496 -0.6807 0.0016 0.6864 3.1792
Random effects:
 Groups
           Name
                       Variance Std.Dev.
```

fit1 <- lmer(outcome ~ warmth + physical\_punishment +</pre>

#### Fixed effects:

	Estimate	Std.	Error	t value
(Intercept)	49.88754	1	.48203	33.662
warmth	0.96155	0	.05875	16.367
<pre>physical_punishment</pre>	-0.84556	0	.07986	-10.588
group	1.08471	0	.22017	4.927
HDI	0.01044	0	.02116	0.493

#### Correlation of Fixed Effects:

(Intr) warmth physc\_ group

warmth -0.126

physcl\_pnsh -0.135 -0.025

group -0.218 -0.010 -0.019

HDI -0.925 -0.006 0.008 -0.001

#### 4.2.3 Julia

#### 4.2.3.1 Get The Data

```
using Tables, MixedModels, StatFiles, DataFrames, CategoricalArrays, DataFramesMeta
df = DataFrame(load("simulated_multilevel_data.dta"))
```

#### 4.2.3.2 Graph

# Outcome by Parental Warmth

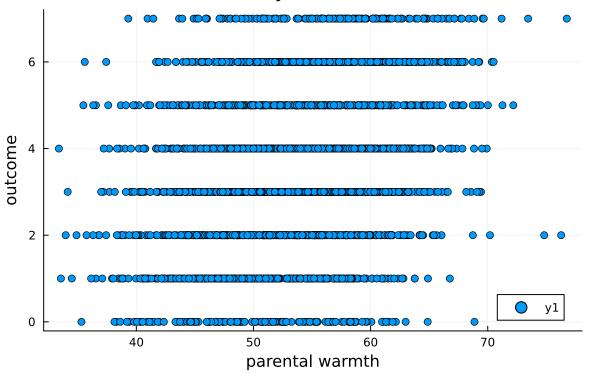


Figure 4.3: Outcome by Parental Warmth (Julia)

#### 4.2.3.3 Change Country To Categorical

```
@transform!(df, :country = categorical(:country))
```

#### 4.2.3.4 Run The Model

```
Linear mixed model fit by maximum likelihood
outcome ~ 1 + warmth + physical_punishment + group + HDI + (1 + warmth | country)
logLik -2 logLik AIC AICC BIC
```

#### -9667.9392 19335.8783 19353.8783 19353.9385 19407.9357

#### Variance components:

Column Variance Std.Dev. Corr.

country (Intercept) 3.2369484 1.7991521

warmth 0.0001080 0.0103903 +1.00

Residual 36.0187144 6.0015593

Number of obs: 3000; levels of grouping factors: 30

#### Fixed-effects parameters:

	Coef.	Std. Error	Z	Pr(> z )
(Intercept)	49.9018	1.43435	34.79	<1e-99
warmth	0.961545	0.0582135	16.52	<1e-60
physical_punishment	-0.845389	0.0798149	-10.59	<1e-25
group	1.08524	0.220055	4.93	<1e-06
HDI	0.0101984	0.0204401	0.50	0.6178

# 5 Longitudinal Multilevel Models

#### 5.1 The Data

The data employed in these examples are a longitudinal extension of the data described in Section 1.2.

•

#### Graphing Longitudinal Data

In the section on *cross-sectional* multilevel models, I employed *scatterplots* to graph the data. In longitudinal models, *time* is a variable of special interest. Often, in graphing *longitudinal* data—especially when graphing outcomes by time—it makes more sense to use *linear fit* plots, although a *scatterplot* could be employed as well.

### 5.2 The Equation

 $outcome_{itj} = \beta_0 + \beta_1 parental warmth_{itj} + \beta_2 physical punishment_{itj} + \beta_3 time_{itj} + (5.1)$ 

$$\beta_4 \text{group}_{itj} + \beta_5 \text{HDI}_{itj} +$$

$$u_{0j} + u_{1j} \times \text{parental warmth}_{itj} \, + \,$$

$$v_{0i} + v_{1i} \times \text{time}_{itj} + e_{itj}$$

### 5.3 Run Models

#### 5.3.1 Stata

#### 5.3.1.1 Get The Data

```
use simulated_multilevel_longitudinal_data.dta
```

#### 5.3.1.2 Graph

```
twoway lfit outcome t, ///
   xtitle("time") ytitle("outcome") ///
   title("Outcome by Time")

quietly graph export lfitlongitudinal.png, replace
```

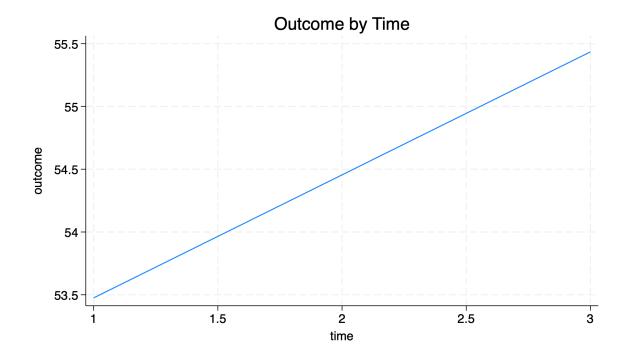


Figure 5.1: Outcome by Parental Warmth (Stata)

#### 5.3.1.3 Run The Model

#### 5.3.1.3.1 Main Effects Only

```
mixed outcome t warmth physical_punishment group HDI || country: warmth
```

Performing EM optimization ...

Performing gradient-based optimization: Iteration 0: Log likelihood = -28795.37 Iteration 1: Log likelihood = -28795.232 Iteration 2: Log likelihood = -28795.232

Computing standard errors ...

Mixed-effects ML regression

Group variable: country

Number of obs = 9,000

Number of groups = 30

Obs per group:

min = 300

avg = 300.0

max = 300

Wald chi2(5) = 1366.93

Log likelihood = -28795.232

Prob > chi2 = 0.0000

outcome | Coefficient Std. err. z P>|z| [95% conf. interval]

t | .9882371 .0761439 12.98 0.000 .8389979 1.137476
warmth | .9427117 .0342282 27.54 0.000 .8756256 1.009798
physical\_punishment | -.9020727 .0452759 -19.92 0.000 -.9908119 -.8133336
group | .9861238 .1249047 7.90 0.000 .7413151 1.230933
HDI | .0073726 .020661 0.36 0.721 -.0331222 .0478674
\_cons | 49.45537 1.414072 34.97 0.000 46.68384 52.2269

Random-effects parameters | Estimate Std. err. [95% conf. interval]

country: Independent | var(warmth) | .0024684 .0082517 3.52e-06 1.72956

var(\_cons) | 3.663663 .9914845 2.155548 6.22692

Note: LR test is conservative and provided only for reference.

#### 5.3.1.3.2 Interactions With Time

```
mixed outcome c.t##(c.warmth c.physical_punishment i.group c.HDI) || country: warmth
```

Performing EM optimization ...

 ${\tt Performing\ gradient-based\ optimization:}$ 

Iteration 0: Log likelihood = -28794.99
Iteration 1: Log likelihood = -28794.855
Iteration 2: Log likelihood = -28794.855

Computing standard errors ...

Mixed-effects ML regression

Group variable: country

Number of obs = 9,000

Number of groups = 30

Obs per group:

min = 300

avg = 300.0

max = 300

Wald chi2(9) = 1365.73Log likelihood = -28794.855 Prob > chi2 = 0.0000

		Coefficient	Std.	err.		Z	P>	· z		[95%	conf.	int	erval]
	+-												
t		1.047448	.361	19795		2.89	0.	004		.3379	816	1.	756915
warmth		.8869901	.087	76058		10.12	0.	000		.715	286	1.	058694
physical_punishment		893285	.119	94705	-	-7.48	0.	000	-:	1.127	443		659127
2.group		.9648545	.329	92217		2.93	0.	003		.3195	918	1.	610117
HDI		.0120622	.02	22474		0.54	0.	591	-	.0319	861	.0	561104
c.t#c.warmth		.0277903	.040	2665		0.69	0.	490	-	.0511	.306	. 1	067112
c.t#													
С.													

physical_punishment		0041479	.0553051	-0.08	0.940	1125439	.1042482
group#c.t							
2	 	.0105177	.1523009	0.07	0.945	2879865	.3090219
c.t#c.HDI	   	002342	.0044172	-0.53	0.596	0109996	.0063155
_cons		50.32233	1.572089	32.01	0.000	47.2411	53.40357

Prob > chi2 = 0.0000

Note: LR test is conservative and provided only for reference.

LR test vs. linear model: chi2(2) = 805.90

#### 5.3.2 R

#### 5.3.2.1 Get The Data

```
library(haven)

dfL <- read_dta("simulated_multilevel_longitudinal_data.dta")</pre>
```

#### 5.3.2.2 Graph

```
library(ggplot2)

ggplot(dfL,
    aes(x = t,
    y = outcome)) +
```

```
geom_smooth(method = "lm") +
labs(title = "Outcome by Time")
```

### Outcome by Time

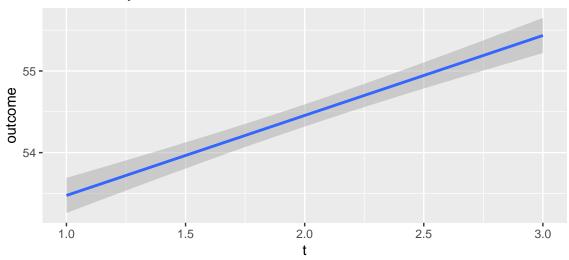


Figure 5.2: Outcome by Parental Warmth (R)

#### 5.3.2.3 Run The Model

#### 5.3.2.3.1 Main Effects Only

```
Linear mixed model fit by REML ['lmerMod']
Formula: outcome ~ t + warmth + physical_punishment + group + HDI + (1 |
        country/id)
    Data: dfL
```

REML criterion at convergence: 57088.4

```
Scaled residuals:
```

```
Min 1Q Median 3Q Max -3.4471 -0.6226 0.0081 0.6153 3.1993
```

#### Random effects:

```
Groups Name Variance Std.Dev. id:country (Intercept) 8.864 2.977 country (Intercept) 3.924 1.981 Residual 26.008 5.100
```

Number of obs: 9000, groups: id:country, 3000; country, 30

#### Fixed effects:

```
Estimate Std. Error t value (Intercept) 49.494782 1.471780 33.629 t 0.987964 0.065840 15.005 warmth 0.946259 0.038200 24.771 physical_punishment -0.926880 0.049970 -18.549 group 0.985786 0.153550 6.420 HDI 0.007543 0.021437 0.352
```

#### Correlation of Fixed Effects:

```
(Intr) t warmth physc_ group t -0.090 warmth -0.085 0.008 physcl_pnsh -0.085 0.003 -0.019 group -0.154 0.000 -0.013 -0.008 HDI -0.943 0.000 -0.003 0.003 0.000
```

#### 5.3.2.3.2 Interactions With Time

REML criterion at convergence: 57107.3

#### Scaled residuals:

Min 1Q Median 3Q Max -3.4431 -0.6248 0.0071 0.6183 3.1961

#### Random effects:

Groups Name Variance Std.Dev. id:country (Intercept) 8.868 2.978 country (Intercept) 3.925 1.981 Residual 26.014 5.100

Number of obs: 9000, groups: id:country, 3000; country, 30

#### Fixed effects:

	Estimate	Std. Error	t value
(Intercept)	49.453036	1.637740	30.196
t	1.008199	0.364915	2.763
warmth	0.865659	0.080487	10.755
physical_punishment	-0.908148	0.110449	-8.222
group	0.966988	0.304936	3.171
HDI	0.012277	0.022761	0.539
t:warmth	0.040170	0.035364	1.136
t:physical_punishment	-0.008932	0.049262	-0.181
t:group	0.009180	0.131714	0.070
t:HDI	-0.002359	0.003820	-0.618

#### Correlation of Fixed Effects:

(Intr) t -0.446 -0.159 0.278 warmth physcl\_pnsh -0.169 0.302 -0.022 group -0.274 0.459 -0.010 -0.014 HDI -0.900 0.227 -0.008 0.009 -0.001 0.141 -0.316 -0.880 0.017 0.010 0.007 t:warmth t:physcl\_pn 0.150 -0.338 0.017 -0.892 0.010 -0.007 -0.015 t:group 0.237 -0.532 0.009 0.012 -0.864 0.001 -0.012 -0.008 t:HDI 

#### 5.3.3 Julia

#### 5.3.3.1 Get The Data

```
using Tables, MixedModels, StatFiles, DataFrames, CategoricalArrays, DataFramesMeta

dfL = DataFrame(load("simulated_multilevel_longitudinal_data.dta"))
```

#### 5.3.3.2 Graph

To make our plot with a smoother in Julia, we set the markercolor and markerstrokecolor to be *white*, and the smooth option to :true.

# Outcome by Parental Warmth

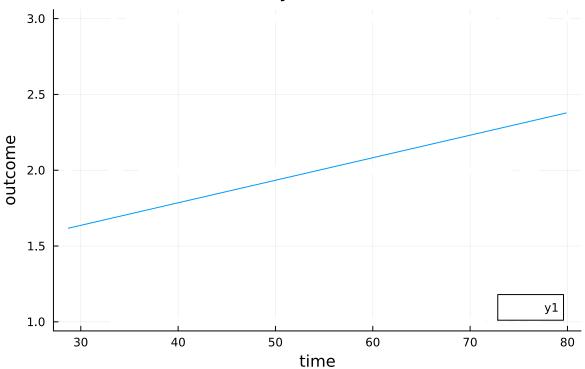


Figure 5.3: Outcome by Parental Warmth (Julia)

#### 5.3.3.3 Run The Model

#### 5.3.3.1 Change Country To Categorical

```
@transform!(dfL, :country = categorical(:country))
```

#### 5.3.3.3.2 Main Effects Only

Linear mixed model fit by maximum likelihood

```
outcome ~ 1 + t + warmth + physical_punishment + group + HDI + (1 + warmth | country) + (1 logLik -2 logLik AIC AICc BIC -28533.9236 57067.8472 57089.8472 57089.8765 57168.0019
```

#### Variance components:

Column Variance Std.Dev. Corr.

id (Intercept) 8.851224 2.975101 country (Intercept) 3.451345 1.857780

warmth 0.000227 0.015065 +1.00

Residual 26.001212 5.099138

Number of obs: 9000; levels of grouping factors: 3000, 30

#### Fixed-effects parameters:

	Coef.	Std. Error	Z	Pr(> z )
(Intercept)	49.5105	1.41854	34.90	<1e-99
t	0.98814	0.0658319	15.01	<1e-50
warmth	0.946252	0.0382851	24.72	<1e-99
<pre>physical_punishment</pre>	-0.926673	0.0499547	-18.55	<1e-76
group	0.98708	0.153484	6.43	<1e-09
HDI	0.00725703	0.0206549	0.35	0.7253

#### 5.3.3.3 Interactions With Time

```
Linear mixed model fit by maximum likelihood
outcome ~ 1 + t + warmth + physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + HDI + t & warmth + t & physical_punishment + group + t & physic
```

#### Variance components:

Column Variance Std.Dev. Corr. id (Intercept) 8.8593774 2.9764706 country (Intercept) 3.4464818 1.8564703

warmth 0.0002394 0.0154717 +1.00

Residual 25.9905210 5.0980899

Number of obs: 9000; levels of grouping factors: 3000, 30

### Fixed-effects parameters:

	Coef.	Std. Error	z	Pr(> z )
(Intercept)	49.4696	1.59007	31.11	<1e-99
t	1.00761	0.36475	2.76	0.0057
warmth	0.865294	0.0804999	10.75	<1e-26
physical_punishment	-0.907816	0.110399	-8.22	<1e-15
group	0.96908	0.304797	3.18	0.0015
HDI	0.0119739	0.0220306	0.54	0.5868
t & warmth	0.0403499	0.0353477	1.14	0.2537
t & physical_punishment	-0.00900605	0.0492392	-0.18	0.8549
t & group	0.00879803	0.131655	0.07	0.9467
t & HDI	-0.00234513	0.00381848	-0.61	0.5391