IS606 Bayesian (Homework 9)

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2.1 (p31)

Model A The following code defines a function for the Model A probabilities.

```
xSeq <- seq(1, 4)
modelA <- function(x)
{
   return (1 / 4)
}

dfModelA <- data.frame(x=xSeq, Px=modelA(xSeq))
kable(dfModelA, caption="Model A Probabilities")</pre>
```

Table 1: Model A Probabilities

X	Px
1	0.25
2	0.25
3	0.25
4	0.25

We don't see any bias in the Model A probabilities. They are all equal.

Model B The following code defines a function for the Model B probabilities.

```
modelB <- function(x)
{
   return (x / 10)
}

dfModelB <- data.frame(x=xSeq, Px=modelB(xSeq))
kable(dfModelB, caption="Model B Probabilities")</pre>
```

Table 2: Model B Probabilities

x	Px	
1	0.1	
2	0.2	
3	0.3	
4	0.4	

Model B is biased toward the higher numbers.

Model C The following code defines a function for the Model C probabilities.

```
modelC <- function(x)
{
   return (12 / (25 * x))
}

dfModelC <- data.frame(x=xSeq, Px=modelC(xSeq))
kable(dfModelC, caption="Model C Probabilities")</pre>
```

Table 3: Model C Probabilities

x	Px
1	0.48
2	0.24
3	0.16
4	0.12

Model C is biased toward the lower numbers, slightly more so than Model B was toward the higher numbers.

5.1 (p118)

The following code works throught the test for a disease and retest scenario for an individual.

```
# Define marginal probabilities
marginalProbDiseasePresent <- 0.001
marginalProbDiseaseAbsent <- 1 - marginalProbDiseasePresent
# Define composite probabilities
probTestPosGivenDisPresent <- 0.99
probTestPosGivenDisAbsent <- 0.05
# Func of Bayes rule
bayesRule <- function(likelihood, prior, evidence)
{
   return ((likelihood * prior) / sum(evidence))
}</pre>
```

First we compute the probability of having the disease given the test is positive.

[1] 0.01943463

Now, after a re-test and a negative result, what is the probability of having the disease?

```
pPrior <- probDisPresentGivenTestPost</pre>
probTestNegGivenDisPresent <- (1 - probTestPosGivenDisPresent)</pre>
evidence <- c(probTestNegGivenDisPresent * pPrior,</pre>
              (1 - probTestPosGivenDisAbsent) * (1 - pPrior))
# Call function to compute probability of disease present given a negative test.
probDisPresentGivenTestNeg <- bayesRule(probTestNegGivenDisPresent,</pre>
                                           pPrior,
                                           evidence)
format(probDisPresentGivenTestNeg, scientific = FALSE)
## [1] "0.0002085862"
5.2 (p118)
n <- 100000
probTestNegGivenDisAbsent <- 1 - probTestPosGivenDisAbsent</pre>
dfTable <- data.frame(ThetaSad=c(99, 1, 100),
                       ThetaHappy=c(probTestPosGivenDisAbsent * marginalProbDiseaseAbsent * n,
                                    probTestNegGivenDisAbsent * marginalProbDiseaseAbsent * n,
                       Col3=c(NA, NA, 100000))
dfTable$Col3 <- dfTable$ThetaSad + dfTable$ThetaHappy</pre>
dfTable
a) Table
     ThetaSad ThetaHappy
##
                            Co13
## 1
          99
                    4995
                            5094
## 2
           1
                   94905 94906
## 3
          100
                   99900 100000
```

b) Proportion of people who have the disease given their test result is positive Computing:

```
b <- 99 / 5094
b
```

[1] 0.01943463