

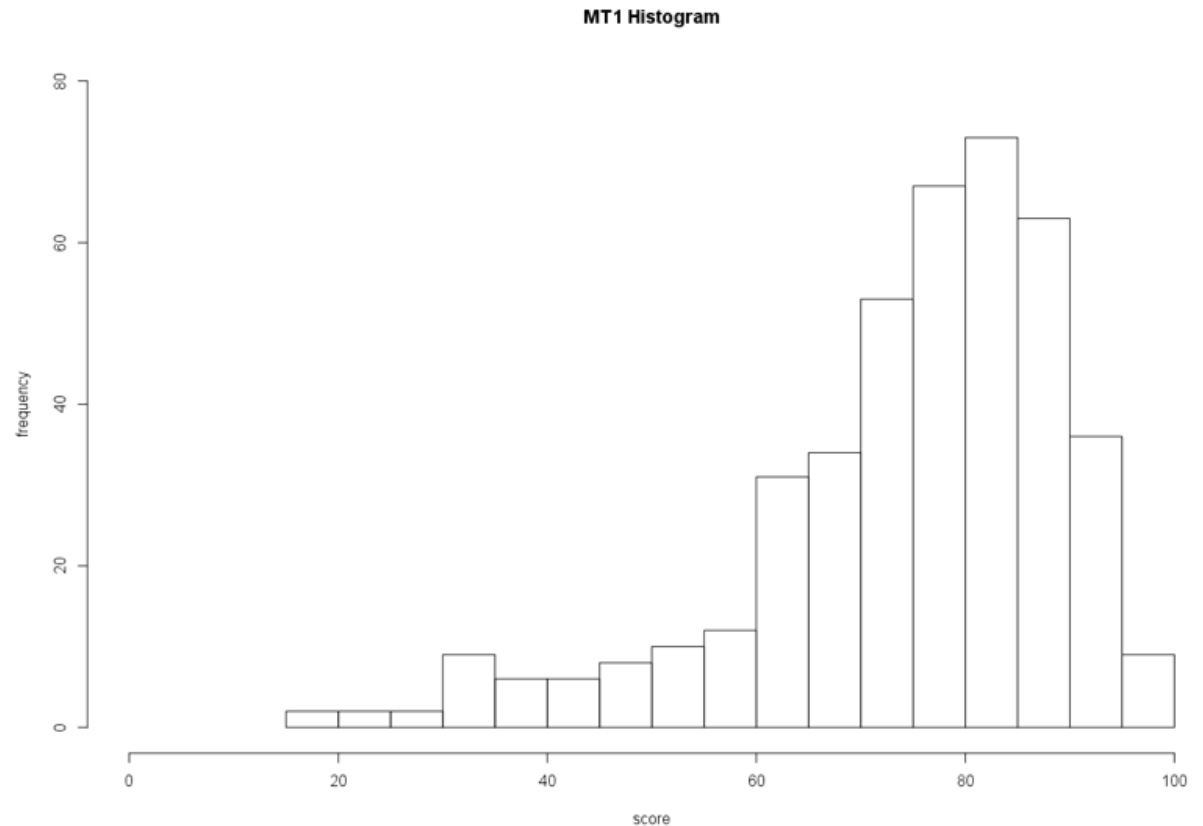
Announcements

MP4 available, due 3/8, 11:59p. EC due 3/1, 11:59p.

Code Challenge #1: Winners!

Exam Visitation: 3/4, 7:30p, Siebel 0216

TODAY: tree definitions
traversals



Complete Binary tree: for any level k in $[0, h-1]$, level k has 2^k nodes, and on level h , all nodes are pushed to the left.

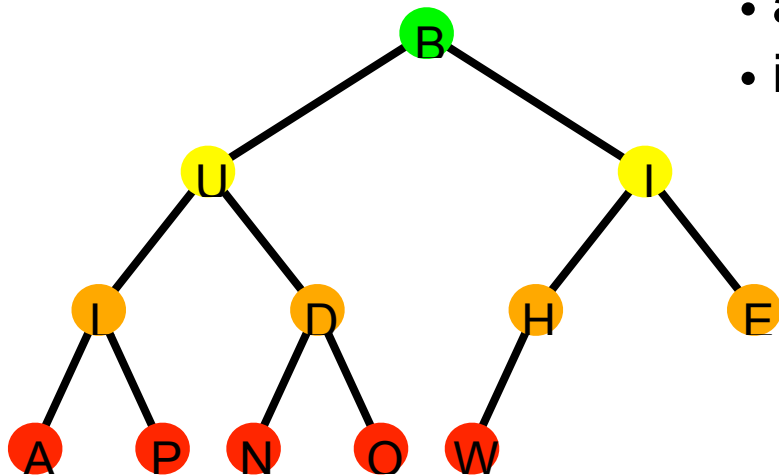
Complete tree of height h , C_h :

- an empty tree is C_{-1}
- if $h > -1$, then C_h is $\{r, T_L, T_R\}$, and either:

T_L is _____ and T_R is _____

OR

T_L is _____ and T_R is _____



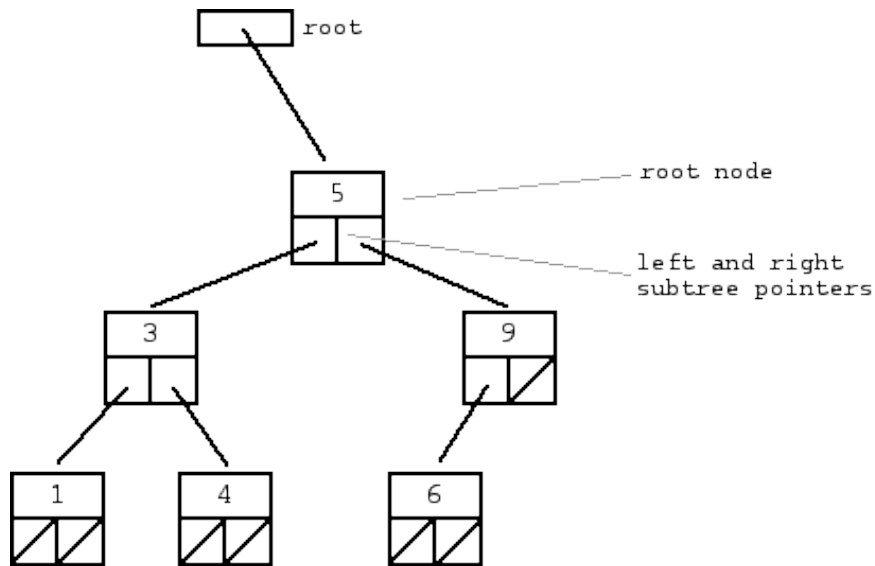
<http://xlinux.nist.gov/dads//HTML/completeBinaryTree.html>

Check for understanding:

Is every full tree complete?

Is every complete tree full?

Rooted, directed, ordered, binary trees



Tree ADT:

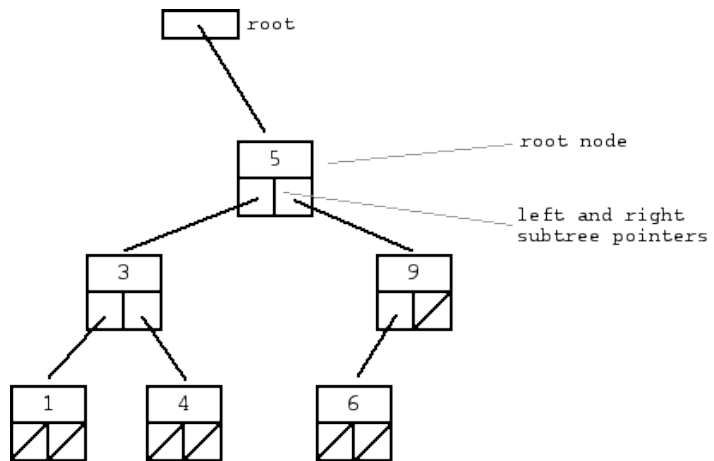
insert

remove

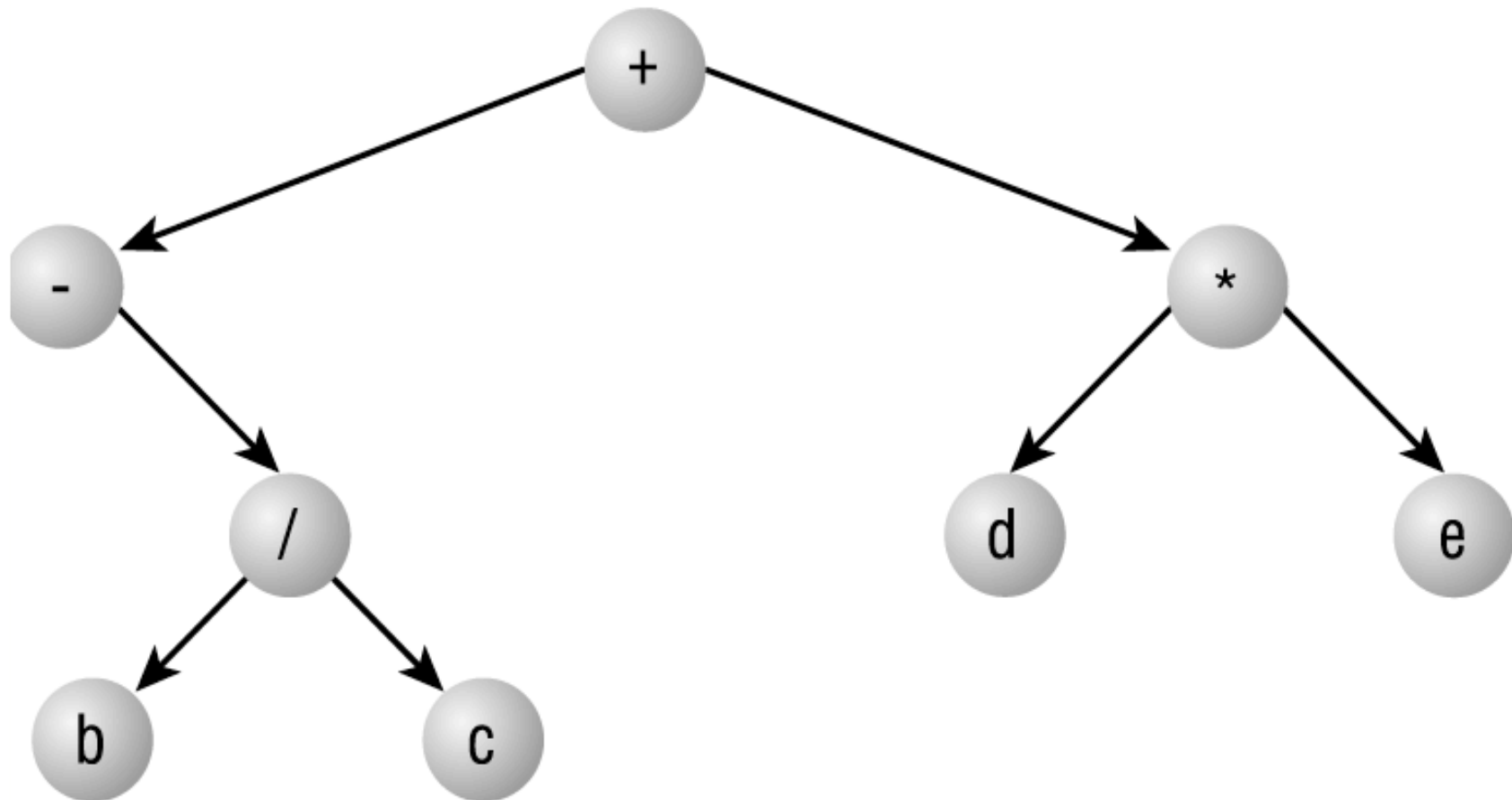
traverse

```
template <class T>
class tree{
public:
...
private:
    struct treeNode{
        T data;
        treeNode * left;
        treeNode * right;
    };
    treeNode * root
...
};
```

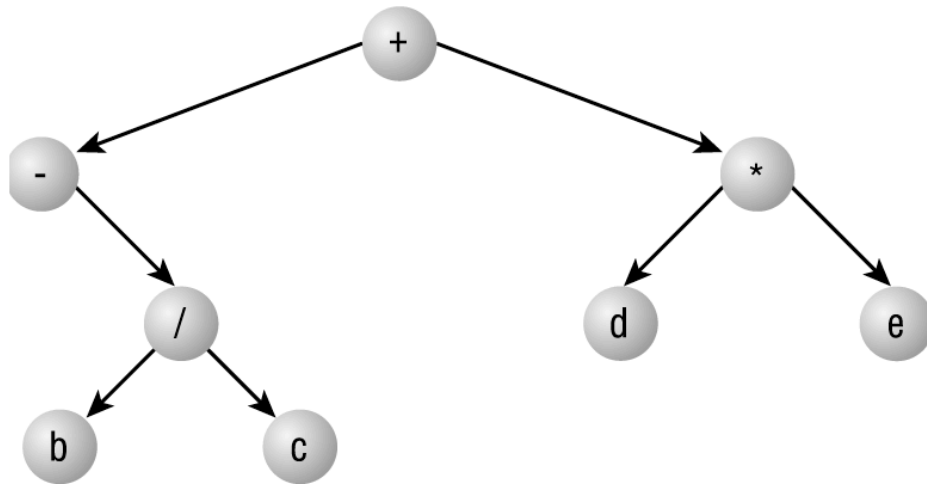
Theorem: if there are n data items in a binary tree, then there are _____ null pointers.



Traversal – scheme for visiting every node.

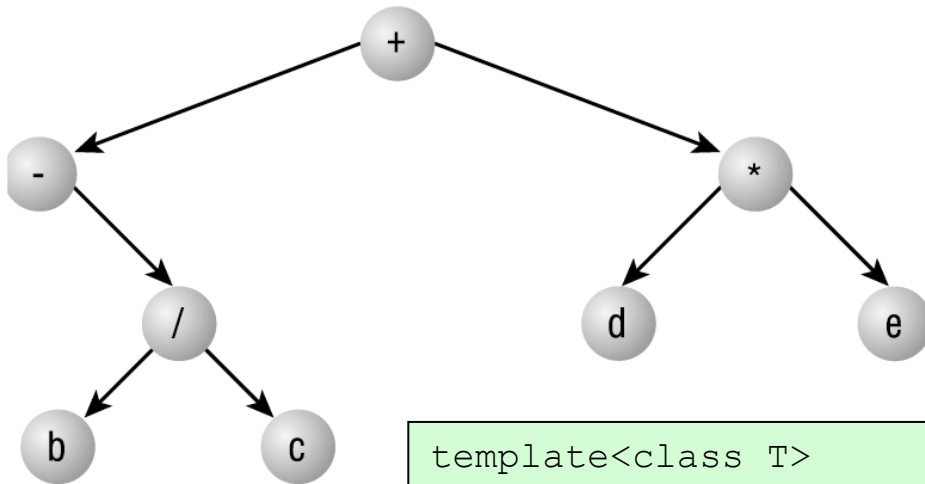


Traversal – scheme for visiting every node.



- At each node, two choices for direction (left, right)
- After both subtrees of a node are complete, move back up tree
- Each node is “visited” 3 times in a traversal.
- Each of those visit times corresponds to a particular kind of traversal.

Traversals:



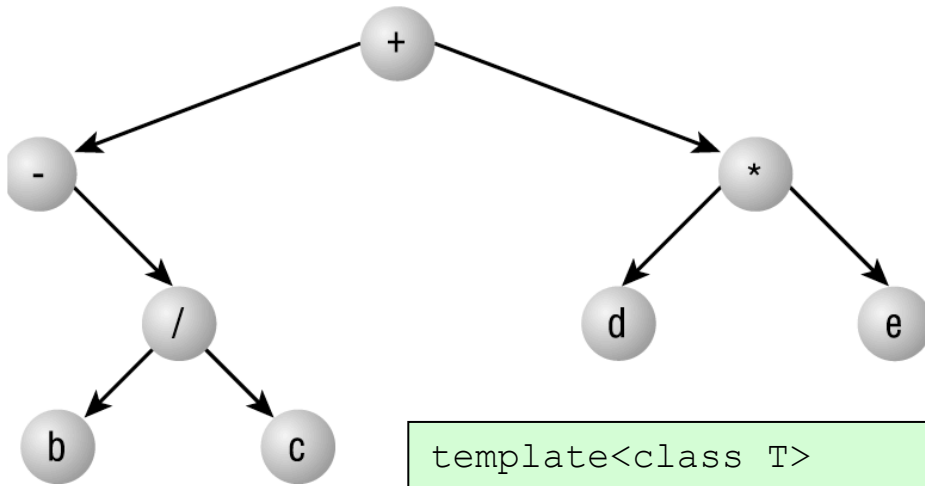
```
template<class T>
void binaryTree<T>::__Order(treeNode * croot){
    if (croot != null){

        __Order(croot->left);

        __Order(croot->right);

    }
}
```

Traversals:



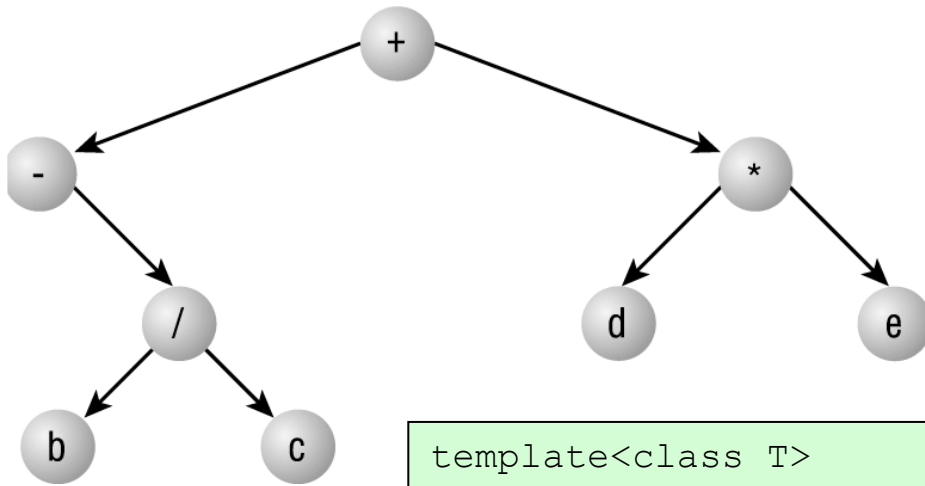
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Traversals:



```
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void binaryTree<T>::__Order(treeNode * croot){
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```

Traversals: A few mechanical questions...

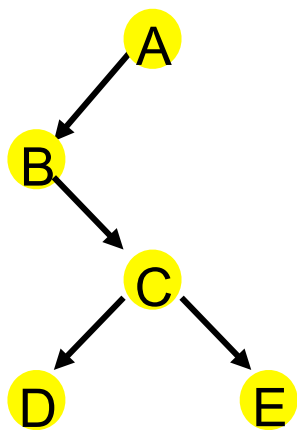
What is the 2nd letter printed in an inOrder traversal of this tree?

In what position is C printed in a postOrder traversal of this tree?

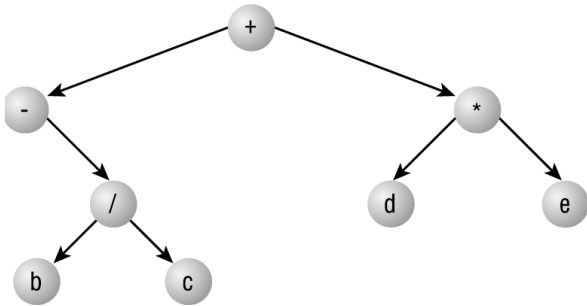
Which traversal prints the data of the tree in ABC order?

Draw and label a tree containing 8 integers so that an inOrder traversal of the tree prints the numbers in order.

Draw and label a tree containing 8 integers so that a preOrder traversal of the tree prints the numbers in order.



Traversals: A few discussion questions...



```
template<class T>
void binaryTree<T>::preOrder(treeNode * croot) {
    if (croot != null) {
        yell(croot->data);
        preOrder(croot->left);
        preOrder(croot->right);
    }
}
```

What is running time?

Is preOrder public or private?

How could we make this function employ a different function upon a visit?