

## The Wave Problem.....

The *Wave Equation* is

$$u_{tt} = c(u_{xx} + u_{yy})$$

where  $c$  is a constant and  $u = u(t, x, y)$ . This equation can be modeled discretely using finite differences as:

$$u_{t+1,x,y} = 2(1 - 2\rho^2)u_{t,x,y} + \rho^2(u_{t,x+1,y} + u_{t,x-1,y} + u_{t,x,y-1} + u_{t,x,y+1}) - u_{t-1,x,y}$$

where  $\rho = \Delta t / h$ ,  $\Delta t$  is the time step in the time direction, and  $h$  is the step size in the  $x$  and  $y$  directions.

Calculating the new value of  $u$  at time  $t+1$  requires only the value of  $u$  at times  $t$  and  $t-1$ . So, only two time steps are needed to be stored in memory simultaneously.