Sequential

1000 Nodes

```
Node 991 BC = 2612.422363
Node 992 BC = 7769.836426
Node 993 BC = 2853.305420
Node 994 BC = 3206.027588
Node 995 BC = 2526.590088
Node 996 BC = 6368.935059
Node 997 BC = 174.078094
Node 998 BC = 2785.130615
Node 999 BC = 501.523682
Node 1000 BC = 5148.713379
BC of graph: 13682.895508
Time taken by program is : 76.612306 sec
shavak@shavak-X11DAi-N:~/Documents/Ahad P0518 Project/Betweenness-Centrality/seq$
```

10,000 Nodes

```
Node 9988 BC = 11826.147461
Node 9989 BC = 33284.664062
Node 9990 BC = 33844.531250
Node 9992 BC = 16429.302734
Node 9993 BC = 16541.593750
Node 9994 BC = 37307.871094
Node 9996 BC = 21152.587891
Node 9997 BC = 13749.150391
Node 9998 BC = 13781.196289
Node 9999 BC = 3701.997070
Node 10000 BC = 64646.992188
BC of graph: 255227.093750
Time taken by program is : 130.722783 sec
shavak@shavak-X11DAi-N:~/Documents/Ahad P0518 Project/Betweenness-Centrality/seq$
```

Parallel

1000 Nodes

```
Node 715 BC = 3061.962158
Node 755 BC = 1946.609497
Node 795 BC = 7899.212402
Node 835 BC = 3710.549072
Node 875 BC = 1475.739258
Node 915 BC = 2468.165039
Node 955 BC = 664.320496
Node 995 BC = 2494.316406
BC of graph: 13429.852539
Time taken by program is : 0.053204 sec
shavak@shavak-X11DAi-N:~/Documents/Ahad P0518 Project/Betweenness-Centrality/parallel$
```

```
Node 9795 BC = 9878.930664

Node 9835 BC = 57948.007812

Node 9875 BC = 28230.451172

Node 9915 BC = 23155.443359

Node 9955 BC = 12078.264648

Node 9886 BC = 34953.761719

Node 9926 BC = 9509.125000

Node 9966 BC = 23660.789062

BC of graph: 255227.078125

Time taken by program is : 1.976344 sec

shavak@shavak-X11DAi-N:~/Documents/Ahad P0518 Project/Betweenness-Centrality/parallel$
```

Parallel with varying logical Threads

1000 Nodes

```
Node 988 BC = 2321.466797
Node 989 BC = 457.508972
Node 990 BC = 921.835205
Node 991 BC = 2612.423340
Node 992 BC = 7768.070312
Node 993 BC = 2852.107178
Node 994 BC = 3206.025635
Node 995 BC = 2526.088623
Node 995 BC = 6368.437012
Node 997 BC = 173.578049
Node 998 BC = 2785.129639
Node 998 BC = 501.523712
Node 1000 BC = 5148.195312
BC of graph: 13667.792969
Time taken by program is : 0.141867 sec
shavak@shavak-X11DAi-N:~/Documents/Ahad P0518 Project/Betweenness-Centrality/Parallel_With_Varrying_Threads$
```

10,000 Nodes

```
Node 6989 BC = 11890.654297
Node 6990 BC = 63935.953125
Node 6991 BC = 35618.812500
Node 6992 BC = 42750.527344
Node 6993 BC = 67390.929688
Node 6994 BC = 36646.730469
Node 6995 BC = 5259.403320
Node 6995 BC = 5259.403320
Node 6996 BC = 33870.761719
Node 6997 BC = 53197.234375
Node 6999 BC = 24555.515625
Node 7000 BC = 37096.304688
BC of graph: 255179.656250
Time taken by program is : 2.001445 sec
shavak@shavak-X11DAi-N:~/Documents/Ahad P0518 Project/Betweenness-Centrality/Parallel_With_Varrying_Threads$
```

1,00,000 Nodes

```
Node 92494 BC = 144300.626123
Node 92495 BC = 427879.156250
Node 92496 BC = 461146.406250
Node 92497 BC = 793396.250000
Node 92498 BC = 718131.625000
Node 92499 BC = 89027.960938
Node 92499 BC = 89027.960938
Node 92500 BC = 627358.125000
Node 92501 BC = 352951.781250
BC of graph: 3900481.000000
Time taken by program is : 559.458491 sec
shavak@shavak-X11DAi-N:~/Documents/Ahad P0518 Project/Betweenness-Centrality/Parallel_With_Varrying_Threads$
```

Parallel With concurrent queues

1000 nodes

```
Node 995 BC = 2526.590088

Node 996 BC = 6368.935059

Node 997 BC = 174.078094

Node 998 BC = 2785.130615

Node 999 BC = 501.523682

Node 1000 BC = 5148.713379

BC of graph: 13682.895508

Time taken by program is: 0.651527 sec
```

10000 nodes

```
Node 7491 BC = 29206.822266

Node 7492 BC = 28235.814453

Node 7493 BC = 5123.822754

Node 7494 BC = 76746.187500

Node 7495 BC = 35269.160156

Node 7496 BC = 28636.351562

Node 7497 BC = 84169.507812

Node 7498 BC = 17218.281250

Node 7499 BC = 30664.011719

Node 7500 BC = 30052.259766

Node 7501 BC = 47875.535156

BC of graph: 255226.781250

Time taken by program is : 15.960636 sec
```

1,00,000 nodes

```
Node 34996 BC = 738027.562500

Node 34997 BC = 650272.000000

Node 34998 BC = 2015205.000000

Node 34999 BC = 490751.187500

Node 35000 BC = 309459.906250

Node 35001 BC = 388442.187500

BC of graph: 3900475.0000000

Time taken by program is : 650.334454 sec
```

Email-Enron.txt

```
vertex 36665: 0.250000
vertex 36666: 0.250000
vertex 36667: 0.250000
Time taken by program is : 30.889447 sec
The betweenness centrality of graph is 43648488.000000shaval
```

16 Threads

```
vertex 36665: 0.250000
vertex 36666: 0.250000
vertex 36667: 0.250000
Time taken by program is : 17.300053 sec
The betweenness centrality of graph is 43648684.000000shavak@sh
```

32 Threads

```
vertex 36665: 0.250000

vertex 36666: 0.250000

vertex 36667: 0.250000

Time taken by program is: 10.603901 sec

The betweenness centrality of graph is 43642832.000000shavak@shavak-X11DA

$ $\begin{align*}
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```

40 Threads

```
vertex 36634: 1.000000

vertex 36665: 0.250000

vertex 36666: 0.250000

vertex 36667: 0.250000

Time taken by program is : 9.909790 sec

The betweenness centrality of graph is 43627852.000000shavak@sh
```

Wiki-Vote.txt

8 Threads

```
vertex 8204: 2.016459
vertex 8263: 7.513928
vertex 8271: 1.698715
Time taken by program is : 0.606520 sec
The betweenness centrality of graph is 446496.593750shavak@s
```

16 Threads

```
vertex 8134: 12.9/2526

vertex 8204: 2.016459

vertex 8263: 7.513927

vertex 8271: 1.698715

Time taken by program is : 0.410013 sec

The betweenness centrality of graph is 444586.468750shavak@shav
```

40 Threads

```
vertex 8134: 12.305855

vertex 8204: 2.016459

vertex 8263: 7.448670

vertex 8271: 1.698715

Time taken by program is : 0.268558 sec

The betweenness centrality of graph is 441387.968750shavak@s
```

Soc-Epinions.txt

8 Threads

```
vertex 75867: 28219.000000
vertex 75871: 112862.500000
vertex 75872: 95366.000000
Time taken by program is : 99.893502 sec
The betweenness centrality of graph is 47885988.0000000shavak@sh
```

16 Threads

```
vertex 75867: 28212.500000

vertex 75867: 112816.500000

vertex 75871: 112816.500000

vertex 75872: 95366.000000

Time taken by program is: 61.756963 sec

The betweenness centrality of graph is 47828880.0000000shavak@sl
```

32 Threads

```
vertex 75865: 143035.500000
vertex 75867: 28219.000000
vertex 75871: 112868.500000
vertex 75872: 95366.000000
Time taken by program is : 43.185026 sec
The betweenness centrality of graph is 47891736.0000000shavak@sh
ss-Centrality/Concurrent-Oueue$ #518 Project/Betweennes
```

```
vertex 75865: 143035.500000
vertex 75867: 28225.500000
vertex 75871: 112886.500000
vertex 75872: 95366.000000
Time taken by program is: 40.135340 sec
The betweenness centrality of graph is 47883636.0000000shavak@sh
ss-Centrality/Concurrent-Oueues 0518 Project/Betweennes
```

Com-dblp.ungraph.txt

32 Threads

```
vertex 4254/3: 1310.1/2/29
vertex 425496: 3992.633057
vertex 425875: 7633.500000
Time taken by program is : 413.707431 sec
The betweenness centrality of graph is 15511676.000000shavak@sh
```

40 Threads

```
vertex 425467: 0.666667

vertex 425473: 1310.171143

vertex 425496: 3992.633545

vertex 425875: 7633.500000

Time taken by program is : 384.107274 sec

The betweenness centrality of graph is 15511650.0000000shavak@sh
```

Parallel with varying threads

P1 dataset 10,000 Nodes of dataset

```
vertex 8667: 850.843848
vertex 8669: 940.511892
vertex 8670: 402.752799
vertex 8671: 508.144673
vertex 8672: 360.196492
vertex 8674: 22.323676
vertex 8677: 1091.526021
vertex 8678: 1387.751688
vertex 8680: 852.980499
vertex 8683: 499.208700
vertex 8685: 694.457832
vertex 8686: 887.412263
vertex 8689: 3.000000
vertex 8690: 78.500000
vertex 8695: 25.500000
vertex 8696: 1155.159880
vertex 8700: 435.935865
vertex 8701: 138.056668
vertex 8705: 450.948737
vertex 8707: 232.615930
vertex 8711: 800.890380
vertex 8714: 1455.235239
Time taken by program is : 0.362151 sec
The betweenness centrality of graph is 294004.593750shavak@shavak-X11DAi
```

```
vertex 8685: 689.437317
vertex 8686: 878.456726
vertex 8689: 3.000000
vertex 8690: 78.500000
vertex 8695: 25.500000
vertex 8696: 1142.156494
vertex 8700: 431.910980
vertex 8701: 139.764984
vertex 8705: 445.353729
vertex 8707: 230.282730
vertex 8711: 786.771484
vertex 8711: 786.771484
vertex 8714: 1447.455444
Time taken by program is : 0.230210 sec
The betweenness centrality of graph is 289995.437500shavak@shavak-X11DAi-N:~/Documents/Ahad P
```

```
vertex 8680: 847.954468
vertex 8683: 487.336090
vertex 8685: 683.981873
vertex 8686: 879.537354
vertex 8689: 3.000000
vertex 8690: 78.500000
vertex 8695: 25.500000
vertex 8696: 1148.743530
vertex 8700: 432.588928
vertex 8701: 139.917755
vertex 8705: 445.353149
vertex 8707: 229.917648
vertex 8707: 229.917648
vertex 8711: 791.027100
vertex 8714: 1437.367920
Time taken by program is : 0.221539 sec
The betweenness centrality of graph is 285998.468750shavak@shavak-X11DAi-N:~/Documents/Ahad F
```

Email-Enron dataset

16 Threads

```
vertex 36380: 1.000000
vertex 36381: 1.000000
vertex 36382: 1.000000
vertex 36383: 1.000000
vertex 36437: 1.000000
vertex 36589: 6.000000
vertex 36597: 134746.000000
vertex 36608: 67372.000000
vertex 36612: 9.500000
vertex 36615: 2.000000
vertex 36626: 6.000000
vertex 36634: 1.000000
vertex 36665: 0.250000
vertex 36666: 0.250000
vertex 36667: 0.250000
Time taken by program is : 7.728368 sec
The betweenness centrality of graph is 43644760.000000shavak@shavak-X11DAi-N:~/Documents/Ahad
```

32 threads

```
vertex 36380: 1.000000
vertex 36381: 1.000000
vertex 36382: 1.000000
vertex 36383: 1.000000
vertex 36437: 1.000000
vertex 36589: 6.000000
vertex 36597: 134738.000000
vertex 36608: 67371.000000
vertex 36612: 9.500000
vertex 36615: 2.000000
vertex 36626: 6.000000
vertex 36634: 1.000000
vertex 36665: 0.250000
vertex 36666: 0.250000
vertex 36667: 0.250000
Time taken by program is : 7.724056 sec
The betweenness centrality of graph is 43541240.000000shavak@shavak-X11DAi-N:~/Documents/Ahad
```

```
vertex 36380: 1.000000
vertex 36381: 1.000000
vertex 36382: 1.000000
vertex 36383: 1.000000
vertex 36437: 1.000000
vertex 36589: 6.000000
vertex 36597: 134738.000000
vertex 36608: 67378.000000
vertex 36612: 9.500000
vertex 36612: 9.500000
vertex 36615: 2.000000
vertex 36626: 6.0000000
vertex 36634: 1.000000
vertex 36634: 1.000000
vertex 36666: 0.250000
vertex 36667: 0.250000
vertex 36667: 0.250000
vertex 36667: 0.250000
Time taken by program is : 7.772647 sec
The betweenness centrality of graph is 43645580.000000shavak@shavak-X11DAi-N:~/Documents/Ahad
```

Wiki-vote data set

```
Vertex /862: 442/.322/54
vertex 7874: 36.425983
vertex 7882: 7269.521484
vertex 7910: 2536.212158
vertex 7924: 58.701458
vertex 7928: 1337.742920
vertex 8021: 1157.871704
vertex 8037: 114.185532
vertex 8042: 1201.307983
vertex 8050: 57.760818
vertex 8051: 6141.307129
vertex 8134: 12.472527
vertex 8204: 2.016459
vertex 8263: 7.486150
vertex 8271: 1.698715
Time taken by program is : 0.371150 sec
The betweenness centrality of graph is 444838.218750shavak@shav
```

```
reitex /055: 4/50./2/051
vertex 7860: 3537.561523
vertex 7862: 4418.170898
vertex 7874: 36.130730
vertex 7882: 7265.913574
vertex 7910: 2535.841797
vertex 7924: 58.466805
vertex 7928: 1321.925903
vertex 8021: 1157.871704
vertex 8037: 113.539597
vertex 8042: 1201.259766
vertex 8050: 57.350941
vertex 8051: 6140.718750
vertex 8134: 12.972528
vertex 8204: 2.016459
vertex 8263: 7.468472
vertex 8271: 1.698715
Time taken by program is : 0.256721 sec
The betweenness centrality of graph is 442168.093750shavak@shav
40 threads
```

```
vertex /800: 353/.050982
vertex 7862: 4416.470215
vertex 7874: 36.386360
vertex 7882: 7265.417969
vertex 7910: 2536.366455
vertex 7924: 58.023907
vertex 7928: 1337.659912
vertex 8021: 1157.871704
vertex 8037: 113.798042
vertex 8042: 1201.302124
vertex 8050: 57.650249
vertex 8051: 6142.503418
vertex 8134: 12.801097
vertex 8204: 2.016459
vertex 8263: 7.421719
vertex 8271: 1.698715
Time taken by program is : 0.216035 sec
The betweenness cent<u>r</u>ality of graph is 441462.437500shavak@shav
```

Com_dblp.ungraph 40 threads

```
vertex 423279: 1336.572876
vertex 423321: 1192.250000
vertex 423339: 2497.147217
vertex 423411: 1399.080322
vertex 423505: 1.000000
vertex 423506: 4841.500000
vertex 423794: 477.798309
vertex 423972: 826.513306
vertex 424034: 1.000000
vertex 424132: 0.250000
vertex 424209: 11966.000000
vertex 424262: 4669.000000
vertex 424272: 34787.500000
vertex 424315: 505.125793
vertex 424337: 4846.032227
vertex 424805: 3109.883057
vertex 425252: 74.824539
vertex 425253: 6431.671387
vertex 425254: 181.198639
vertex 425467: 0.666667
vertex 425473: 1310.170898
vertex 425496: 3992.633789
vertex 425875: 7633.500000
Time taken by program is: 301.118171 sec
The betweenness centrality of graph is 15511648.000000shavak@sh
```

Com_amazon.ungraph

8Threads

16 threads

32 Threads

```
vertex 548181: 8.500000
vertex 548188: 8.116666
vertex 548190: 10.666667
vertex 548191: 0.666667
vertex 548199: 253.083344
vertex 548238: 41.833336
vertex 548240: 23.916662
vertex 548250: 279.333313
vertex 548268: 0.250000
vertex 548271: 0.125000
vertex 548299: 14.583334
vertex 548304: 26.374998
vertex 548319: 22.325001
vertex 548328: 85.250023
vertex 548339: 3.750000
vertex 548343: 21.500000
vertex 548354: 13.500000
vertex 548368: 151.000000
vertex 548391: 137.558350
vertex 548411: 86.366661
Time taken by program is: 119.985304 sec
The betweenness centrality of graph is 202970.656250shavak@shav
```

```
vertex 548199: 253.083344
vertex 548238: 41.833336
vertex 548240: 23.916656
vertex 548250: 279.333344
vertex 548268: 0.250000
vertex 548271: 0.125000
vertex 548299: 14.583335
vertex 548304: 26.374996
vertex 548319: 22.325001
vertex 548328: 85.249992
vertex 548339: 3.750000
vertex 548343: 21.500000
vertex 548354: 13.500000
vertex 548368: 151.000000
vertex 548391: 137.558350
vertex 548411: 86.366684
Time taken by program is : 123.941191 sec
```

Com-youtube.ungraph

32 Threads
// could not run
40 Threads
// could not run

Soc-epinions dataset

8 Threads

16 Threads

```
vertex 75686: 23839.000000
vertex 75704: 23838.500000
vertex 75706: 23839.000000
vertex 75756: 7.250000
vertex 75757: 0.750000
vertex 75763: 2.950000
vertex 75764: 24.000000
vertex 75765: 1.150000
vertex 75767: 33.450001
vertex 75768: 27.250000
vertex 75769: 14.900000
vertex 75779: 2.000000
vertex 75788: 10.500000
vertex 75791: 13.250000
vertex 75800: 3.000000
vertex 75801: 6.750000
vertex 75829: 166866.000000
vertex 75837: 112867.500000
vertex 75842: 169322.000000
vertex 75865: 143035.500000
vertex 75867: 28218.500000
vertex 75871: 112862.500000
vertex 75872: 95366.000000
Time taken by program is : 34.198587 sec
The betweenness centrality of graph is 47862596.000000shavak@sh
```

40 Threads

```
vertex 75769: 14.900000
vertex 75779: 2.000000
vertex 75788: 10.500000
vertex 75791: 13.250000
vertex 75800: 3.000000
vertex 75801: 6.750000
vertex 75829: 166866.000000
vertex 75837: 112889.500000
vertex 75842: 169331.000000
vertex 75865: 143035.500000
vertex 75867: 28221.000000
vertex 75871: 112864.500000
vertex 75872: 95366.000000
Time taken by program is: 30.830535 sec
The betweenness centrality of graph is 47889792.0000000shavak@sh
```

Code:

```
#include <iostream>
#include <fstream>
#include <vector>
#include <map>
#include <set>
#include <sits/stdc++.h>
#include <string>
#include <queue>
#include <stack>
#include <mutex>
#include <thread>
#include <chrono>
#include <time.h>
using namespace std;

// #define v_size 367663
```

```
vector<vector<int>> graph;
vector<int> vertices:
int numberOfVertices;
int main(int argc, char *argv[])
  string inputFileName(argv[1]); //, outputFileName(argv[2]);
  // int numberOfThreads = stoi(strThreads);
  ifstream input(inputFileName);
  // ofstream output(outputFileName);
  int freeIndex = 0;
  struct timespec start, end;
  vector<pair<int, int>> edges;
  map<int, int> myMap;
  // start = clock();
  printf("clock started\n");
  clock_gettime(CLOCK_MONOTONIC, &start);
  ios base::sync with stdio(false);
  printf("Reading file\n");
  while (!input.eof())
  {
     int u, v;
     input >> u >> v;
     edges.push back(make pair(u, v));
     myMap.insert(make pair(u, 0));
     myMap.insert(make_pair(v, 0));
     if (input.eof())
       break;
  }
  input.close();
  printf("Done reading file\n");
  for (auto &m: myMap)
     m.second = freeIndex++;
  for (const auto &m: myMap)
     vertices.push_back(m.first);
  numberOfVertices = freeIndex;
  graph.resize(freeIndex);
  for (const auto &p : edges)
  {
     int u = p.first, v = p.second;
     graph[myMap[u]].push_back(myMap[v]);
  }
```

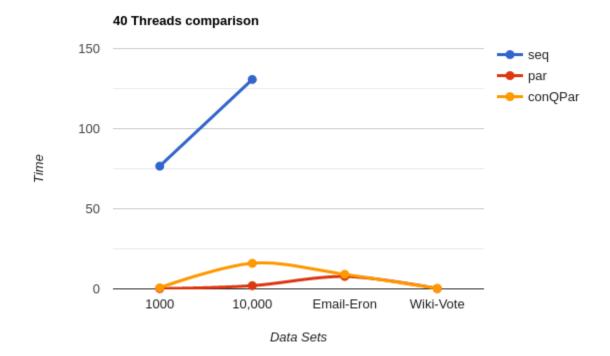
```
//vector<double> betweenness(numberOfVertices, 0.0);
float betweenness[numberOfVertices];
printf("graph created...\n\n");
// for (int i = 0; i < graph.size(); i++) {
    for (int j = 0; j < graph[i].size(); j++)
//
       cout << graph[i][j] << " ";
//
    cout << endl;
// }
printf("Initializing BC\n");
#pragma omp parallel for num_threads(40)
for (int v = 0; v < numberOfVertices; v++)
{
  betweenness[v] = 0.0;
printf("Starting BFS for each vertex...\n");
clock_gettime(CLOCK_MONOTONIC, &start);
ios_base::sync_with_stdio(false);
#pragma omp parallel for num threads(40)
for (int s = 0; s < numberOfVertices-1; s++)
  stack<int> S;
  vector<vector<int>> P(numberOfVertices);
  vector<int> sigma(numberOfVertices, 0);
       vector<int> d(numberOfVertices, -1);
       vector<double> delta(numberOfVertices, 0.0);
  sigma[s] = 1;
  d[s] = 0;
  queue<int> Q;
  Q.push(s);
  while (!Q.empty())
     int v = Q.front();
     Q.pop();
     S.push(v);
     for (const auto &w : graph[v])
       if (d[w] < 0)
```

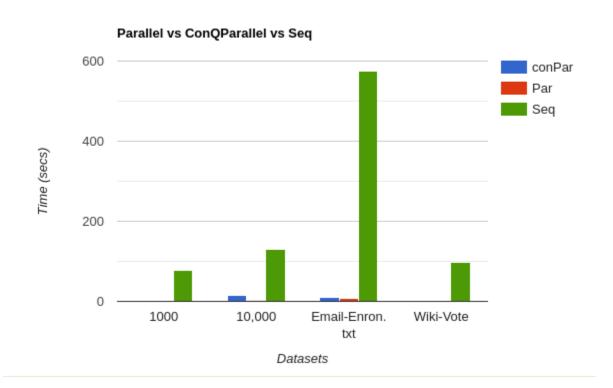
```
Q.push(w);
          d[w] = d[v] + 1;
       if (d[w] == d[v] + 1)
          sigma[w] += sigma[v];
          P[w].push_back(v);
       }
     }
  // #pragma omp parallel for num_threads(40)
  // for (int i = 0; i < numberOfVertices; i++)
  // {
  //
      delta[i] = 0.0;
  // }
  while (!S.empty())
     int w = S.top();
     S.pop();
     for (const auto &v : P[w])
       delta[v] += ((double)sigma[v] / (double)sigma[w]) * (1.0 + delta[w]);
     if (w != s)
       betweenness[w] += delta[w] / 2;
}
printf("Completed BFS..\n");
clock_gettime(CLOCK_MONOTONIC, &end);
float max = -1.0;
// #pragma omp parallel for num_threads(40)
for(int i=0; i<freeIndex; i++) {
     if(graph[i].size() > 0 && betweenness[i]>0){
            printf("\nvertex %d: %f", vertices[i], betweenness[i] );
  if(betweenness[i] > max)
     max = betweenness[i];
```

Algorithm:

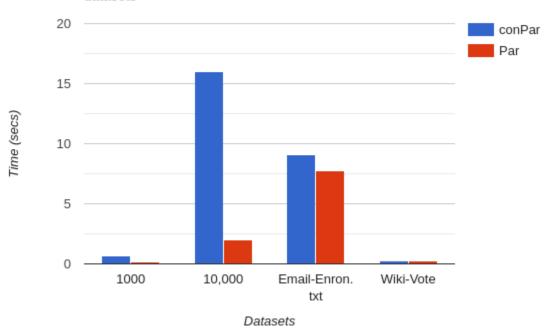
```
Algorithm Parallel Betweenness Centrality
Input Graph G = (V, E)
DECLARE r size := 10001
DECLARE c\_size := 30100
Begin
      Procedure parallelBC With BFS(Graph G, r size, c size)
             For each node s in G in Parallel do
                   DEFINE S AS stack
                   DEFINE d AS array
                                                                 //Distance vector
                   DEFINE Q AS queue
                                                                 //Queue for BFS
                   DEFINE sigma AS array
                   DEFINE P AS map of vector
                                                                 //Paths
                   For i:=0 To 10 in Parallel do
                                                          //Initialize BFS variables
                          D[i] := -1
                          Sigma[i] := 0
                   End For
                   Sigma[s] := 1
                   d/s] := 0
                   ENQUEUE Q := s
                   While Q is NOT empty do
                                                          //Perform BFS
                          v := FRONT \text{ of } Q
                          DEQUEUE Q
                          PUSH v INTO S
                          DECLARE mAS integer
                          If v + 1 \ge r_size then
```

```
m := c\_size
Else
       m := r/v+1
End if
For j:=r/v To r/v+1 do
                                  //Traverse neighbors of v
       W := c/i
      If d/w < 0 then
             PUSH w into Q
              d(w) := d(v) + 1
      End if
       //Update sigma value of w if path through v is shortest
      If d/w == d/v + 1 then
              Sigma[w] := sigma[w] + sigma[v]
             PUSH_BACK v into P/w]
       End if
End For
```

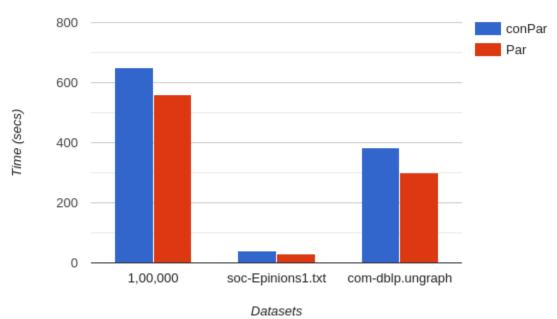




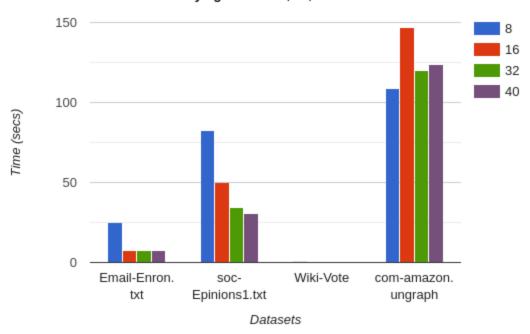
40 Threads Parallel vs ConQParallel comparison small datasets



40 Threads Parallel vs ConQParallel comparison larger datasets



Parallel with Varrying Threads 8, 16, 32 and 40



Parallel Concurrent Queue with Varrying Threads 8, 16, 32 and 40

