

NUMERICAL PROJECT 1

MTH 5500 STOCHASTIC CALCULUS

- This project counts as **extra credit** (3 points on the final grade).
- The project has to be handed in by **May 7** to get the credits.
- It can be done in teams or **three people or less**.
- The codes have to be **Python**.

- (1) Write a program in Python that does the following:
- (a) Sample 100 independent standard Gaussians using the Box-Muller method.
 - (b) Draw the graph of 10 paths of Brownian motion at 100 integer times.
 - (c) Draw the graph of 10 paths of Brownian motion on $[0, 1]$ with points at every one-hundredth.
 - (d) Draw the graph of 10 paths of Brownian bridge at 100 times.
- I want to see the code and the graph of the paths!
- (2) Consider the stopping time

$$\tau = \min\{t \geq 0 : |B_t| \geq 1\} .$$

This is the first time that B_t reaches 1 or -1 . Draw a histogram for the distribution of τ on $[0, 3]$ using 1000 Brownian paths on $[0, 3]$.