

COLLECTION

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1 Bayes' Theorem

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Axiom 1 (Conditional probability):

$$P(A \cap B) = P(A)P(B|A) = P(B \cap A) = P(B)P(A|B) \quad (1)$$

Axiom 2:

$$\begin{aligned} P(A) &= P(A \cap B) + P(A \cap \neg B) \\ &= P(B)P(A|B) + P(\neg B)P(A|\neg B) \end{aligned} \quad (2)$$

Bayes' Theorem:

$$P(A|B) \stackrel{(1)}{=} \frac{P(A)P(B|A)}{P(B)} \quad (3)$$

$$\stackrel{(2)}{=} \frac{P(A)P(B|A)}{P(A)P(B|A) + P(\neg A)P(B|\neg A)} \quad (4)$$
