$$\| \times \| = | \underbrace{ \times_0^2 + \times_1^2 + \times_2^2} |$$

$$\times = \begin{pmatrix} \times_0 \\ \times_i \\ \lambda_i \end{pmatrix}$$

Definition A nom is a function 11.11 from a vector space V into the real numbers that satisfies:

- ||×|| ≥0
- ||x+y|| ≤ ||x||+||y||
  (triangle inequality)
- · || dx || = | a | | x ||
- · ||x|=0=) x=0

Examples Let p>1. Then we define for a vector x with coordinates (x,,...,xn)

$$\|\mathbf{x}\|_{\mathbf{p}} = \frac{\mathbf{p}}{\mathbf{x}_1} \|\mathbf{x}_1\|_{\mathbf{p}} + \|\mathbf{x}_2\|_{\mathbf{p}} + \dots + \|\mathbf{x}_m\|_{\mathbf{p}}$$

