DESIGN AND IMPLEMENTATION OF SENSOR DATA FUSION FOR AN AUTONOMOUS QUADROTOR

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Abstract—This paper describes the design and integration of an instrumentation and sensor fusion that is used to allow the autonomous flight of a quadrotor. A comercial frame is used, a mathematical model for the quadrotor is developed and its parameters determined from the characterization of the unit. A 9 degrees of freedom Inertial Measurement Unit (IMU) equipped with a barometer is calibrated and added to the platform. Sensor fusion is done by two modified Extended Kalman Filters (EKF): one combining data provided by IMU and the other also including the information provided by GPS. A reliable estimation of the state variables is obtained. Three states representing systematic bias in the accelerometer measurements are also added to the EKF, which improves the inertial estimation of the position. A stable autonomous platform is achieved.

I. INTRODUCTION

There is an important growth in the interest about unmanned aerial vehicles (UAV) in relation to its capabilities to perform a wide spectrum of tasks as monitoring, surveillance, aerial photography, exploration, delivery, rescue, remote sensing, etc. The continuous advances in low power MEMS sensor devices, low power embedded processors, energy storage through efficient electric batteries and electrical motors technologies have been driving forces in the process of implementation of new and more sophisticated devices of this kind, particularly miniature flying robots. Quadrotors UAV is one of the most popular architectures. They emerged also as a typical platform for research. There is much research work about path planning and vision towards navigation in unstructured scenarios (e.g.: [1]–[3]), fault tolerant navigation (e.g.: [4]), path tracking (e.g.: [5]), control techniques for UAV such as neural networks [6], gain-schedulling [4], feedback linearization (e.g.: [3], [7]), PI control [5], Adaptive Control [8], LQR (e.g.: [2], [9]), backstepping control (e.g.: [1], [3]), etc. If state estimation, path planning or control techniques are to be experimented in a physical setup, an important issue is to have the possibility to gain access to the different blocks of the navigational system. This work is part of the development of the instrumentation and control of an autonomous quadrotor in which is possible to modify and test different state estimation techniques, path planning algorithms and control laws. The solution was reached using a commercial mechanical platform, and design and build an ad-hoc instrumentation and control navigation system. This paper focuses on the filtering techniques applied
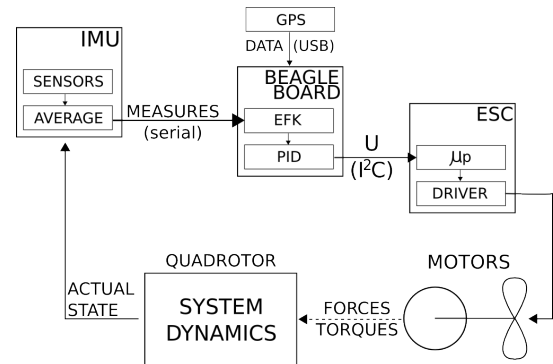

Fig. 1: **Commercial motorized-frame used.**

Fig. 2: **General diagram.**

for sensor data fusion which gives the state estimation needed by the control system, that allows the quadrotor to fly.

II. SYSTEM ARCHITECTURE

The platform is based on the commercial radio controlled quadrotor shown in Figure (1). The length between opposite propellers is $61.5cm$, the weight is $990g$ (including battery), and it has $1300g$ of payload. The frame, motors and the Electronic Speed Controllers (ESCs) used for the motors were preserved, whereas the IMU and intelligence were replaced by the flight controller that was developed. A BeagleBoard[1] running Linux[2] performs the computations required to convert raw data received from the IMU[3] over a UART and combine

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[1]BeagleBoard development board - http://beagleboard.org/
[2]Angstrom distribution: http://www.angstrom-distribution.org/
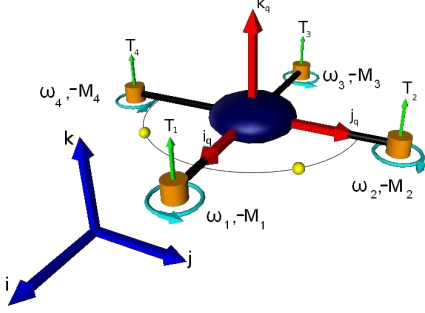[3]*Mongoose* IMU - http://store.ckdevices.com/

Fig. 3: **Model of the quadrotor -** The blue arrows represent the inertial reference frame S_I, and the red arrows represent the non-inertial reference frame S_q. The cyan "looped" arrows indicate the direction of rotation of each motor, which rotate at ω_i and generate a torque M_i opposite to their direction of rotation. The arrows labeled $T_{[1,2,3,4]}$ represent the thrust of the motors. The semicircle and the two yellow spheres indicate the x_q axis of the unit.

it using an EKF. The EKF overcomes the problems inherent to each sensor and filters out noise, providing a reliable estimation of the state vector. Once the current state is known, the LQR algorithm is used to derive the control actions required to bring the system to the desired set-point. A complete diagram of the implemented system is shown in Figure (2). The two main goals are to integrate additional sensors and intelligence to the available platform to obtain a state estimation, and design and integrate a control system that, using the state estimation, achieves the autonomous flight.

III. MODEL OF A QUADROTOR

A. Definitions

A diagram of the quadrotor is shown in Figure (3). Two of the motors rotate clockwise (2 and 4) and the other two (1 and 3) rotate counterclockwise. This configuration allows the quadrotor to rotate, tilt and gain/lose altitud by setting different speeds on each motor. Two frames of reference (Figure (3)) are constantly used through out this paper: an intertial frame $S_I - \{\hat{i}, \hat{j}, \hat{k}\}$ ($\{\vec{x}, \vec{y}, \vec{z}\}$), relative to the Earth, mapped to North, West and Up respectively, and a non-inertial frame $S_q - \{\hat{i}_q, \hat{j}_q, \hat{k}_q\}$ ($\{\vec{x}_q, \vec{y}_q, \vec{z}_q\}$) relative to the quadrotor. The mapping of one frame to the other can be achieved by applying the three rotations shown in Figure (4). The angles $\{\theta, \varphi, \psi\}$ are known as Euler angles.

B. Dynamics-kinematics of the system

From a detailed analysis of the dynamics and kinematics of the quadrotor, the equations (1) are obtained, and the state vector shown in (2) is built to describe the system at any given time. The variables with subscript q are referenced to

the quadrotor frame S_q, the rest are relative to S_I:

$$
\begin{aligned}
\dot{x} &= v_{q_x}\cos\varphi\cos\theta + v_{q_y}(\cos\theta\sin\varphi\sin\psi - \cos\varphi\sin\theta) \\
&\quad + v_{q_z}(\sin\psi\sin\theta + \cos\psi\cos\theta\sin\varphi) \\
\dot{y} &= v_{q_x}\cos\varphi\sin\theta + v_{q_y}(\cos\psi\cos\theta + \sin\theta\sin\varphi\sin\psi) \\
&\quad + v_{q_z}(\cos\psi\sin\theta\sin\varphi - \cos\theta\sin\psi) \\
\dot{z} &= -v_{q_x}\sin\varphi + v_{q_y}\cos\varphi\sin\psi + v_{q_z}\cos\varphi\cos\psi \\
\dot{\psi} &= \omega_{q_x} + \omega_{q_z}\tan\varphi\cos\psi + \omega_{q_y}\tan\varphi\sin\psi \\
\dot{\varphi} &= \omega_{q_y}\cos\psi - \omega_{q_z}\sin\psi \\
\dot{\theta} &= \omega_{q_z}\frac{\cos\psi}{\cos\varphi} + \omega_{q_y}\frac{\sin\psi}{\cos\varphi} \\
\dot{v_{q_x}} &= v_{q_y}\omega_{q_z} - v_{q_z}\omega_{q_y} + g\sin\varphi \\
\dot{v_{q_y}} &= v_{q_z}\omega_{q_x} - v_{q_x}\omega_{q_z} - g\cos\varphi\sin\psi \\
\dot{v_{q_z}} &= v_{q_x}\omega_{q_y} - v_{q_y}\omega_{q_x} - g\cos\varphi\cos\psi + \frac{1}{M}\sum_{i=1}^{4}T_i \\
\dot{\omega_{q_x}} &= \frac{1}{I_{xx}}\omega_{q_y}\omega_{q_z}(I_{yy} - I_{zz}) \\
&\quad + \frac{1}{I_{xx}}\omega_{q_y}I_{zz_m}(\omega_1 - \omega_2 + \omega_3 - \omega_4) \\
&\quad - \frac{1}{I_{xx}}dMg\cos\varphi\sin\psi + \frac{1}{I_{xx}}L(T_2 - T_4) \\
\dot{\omega_{q_y}} &= \frac{1}{I_{yy}}\omega_{q_x}\omega_{q_z}(-I_{xx} + I_{zz}) \\
&\quad + \frac{1}{I_{yy}}\omega_{q_x}I_{zz_m}(\omega_1 - \omega_2 + \omega_3 - \omega_4) \\
&\quad - \frac{1}{I_{yy}}dMg\sin\varphi + \frac{1}{I_{yy}}L(T_3 - T_1) \\
\dot{\omega_{q_z}} &= \frac{1}{I_{zz}}(-Q_1 + Q_2 - Q_3 + Q_4)
\end{aligned}
\tag{1}
$$

$$
\mathbf{x} = \{x, y, z, \theta, \varphi, \psi, v_{q_z}, v_{q_y}, v_{q_z}, \omega_{q_x}, \omega_{q_y}, \omega_{q_z}\} \tag{2}
$$

where:

- $\{x, y, z\}$ represent the position of the center of mass of the system in S_I.
- $\{\theta, \varphi, \psi\}$ are the Euler angles shown in Figure (4).
- $\{v_{q_x}, v_{q_y}, v_{q_z}\}$ are the linear velocities relative to S_q.
- $\{w_{q_x}, w_{q_y}, w_{q_z}\}$ are the angular velocities relative to S_q (right hand rule applied on $\{\hat{i}_q, \hat{j}_q, \hat{k}_q\}$).
- $T_1(\omega_1)$, $T_2(\omega_2)$, $T_3(\omega_3)$, $T_4(\omega_4)$ are the thrust of the motors.

The dynamical model considered, derived from equations 1, is

$$
\dot{\mathbf{x}} = \mathcal{F}(\mathbf{x}, \mathbf{u}) \tag{3}
$$

where $\mathbf{u} = \{\omega_1, \omega_2, \omega_3, \omega_4\}$ is the controllable input of the system.

The mathematical model developed is similar to the ones presented in [10], [11], but also takes into account that the center of gravity of the quadrotor is not at the same height as the propellers. Thus a momentum produced by the gravity force has to be added. While in [11] the linear velocities are expressed in an inertial frame, in this work are referenced to the quadrotor frame. This choice simplifies the theoretical development and the interpretation of the data provided by the IMU, which is mounted on the quadrotor and hence provides accelerations and angular velocities that are relative to S_q.
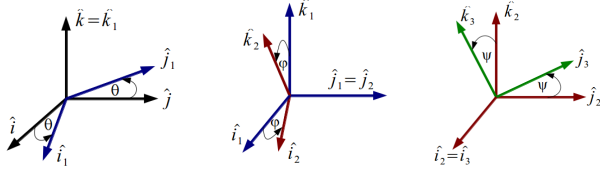
(a) Rotation 1: Axis $\hat{k}$ (b) Rotation 2: Axis $\hat{j}$ (c) Rotation 3: Axis $\hat{i}$

Fig. 4: **Mapping -** Rotations applied on S_I to obtain S_q.

IV. SENSORS

In order to determine what actions should be taken, the state of the system must be known. The system uses a 9 degrees of freedom IMU and a GPS. This equipment enables direct measurement of most of the state variables. There is no direct measurement of the linear speed of the system $\{v_{q_x}, v_{q_y}, v_{q_z}\}$, so the model developed in (III) is used to estimate them.

A. IMU

The IMU is equiped with the following sensors:

- **Barometer:** Measures the absolute pressure of the environment. Variations of pressure are used to estimate variations in the altitude of the system.
- **Thermometer:** The barometer includes a thermometer. The temperature data is used to apply a temperature compensation to the calibrations performed on the gyroscope and the accelerometer. The reader can find the details in this procedure in [12].
- **Gyroscope:** A 3-axis gyroscope is used to measure angular velocity of S_q. A calibration based on [13] was designed and applied to this device. Furthermore, a temperature compensation was designed and implemented.
- **Accelerometer:** A 3-axis accelerometer is used to measure gravity. Under the hypothesis that no other accelerations are present, this allows the determination of two of the three Euler angles: $\{\psi, \phi\}$. This hypothesis is acceptable, since the accelerations involved are not significant compared to gravity. A calibration, based on [13], was designed and applied to this device, as well as a temperature-compensation.
- **Magnetometer:** In an area free of magnetic interference this 3-axis sensor will measure $\mathbf{B}$, the Earth's magnetic field, allowing to determine what direction is North. If the system is horizontal (or the inclination is estimated using other sensors) this sensor can be used to determine the last of the three Euler angles: θ. A calibration based on [14], [15] was performed on this sensor.

B. GPS

In theory, given some initial position $\{x_0, y_0\}$ the accelerometer could be used to determine variations $\{x_0 + \Delta x, y_0 + \Delta y\}$. In practice this estimation drifts rapidly (ten meters in about ten seconds), so a GPS is used to determine the absolute position $\{x, y\}$ of the system, correcting the drift. The accuracy, with good sky visibility, is of 2-3 meters. The GPS's performance improves when the system is moving.

C. Sensor Specifications

Table (I) shows an outline of the specifications of the sensors used.

	Rate	Resolution
Accelerometer XY	10ms (x2)	4mg
Accelerometer Z	10ms (x2)	4mg
Gyro XY	10ms (x2)	0.07 $^o/s$
Gyro Z	10ms (x2)	0.07 $^o/s$
Barometer	10ms (x1)	1Pa
Magnetometer XY	10ms (x2)	5 mGa
Magnetometer Z	10ms (x2)	5 mGa
GPS	1s	-

TABLE I: **Sensor specifications:** A rate of "*10ms (x2)*" means that every 10ms the result of averaging 2 samples is received from the IMU.

V. KALMAN FILTER

In order to perform adequate control actions, a reliable estimation of the state variables must be available in real time. The Kalman Filter uses the mathematical model for the system to predict what should happen next given the current state. It corrects the prediction with the information read from the sensors, taking into consideration how much confidence is placed on the prediction and how much on the measurements. This weighted prediction-correction technique allows a smooth state estimation without the typical delay introduced by filtering, even small delays can severely affect the performance of the system.

Every sensor has its issues, the accelerometer drifts over time; the gyroscope is very sensible to the vibrations generated by the motors; the magnetometer measure is distorted by ferromagnetic materials; the GPS has a very poor accuracy and a slow update rate. Each sensor by itself is very limited, but they can be combined to compensate for their limitations. The filter takes care of this by integrating all sensors in order to obtain a more accurate state estimation.

The theory behind a standard Kalman Filter does not hold for a nonlinear system. The model for the quadrotor given by (1) is highly nonlinear, so an Extended Kalman Filter (EKF) is implemented. Several authors (e.g. [16], [17]) used EKF to overcome this difficulty. In this work a modified EKF was developed, similar to [16], [17], but with 3 states added representing the accelerometer bias, which improved substantially the linear velocities and position estimation. While the Kalman Filter ensures a statistical optimal performance, the EKF is not optimal, and it is not possible to determine the error a priori, due to high dependency of the performance with the linearization [18]. Although, EKF is the most used and popular filtering technique in navigation problems.

A. Mathematical model

Let us define an extended state vector $\mathbf{x}^e$, similar to the described in equation (2), but with 3 added states $\{a_x^b, a_y^b, a_z^b\}$ representing an estimation of the systematic error introduced

by the accelerometer. Let $\mathbf{x}_k^e$ be the extended state vector estimation at time k

$$\mathbf{x}_k^e = \left\{ x, y, z, \theta, \varphi, \psi, v_{q_z}, v_{q_y}, v_{q_z}, \omega_{q_x}, \omega_{q_y}, \omega_{q_z}, a_x^b, a_y^b, a_z^b \right\}$$

$\boldsymbol{\eta}_k^w$ and $\boldsymbol{\eta}_k^v$ are the process and observation noises, which are both assumed to be zero mean multivariate Gaussian noises with covariance $\mathbf{Q}_k$ and $\mathbf{R}_k$ respectively.

The dynamic system follows the model:

$$\mathbf{x}_k^e = f(\mathbf{x}_{k-1}^e, \mathbf{u}_{k-1}) + \boldsymbol{\eta}_{k-1}^w \quad (4)$$
$$\mathbf{z}_k = h(\mathbf{x}_k) + \boldsymbol{\eta}_k^v \quad (5)$$

where $\mathbf{z}_k$ is the observation at time k. The function f, based on the dynamics of the system is deduced form equation (3) and is used to compute the predicted state from the previous one. The function h is used to compute the predicted measurement from the predicted state. In other words, f keeps the information about state evolution, and h represents the transformation between the state vector and the ideal (noiseless) observation. The state transition and observation models do not need to be linear functions, but must be differentiable. f and h cannot be directly applied to the covariance. Instead a partial differential matrix (the *Jacobian*) is computed, which is evaluated in the current state at each time step. Due to dynamical linearization, the EKF cannot ensure statistic optimality, because the precision highly depends on the linearization precision [18].

B. Implementation

The implementation of the modified EKF uses the inertial measurements obtained from the IMU and integrates the position information provided by the GPS. Due to the very slow sampling rate of GPS (approximately 1Hz), and the need of taking a new control action much faster, two different EKFs are implemented; the first one using only the inertial measurements (EKF_{IMU}) while there is no GPS information, and the other one to be used when a new GPS sample is available ($EKF_{IMU+GPS}$). The prediction and update equations are presented below.

1) Prediction and update equations for EKF_{IMU}:
- Prediction:
  - $\hat{\mathbf{x}}_{k|k-1}^e = f(\hat{\mathbf{x}}_{k-1|k-1}^e, \mathbf{u}_{k-1})$
  - $\mathbf{P}_{k|k-1} = \mathbf{F}_{k-1}\mathbf{P}_{k-1|k-1}\mathbf{F}_{k-1}^T + \mathbf{Q}_{k-1}$
- Update
  - $\tilde{\mathbf{y}}_k = \mathbf{z}_k - h(\hat{\mathbf{x}}_{k|k-1}^e)$
  - $\mathbf{S}_k = \mathbf{H}_k\mathbf{P}_{k|k-1}\mathbf{H}_k^\top + \mathbf{R}_k$
  - $\mathbf{K}_k = \mathbf{P}_{k|k-1}\mathbf{H}_k^\top\mathbf{S}_k^{-1}$
  - $\hat{\mathbf{x}}_{k|k}^e = \hat{\mathbf{x}}_{k|k-1}^e + \mathbf{K}_k\tilde{\mathbf{y}}_k$
  - $\mathbf{P}_{k|k} = (I - \mathbf{K}_k\mathbf{H}_k)\mathbf{P}_{k|k-1}$

where $\mathbf{z}_k$ is the observation at time k.
The state and observation transition matrices are

$$\mathbf{F}_{k-1} = \left. \frac{\partial f}{\partial \mathbf{x}^e} \right|_{\hat{\mathbf{x}}_{k-1|k-1}^e, \mathbf{u}_{k-1}}, \qquad \mathbf{H}_k = \left. \frac{\partial h}{\partial \mathbf{x}^e} \right|_{\hat{\mathbf{x}}_{k|k-1}^e}$$

2) Prediction and update equations for $EKF_{IMU+GPS}$:
- Prediction:
  - $\hat{\mathbf{x}}_{k|k-1}^e = f_G(\hat{\mathbf{x}}_{k-1|k-1}^e, \mathbf{u}_{k-1})$
  - $\mathbf{P}_{k|k-1} = \mathbf{F}_{\mathbf{G}k-1}\mathbf{P}_{k-1|k-1}\mathbf{F}_{\mathbf{G}k-1}^T + \mathbf{Q}_{k-1}$
- Update
  - $\tilde{\mathbf{y}}_{\mathbf{G}k} = \mathbf{z}_{\mathbf{G}k} - h_G(\hat{\mathbf{x}}_{k|k-1}^e)$
  - $\mathbf{S}_{\mathbf{G}k} = \mathbf{H}_{\mathbf{G}k}\mathbf{P}_{\mathbf{G}k|k-1}\mathbf{H}_{\mathbf{G}k}^\top + \mathbf{R}_{\mathbf{G}k}$
  - $\mathbf{K}_{\mathbf{G}k} = \mathbf{P}_{\mathbf{G}k|k-1}\mathbf{H}_{\mathbf{G}k}^\top\mathbf{S}_{\mathbf{G}k}^{-1}$
  - $\hat{\mathbf{x}}_{k|k}^e = \hat{\mathbf{x}}_{k|k-1}^e + \mathbf{K}_{\mathbf{G}k}\tilde{\mathbf{y}}_k$
  - $\mathbf{P}_{k|k} = (I - \mathbf{K}_{\mathbf{G}k}\mathbf{H}_{\mathbf{G}k})\mathbf{P}_{k|k-1}$

The two sets of prediction and update equations, for EKF_{IMU} and $EKF_{IMU+GPS}$ are very similar, and the subindex $_G$ is used to explicitly show that the variables are different in each filter. This difference is caused because $\mathbf{z}_k$ and $\mathbf{z}_{\mathbf{G}k}$ are different since $\mathbf{z}_{\mathbf{G}k}$ includes GPS data. Note that $\hat{\mathbf{x}}_{k|k-1}^e$ is always the same.

This two filters are in fact very similar, but while in the EKF_{IMU} the position is estimated by the prediction based on the dynamics-kinematics of the system, in the $EKF_{IMU+GPS}$ the samples from GPS are used as feedback for the position estimation.

The position estimation without using GPS is very poor, because of the accumulated error produced by the double integration of the accelerometer measurement. The EKF_{IMU} is meant to keep a reasonable estimation of position while the system is waiting for a new GPS sample. $EKF_{IMU+GPS}$ gives a high weight to the GPS measurement so it can be used as a correction measurement, avoiding the drift that the integration may cause.

Figure (5) shows a diagram of how data from the sensors is combined within the filter (EKF), assisted by the model of the system.

Euler angles are primary estimated from the combination of Magnetometer and Accelerometer measurements as follows [16]:

$$\phi = -\arcsin\left(\frac{a_x}{||\mathbf{a}||}\right), \quad \psi = -\arctan\left(\frac{a_y}{a_z}\right)$$

$$\mathbf{M} = \begin{pmatrix} \cos(\phi) & \sin(\phi)\sin(\psi) & \cos(\psi)\sin(\phi) \\ 0 & \cos(\psi) & -\sin(\psi) \\ -\sin(\phi) & \cos(\phi)\sin(\psi) & \cos(\phi)\cos(\psi) \end{pmatrix}$$

$$\theta = -\arctan\left(\frac{m[1]}{m[0]}\right), \quad \text{where } \mathbf{m} = \mathbf{M}\,\mathbf{B}$$

From that estimation of Euler angles and the Accelerometer measurements, the quadrotor velocities $\{v_{qx},\ v_{qy}\ v_{qz}\}$ can be deduced by subtracting gravity and an integration, which are introduced to the filter. Angular velocities referenced to the quadrotor and height can be easily deduced from Gyroscope and Barometer measurements respectively, which are also introduced to the filter.
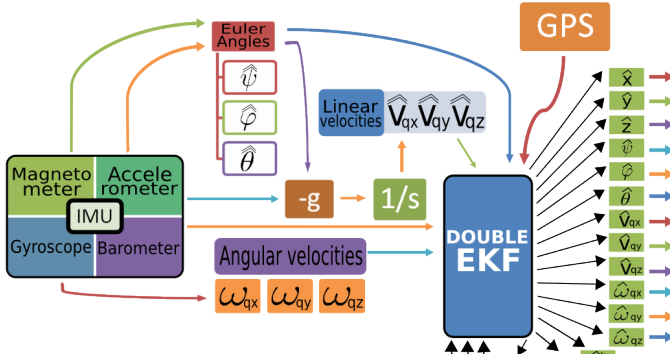
(a) **General diagram**
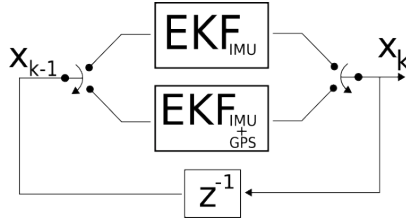
(b) **Double EKF -** Detail.

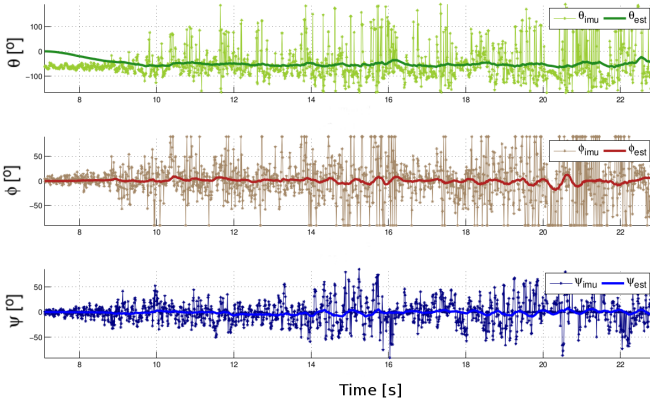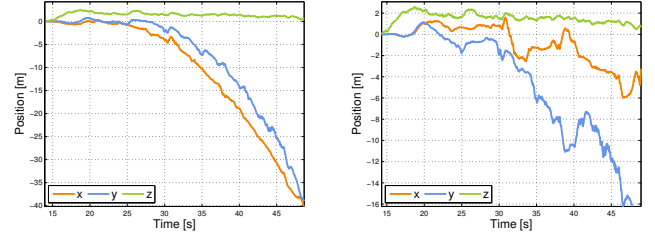Fig. 5: **EKF -** Outline of how sensor data is combined to estimate the state variables.

Fig. 6: **Kalman -** The three Euler angles estimation with all the motors turned on and the quadrotor in equilibrium.

(a) Without bias estimation (b) With bias estimation

Fig. 7: **Comparison -** Position estimation.

Fig. 8: **Position estimation -** Using GPS.

VI. RESULTS

A. Sensor fusion

The implementation of the double EKF gave very good results, and proved to play a critical part in the system. As an example, the data provided by the accelerometer is "unusable" without filtering, and experiments with a simple low pass filter (LPF) showed that a 60ms delay introduced by the LPF severely deteriorates the performance of the system. When the EKF was assigned the task of reducing noise, the performance was significantly improved.

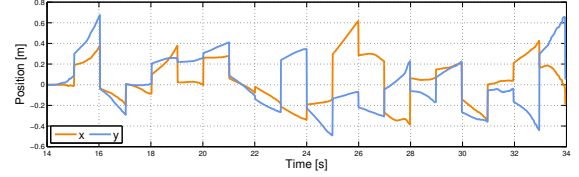In each graphic of Figure (6) is shown the primary estimation obtained from sensors and the kalman estimation of that

state variable for the three Euler angles. As can be seen, the noise is greatly reduced and no delay is introduced.

Although the accelerometer is calibrated considering axis non-orthogonality and temperature dependency, there are some other effects that may affect the measurement, such as humidity, nonlinearities or some not considered interference. For estimating the position, the acceleration is integrated twice, so every error is propagated and may become considerable. In the calibration procedure [12], there can be some error while ensuring horizontality that causes a systematic error in the measurements. The three added states $\{a_x^b, a_y^b, a_z^b\}$ keeps an estimation of the systematic error induced by the accelerometer and improves significantly the estimation of the linear velocities and position. In Figure (7) is shown the position estimation in a real flight using only EKF_{IMU} with the bias estimation (Figure (7b)), and without using it (Figure (7a)). Although not having a ground truth for the position, it is clear that the position drift is considerably reduced. Taking into account that the flight was performed in a 10m square room, the real movement is bounded by the room size.

As said, two different types of data will be available, depending on the availability of GPS information. When GPS data is available, $EKF_{IMU+GPS}$ shows up and gives feedback to position estimation. Figure (8) shows the results of estimating the position using the combination of the two EKFs described. The same real flight data is used for this estimation, but simulated GPS data is added. As can be seen, GPS data is available at 1Hz, and the position is improved.

B. Closed loop stability: Attitude control

The described state estimation was used by the control system, as shown in figure (2). The control algorithm uses the state estimation as input and produces the instantaneous speed of each motor, thus establish the thrust and momentum.

The quadrotor was able to maintain horizontality by controlling $\{\psi, \phi, \omega_{q_x}, \omega_{q_y}\}$. Figure (9) shows the response of the quadrotor to a perturbation in the Roll (ψ) angle. While in Figure (9a) is shown the mechanical perturbation imposed, the reaction (controller commands) can be observed in Figure (9b). From $t_0 = 80.9s$ to $t_1 = 81.3s$ the perturbation is present. After this, the controller is working freely. The system step response for a step of more than 20° shows a overshoot of 3° or 4° and a rise time of about $0.4\ s$, which means an excellent performance, as can be seen in Figure (9a).

(a) Roll angle deviation

(b) Difference between ω and ω_{hover} for each motor
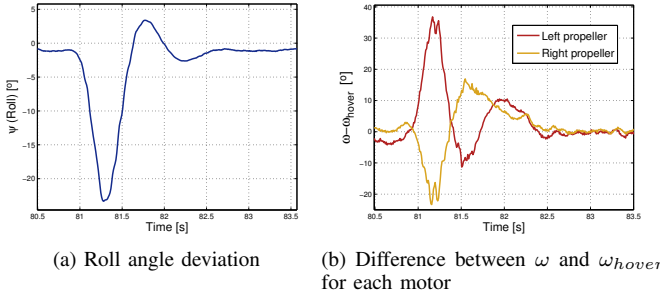
Fig. 9: **Stablization experiment -** The Roll angle is deviated from equilibrium and the quadrotor manage to stabilize itself.

C. Closed loop stability: Limited Flying

At this point the three Euler angles are controlled, so a basic level of stability is expected, and the quadrotor is allowed to fly. After this test, the control system was able to take-off and to hold altitud and vertical speed: $\{z, v_{q_z}\}$.

Figure (10) shows altitude during takeoff from altitude 0m until a target altitude of 1m is achieved. As can be seen, the system presents an overshoot of about a meter, which is considered as acceptable for many applications.
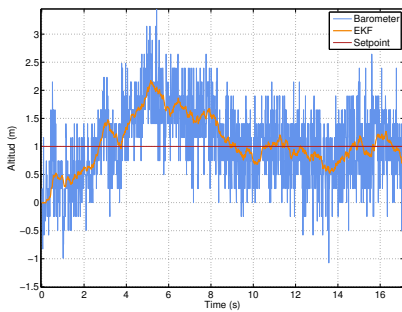

Fig. 10: **Altitude:** Performance during takeoff (from 0m to 1m).

VII. CONCLUSION

The main goal was successfuly achieved. The design and implementation of the sensor fusion for a quadrotor was accomplished by the integration of all the measurements in a double modified Extended Kalman Filter which is used for denoising purposes without introducing delay. A simplified dynamic model was derived as a first step for the Kalman Filter.

Through the implementation of the double Kalman filter, two important problems were solved: the difference between the IMU and GPS sampling rates and the effect of the bias drift in the accelerometer measurements.

The developed sensor fusion technique was implemented as part of a closed loop control system. It was successfully tested for attitude and height.

This system is an experimental platform for future research.

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