

# <sup>1</sup> cosmo-numba: B-modes and COSEBIs computations accelerated by Numba

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## Software

- <sup>6</sup> [Review](#) 
- <sup>7</sup> [Repository](#) 
- <sup>8</sup> [Archive](#) 

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<sup>10</sup> Creative Commons Attribution 4.0 International License ([CC BY 4.0](#)).  
<sup>11</sup> Cosmo-numba facilitate the computation of E-/B-modes decomposition using two methods. One  
<sup>12</sup> of them is the Complete Orthogonal Sets of E-/B-mode Integrals (COSEBIs) as presented in  
<sup>13</sup> P. Schneider et al. (2010). The COSEBIs rely on very high precision computation requiring  
<sup>14</sup> more than 80 decimal numbers. P. Schneider et al. (2010) propose an implementation  
<sup>15</sup> using mathematica. cosmo-numba make use of combination of sympy and mpmath to reach the  
<sup>16</sup> required precision. This python version enable an easier integration in cosmology pipeline and  
<sup>17</sup> facilitate the null tests.

<sup>18</sup> This software package also include the computation of the pure-mode correlation functions  
<sup>19</sup> presented in Peter Schneider et al. (2022). Those integrals have less constraints than the  
<sup>20</sup> COSEBIs but having a fast computation is necessary to computing the covariance matrix. One  
<sup>21</sup> can also include use those correlation function for cosmological inference in which case the  
<sup>22</sup> multiple call to the likelihood will also require a fast implementation.

## COSEBIs

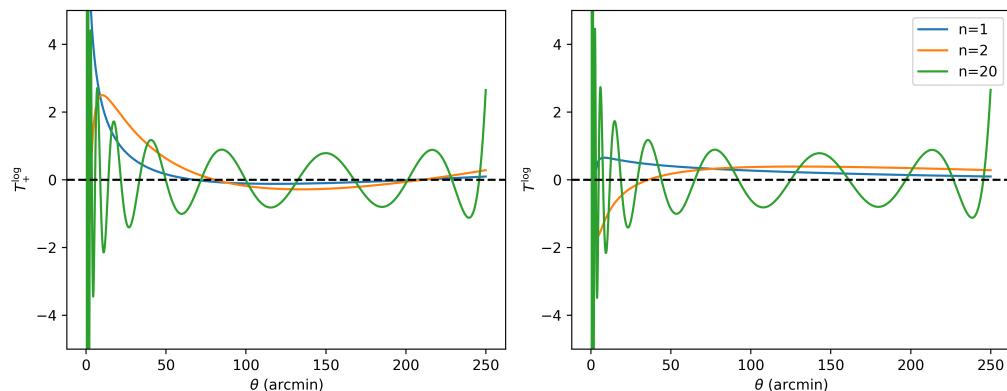
<sup>23</sup> The COSEBIs are defined as:

$$E_n = \frac{1}{2} \int_0^\infty d\theta \theta [T_{n,+}(\theta) \xi_+(\theta) + T_{n,-}(\theta) \xi_-(\theta)] B_n = \frac{1}{2} \int_0^\infty d\theta \theta [T_{n,+}(\theta) \xi_+(\theta) - T_{n,-}(\theta) \xi_-(\theta)] \quad (1)$$

<sup>24</sup> where  $\xi_\pm(\theta)$  are the shear correlation functions, and  $T_{n,\pm}$  are the weight functions for the  
<sup>25</sup> mode  $n$ . The complexity is in the computation of reside in the computation of the weight  
<sup>26</sup> functions. Cosmo-numba include do the computation of the weight functions in logarithmic  
<sup>27</sup> scale defined by:

$$T_{n,+}^{\log}(\theta) = t_{n,+}^{\log}(z) = N_n \sum_{j=0}^{n+1} c_{jn}^- z^j \quad (2)$$

<sup>28</sup> where  $z = \log(\theta/\theta_{\min})$ ,  $N_n$  is the normalization for the mode  $n$ , and  $c_{jn}^-$  are defined iteratively  
<sup>29</sup> from Bessel functions (we refer the readers to P. Schneider et al. (2010) for more details).



**Figure 1:** Caption for example figure.

## 30 Mathematics

- 31 Single dollars (\$) are required for inline mathematics e.g.  $f(x) = e^{\pi/x}$
- 32 Double dollars make self-standing equations:

$$\Theta(x) = \begin{cases} 0 & \text{if } x < 0 \\ 1 & \text{else} \end{cases}$$

- 33 You can also use plain L<sup>A</sup>T<sub>E</sub>X for equations

$$\hat{f}(\omega) = \int_{-\infty}^{\infty} f(x) e^{i\omega x} dx \quad (3)$$

- 34 and refer to [Equation 3](#) from text.

## 35 Citations

- 36 Citations to entries in paper.bib should be in [rMarkdown](#) format.
- 37 If you want to cite a software repository URL (e.g. something on GitHub without a preferred citation) then you can do it with the example BibTeX entry below for (?).
- 38 For a quick reference, the following citation commands can be used: - @author:2001 -> "Author et al. (2001)" - [@author:2001] -> "(Author et al., 2001)" - [@author1:2001; @author2:2001] -> "(Author1 et al., 2001; Author2 et al., 2002)"

## 42 Figures

- 43 Figures can be included like this: [Caption for example figure.](#) and referenced from text using [section](#).
- 44 Figure sizes can be customized by adding an optional second parameter: [Caption for example figure.](#)

## 47 Acknowledgements

- 48 We acknowledge contributions from Brigitta Sipocz, Syrtis Major, and Semyeong Oh, and
- 49 support from Kathryn Johnston during the genesis of this project.

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