Survival Analysis of Corporal Punishment Bans

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Introduction

Corporal punishment is associated with a number of deleterious outcomes for children, including increases in behavior problems and mental health problems.

A number of countries have instituted country wide bans upon the use of corporal punishment with children.

Below, we employ a variety of empirical strategies to explore the institution of these bans.

Get The Data

```
. use "../CPBans_w_AllCountries.dta", clear // data with ALL Countries; not just bans
```

NB It is important to have data with the *correct risk set* which includes *all countries*, not just countries that eventually ban corporal punishment.

In web versions of this tutorial, click the tabs below to access different sections of the tutorial.

Setup

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Discrete Time Survival Analysis

Cox Model 2

Compare Estimates

Setup

stset The Data

```
. generate current_year = year(today()) // variable with current year
```

- . replace $year_of_prohibition = current_year$ if $year_of_prohibition == . // replace missing w/ current year (186 real changes made)$
- . generate f = type == "CP Ban" // "failure" variable

```
. stset year_of_prohibition, failure(f = 1) // stset the data with time and failure variables
Survival-time data settings
        Failure event: f==1
Observed time interval: (0, year_of_prohibition]
    Exit on or before: failure
       248 total observations
            exclusions
       248 observations remaining, representing
        62 failures in single-record/single-failure data
   500,452 total analysis time at risk and under observation
                                                                         0
                                                At risk from t =
                                    Earliest observed entry t =
                                                                         0
                                         Last observed exit t =
                                                                     2,021
```

Data Wrangling

. encode continent, generate(continent_NUMERIC) // numeric version of continent

Graphs

Survival Function

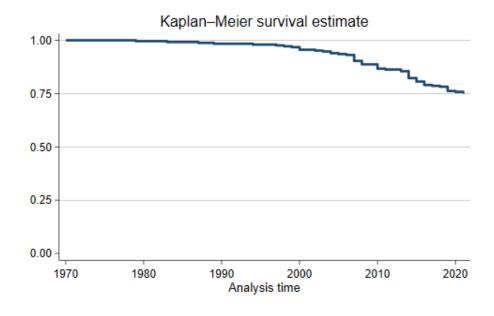


Figure 1: Kaplan-Meier Survivor Function

Failure Function

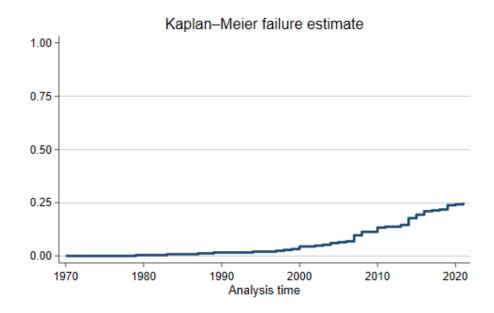


Figure 2: Kaplan-Meier Failure Function

Parametric Survival Models

Unlike other regression commands in Stata, survival analysis commands seem to require covariates. Since Europe is where these bans started, we will use Europe (category 4) as the reference category.

Weibull

```
. streg ib4.continent_NUMERIC, distribution(weibull) // Weibull distribution
        Failure _d: f==1
 Analysis time _t: year_of_prohibition
Fitting constant-only model:
              log likelihood = -148.2325
Iteration 0:
               log likelihood = -86.999055
Iteration 1:
Iteration 2:
               log likelihood = -27.073844
               log likelihood = 29.365489
Iteration 3:
Iteration 4:
               log likelihood = 77.015953
               log likelihood =
                                106.62899
Iteration 5:
               log likelihood =
Iteration 6:
                                115.32234
Iteration 7:
               log likelihood =
                                115.88805
               log likelihood =
Iteration 8:
                                115.89021
               log likelihood = 115.89021
Iteration 9:
Fitting full model:
              log likelihood = 115.89021
Iteration 0:
```

```
log likelihood = 139.32561
log likelihood = 142.87372
Iteration 1:
Iteration 2:
Iteration 3:
                log likelihood = 143.05492
                log likelihood = 143.05732
log likelihood = 143.05732
Iteration 4:
Iteration 5:
Weibull PH regression
No. of subjects =
                         248
                                                                Number of obs =
                                                                                      248
No. of failures =
                  = 500,452
Time at risk
                                                                LR chi2(5)
                                                                                = 54.33
                                                                               = 0.0000
Log likelihood = 143.05732
                                                                Prob > chi2
```

_t	Haz. ratio	Std. err.	z	P> z	[95% conf.	interval]
continent_NUMERIC						
Africa	.1684617	.0612563	-4.90	0.000	.0826011	.3435709
Americas	.1938708	.0704541	-4.51	0.000	.0950997	.395226
Asia	.1520997	.0603348	-4.75	0.000	.0698995	.3309653
NA	.0916735	.0931508	-2.35	0.019	.0125119	.6716806
Oceania	.0356574	.0362323	-3.28	0.001	.0048666	.2612621
_cons	0	0	-8.57	0.000	0	0
/ln_p	5.278967	.1166492	45.26	0.000	5.050339	5.507596
p	196.1672	22.88274			156.0754	246.5576
1/p	.0050977	.0005946			.0040558	.0064072

Note: _cons estimates baseline hazard.

Exponential

. streg ib4.continent_NUMERIC, distribution(exponential) // Exponential distribution Failure _d: f==1

Analysis time _t: year_of_prohibition

Iteration 0: log likelihood = -148.2325 \log likelihood = -139.40941 Iteration 1: Iteration 2: log likelihood = -131.58499 Iteration 3: log likelihood = -131.55897 Iteration 4: log likelihood = -131.55892 Iteration 5: log likelihood = -131.55892

Exponential PH regression

No. of subjects = Number of obs = 248 No. of failures =

= 500,452 Time at risk

LR chi2(5) = 33.35 Log likelihood = -131.55892Prob > chi2 = 0.0000

t	Haz. ratio	Std. err.	z	P> z	[95% conf.	interval]
continent_NUMERIC						
Africa	.2736219	.099129	-3.58	0.000	.134516	.5565804
Americas	.3052592	.1105907	-3.28	0.001	.1500692	.6209345
Asia	. 2489781	.0984172	-3.52	0.000	.1147345	.5402914
NA	.1586176	.1610769	-1.81	0.070	.0216746	1.160782
Oceania	.061017	.061963	-2.75	0.006	.0083378	.4465293
_cons	.000312	.0000552	-45.67	0.000	.0002206	.0004412

Note: _cons estimates baseline hazard.

[.] est store Weibull

[.] est store Exponential

Cox Proportional Hazards Model

. stcox ib4.continent_NUMERIC // Cox Proportional Hazards Model Failure _d: f==1 Analysis time _t: year_of_prohibition Iteration 0: log likelihood = -333.92184 Iteration 1: log likelihood = -317.94407 Iteration 2: log likelihood = -308.96171Iteration 3: log likelihood = -308.00801 Iteration 4: log likelihood = -308.00737 Refining estimates: Iteration 0: log likelihood = -308.00737 Cox regression with Breslow method for ties No. of subjects = 248 Number of obs = 248 No. of failures = Time at risk = 500,452LR chi2(5) = 51.83 Log likelihood = -308.00737Prob > chi2 = 0.0000

_t	Haz. ratio	Std. err.	z	P> z	[95% conf.	interval]
continent_NUMERIC						
Africa	.1769827	.0643396	-4.76	0.000	.0867938	.3608887
Americas	.2023186	.0735008	-4.40	0.000	.0992661	.4123544
Asia	.1610376	.0638871	-4.60	0.000	.0740009	.3504428
NA	.0969297	.0984941	-2.30	0.022	.0132287	.7102257
Oceania	.0380401	.038653	-3.22	0.001	.0051919	.2787139

. est store Cox

Survival Curves

```
. graph export survival1A.png, width(500) replace
file survival1A.png saved as PNG format

. stcurve, failure scheme(michigan) // failure curve

. graph export survival1B.png, width(500) replace
file survival1B.png saved as PNG format

. stcurve, failure at(continent_NUMERIC= (1 2 3 4 5 6)) ///
> legend(order(1 "Africa" 2 "Americas" 3 "Asia" ///
> 4 "Europe" 5 "NA" 6 "Oceania")) ///
> scheme(michigan) // survival curve by continent
```

. stcurve, survival scheme(michigan) // survival curve

Proportional Hazards Assumption

file survival2.png saved as PNG format

. estat phtest // formal test of PH assumption Test of proportional-hazards assumption Time function: Analysis time

. graph export survival2.png, width(500) replace

	chi2	df	Prob>chi2
Global test	6.20	5	0.2870

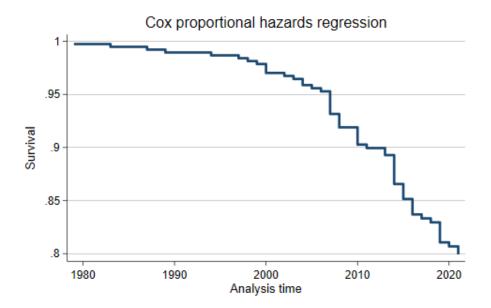


Figure 3: Survival Curve

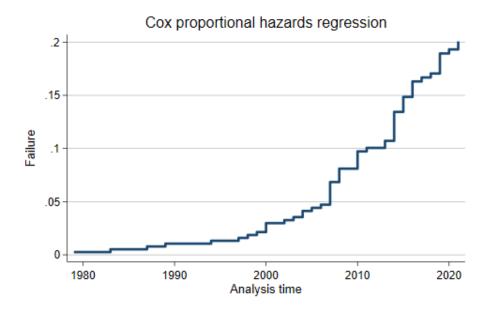


Figure 4: Failure Curve

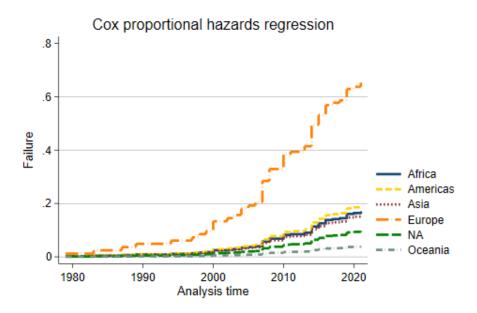


Figure 5: Failure Curve By Continent

Life Table

. ltable year_of_prohibition f, graph failure scheme(michigan) // lifetable

		Beg.			Cum.	Std.		
Int	erval	Total	Deaths	Lost	Failure	Error	[95% Con	f. Int.]
1979	1980	248	1	0	0.0040	0.0040	0.0006	0.0283
1983	1984	247	1	0	0.0081	0.0057	0.0020	0.0319
1987	1988	246	1	0	0.0121	0.0069	0.0039	0.0370
1989	1990	245	1	0	0.0161	0.0080	0.0061	0.0424
1994	1995	244	1	0	0.0202	0.0089	0.0084	0.0478
1997	1998	243	1	0	0.0242	0.0098	0.0109	0.0531
1998	1999	242	1	0	0.0282	0.0105	0.0136	0.0583
1999	2000	241	1	0	0.0323	0.0112	0.0163	0.0635
2000	2001	240	3	0	0.0444	0.0131	0.0248	0.0787
2002	2003	237	1	0	0.0484	0.0136	0.0278	0.0836
2003	2004	236	1	0	0.0524	0.0142	0.0308	0.0886
2004	2005	235	2	0	0.0605	0.0151	0.0369	0.0983
2005	2006	233	1	0	0.0645	0.0156	0.0400	0.1032
2006	2007	232	1	0	0.0685	0.0160	0.0432	0.1080
2007	2008	231	7	0	0.0968	0.0188	0.0659	0.1409
2008	2009	224	4	0	0.1129	0.0201	0.0794	0.1593
2010	2011	220	5	0	0.1331	0.0216	0.0965	0.1820
2011	2012	215	1	0	0.1371	0.0218	0.1000	0.1865
2013	2014	214	2	0	0.1452	0.0224	0.1069	0.1955
2014	2015	212	8	0	0.1774	0.0243	0.1352	0.2309
2015	2016	204	4	0	0.1935	0.0251	0.1496	0.2484
2016	2017	200	4	0	0.2097	0.0258	0.1641	0.2658
2017	2018	196	1	0	0.2137	0.0260	0.1677	0.2701

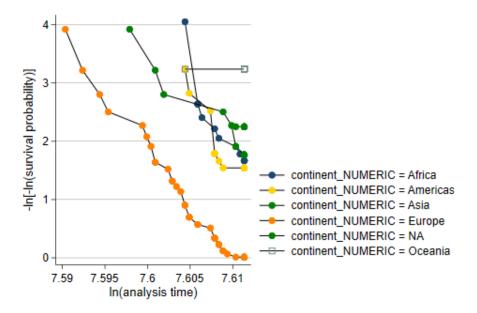


Figure 6: Graphical Test of Proportional Hazards Assumption

2018	2019	195	1	0	0.2177	0.0262	0.1713	0.2745
2019	2020	194	5	0	0.2379	0.0270	0.1897	0.2960
2020	2021	189	1	0	0.2419	0.0272	0.1934	0.3002
2021	2022	188	2	186	0.2579	0.0289	0.2062	0.3196

[.] graph export myltable.png, width(500) replace file myltable.png saved as PNG format

Discrete Time Survival Analysis

Discrete time survival analysis is placed at the end because it requires us to restructure the data into a long format, where every row is a *country-year*.

Restructuring the Data

We first need to generate a variable for the years during which a country was "at risk" of enacting a ban. Countries that have never enacted a ban are at risk up until the current year. Countries that enacted a ban leave the risk set once they have enacted a ban, and are thus at risk for a shorter time period.

```
. generate years_at_risk = year_of_prohibition - 1978 + 1 // years "at risk" of enacting a ban
```

We expand the data to generate one row of data for every year that each country is at risk.

```
. expand years_at_risk // "expand" the data; 1 row for every year at risk (9,908 observations created)
```

We create a year variable.

```
. bysort country_code: generate year = _n + 1977 // generate a year variable for each row
```

Lastly, we generate an indicator of the event, a 0/1' variable, which takes the value 1 for rows in which a ban was enacted, and 0 otherwise.

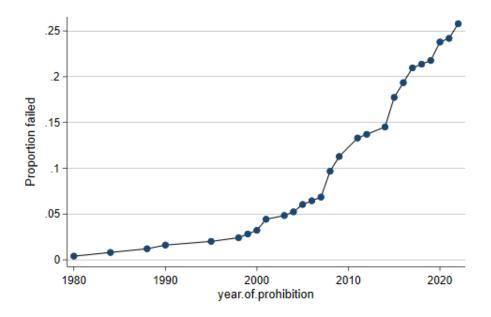


Figure 7: Graph Of Life Table

. generate event = type == "CP Ban" & year_of_prohibition == year // generate an event indicator

We list out a sample of the data to make sure that the data conform to our expectations. We focus on Norway, a country that *has* enacted a ban, and Great Britain, a country that *has not* enacted a ban.

. list country_code year_of_prohibition event continent years_at_risk year ///
> if country_code == "NOR" | country_code == "GBR" , ab(20) // list out a sample of the data

	country_code	year_of_prohibition	event	continent	years_at_risk	year
3172.	GBR	2021	0	Europe	44	1978
3173.	GBR	2021	0	Europe	44	1979
3174.	GBR	2021	0	Europe	44	1980
3175.	GBR	2021	0	Europe	44	1981
3176.	GBR	2021	0	Europe	44	1982
3177.	GBR	2021	0	Europe	44	1983
3178.	GBR	2021	0	Europe	44	1984
3179.	GBR	2021	0	Europe	44	1985
3180.	GBR	2021	0	Europe	44	1986
3181.	GBR	2021	0	Europe	44	1987
3182.	GBR	2021	0	Europe	44	1988
3183.	GBR	2021	0	Europe	44	1989
3184.	GBR	2021	0	Europe	44	1990
3185.	GBR	2021	0	Europe	44	1991
3186.	GBR	2021	0	Europe	44	1992
3187.	GBR	2021	0	Europe	44	1993
3188.	GBR	2021	0	Europe	44	1994
3189.	GBR	2021	0	Europe	44	1995
3190.	GBR	2021	0	Europe	44	1996
3191.	GBR	2021	0	Europe	44	1997
3192.	GBR	2021	0	Europe	44	1998
3193.	GBR	2021	0	Europe	44	1999
3194.	GBR	2021	0	Europe	44	2000
3195.	GBR	2021	0	Europe	44	2001
3196.	GBR	2021	0	Europe	44	2002

3197.	GBR	2021	0	Europe	44	2003
3198.	GBR	2021	0	Europe	44	2004
3199.	GBR	2021	0	Europe	44	2005
3200.	GBR	2021	0	Europe	44	2006
3201.	GBR	2021	0	Europe	44	2007
3202.	GBR	2021	0	Europe	44	2008
3203.	GBR	2021	0	Europe	44	2009
3204.	GBR	2021	0	Europe	44	2010
3205.	GBR	2021	0	Europe	44	2011
3206.	GBR	2021	0	Europe	44	2012
3207.	GBR	2021	0	Europe	44	2013
3208.	GBR	2021	0	Europe	44	2013
3209.	GBR	2021	0	Europe	44	2015
3210.	GBR	2021	0	Europe	44	2016
3210.	GBR	2021	0	Europe	44	2017
3211.	GDR			Europe		2017
3212.	GBR	2021	0	Europe	44	2018
3213.	GBR	2021	0	Europe	44	2019
3214.	GBR	2021	0	Europe	44	2020
3215.	GBR	2021	0	Europe	44	2021
6811.	NOR	1987	0	Europe	10	1978
2040	NOD	4007		T	10	1070
6812.	NOR	1987	0	Europe	10	1979
6813.	NOR	1987	0	Europe	10	1980
6814.	NOR	1987	0	Europe	10	1981
6815.	NOR	1987	0	Europe	10	1982
6816.	NOR	1987	0	Europe	10	1983
6817.	NOR	1987	0	Europe	10	1984
6818.	NOR	1987	0	Europe	10	1985
6819.	NOR	1987	Ö	Europe	10	1986
6820.	NOR	1987	1	Europe	10	1987
3020.						

Analysis

Lastly, we analyze the data using a straightforward logistic regression model. While there is some discussion on this point, we choose not to cluster the standard errors on country, because of the argument from Singer and Willett (2003) that the rows of data are *conditionally* independent.

We ask for *odds ratios* so that our results are roughly comparable to those from the continuous time survival models.

```
. logit event ib4.continent_NUMERIC year, or
               log likelihood = -377.92887
Iteration 0:
               log likelihood = -372.7393
Iteration 1:
Iteration 2:
               log\ likelihood = -330.01528
               log likelihood = -328.96762
Iteration 3:
               log \ likelihood = -328.96528
Iteration 4:
Iteration 5:
               log likelihood = -328.96528
Logistic regression
                                                         Number of obs = 10,156
                                                         LR chi2(6)
                                                                       = 97.93
                                                         Prob > chi2
                                                                       = 0.0000
Log likelihood = -328.96528
                                                         Pseudo R2
                                                                       = 0.1296
            event
                    Odds ratio
                                 Std. err.
                                                      P>|z|
                                                                 [95% conf. interval]
continent_NUMERIC
          Africa
                      .1666907
                                  .0611921
                                              -4.88
                                                      0.000
                                                                 .0811775
                                                                             .3422843
                      .1916195
                                  .0703136
                                              -4.50
                                                      0.000
                                                                 .0933462
                                                                             .3933534
        Americas
            Asia
                      .1507161
                                  .0603004
                                              -4.73
                                                      0.000
                                                                 .0688019
                                                                             .3301562
```

.092426

.0358209

.013881

.0906814

.0351902

1.088786

NA

year

Oceania

-2.36

-3.29

6.67

0.019

0.001

0.000

.012301

.0047859

1.061917

.6684916

.2587488

1.116335

```
_cons | 2.05e-76 5.25e-75 -6.81 0.000 3.38e-98 1.24e-54
```

Note: _cons estimates baseline odds.

. est store Discrete

Cox Model With Multiple Records Per Observation and Time Varying Covariates

We make use of the fact that the data are structured with multiple records per individual to include the effect of year, which is a *time varying covariate*. I am not sure how to use the tvc option to program this when there is only one record per *individual*.

```
. stcox ib4.continent_NUMERIC year
        Failure _d: f==1
  Analysis time _t: year_of_prohibition
Iteration 0:
              log likelihood = -18004.477
               log likelihood = -17501.348
Iteration 1:
               \log likelihood = -17184.551
Iteration 2:
               log likelihood = -17166.754
Iteration 3:
Iteration 4:
               log\ likelihood = -17166.743
Refining estimates:
Iteration 0:
               log\ likelihood = -17166.743
Cox regression with Breslow method for ties
No. of subjects =
                      10,156
                                                         Number of obs = 10,156
No. of failures =
                       1,972
                = 20,506,348
Time at risk
                                                         LR chi2(6)
                                                                        = 1675.47
Log likelihood = -17166.743
                                                                       = 0.0000
                                                         Prob > chi2
                                  Std. err.
                                                       P>|z|
                                                                 [95% conf. interval]
                    Haz. ratio
continent_NUMERIC
                                                       0.000
                                             -25.20
          Africa
                       .2095718
                                  .0129973
                                                                  .185585
                                                                              .2366588
                                             -23.26
                                  .0145656
                                                       0.000
                                                                  .2046728
                                                                              .2619136
        Americas
                        .231531
                                  .0121687
                                             -25.12
                                                       0.000
                                                                 .1535135
                                                                              .2013605
                       .1758169
            Asia
              NA
                       .1294716
                                  .0204464
                                             -12.94
                                                       0.000
                                                                   .095006
                                                                              .1764404
                        .036336
                                  .0067455
                                                                  .0252533
                                                                              .0522826
         Oceania
                                              -17.86
                                                       0.000
                       .9727888
                                  .0018314
                                             -14.65
                                                       0.000
                                                                 .9692059
                                                                              .9763849
```

Compare Estimates

Note the difference in the effect of year in the two models where this is included.

```
. estimates table Weibull Exponential Cox Discrete CoxTVC2, /// > b(\%9.3f) star stats(N r2_a) equations(1) // nice table of estimates
```

Variable Weibull		Exponential	Cox	Discrete	CoxTVC2
#1					
continentC					
Africa	-1.781***	-1.296***	-1.732***	-1.792***	-1.563***
Americas	-1.641***	-1.187**	-1.598***	-1.652***	-1.463***
Asia	-1.883***	-1.390***	-1.826***	-1.892***	-1.738***

[.] est store CoxTVC2

continentC NA Oceania	-2.390* -3.334**	-1.841 -2.797**	-2.334* -3.269**	-2.400* -3.347**	-2.044*** -3.315***
year _cons	-1492.992***	-8.073***		0.085*** -174.278***	-0.028***
ln_p _cons	5.279***				
Statistics N r2_a	248	248	248	10156	10156

Legend: * p<0.05; ** p<0.01; *** p<0.001

References

Allison, P. D. (1984). Event History Analysis: Regression for Longitudinal Event Data. SAGE Publications.

Singer, J. D., & Willett, J. B. (2003). Applied longitudinal data analysis: modeling change and event occurrence. Oxford; New York: Oxford University Press.

StataCorp. 2021. Stata 17 Survival Analysis Reference Manual. College Station, TX: Stata Press