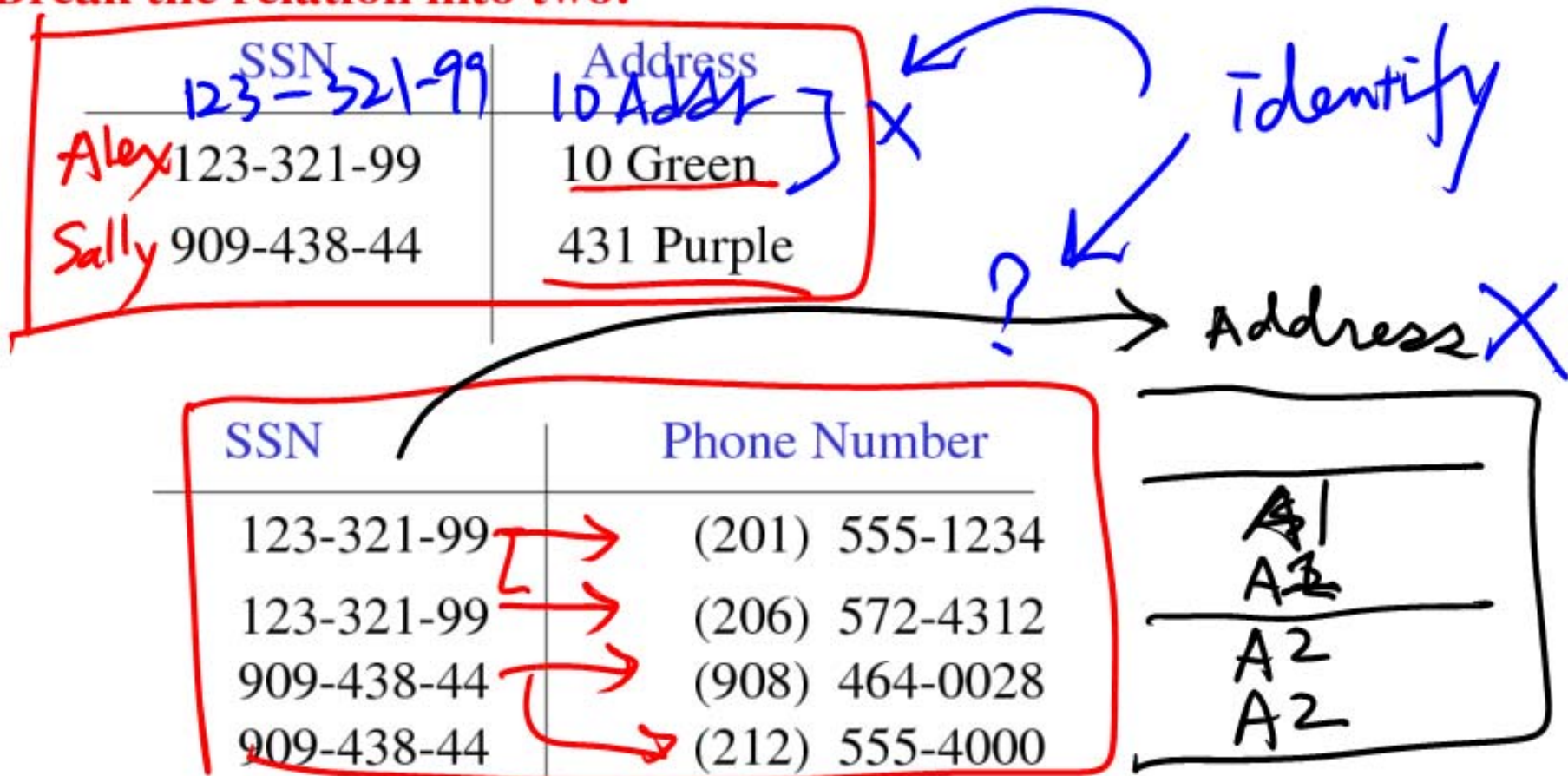


Better Designs Exist

Break the relation into two:



Reminder

Tutorial #2.

→ Today! 4:30-5:30pm
1302 SC.

P-Fun Topics?

— Translation ER to Rel. model.

— 10% { RAT



— Attr closure (today) — BCNF (tod.)
— F.D. closure (") — " " " "

Functional Dependencies

- A form of constraint (hence, part of the schema)
- Finding them is part of the database design
- Used heavily in schema refinement

Definition:

(SSN) Name Addr Phone

10 green

10 green

Name Address

If two tuples agree on the attributes

Name A_1, A_2, \dots, A_n

T_1 Alex ...

T_2 Alex ...

then they must also agree on the attributes

Address B_1, B_2, \dots, B_m

Formally: $A_1, A_2, \dots, A_n \longrightarrow B_1, B_2, \dots, B_m$

Examples

| <u>EmpID</u> | Name | Phone | Position |
|--------------|-------|-------------|-----------------|
| E0045 | Smith | <u>1234</u> | Clerk |
| E1847 | John | 9876 | <u>Salesrep</u> |
| E1111 | Smith | 9876 | <u>Salesrep</u> |
| E9999 | Mary | <u>1234</u> | <u>Lawyer</u> |

- EmpID → Name, Phone, Position
- Position → Phone
- but Phone ~~→~~ Position
1234 clerk, Lawyer

In General

- To check if $A \rightarrow B$ violation:

Erase all other columns

phone ← position

| | | | | |
|-----|-----|-----|-----|--|
| ... | A | ... | B | |
| | X1 | | Y1 | |
| | X2 | | Y2 | |
| | ... | | ... | |

one ← many / one

- check if the remaining relation is many-one
(called functional in mathematics)

Example

| EmplID | Name | Phone | Position |
|--------|-------|-------|------------|
| E0045 | Smith | 1234 | Clerk ✓ |
| E1847 | John | 9876 | Salesrep ✓ |
| E1111 | Smith | 9876 | Salesrep ✓ |
| E9999 | Mary | 1234 | lawyer ✓ |

More examples:

Product: name \rightarrow price, manufacturer

Person: ssn \rightarrow name, age

Company: name \rightarrow stock price, president

No violation
for Pos \rightarrow Phone

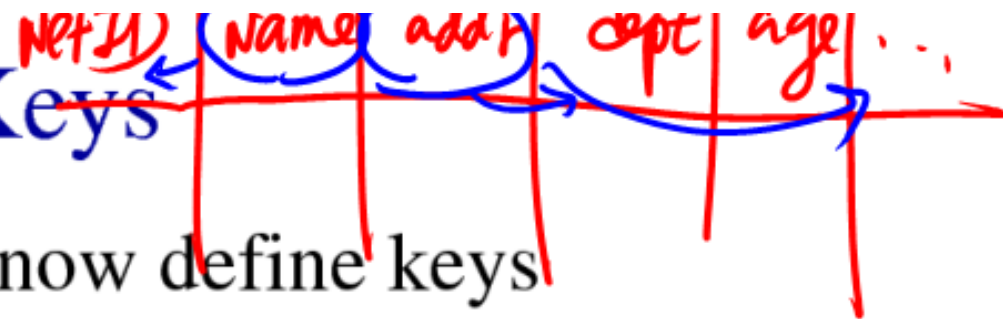
Q: From this, can you conclude phone \rightarrow SSN?

a phone is only used by
ONE person.

| SSN // | | Phone Number // |
|-------------------|----------------|-----------------|
| 123-321-99 | Alex | (201) 555-1234 |
| 123-321-99 | Alex | (206) 572-4312 |
| 909-438-44 | | (908) 464-0028 |
| 909-438-44 | | (212) 555-4000 |
| <u>123-321-88</u> | Alex Junior | (201) 555-1234 |

F.D. stated at schema design
 \Rightarrow assertion

Relation Keys



- After defining FDs, we can now define keys

- Key of a relation R is a set of attributes that

- functionally determines all attributes of R

$\{N, A\} \rightarrow \{NetID, dept, age, \dots\}$

- none of its subsets determines all attributes of R

- Superkey

- a set of attributes that contains a key

- We will need to know the keys of the relations in a DB schema, so that we can refine the schema

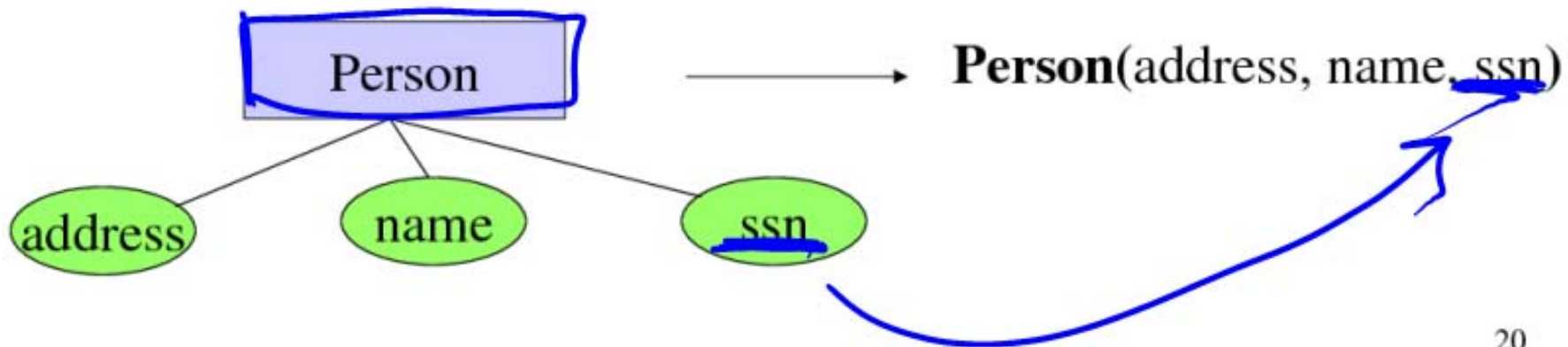
| | (name, Addr) | (NetID) | (NetID, dept) |
|-------|--------------|---------|---------------|
| key | ✓ | ✓ | ✗ |
| s-key | ✓ | ✓ | ✓ |

Finding the Keys of a Relation

Given a relation constructed from an E/R diagram, what is its key?

Rules:

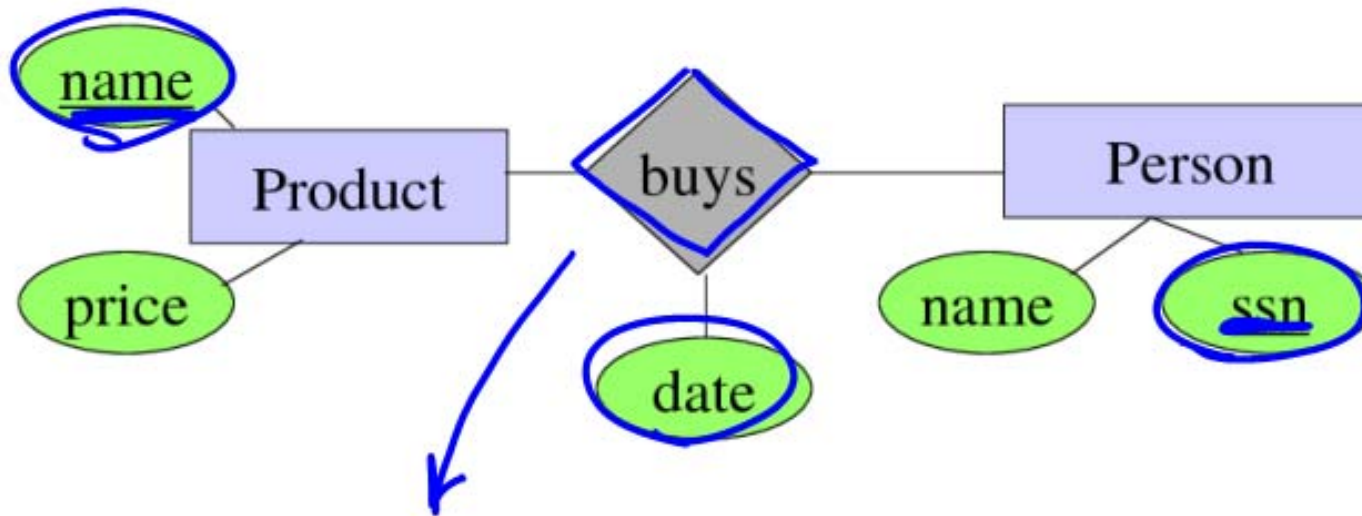
1. If the relation comes from an entity set, the key of the relation is the set of attributes which is the key of the entity set.



Finding the Keys

Rules:

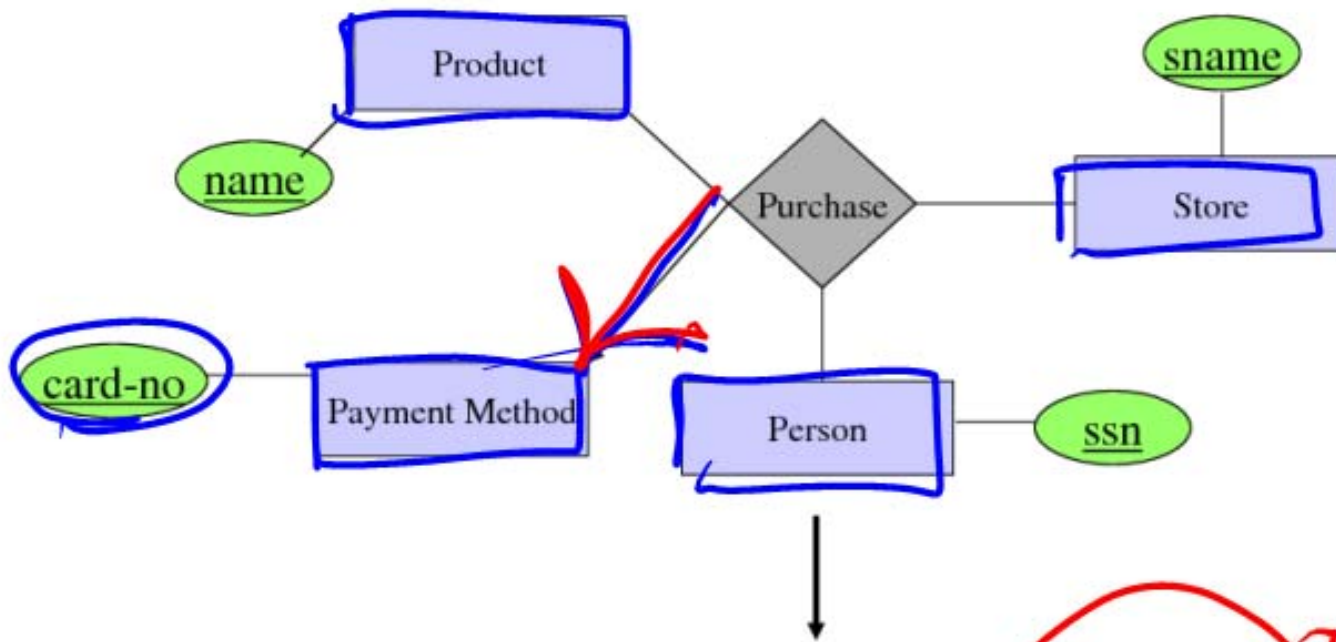
2. If the relation comes from a many-many relationship, the key of the relation include the set of all attribute keys in the relations corresponding to the entity sets (and additional attributes if necessary)



buys(name, ssn, date)
 ↓ prod ↓ person

Finding the Keys

But: if there is an arrow from the relationship to E, then we don't need the key of E as part of the relation key.



Purchase(name , sname, ssn, ~~card-no~~)

Finding the Keys

More specific rules:

- Many-one, one-many, one-one relationships
- Multi-way relationships
- Weak entity sets

(Try to find them yourself)

Reasoning with FDs

- 1) closure of FD sets
- 2) closure of attribute sets

Closure of FD sets

You

- Given a relation schema R & a set S of FDs
 - is the FD f logically implied by S ?

who gives FDs?

Example

$R = \{A, B, C, G, H, I\}$ 6 attr's

$name \rightarrow age$
 $age \rightarrow drinkable$

} name
↓
drinkable

$S = A \rightarrow B, A \rightarrow C, CG \rightarrow H, CG \rightarrow I, B \rightarrow H$

would $A \rightarrow H$ be logically implied? new rule

yes (you can prove this, using the definition of FD)

- Closure of S : $S^+ =$ all FDs logically implied by S

How to compute S^+ ?

we can use Armstrong's axioms

such as

$A \rightarrow H$

Armstrong's Axioms RULES

- Reflexivity rule

$NetID \rightarrow dept. add.$ proven by def.

– $A_1A_2...A_n \rightarrow$ a subset of $A_1A_2...A_n \Rightarrow NetID \rightarrow dept$

- Augmentation rule

$Name, NetID \rightarrow dept. add., Name$

– $A_1A_2...A_n \rightarrow B_1B_2...B_m$, then

$A_1A_2...A_n C_1C_2...C_k \rightarrow B_1B_2...B_m C_1C_2...C_k$

- Transitivity rule

– $A_1A_2...A_n \rightarrow B_1B_2...B_m$ and

$B_1B_2...B_m \rightarrow C_1C_2...C_k$, then

$A_1A_2...A_n \rightarrow C_1C_2...C_k$

$Name \rightarrow age$

$age \rightarrow drink$

$\Rightarrow Name \rightarrow drink$

Inferring S+ using Armstrong's Axioms

- $S^+ = S$
- Loop
 - foreach f in S , apply reflexivity and augment. rules
 - add the new FDs to S^+
 - foreach pair of FDs in S , apply the transitivity rule
 - add the new FD to S^+
- Until S^+ does not change any further

$$S = \{ \overset{f_1}{A \rightarrow B}, \overset{f_2}{B \rightarrow C}, \overset{f_3}{AC \rightarrow D} \}$$

$S^+ ?$

"form changing"

so that $B \rightarrow B$

$$f_1, f_2, Tr \Rightarrow + A \rightarrow C$$

(want to use $AC \rightarrow D$)

$$\begin{array}{l} f_2: AB \rightarrow AC \\ f_1: AA \rightarrow AB \end{array} \Rightarrow AA \rightarrow D \Rightarrow A \rightarrow D$$

Name

NetID

Q1: What do you like best of this cls.
that we must keep?

Q2: What dislike
..... go?

Additional Rules

- **Union rule**

(aug)
 $X \rightarrow Y$ and $X \rightarrow Z$, then $X \rightarrow YZ$
 $(X, Y, Z \text{ are sets of attributes})$

Handwritten example:
 $netid \rightarrow dept$ and $netid \rightarrow addr$, then $netid \rightarrow dept\ addr$

$xx \rightarrow xy \Rightarrow xx \rightarrow yz$
 $xy \rightarrow yz$

- Decomposition rule

$X \rightarrow YZ$, then $X \rightarrow Y$ and $X \rightarrow Z$

- Pseudo-transitivity rule

$X \rightarrow Y$ and $YZ \rightarrow U$, then $XZ \rightarrow U$

- These rules can be inferred from Armstrong's axioms

Closure of a Set of Attributes

(name, addr) \rightarrow ?

Given a set of attributes $\{A_1, \dots, A_n\}$ and a set of dependencies S .

Problem: find all attributes B such that:

any relation which satisfies S also satisfies:

$$A_1, \dots, A_n \rightarrow B$$

(You)

The **closure** of $\{A_1, \dots, A_n\}$, denoted $\{A_1, \dots, A_n\}^+$, is the set of all such attributes B

We will discuss the motivations for attribute closures soon

Is $\{name, addr\}$ a key?
 $\{name, addr\}^+ \Rightarrow$ all attr.

Algorithm to Compute Closure

Start with $X = \{A_1, \dots, A_n\}$. $\{name, addr\}$

Repeat until X doesn't change **do:**

if $B_1, B_2, \dots, B_n \longrightarrow \underline{\underline{C}}$ is in S, **and**

B_1, B_2, \dots, B_n are all in X, **and**

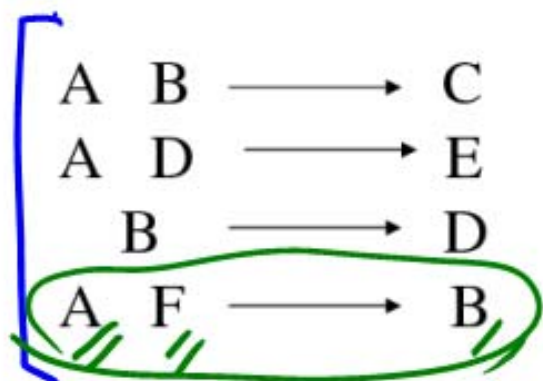
C is not in X

then

add C to X. $X = X + \{C\}$

Example

$R: \langle A, B, C, D, E, F \rangle$ Is (A, f) a key?



Name Addr \rightarrow age

Closure of $\{A, B\}$: $X = \{A, B, C, D, E\}$

Closure of $\{A, F\}$: $X = \{A, F, B, D, C, E\}$

✓ $(A, F)^+ = \{A, \dots, F\}$
 ✗ $(A)^+ = \{\dots\}$
 ✗ $(F)^+ = \{\dots\}$

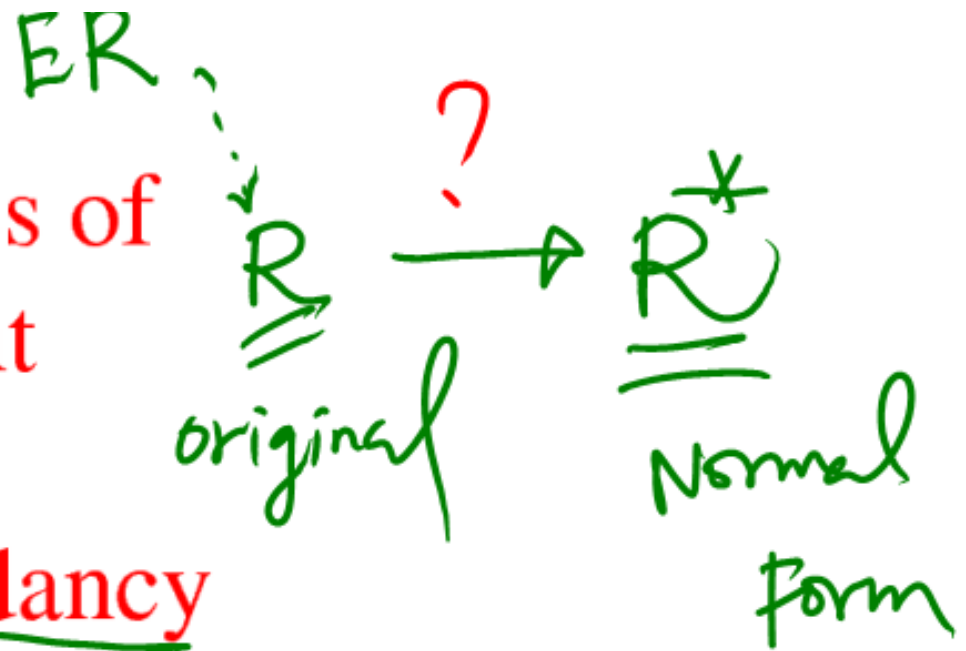
| | (A, F) | $(A)?$ |
|--------------------|------------------|--------|
| $AF \rightarrow B$ | A, B, F | |
| $B \rightarrow D$ | A, B, D, F | |
| $AD \rightarrow E$ | A, B, D, E, F | |
| $AB \rightarrow C$ | A, B, C, D, E, F | stop |

Usage for Attribute Closure

- Test if X is a superkey
 - compute X^+ , and check if X^+ contains all attrs of R
- Check if $X \rightarrow Y$ holds
 - by checking if Y is contained in X^+

$$Y \subseteq X^+ \iff X \rightarrow Y$$

Desirable Properties of Schema Refinement



- 1) minimize redundancy
- 2) avoid info loss
- 3) preserve dependency
- 4) ensure good query performance

Normal Forms

x set,

string,

x array,

Float,

✓ **First Normal Form** = all attributes are atomic
Second Normal Form (2NF) = old and obsolete

SQL,

Ted Codd.

Boyce Codd Normal Form (BCNF) ←

Third Normal Form (3NF)

Fourth Normal Form (4NF)

Others...

Boyce-Codd Normal Form

BCNF (NO)

| ssn | addr | phone |
|------|------|-------|
| Alex | 10 G | 123 |
| Alex | 10 G | 456 |

A simple condition for removing anomalies from relations:

A relation R is in BCNF if and only if:



ssn

~~Bad~~

addr

Whenever there is a nontrivial FD

$$A_1, A_2, \dots, A_n \rightarrow B$$

for R, it is the case that $\{A_1, A_2, \dots, A_n\}$ is a super-key for R.

then

ssn is superkey

In English (though a bit vague):



ssn

~~all attr~~

ssn, addr, phone

Whenever a set of attributes of R is determining another attribute, it should determine all attributes of R. In Contrast

ssn

addr

ssn

phone

✓ ssn → addr

✓ ssn a key **yes**

BCNF ?

| | |
|--------|------|
| X Alex | 10 G |
| X Alex | 10 G |

| | |
|------|-----|
| Alex | 123 |
| Alex | 456 |

Example

| Name | SSN | Phone Number |
|------|------------|----------------|
| Fred | 123-321-99 | (201) 555-1234 |
| Fred | 123-321-99 | (206) 572-4312 |
| Joe | 909-438-44 | (908) 464-0028 |
| Joe | 909-438-44 | (212) 555-4000 |

What are the dependencies?

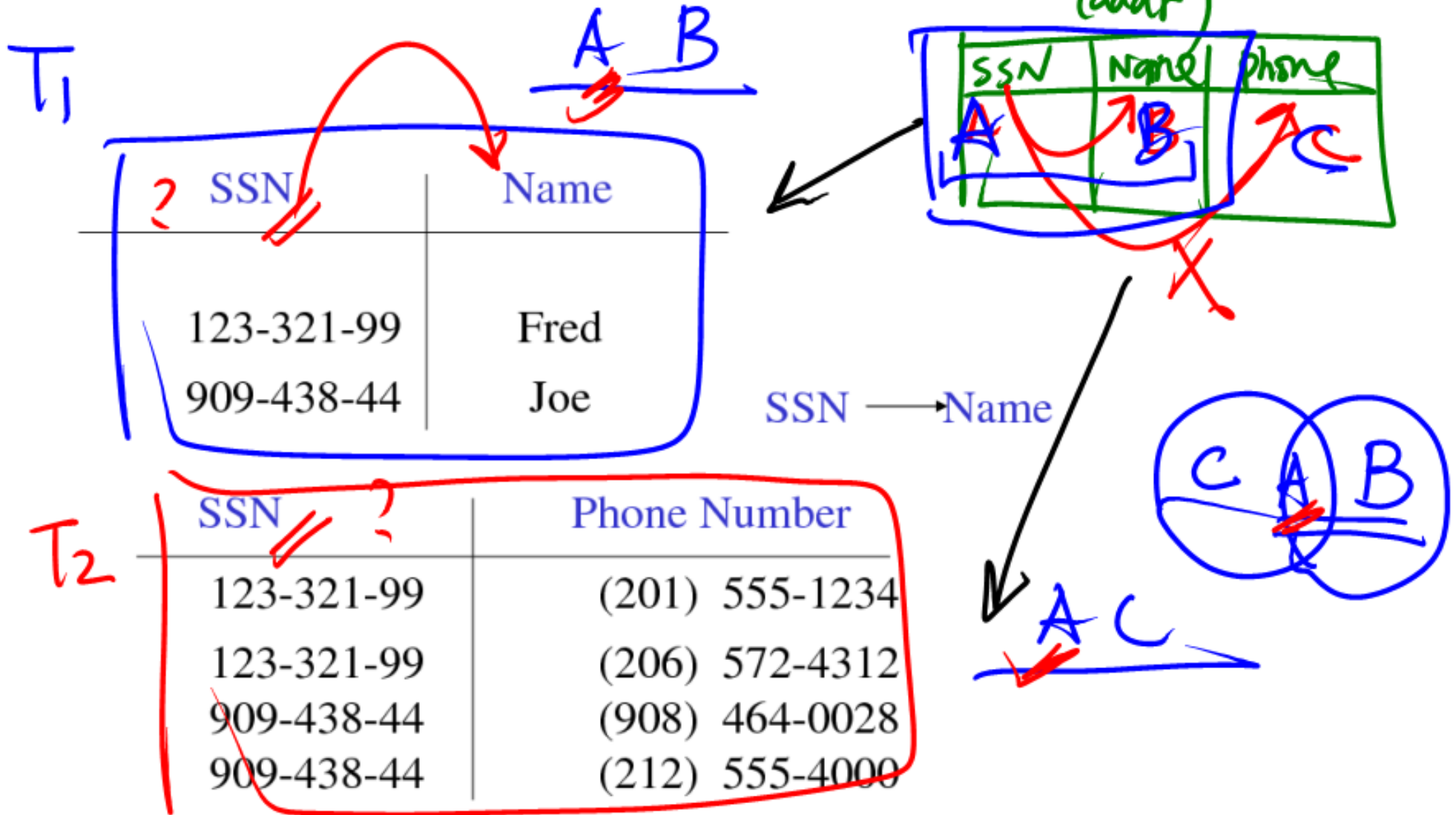
$SSN \rightarrow Name$

What are the keys?

Is it in BCNF?

Decompose it into BCNF

NOT BCNF



What About This?

| Name | Price | Category |
|----------|---------|----------|
| Gizmo | \$19.99 | gadgets |
| OneClick | \$24.99 | camera |

Name → Price, Category