Events A and B are independent if and only if

$$P(B|A) = P(B)$$
 $P(A|B) = P(A)$
 $P(A \cap B) = P(A) \cdot P(B)$

1. The probability that a randomly selected student at Anytown College owns a bicycle is 0.55, the probability that a student owns a car is 0.30, and the probability that a student owns both is 0.10. Are events {a student owns a bicycle} and {a student owns a car} independent?

Events A, B and C are independent if and only if

$$P(A \cap B) = P(A) \cdot P(B), \quad P(A \cap C) = P(A) \cdot P(C), \quad P(B \cap C) = P(B) \cdot P(C),$$

and $P(A \cap B \cap C) = P(A) \cdot P(B) \cdot P(C)$

- A girl is told by her boyfriend that she is "one in a billion." She has a dimple in her chin, probability $\frac{1}{100}$, eyes of different colors, probability $\frac{1}{1000}$, and is absolutely crazy about mathematics, probability $\frac{1}{10000}$.
- a) Do these events seem to be independent or dependent?
- b) Show why the girl is "one in a billion."

- 3. Bart and Nelson talked Milhouse into throwing water balloons at Principal Skinner. Suppose that Bart hits his target with probability 0.80, Nelson misses 25% of the time, and Milhouse hits the target half the time. Assume that their attempts are independent of each other.
- a) Find the probability that all of them will hit Principal Skinner.

b) Find the probability that exactly one of the boys will hit Principal Skinner.

c) Find the probability that at least one of the boys will hit Principal Skinner.

Idea: P(at least one of A_i occurs) = 1 - P(none of A_i occurs)

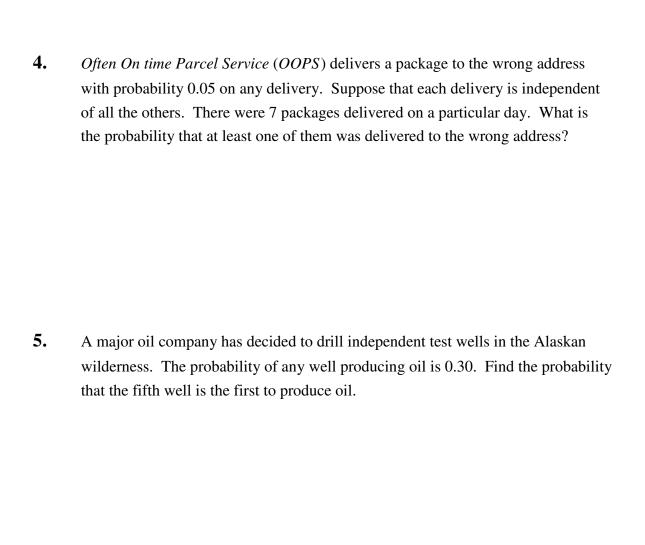
$$P(A_1 \text{ or } A_2 \text{ or ... or } A_n) = 1 - P((\text{not } A_1) \text{ and } (\text{not } A_2) \text{ and ... and } (\text{not } A_n))$$

$$P(A_1 \cup A_2 \cup ... \cup A_n) = 1 - P(A_1' \cap A_2' \cap ... \cap A_n')$$

For independent events

$$P(A_1 \text{ or } A_2 \text{ or } ... \text{ or } A_n) = 1 - P(\text{ not } A_1) \cdot P(\text{ not } A_2) \cdot ... \cdot P(\text{ not } A_n)$$

$$P(A_1 \cup A_2 \cup ... \cup A_n) = 1 - P(A_1') \cdot P(A_2') \cdot ... \cdot P(A_n')$$

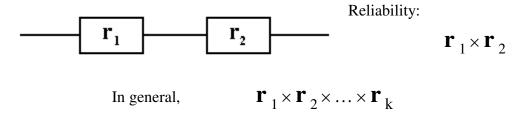


An automobile salesman thinks that the probability of making a sale is 0.30. If he talks to five customers on a particular day, what is the probability that

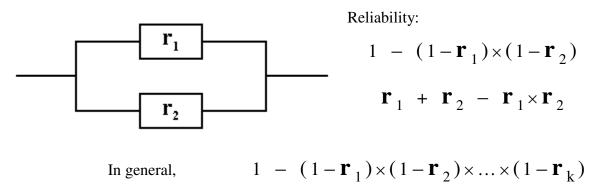
he will make exactly 2 sales? (Assume independence.)

6.

Series Connection:



<u>Parallel Connection</u>:



7. Compute the reliability of the following system of independent components (the numbers represent the reliability of each component):

