Computing the Rank

```
In [16]:
```

```
#keep
import numpy as np
```

```
In [17]:
```

```
#keep
n = 5
A = np.random.randn(n, n)
```

Now decrease the rank of A:

```
In [18]:
```

```
#keep
A[4] = A[0] + 5 * A[2]
A[1] = 3 * A[0] -2 * A[2]
```

What should the rank be now?

Let's run Gaussian Elimination:

In [19]:

```
#keep
np.set printoptions(precision=4)
for i in range(n):
    # find biggest entry
    j = max(
        (j for j in range(i, n)),
        key=lambda j: abs(A[j, i]))
    # swap rows i and piv_row
   row_i = A[i].copy()
    row_j = A[j]
   A[i] = row_j
   A[j] = row_i
    # eliminate down
    for j in range(i+1, n):
        A[j] = A[i] * A[j,i]/A[i,i]
    print(A)
    print()
```

```
0.0000e+00
                                                           5.3686e-01]
                  4.5908e+00
                              -3.3457e+00
                                             2.1521e+00
 [-2.2204e-16]
                 -2.7005e-01
                                1.9681e-01
                                            -1.2660e-01
                                                          -3.1580e-02]
    0.0000e+00
                 -1.5893e+00
                               -1.1484e+00
                                             9.0711e-01
                                                          -1.9974e+00]
                  1.3502e+00
                                                           1.5790e-01]]
    0.0000e+00
                              -9.8403e-01
                                              6.3298e-01
 [
[ [
    6.2344e+00
                 -5.5712e+00
                              -2.7390e-01
                                            -1.1447e+00
                                                          -4.1407e+00]
    0.0000e+00
                  4.5908e+00
                              -3.3457e+00
                                             2.1521e+00
                                                           5.3686e-01]
 [ -2.2204e-16
                  0.0000e+00
                              -2.7756e-17
                                            -2.7756e-17
                                                           1.0408e-16]
    0.0000e+00
                  0.0000e+00
                              -2.3067e+00
                                              1.6522e+00
                                                          -1.8116e+00]
 [
    0.0000e+00
                  0.0000e+00
                                2.2204e-16
                                              0.0000e+00
                                                           5.5511e-17]]
 6.2344e+00
                 -5.5712e+00
                              -2.7390e-01
                                            -1.1447e+00
                                                          -4.1407e+00]
[ [
    0.0000e+00
                  4.5908e+00
                              -3.3457e+00
                                             2.1521e+00
                                                           5.3686e-01]
 [
    0.0000e+00
                  0.0000e+00
                              -2.3067e+00
                                              1.6522e+00
                                                          -1.8116e+00]
 [ -2.2204e-16
                  0.0000e+00
                                0.0000e+00
                                            -4.7635e-17
                                                           1.2588e-16]
    0.0000e+00
                                                          -1.1887e-16]]
                  0.0000e+00
                                0.0000e+00
                                              1.5904e-16
    6.2344e+00
                 -5.5712e+00
                              -2.7390e-01
                                            -1.1447e+00
                                                          -4.1407e+00]
[ [
    0.0000e+00
                                                           5.3686e-01]
                  4.5908e+00
                              -3.3457e+00
                                             2.1521e+00
 0.0000e+00
                              -2.3067e+00
                  0.0000e+00
                                              1.6522e+00
                                                          -1.8116e+00]
 0.0000e+00
                  0.0000e+00
                                0.0000e+00
                                              1.5904e-16
                                                          -1.1887e-16]
 0.0000e+00
                                0.0000e+00
  -2.2204e-16
                                              6.1630e-33
                                                           9.0277e-17]]
    6.2344e+00
                 -5.5712e+00
                              -2.7390e-01
                                            -1.1447e+00
                                                          -4.1407e+00]
[ [
    0.0000e+00
                  4.5908e+00
                               -3.3457e+00
                                             2.1521e+00
                                                           5.3686e-01]
 [
 0.0000e+00
                  0.0000e+00
                              -2.3067e+00
                                              1.6522e+00
                                                          -1.8116e+00]
    0.0000e+00
                  0.0000e+00
                                0.0000e+00
                                             1.5904e-16
                                                          -1.1887e-16]
 -2.2204e-16
                  0.0000e+00
                                0.0000e+00
                                              6.1630e-33
                                                           9.0277e-17]]
```

-2.7390e-01

-1.1447e+00

-4.1407e+00]

Now what is the rank of that matrix?

6.2344e+00

[[

-5.5712e+00