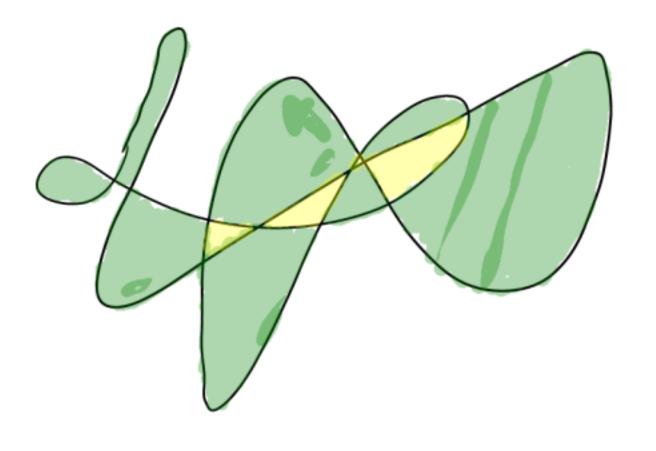
CS ZZZ5

Midterm Z

Review Session

Welcome



# University of Illinois at Urbana-Champaign Department of Computer Science

# Second Examination

CS 225 Data Structures and Software Principles Fall 2010 7p-9p, Tuesday, November 2

Name:
NetID:
Lab Section (Day/Time):

- This is a closed book and closed notes exam. No electronic aids are allowed, either.
- You should have 5 problems total on 15 pages. The last sheet is scratch paper; you may
  detach it while taking the exam, but must turn it in with the exam when you leave. Use
  scantron forms for Problems 1 and 2.
- Unless otherwise stated in a problem, assume the best possible design of a particular implementation is being used.
- Unless the problem specifically says otherwise, (1) assume the code compiles, and thus any
  compiler error is an exam typo (though hopefully there are not any typos), and (2) assume
  you are NOT allowed to write any helper methods to help solve the problem, nor are you
  allowed to use additional arrays, lists, or other collection data structures unless we have said
  you can.
- We will be grading your code by first reading your comments to see if your plan is good, and then reading the code to make sure it does exactly what the comments promise. In general, complete and accurate comments will be worth approximately 30% of the points on any coding problem.
- Please put your name at the top of each page.

Problem	Points	Score	Grader
1	20		scantron
2	25		scantron
3	30		
4	15		
5	10		
Total	100		

### [Miscellaneous – 20 points].

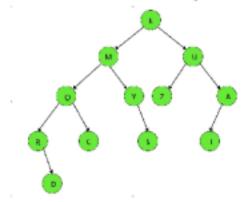
# MC1 (2.5pts)

Which of the following is not a reasonable choice for implementing the Dictionary Abstract Data Type?

- (a) AVL Tree
- (b) B-Tree
- (c) Binary Search Tree
- (d) Stack
- (e) All of these are reasonable choices for implementing a Dictionary.

# MC2 (2.5pts)

Suppose we do a level order traversal of the following binary tree. What is the maximum number of non-null nodes on the queue at one time in the execution of the algorithm?



- (a) 4
- (b) 5
- (c) 6
- (d) 12
- (e) None of these is the correct number.

# MC3 (2.5pts)

Suppose we implement a stack using a dynamically allocated array. If the array fills, we are faced with a dilemma. From among the following choices, select the one that best describes our strategy for handling a filled array.

- (a) We declare a new array, twice as big as the original, and copy the data into the new space for a total cost of O(n), over a sequence of n pushes.
- (b) We declare another array and keep track of which of the two (or more) arrays contain the current top of the stack in a private member of the stack class. This costs us O(1) per push.
- (c) For some fixed k, we create a new array of size n + 2<sup>k</sup> and copy the data into the new space for an average cost of O(1) per push operation.
- (d) We avoid implementing a stack using a dynamically allocated array, because it is inefficient to have to reallocate memory.
- (e) None of these answers is a reasonable response.

# MC4 (2.5pts) Consider the following partial C++ code: #include <vector> #include <iostrean> using namespace std; template <class Iter, class Formatter> void mystery (Iter front, Iter end, Formatter doSomething) { } template <class T> class dunno { public: void operator()(T & a, T & b) { a = a + b;7 int main() { // insert an odd number of elements in vector<int>::iterator it1 = v.begin(); westery 2 Iter, Fundars vector<int>::iterator it2 = v.end();

If you assume that all iterators are bi-directional and non-constant, which of the following statements is true?

(a) This code does not compile because of a type mismatch in the nystery parameter list. (b) This code does not compile because of a syntax error in the template instantiation for mystery.

If the vector consists of the integers 1, 2, 3, 4, 5, 6, 7 in that order, with the first item on the left, then the output is 1, 2, 3, 4, 5, 6, 7. (i.e. the code does not change the vector.)

If the vector consists of the integers 1, 2, 3, 4, 5, 6, 7 in that order, with the first item on the left, then the output is 8, 8, 8, 4, 5, 6, 7.

(e) None of these options describes the behavior of this code.

mystery<vector<int>::iterator,dunno<int>

for (int i = 0; i < v.size(); i++) cout << v[i] << endl;

it2-

dunmo<int> d;

return 0; }

leftrotate right Left Rotate right Rotate left Right Rotate

loft Right Robbe

iter of ors;

\*
++; --;
!-

arr = new in [4]

for lintizo; i!=4; i++)

arr[i] = 7;

arr[4] X

# MC5 (2.5pts)

What is the real name of mysteryFunction? Note that in context, t->right will not be null.

void nysteryFunction(treeNode \* & t) {
 treeNode \* y = t->right;
 t->right = y->left;
 y->left = t;
 y->height = max( height(y->right), height(y->left)) + 1;
 t->height = max( height(t->right), height(t->left)) + 1;
 t = y;
}

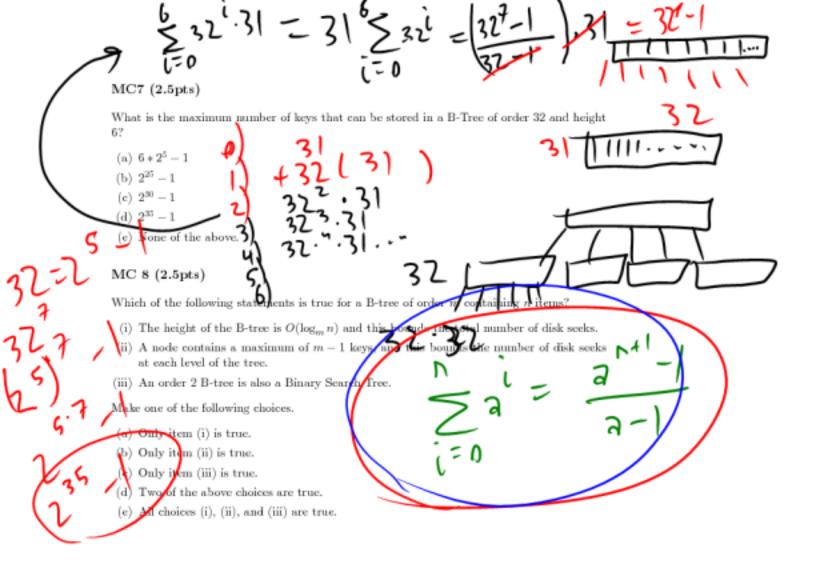
(a) leftRotate
(b) rightRotate
(c) rightLeftRotate
(d) leftRightRotate

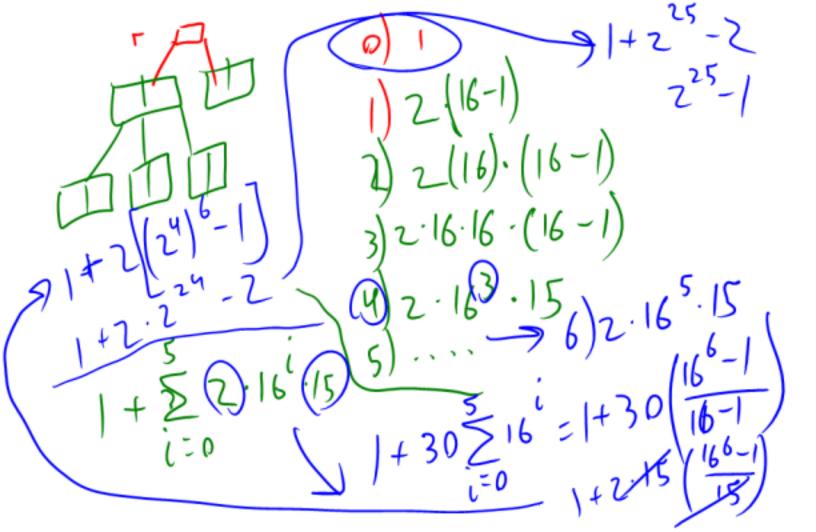
### MC6 (2.5pts)

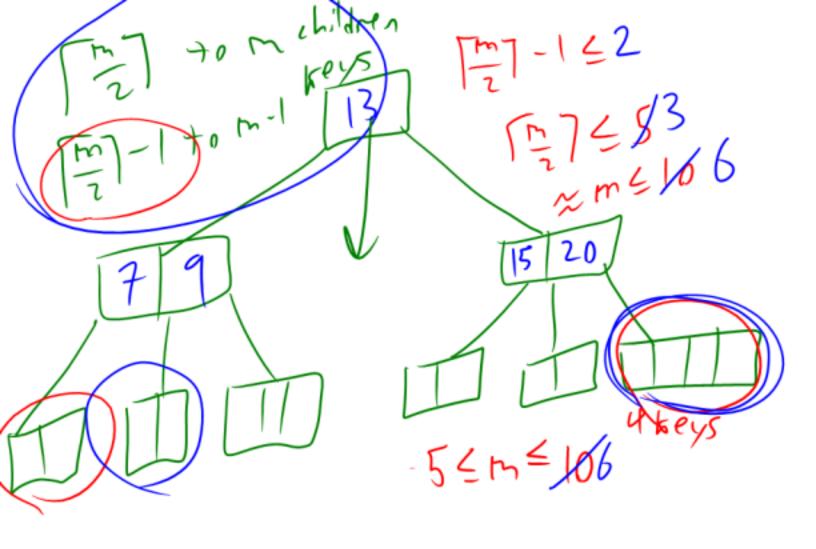
Consider the Binary Search Tree built by inserting the following sequence of integers, one at a time: 5, 4, 7, 9, 8, 6, 2, 3, 1. If the node containing 5 were removed from the tree, what would be the right child of the node containing 2?

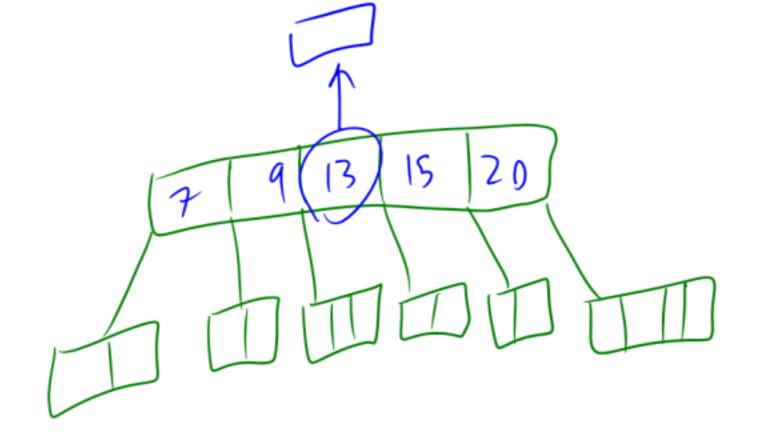
- (a) Null
- (b) The node containing 3.
- (c) The node containing 4.
- (d) The node containing 6.
- (e) None of these answers is correct.

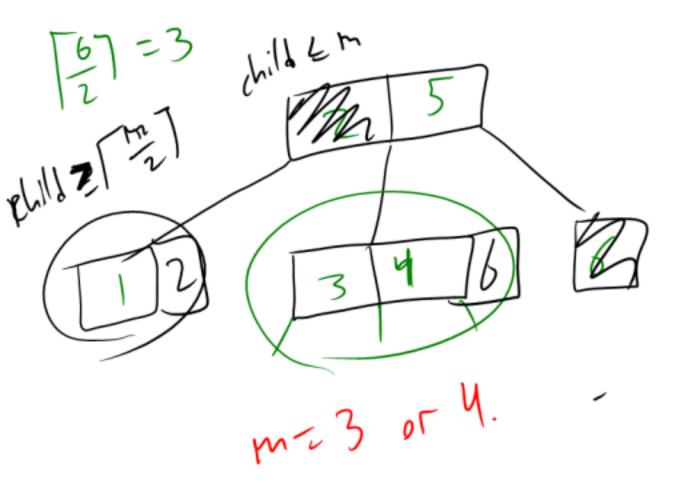
(e) None of these choices are correct.







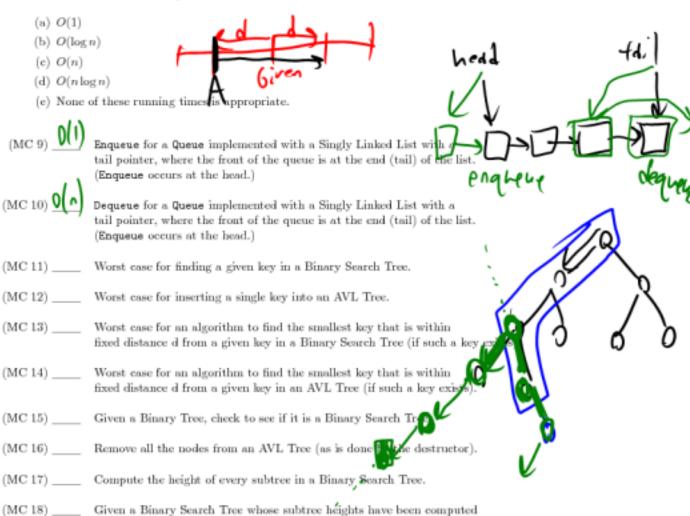


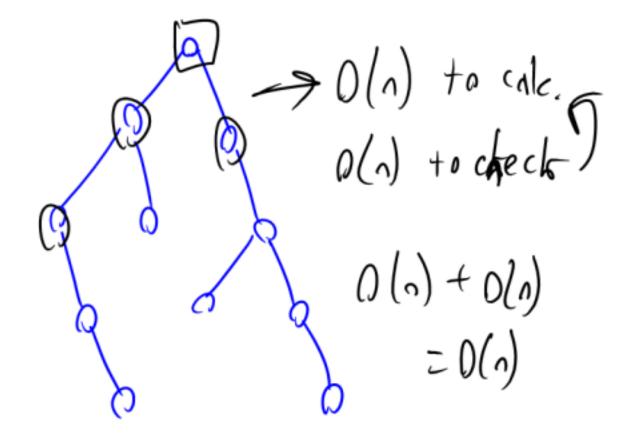


#### [Efficiency – 25 points].

Each item below is a description of a data structure, its implementation, and an operation on the structure. In each case, choose the appropriate running time from the list below. The variable n represents the number of items (keys, data, or key/data pairs) in the structure. In answering this question you should assume the best possible implementation given the constraints, and also assume that every array is sufficiently large to handle all items. Please use the scantron sheets for your answers.

determine if the Binary Search Tree is an AVL Tree.





height(T)= \ \ -1 if empty

mu(height(L))

height(R)) \( + \) height (T)
{

Tetwn

#### [Quadtrees – 30 points].

For this question, consider the following partial class definition for the Quadtree class, which uses a quadtree to represent a d-by-d square bitmap image as in MP5. As a simplifying assumption for this problem, you may assume that only leaf nodes contain valid RGBApixel elements, and that the element field in all non-leaf nodes is not initialized to any particular value (we will not be doing any pruning of this tree, though it may already have been pruned). Just as in MP5, you may assume that d is a power of 2.

```
class Quadtree
  public:
    // constructors and destructor; all of the public methods from MP5, including:
   void buildTree(BMP const & source, int newResolution);
   RGBApixel getPixel(int x, int y) const;
   BMP decompress() comst;
   void clockwiseRotate(); // 90 degree turn to the right
   void prume(int tolerance);
   int pruneSize(int tolerance) const;
   int idealPrune(int numLeaves) const;
  private:
     struct QuadtreeNode {
        QuadtreeNode* mwChild; // pointer to northwest child
        QuadtreeNode* meChild; // pointer to northeast child
        QuadtreeNode* swChild; // pointer to southwest child
        QuadtreeNode* seChild; // pointer to southeast child
        RGBApixel element; // the pixel stored as this node's "data"
        QuadtreeNode(RGBApixel const & elem);
        QuadtreeNode();
    }:
                            // ptr to root of quadtree, NULL if tree is empty.
     QuadtreeNode* root;
     int resolution; // number of pixels on a side of the image (assume 2 k)
     void copy(QuadtreeNode *& firstNode, QuadtreeNode * secondNode);
     void clear(QuadtreeNode *& curNode);
     // plus many helper functions of your own design
Э;
```

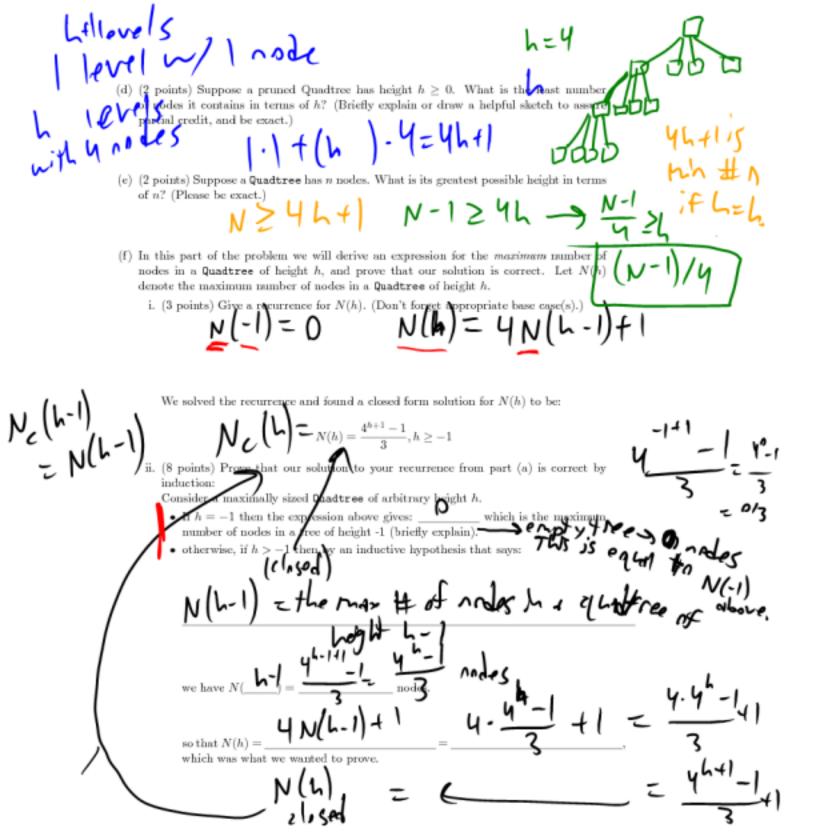
You may assume that each child pointer in a new QuadtreeNode is NULL, and that the Quadtree has been accurately constructed so that the resolution is set. (a) (3 points) Write the getPixel function declared in the public section above. This function takes two arguments,x and y, in that order, both nonnegative integers. It returns the RGBApixel corresponding to the pixel at coordinates (x, y) in the bitmap image which the quadtree represents (where (0,0) is in the upper left corner of the image). Note that the quadtree may not contain a node specifically corresponding to this pixel since the tree may have been pruned. In this case, getPixel retrieves the pixel (i.e. the color) of the smallest square region within which point (x, y) would lie. If the supplied coordinates fall outside of the bounds of the underlying bitmap, or if the current Quadtree is "empty" then the returned RGBApixel should be the one which is created by the default RGBApixel constructor. Write the function as it would appear in the quadtree.cpp file for the Quadtree class. (Note: part (b) of this problem asks you to write a helper function that you may call here.)

	::
-{	

}

(b)	function than ou	ts) Write the private helper function that actually does the work for the getPixel a in part (a). (Note that if your approach to this problem is markedly different ars, just write your solution on the back of the previous page. Your entire solution
	to getP	'ixel will then be graded out of ten points.)
	-{	
	}	
(c)	(5 poin	ts) Analyze and give a tight asymptotic bound on the running time of your

(c) (5 points) Analyze and give a tight asymptotic bound on the running time of your implementation for part (b). Your bound should be stated in terms of d, the number of pixels in the width (or height) of the original image represented by the Quadtree. Briefly justify your answer.



# 4. [AVL Trees - 15 points].

Parts (a) through (e) below refer to this AVL Tree: (Note that no part is dependent on any other-each operation is performed on the original tree.)



- (a) (3 points) If key 15 is inserted into the tree, the result will be a \_\_\_\_\_\_\_\_ rotation about the node containing key \_\_\_\_\_\_\_.
- (b) (3 points) If keys 0 and 1 are inserted into the tree, in that order, the result will be a rotation about the node containing key \_\_\_\_\_\_.
- (c) (3 points) If key 10 is removed from the tree, the result will be a left Right rotation about the node containing key \_\_\_\_\_\_.
- (d) (3 points) Name a key, that when removed results in a right rotation:
- (e) (3 points) Name a key that when removed results in a right-left rotation, followed by a right rotation: \_\_\_\_\_\_\_.

Fight Rotote (Node &c)

Node \* B= C>left

Node \* B= B>left Node \* A = B->left; Node \* +Ne2 = B->right B > right = C; C = B; C = B;

Pert Right Rotate (Node \*8c)

North Rotate (C> loft).

right Rotate (C) reft Right Robble (Node \* & C) Note \* B= A sigh Nade + + 3 = B -> 19h C=B)

#### [Tricky – 10 points].

Here are the Stack and Queue class definitions you used in MP4:

```
template<class T> class Stack {
public:
    void push(T const & newItem); // adds new item to top of stack
    T pop(); // removes top item from the stack and returns its value
    T peek() const; // returns value of top item on stack, but does not remove
    bool isEmpty() const; // returns true if stack is empty, false o/w
private: ... // not relevant here
};

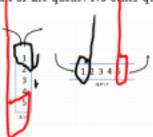
template<class T> class Queue {
    public:
        void enqueue(T const & newItem); // adds new item to back of queue
        T dequeue(); // removes front item from the queue and returns its value
        T peek() const; // returns value of front item on queue, but does not remove
        bool isEmpty() const; // returns true if queue is empty, false o/w
private: ... // not relevant here
};
```

Write the recursive function verifySame whose function prototype is below. The function should return true if the parameter stack and queue contain only elements of exactly the same values in exactly the same order, and false otherwise (see example below). You may assume the stack and queue contain the same number of items!

We're going to constrain your solution so as to make you think hard about solving it elegantly:

1) Your function may not use any loops; 2) In your function you may only declare ONE local boolean variable to use in your return statement, and you may only declare TWO local variables of parameterized type T to use however you wish-no other local variables can be used; and 3) After execution of verifySame, the stack and queue must be unchanged. Be sure to comment your code VERY well.

Example: This stack and queue are considered to be the same. Note that we match the bottom of the stack with the front of the queue. No other queue matches this stack.



Sum ( stack 5)

3 az S. Pop()

6 = sum(s)

5. push(a)

redurn a + b;

Verify Same (stacks, queue a)

Yop = s. popl); roturn false;

If (!verify Same(s, a)); s.push (+op);

Q. push (Q.popl)); s.push (+op);

Ye (a.front()) = top)

Ye (a.front()) = top)

Teturn false;

return (recuse worked = top);

Q. enqueue (front);

Return (recuse worked);

Q. enqueue (front);

Return (recuse worked);

template	class	T>	bool	verify:	Sane(St	ack <t></t>	ks,	Queue <t></t>	å q)	{
-										
-										
-										

scratch paper