

$$c) \bar{\pi}(Y=+1) = \int \int_{x_1, x_2} P(Y=+1 | X) \cdot P(X) \, dx_1, dx_2$$

$$= \int_0^1 \int_0^1 \frac{x_1 + x_2}{2} \cdot 3x_2^2 \, dx_1, dx_2$$

$$= \frac{3}{2} \int_0^1 \int_0^1 (x_1 x_2^2 + \frac{2}{3} x_2^3) \, dx_1, dx_2$$

$$= \frac{3}{2} \int_0^1 \left[ \frac{1}{2} x_1^2 x_2^2 + \frac{2}{3} x_1 x_2^3 \right]_0^1 dx_2$$

$$= \frac{3}{2} \int_0^1 \left( \frac{1}{2} x_2^2 + \frac{2}{3} x_2^3 \right) dx_2$$

$$= \frac{3}{2} \left[ \frac{1}{6} x_2^3 + \frac{2}{4} x_2^4 \right]_0^1$$

$$= \frac{3}{2} \left[ \frac{1}{6} + \frac{1}{2} \right]$$