

# Redes Neuronales

Adaptive-Network-Based  
Fuzzy Inference Systems  
(redes ANFIS)



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## Redes Neuronales: ANFIS

- "Esta goma es blanca"

- "Y... sí"



color<sub>blanco</sub> (*Maped*) = 1

## Redes Neuronales: ANFIS

- "Esta goma es blanca"
- "Mmm... más o menos"

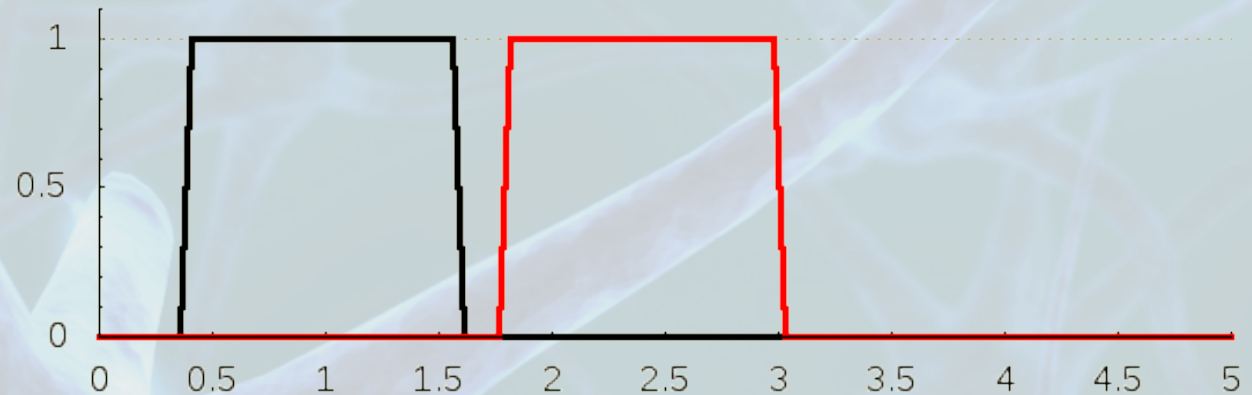


color<sub>blanco</sub> (*Faber-Castell*) = 0.65

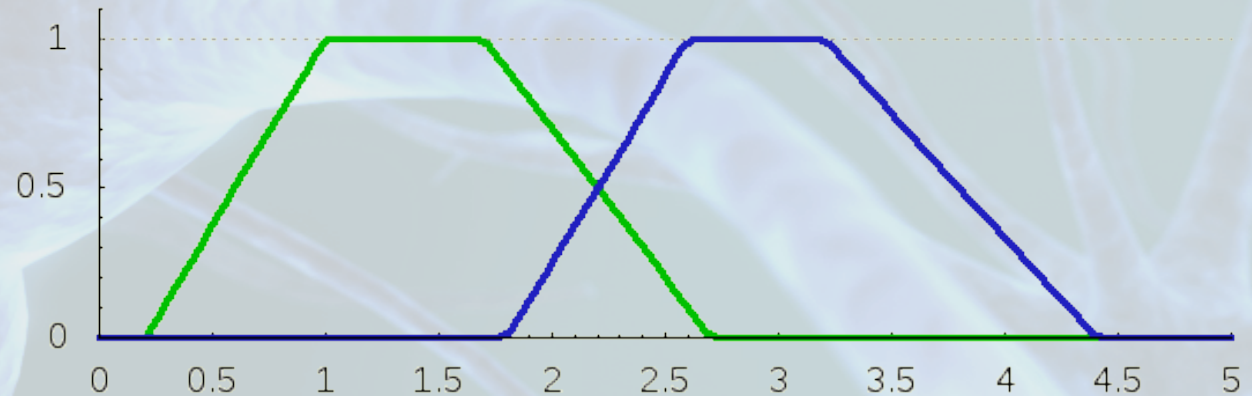
color<sub>gris</sub> (*Faber-Castell*) = 0.35

# Redes Neuronales: ANFIS

Caso “crisp”:

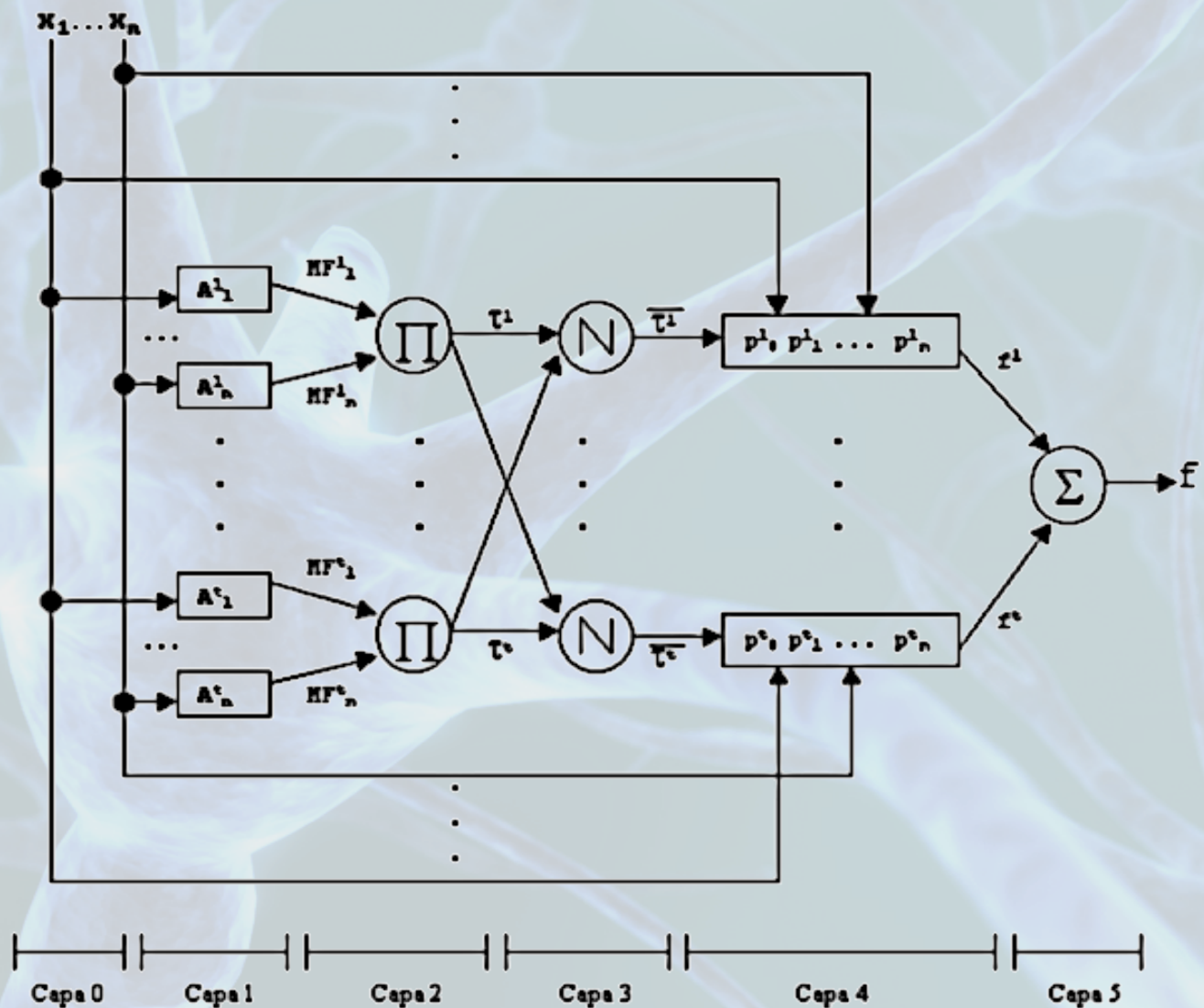


Caso “difuso”:



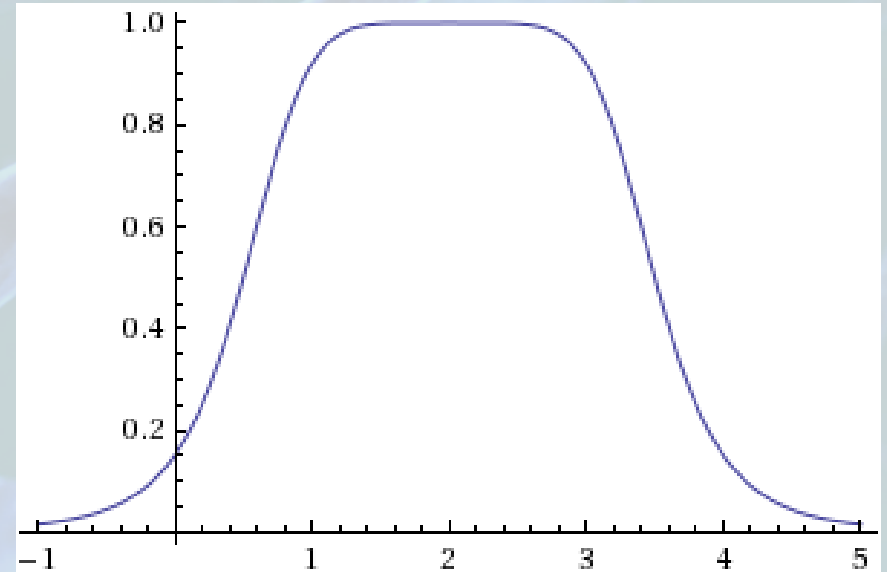
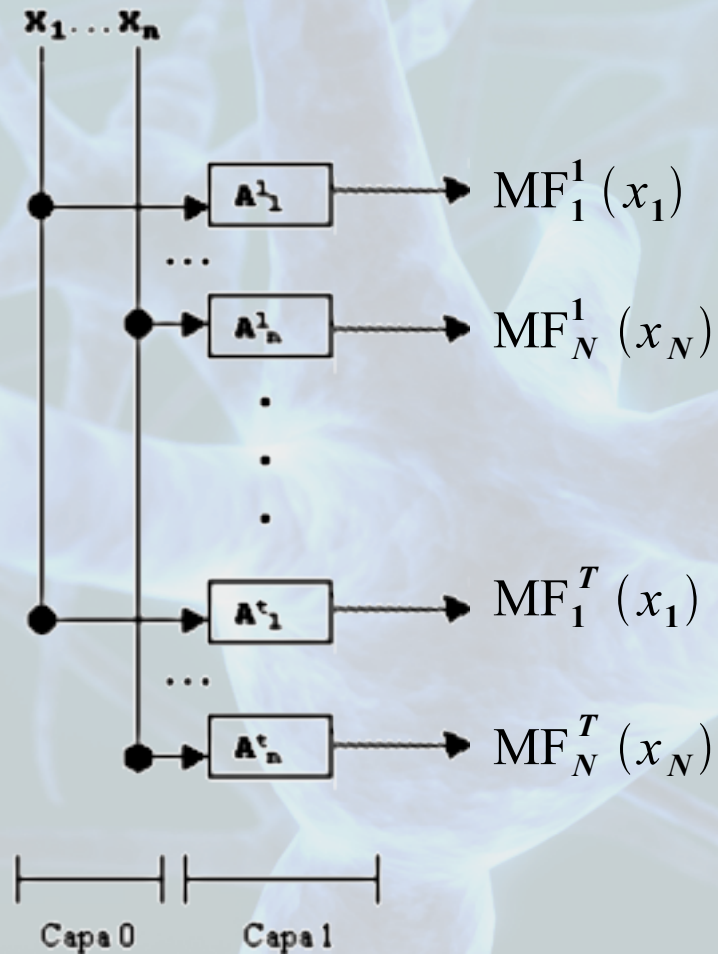


# Redes Neuronales: ANFIS



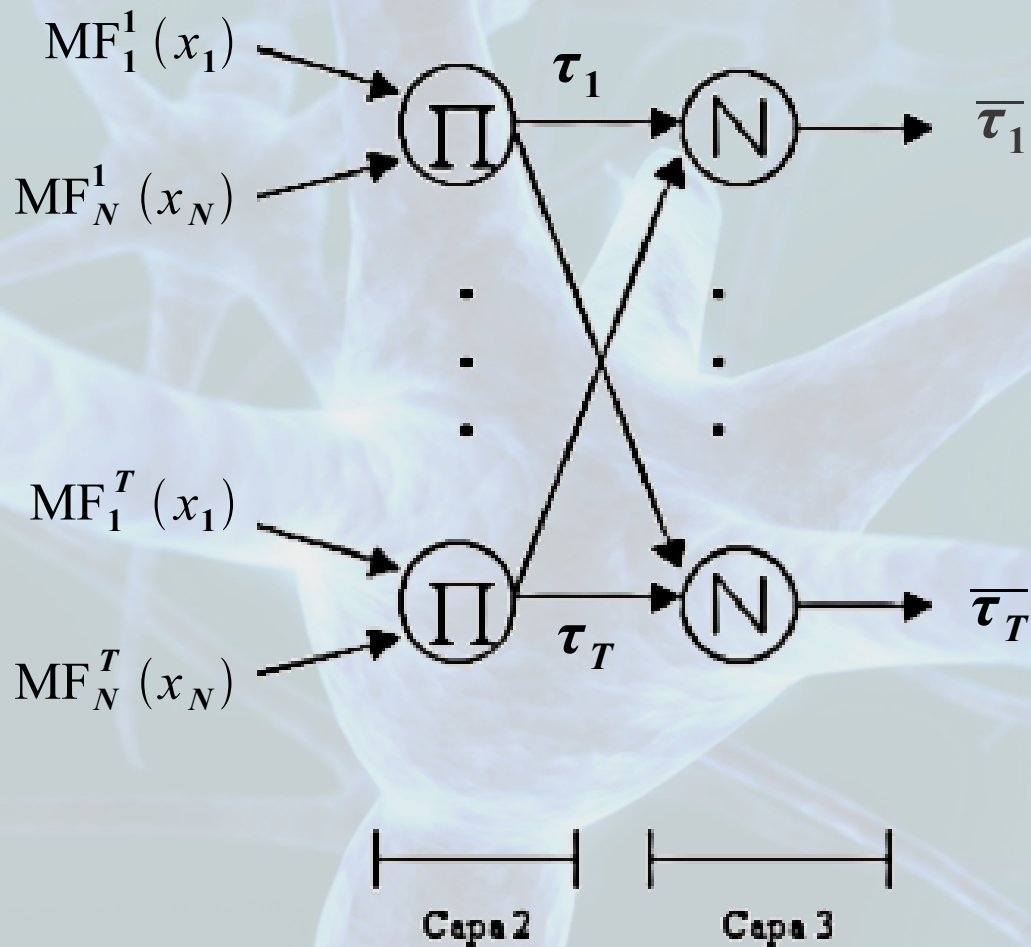
# Redes Neuronales: ANFIS

Funciones membresía de tipo bell:



$$f_{a,b,c}(x) = \frac{1}{1 + \left| \frac{x-c}{a} \right|^{2b}}$$

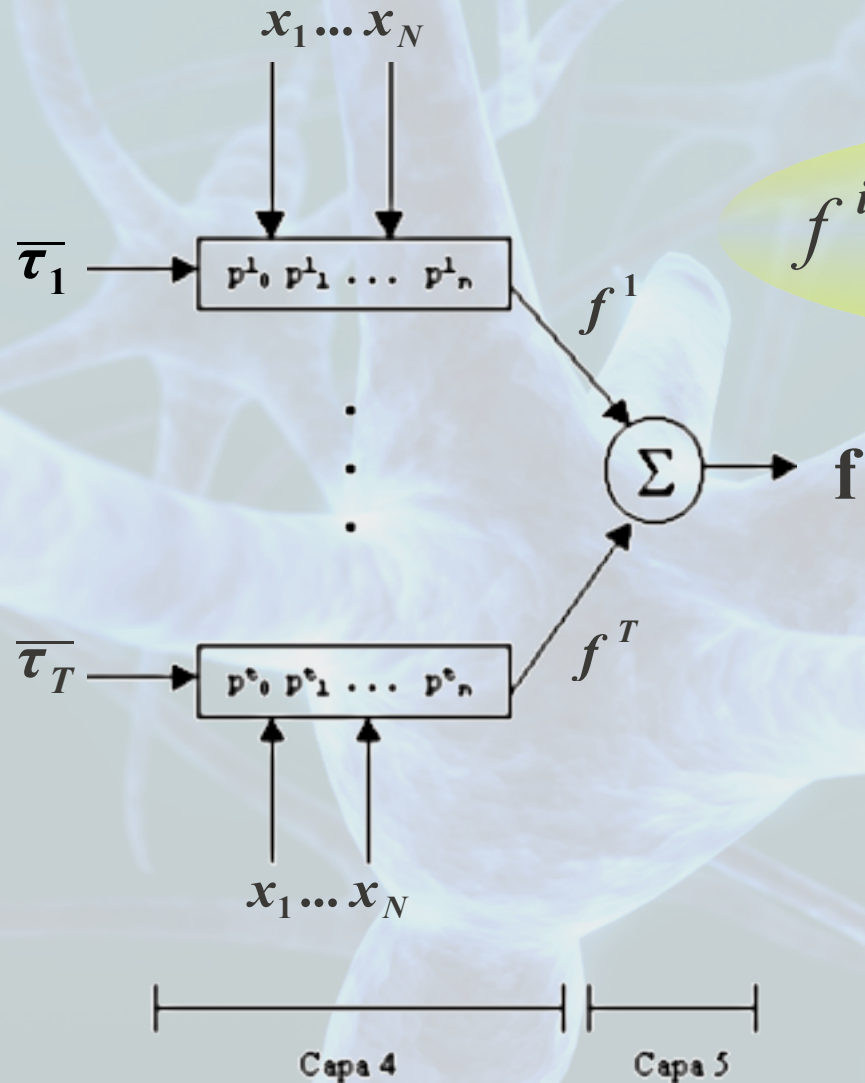
# Redes Neuronales: ANFIS



$$\tau_i(\vec{x}) = \prod_{j=1}^N MF_j^i(\vec{x})$$

$$\bar{\tau}_i(\vec{x}) = \frac{\tau_i(\vec{x})}{\sum_{j=1}^T \tau_j(\vec{x})}$$

# Redes Neuronales: ANFIS



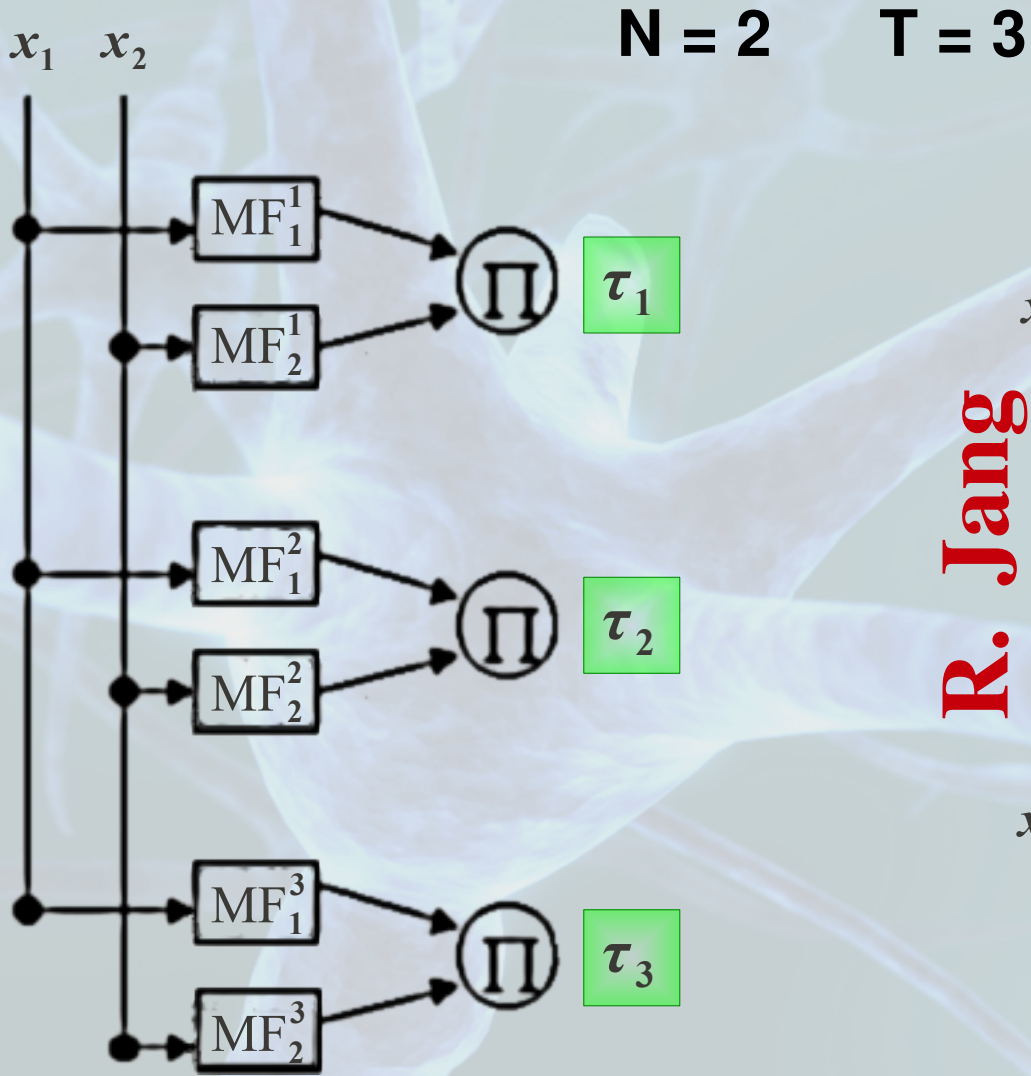
$$f^i(\vec{x}) = (p^i_0 + x_1 p^i_1 + \dots + x_N p^i_N) \bar{\tau}_i$$

$$f(\vec{x}) = \sum_{i=1}^T f^i(\vec{x})$$

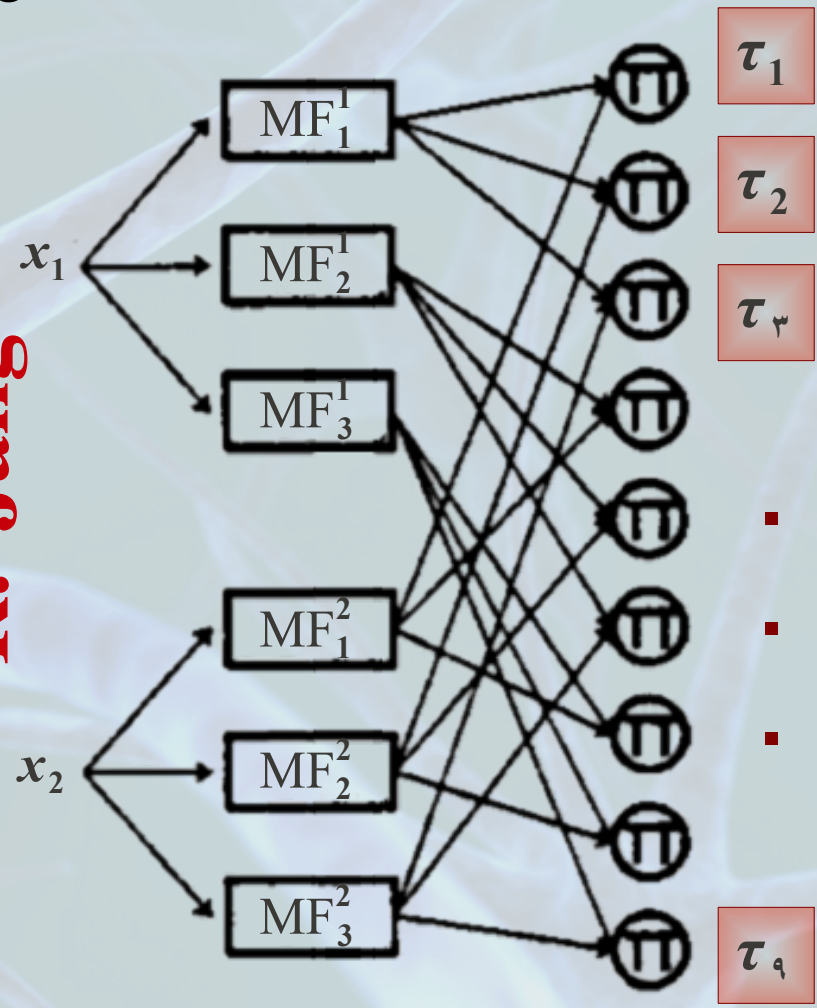


# Redes Neuronales: ANFIS

N. Bruno



R. Jang



# Redes Neuronales: ANFIS

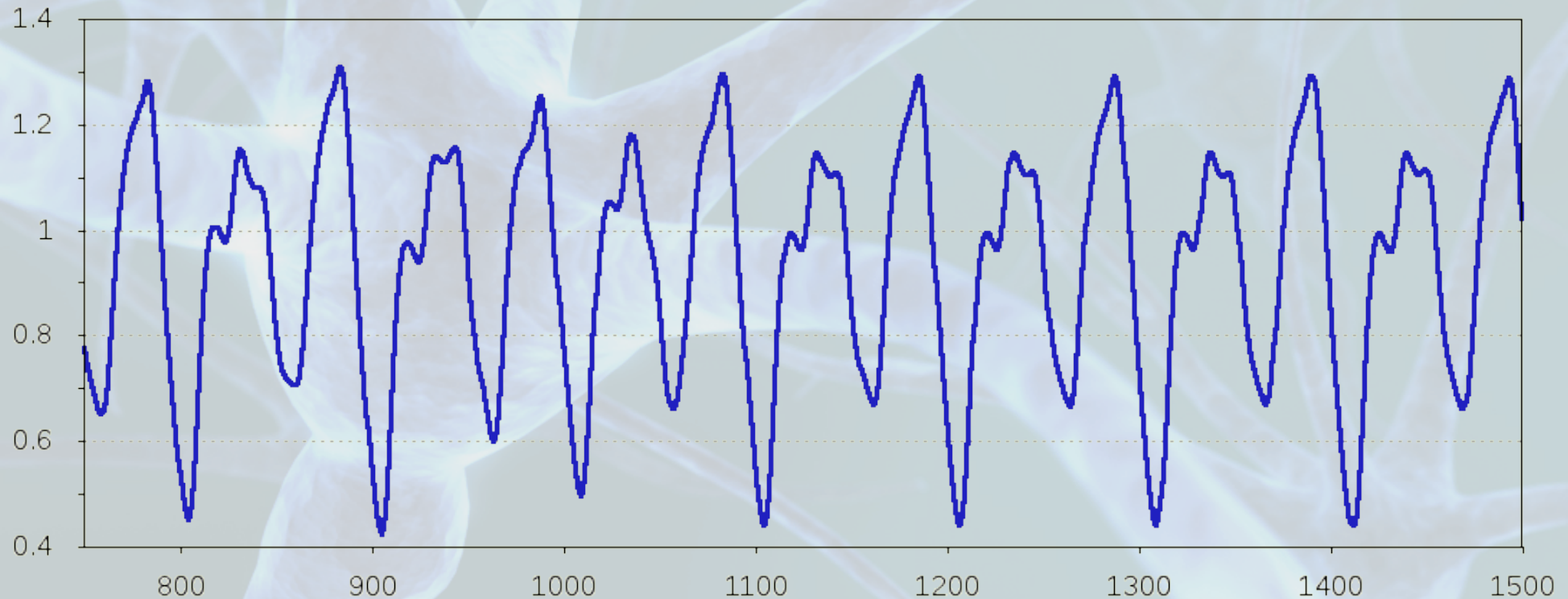
**Mackey-Glass** differential delay equation:

$$\dot{x}(t) = \frac{0.2 \ x(t-\tau)}{1 + x^{10}(t-\tau)} - 0.1 \ x(t)$$

Parameters:

$$\tau = 17$$

$$x(0) = 1.2$$



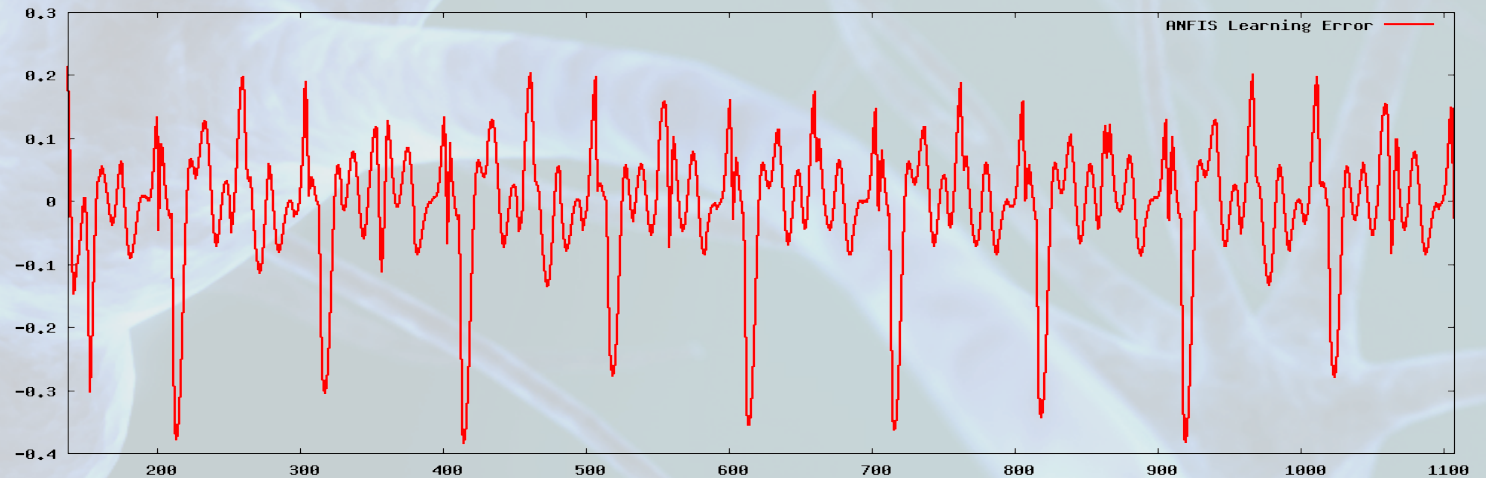
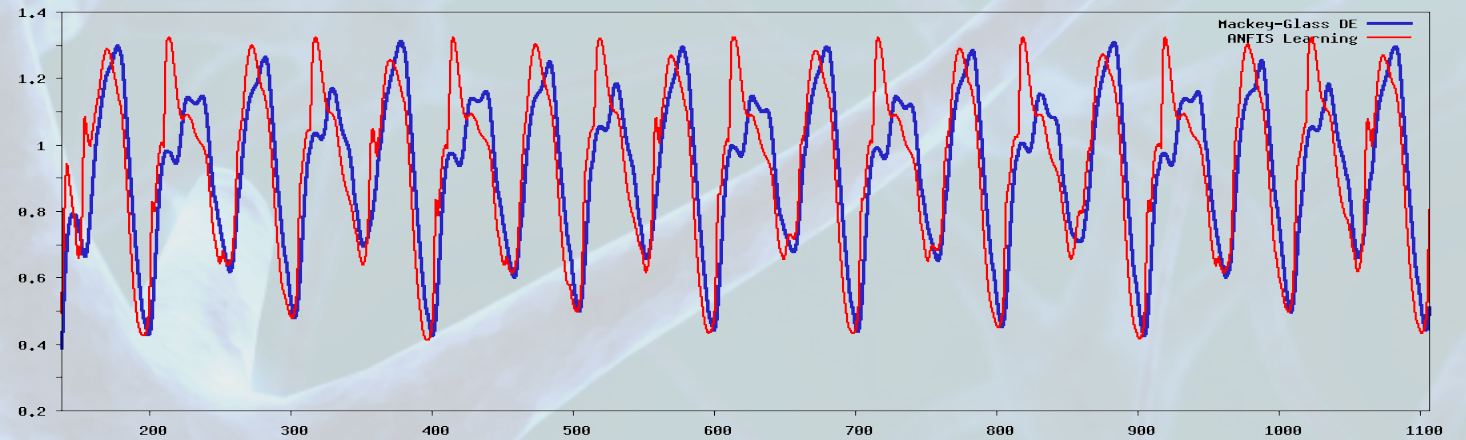
# Redes Neuronales: ANFIS

**N. Bruno**

$T = 2$

$N = 4$

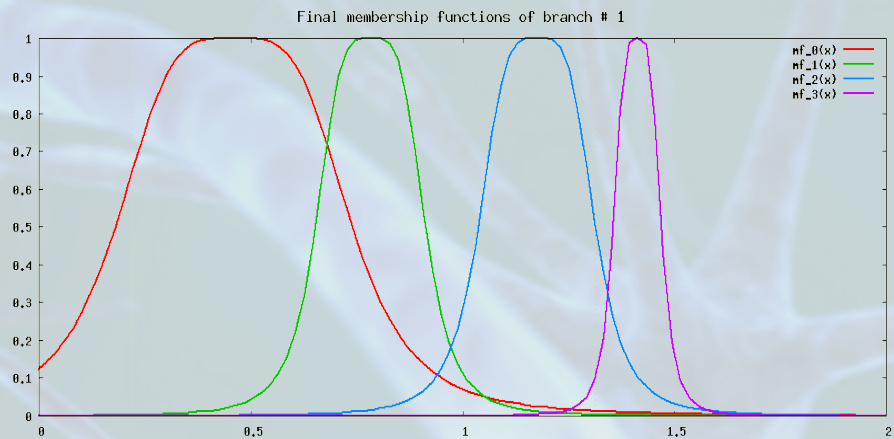
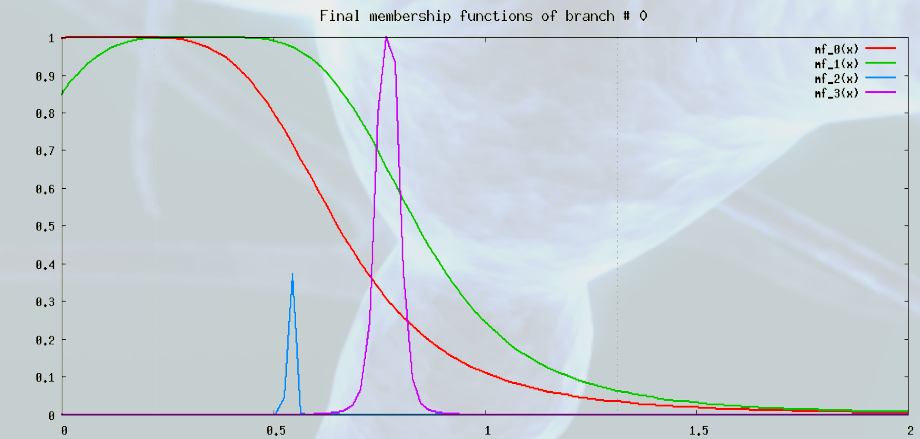
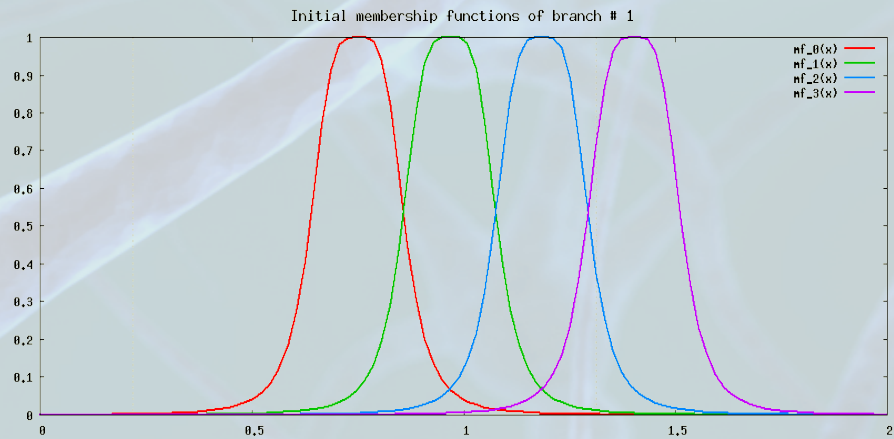
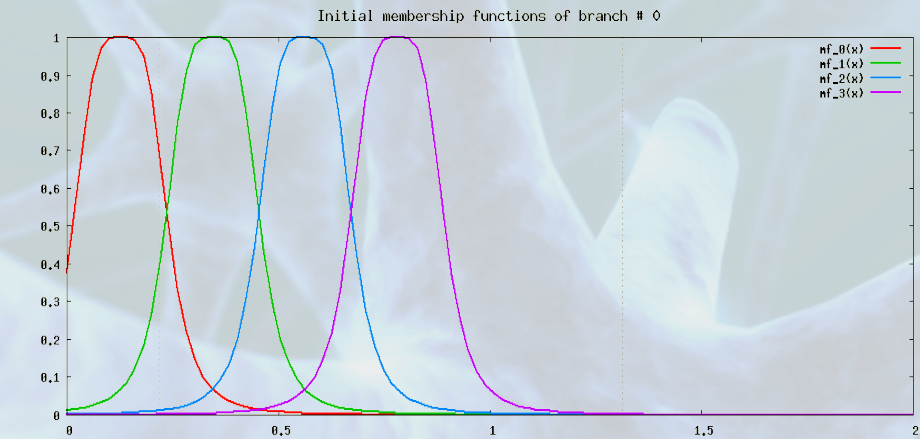
error ~  
[-0.4 , 0.2]



# Redes Neuronales: ANFIS

N.Bruno

T=2    N=4





# Redes Neuronales: ANFIS

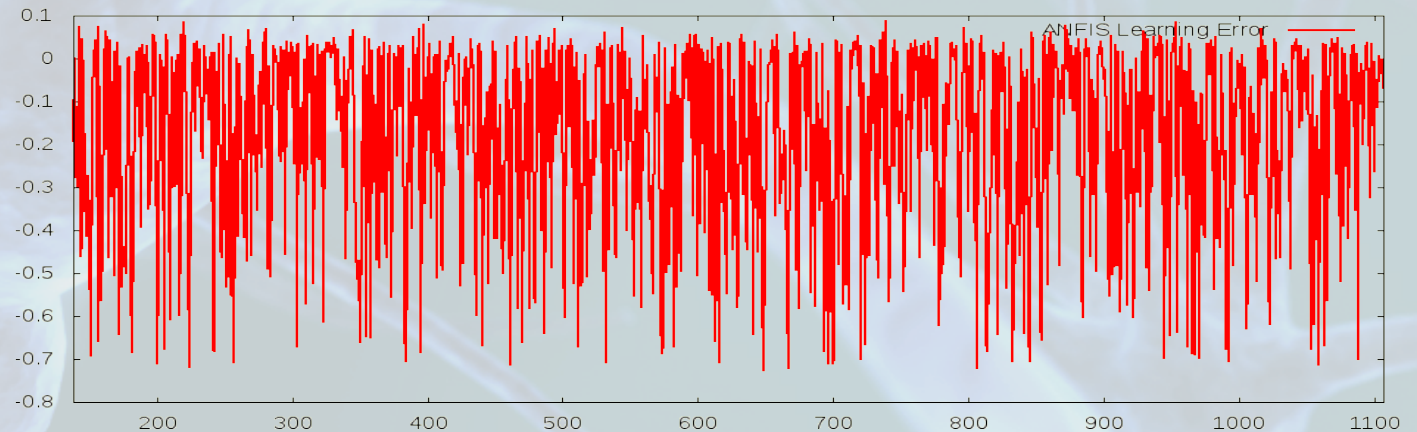
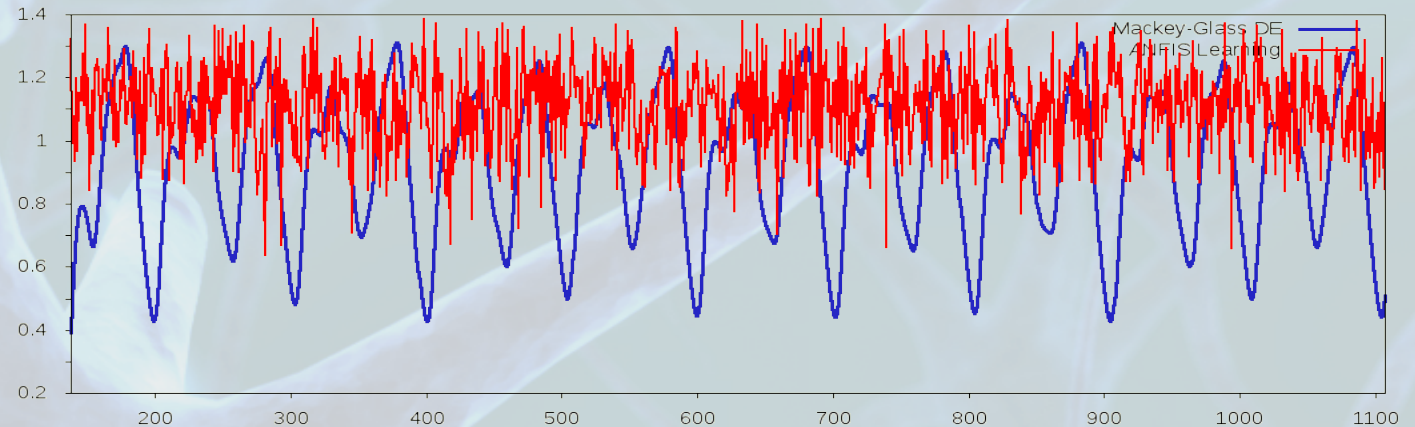
**N. Bruno**

$T = 2$

$N = 4$

random

error ~  
horrible

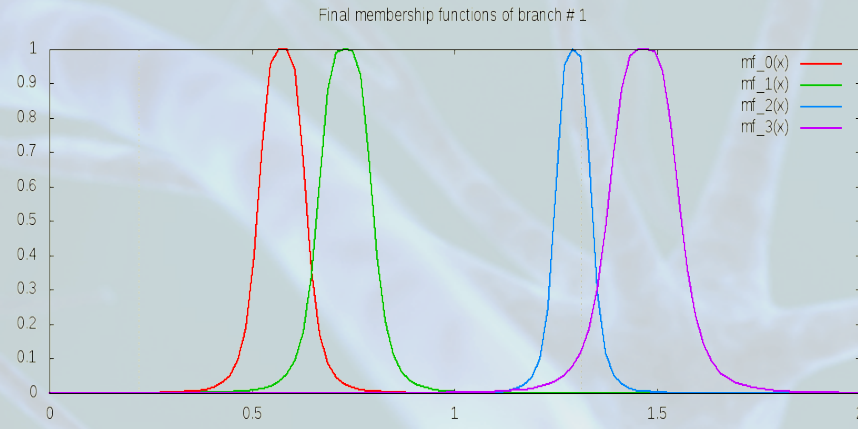
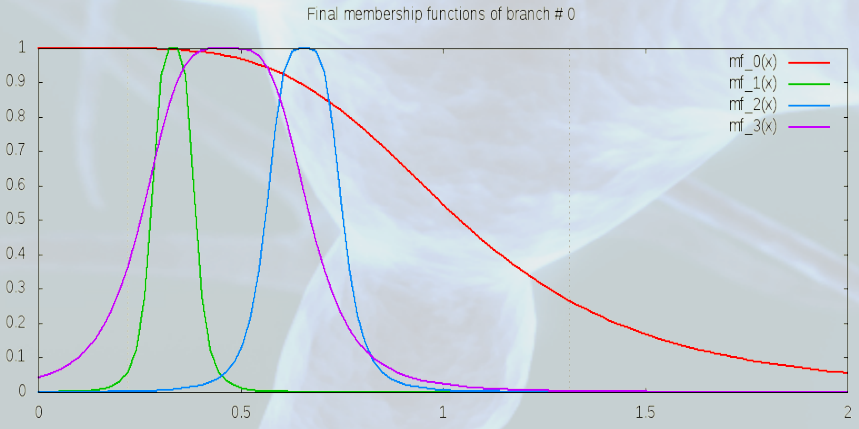
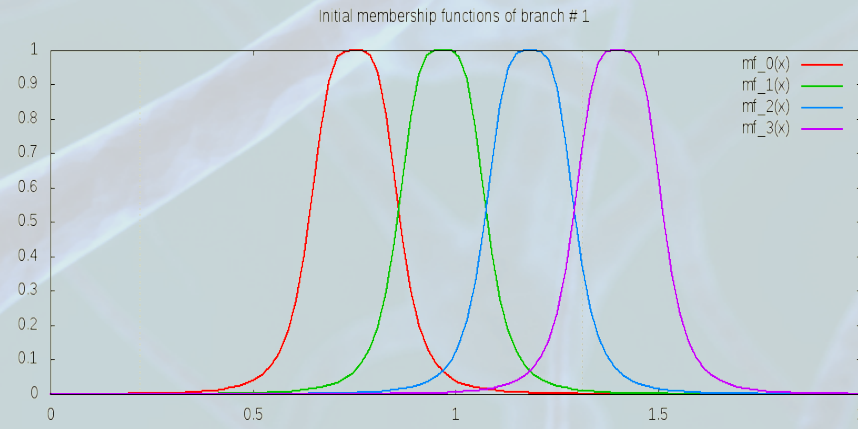
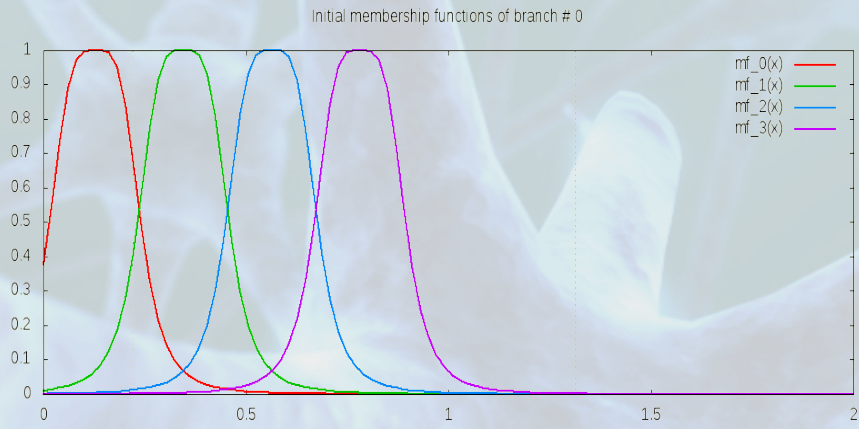


# Redes Neuronales: ANFIS

**N.Bruno**

**random**

**T=2   N=4**



# Redes Neuronales: ANFIS

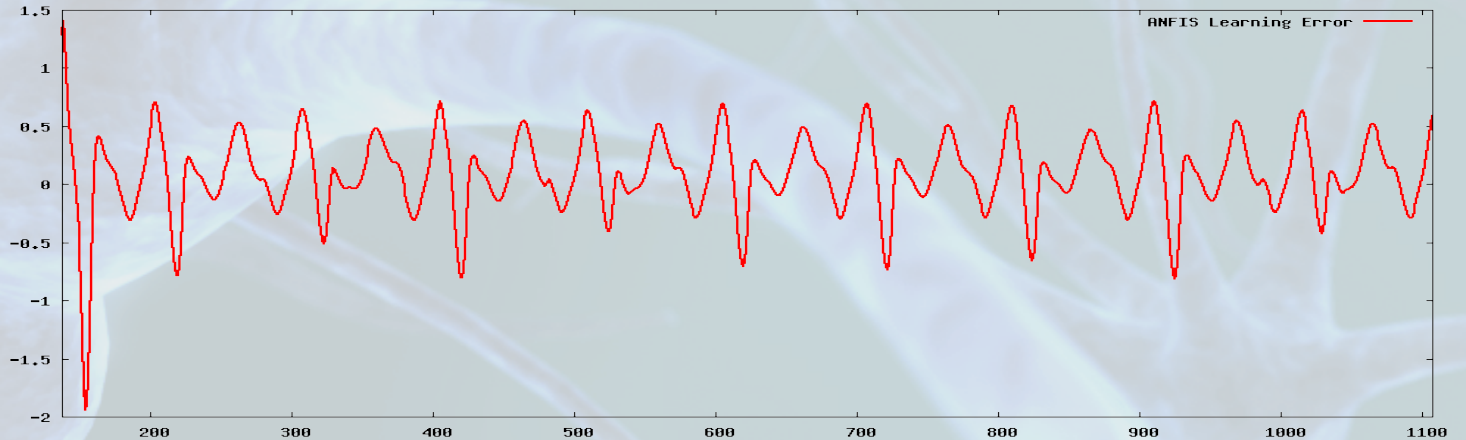
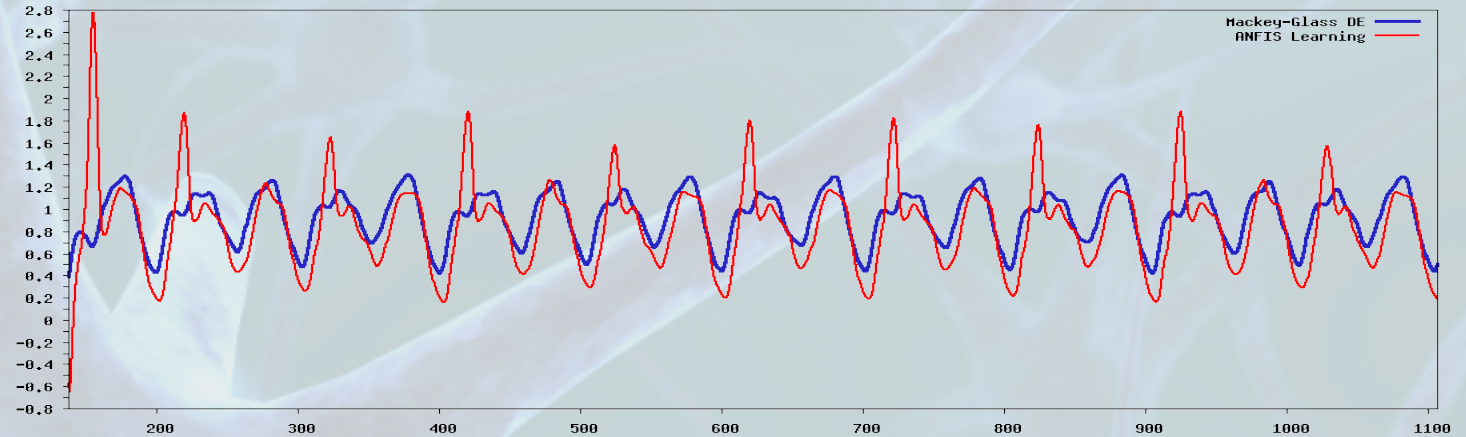
R.Jang

$T = 2$

$N = 4$

error ~

$[-0.8, 0.7]$

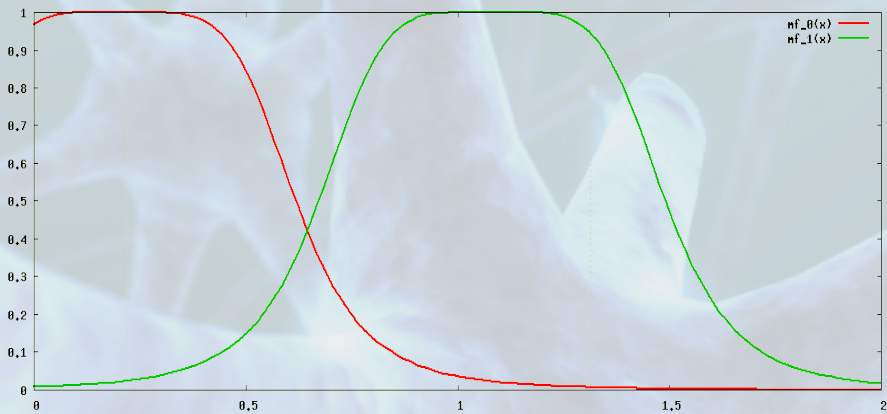


# Redes Neuronales: ANFIS

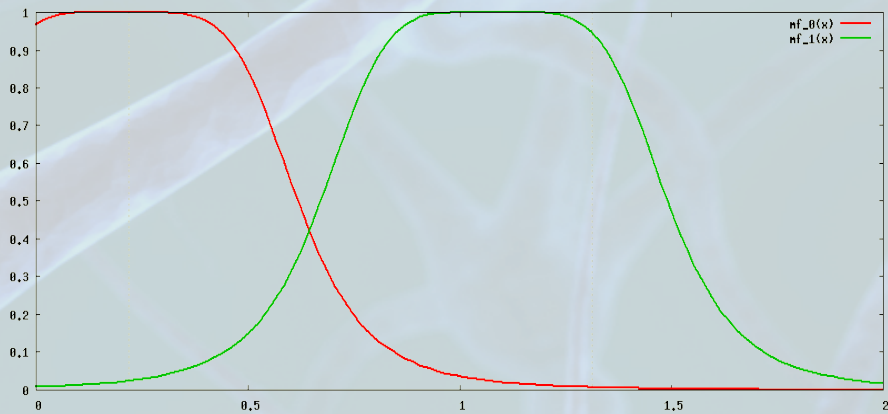
R.Jang

T=2 N=4

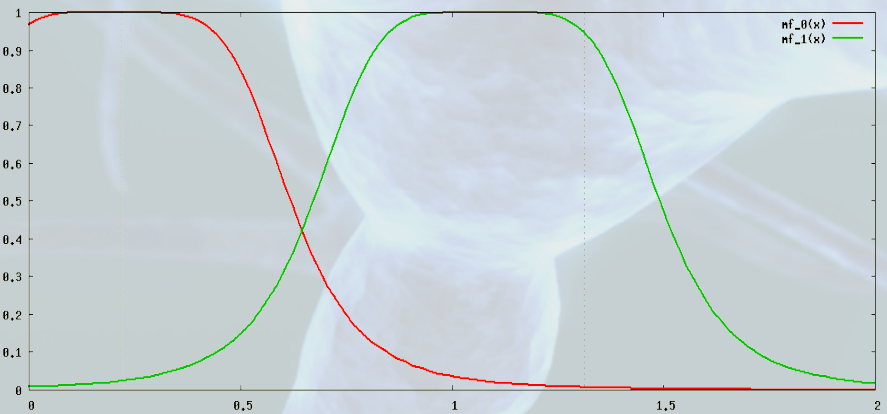
Initial membership functions for input # 0



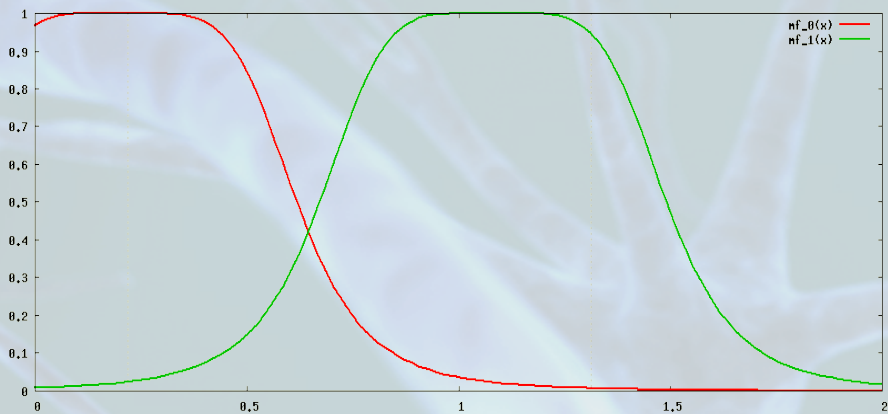
Initial membership functions for input # 1



Initial membership functions for input # 2



Initial membership functions for input # 3



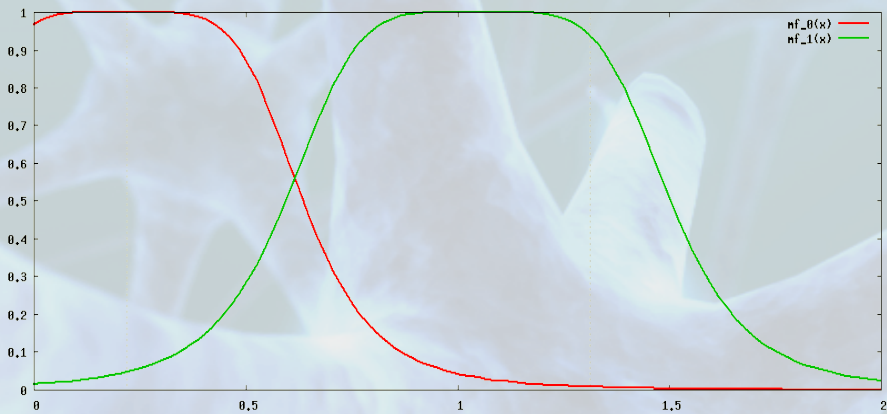


# Redes Neuronales: ANFIS

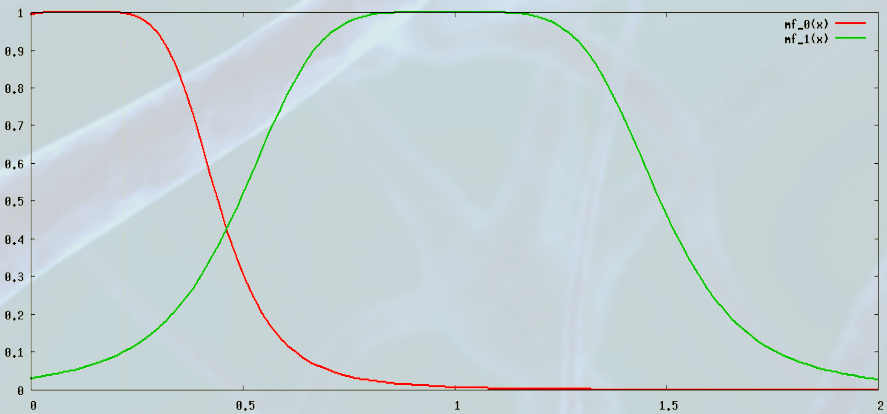
R.Jang

T=2 N=4

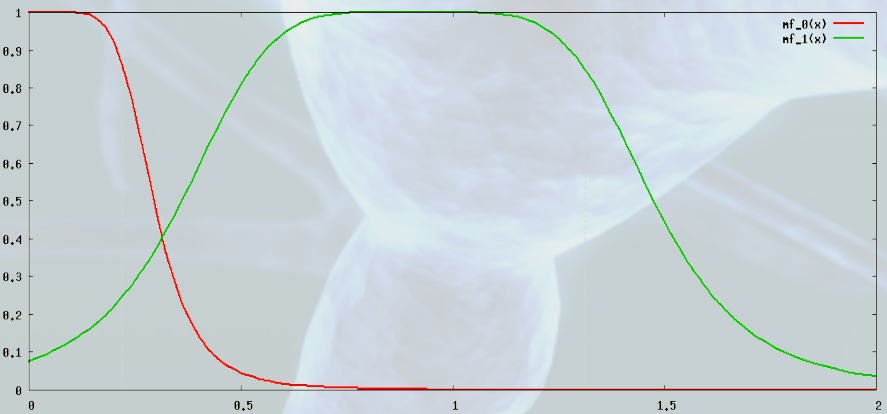
Final membership functions for input # 0



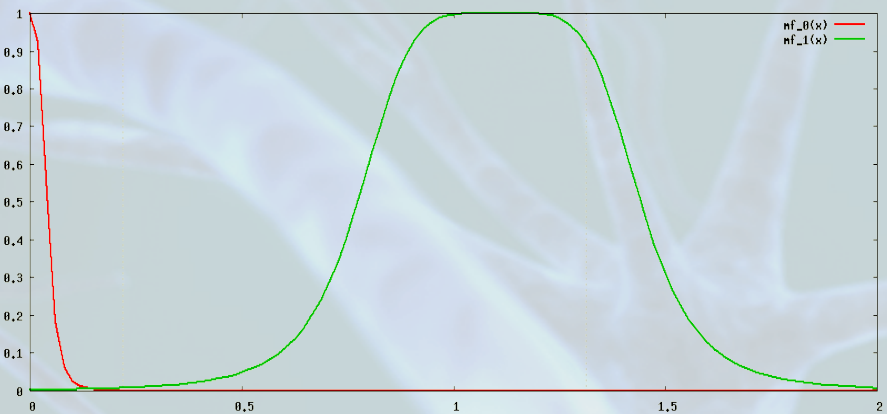
Final membership functions for input # 1



Final membership functions for input # 2



Final membership functions for input # 3



# Redes Neuronales: ANFIS

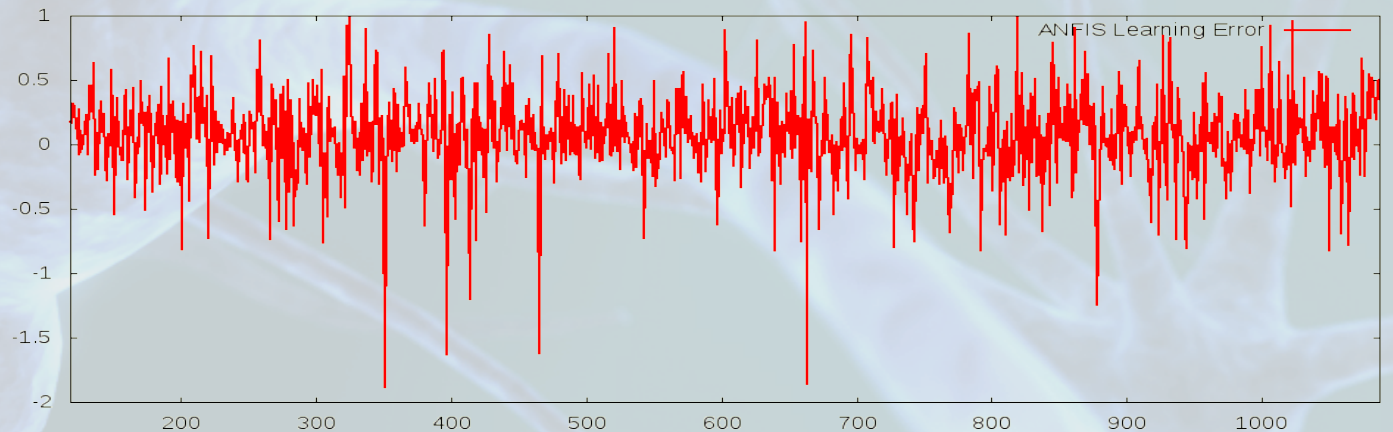
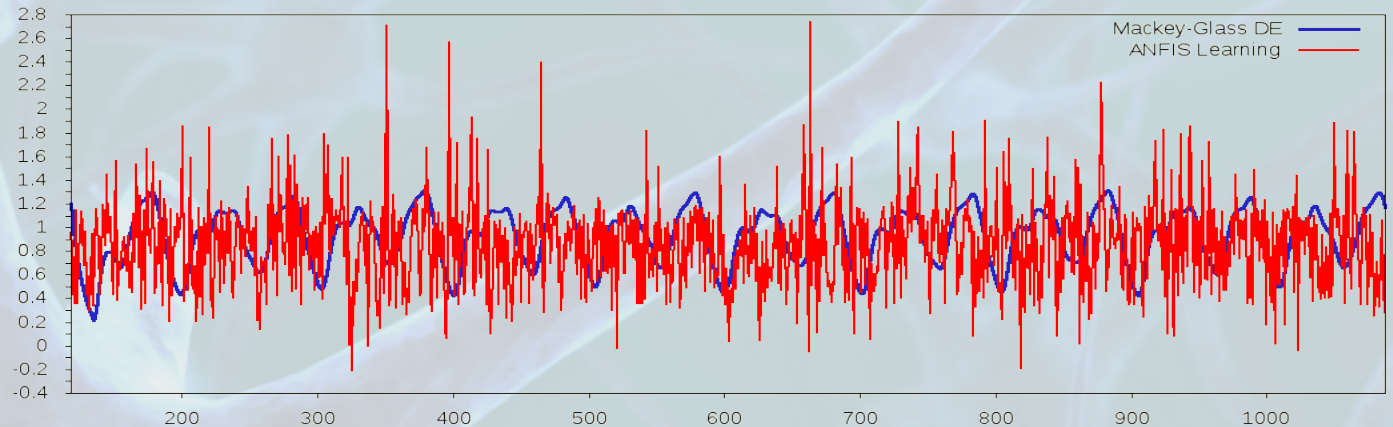
R.Jang

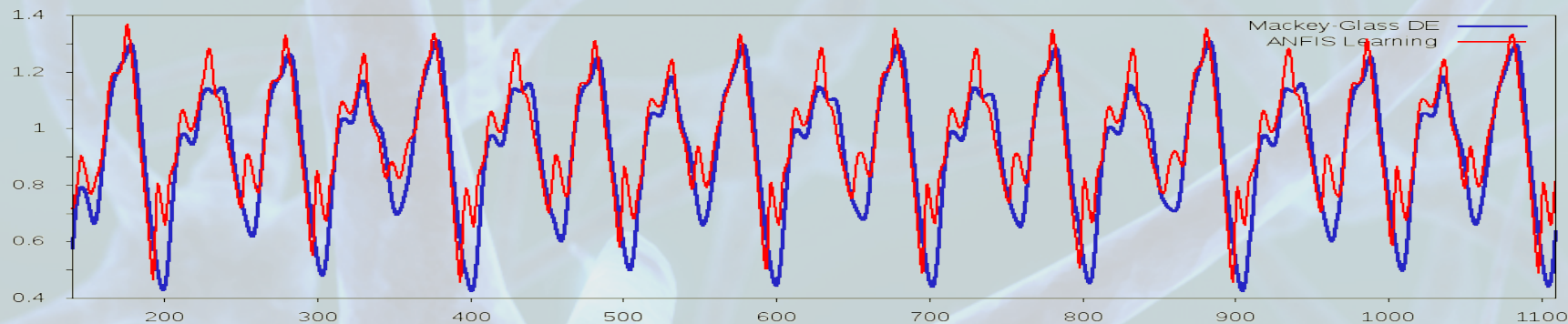
$T = 2$

$N = 4$

random

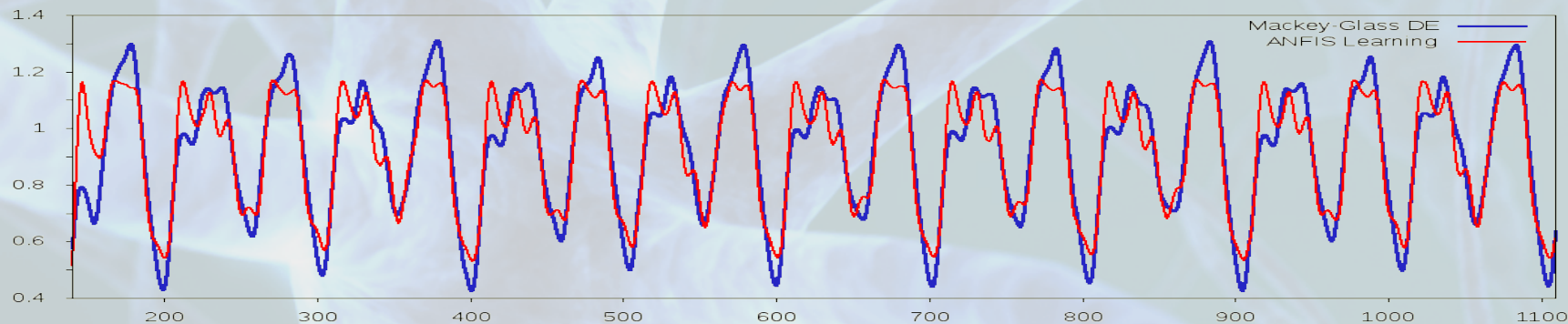
error ~  
horrible





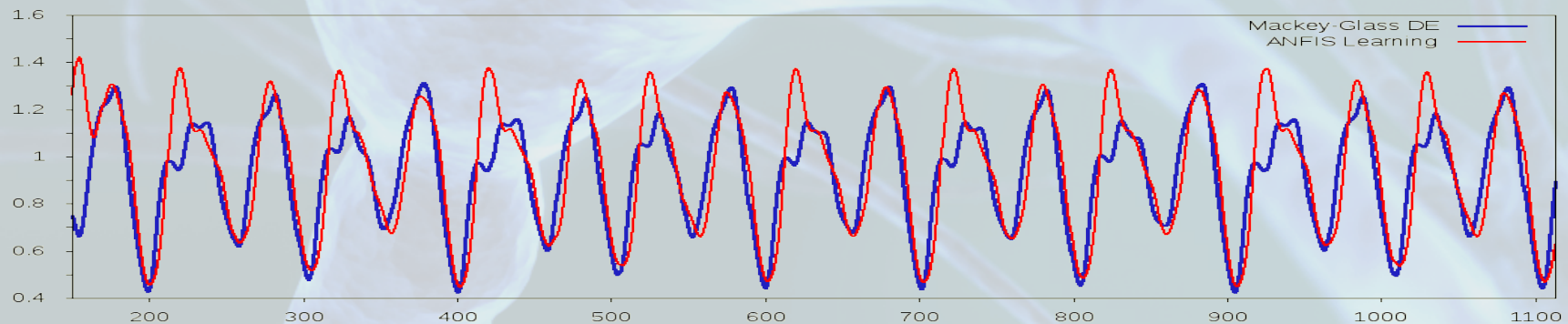
$T = 3$

$N = 4$



$T = 1$

$N = 4$

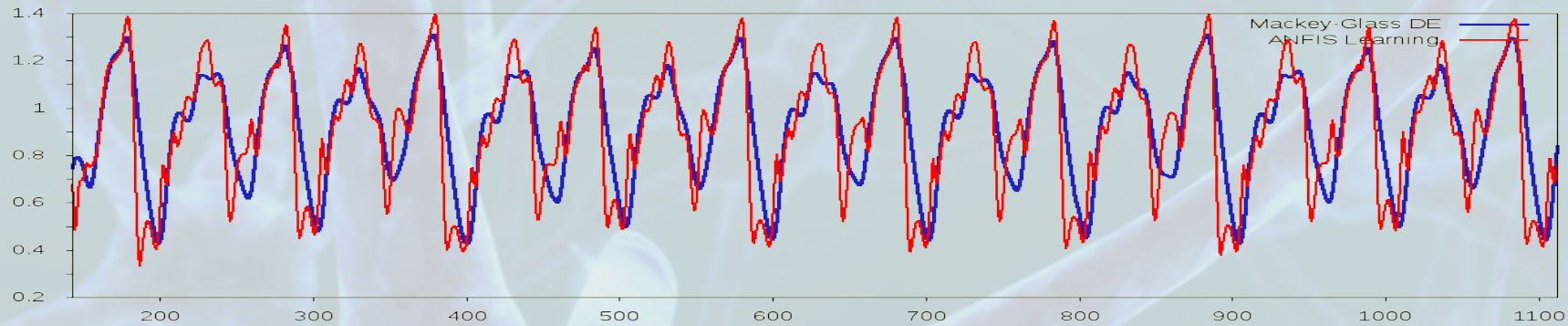


$T = 2$

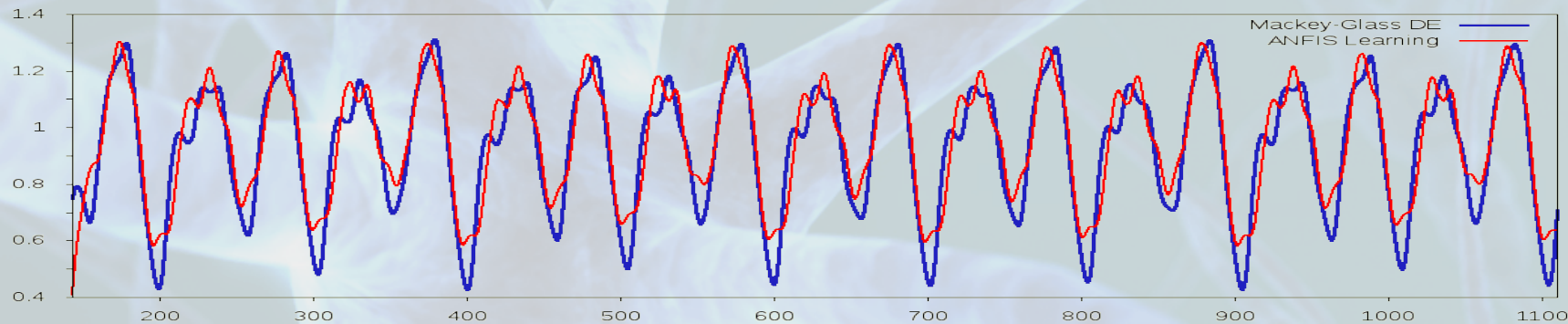
$N = 5$

# Redes Neuronales: ANFIS

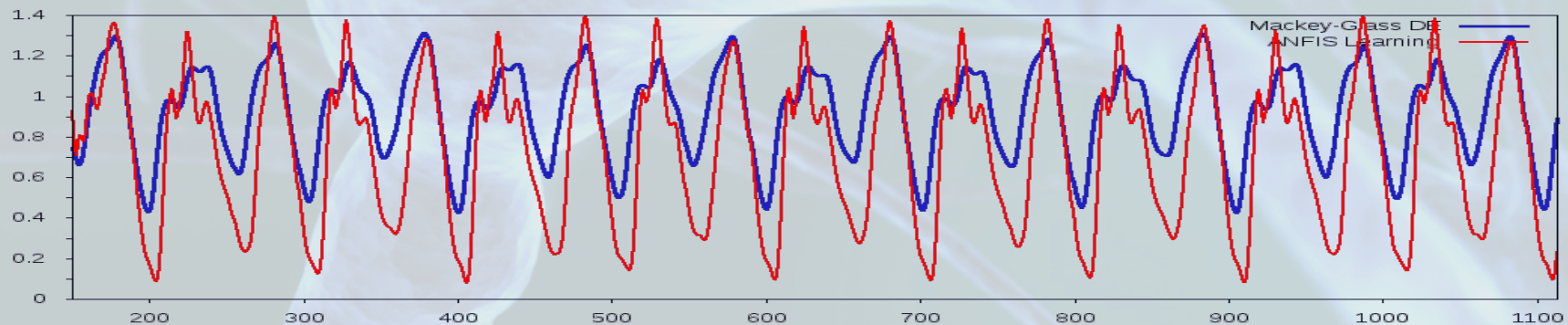
R.Jang



$T = 3$   
 $N = 4$



$T = 1$   
 $N = 4$



$T = 2$   
 $N = 5$



## Bibliografía:

- ▶ J.R. Jang ; *ANFIS: Adaptive-Network-Based Fuzzy Inference System* ; IEEE Trans. on Systems, Man & Cybernetics ; Vol. 23, No 3 ; pp. 666-686 ; 1993
- ▶ N. Bruno ; *Sistemas de inferencia difusos basados en redes neuroadaptativas* ; Universidad de Murcia, Facultad de Informática ; 1999
- ▶ J. Hertz et al. ; *Introduction to the theory of neural computation* ; Santa Fe institute ; Perseus Books Publishing ; pp. 90-156 ; 1991