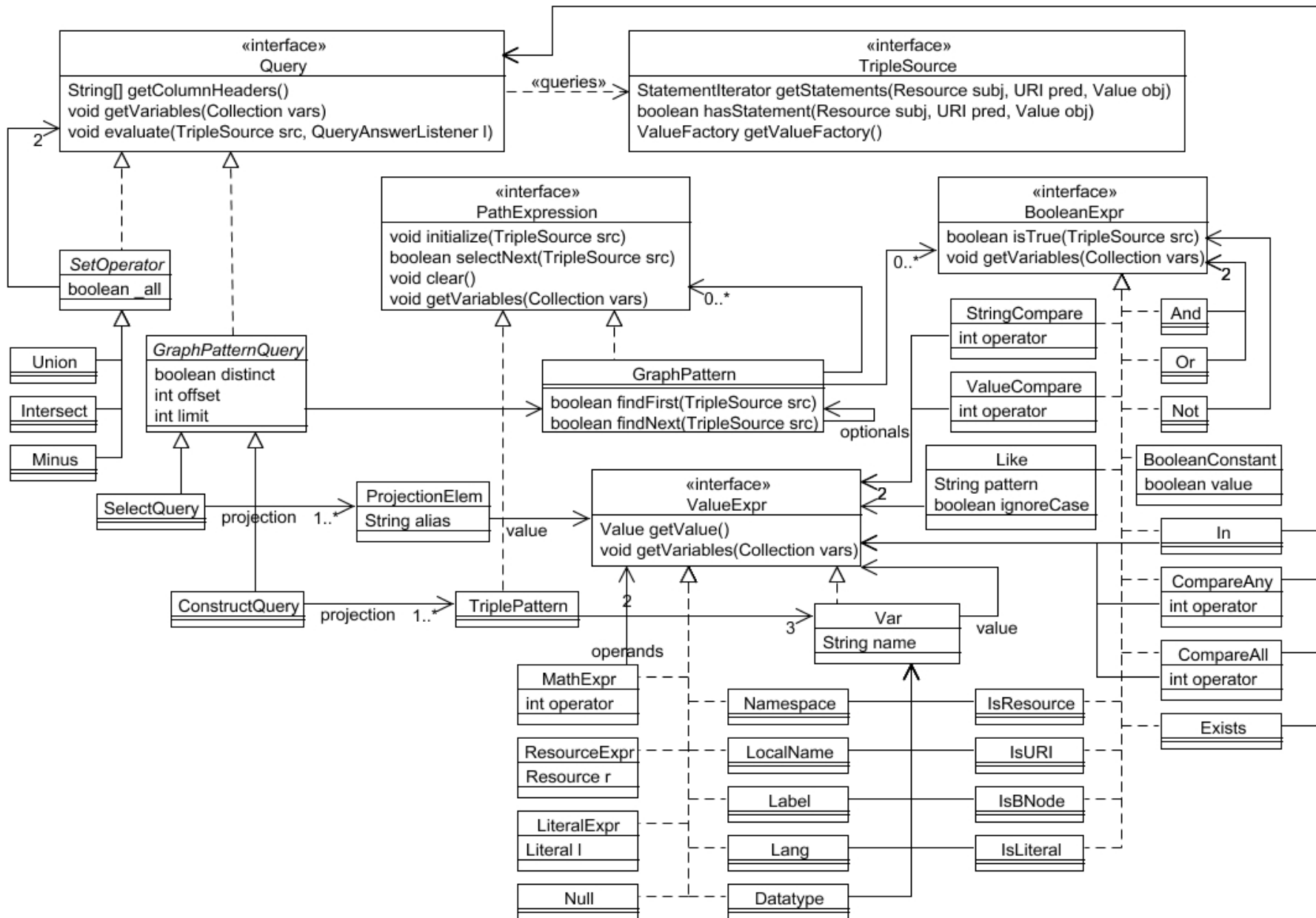
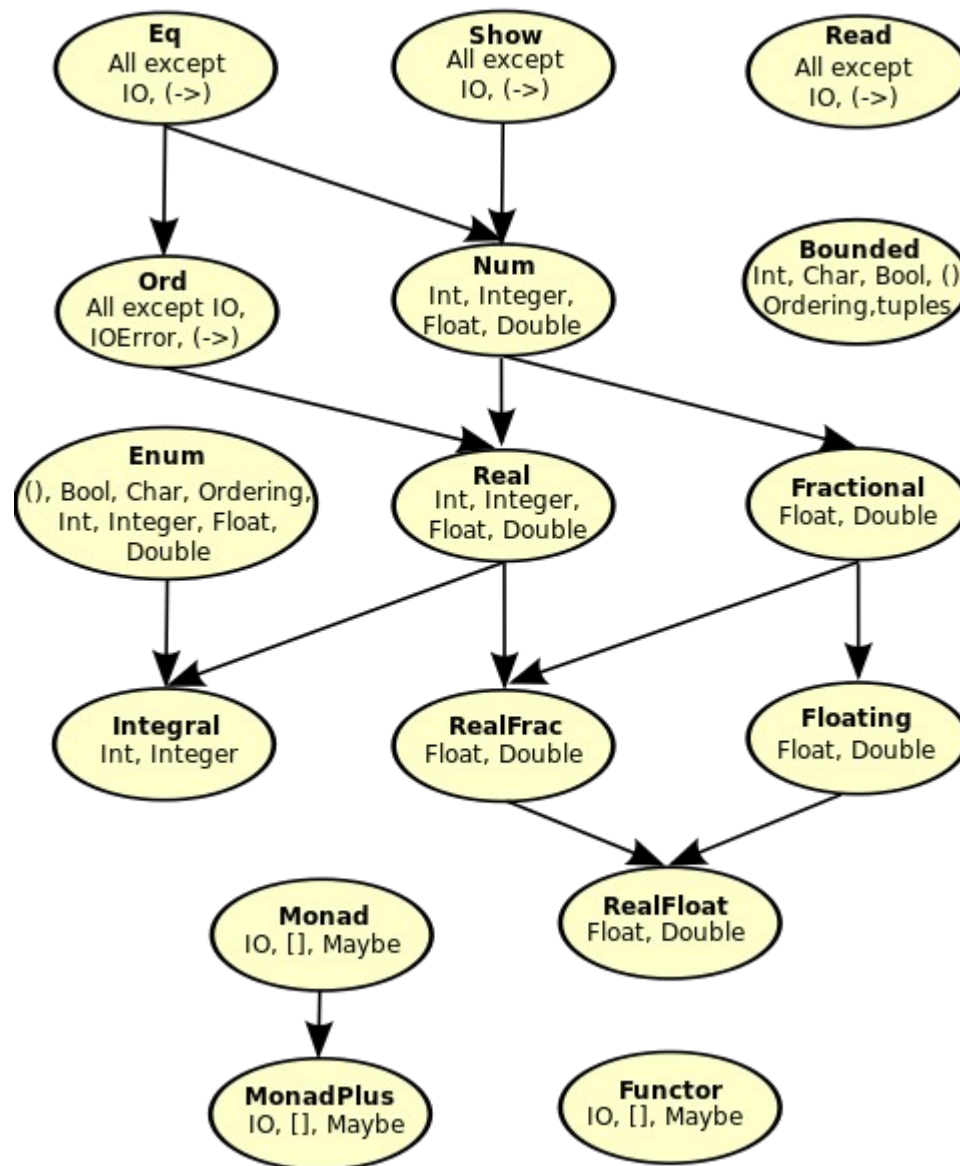


# Типы



# Типы





# Типы

```
data Anniversary =  
    Birthday String Int Int Int  
    | Wedding String String Int Int Int  
    | Death String Int Int Int  
  
> Birthday "someone" 2012 11 7  
Birthday "someone" 2012 11 7  
> let today = Birthday "someone" 2012 11 7  
> today  
Birthday "someone" 2012 11 7  
> :t today  
today :: Anniversary
```

# Типы

```
> :t Birthday
```

```
Birthday :: String -> Int -> Int -> Int ->  
Anniversary
```

```
> :t Death
```

```
Birthday :: String -> Int -> Int -> Int ->  
Anniversary
```

# Типы

```
kurtCobain :: Anniversary
```

```
kurtCobain = Birthday "Kurt Cobain" 1967 2 20
```

```
kurtWedding :: Anniversary
```

```
kurtWedding = Wedding "Kurt Cobain" "Courtney  
Love" 1990 1 12
```

# Типы

```
anniversaries = [  
    kurtCobain,  
    kurtWedding,  
    Death "Kurt Cobain" 1994 4 5  
]
```

# Типы

```
type AnniversaryBook = [Anniversary]
```

```
showDate :: Int -> Int -> Int -> String
```

```
showDate y m d = show y ++ "." ++ show m ++ "."  
++ show d
```



# Типы

```
showAnniversary :: Anniversary -> String
```

```
showAnniversary (Birthday name year month day) =  
    name ++ " born " ++ showDate year month day
```

```
showAnniversary (Wedding name1 name2 year month day) =  
    name1 ++ " married " ++ name2 ++ " on " ++ showDate  
    year month day
```

```
showAnniversary (Death name year month day) =  
    name ++ " dead in " ++ showDate year month day
```

# Типы

```
who :: Anniversary -> String
who (Birthday him _ _ _) = him
who (Wedding him _ _ _ _) = him
who (Death him _ _ _) = him
```

```
map who anniversaries
```

# Типы

```
showAnniversaries :: AnniversaryBook -> [String]
```

```
showAnniversaries = map showAnniversary
```

```
["Kurt Cobain born 1967-2-20", "Kurt Cobain married  
Courtney Love on 1990-1-12", "Kurt Cobain dead 1994-4-5"]
```

1) Kurt Cobain born 1967-2-20

2) Kurt Cobain married Courtney Love on 1990-1-12

3) Kurt Cobain dead 1994-4-5

?

# Типы

```
> anniversaries
```

```
No instance for (Show Anniversary)
  arising from a use of `print'
```

```
Possible fix: add an instance declaration for (Show Anniversary)
```

```
In a stmt of an interactive GHCi command: print it
```

```
data Anniversary =
  Birthday String Int Int Int
  | Wedding String String Int Int Int
  | Death String Int Int Int
deriving (Show)
```

# Всё человечно м.б.

```
data Point = Pt {pointx, pointy :: Float}
```

```
> let myPoint = Pt {pointx = 42.0, pointy = 13.666}
```

json?

```
pointx :: Point -> Float
```

```
pointy :: Point -> Float
```

```
absPoint :: Point -> Float
```

```
absPoint p = sqrt (pointx p * pointx p + pointy p * pointy p)
```

```
absPoint (Pt {pointx = x, pointy = y}) = sqrt (x*x + y*y)
```

# Параметры типов

```
data Maybe a = Nothing | Just a
```

привет, полиморфизм!  
дженерики

```
> Just "str"
```

```
Just "str"
```

```
> :t Just "str"
```

```
Just "str" :: Maybe [Char]
```

```
> Just 42
```

```
Just 42
```

```
> :t Just 42
```

```
Just 42 :: (Num t) => Maybe t
```

```
> :t Nothing
```

```
Nothing :: Maybe a
```

```
> Just 42 :: Maybe Double
```

```
Just 42.0
```

```
> Just 42 : [Nothing] ?
```

```
> Just 42 : [Just "str", Nothing] ?
```

# Рекурсивные структуры

```
data List a = Nil | Cons a (List a) deriving (Show,  
                                             Read, Eq, Ord)
```

```
> 3 `Cons` (4 `Cons` (5 `Cons` Nil))  
Cons 3 (Cons 4 (Cons 5 Nil))
```

# Рекурсивные структуры

```
infixr 5 :-:
```

```
data List a = Nil | a :-: (List a) deriving (Show, Read, Eq, Ord)
```

```
> let a = 3 :-: 4 :-: 5 :-: Nil
```

```
> 100 :-: a
```

```
(:-:) 100 ((:-:) 3 ((:-:) 4 ((:-:) 5 Nil)))
```

слонёнок



# Рекурсивные структуры

```
infixr 5 .++
```

```
(.++) :: List a -> List a -> List a
```

```
Nil .++ ys = ys
```

```
(x :-: xs) .++ ys = x :-: (xs .++ ys)
```

```
> let a = 3 :-: 4 :-: 5 :-: Nil
```

```
> let b = 6 :-: 7 :-: Nil
```

```
> a .++ b
```

```
(:-:) 3 ((:-:) 4 ((:-:) 5 ((:-:) 6 ((:-:) 7 Nil))))
```



# Рекурсивные структуры

```
data Tree a =  
  EmptyTree  
  | Node a (Tree a) (Tree a)  
  deriving (Show, Read, Eq)
```

# Рекурсивные структуры

```
singleton :: a -> Tree a
singleton x = Node x EmptyTree EmptyTree

treeInsert :: (Ord a) => a -> Tree a -> Tree a
treeInsert x EmptyTree = singleton x
treeInsert x (Node a left right)
  | x == a = Node x left right
  | x < a  = Node a (treeInsert x left) right
  | x > a  = Node a left (treeInsert x right)
```

# W/o foldr

`list2tree :: (Ord a) => [a] -> Tree a`

`list2tree = l2t EmptyTree`

where

`l2t acc [] = acc`

`l2t acc (head:tail) = l2t (treeInsert head acc) tail`

`list2tree [12, 1, 6, 4, 90, 9]`

# tree2list

`tree2list :: (Ord a) => Tree a -> [a]`

`tree2list EmptyTree = ?`

`tree2list (Node val left right) = ?`

# tree2list

```
tree2list :: (Ord a) => Tree a -> [a]
tree2list EmptyTree = []
tree2list (Node val left right) =
    (tree2list left) ++ (val : tree2list right)
```

```
treeSort :: (Ord a) => [a] -> [a]
treeSort = tree2list . list2tree
```

```
> treeSort [12, 1, 6, 4, 90, 9]
```

# tree2list

```
tree2list :: (Ord a) => Tree a -> [a]  
tree2list EmptyTree = []  
tree2list (Node val left right) = ?
```

```
treeSortDesc :: (Ord a) => [a] -> [a]  
treeSortDesc = tree2list . list2tree
```

```
> treeSort [12, 1, 6, 4, 90, 9]
```



# Рекурсивные структуры

Кол-во вершин дерева (== кол-во чисел в нём)

```
treeNum :: Tree a -> Int
```

# Рекурсивные структуры

```
treeNum :: Tree a -> Int
```

```
treeNum EmptyTree = 0
```

```
treeNum (Node val left right) = 1 + (treeNum left) +  
(treeNum right)
```

# Рекурсивные структуры

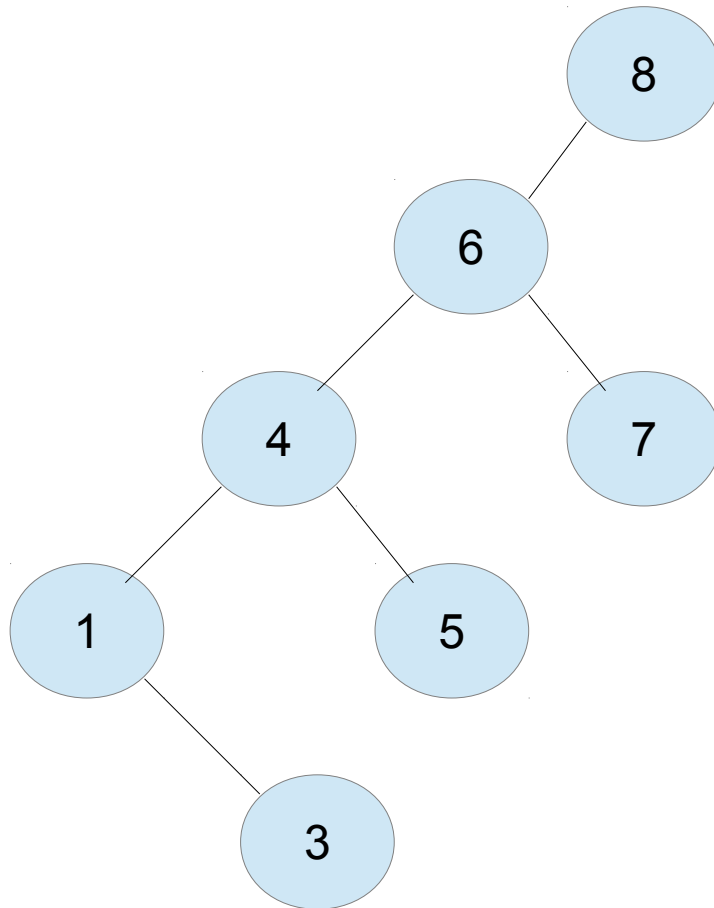
Дерево можно кодировать наборами из нулей и единиц. Рассмотрим, например, укладку дерева на плоскости. Начиная с какой либо вершины, будем двигаться по ребрам дерева, сворачивая в каждой вершине на ближайшее справа ребро и поворачивая назад в концевых вершинах дерева. Проходя по некоторому ребру, записываем 0 при движении по ребру в первый раз и 1 при движении по ребру второй раз (в обратном направлении). Если  $m$  — число рёбер дерева, то через  $2m$  шагов мы вернемся в исходную вершину, пройдя по каждому ребру дважды. Полученная при этом последовательность из 0 и 1 (код дерева) длины  $2m$  позволяет однозначно восстанавливать не только само дерево  $D$ , но и его укладку на плоскости.

# Рекурсивные структуры

```
treeCode :: Tree a -> [Int]
treeCode EmptyTree = []
treeCode (Node val left right) =
    ([0] ++ treeCode left ++ [1]) ++ ([0] ++ treeCode right ++ [1])
```

```
>treeCode $ list2tree [8,6,4,1,7,3,5]
[0,0,0,0,1,0,0,1,0,1,1,1,0,0,1,0,1,1,1,0,0,1,0,1,1,1,0,1]
```

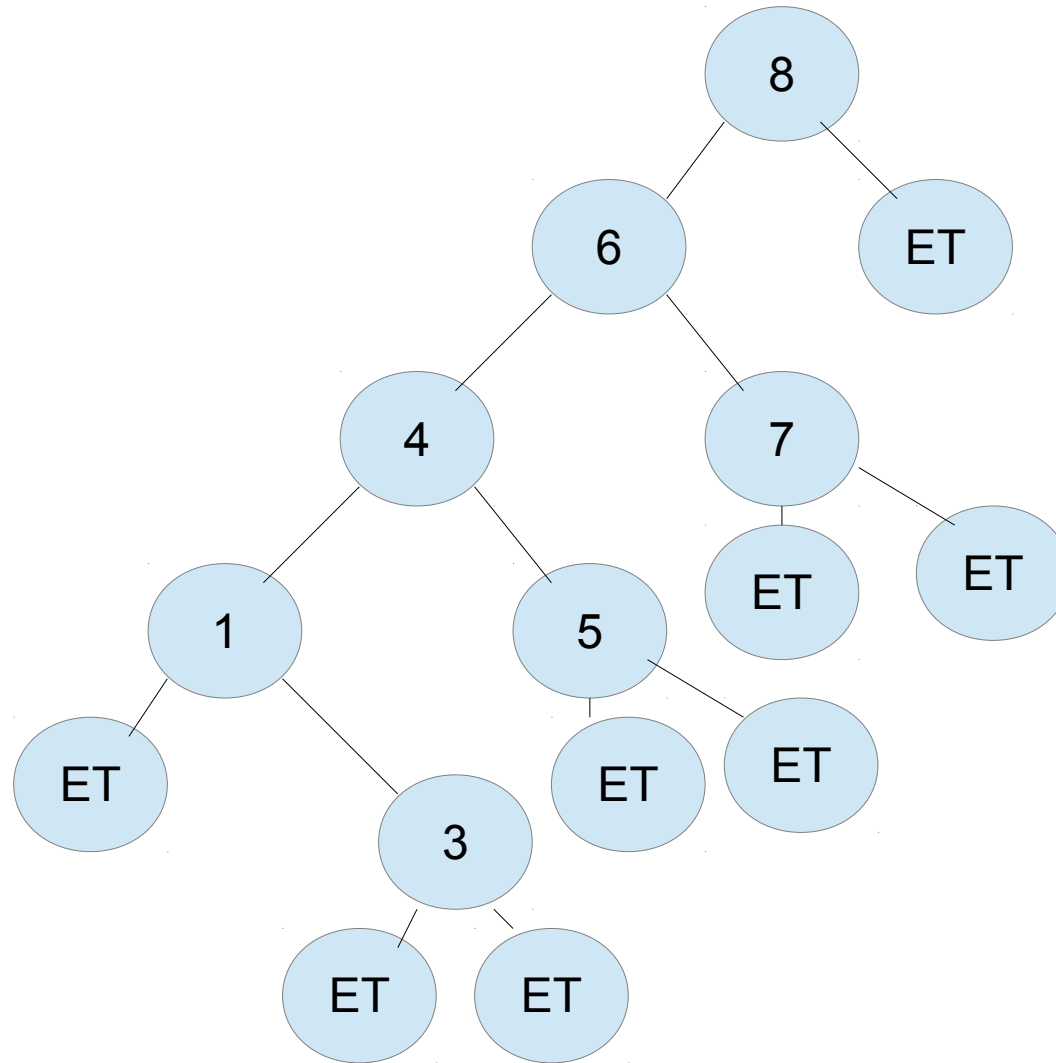
# Рекурсивные структуры



Моя функция не работает!!!111  
Why?

[0,0,0,0,1,0,0,1,0,1,1,1,0,0,1,0,1,1,1,0,0,1,0,1,1,1,0,1]

# Рекурсивные структуры



[0,0,0,0,1,0,0,1,0,1,1,1,0,0,1,0,1,1,1,0,0,1,0,1,1,1,0,0,1]

# Рекурсивные структуры

`list2tree [12, 12, 12, 13, 13, 14]`

Как будет выглядеть дерево?

# Рекурсивные структуры

data Tree = ?

singleton :: a -> Tree a  
singleton x = ?

treeInsert :: (Ord a) => a -> Tree a -> Tree a  
treeInsert x EmptyTree = singleton x  
?

list2tree :: (Ord a) => [a] -> Tree a  
list2tree = ?



# Рекурсивные структуры

```
data Tree a = EmptyTree | Node a Int (Tree a) (Tree a) deriving (Show, Read, Eq)
```

```
singleton :: a -> Tree a
singleton x = Node x 1 EmptyTree EmptyTree
```

```
treeInsert :: (Ord a) => a -> Tree a -> Tree a
treeInsert x EmptyTree = singleton x
treeInsert x (Node a i left right)
  | x == a = Node x (i+1) left right
  | x < a  = Node a i (treeInsert x left) right
  | x > a  = Node a i left (treeInsert x right)
```

```
list2tree :: (Ord a) => [a] -> Tree a
list2tree = l2t EmptyTree
  where
    l2t acc [] = acc
    l2t acc (head:tail) = l2t (treeInsert head acc) tail
```