## Out-of-Distribution Aware Classification for Tabular Data Supplementary Results

In the main paper, we presented results averaged across all datasets. In this document, we provide detailed results for each individual dataset, including the standard errors. The reported results are as follows:

- OOD-Aware Classification, Test Settings I: Detailed results for test settings I are presented for each dataset in the following tables: Adult in Table 1, Compas in Table 2, Cover in Table 3, Dilbert in Table 4, GMSC in Table 5, Heloc in Table 6, and Jannis in Table 7.
- OOD-Aware Classification, Test Settings II: Detailed results for test settings II are presented for each dataset in the following tables: Adult in Table 8, Compas in Table 9, Cover in Table 10, Dilbert in Table 11, GMSC in Table 12, Heloc in Table 13, and Jannis in Table 14.
- **Counterfactual Experiment**: Detailed results for the counterfactual experiment, including standard errors, are presented in Table 15.

Table 1. Detailed results for the Adult dataset in Test settings I.

Method	OOD	class: 0	OOD	class: 1
	In	OOD	In	OOD
Pipeline	$99.2 \pm 0.0$	$99.2 \pm 0.0$	$99.0 \pm 0.0$	$99.0 \pm 0.0$
OCT	$96.5 \pm 0.4$	$96.4 \pm 0.5$	$95.7 \pm 1.0$	$95.4 \pm 1.2$
MCDD	$90.8 \pm 0.0$	$89.4 \pm 0.0$	$72.9 \pm 0.0$	$46.1 \pm 0.0$
O-GBDT	$66.7\pm0.0$	$0.0\pm0.0$	$66.7 \pm 0.0$	$0.0\pm0.0$
DK	$66.9 \pm 0.0$	$2.5\pm0.2$	$69.3 \pm 0.1$	$20.8\pm0.3$
Multi	$86.1\pm0.0$	$89.1 \pm 0.0$	$84.7\pm0.0$	$88.3\pm0.0$
Incremental	$66.8 \pm 0.1$	$1.4\pm0.6$	$68.8 \pm 0.2$	$17.3 \pm 1.6$
Energy+	$91.0 \pm 0.7$	$89.4 \pm 1.0$	$93.2 \pm 0.4$	$92.4 \pm 0.6$
Self	$95.5 \pm 0.5$	$95.7 \pm 0.5$	$96.6 \pm 0.2$	$96.7 \pm 0.3$
Exposure	$66.7 \pm 0.0$	$0.0\pm0.0$	$66.7 \pm 0.0$	$0.0\pm0.0$
POEM	$70.9 \pm 0.0$	$33.6 \pm 0.0$	$91.0 \pm 0.0$	$89.3 \pm 0.0$
WOODS	$69.6 \pm 2.3$	$21.5 \pm 13.2$	$73.4 \pm 3.1$	$38.0 \pm 15.5$
Logitnorm	$68.3 \pm 1.1$	$17.1 \pm 6.9$	$66.3 \pm 0.2$	$3.9 \pm 2.0$
VOS	$68.9 \pm 0.0$	$22.5\pm0.0$	$66.3 \pm 0.0$	$6.1\pm0.0$
ReAct	$66.1 \pm 0.2$	$3.8 \pm 1.8$	$66.4 \pm 0.3$	$4.8 \pm 2.5$
Energy	$66.4 \pm 0.3$	$4.4 \pm 2.3$	$66.1 \pm 0.2$	$2.3\pm1.3$
Confidence	$66.7 \pm 0.0$	$0.0\pm0.0$	$66.7 \pm 0.0$	$0.0 \pm 0.0$
Original	$66.7 \pm 0.0$	$0.0\pm0.0$	$66.7 \pm 0.0$	$0.0 \pm 0.0$

Table 2. Detailed results for the Compas dataset in Test settings I.

Method	OOD 0	class: 0	OOD	class: 1	
	In	OOD	In	OOD	
Pipeline	$100.0\pm0.0$	$100.0\pm0.0$	$98.4 \pm 0.0$	$98.4 \pm 0.0$	
OCT	$96.4 \pm 0.2$	$96.4 \pm 0.2$	$96.2 \pm 0.5$	$96.3 \pm 0.5$	
MCDD	$66.0 \pm 0.0$	$2.0\pm0.0$	$86.8 \pm 0.0$	$84.4 \pm 0.0$	
O-GBDT	$66.7 \pm 0.0$	$0.0\pm0.0$	$66.7 \pm 0.0$	$0.0\pm0.0$	
DK	$67.5 \pm 0.1$	$7.1 \pm 0.8$	$68.1\pm0.6$	$13.1 \pm 4.4$	
Multi	$76.7\pm0.0$	$84.1\pm0.0$	$76.3 \pm 0.0$	$83.9 \pm 0.0$	
Incremental	$67.4 \pm 0.1$	$6.7 \pm 1.0$	$67.0\pm0.1$	$4.3\pm0.6$	
Energy+	$88.2 \pm 0.6$	$85.4 \pm 0.9$	$79.5 \pm 0.2$	$68.1 \pm 0.7$	
Self	$96.4 \pm 0.3$	$96.7 \pm 0.3$	$93.7 \pm 0.3$	$94.1 \pm 0.3$	
Exposure	$66.7 \pm 0.0$	$0.0\pm0.0$	$66.7 \pm 0.0$	$0.0 \pm 0.0$	
POEM	$91.0 \pm 0.0$	$89.5 \pm 0.0$	$77.9 \pm 0.0$	$63.3 \pm 0.0$	
WOODS	$68.2 \pm 2.5$	$13.4 \pm 12.4$	$69.2 \pm 2.3$	$20.4 \pm 12.0$	
Logitnorm	$67.2 \pm 0.9$	$9.9 \pm 6.7$	$67.6 \pm 1.4$	$12.5 \pm 9.0$	
VOS	$66.9 \pm 0.0$	$5.9 \pm 0.0$	$66.0\pm0.0$	$0.0\pm0.0$	
ReAct	$67.1 \pm 0.8$	$10.0 \pm 5.2$	$69.8 \pm 2.3$	$24.7 \pm 11.9$	
Energy	$66.7 \pm 0.6$	$8.9 \pm 3.0$	$69.7 \pm 2.3$	$23.0\pm12.4$	
Confidence	$66.7 \pm 0.0$	$0.0\pm0.0$	$66.7 \pm 0.0$	$0.0 \pm 0.0$	
Original	$66.7 \pm 0.0$	$0.0 \pm 0.0$	$66.7 \pm 0.0$	$0.0 \pm 0.0$	

Table 3. Detailed results for the Cover dataset in Test settings I. For this dataset, all samples from class 4 were detected as in-distribution by the OOD oracle, and this class was excluded from the experiment. DK could not be applied to this dataset due to huge memory requirement.

Method	OOD	class: 0	OOD	class: 1	OOD	class: 2	OOD	class: 3	OOD	class: 5	OOD	class: 6
memou	In	OOD	In	OOD	In	OOD	In	OOD	In	OOD	In	OOD
Pipeline	86.3 ± 0.2	97.6 ± 0.1	$86.4 \pm 0.4$	$96.7 \pm 0.3$	$81.5 \pm 0.4$	$98.6 \pm 0.0$	$80.8 \pm 0.5$	$97.3 \pm 0.4$	$83.4 \pm 0.3$	96.1 ± 0.2	$78.8 \pm 0.5$	95.8 ± 0.2
OCT	$79.6 \pm 0.4$	$93.8 \pm 0.5$	$80.7 \pm 0.6$	93.1 ± 0.5	$71.2 \pm 0.5$	$95.8 \pm 0.2$	$73.2 \pm 0.5$	$94.5 \pm 0.4$	$76.9 \pm 0.4$	$93.5 \pm 0.3$	$70.6 \pm 0.7$	$92.7 \pm 0.5$
MCDD O-GBDT DK Multi Incremental	$75.3 \pm 0.1$ $71.5 \pm 0.1$ - $27.8 \pm 0.3$ $5.6 \pm 0.4$	$12.8 \pm 0.4$ $1.0 \pm 0.1$ $ 2.0 \pm 0.4$ $0.0 \pm 0.0$	$71.6 \pm 0.6$ $66.7 \pm 0.5$ $ 24.6 \pm 0.5$ $10.2 \pm 0.3$	$26.4 \pm 1.8$ $9.9 \pm 1.1$ - $32.1 \pm 1.0$	$67.9 \pm 0.3$ $63.1 \pm 0.2$ - $26.8 \pm 0.3$ $6.7 \pm 0.1$	$34.0 \pm 0.7$ $0.0 \pm 0.0$ $0.8 \pm 0.1$	$72.0 \pm 0.9$ $67.4 \pm 1.2$ $ 23.6 \pm 0.9$	$23.7 \pm 1.8$ $0.0 \pm 0.0$ $ 0.1 \pm 0.1$	$76.6 \pm 0.2$ $73.7 \pm 0.2$ $ 26.6 \pm 0.4$	$11.0 \pm 0.9$ $0.0 \pm 0.0$ - $1.1 \pm 0.1$	$73.4 \pm 0.4$ $71.2 \pm 0.3$ $ 26.5 \pm 0.2$	$15.3 \pm 2.6$ $0.1 \pm 0.0$ $0.4 \pm 0.1$
Energy+ Self Exposure	$76.0 \pm 0.5$ $71.4 \pm 0.4$ $73.8 \pm 0.4$	$81.5 \pm 1.7$ $46.5 \pm 1.9$ $35.4 \pm 2.5$	$72.7 \pm 0.7$ $71.8 \pm 0.5$ $69.4 \pm 0.5$	$0.0 \pm 0.0$ $74.2 \pm 1.6$ $68.0 \pm 3.4$ $40.0 \pm 2.4$	$70.6 \pm 0.6$ $58.2 \pm 0.3$ $63.1 \pm 0.3$	$0.0 \pm 0.0$ $94.5 \pm 0.3$ $0.7 \pm 0.1$ $7.2 \pm 0.7$	$6.9 \pm 0.2$ $69.4 \pm 1.2$ $64.8 \pm 1.2$ $67.0 \pm 1.2$	$0.0 \pm 0.0$ $83.8 \pm 1.3$ $1.0 \pm 0.3$ $4.5 \pm 1.9$	$6.3 \pm 0.1$ $77.1 \pm 0.4$ $72.8 \pm 0.2$ $75.4 \pm 0.2$	$0.0 \pm 0.0$ $87.8 \pm 0.8$ $1.9 \pm 0.3$ $4.4 \pm 1.0$	$4.0 \pm 0.2$ $71.1 \pm 0.9$ $71.2 \pm 0.4$ $71.9 \pm 0.5$	$0.0 \pm 0.0$ $84.2 \pm 1.5$ $72.1 \pm 2.7$ $42.1 \pm 3.4$
POEM WOODS Logitnorm VOS ReAct Energy Confidence	$62.7 \pm 0.2$ $66.1 \pm 0.4$ $69.9 \pm 0.9$ $68.2 \pm 0.3$ $67.7 \pm 0.9$ $71.3 \pm 0.3$ $72.2 \pm 0.2$	$0.2 \pm 0.1$ $0.6 \pm 0.3$ $1.6 \pm 0.9$ $0.0 \pm 0.0$ $4.9 \pm 2.4$ $3.0 \pm 1.3$ $0.3 \pm 0.1$	$60.3 \pm 0.9$ $62.4 \pm 0.8$ $64.7 \pm 1.2$ $61.5 \pm 0.8$ $64.9 \pm 0.7$ $67.4 \pm 0.7$ $66.3 \pm 0.7$	$22.1 \pm 1.5$ $14.6 \pm 3.2$ $4.4 \pm 0.8$ $0.1 \pm 0.0$ $19.6 \pm 3.1$ $20.6 \pm 3.3$ $4.2 \pm 0.8$	$56.8 \pm 0.1$ $58.3 \pm 0.5$ $61.2 \pm 0.5$ $59.2 \pm 0.4$ $55.3 \pm 1.4$ $62.5 \pm 0.3$ $63.2 \pm 0.3$	$51.3 \pm 2.2$ $0.0 \pm 0.0$ $3.0 \pm 1.3$ $25.1 \pm 3.5$ $3.4 \pm 1.6$ $3.5 \pm 1.7$ $0.3 \pm 0.0$	$62.3 \pm 0.8$ $62.8 \pm 1.1$ $64.3 \pm 1.7$ $66.3 \pm 0.0$ $59.2 \pm 1.8$ $65.9 \pm 1.0$ $66.8 \pm 1.0$	$2.9 \pm 0.8$ $0.0 \pm 0.0$ $1.1 \pm 0.6$ $0.0 \pm 0.0$ $0.6 \pm 0.5$ $0.1 \pm 0.1$ $0.0 \pm 0.0$	$69.4 \pm 0.3$ $71.3 \pm 0.2$ $73.4 \pm 0.9$ $70.0 \pm 0.1$ $70.2 \pm 0.8$ $74.4 \pm 0.2$ $75.2 \pm 0.3$	$19.5 \pm 1.6$ $0.0 \pm 0.0$ $1.1 \pm 0.6$ $0.4 \pm 0.1$ $0.2 \pm 0.1$ $0.4 \pm 0.2$ $0.1 \pm 0.0$	$64.5 \pm 0.4$ $69.5 \pm 0.4$ $70.1 \pm 0.4$ $68.7 \pm 0.3$ $66.9 \pm 0.9$ $71.4 \pm 0.4$ $72.2 \pm 0.4$	$0.0 \pm 0.0$ $0.4 \pm 0.2$ $0.3 \pm 0.2$ $0.0 \pm 0.0$ $7.3 \pm 3.2$ $1.7 \pm 0.9$ $0.1 \pm 0.0$
Original	$71.8 \pm 0.3$	$0.0 \pm 0.0$	66.3 ± 0.7	$0.0 \pm 0.0$	$62.8 \pm 0.4$	$0.0 \pm 0.0$	66.2 ± 1.0	$0.0 \pm 0.0$	$74.9 \pm 0.2$	$0.0 \pm 0.0$	$72.1 \pm 0.3$	$0.0 \pm 0.0$

Table 4. Detailed results for the Dilbert dataset in Test settings I. For this dataset, all samples from classes 1, 2, and 4 were detected as in-distribution by the OOD oracle, and these classes were excluded from the experiment. DK could not be applied to this dataset due to huge memory requirement.

Method	OOD	class: 0	OOD	class: 3
Wicthou	In	OOD	In	OOD
Pipeline	$95.2 \pm 0.6$	$98.8 \pm 0.1$	$96.1 \pm 0.2$	$98.9 \pm 0.1$
OCT	78.1 ± 1.1	$68.9 \pm 2.7$	$84.8 \pm 0.9$	$91.1 \pm 0.6$
MCDD	$74.0 \pm 0.3$	$40.8 \pm 2.6$	$76.7 \pm 0.6$	$39.7 \pm 3.7$
O-GBDT	$75.9 \pm 0.8$	$59.6 \pm 2.0$	$75.1 \pm 0.4$	$69.2 \pm 1.3$
DK	-	-	-	-
Multi	$51.0 \pm 1.2$	$68.5 \pm 2.0$	$59.2 \pm 0.6$	$97.8 \pm 0.1$
Incremental	$39.6 \pm 1.8$	$0.0\pm0.0$	$35.6 \pm 1.6$	$0.0\pm0.0$
Energy+	$78.0 \pm 0.9$	62.7 ± 2.8	$78.4 \pm 0.6$	$75.0 \pm 1.6$
Self	$64.8 \pm 4.0$	$12.8 \pm 3.9$	$79.4 \pm 0.6$	$67.5 \pm 2.0$
Exposure	$81.5 \pm 0.9$	$64.0 \pm 2.9$	$84.7\pm0.6$	$80.4 \pm 1.5$
POEM	$61.0 \pm 0.8$	$0.0 \pm 0.0$	$73.9 \pm 0.3$	$0.2 \pm 0.1$
WOODS	$58.0 \pm 1.2$	$2.7 \pm 2.5$	$60.4\pm0.7$	$3.3 \pm 1.5$
Logitnorm	$72.4\pm0.4$	$4.5 \pm 1.7$	$74.6 \pm 0.7$	$10.3 \pm 2.6$
VOS	$70.1\pm0.4$	$0.0\pm0.0$	$71.7\pm0.1$	$0.0\pm0.0$
ReAct	$73.6 \pm 1.0$	$15.8 \pm 4.4$	$72.9 \pm 0.8$	$13.3 \pm 3.8$
Energy	$73.8 \pm 0.8$	$17.6 \pm 4.9$	$73.3 \pm 0.4$	$6.7 \pm 2.7$
Confidence	$72.2\pm0.9$	$27.2 \pm 3.6$	$71.7 \pm 2.9$	$19.8 \pm 3.1$
Original	$72.4 \pm 0.6$	$0.0 \pm 0.0$	$73.4 \pm 0.3$	$0.0 \pm 0.0$

Table 5. Detailed results for the GMSC dataset in Test settings I.

Method	OOD	class: 0	OOD c	lass: 1
	In	OOD	In	OOD
Pipeline	$98.9 \pm 0.0$	$99.0 \pm 0.0$	$98.7 \pm 0.0$	$98.8 \pm 0.0$
OCT	95.1 ± 1.2	94.7 ± 1.4	89.1 ± 0.9	$86.9 \pm 1.5$
MCDD	$66.8 \pm 0.0$	$1.2 \pm 0.0$	$82.9 \pm 0.0$	$75.4 \pm 0.0$
O-GBDT	$67.7 \pm 0.1$	$8.9 \pm 0.5$	$66.8 \pm 0.0$	$3.1 \pm 0.2$
DK	$66.8 \pm 0.0$	$1.0 \pm 0.2$	$67.0 \pm 0.0$	$3.6 \pm 0.4$
Multi	$94.6 \pm 0.0$	$95.1 \pm 0.0$	$95.1 \pm 0.0$	$95.6 \pm 0.0$
Incremental	$66.9 \pm 0.1$	$1.7\pm0.5$	$67.7\pm0.1$	$8.8\pm1.1$
Energy+	91.1 ± 1.4	89.4 ± 2.1	$79.9 \pm 0.7$	68.7 ± 1.7
Self	$74.3 \pm 18.6$	$86.9 \pm 5.3$	$54.0 \pm 21.0$	$77.7 \pm 5.0$
Exposure	$66.7\pm0.0$	$0.0\pm0.0$	$66.7\pm0.0$	$0.0\pm0.0$
POEM	$82.2 \pm 0.0$	$73.8 \pm 0.0$	$80.3 \pm 0.0$	$69.7 \pm 0.0$
WOODS	$71.9 \pm 3.8$	$28.6 \pm 17.5$	$70.3 \pm 1.7$	$29.6 \pm 9.1$
Logitnorm	$66.6 \pm 0.3$	$6.0 \pm 2.4$	$68.9 \pm 1.1$	$21.8 \pm 7.4$
VOS	$66.2\pm0.0$	$3.0 \pm 0.0$	$65.4\pm0.0$	$0.0\pm0.0$
ReAct	$67.5 \pm 0.7$	$13.0 \pm 4.8$	$67.1 \pm 0.4$	$10.1 \pm 3.0$
Energy	$67.4 \pm 0.7$	$12.1 \pm 4.5$	$68.4 \pm 0.9$	$17.0 \pm 5.7$
Confidence	$66.7\pm0.0$	$0.0\pm0.0$	$66.7\pm0.0$	$0.0\pm0.0$
Original	$66.7 \pm 0.0$	$0.0 \pm 0.0$	$66.7 \pm 0.0$	$0.0 \pm 0.0$

Table 6. Detailed results for the Heloc dataset in Test settings I.

Method	OOD	class: 0	OOD	class: 1	
	In	OOD	In	OOD	
Pipeline	$98.8 \pm 0.0$	$98.8 \pm 0.0$	$99.1 \pm 0.0$	$99.1 \pm 0.0$	
OCT	$88.9 \pm 1.4$	$86.6 \pm 2.3$	$89.4 \pm 0.9$	$87.6 \pm 1.4$	
MCDD	$75.1 \pm 0.0$	$53.9 \pm 0.0$	$72.7 \pm 0.0$	$43.2 \pm 0.0$	
O-GBDT	$67.8 \pm 0.1$	$10.3 \pm 0.9$	$67.2 \pm 0.3$	$5.8 \pm 3.5$	
DK	$67.0 \pm 0.1$	$3.0 \pm 0.5$	$66.7 \pm 0.0$	$0.0 \pm 0.0$	
Multi	$95.0 \pm 0.0$	$95.5 \pm 0.0$	$96.4 \pm 0.0$	$96.6 \pm 0.0$	
Incremental	$67.1\pm0.1$	$3.4\pm0.6$	$66.7\pm0.0$	$0.0\pm0.0$	
Energy+	$81.6 \pm 0.4$	$72.7 \pm 0.9$	$80.4 \pm 0.8$	69.4 ± 1.9	
Self	$91.9 \pm 0.7$	$91.3 \pm 1.0$	$85.8 \pm 1.1$	$81.6 \pm 2.4$	
Exposure	$66.7\pm0.0$	$0.0\pm0.0$	$66.7\pm0.0$	$0.0\pm0.0$	
POEM	$78.9 \pm 0.0$	$65.6 \pm 0.0$	$72.4 \pm 0.0$	$44.7 \pm 0.0$	
WOODS	$67.2 \pm 1.7$	$9.8 \pm 9.8$	$69.2 \pm 1.5$	$22.1 \pm 10.1$	
Logitnorm	$67.6 \pm 1.3$	$14.1\pm8.0$	$67.8\pm0.4$	$11.6 \pm 2.7$	
VOS	$66.6 \pm 0.0$	$8.2 \pm 0.0$	$67.1 \pm 0.0$	$9.8 \pm 0.0$	
ReAct	$67.9 \pm 0.8$	$15.9 \pm 4.8$	$67.0 \pm 0.9$	$12.8 \pm 6.5$	
Energy	$67.9 \pm 0.8$	$17.6 \pm 5.4$	$67.8 \pm 0.8$	$17.0 \pm 6.1$	
Confidence	$66.7 \pm 0.0$	$0.0\pm0.0$	$66.7 \pm 0.0$	$0.0\pm0.0$	
Original	$66.7 \pm 0.0$	$0.0 \pm 0.0$	$66.7 \pm 0.0$	$0.0 \pm 0.0$	

Table 7. Detailed results for the Jannis dataset in Test settings I. For this dataset, all samples from class 0 were detected as in-distribution by the OOD oracle, and this class was excluded from the experiment. DK could not be applied to this dataset due to huge memory requirement.

Method	OOD	class: 1	OOD	class: 2	OOD	class: 3
	In	OOD	In	OOD	In	OOD
Pipeline	$63.3 \pm 1.1$	$98.8 \pm 0.1$	$52.2 \pm 0.7$	$99.2 \pm 0.1$	$51.8 \pm 0.2$	99.1 ± 0.0
OCT	$52.2 \pm 2.4$	87.9 ± 1.0	$41.9 \pm 2.0$	88.1 ± 1.0	$44.9 \pm 0.6$	$91.7 \pm 0.5$
MCDD	$42.0 \pm 0.9$	$12.8 \pm 0.3$	$29.2 \pm 0.7$	$3.5 \pm 0.5$	$25.2 \pm 0.4$	$2.1 \pm 0.2$
O-GBDT	$42.8 \pm 1.0$	$1.5 \pm 0.2$	$43.2 \pm 1.5$	$1.2 \pm 0.2$	$42.1\pm0.2$	$17.4 \pm 1.7$
DK	-	-	-	-	-	-
Multi	$41.6 \pm 0.3$	$57.2 \pm 1.2$	$34.4 \pm 0.3$	$44.9 \pm 1.1$	$38.9 \pm 0.4$	$81.6 \pm 1.2$
Incremental	$11.7 \pm 1.0$	$0.0\pm0.0$	$12.9\pm0.9$	$1.9\pm0.2$	$17.4\pm0.7$	$0.1\pm0.0$
Energy+	$45.8 \pm 0.8$	49.7 ± 1.7	$40.3 \pm 0.6$	$38.9 \pm 2.3$	$46.4 \pm 0.5$	$75.1 \pm 2.3$
Self	$41.3 \pm 1.9$	$49.8 \pm 3.0$	$32.4 \pm 2.0$	$31.3 \pm 3.5$	$38.0 \pm 1.5$	$78.9 \pm 1.4$
Exposure	$44.9\pm0.8$	$31.9 \pm 2.5$	$37.8 \pm 1.6$	$9.2 \pm 1.4$	$42.4\pm0.3$	$9.5 \pm 1.3$
POEM	44.9 ± 1.1	$50.5 \pm 0.4$	$39.9 \pm 0.5$	$61.1 \pm 0.6$	$39.0 \pm 0.2$	$14.7 \pm 0.5$
WOODS	$45.5\pm1.0$	$41.7 \pm 4.4$	$39.9 \pm 0.5$	$50.5 \pm 5.9$	$39.9 \pm 0.4$	$8.5 \pm 1.2$
Logitnorm	$41.3\pm0.7$	$4.3 \pm 0.6$	$36.5 \pm 0.6$	$3.9 \pm 1.2$	$40.4\pm0.3$	$0.3 \pm 0.1$
VOS	$40.9 \pm 0.7$	$10.9 \pm 0.8$	$38.3 \pm 0.6$	$1.0 \pm 0.2$	$39.8 \pm 0.3$	$0.0 \pm 0.0$
ReAct	$41.1 \pm 0.7$	$7.7 \pm 1.3$	$36.9 \pm 0.5$	$3.2 \pm 1.5$	$39.8 \pm 0.4$	$2.9 \pm 1.5$
Energy	$41.4 \pm 0.7$	$7.3 \pm 1.2$	$37.3 \pm 0.5$	$3.3 \pm 1.5$	$40.2 \pm 0.2$	$2.6 \pm 1.1$
Confidence	$41.7\pm0.6$	$9.6 \pm 0.8$	$36.7 \pm 1.0$	$0.5\pm0.1$	$40.5\pm0.2$	$1.2\pm0.4$
Original	$41.1 \pm 0.7$	$0.0 \pm 0.0$	$37.3 \pm 0.4$	$0.0 \pm 0.0$	$40.4 \pm 0.2$	$0.0 \pm 0.0$

Table 8. Detailed results for the Adult dataset in Test settings II.

Method	Method $T_1$			$T_2$		$\overline{T_3}$		$T_4$
Wicthod	Actual	OOD	Actual	OOD	Actual	OOD	Actual	OOD
Pipeline	$74.8 \pm 0.6$	$99.1 \pm 0.0$	$74.8 \pm 0.6$	$99.1 \pm 0.0$	$74.8 \pm 0.6$	$99.1 \pm 0.0$	$74.8 \pm 0.6$	$99.1 \pm 0.0$
OCT	$74.1 \pm 0.5$	$98.4 \pm 0.0$	$74.1 \pm 0.5$	$98.3 \pm 0.0$	$74.2 \pm 0.5$	$98.4 \pm 0.0$	$74.2 \pm 0.5$	$98.5 \pm 0.1$
MCDD O-GBDT DK Multi Incremental	$52.8 \pm 0.0$ $57.6 \pm 0.0$ $57.0 \pm 0.1$ $62.7 \pm 0.0$ $39.6 \pm 1.0$	$27.3 \pm 0.0$ $52.4 \pm 0.0$ $56.7 \pm 1.0$ $90.6 \pm 0.0$ $53.3 \pm 2.5$	$53.8 \pm 0.0$ $57.9 \pm 0.0$ $57.3 \pm 0.2$ $62.7 \pm 0.0$ $40.2 \pm 1.1$	$33.2 \pm 0.0$ $55.1 \pm 0.0$ $58.1 \pm 1.2$ $90.6 \pm 0.0$ $54.9 \pm 2.5$	$55.2 \pm 0.0$ $56.8 \pm 0.0$ $59.5 \pm 0.2$ $62.7 \pm 0.0$ $41.1 \pm 1.1$	$43.3 \pm 0.0$ $49.4 \pm 0.0$ $67.3 \pm 1.0$ $90.6 \pm 0.0$ $62.9 \pm 2.7$	$56.1 \pm 0.0$ $78.0 \pm 0.1$ $71.0 \pm 0.3$ $62.7 \pm 0.0$ $48.3 \pm 1.7$	$42.7 \pm 0.0$ $100.0 \pm 0.0$ $94.8 \pm 0.4$ $90.6 \pm 0.0$ $93.8 \pm 0.6$
Energy+ Self Exposure	$72.9 \pm 1.0$ $72.8 \pm 0.7$ $64.7 \pm 1.7$	$98.6 \pm 0.1$ $97.6 \pm 0.1$ $79.3 \pm 4.6$	$72.9 \pm 1.0$ $72.6 \pm 0.7$ $63.2 \pm 2.2$	$98.5 \pm 0.1$ $97.3 \pm 0.1$ $73.5 \pm 6.8$	$72.9 \pm 1.0$ $72.3 \pm 0.7$ $62.8 \pm 2.8$	$98.6 \pm 0.1$ $97.0 \pm 0.2$ $68.9 \pm 10.0$	$73.2 \pm 1.0$ $73.0 \pm 0.7$ $65.2 \pm 4.0$	$99.0 \pm 0.0$ $97.8 \pm 0.1$ $66.7 \pm 14.6$
POEM WOODS Logitnorm VOS ReAct Energy Confidence	$68.0 \pm 0.0$ $54.8 \pm 2.3$ $50.0 \pm 0.3$ $48.5 \pm 0.0$ $50.3 \pm 0.4$ $50.9 \pm 0.6$ $50.2 \pm 0.2$	$87.2 \pm 0.0$ $47.2 \pm 19.3$ $7.4 \pm 3.5$ $0.1 \pm 0.0$ $11.8 \pm 4.6$ $13.0 \pm 6.6$ $2.8 \pm 0.3$	$70.7 \pm 0.0$ $56.8 \pm 2.8$ $50.5 \pm 0.2$ $49.1 \pm 0.0$ $50.6 \pm 0.5$ $51.5 \pm 0.6$ $50.6 \pm 0.3$	$92.3 \pm 0.0$ $51.6 \pm 21.1$ $8.3 \pm 3.4$ $0.4 \pm 0.0$ $11.4 \pm 4.2$ $13.8 \pm 7.3$ $2.4 \pm 0.3$	$71.6 \pm 0.0$ $58.1 \pm 3.1$ $50.6 \pm 0.2$ $49.6 \pm 0.0$ $50.7 \pm 0.5$ $51.6 \pm 0.8$ $50.5 \pm 0.3$	$93.8 \pm 0.0$ $54.0 \pm 22.0$ $9.5 \pm 3.4$ $0.9 \pm 0.0$ $11.3 \pm 3.6$ $15.4 \pm 8.1$ $2.4 \pm 0.5$	$75.4 \pm 0.0$ $62.0 \pm 4.2$ $54.0 \pm 0.2$ $52.8 \pm 0.0$ $52.7 \pm 1.0$ $54.7 \pm 0.4$ $54.0 \pm 0.4$	$99.0 \pm 0.0$ $59.4 \pm 24.3$ $6.6 \pm 5.1$ $0.1 \pm 0.0$ $4.1 \pm 2.1$ $9.4 \pm 7.6$ $0.6 \pm 0.2$
Original	$50.1 \pm 0.2$	$0.0 \pm 0.0$	$50.6 \pm 0.2$	$0.0 \pm 0.0$	$50.6 \pm 0.2$	$0.0 \pm 0.0$	$54.5 \pm 0.3$	$0.0 \pm 0.0$

Table 9. Detailed results for the Compas dataset in Test settings II.

Method	ethod $T_1$			$T_2$		$T_3$		$T_4$
Wethou	Actual	OOD	Actual	OOD	Actual	OOD	Actual	OOD
Pipeline	$67.6 \pm 0.7$	$98.7 \pm 0.0$	$67.6 \pm 0.7$	$98.7 \pm 0.0$	$67.6 \pm 0.7$	$98.7 \pm 0.0$	$67.6 \pm 0.7$	$98.7 \pm 0.0$
OCT	$67.3 \pm 0.7$	$97.9 \pm 0.1$	$67.3 \pm 0.7$	$98.0 \pm 0.1$	$67.3 \pm 0.7$	$98.0 \pm 0.1$	$67.3 \pm 0.7$	$98.0 \pm 0.1$
MCDD O-GBDT	$54.1 \pm 0.0$ $52.9 \pm 0.1$	$57.5 \pm 0.3$ $63.0 \pm 0.0$	$55.2 \pm 0.1$ $52.0 \pm 0.1$	$61.8 \pm 0.1$ $58.8 \pm 0.0$	$57.1 \pm 0.0$ $51.2 \pm 0.1$	$69.0 \pm 0.4$ $54.7 \pm 0.0$	$58.5 \pm 0.3$ $69.1 \pm 0.1$	$73.5 \pm 0.4$ $100.0 \pm 0.0$
DK	$51.8\pm0.8$	$54.6 \pm 4.8$	$53.0 \pm 1.0$	$60.9 \pm 4.9$	$55.1 \pm 1.0$	$69.8 \pm 3.9$	$63.7 \pm 1.6$	$91.7 \pm 3.0$
Multi Incremental	$51.0 \pm 0.0$ $40.4 \pm 1.8$	$85.5 \pm 0.0$ $38.1 \pm 2.5$	$51.0 \pm 0.0$ $40.6 \pm 1.9$	$85.5 \pm 0.0$ $41.1 \pm 2.4$	$51.0 \pm 0.0$ $41.9 \pm 1.9$	$85.5 \pm 0.0$ $50.9 \pm 2.7$	$51.0 \pm 0.0$ $49.0 \pm 2.5$	$85.5 \pm 0.0$ $83.8 \pm 3.2$
Energy+ Self Exposure	$66.4 \pm 0.9$ $66.3 \pm 0.7$ $49.3 \pm 0.8$	$97.7 \pm 0.2$ $97.3 \pm 0.4$ $35.3 \pm 10.5$	$66.6 \pm 0.8$ $66.3 \pm 0.7$ $49.3 \pm 0.9$	$97.9 \pm 0.1$ $97.3 \pm 0.4$ $36.0 \pm 10.7$	$66.7 \pm 0.8$ $66.4 \pm 0.7$ $49.3 \pm 0.9$	$98.2 \pm 0.1$ $97.4 \pm 0.4$ $33.3 \pm 10.9$	$67.1 \pm 0.8$ $66.5 \pm 0.7$ $50.0 \pm 1.3$	$98.5 \pm 0.0$ $97.5 \pm 0.4$ $33.9 \pm 12.4$
POEM WOODS Logitnorm VOS ReAct Energy	$56.0 \pm 0.0$ $55.8 \pm 0.6$ $45.7 \pm 0.7$ $45.0 \pm 0.0$ $45.8 \pm 0.5$ $45.7 \pm 0.4$	$89.2 \pm 0.0$ $84.5 \pm 0.7$ $16.4 \pm 5.2$ $21.7 \pm 0.0$ $9.3 \pm 4.5$ $7.4 \pm 3.6$	$57.6 \pm 0.0$ $58.3 \pm 0.6$ $45.8 \pm 0.7$ $45.5 \pm 0.0$ $45.6 \pm 0.4$ $45.5 \pm 0.3$	$92.5 \pm 0.0$ $90.3 \pm 0.4$ $16.9 \pm 5.5$ $26.5 \pm 0.0$ $9.1 \pm 3.1$ $7.1 \pm 2.7$	$58.8 \pm 0.0$ $59.7 \pm 0.5$ $46.3 \pm 0.9$ $46.4 \pm 0.0$ $46.1 \pm 0.4$ $45.9 \pm 0.3$	$94.8 \pm 0.0$ $93.3 \pm 0.2$ $17.8 \pm 6.9$ $33.7 \pm 0.0$ $10.3 \pm 2.6$ $7.7 \pm 3.0$	$61.4 \pm 0.0$ $63.0 \pm 0.5$ $46.7 \pm 0.8$ $48.7 \pm 0.0$ $46.0 \pm 0.4$ $45.8 \pm 0.4$	$98.7 \pm 0.0$ $98.3 \pm 0.1$ $18.1 \pm 7.1$ $49.4 \pm 0.0$ $9.3 \pm 3.3$ $6.7 \pm 3.3$
Confidence Original	$43.9 \pm 0.6$ $45.5 \pm 0.3$	$5.7 \pm 1.4$ $0.0 \pm 0.0$	$44.1 \pm 0.6 \\ \hline 45.4 \pm 0.3$	$4.7 \pm 1.4$ $0.0 \pm 0.0$	$44.7 \pm 0.6 \\ \hline 45.8 \pm 0.3$	$4.3 \pm 1.4$ $0.0 \pm 0.0$	$45.4 \pm 0.6$ $45.8 \pm 0.3$	$4.4 \pm 1.6$ $0.0 \pm 0.0$

Table 10. Detailed results for the Cover dataset in Test settings II. DK could not be applied to this dataset due to huge memory requirement.

Method	7	T <sub>1</sub>	7		7	r <sub>3</sub>		$T_4$
Welloa	Actual	OOD	Actual	OOD	Actual	OOD	Actual	OOD
Pipeline	$66.1 \pm 0.3$	$99.0 \pm 0.0$	$66.1 \pm 0.3$	$99.0 \pm 0.0$	$66.1 \pm 0.3$	$99.0 \pm 0.0$	$66.1 \pm 0.3$	$99.0 \pm 0.0$
OCT	$62.0 \pm 0.3$	$98.3 \pm 0.1$	$62.0 \pm 0.3$	$98.3 \pm 0.1$	$62.1 \pm 0.3$	$98.4 \pm 0.1$	$62.1 \pm 0.3$	$98.4 \pm 0.1$
MCDD O-GBDT DK Multi Incremental	$66.1 \pm 0.4$ $50.0 \pm 0.1$ - $17.7 \pm 0.1$ $7.3 \pm 0.1$	$35.3 \pm 1.9$ $69.1 \pm 0.5$ - $38.7 \pm 0.5$ $12.1 \pm 0.4$	$66.7 \pm 0.4$ $50.9 \pm 0.1$ $-$ $19.1 \pm 0.1$ $7.5 \pm 0.1$	$37.8 \pm 2.0$ $78.5 \pm 0.2$ $-$ $61.8 \pm 0.4$ $13.4 \pm 0.4$	$68.5 \pm 0.4$ $58.6 \pm 0.1$ - $25.8 \pm 0.2$ $8.4 \pm 0.1$	$51.3 \pm 3.3$ $95.9 \pm 0.1$ - $98.3 \pm 0.0$ $49.6 \pm 0.4$	$75.5 \pm 0.5$ $67.2 \pm 0.1$ - $27.5 \pm 0.2$ $9.2 \pm 0.1$	$68.7 \pm 7.7$ $100.0 \pm 0.0$ $-$ $100.0 \pm 0.0$ $99.9 \pm 0.0$
Energy+ Self Exposure	$66.9 \pm 0.5$ $62.7 \pm 0.5$ $71.2 \pm 0.4$	$99.0 \pm 0.0$ $99.8 \pm 0.0$ $98.9 \pm 0.0$	$67.0 \pm 0.5$ $62.9 \pm 0.5$ $71.4 \pm 0.4$	$99.0 \pm 0.0$ $99.8 \pm 0.0$ $99.0 \pm 0.0$	$67.0 \pm 0.5$ $62.9 \pm 0.5$ $71.5 \pm 0.4$	$99.0 \pm 0.0$ $99.9 \pm 0.0$ $99.0 \pm 0.0$	$67.0 \pm 0.5$ $63.0 \pm 0.5$ $71.5 \pm 0.4$	$99.0 \pm 0.0$ $99.9 \pm 0.0$ $99.0 \pm 0.0$
POEM WOODS Logitnorm VOS ReAct Energy Confidence	$51.2 \pm 0.1$ $43.4 \pm 0.7$ $52.4 \pm 0.8$ $35.7 \pm 0.4$ $53.9 \pm 0.9$ $55.3 \pm 0.7$ $51.5 \pm 1.1$	$91.3 \pm 0.3$ $2.3 \pm 0.6$ $0.9 \pm 0.3$ $5.9 \pm 0.2$ $6.0 \pm 1.6$ $5.8 \pm 2.2$ $0.4 \pm 0.1$	$51.8 \pm 0.1$ $43.8 \pm 0.7$ $53.0 \pm 0.8$ $34.3 \pm 0.3$ $54.3 \pm 1.0$ $55.7 \pm 0.7$ $51.8 \pm 1.1$	$93.1 \pm 0.2$ $2.1 \pm 0.6$ $0.7 \pm 0.3$ $5.7 \pm 0.2$ $6.3 \pm 1.7$ $6.1 \pm 2.4$ $0.3 \pm 0.1$	$53.9 \pm 0.1$ $44.1 \pm 0.6$ $54.3 \pm 0.9$ $31.0 \pm 0.2$ $55.0 \pm 1.1$ $56.5 \pm 0.8$ $52.8 \pm 1.3$	$97.1 \pm 0.0$ $1.3 \pm 0.2$ $0.5 \pm 0.3$ $2.6 \pm 0.1$ $7.5 \pm 2.2$ $7.6 \pm 3.2$ $0.1 \pm 0.0$	$57.3 \pm 0.2$ $51.2 \pm 0.7$ $57.3 \pm 0.9$ $34.0 \pm 0.4$ $57.0 \pm 0.9$ $60.1 \pm 0.8$ $57.6 \pm 1.2$	$99.0 \pm 0.0$ $0.0 \pm 0.0$ $0.2 \pm 0.2$ $1.4 \pm 0.0$ $7.1 \pm 3.7$ $7.3 \pm 4.8$ $0.0 \pm 0.0$
Original	$55.3 \pm 0.7$	$0.0 \pm 0.0$	55.7 ± 0.7	$0.0 \pm 0.0$	$56.4 \pm 0.8$	$0.0 \pm 0.0$	$60.1 \pm 0.7$	$0.0 \pm 0.0$

Table 11. Detailed results for the Dilbert dataset in Test settings II. DK could not be applied to this dataset due to huge memory requirement.

Method	7	1	7	<u></u>	7	3	7	4
Wiethod	Actual	OOD	Actual	OOD	Actual	OOD	Actual	OOD
Pipeline	89.9 ± 3.5	$99.1 \pm 0.0$	89.9 ± 3.5	$99.1 \pm 0.0$	89.9 ± 3.5	$99.1 \pm 0.0$	$89.9 \pm 3.5$	$99.1 \pm 0.0$
OCT	$87.3 \pm 0.6$	$96.3 \pm 0.2$	$87.1 \pm 0.6$	$96.1 \pm 0.2$	$88.3 \pm 0.6$	$97.5 \pm 0.3$	$88.3 \pm 0.6$	$97.5 \pm 0.3$
MCDD O-GBDT DK Multi Incremental	$69.4 \pm 0.2$ $81.0 \pm 0.2$ - $53.6 \pm 0.2$ $27.8 \pm 1.5$	$31.3 \pm 1.7$ $91.6 \pm 0.2$ - $98.3 \pm 0.0$ $0.2 \pm 0.0$	$68.9 \pm 0.2$ $81.3 \pm 0.2$ - $53.9 \pm 0.1$ $27.7 \pm 1.5$	$29.2 \pm 1.6$ $92.0 \pm 0.2$ - $98.9 \pm 0.0$ $0.2 \pm 0.0$	$72.0 \pm 0.2$ $85.2 \pm 0.1$ - $54.0 \pm 0.1$ $28.0 \pm 1.5$	$28.1 \pm 2.5$ $97.7 \pm 0.1$ - $99.2 \pm 0.0$ $3.7 \pm 0.2$	$76.3 \pm 0.7$ $86.9 \pm 0.1$ - $54.0 \pm 0.1$ $40.5 \pm 2.0$	$30.1 \pm 4.4$ $99.8 \pm 0.0$ - $99.2 \pm 0.0$ $96.0 \pm 4.0$
Energy+ Self Exposure	$87.1 \pm 0.4$ $76.9 \pm 5.2$ $90.4 \pm 0.2$	$96.8 \pm 0.1$ $92.9 \pm 1.6$ $95.3 \pm 0.1$	$87.1 \pm 0.4$ $76.1 \pm 5.1$ $90.2 \pm 0.3$	$96.8 \pm 0.1$ $91.7 \pm 1.5$ $95.0 \pm 0.1$	$88.4 \pm 0.4$ $80.0 \pm 5.4$ $92.8 \pm 0.2$	$98.3 \pm 0.1$ $96.8 \pm 1.8$ $98.0 \pm 0.1$	$88.4 \pm 0.4$ $80.0 \pm 5.4$ $92.4 \pm 0.4$	$98.3 \pm 0.1$ $96.8 \pm 1.8$ $97.1 \pm 0.9$
POEM WOODS Logitnorm VOS ReAct Energy Confidence	$61.5 \pm 0.3$ $62.9 \pm 0.7$ $67.0 \pm 0.2$ $62.7 \pm 0.4$ $62.7 \pm 2.5$ $64.1 \pm 2.5$ $64.1 \pm 0.5$	$44.8 \pm 0.3$ $59.6 \pm 5.2$ $13.0 \pm 1.8$ $3.2 \pm 0.4$ $9.0 \pm 1.1$ $9.5 \pm 1.4$ $15.7 \pm 1.6$	$61.8 \pm 0.3$ $62.8 \pm 0.7$ $66.9 \pm 0.2$ $62.8 \pm 0.3$ $62.6 \pm 2.5$ $64.0 \pm 2.5$ $63.9 \pm 0.5$	$48.9 \pm 0.8$ $60.1 \pm 5.2$ $11.9 \pm 1.7$ $2.1 \pm 0.3$ $7.8 \pm 1.1$ $8.0 \pm 1.4$ $14.1 \pm 1.5$	$69.4 \pm 0.3$ $72.4 \pm 1.0$ $70.2 \pm 0.3$ $66.4 \pm 0.5$ $65.6 \pm 2.6$ $67.0 \pm 2.7$ $65.8 \pm 0.6$	$77.2 \pm 0.3$ $80.4 \pm 7.2$ $10.2 \pm 1.6$ $0.4 \pm 0.1$ $5.3 \pm 1.3$ $5.3 \pm 1.8$ $13.8 \pm 1.6$	$79.3 \pm 0.3$ $74.7 \pm 0.9$ $75.6 \pm 0.6$ $72.1 \pm 0.4$ $72.2 \pm 2.9$ $72.8 \pm 2.9$ $71.8 \pm 0.8$	$99.0 \pm 0.0$ $83.1 \pm 7.4$ $2.5 \pm 1.1$ $0.0 \pm 0.0$ $2.9 \pm 2.4$ $1.1 \pm 0.8$ $5.7 \pm 1.0$
Original	$63.7 \pm 2.5$	$0.0 \pm 0.0$	$63.8 \pm 2.5$	$0.0 \pm 0.0$	$67.2 \pm 2.7$	$0.0 \pm 0.0$	$73.4 \pm 3.0$	$0.0 \pm 0.0$

Table 12. Detailed results for the GMSC dataset in Test settings II.

Method	Method $T_1$			$T_2$		$\overline{I_3}$		$T_4$
Wicthod	Actual	OOD	Actual	OOD	Actual	OOD	Actual	OOD
Pipeline	$58.2 \pm 0.7$	$99.1 \pm 0.0$						
OCT	$60.3 \pm 0.5$	$99.3 \pm 0.1$	$60.4 \pm 0.5$	$99.3 \pm 0.1$	$60.4 \pm 0.5$	$99.4 \pm 0.1$	$60.4\pm0.5$	$99.4 \pm 0.1$
MCDD	$46.0 \pm 0.0$	40.2 ± 0.0	46.2 ± 0.0	$42.8 \pm 0.0$	$48.8 \pm 0.0$	66.4 ± 0.0	49.9 ± 0.0	$70.0 \pm 0.0$
O-GBDT DK	$52.0 \pm 0.2$ $48.4 \pm 0.8$	$79.4 \pm 0.4$ $57.7 \pm 1.4$	$51.5 \pm 0.2$ $48.8 \pm 0.8$	$77.6 \pm 0.5$ $63.3 \pm 1.1$	$48.4 \pm 0.2$ $50.2 \pm 0.9$	$66.7 \pm 0.8$ $77.2 \pm 0.7$	$62.8 \pm 0.1$ $60.5 \pm 1.5$	$100.0 \pm 0.0$ $100.0 \pm 0.0$
Multi Incremental	$49.3 \pm 0.0$ $35.6 \pm 2.8$	$98.0 \pm 0.0$ $48.3 \pm 1.3$	$49.4 \pm 0.0$ $36.3 \pm 2.9$	$98.1 \pm 0.0$ $54.4 \pm 1.5$	$49.5 \pm 0.0$ $37.7 \pm 3.2$	$98.3 \pm 0.0$ $76.0 \pm 0.3$	$49.5 \pm 0.0$ $43.6 \pm 4.0$	$98.3 \pm 0.0$ $100.0 \pm 0.0$
Energy+ Self Exposure	$60.8 \pm 1.6$ $58.8 \pm 0.5$ $60.3 \pm 0.7$	$99.0 \pm 0.0$ $97.4 \pm 0.1$ $95.0 \pm 0.4$	$60.9 \pm 1.6$ $59.4 \pm 0.7$ $60.9 \pm 0.7$	$99.1 \pm 0.0$ $98.0 \pm 0.2$ $95.5 \pm 0.4$	$60.9 \pm 1.6$ $58.9 \pm 0.7$ $61.5 \pm 0.8$	$99.1 \pm 0.0$ $97.5 \pm 0.3$ $95.6 \pm 0.6$	$60.9 \pm 1.6$ $60.1 \pm 0.8$ $64.7 \pm 0.7$	$99.1 \pm 0.0$ $98.5 \pm 0.3$ $99.0 \pm 0.0$
POEM WOODS	$55.1 \pm 0.0$ $46.0 \pm 0.5$	$91.0 \pm 0.0$ $13.3 \pm 13.3$	$56.8 \pm 0.0$ $46.5 \pm 0.5$ $44.0 \pm 1.0$	$94.1 \pm 0.0$ $14.6 \pm 14.6$	$58.8 \pm 0.0$ $47.4 \pm 1.2$	$96.5 \pm 0.0$ $18.5 \pm 18.5$ $13.7 \pm 3.8$	$61.4 \pm 0.0$ $48.5 \pm 1.8$ $42.8 \pm 1.6$	$99.1 \pm 0.0$ $19.8 \pm 19.8$
Logitnorm VOS	$44.3 \pm 1.0$ $45.3 \pm 0.0$	$9.8 \pm 2.8$ $5.2 \pm 0.0$	$44.0 \pm 1.0$ $45.6 \pm 0.0$	$10.7 \pm 3.1$ $4.4 \pm 0.0$	$42.6 \pm 1.3$ $45.5 \pm 0.0$	$13.7 \pm 3.8$ $4.3 \pm 0.0$	$42.8 \pm 1.6$ $47.4 \pm 0.0$	$7.3 \pm 3.6$ $0.1 \pm 0.0$
ReAct Energy Confidence	$42.8 \pm 1.3$ $41.4 \pm 0.8$ $41.1 \pm 0.3$	$9.5 \pm 5.8$ $11.0 \pm 5.5$ $2.1 \pm 0.6$	$42.5 \pm 1.3$ $41.1 \pm 0.9$ $40.6 \pm 0.3$	$10.4 \pm 6.5$ $11.8 \pm 5.9$ $2.4 \pm 0.6$	$41.5 \pm 1.2$ $40.2 \pm 0.7$ $39.8 \pm 0.2$	$9.8 \pm 6.5$ $10.2 \pm 5.2$ $1.7 \pm 0.2$	$42.2 \pm 1.7$ $41.2 \pm 0.9$ $40.5 \pm 0.2$	$10.4 \pm 9.4$ $11.2 \pm 6.2$ $0.7 \pm 0.2$
Original	$41.1 \pm 0.5$	$0.0 \pm 0.0$	$40.7 \pm 0.5$	$0.0 \pm 0.0$	$40.0 \pm 0.4$	$0.0 \pm 0.0$	$40.4 \pm 0.7$	$0.0 \pm 0.0$

Table 13. Detailed results for the Heloc dataset in Test settings II.

Method	$T_1$		$T_2$		$T_3$		$T_4$	
Wicthou	Actual	OOD	Actual	OOD	Actual	OOD	Actual	OOD
Pipeline	$72.6 \pm 0.1$	$98.8 \pm 0.0$						
OCT	$70.5 \pm 0.2$	$97.2 \pm 0.1$	$70.7 \pm 0.3$	$97.5 \pm 0.2$	$70.8 \pm 0.3$	$97.6 \pm 0.2$	$70.7 \pm 0.3$	$97.5 \pm 0.2$
MCDD O-GBDT DK Multi Incremental	$52.5 \pm 0.0$ $65.2 \pm 0.3$ $51.5 \pm 0.4$ $69.0 \pm 0.0$ $26.0 \pm 2.8$	$46.0 \pm 0.0$ $67.5 \pm 0.7$ $14.9 \pm 0.7$ $97.1 \pm 0.0$ $10.6 \pm 0.2$	$52.5 \pm 0.0$ $65.3 \pm 0.3$ $51.8 \pm 0.4$ $69.0 \pm 0.0$ $26.1 \pm 2.8$	$46.8 \pm 0.0$ $68.2 \pm 0.6$ $16.1 \pm 0.8$ $97.2 \pm 0.0$ $11.8 \pm 0.2$	$57.9 \pm 0.0$ $65.4 \pm 0.3$ $59.3 \pm 0.4$ $69.1 \pm 0.0$ $30.4 \pm 2.8$	$72.0 \pm 0.0$ $68.5 \pm 0.7$ $65.5 \pm 1.7$ $97.3 \pm 0.0$ $57.9 \pm 0.2$	$60.0 \pm 0.0$ $80.6 \pm 0.1$ $73.1 \pm 0.3$ $69.1 \pm 0.0$ $39.0 \pm 3.3$	$78.0 \pm 0.0$ $99.9 \pm 0.0$ $100.0 \pm 0.0$ $97.3 \pm 0.0$ $100.0 \pm 0.0$
Energy+ Self Exposure	$70.6 \pm 0.2$ $70.8 \pm 0.3$ $55.2 \pm 0.6$	$97.3 \pm 0.1$ $97.1 \pm 0.1$ $44.3 \pm 5.6$	$71.1 \pm 0.3$ $71.2 \pm 0.3$ $55.5 \pm 0.6$	$98.0 \pm 0.0$ $97.7 \pm 0.1$ $45.4 \pm 5.6$	$71.3 \pm 0.3$ $71.5 \pm 0.3$ $55.0 \pm 1.0$	$98.3 \pm 0.1$ $98.1 \pm 0.0$ $40.1 \pm 6.0$	$71.3 \pm 0.3$ $71.5 \pm 0.3$ $54.4 \pm 0.5$	$98.3 \pm 0.1$ $98.1 \pm 0.0$ $19.4 \pm 8.8$
POEM WOODS Logitnorm VOS ReAct Energy Confidence	$57.9 \pm 0.0$ $30.3 \pm 4.4$ $49.3 \pm 1.9$ $49.5 \pm 0.0$ $50.5 \pm 0.4$ $50.9 \pm 0.2$ $50.0 \pm 0.3$	$68.2 \pm 0.0$ $55.2 \pm 2.7$ $20.0 \pm 3.8$ $11.5 \pm 0.0$ $7.3 \pm 0.5$ $8.7 \pm 1.0$ $3.8 \pm 0.2$	$57.8 \pm 0.0$ $30.4 \pm 4.4$ $49.4 \pm 1.9$ $49.7 \pm 0.0$ $50.6 \pm 0.3$ $51.1 \pm 0.2$ $50.2 \pm 0.3$	$68.0 \pm 0.0$ $55.7 \pm 3.0$ $19.4 \pm 4.0$ $14.3 \pm 0.0$ $6.9 \pm 0.8$ $8.6 \pm 1.3$ $4.0 \pm 0.2$	$67.3 \pm 0.0$ $37.1 \pm 4.8$ $52.0 \pm 2.1$ $50.8 \pm 0.0$ $52.2 \pm 0.4$ $52.8 \pm 0.2$ $51.0 \pm 0.3$	$92.4 \pm 0.0$ $89.6 \pm 0.9$ $30.7 \pm 8.3$ $17.3 \pm 0.0$ $7.5 \pm 0.6$ $9.1 \pm 2.1$ $2.5 \pm 0.2$	$71.4 \pm 0.0$ $40.7 \pm 5.0$ $54.9 \pm 1.6$ $53.8 \pm 0.0$ $54.0 \pm 0.6$ $54.8 \pm 0.3$ $53.9 \pm 0.4$	$98.8 \pm 0.0$ $98.9 \pm 0.0$ $37.9 \pm 16.0$ $2.3 \pm 0.0$ $3.1 \pm 2.7$ $5.7 \pm 5.1$ $1.8 \pm 0.9$
Original	$50.7 \pm 0.2$	$0.0 \pm 0.0$	$50.9 \pm 0.2$	$0.0 \pm 0.0$	$52.5 \pm 0.2$	$0.0 \pm 0.0$	$55.0 \pm 0.1$	$0.0 \pm 0.0$

Table 14. Detailed results for the Jannis dataset in Test settings II. DK could not be applied to this dataset due to huge memory requirement.

Method	$T_1$		$T_2$		$T_3$		$T_4$	
Welloa	Actual	OOD	Actual	OOD	Actual	OOD	Actual	OOD
Pipeline	$50.8 \pm 0.2$	$99.0 \pm 0.0$						
OCT	$45.0 \pm 0.4$	$93.7 \pm 0.6$	$45.0 \pm 0.4$	$93.8 \pm 0.6$	$45.0 \pm 0.4$	$93.8 \pm 0.6$	$45.0 \pm 0.4$	$93.8 \pm 0.6$
MCDD O-GBDT DK Multi Incremental	$31.2 \pm 0.1$ $49.4 \pm 0.1$ - $36.8 \pm 0.2$ $12.1 \pm 0.7$	$6.6 \pm 0.4$ $90.1 \pm 0.2$ $-$ $88.2 \pm 0.4$ $0.3 \pm 0.0$	$31.3 \pm 0.1$ $51.2 \pm 0.1$ - $38.9 \pm 0.1$ $12.2 \pm 0.7$	$7.2 \pm 0.5$ $95.2 \pm 0.1$ - $95.2 \pm 0.2$ $0.5 \pm 0.0$	$34.2 \pm 0.2$ $53.0 \pm 0.2$ - $40.4 \pm 0.1$ $15.4 \pm 0.8$	$37.5 \pm 1.3$ $99.7 \pm 0.0$ - $99.5 \pm 0.0$ $60.5 \pm 0.4$	$33.2 \pm 0.2$ $53.1 \pm 0.2$ - $40.4 \pm 0.1$ $18.9 \pm 1.0$	$28.4 \pm 1.8$ $100.0 \pm 0.0$ - $99.5 \pm 0.0$ $99.9 \pm 0.0$
Energy+ Self Exposure	$47.2 \pm 0.7$ $37.8 \pm 2.2$ $42.9 \pm 0.5$	$97.2 \pm 0.2$ $92.1 \pm 1.7$ $66.3 \pm 2.3$	$47.9 \pm 0.6$ $38.0 \pm 2.2$ $44.7 \pm 0.7$	$98.8 \pm 0.0$ $92.7 \pm 1.7$ $74.0 \pm 2.4$	$48.0 \pm 0.6$ $38.2 \pm 2.2$ $48.3 \pm 0.9$	$98.9 \pm 0.0$ $93.0 \pm 1.6$ $83.8 \pm 3.0$	$48.0 \pm 0.6$ $38.2 \pm 2.2$ $49.1 \pm 0.8$	$98.9 \pm 0.0$ $93.0 \pm 1.6$ $85.0 \pm 3.4$
POEM WOODS Logitnorm VOS ReAct Energy Confidence	$29.8 \pm 0.7$ $34.3 \pm 0.2$ $34.4 \pm 0.2$ $31.9 \pm 0.1$ $33.8 \pm 0.2$ $34.4 \pm 0.1$ $34.8 \pm 0.1$	$19.0 \pm 0.3$ $11.9 \pm 1.3$ $2.8 \pm 0.1$ $5.4 \pm 0.1$ $4.6 \pm 0.4$ $4.5 \pm 0.3$ $4.6 \pm 0.5$	$30.1 \pm 0.7$ $34.4 \pm 0.3$ $34.4 \pm 0.2$ $31.9 \pm 0.1$ $33.9 \pm 0.2$ $34.5 \pm 0.1$ $34.9 \pm 0.1$	$23.2 \pm 0.3$ $14.2 \pm 1.6$ $2.7 \pm 0.1$ $5.7 \pm 0.1$ $4.7 \pm 0.5$ $4.7 \pm 0.4$ $4.7 \pm 0.6$	$39.0 \pm 1.0$ $41.2 \pm 1.1$ $35.6 \pm 0.3$ $32.0 \pm 0.1$ $35.3 \pm 0.3$ $35.9 \pm 0.2$ $36.1 \pm 0.3$	$87.8 \pm 0.0$ $54.1 \pm 8.0$ $0.8 \pm 0.1$ $4.5 \pm 0.2$ $6.1 \pm 1.6$ $4.3 \pm 0.7$ $5.8 \pm 1.9$	$43.5 \pm 1.1$ $46.3 \pm 1.3$ $37.4 \pm 0.3$ $32.9 \pm 0.2$ $36.9 \pm 0.4$ $38.0 \pm 0.3$ $38.0 \pm 0.4$	$99.0 \pm 0.0$ $63.4 \pm 9.7$ $0.4 \pm 0.1$ $2.6 \pm 0.3$ $5.0 \pm 1.9$ $2.9 \pm 0.8$ $5.7 \pm 1.7$
Original	$34.4 \pm 0.1$	$0.0 \pm 0.0$	$34.5 \pm 0.1$	$0.0 \pm 0.0$	$35.8 \pm 0.2$	$0.0 \pm 0.0$	$38.0 \pm 0.3$	$0.0 \pm 0.0$

 $Table\ 15.\ Detailed\ counterfactual\ experiment\ results\ including\ standard\ errors.$ 

	cf alg.	classifier	success rate ↑	valid rate ↑	numerical cost ↓	categorical cost ↓
Adult	GD	Original DK OCT	$100.0 \pm 0.0$ $100.0 \pm 0.0$ $99.8 \pm 0.1$	$90.8 \pm 0.8$ $84.3 \pm 0.5$ $99.4 \pm 0.2$	$5.0 \pm 0.2$ $4.9 \pm 0.1$ $7.5 \pm 0.4$	$22.9 \pm 0.1$ $0.9 \pm 0.2$ $12.2 \pm 2.8$
	GS	Original DK OCT	$100.0 \pm 0.0$ $100.0 \pm 0.0$ $100.0 \pm 0.0$	$74.8 \pm 1.1$ $88.8 \pm 5.0$ $100.0 \pm 0.0$	$4.3 \pm 0.1$ $4.1 \pm 0.1$ $4.5 \pm 0.1$	$26.7 \pm 1.4$ $26.9 \pm 0.8$ $29.1 \pm 1.1$
	CCHVAE	Original DK OCT	$100.0 \pm 0.0$ $100.0 \pm 0.0$ $100.0 \pm 0.0$	$99.8 \pm 0.1$ $99.2 \pm 0.3$ $100.0 \pm 0.0$	$16.7 \pm 0.1$ $16.9 \pm 0.2$ $17.1 \pm 0.1$	$19.4 \pm 1.4$ $22.1 \pm 1.7$ $21.8 \pm 1.8$
	Revise	Original DK OCT	$99.9 \pm 0.1$ $100.0 \pm 0.0$ $99.9 \pm 0.1$	$98.2 \pm 0.5$ $99.2 \pm 0.2$ $99.9 \pm 0.1$	$16.1 \pm 0.5$ $15.9 \pm 0.2$ $16.0 \pm 0.7$	$13.6 \pm 1.1$ $15.7 \pm 2.1$ $21.9 \pm 1.6$
Compas	GD	Original DK OCT	$100.0 \pm 0.0$ $100.0 \pm 0.0$ $99.7 \pm 0.2$	83.7 ± 1.2 90.1 ± 1.1 99.4 ± 0.4	$21.4 \pm 1.4$ $20.7 \pm 0.8$ $20.3 \pm 0.8$	$55.1 \pm 0.4$ $4.9 \pm 4.2$ $31.0 \pm 2.0$
	GS	Original DK OCT	$100.0 \pm 0.0$ $100.0 \pm 0.0$ $100.0 \pm 0.0$	$77.5 \pm 2.1$ $79.2 \pm 4.7$ $99.9 \pm 0.1$	$10.6 \pm 0.6$ $12.4 \pm 0.5$ $14.3 \pm 1.0$	$61.4 \pm 1.6$ $67.3 \pm 2.9$ $63.0 \pm 2.2$
	CCHVAE	Original DK OCT	$100.0 \pm 0.0$ $100.0 \pm 0.0$ $100.0 \pm 0.0$	$100.0 \pm 0.0$ $93.7 \pm 6.3$ $100.0 \pm 0.0$	$27.7 \pm 0.4$ $28.2 \pm 0.5$ $26.5 \pm 0.2$	$21.2 \pm 5.1$ $31.1 \pm 13.2$ $14.1 \pm 3.0$
	Revise	Original DK OCT	$93.8 \pm 6.0$ $99.9 \pm 0.1$ $99.9 \pm 0.1$	$93.8 \pm 6.0$ $99.9 \pm 0.1$ $99.9 \pm 0.1$	$28.8 \pm 0.2$ $33.4 \pm 2.4$ $32.0 \pm 1.9$	$9.1 \pm 1.2$ $14.4 \pm 4.6$ $10.0 \pm 1.2$
GMSC	GD	Original DK OCT	$100.0 \pm 0.0$ $99.9 \pm 0.1$ $90.4 \pm 2.9$	$88.0 \pm 3.3$ $97.8 \pm 0.9$ $90.4 \pm 2.9$	$18.1 \pm 0.4$ $18.0 \pm 0.5$ $18.5 \pm 0.7$	- - -
	GS	Original DK OCT	$100.0 \pm 0.0$ $99.6 \pm 0.1$ $99.4 \pm 0.0$	$67.0 \pm 2.9$ $78.3 \pm 11.4$ $99.4 \pm 0.1$	$12.4 \pm 0.4$ $15.1 \pm 0.7$ $16.0 \pm 0.5$	- - -
	CCHVAE	Original DK OCT	$100.0 \pm 0.0$ $100.0 \pm 0.0$ $100.0 \pm 0.0$	$100.0 \pm 0.0$ $99.9 \pm 0.1$ $100.0 \pm 0.0$	$15.6 \pm 0.2$ $15.6 \pm 0.3$ $15.8 \pm 0.2$	- - -
	Revise	Original DK OCT	$100.0 \pm 0.0$ $100.0 \pm 0.0$ $99.2 \pm 0.3$	$100.0 \pm 0.0$ $100.0 \pm 0.0$ $99.2 \pm 0.3$	$18.6 \pm 0.3$ $18.9 \pm 0.2$ $18.2 \pm 0.3$	- - -
Heloc	GD	Original DK OCT	$100.0 \pm 0.0$ $100.0 \pm 0.0$ $99.6 \pm 0.3$	$93.6 \pm 2.0$ $92.2 \pm 1.7$ $99.5 \pm 0.2$	$11.8 \pm 0.1$ $11.3 \pm 0.3$ $12.9 \pm 0.4$	- - -
	GS	Original DK OCT	$100.0 \pm 0.0$ $100.0 \pm 0.0$ $99.8 \pm 0.1$	96.6 ± 0.5 96.4 ± 1.2 99.4 ± 0.1	$12.5 \pm 0.3$ $12.9 \pm 0.4$ $12.4 \pm 0.8$	- - -
	CCHVAE	Original DK OCT	$100.0 \pm 0.0$ $100.0 \pm 0.0$ $100.0 \pm 0.0$	$100.0 \pm 0.0$ $100.0 \pm 0.0$ $100.0 \pm 0.0$	$22.9 \pm 0.2$ $22.4 \pm 0.1$ $22.7 \pm 0.3$	- - -
	Revise	Original DK OCT	$100.0 \pm 0.0$ $97.4 \pm 2.2$ $96.9 \pm 2.6$	$100.0 \pm 0.0$ $97.4 \pm 2.2$ $96.9 \pm 2.6$	$23.1 \pm 0.2$ $21.7 \pm 0.3$ $22.5 \pm 0.3$	- - -