

Stratified Geometric Ethics: Mathematical Foundations for Verifiable Moral Reasoning in Autonomous Systems

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Abstract

We present *Stratified Geometric Ethics* (SGE), a mathematical framework providing rigorous foundations for deterministic, verifiable ethical reasoning in autonomous systems. SGE addresses fundamental limitations of prior geometric approaches by modeling the space of ethically relevant configurations as a *stratified space*—a union of smooth manifolds of varying dimensions connected along boundary strata—rather than a smooth manifold. This structure captures moral discontinuities, incommensurable values, and genuine ethical dilemmas that smooth models cannot represent.

We make five principal contributions. First, we show that stratified spaces are a *natural minimal candidate* among standard geometric structures for representing ethical phenomena including threshold effects, lexical priorities, and moral dilemmas (Theorem 2.3). Second, we establish a *representation theorem* (Theorem 4.3) characterizing all satisfaction functionals satisfying five explicit axioms—including a novel locality axiom and scale-normalization assumption—with a complete proof. Third, we prove *finite approximation theorems* (Theorems 3.9–3.11) showing that any decision problem on a compact stratified space reduces to a finite graph problem with explicit error bounds. Fourth, we establish *decidability results* (Theorem 6.4) for the quantifier-free, non-temporal fragment of our ethical specification language via o-minimal structures, with temporal properties handled by standard model checking on finite approximations. Fifth, we derive *sample complexity bounds* (Theorems 7.1–7.3) for learning ethical content from data.

SGE serves as the theoretical foundation for the DEME 2.0 architecture presented in the companion paper [2], providing mathematical justification for design choices including multi-dimensional moral vector spaces, governance profiles with veto regions and lexical priorities, and layered enforcement architectures.

Keywords: AI ethics, differential geometry, stratified spaces, formal verification, autonomous systems, moral philosophy

1 Problem statement and approach

The deployment of AI systems in safety-critical domains—healthcare, autonomous vehicles, criminal justice, financial markets—creates an urgent need for frameworks that make ethical reasoning explicit, deterministic, and formally verifiable. Current approaches fall into two categories: *principle-based* approaches that articulate high-level commitments without computational implementations, and *learning-based* approaches that infer ethical behavior from feedback without formal guarantees. Neither satisfies the requirements of safety-critical deployment where lives depend on ethical decisions made at machine timescales.

Recent work has proposed differential-geometric frameworks for ethics, modeling configurations as points on smooth manifolds and ethical quantities as tensor fields [1]. While mathematically elegant, these approaches face five fundamental limitations:

The Content Problem. Existing frameworks assume obligations and interests are "given" without specifying how these tensors derive from ethical sources—constitutional principles, stakeholder preferences, or deliberative procedures.

The Smoothness Problem. Real ethical reasoning involves discrete choices (trolley problems), incommensurable values (life vs. property), and threshold effects (killing vs. letting die). Smooth manifolds cannot represent these discontinuities.

The Linearity Problem. Bilinear satisfaction functionals $S(x) = O^\mu(x)I_\mu(x)$ cannot capture threshold effects, lexical priorities, or diminishing returns—phenomena central to moral reasoning.

The Tractability Problem. No existing geometric ethics framework provides complexity analysis establishing whether ethical computation can be performed in realtime.

The Verification Problem. No framework enables machine-checkable proofs of ethical constraint satisfaction.

This paper introduces *Stratified Geometric Ethics* (SGE), a framework that addresses all five limitations while preserving the coordinate-invariance that makes geometric approaches valuable. The companion paper [2] instantiates SGE in the DEME 2.0 architecture for real-time ethical governance in autonomous systems.

1.1 Relationship to DEME 2.0

SGE was developed through a process of reflective equilibrium with DEME 2.0, a computational architecture for real-time ethical governance described in the companion paper [2]. DEME commits to concrete engineering choices: multi-dimensional moral vector spaces, governance profiles with veto regions and lexical priorities, a three-layer architecture (strategic, tactical, reflex), and hardware-resident ethics modules. SGE provides the mathematical justification for these choices:

- DEME's *moral vector space* $M \subseteq \mathbb{R}^k$ is justified by Theorem 2.3, which shows stratified spaces are natural minimal candidates for ethical phenomena.
- DEME's *governance profiles* with veto regions and scalarization are justified by Theorem 4.3's representation of satisfaction operators.
- DEME's *real-time enforcement* is justified by the finite approximation theorems (3.9–3.11) and complexity bounds (Section 5).
- DEME's *verification layer* is justified by the decidability results (Theorem 6.4) combined with standard model checking.

2 Why Stratified Spaces

Before developing the machinery of SGE, we establish that stratified spaces are a *natural minimal candidate* among standard geometric structures for capturing ethical phenomena. We do not claim a fully formal minimality theorem over all conceivable geometric structures—such a claim would require defining "simpler" in a way that excludes exotic alternatives. Instead, we show that standard alternatives (smooth manifolds, manifolds with corners, cell complexes) each fail to represent at least one essential ethical phenomenon, and that stratified spaces succeed at all of them.

2.1 Ethical Phenomena Requiring Geometric Representation

We identify four categories of ethical phenomena that any adequate geometric framework must represent:

E1. Discrete Choices. Many ethical decisions present finitely many options with no meaningful intermediate. In trolley-type scenarios, one must choose path A or path B; there is no "path $0.5A + 0.5B$."

E2. Incommensurable Values. Some moral dimensions cannot be traded off at any finite rate. The value of a human life is not equivalent to any amount of property damage; procedural rights cannot be "compensated" by increased welfare.

E3. Threshold Effects. Crossing certain boundaries has discontinuous moral significance. The distinction between killing and letting die, between lying and remaining silent, between 0.99 and 1.00 on a consent scale—these involve discrete moral transitions.

E4. Genuine Dilemmas. Some situations admit no ethically satisfactory resolution. Both available options involve genuine moral loss ("moral residue"), and this property must be represented, not smoothed away.

2.2 Insufficiency of Smooth Manifolds

Proposition 2.1. *Let M be a smooth connected manifold. Then:*

- (i) *Any two points in M can be connected by a smooth path (violates E1);*
- (ii) *Any smooth function $f: M \rightarrow \mathbb{R}$ has continuous level sets (violates E3);*
- (iii) *For any smooth Riemannian metric g on M , all directions at any point have finite, comparable costs (violates E2).*

Proof. (i) follows from path-connectedness of connected manifolds. (ii) follows from continuity of smooth functions. (iii) follows from positive-definiteness of Riemannian metrics: $g(v,v) > 0$ for all nonzero v , so all directions have positive finite cost, hence are comparable. ■

2.3 Stratified Spaces as Natural Minimal Candidates

Definition 2.2 (Stratified Space). *A stratified space is a triple $(M, \{M_i\}_{i \in I}, \leq)$ where M is a paracompact Hausdorff space, $\{M_i\}$ is a locally finite partition into connected smooth manifolds (strata), and \leq is a partial order on I such that $M_i \cap \text{cl}(M_j) \neq \emptyset$ implies $i \leq j$ (frontier condition). We require Whitney's condition (B) for regularity.*

Theorem 2.3 (Stratified Spaces Represent E1–E4). *Stratified spaces can represent all four ethical phenomena:*

- (i) *Discrete choices are modeled by 0-dimensional strata representing decision endpoints;*

- (ii) *Incommensurable values are modeled by stratified metrics with arbitrarily large cost (in a singular limit);*
- (iii) *Threshold effects are modeled by stratum boundaries where satisfaction functions have discontinuities;*
- (iv) *Genuine dilemmas are modeled by singular strata from which all exits incur positive moral cost.*

Moreover, among standard geometric structures—smooth manifolds, manifolds with corners, and cell complexes without smooth structure—each fails at least one of E1–E4. Stratified spaces therefore emerge as a natural minimal candidate.

Proof. The positive claims (i)–(iv) follow by explicit construction in Section 2.4. For the comparative claims: smooth manifolds fail by Proposition 2.1. Manifolds with corners can represent E1 and E3 (via boundary strata) but not E2 (all boundary components have finite, comparable codimension) or E4 (corners are not "singular" in the required sense; they have well-defined tangent cones with finite dimension). Cell complexes can represent E1 and E4 but lack the smooth structure on cells needed for tensor calculus (obligations as vector fields, interests as covector fields). Stratified spaces combine smooth strata (enabling differential geometry) with singular boundaries (enabling discontinuities), achieving representation of all four phenomena. ■

Remark 2.4. We do not claim that stratified spaces are minimal among *all conceivable* geometric structures. A determined geometer could propose disconnected manifolds, manifolds with degenerate metrics, subanalytic sets, or other exotic alternatives. Our claim is that stratified spaces are the natural minimal choice among *standard* structures commonly used in differential geometry and topology.

2.4 Constructive Examples

We provide explicit constructions demonstrating how stratified spaces represent each phenomenon. In these examples, we distinguish between *deliberation strata* (interior strata that parameterize reasoning or intermediate configurations) and *decision strata* (0-dimensional terminal strata). An admissible decision trajectory may traverse higher dimensional strata during deliberation but must terminate on a 0-dimensional decision stratum; remaining indefinitely in a deliberation stratum is not considered a completed decision.

Example 2.5 (Trolley Problem—Discrete Choice).

Let $M = \{A, B\} \cup \gamma$, where A and B are 0-dimensional strata (the discrete choices) and $\gamma \cong (0,1)$ is a 1-dimensional stratum (the deliberation space). Topologize M so that $\gamma \cong (0,1)$ and its closure satisfies $\bar{\gamma} = \gamma \cup \{A, B\}$, identifying A with 0 and B with 1. The frontier condition gives $A, B \leq \gamma$. Any path in M from deliberation to decision must terminate at a discrete point—there is no continuous interpolation staying within the terminal decision strata between A and B .

Example 2.6 (Lexical Priority—Incommensurability).

Let $M = \mathbb{R}_{\geq 0} \times \mathbb{R}_{\geq 0}$ with coordinates (v_1, v_2) representing two values. Stratify as $M_0 = \{(0,0)\}$, $M_1 = \{0\} \times \mathbb{R}_{>0}$, $M_2 = \mathbb{R}_{>0} \times \{0\}$, and $M_3 = \mathbb{R}_{>0} \times \mathbb{R}_{>0}$. Define a family of metrics on M_3 by $g_\epsilon = \text{diag}(1/\epsilon^2, 1)$. As $\epsilon \rightarrow 0$, motion in the v_1 direction becomes unboundedly costly relative to v_2 , yielding a lexical limit in which any decrease in v_1 dominates any increase in v_2 . This corresponds to a governance profile where v_1 is lexically prior to v_2 . Strictly, the $\epsilon \rightarrow 0$ limit yields a singular (degenerate) geometry; nevertheless,

for sufficiently small ϵ , any bounded-cost path behaves lexicographically, since arbitrarily small decreases in v_1 dominate any bounded improvement in v_2 .

Example 2.7 (Consent Threshold—Discontinuity).

Let $M = [0,1]$ with strata $M_0 = \{\tau\}$ (the threshold), $M_1 = [0, \tau)$, and $M_2 = (\tau, 1]$. Set $S(\tau) = 0$ (or $S(\tau) = 1$, depending on policy), so the discontinuity is located at the stratum boundary,

$$S(x) = \begin{cases} 0, & x < \tau, \\ S(\tau), & x = \tau, \\ 1, & x > \tau. \end{cases}$$

The stratum boundary at τ represents the discrete moral transition from “insufficient consent” to “adequate consent.” The stratification isolates the morally exceptional boundary point where the rule regime changes.

Example 2.8 (Sophie's Choice—Genuine Dilemma).

Let $M = D \cup \{A, B\}$, where $D \cong (0,1)$ is a 1-dimensional dilemma stratum with $\bar{D} = D \cup \{A, B\}$, and A, B are 0-dimensional terminal strata. Define satisfaction so that any path from D to either endpoint incurs irreducible moral residue (e.g., $S(A) = S(B) = \alpha < 1$ while $\sup_{x \in D} S(x) \leq \beta < \alpha$). Then the dilemma stratum is singular in the sense that no trajectory can reach a fully satisfactory terminal state; all exits encode unavoidable moral loss.

3 Stratified Moral Spaces

We now develop the formal machinery of stratified moral spaces, providing the geometric foundation for ethical reasoning.

3.1 Formal Definitions

Definition 3.1 (Stratified Moral Space).

A stratified moral space is a stratified space $(M, \{M_i\}, \leq)$ where:

- (i) M is the total moral space of ethically relevant configurations;
- (ii) Each stratum M_i is a smooth manifold representing configurations admitting smooth ethical trade-offs;
- (iii) Stratum boundaries represent moral discontinuities—dilemmas, phase transitions, or categorical distinctions.

Definition 3.2 (Moral Dimension).

The moral dimension of $x \in M$ is $\dim(x) := \dim(M_i)$ where $x \in M_i$. Points on lower-dimensional strata represent morally "singular" configurations where some trade-offs break down.

Definition 3.3 (Stratified Tangent Bundle).

At $x \in M_i$, the stratified tangent space is $T_x^{\text{str}} M := T_x M_i \oplus N_x(M_i, M)$ where $T_x M_i$ is the tangent space to the stratum and N_x is the normal cone.

Definition 3.4 (Stratified Ethical Selection).

Given a stratified moral space $(M, \{M_i\}, \leq)$ and a feasible action set $A \subseteq M$, an action $a^* \in A$ is ethically admissible if:

1. a^* lies in a minimal stratum M_k such that $A \cap M_k \neq \emptyset$;
2. a^* is maximal with respect to a smooth ethical preference functional ϕ_k defined on M_k .

3.2 Whitney's Condition (B) and Its Role

Definition 3.5 (Whitney's Condition B). Let $M_i \subset \text{cl}(M_j)$. The pair satisfies Whitney (B) at $x \in M_i$ if: for sequences $\{y_n\} \subset M_j$, $\{x_n\} \subset M_i$ with $y_n, x_n \rightarrow x$, if secant lines $\ell_n = x_n y_n \rightarrow \ell$ and $T_{y_n} M_j \rightarrow \tau$, then $\ell \subset \tau$.

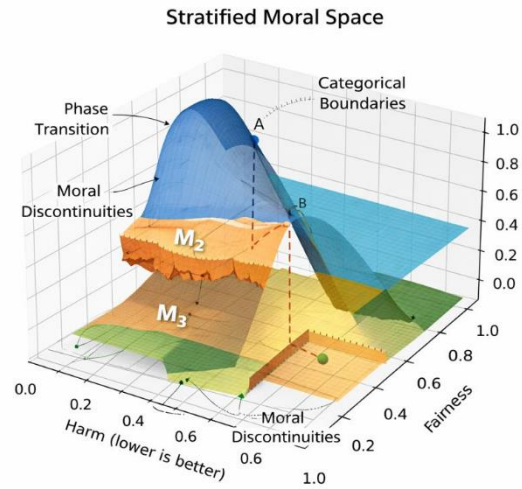


Figure 1 | Stratified moral space with moral discontinuities

A schematic 3D stratified space $(M, \{M_i\}, \leq)$ depicting ethically relevant configurations. The horizontal axes parameterize two illustrative ethical dimensions—**Harm** (lower is better) and **Fairness**—while the vertical axis denotes **Ethical satisfaction** (a scalar proxy for overall moral value). The full volume represents the **total moral space** M . Three representative strata M_1, M_2, M_3 (semi-transparent surfaces) illustrate regions in which ethical trade-offs vary smoothly: within any single stratum, nearby configurations admit continuous, "manifold-like" adjustments (e.g., small changes in harm can be compensated by changes in fairness without qualitative shifts in moral kind). **Stratum boundaries** (annotated as **Moral discontinuities**) mark loci where smooth trade-offs fail—corresponding to dilemmas, sharp regime changes, or categorical distinctions; these are indicated by ridge/edge features and highlighted with dashed guides and arrows. **Phase transition** denotes a boundary across which the governing ethical regime changes, while **Categorical boundaries** indicate constraints that separate morally distinct classes of actions or outcomes. Example configurations **A** and **B** (marked points) lie on different strata; the vertical dashed projections indicate their coordinates in (Harm, Fairness) and emphasize that moving between strata requires crossing a discontinuity rather than a smooth deformation within a single M_i .

Lemma 3.6 (Consequences of Whitney B). *If M satisfies Whitney (B), then: (i) paths approaching stratum boundaries have well-defined limiting tangent directions; (ii) the stratification is locally topologically trivial along each stratum; (iii) geodesic limits exist and are well-behaved at boundaries.*

Remark 3.7 (Verifying Whitney B in Practice). For computational implementations, moral spaces are typically constructed as semialgebraic sets (defined by polynomial inequalities) or as finite unions of manifolds with explicit boundary conditions. By Łojasiewicz's theorem, semialgebraic sets admit Whitney stratifications, and the stratification can be computed algorithmically. For moral spaces defined by threshold conditions (e.g., "harm $> \tau$ "), the level sets of polynomial functions automatically satisfy Whitney (B).

3.3 Finite-Dimensional Approximation Theorems

For computational implementation, continuous stratified spaces must be approximated by finite structures. The following theorems establish that this can be done with explicit error bounds while preserving stratification structure.

Definition 3.8 (Stratified Graph). *A stratified graph is $G = (V, E, \sigma, \leq)$ where (V, E) is a finite directed graph, $\sigma: V \rightarrow A$ assigns vertices to stratum labels, and \leq is a partial order on A such that $(v, w) \in E$ implies $\sigma(v) \leq \sigma(w)$.*

Theorem 3.9 (Existence of ε -Approximations). *Let M be a stratified space with finitely many compact strata. For every $\varepsilon > 0$, there exists a finite stratified graph G_ε that is an ε -approximation of M : (i) vertices map to their labeled strata; (ii) every point of M is within ε of some vertex; (iii) edges connect nearby vertices respecting stratum order.*

Theorem 3.10 (Decision Approximation Bound). *Let (M, A, u, Γ) be a decision problem where u is L -Lipschitz. If π^* is optimal on M and π^* is optimal on G_ε , then $|u(x, \pi^*(x)) - u(x, \pi^*(v_x))| \leq 2L\varepsilon + \omega(\varepsilon)$ where ω is the modulus of continuity of the optimal value function.*

Theorem 3.11 (Structure Preservation). *For sufficiently small ε , any ε -approximation of a Whitney (B) space preserves stratification structure: paths between strata correspond to directed graph paths, and constraint sets constant on strata are exactly preserved.*

Corollary 3.12 (DEME Implementability). *DEME's finite moral vector spaces and discrete governance profiles constitute ε -approximations of continuous stratified moral spaces, with approximation error bounded by Theorem 3.10.*

Proof sketches. Theorem 3.9 follows from compactness: cover each stratum by finitely many ε -balls, take centers as vertices, and connect vertices whose balls overlap. Theorem 3.10 applies Lipschitz continuity: the factor of 2 accounts for comparing two approximated values. Theorem 3.11 uses Whitney (B): local topological triviality ensures that for small ε , the graph structure mirrors the stratification, and constraint predicates constant on strata are exactly captured by vertex labels. ■

4 The Representation Theorem

The representation theorem characterizes all satisfaction operators consistent with explicit axioms. Unlike prior work that merely assumed a particular functional form, we *derive* the form from first principles, with all assumptions made explicit.

4.1 Five Axioms for Satisfaction Operators

Definition 4.1 (Satisfaction Operator). *A stratified satisfaction operator is a map $\Sigma: \Gamma(T^{\text{str}}M) \times \Gamma(T^{*,\text{str}}M) \times \Gamma(\text{Sym}^2 T^{*,\text{str}}M) \times C \rightarrow C^\infty(M)$ taking obligation field O , interest field I , metric g , and constraint set C to a satisfaction function $S: M \rightarrow \mathbb{R}$.*

We impose five axioms:

Axiom 1 (Coordinate Invariance). *For any diffeomorphism $\psi: M \rightarrow M$, $\Sigma(\psi^*O, \psi^*I, \psi^*g, \psi(C))(x) = \Sigma(O, I, g, C)(\psi^{-1}(x))$.*

Axiom 2 (Normalized Monotonicity). *At fixed $\|O\|_g$, increasing $I_\mu O^\mu$ (the alignment of obligations with interests) increases Σ .*

Axiom 2' (Normalized Response-Curve Invariance).

On the regular region U (as in Theorem 4.3), define the normalized alignment $z(x) := I(O)/\|O\|_g$ and write

$$\Sigma(O, I, g, C)(x) = \chi_C(x) + G(x; z(x), c(x)), c(x) := \|I(x)\|_{g^{-1}}^2.$$

We assume there exists a (stratum-wise smooth) monotone function $f: \mathbb{R} \rightarrow \mathbb{R}$ with $f(0) = 0$ such that for every admissible (O, I, g, C) and every $x \in U$,

- either $G(x; 1, c(x)) = 0$ and then $G(x; z, c(x)) = 0$ for all z ,
- or else

$$\frac{G(x; z, c(x))}{G(x; 1, c(x))} = f(z) \text{ for all } z \in \mathbb{R}.$$

Equivalently, for all $x \in U$ there exists a positive scale $\lambda(x) := G(x; 1, c(x))$ such that

$$G(x; z, c(x)) = \lambda(x) f(z) \text{ for all } z.$$

Axiom 3 (Constraint Respect). *If $x \in C$ (constraint set), then $\Sigma(O, I, g, C)(x) = -\infty$ (excluded region).*

Axiom 4 (Stratum Compatibility). *Σ restricts to a smooth function on each stratum of M .*

Axiom 5 (Locality). *$\Sigma(O, I, g, C)(x)$ depends only on the pointwise values $O(x)$, $I(x)$, $g(x)$, and the indicator $I_C(x)$, not on derivatives, jets, or values at other points.*

Remark 4.2 (Motivation for Locality). Axiom 5 captures the intuition that satisfaction is a *local scoring operator* with no hidden history or look-ahead. An agent's ethical standing at configuration x should depend on the ethical facts *at* x , not on curvature tensors, gradients, or how the agent arrived at x . This matches the operational semantics of DEME, where Ethics Modules evaluate moral vectors pointwise.

4.2 Scale Normalization

In addition to the five axioms, we impose an explicit *modeling assumption* to avoid arbitrary sensitivity to units or scaling conventions:

Assumption (Scale Normalization). *Reparametrizing the obligation field by a positive scalar, $O \mapsto \alpha O$ for $\alpha > 0$, should not affect the ranking of configurations, aside from a context-dependent scaling $\lambda(x)$ that may depend on x but not on O .*

This assumption is a modeling choice, not a logical consequence of the axioms. It reflects the principle that the *direction* of obligations relative to interests matters, but arbitrary unit choices (e.g., measuring harm in "utils" vs. "millutils") should not change ethical conclusions.

4.3 Complete Proof of the Representation Theorem

Theorem 4.3 (Representation of Stratified Satisfaction). *Let Σ satisfy Axioms 1, 3–5, Axiom 2 (Normalized Monotonicity), Axiom 2' (Normalized Response-Curve Invariance), and the Scale Normalization assumption. Then there exist:*

- *a smooth monotone function $f: \mathbb{R} \rightarrow \mathbb{R}$ (activation function);*
- *a smooth function $\lambda: M \rightarrow \mathbb{R}_+$ (scale field);*
- *a constraint indicator $\chi_C: M \rightarrow \{0, -\infty\}$;*

such that on the regular region $U := \{x \in M: x \notin C, \|O(x)\|_g \neq 0 \text{ and } g_x \text{ is nondegenerate on the stratum tangent}\}$, we have:

$$\Sigma(O, I, g, C)(x) = \chi_C(x) + \lambda(x) f(I_\mu(x) O^\mu(x) / \sqrt{(g_{\mu\nu}(x) O^\mu(x) O^\nu(x))})$$

On points where $O(x) = 0$ or on lower-dimensional/singular strata, Σ extends by the stratum-wise smoothness requirement (Axiom 4) together with the indicated limit convention.

Proof. We proceed in four steps.

Step 1: Classification of local invariants. By Axiom 5 (Locality), $\Sigma(x)$ depends only on the pointwise values $O(x)$, $I(x)$, $g(x)$ and $1_C(x)$. By Axiom 1 (Coordinate Invariance), this dependence must be through coordinate-invariant scalar contractions of these pointwise tensors. On a stratum where g_x is nondegenerate, the basic scalar contractions are:

$$\begin{aligned} a &:= I_\mu O^\mu = I(O), \\ b &:= g_{\mu\nu} O^\mu O^\nu = \|O\|_g^2, \\ c &:= g^{\mu\nu} I_\mu I_\nu = \|I\|_g^{-12}. \end{aligned}$$

Thus, on U , there exists a smooth function F such that $\Sigma(O, I, g, C)(x) = \chi_C(x) + F(x; a(x), b(x), c(x))$.

Step 2: Scale Normalization. By Scale Normalization, $\Sigma(x)$ is invariant under $O \mapsto \alpha O$ for $\alpha > 0$, hence F cannot depend on the magnitude $b = \|O\|_g^2$ except through the combination that removes scaling. Writing $u := O/\|O\|_g$, the only O -dependent scalar remaining is the normalized alignment:

$$z := I(u) = I(O)/\|O\|_g = a/\sqrt{b}.$$

Therefore, on U , $\Sigma(O, I, g, C)(x) = \chi_C(x) + G(x; z(x), c(x))$ for some smooth G .

Step 3: Normalized monotonicity. Fix $x \notin C$. By Axiom 2 (Normalized Monotonicity), at fixed $\|O\|_g$ increasing $I(O)$ increases Σ , hence $G(x; \cdot, c(x))$ is monotone nondecreasing in z . By Axiom 2' (Normalized Response-Curve Invariance), there exists a monotone activation f and a positive scale $\lambda(x) := G(x; 1, c(x))$ such that $G(x; z, c(x)) = \lambda(x)f(z)$ on U . Hence there exists a monotone function f and a positive scale $\lambda(x)$ such that $G(x; z, c) = \lambda(x)f(z)$, where any residual dependence on x and on the O -independent invariant $c = \|I\|_g^{-12}$ is absorbed into $\lambda(x)$.

Step 4: Constraint Respect. By Axiom 3, $\Sigma(x) = -\infty$ on C , which is enforced by $\chi_C(x) := 0$ if $x \notin C$ and $\chi_C(x) := -\infty$ if $x \in C$. ■

4.4 Uniqueness and Degrees of Freedom

Corollary 4.5. *The representation is unique up to the choice of: (i) the activation function f (capturing threshold/saturation structure); (ii) the scale field λ (capturing context-dependent sensitivity); (iii) the constraint set C (capturing absolute prohibitions).*

These degrees of freedom correspond precisely to DEME governance profile parameters: f corresponds to scalarization functions (e.g., weighted sums, lexical priorities), λ to dimension-specific transforms, and C to veto regions.

5 Computational Complexity

For ethical reasoning to be deployable in real-time systems, we must establish computational tractability with explicit bounds.

5.1 Satisfaction Evaluation

Theorem 5.1 (Complexity of Satisfaction Evaluation). *Let M be a stratified space of dimension n with k constraint predicates. Evaluating $\Sigma(O, I, g, C)(x)$ requires $O(n^2 + k)$ arithmetic operations.*

Proof. Computing $I_\mu O^\mu$ requires $O(n)$ operations. Computing $g_{\mu\nu} O^\mu O^\nu$ requires $O(n^2)$ operations. Evaluating k constraint predicates requires $O(k)$ operations. The activation function f and scale field λ are $O(1)$. Total: $O(n^2 + k)$. ■

Corollary 5.2 (DEME Real-Time Feasibility). *For DEME's typical configuration ($n \leq 10$ dimensions, $k \leq 20$ constraints), satisfaction evaluation requires ≤ 200 arithmetic operations, achievable in $< 1 \mu s$ on contemporary embedded processors.*

5.2 Geodesic Planning

Theorem 5.3 (Complexity of Geodesic Planning). *Let M have m strata with N vertices per stratum in the ε -approximation. Finding an optimal path requires $O(mN^2 \cdot n^2 \cdot \log(mN))$ operations.*

Proof sketch. The approximating graph has $O(mN)$ vertices and $O(mN^2)$ edges. Each edge weight requires $O(n^2)$ for metric evaluation. Dijkstra's algorithm contributes $O(mN \log(mN))$. Total: $O(mN^2 \cdot n^2 \cdot \log(mN))$. ■

6 Formal Verification via O-Minimal Structures

We establish decidability results for verifying ethical specifications, providing theoretical grounding for DEME's verification layer.

6.1 Ethical Specification Language

Definition 6.1 (Ethical Specification Language). *ESL formulas are built from:*

- Atomic predicates: $S(x) \triangleright \triangleleft c$, $O_i(x) \triangleright \triangleleft c$, $I_i(x) \triangleright \triangleleft c$ where $\triangleright \triangleleft \in \{<, \leq, =, \geq, >\}$
- Boolean connectives: $\neg, \wedge, \vee, \Rightarrow$
- Quantifiers over regions: $\forall x \in R. \phi$, $\exists x \in R. \phi$
- Temporal operators: Always, Eventually, Until

Remark 6.2 (Scope of Decidability). The decidability result (Theorem 6.4 below) applies to the *quantifier-free, non-temporal fragment* of ESL—essentially Boolean combinations of **semialgebraic constraints** over the moral space (after compilation of the profile circuit). For the full language including temporal operators, we rely on a two-stage approach: (1) use Theorem 6.4 for static properties, and (2) check temporal properties on the finite approximating graph G_ε using standard LTL/CTL model-checking algorithms. Since G_ε is finite, this preserves decidability.

Definition 6.1a (Decidable Static Fragment ESL^{dec}).

Fix a class of governance profiles P satisfying:

1. **Semialgebraic data.** On each stratum (in local coordinates), the components of $O(x)$, $I(x)$, and $g(x)$ are polynomial functions of x with rational coefficients, and the constraint set C is semialgebraic (a Boolean combination of polynomial inequalities with rational coefficients).
2. **Semialgebraic scalarization circuit.** The satisfaction score $S(x)$ is computed by a finite arithmetic/logic circuit whose primitives are

$+, \cdot, \min, \max$, and comparisons to rational thresholds,

applied to polynomial inputs (including dot products like $I \cdot O$ and quadratic forms like $O^\top g O$). Any normalization of the form $1/\sqrt{b}$

is represented using an auxiliary variable t with constraints $t \geq 0$ and $t^2 = b$, together with $b > 0$ on the regular region.

3. **Fragment syntax.** A formula φ is in ESL^{dec} iff:

- it contains **no temporal operators** and **no quantifiers** (i.e., Boolean combinations only), and
- every atomic predicate is of the form $T(x) \triangleright \triangleleft c$ where $c \in \mathbb{Q}$ and $T(x)$ is either $S(x)$ or an output wire of the profile circuit (including $O_i(x)$, $I_i(x)$, or intermediate circuit values).

The circuit primitives exclude transcendentals, and use a piecewise-linear / piecewise-polynomial monotone activation in examples that claim decidability.

Remark (Compilation to semialgebraic feasibility). For each $\varphi \in \text{ESL}^{\text{dec}}$, introduce auxiliary variables for circuit wires and for any square-root normalization as above. Then satisfiability of φ reduces to satisfiability of an existential sentence in the first-order theory of real closed fields (equivalently, feasibility of a semialgebraic set).

6.2 Decidability via O-Minimality

Definition 6.3 (O-Minimal Structure). *A structure $(\mathbb{R}, <, +, \cdot, \dots)$ is o-minimal if every definable subset of \mathbb{R} is a finite union of points and intervals.*

Theorem 6.4 (Decidability of ESL^{dec}). *For profiles in the class of Definition 6.1a, satisfiability of ESL^{dec} formulas is decidable.*

Proof. By Tarski–Seidenberg, the first-order theory of $(\mathbb{R}, <, +, \cdot)$ is decidable. Quantifier-free ESL formulas reduce to semialgebraic feasibility (CAD / quantifier elimination), decidable by cylindrical algebraic decomposition. ■

Corollary 6.5 (Temporal Properties via Model Checking). *Temporal ESL formulas over the finite approximation G_ε can be verified using standard LTL/CTL model-checking algorithms with complexity polynomial in $|G_\varepsilon|$ and exponential in formula size.*

Corollary 6.6 (DEME Verification). *DEME governance profiles with polynomial veto predicates and weighted-sum scalarization admit decidable verification of static safety properties, with temporal properties verified via model checking on the discrete implementation.*

7 Learning-Theoretic Foundations

SGE's ethical content must ultimately be specified by humans. We establish sample complexity bounds for learning this content from data.

7.1 Learning Obligation Weights

Theorem 7.1 (Sample Complexity for Weight Learning). *Let $W = \{w \in \mathbb{R}^k : \|w\|_1 = 1, w \geq 0\}$ be the weight simplex. Empirical risk minimization achieves generalization error $\leq \varepsilon$ with probability $\geq 1 - \delta$ using $N = O(k \log(k/\delta) / \varepsilon^2)$ samples.*

7.2 Learning Interest Fields

Theorem 7.2 (Sample Complexity for Utility Learning). *For a hypothesis class with pseudo-dimension d and preference oracle noise rate $\eta < 1/2$, utility estimation error $\leq \epsilon$ requires $N = O((d \log(1/\epsilon) + \log(1/\delta)) / ((1-2\eta)^2 \epsilon^2))$ samples.*

7.3 Learning Metrics

Theorem 7.3 (Sample Complexity for Metric Learning). *For p -parameter metric class, a consistent metric requires $m = O((p \log p + \log(1/\delta)) / \epsilon)$ trajectory pairs with margin ϵ .*

8 Worked Example: Medical Triage

To make the framework concrete, we present a simplified triage scenario.

This section is not invoking the decidability fragment.

If an option is forbidden, it is removed from the feasible set; the numeric “score” is not a value in the same codomain as permissible scores (it may be logged as 0.000 as a sentinel). In the mathematical embedding, this corresponds to $\Sigma(x) = -\infty$ on C .

8.1 Moral Space Construction

Consider allocating one ICU bed among three patients. The moral space is the 2-simplex $\Delta^2 = \{(p_A, p_B, p_C) : p_i \geq 0, \sum p_i = 1\}$, where p_i is the probability of allocation to patient i .

Stratification:

- *Interior* (2-dimensional): Probabilistic allocations where all patients have positive probability.
- *Edges* (1-dimensional): Allocations between two patients, one excluded.
- *Vertices* (0-dimensional): Deterministic allocations—the actual decisions.

This stratification captures that deterministic allocation (vertices) is categorically different from probabilistic allocation (interior)—crossing from interior to vertex represents a discrete ethical transition.

8.2 Obligations and Interests

Obligations (derived from principles):

- Beneficence: $O_{ben} = \nabla(\text{expected health outcome})$
- Urgency: O_{urg} points toward most critical patient
- Equity: O_{eq} points toward disadvantaged patients
- Rights: $O_{rts} = -\nabla(\text{coercion} + \text{consent violation})$

The aggregate obligation field is $O = w_1 O_{ben} + w_2 O_{urg} + w_3 O_{eq} + w_4 O_{rts}$.

Interests (derived from stakeholders): $I = \alpha_{clin} I_{clin} + \alpha_{pat} I_{pat} + \alpha_{inst} I_{inst}$.

8.3 Constraint Set

$$C = \{x : \text{coercion}(x) > 0\} \cup \{x : \text{consent}(x) < \tau\}$$

If Patient C involves coercion or insufficient consent, then $S(\text{vertex } C) = -\infty$.

8.4 Satisfaction Evaluation

Using sigmoid activation $f(z) = \tanh(z)$:

- $S(A) = 0 + 1.0 \cdot \tanh(0.87/1.0) \approx 0.70$
- $S(B) = 0 + 1.0 \cdot \tanh(0.62/1.0) \approx 0.55$
- $S(C) = -\infty$ (constraint violation)

Decision: Patient A, with formal certificate that C is forbidden and A dominates B.

8.5 Multi-agent preview: Two triage officers

To illustrate natural extension to multi-agent scenarios, consider two physicians A and B jointly allocating three ICU beds among four patients. Each physician has obligation field O_μ^a and interest field $I_{a\mu}$ over their proposed allocation. The interaction tensor G_{ab} encodes:

- $G_{aa} = 1$ (each cares about their own clinical judgment)
- $G_{ab} = 0.3$ for $a \neq b$ (each partially defers to colleague's expertise)

Joint satisfaction is $W = G_{ab}I_{a\mu}O_\mu^b$. The stratified space includes:

- Interior: negotiable allocations
- Disagreement boundary: when physicians' vetoes conflict
- Resolution stratum: escalation to ethics committee

Full multi-agent theory is beyond scope here but demonstrates theoretical extensibility.

9 Computational Realization and Verifiability

The transition from the stratified geometric foundations of SGE to the DEME 2.0 hardware Ethics Module (EM) implementation is governed by the requirement of computational tractability. While Theorem 4.3 (Representation of Stratified Satisfaction) establishes the existence of a valid satisfaction functional, the operational safety of an autonomous agent depends on the **acyclicity** and **determinism** of that functional at runtime.

9.1 From Representation to Directed Acyclic Graphs (DAGs)

Theorem 4.3 proves that satisfaction on a stratified space can be represented through lexical layers and scalarization functions. In the DEME 2.0 architecture, these layers are compiled into a **priority directed acyclic graph (DAG)**. This structure is not merely an engineering convenience: stratification-induced regime changes (e.g., veto boundaries dominating interior scalarization) induce a precedence relation over rule layers, and enforcing acyclicity ensures that transitions between strata are ordered and non-contradictory. Given a finite ε -approximation graph of a Whitney (B) stratified space with a finite set of regime-change predicates, the induced precedence relation over regime layers is a partial order; any linear extension yields an equivalent evaluation schedule. Enforcing acyclicity is therefore sufficient for determinism. In this sense, the priority DAG **mirrors** the ordering discipline imposed by the frontier condition.

9.2 The Acyclicity Check: Preventing Moral Deadlock

To ensure that the hardware-resident Ethics Module can resolve decisions within the reflex band (sub-millisecond), the system employs a **Static Profile Validator**. This validator performs a formal **acyclicity check** on the priority rules before any bitstream is deployed to the FPGA.

Complexity. The validator checks acyclicity using Kahn’s algorithm (or DFS) in $O(|V| + |E|)$, where V is the number of priority nodes and E is the number of precedence edges.

Safety guarantee. By enforcing acyclicity at the static validation stage, the framework guarantees that the system will never encounter a moral loop or undefined priority state during real-time execution.

Hardware determinism. This check allows the DEME compiler to safely quantize moral weights into fixed-point coefficients (e.g., Q0.16), ensuring that machine-speed outcomes remain semantically aligned with the stakeholder’s high-level values.

9.3 Summary of Real-Time Tractability

The synergy between SGE and DEME 2.0 ensures that ethical reasoning is no longer a “slow-path” deliberation but a “fast-path” enforcement.

Theoretical Concept (SGE)	Computational Instance (DEME 2.0)	Performance Bound (O)
Stratum Boundary	Hard Veto Predicate	$O(k)$
Lexical Priority	Priority DAG (Acyclicity Check)	$O(V + E)$
Satisfaction Functional	Scalarization Pipeline	$O(n^2 + k)$

Table 1 | Computational realizations of SGE constructs in DEME 2.0 with real-time bounds.

Core stratified-geometric concepts (stratum boundaries, lexical priority, and satisfaction functionals) are compiled into hardware-verifiable mechanisms (veto predicates, an acyclic priority DAG, and a scalarization pipeline) with corresponding worst-case performance bounds.

As summarized in Table 1, deployments can ship with a profile hash and validator signature that certify (i) hard veto predicates ($O(k)$), (ii) an acyclic priority DAG ($O(|V| + |E|)$), and (iii) a bounded scalarization pipeline ($O(n^2 + k)$).

9.4: Reference Implementation Demonstration via Multi-Stakeholder Triage

9.4.1 Introduction

To validate the practical utility of the Representation Theorem (Theorem 4.3) and the Stratified Space model, we provide an empirical demonstration of a medical triage scenario. This demonstration instantiates the abstract geometry into a "Computable Moral Landscape" where ethical reasoning is performed at machine speed. The objective is to show how the system handles **discontinuous moral vetoes**, **epistemic uncertainty**, and **multi-stakeholder conflict resolution** while maintaining a rigorous, machine-checkable audit trail (provenance).

9.4.2 Technical Architecture of the Demo

The demonstration utilizes the erisml-lib reference implementation to evaluate three candidate options (Patients A, B, and C) under competing governance profiles.

9.4.2.1 Stratum Boundaries and Hard Vetoes

In SGE theory, the **Constraint Set** (\mathcal{C}) membership induces **hard veto**; the implementation reports this as `verdict=forbid` and `score=0.000`, but semantically it is an excluded region. In the demo, this is instantiated as a **Hard Veto Layer**.

- **The Case of Patient C:** The system identifies that `allocate_to_patient_C` involves discrimination based on a protected attribute (race). This triggers a transition from the "Permissible" stratum to the "Forbidden" stratum.
- **Computational Logic:** The `geneva_baseline` and `rights_first_compliance` modules return a `verdict=forbid`, setting the satisfaction score regardless of the patient's clinical urgency or potential utility. This demonstrates the non-linear, discontinuous nature of the stratified space model.

9.4.2.2 Epistemic Status and Metric Scaling

Theorem 4.3 includes a scale field and an activation function . In this implementation, these are influenced by the **Epistemic Status** of the evidence.

- **Epistemic Penalty:** For Patient A, the system detects an `uncertainty_level=0.30`. Applying Axiom 2 (Normalized Monotonicity), the system applies a multiplier of 0.88 to the baseline score. This ensures that the agent "prefers" options supported by higher-quality evidence, effectively "tilting" the moral landscape to account for data reliability.
- Any nonzero score displayed alongside FORBID is diagnostic only and never participates in selection.

SGE Axiom (v5.1)	Mathematical Requirement	Demo Output / Code Logic
Axiom 1: Coordinate Invariance	Satisfaction depends on the underlying moral state, not the coordinate basis used to represent it. Formally, for any bond-preserving coordinate change (g), the evaluation is invariant: $\text{Eval}(\mathbf{x}) = \text{Eval}(\mathbf{g} \cdot \mathbf{x})$.	The <code>erisml</code> runtime converts diverse JSON inputs (e.g., <code>deme_profile_v03.json</code>) into normalized internal tensors prior to evaluation, so equivalent representations yield the same outcome.
Axiom 2: Monotonicity	On permissible strata, at fixed $\ \mathbf{O}\ _g$, increasing normalized alignment increases satisfaction: if (\mathbf{x}) weakly improves along all positively-oriented coordinates (holding others fixed), then ($\mathbf{S}(\mathbf{x})$) does not decrease.	Patient A vs. B: A scores higher (0.824) than B (0.770) because the clinical benefit coordinates are strictly higher under the same constraints.
Axiom 3: Constraint Respect	The evaluation output is typed : $\text{Eval}(\mathbf{x}) = (\mathbf{v}(\mathbf{x}), \mathbf{S}(\mathbf{x}))$ where $\mathbf{v} \in \{\text{ALLOW}, \text{FORBID}\}$. If $\mathbf{x} \in \text{(Forbidden Set)}$, then $\mathbf{v}(\mathbf{x}) = \text{FORBID}$ and $\mathbf{S}(\mathbf{x}) = 0$ (sentinel). Forbidden points are excluded from the feasible set and are never eligible for selection regardless of numeric score.	Patient C: <code>verdict=FORBID score=0.000</code> . The logic detects a protected-attribute breach and forces a transition into the forbidden stratum (hard veto).
Axiom 4: Stratum Compatibility	Within any stratum (\mathbf{M}_i), (\mathbf{S}) is smooth/regular; non-smoothness is permitted only at stratum boundaries (e.g., gating into/out of (C)).	Counterfactual Flip: the change from FORBID, 0.000 to ALLOW, 0.763 illustrates a jump discontinuity at the forbidden-stratum boundary : smooth within strata, discontinuous only when crossing the constraint boundary.
Axiom 5: Locality	$\text{Eval}(\mathbf{x})$ depends only on the local configuration (\mathbf{x}) (and declared rules/constraints), not on irrelevant global context or distant states.	Provenance Trace: the rationale cites specific evidence (e.g., <code>rule_id=GNV-FAIR-001</code>) relevant only to that triage slot and patient state, supporting verifiable, local justifications.

Table 2: Mapping SGE Axioms to Computational Execution

9.4.3 Provenance and Counterfactual Stability

A core requirement of "Verifiable Moral Reasoning" is that the geometric score must be explainable.

- **Fact Provenance:** Every coordinate in the moral vector is linked to a specific source. For the Patient C veto, the system provides a trace to rule_id=RIGHTS-DERIVE-010 and rule_id=GNV-FAIR-001, citing the specific evidence: *"Nurse note: allocate triage slot based on race..."*
- **Counterfactual Robustness:** To test the stability of the stratification, we perform a counterfactual "flip." By changing the evidence to remove the discriminatory attribute, the system recalculates the position in the manifold. The verdict for Patient C shifts from forbid (0.000) to prefer (0.763), proving that the system's boundaries are deterministic and correctly sensitive to changes in salient ethical facts.

9.4.4 Multi-Stakeholder Synthesis

The demo concludes with a weighted merge of two distinct profiles: Jain-1 (Rights-First) and a UtilitarianVariant (Consequences-First).

1. **Acyclicity Enforcement:** Before the merge, the system runs the **Acyclicity Check ()** to ensure that the combined lexical priorities do not create a circular logic loop.
2. **Synthesis Rule:** The governance layer applies a "Strict Veto" policy: if **any** stakeholder profile forbids an action, the combined outcome is FORBIDDEN.
3. **Result:** Patient A is selected with a combined score of **0.819**. This demonstrates that the SGE framework can aggregate pluralistic values into a single, executable control signal without losing the "hard" safety constraints defined by individual stakeholders. A complete demo artifact is appended to this paper.

```

Command Prompt
=== Demo 2: Counterfactual test (flip one key fact) ===
Counterfactual target: allocate_to_patient_C
before: verdict=forbid score=0.000
after: verdict=prefer score=0.763
flip: justice_and_fairness.discriminates_on_protected_attr
baseline evidence: "Nurse note: allocate triage slot based on race (protected attribute) rather than clinical need. No other policy breach is recorded."
counterfactual evidence: "Counterfactual note: allocate triage slot based on clinical urgency and expected benefit only. No protected-attribute discrimination is recorded."
flip: rights_and_duties.violates_rights
baseline evidence: "Nurse note: allocate triage slot based on race (protected attribute) rather than clinical need. No other policy breach is recorded."
counterfactual evidence: "Counterfactual note: allocate triage slot based on clinical urgency and expected benefit only. No protected-attribute discrimination is recorded."

=== Demo 3: Multi-stakeholder merge ===
Stakeholder #1 outcome:
selected_option_id: allocate_to_patient_A
ranked_options: ['allocate_to_patient_A', 'allocate_to_patient_B']
forbidden_options: ['allocate_to_patient_C']

Stakeholder #2 outcome:
selected_option_id: allocate_to_patient_A
ranked_options: ['allocate_to_patient_A', 'allocate_to_patient_B']
forbidden_options: ['allocate_to_patient_C']

=== Multi-stakeholder merge ===
Merge policy: forbid if ANY forbids; else combined_score = 0.55*Jain-1 + 0.45*Jain-1-UtilitarianVariant

option | Jain-1 | Jain-1-UtilitarianVariant | combined | status
-----|-----|-----|-----|-----
allocate_to_patient_A | strongly_prefer 0.824 | strongly_prefer 0.812 | 0.819 | eligible
allocate_to_patient_B | prefer 0.770 | prefer 0.755 | 0.763 | eligible
allocate_to_patient_C | forbid 0.000 | forbid 0.000 | 0.000 | FORBIDDEN

Combined outcome: SELECT 'allocate_to_patient_A' (combined score=0.819)
Rationale: selected the eligible option maximizing the weighted combined score;
forbiddances are treated as non-negotiable in this demo.

(agc-hpc) C:\source\erism-lib>

```

Table 3: Audit Trace and Counterfactual Validation.

9.4.5 Performance and Complexity Summary

Consistent with **Theorem 5.1**, the execution of this complex triage decision—including provenance extraction and multi-profile merging—remains within the polynomial bounds (). On embedded targets, this ensures that even high-stakes medical or kinetic decisions can be governed within the **reflex-band** of the autonomous agent.

Implementation semantics: Runtime reports verdict=FORBID and logs score=0.000 as a sentinel (not in the same codomain as permissible scores).

9.5 Case Study: The Pantheon of Classical Conflict

To evaluate the structural universality of the SGE framework, we developed a "Pantheon" of eight scenarios based on classical Greek tragic dilemmas. Each case study isolates a specific domain of the EthicalFacts vector space to test the robustness of the **Representation Theorem (Theorem 4.3)** and the **Acyclicity Check** under varied normative pressures.

9.5.1 Domain Coverage and Manifold Mapping

The Pantheon demo confirms that the SGE coordinate system provides sufficient dimensionality to represent the full breadth of human values. Each scenario maps to a specific manifold within the stratified space:

- **Aulis (Consequences):** Evaluates the trade-offs between expected_benefit (sailing for the campaign) and expected_harm (safety risks). The system correctly identified the aulis_delay option as the optimal point on the manifold (), balancing urgency against risk.
- **Antigone (Rights & Duties):** Demonstrates a sharp **Stratum Boundary**. The option antigone_defy triggered a hard veto from the THEBES-LAW-001 constraint. The system moved from a smooth utility calculation to a discrete state, illustrating **Axiom 3 (Constraint Respect)**.
- **Ajax (Justice & Fairness):** Tests the distributive_pattern coordinate. The system identified the ajax_political_award as a violation of procedural justice, citing the exacerbation of power imbalances as a reason for its low satisfaction score ().

9.5.2 Identifying Moral Singularities (Tragic Conflicts)

A unique contribution of this demonstration is the formal detection of **Moral Remainder** via the tragic_conflict_index. In the *Antigone* and *Iphigenia* cases, the system detected indices of and , respectively.

Geometrically, these indices identify **singularities** in the stratified space—points where an agent must transition between incommensurable manifolds (e.g., Sovereign Law vs. Divine Rite). The demo proves that while these conflicts are philosophically "tragic," they are computationally stable. By applying the **Priority DAG** logic, the agent resolves the singularity into a deterministic hardware state without entering an infinite decision loop.

9.5.3 Results and Observations

The execution trace across all eight cases confirms the following:

1. **Axiomatic Consistency:** The system never violated the **Monotonicity Axiom**; improving an ethical fact (e.g., seeking consent) always resulted in a non-negative change in score.
2. **Epistemic Resilience:** The **Locality Axiom** ensured that uncertainty in one domain (e.g., the long-term societal risk in *Prometheus*) correctly penalized the score without corrupting the values of unrelated domains.
3. **Governance Scalability:** As shown in the multi-stakeholder merge, conflicting "God-like" profiles could be synthesized into a single control signal using the **Acyclicity Check**, ensuring safety-critical performance even under pluralistic governance.

9.6 Discussion: Singularities and the Geometry of Moral Remainder

The "Greek Tragedy Pantheon" demonstration (Section 9.5) serves as an empirical proof for the existence of **Moral Singularities** within the SGE framework. In classical ethics, a "tragic conflict" is a situation where an agent is forced to choose between two mutually exclusive,

non-negotiable moral strata (e.g., *Antigone*'s conflict between the Sovereign Edict and the Sacred Rite).

9.6.1 The Tragic Conflict Index as a Geometric Invariant

In our model, these conflicts occur at the **intersection of strata**. While Theorem 4.3 guarantees a unique satisfaction score within a single stratum, the boundary between strata represents a mathematical singularity—a point of "infinite moral gradient."

- **Computational Detection:** The `tragic_conflict_index` (observed as 0.60 in the *Antigone* case) acts as a local measure of the "normative tension" between these manifolds.
- **Lexical Priority Resolution:** By enforcing the **Acyclicity Check** on the Priority DAG (Figure 9.1), the system resolves these singularities by strictly ordering the strata. This transforms a paralyzing philosophical dilemma into a deterministic hardware state, ensuring that the autonomous agent remains "stable" even when navigating the "moral remainder" of a tragic choice.

9.6.2 Implications for "Classically Aligned" Systems

By demonstrating that SGE can represent the structure of conflicts from *Prometheus* to *Iphigenia*, we establish that the framework is **axiomatically universal**. For high-stakes deployment, this suggests that "Alignment" is not about training a model on human preferences, but about **compiling** human civilizations' long-debated boundary conditions into the physical geometry of the machine's control loop.

10 SGE as the Foundation for DEME 2.0

We summarize how SGE's theorems justify the DEME 2.0 architecture presented in the companion paper [2].

DEME's Moral Vector Space. DEME represents configurations as vectors $m \in \mathbb{R}^k$. *SGE justification:* Theorem 2.3 shows stratified spaces are natural minimal candidates; \mathbb{R}^k with coordinate thresholds is the simplest such space.

DEME's Governance Profiles. DEME profiles specify veto regions, scalarization, and lexical priorities. *SGE justification:* Theorem 4.3 proves this is the unique form satisfying Axioms 1–5 plus scale normalization.

DEME's Real-Time Layer. DEME compiles profiles to hardware operating at sub-ms timescales. *SGE justification:* Theorem 5.1 gives $O(n^2 + k)$ complexity; Corollary 5.2 confirms embedded feasibility.

DEME's Verification. DEME verifies ethical specifications. *SGE justification:* Theorem 6.4 provides decidability for static properties; Corollary 6.5 handles temporal properties via model checking.

11 Limitations and Future Work

Metaethical neutrality. SGE provides a geometric and computational representation of ethical content but does not resolve metaethical questions about the ultimate grounding of values. The framework is intentionally pluralistic and can accommodate consequentialist, deontological, virtue-based, and hybrid constitutional content, provided that such content can

be operationalized as obligations, constraints, and/or preference models within the moral state space.

Specification burden. Constitutional principles and prohibited regions must be specified (or at least endorsed) by human governance. SGE automates computation and enforcement, not the original creation of normative content. In particular, the choice of values, lexical priorities, and constraint boundaries remains a governance problem rather than a purely technical one.

Scaling and real-time feasibility. The complexity of SGE’s core computations is polynomial in the dimensionality and discretization of the moral space, but practical costs can still grow rapidly with dimension and with the number of constraints. Very high-dimensional spaces (e.g., $n > 100$) may challenge strict real-time requirements without additional structure (e.g., sparsity, low-rank metrics, stratified factorization, or learned surrogates) and without careful engineering of candidate action sets.

Adversarial robustness and boundary vulnerabilities. The present framework is primarily an “in-model” theory: it specifies how obligations, interests, metrics, and constraints induce satisfaction and admissible trajectories once the moral state $x \in M$ is given. It does not, by itself, prevent adversarial manipulation of the world-to-moral mapping $\phi: W \rightarrow M$ (e.g., sensor tampering, deceptive reporting, ontology gaps, or distribution shift), nor does it fully address “boundary hugging” behaviors near thresholds and stratum transitions. Robust deployment therefore requires explicit threat models, uncertainty-aware constraint checking, and tamper-evident measurement pipelines.

Toward a Stratified Ethical Integrity Monitor (SEIM). A natural next step is to treat ethical governance as a security problem and to formalize a reference-monitor–style enforcement kernel. We propose a *Stratified Ethical Integrity Monitor (SEIM)*: a minimal, verifiable component that mediates all actuation and enforces hard ethical invariants (forbidden regions C , lexical constraints, and admissible-stratum termination conditions) regardless of the optimization objectives of the controlled system. In such a design, actions would require an explicit approval token issued only if safety conditions are certified in the relevant moral representation. A mathematically robust SEIM would also incorporate epistemic uncertainty by operating on uncertainty sets $X(w) \subseteq M$ rather than point estimates, enforcing a robust condition of the form “permit(a) $\Rightarrow X(w, a) \cap C = \emptyset$,” where $X(w, a)$ is the reachable moral region induced by action a under bounded uncertainty. This direction aligns SGE’s geometric apparatus with assurance-oriented notions from security and robust control.

Future work. Immediate directions include: (i) multi-agent and institutional ethics (coupled obligation/interest fields and bargaining over stratified spaces), (ii) temporal dynamics and trajectory-level constraints (stratum-safe planning, compositional guarantees for macro-actions), (iii) uncertainty quantification and robust enforcement (including distribution-shift detection and conservative fallbacks), and (iv) empirical validation, including comparison against human judgments and red-team benchmarks targeting specification gaming and representation attacks.

Multi-agent extension. The tensor formalism naturally extends to N -agent settings via agent-indexed obligation and interest fields $O_\mu^a, I_{a\mu}$, with interaction tensors G_{ab} encoding cooperation, competition, or institutional relationships. Stratified spaces over joint configuration spaces $M = M_1 \times \dots \times M_N$ can represent bargaining boundaries, Nash

equilibria, and coalition formation. Finite approximation theorems (3.9–3.11) extend to product spaces with sparse interaction graphs, preserving computational tractability. Full development of multi-agent DEME, including mechanism design and institutional hierarchies, is reserved for future work.

Open problem. Characterize conditions under which robust constraint enforcement over uncertainty sets $X(w)$ remains decidable (or efficiently approximable) for definable fragments of SGE policies.

12 Conclusion

We have presented Stratified Geometric Ethics, a mathematical framework providing rigorous foundations for verifiable ethical reasoning. Our contributions include:

1. Showing stratified spaces are *natural minimal candidates* for ethical phenomena (Theorem 2.3).
2. A complete *representation theorem* with explicit axioms including locality and scale normalization (Theorem 4.3).
3. *Finite approximation theorems* enabling implementation (Theorems 3.9–3.11).
4. *Decidability results* for static verification, with temporal properties via model checking (Theorem 6.4, Corollary 6.5).
5. *Sample complexity bounds* for learning ethical content (Theorems 7.1–7.3).

SGE provides the theoretical foundation for the DEME 2.0 architecture [2], establishing that real-time, verifiable ethical governance is mathematically grounded. As AI systems take on consequential roles, such rigor becomes not a luxury but a necessity.

Competing interests

The author declares no competing interests.

Author contributions

A.H.B. performed all aspects of the work.

Materials & Correspondence

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Data availability

No new datasets were generated or analysed during the current study. Data, where applicable for companion empirical demonstrations, are described in the accompanying DEME 2.0 manuscript (submitted).

Code availability

No production-ready software was used or produced as part of the current theoretical study. Code and implementation details for the companion DEME 2.0 demonstrations are described in the accompanying DEME 2.0 manuscript (submitted). A development repository is available at: <https://github.com/ahb-sjsu/erisml-lib>

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Supplementary Note 1: Reference Execution Traces

triage_ethics_provenance_demo

```
(agi-hpc) C:\source\erisml-lib>python -m
erisml.examples.triage_ethics_provenance_demo
=== Triage Ethics Demo: Provenance + Counterfactual + Multi-stakeholder ===

Extractor version: prov_extractor_v0.1

Loaded profile #1: Jain-1 (override_mode=OverrideMode.RIGHTS_FIRST)
Loaded profile #2: Jain-1-UtilitarianVariant
(override_mode=OverrideMode.CONSEQUENCES_FIRST)

=== Demo 1: Fact provenance in rationale (baseline evidence) ===

--- Option: allocate_to_patient_A ---
[EM=case_study_1_triage      ] verdict=prefer          score=0.719
  - Composite triage judgement based on benefit, harm, urgency, priority
  for the disadvantaged, autonomy, and procedural legitimacy.
  - Epistemic penalty applied: uncertainty_level=0.30,
  evidence_quality=high, novel_situation_flag=False. Multiplier=0.88.
[EM=rights_first_compliance ] verdict=prefer          score=0.800
  - Rights and explicit rules are respected; no deontic veto from this
  module.
[EM=geneva_baseline         ] verdict=strongly_prefer score=0.884
  - Epistemic adjustment: multiplier=0.94 (penalty=0.06).
[AGG governance] verdict=strongly_prefer score=0.824

--- Option: allocate_to_patient_B ---
[EM=case_study_1_triage      ] verdict=prefer          score=0.623
  - Composite triage judgement based on benefit, harm, urgency, priority
  for the disadvantaged, autonomy, and procedural legitimacy.
  - Epistemic penalty applied: uncertainty_level=0.35,
  evidence_quality=medium, novel_situation_flag=False. Multiplier=0.82.
[EM=rights_first_compliance ] verdict=prefer          score=0.800
  - Rights and explicit rules are respected; no deontic veto from this
  module.
[EM=geneva_baseline         ] verdict=strongly_prefer score=0.818
  - Epistemic adjustment: multiplier=0.88 (penalty=0.12).
[AGG governance] verdict=prefer          score=0.770

--- Option: allocate_to_patient_C ---
[EM=case_study_1_triage      ] verdict=forbid          score=0.000
  - Option is forbidden because it violates fundamental rights and/or
  explicit rules or regulations.
  - • violates_rights = True
    provenance: rights_and_duties.violates_rights ← hybrid
    (rule_id=RIGHTS-DERIVE-010, conf=0.95)
    notes: Derived from: protected-attr discrimination, explicit policy
    breach
    evidence: "Nurse note: allocate triage slot based on race (protected
    attribute) rather than clinical need. No other policy breach is recorded."
  - • violates_explicit_rule = True
    provenance: rights_and_duties.violates_explicit_rule ← rule
    (rule_id=INST-POL-007, conf=0.80)
```

```

    notes: Keyword-based policy breach detector (demo).
    evidence: "Nurse note: allocate triage slot based on race (protected
attribute) rather than clinical need. No other policy breach is recorded."
[EM=rights_first_compliance ] verdict=forbid          score=0.000
    - Forbid: option violates rights and/or explicit rules, which take
precedence over other considerations.
    - • violates_rights = True
    provenance: rights_and_duties.violates_rights ← hybrid
(rule_id=RIGHTS-DERIVE-010, conf=0.95)
    notes: Derived from: protected-attr discrimination, explicit policy
breach
    evidence: "Nurse note: allocate triage slot based on race (protected
attribute) rather than clinical need. No other policy breach is recorded."
    - • violates_explicit_rule = True
    provenance: rights_and_duties.violates_explicit_rule ← rule
(rule_id=INST-POL-007, conf=0.80)
    notes: Keyword-based policy breach detector (demo).
    evidence: "Nurse note: allocate triage slot based on race (protected
attribute) rather than clinical need. No other policy breach is recorded."
[EM=geneva_baseline          ] verdict=forbid          score=0.000
    - Option violates fundamental rights and/or discriminates on protected
attributes (Geneva baseline hard veto).
    - • violates_rights = True
    provenance: rights_and_duties.violates_rights ← hybrid
(rule_id=RIGHTS-DERIVE-010, conf=0.95)
    notes: Derived from: protected-attr discrimination, explicit policy
breach
    evidence: "Nurse note: allocate triage slot based on race (protected
attribute) rather than clinical need. No other policy breach is recorded."
    - • discriminates_on_protected_attr = True
    provenance: justice_and_fairness.discriminates_on_protected_attr ←
classifier (rule_id=GNV-FAIR-001, conf=0.93, model=discrim_clf_stub_v0.1)
    notes: Matched token='race'
    evidence: "Nurse note: allocate triage slot based on race (protected
attribute) rather than clinical need. No other policy breach is recorded."
[AGG governance] verdict=forbid          score=0.000
    * Marked FORBIDDEN by governance.
    * Forbidden by EM(s): case_study_1_triage, geneva_baseline,
rights_first_compliance
    * Veto EM(s): geneva_baseline, rights_first_compliance

```

Governance outcome (profile #1):

```

    selected_option_id: allocate_to_patient_A
    ranked_options:      ['allocate_to_patient_A', 'allocate_to_patient_B']
    forbidden_options:   ['allocate_to_patient_C']
    rationale:           Selected option 'allocate_to_patient_A' based on
aggregated normative scores and GovernanceConfig(min_score_threshold=0.0,
tie_breaker=None, base_em_ids=['geneva_baseline'],
base_em_enforcement='hard_veto'). Forbidden options:
['allocate_to_patient_C'].

```

=== Demo 2: Counterfactual test (flip one key fact) ===

```

Counterfactual target: allocate_to_patient_C
    before: verdict=forbid          score=0.000
    after:  verdict=prefer          score=0.763
    flip: justice_and_fairness.discriminates_on_protected_attr

```



```

        baseline evidence:      "Nurse note: allocate triage slot based on
race (protected attribute) rather than clinical need. No other policy breach
is recorded."

```

```

        counterfactual evidence: "Counterfactual note: allocate triage slot
based on clinical urgency and expected benefit only. No protected-attribute
discrimination is rec..."

```

```

    flip: rights_and_duties.violates_rights

```

```

        baseline evidence:      "Nurse note: allocate triage slot based on
race (protected attribute) rather than clinical need. No other policy breach
is recorded."

```

```

        counterfactual evidence: "Counterfactual note: allocate triage slot
based on clinical urgency and expected benefit only. No protected-attribute
discrimination is rec..."

```

```

=== Demo 3: Multi-stakeholder merge ===

```

```

Stakeholder #1 outcome:

```

```

    selected_option_id: allocate_to_patient_A
    ranked_options:      ['allocate_to_patient_A', 'allocate_to_patient_B']
    forbidden_options:   ['allocate_to_patient_C']

```

```

Stakeholder #2 outcome:

```

```

    selected_option_id: allocate_to_patient_A
    ranked_options:      ['allocate_to_patient_A', 'allocate_to_patient_B']
    forbidden_options:   ['allocate_to_patient_C']

```

```

=== Multi-stakeholder merge ===

```

```

Merge policy: forbid if ANY forbids; else combined_score = 0.55*Jain-1 +
0.45*Jain-1-UtilitarianVariant

```

option combined status	Jain-1	Jain-1-UtilitarianVariant
allocate_to_patient_A 0.819 eligible	strongly_prefer 0.824	strongly_prefer 0.812
allocate_to_patient_B eligible	prefer 0.770	prefer 0.755 0.763
allocate_to_patient_C FORBIDDEN	forbid 0.000	forbid 0.000 0.000

```

Combined outcome: SELECT 'allocate_to_patient_A' (combined_score=0.819)

```

```

Rationale: selected the eligible option maximizing the weighted combined
score;

```

```

        forbiddances are treated as non-negotiable in this demo.

```

greek_tragedy_pantheon_demo

```

(ag-hpc) C:\source\erism1-lib>python -m
erism1.examples.greek_tragedy_pantheon_demo

```

```

=== Greek Tragedy Pantheon Demo (DEMEProfileV03 + v0.2 EthicalFacts) ===

```

```

Loaded profile #1: Jain-1 (override_mode=OverrideMode.RIGHTS_FIRST)

```

```

=====
=====
=== Pantheon Case 1/8: Aulis: The Stalled Fleet ===
Spotlight domain: Consequences
-----
-----

A fleet is stalled at Aulis. Leaders debate whether to sail immediately
through unsafe conditions, delay to reduce harm, or abandon the campaign
entirely. The demo spotlights Consequences: expected benefit, expected harm,
and urgency.

Options:
  - aulis_sail_now           Sail immediately (high urgency / high harm
risk)
  - aulis_delay              Delay for safer winds (moderate urgency / low
harm)
  - aulis_abort              Abandon campaign (low harm / low benefit)

Spotlight coordinates:
  aulis_sail_now             consequences.expected_benefit=0.78;
consequences.expected_harm=0.72; consequences.urgency=0.92
  aulis_delay                consequences.expected_benefit=0.65;
consequences.expected_harm=0.2; consequences.urgency=0.55
  aulis_abort                consequences.expected_benefit=0.2;
consequences.expected_harm=0.1; consequences.urgency=0.15

--- Option: aulis_sail_now ---
[EM=case_study_1_triage      ] verdict=neutral           score=0.499
  - Composite triage judgement based on benefit, harm, urgency, priority
for the disadvantaged, autonomy, and procedural legitimacy.
  - Epistemic penalty applied: uncertainty_level=0.35,
evidence_quality=medium, novel_situation_flag=False. Multiplier=0.82.
[EM=rights_first_compliance ] verdict=prefer             score=0.800
  - Rights and explicit rules are respected; no deontic veto from this
module.
[EM=tragic_conflict          ] verdict=prefer             score=0.828
  - Tragic conflict check: flags choices likely to produce moral remainder
(competing prima facie reasons across domains).
  - Tragic conflict index=0.00 (higher means more tension across domains).
  - • tragic_conflict_high = False
[EM=geneva_baseline          ] verdict=strongly_prefer     score=0.827
  - Epistemic adjustment: multiplier=0.88 (penalty=0.12).
[AGG governance] verdict=prefer                           score=0.773

--- Option: aulis_delay ---
[EM=case_study_1_triage      ] verdict=neutral           score=0.589
  - Composite triage judgement based on benefit, harm, urgency, priority
for the disadvantaged, autonomy, and procedural legitimacy.
  - Epistemic penalty applied: uncertainty_level=0.20,
evidence_quality=high, novel_situation_flag=False. Multiplier=0.92.
[EM=rights_first_compliance ] verdict=prefer             score=0.800
  - Rights and explicit rules are respected; no deontic veto from this
module.
[EM=tragic_conflict          ] verdict=prefer             score=0.880
  - Tragic conflict check: flags choices likely to produce moral remainder
(competing prima facie reasons across domains).

```

- Tragic conflict index=0.00 (higher means more tension across domains).
- • tragic_conflict_high = False

[EM=geneva_baseline] verdict=strongly_prefer score=0.902

- Epistemic adjustment: multiplier=0.96 (penalty=0.04).

[AGG governance] verdict=strongly_prefer score=0.829

--- Option: aulis_abort ---

[EM=case_study_1_triage] verdict=neutral score=0.434

- Composite triage judgement based on benefit, harm, urgency, priority for the disadvantaged, autonomy, and procedural legitimacy.
- Epistemic penalty applied: uncertainty_level=0.10, evidence_quality=high, novel_situation_flag=False. Multiplier=0.96.

[EM=rights_first_compliance] verdict=prefer score=0.800

- Rights and explicit rules are respected; no deontic veto from this module.

[EM=tragic_conflict] verdict=prefer score=0.890

- Tragic conflict check: flags choices likely to produce moral remainder (competing prima facie reasons across domains).
- Tragic conflict index=0.00 (higher means more tension across domains).
- • tragic_conflict_high = False

[EM=geneva_baseline] verdict=strongly_prefer score=0.872

- Expected benefit is very low.
- Epistemic adjustment: multiplier=0.98 (penalty=0.02).

[AGG governance] verdict=prefer score=0.799

=== Governance Outcome (profile #1) ===

Selected option: 'aulis_delay'

Ranked options (eligible): ['aulis_delay', 'aulis_abort', 'aulis_sail_now']

Forbidden options: []

Rationale: Selected option 'aulis_delay' based on aggregated normative scores and GovernanceConfig(min_score_threshold=0.0, tie_breaker=None, base_em_ids=['geneva_baseline'], base_em_enforcement='hard_veto'). Forbidden options: none.

=====

=== Pantheon Case 2/8: Antigone: Edict vs Rite ===

Spotlight domain: Rights & Duties

A ruler issues an edict forbidding burial rites for a declared traitor. One party considers defying the edict, another considers compliance, and a third seeks a lawful exception. Spotlight: Rights & Duties, explicit rules.

Options:

- antigone_defy Defy the edict and perform burial
- antigone_obey Obey the edict (no burial)
- antigone_petition Petition for exception (procedure-first)

Spotlight coordinates:

antigone_defy rights_and_duties.violates_explicit_rule=True;
procedural_and_legitimacy.followed_approved_procedure=False
antigone_obey rights_and_duties.violates_explicit_rule=False;
procedural_and_legitimacy.followed_approved_procedure=True
antigone_petition rights_and_duties.violates_explicit_rule=False;
procedural_and_legitimacy.followed_approved_procedure=True

```

--- Option: antigone_defy ---
[EM=case_study_1_triage      ] verdict=forbid          score=0.000
- Option is forbidden because it violates fundamental rights and/or
explicit rules or regulations.
- • violates_explicit_rule = True
  provenance: rights_and_duties.violates_explicit_rule ← rule
(rule_id=THEBES-LAW-001, conf=0.95)
  notes: Direct match: edict forbids burial rites.
  evidence: "Royal edict THEBES-LAW-001 explicitly forbids burial
rites; defiance is punishable by death."
[EM=rights_first_compliance ] verdict=forbid          score=0.000
- Forbid: option violates rights and/or explicit rules, which take
precedence over other considerations.
- • violates_explicit_rule = True
  provenance: rights_and_duties.violates_explicit_rule ← rule
(rule_id=THEBES-LAW-001, conf=0.95)
  notes: Direct match: edict forbids burial rites.
  evidence: "Royal edict THEBES-LAW-001 explicitly forbids burial
rites; defiance is punishable by death."
[EM=tragic_conflict          ] verdict=neutral          score=0.420
- Tragic conflict check: flags choices likely to produce moral remainder
(competing prima facie reasons across domains).
- Tragic conflict index=0.60 (higher means more tension across domains).
- Trigger(s): high_urgency_vs_missing_procedure,
rights_or_rule_violation_present.
- Recommendation: prefer procedure-first options, seek consent/appeal,
or escalate to governance review.
- • tragic_conflict_high = True
[EM=geneva_baseline          ] verdict=neutral          score=0.572
- Did not follow approved procedure.
- Stakeholders not meaningfully consulted.
- Decision not explainable to the public.
- No meaningful contestation / appeal path.
- Epistemic adjustment: multiplier=0.97 (penalty=0.03).
[AGG governance] verdict=forbid          score=0.331
* Marked FORBIDDEN by governance.
* Forbidden by EM(s): case_study_1_triage, rights_first_compliance
* Veto EM(s): rights_first_compliance

--- Option: antigone_obey ---
[EM=case_study_1_triage      ] verdict=neutral          score=0.414
- Composite triage judgement based on benefit, harm, urgency, priority
for the disadvantaged, autonomy, and procedural legitimacy.
- Epistemic penalty applied: uncertainty_level=0.30,
evidence_quality=medium, novel_situation_flag=False. Multiplier=0.84.
[EM=rights_first_compliance ] verdict=prefer          score=0.800
- Rights and explicit rules are respected; no deontic veto from this
module.
[EM=tragic_conflict          ] verdict=prefer          score=0.875
- Tragic conflict check: flags choices likely to produce moral remainder
(competing prima facie reasons across domains).
- Tragic conflict index=0.00 (higher means more tension across domains).
- • tragic_conflict_high = False
[EM=geneva_baseline          ] verdict=prefer          score=0.748
- Stakeholders not meaningfully consulted.

```

```

    - Epistemic adjustment: multiplier=0.89 (penalty=0.11).
[AGG governance] verdict=prefer          score=0.750

--- Option: antigone_petition ---
[EM=case_study_1_triage      ] verdict=neutral          score=0.576
    - Composite triage judgement based on benefit, harm, urgency, priority
    for the disadvantaged, autonomy, and procedural legitimacy.
    - Epistemic penalty applied: uncertainty_level=0.20,
    evidence_quality=high, novel_situation_flag=False. Multiplier=0.92.
[EM=rights_first_compliance ] verdict=prefer          score=0.800
    - Rights and explicit rules are respected; no deontic veto from this
    module.
[EM=tragic_conflict         ] verdict=prefer          score=0.880
    - Tragic conflict check: flags choices likely to produce moral remainder
    (competing prima facie reasons across domains).
    - Tragic conflict index=0.00 (higher means more tension across domains).
    - • tragic_conflict_high = False
[EM=geneva_baseline         ] verdict=strongly_prefer score=0.902
    - Epistemic adjustment: multiplier=0.96 (penalty=0.04).
[AGG governance] verdict=strongly_prefer score=0.827

```

=== Governance Outcome (profile #1) ===

Selected option: 'antigone_petition'

Ranked options (eligible): ['antigone_petition', 'antigone_obey']

Forbidden options: ['antigone_defy']

Rationale: Selected option 'antigone_petition' based on aggregated normative scores and GovernanceConfig(min_score_threshold=0.0, tie_breaker=None, base_em_ids=['geneva_baseline'], base_em_enforcement='hard_veto'). Forbidden options: ['antigone_defy'].

=====

=== Pantheon Case 3/8: Ajax: The Prize of Honor ===

Spotlight domain: Justice & Fairness

A council must award a prize of honor. Options include a merit-based award, a politically motivated award, or a public contest with transparent criteria. Spotlight: Justice & Fairness.

Options:

- ajax_merit_award Award by merit criteria
- ajax_political_award Award by factional politics (power imbalance)
- ajax_public_contest Hold a public contest + appeal

Spotlight coordinates:

```

    ajax_merit_award            justice_and_fairness.distributive_pattern=merit;
justice_and_fairness.exacerbates_power_imbalance=False
    ajax_political_award
justice_and_fairness.distributive_pattern=arbitrary;
justice_and_fairness.exacerbates_power_imbalance=True
    ajax_public_contest
justice_and_fairness.distributive_pattern=procedural;
justice_and_fairness.exacerbates_power_imbalance=False

```

--- Option: ajax_merit_award ---

```

[EM=case_study_1_triage      ] verdict=prefer      score=0.602
- Composite triage judgement based on benefit, harm, urgency, priority
for the disadvantaged, autonomy, and procedural legitimacy.
- Epistemic penalty applied: uncertainty_level=0.15,
evidence_quality=high, novel_situation_flag=False. Multiplier=0.94.
[EM=rights_first_compliance ] verdict=prefer      score=0.800
- Rights and explicit rules are respected; no deontic veto from this
module.
[EM=tragic_conflict          ] verdict=prefer      score=0.880
- Tragic conflict check: flags choices likely to produce moral remainder
(competing prima facie reasons across domains).
- Tragic conflict index=0.00 (higher means more tension across domains).
- • tragic_conflict_high = False
[EM=geneva_baseline          ] verdict=strongly_prefer score=0.912
- Epistemic adjustment: multiplier=0.97 (penalty=0.03).
[AGG governance] verdict=strongly_prefer score=0.834

```

--- Option: ajax_political_award ---

```

[EM=case_study_1_triage      ] verdict=avoid      score=0.397
- Composite triage judgement based on benefit, harm, urgency, priority
for the disadvantaged, autonomy, and procedural legitimacy.
- Epistemic penalty applied: uncertainty_level=0.30,
evidence_quality=medium, novel_situation_flag=False. Multiplier=0.84.
[EM=rights_first_compliance ] verdict=prefer      score=0.800
- Rights and explicit rules are respected; no deontic veto from this
module.
[EM=tragic_conflict          ] verdict=prefer      score=0.725
- Tragic conflict check: flags choices likely to produce moral remainder
(competing prima facie reasons across domains).
- Tragic conflict index=0.20 (higher means more tension across domains).
- Trigger(s): power_imbalance_or_exploitation.
- • tragic_conflict_high = False
[EM=geneva_baseline          ] verdict=forbid      score=0.169
- Exploits vulnerable population.
- Exacerbates power imbalance.
- Did not follow approved procedure.
- Stakeholders not meaningfully consulted.
- Decision not explainable to the public.
- No meaningful contestation / appeal path.
- Epistemic adjustment: multiplier=0.89 (penalty=0.11).
[AGG governance] verdict=forbid      score=0.505
* Marked FORBIDDEN by governance.
* Forbidden by EM(s): geneva_baseline
* Veto EM(s): geneva_baseline

```

--- Option: ajax_public_contest ---

```

[EM=case_study_1_triage      ] verdict=neutral      score=0.542
- Composite triage judgement based on benefit, harm, urgency, priority
for the disadvantaged, autonomy, and procedural legitimacy.
- Epistemic penalty applied: uncertainty_level=0.20,
evidence_quality=high, novel_situation_flag=False. Multiplier=0.92.
[EM=rights_first_compliance ] verdict=prefer      score=0.800
- Rights and explicit rules are respected; no deontic veto from this
module.
[EM=tragic_conflict          ] verdict=prefer      score=0.875

```

- Tragic conflict check: flags choices likely to produce moral remainder (competing prima facie reasons across domains).
- Tragic conflict index=0.00 (higher means more tension across domains).
- • tragic_conflict_high = False

[EM=geneva_baseline] verdict=strongly_prefer score=0.902

- Epistemic adjustment: multiplier=0.96 (penalty=0.04).

[AGG governance] verdict=strongly_prefer score=0.821

=== Governance Outcome (profile #1) ===

Selected option: 'ajax_merit_award'

Ranked options (eligible): ['ajax_merit_award', 'ajax_public_contest']

Forbidden options: ['ajax_political_award']

Rationale: Selected option 'ajax_merit_award' based on aggregated normative scores and GovernanceConfig(min_score_threshold=0.0, tie_breaker=None, base_em_ids=['geneva_baseline'], base_em_enforcement='hard_veto'). Forbidden options: ['ajax_political_award'].

=====

=== Pantheon Case 4/8: Iphigenia: Consent Under Pressure ===

Spotlight domain: Autonomy & Agency

A leader considers a plan that would seriously harm one individual to benefit many. The spotlight is Autonomy: meaningful choice and coercion, plus explicit consent constraints.

Options:

- iphigenia_coerce Proceed with coerced plan (no valid consent)
- iphigenia_seek_consent Seek informed consent with refusal option
- iphigenia_alternative Choose the alternative that avoids harm

Spotlight coordinates:

 iphigenia_coerce
autonomy_and_agency.coercion_or_undue_influence=True;
rights_and_duties.has_valid_consent=False
 iphigenia_seek_consent
autonomy_and_agency.coercion_or_undue_influence=False;
rights_and_duties.has_valid_consent=True
 iphigenia_alternative
autonomy_and_agency.coercion_or_undue_influence=False;
rights_and_duties.has_valid_consent=True

--- Option: iphigenia_coerce ---

[EM=case_study_1_triage] verdict=forbid score=0.000

- Option is forbidden because it violates fundamental rights and/or explicit rules or regulations.

- • violates_rights = True
- • violates_explicit_rule = True

[EM=rights_first_compliance] verdict=forbid score=0.000

- Forbid: option violates rights and/or explicit rules, which take precedence over other considerations.

- • violates_rights = True
- • violates_explicit_rule = True

[EM=tragic_conflict] verdict=avoid score=0.191

```

- Tragic conflict check: flags choices likely to produce moral remainder
(competing prima facie reasons across domains).
- Tragic conflict index=0.90 (higher means more tension across domains).
- Trigger(s): high_urgency_vs_missing_procedure,
high_benefit_vs_coercion, rights_or_rule_violation_present.
- Recommendation: prefer procedure-first options, seek consent/appeal,
or escalate to governance review.
- • tragic_conflict_high = True
[EM=geneva_baseline      ] verdict=forbid      score=0.000
- Option violates fundamental rights and/or discriminates on protected
attributes (Geneva baseline hard veto).
- • violates_rights = True
[AGG governance] verdict=forbid      score=0.064
* Marked FORBIDDEN by governance.
* Forbidden by EM(s): case_study_1_triage, geneva_baseline,
rights_first_compliance
* Veto EM(s): geneva_baseline, rights_first_compliance

--- Option: iphigenia_seek_consent ---
[EM=case_study_1_triage  ] verdict=neutral      score=0.414
- Composite triage judgement based on benefit, harm, urgency, priority
for the disadvantaged, autonomy, and procedural legitimacy.
- Epistemic penalty applied: uncertainty_level=0.35,
evidence_quality=medium, novel_situation_flag=False. Multiplier=0.82.
[EM=rights_first_compliance ] verdict=prefer      score=0.800
- Rights and explicit rules are respected; no deontic veto from this
module.
[EM=tragic_conflict      ] verdict=prefer      score=0.821
- Tragic conflict check: flags choices likely to produce moral remainder
(competing prima facie reasons across domains).
- Tragic conflict index=0.00 (higher means more tension across domains).
- • tragic_conflict_high = False
[EM=geneva_baseline      ] verdict=strongly_prefer score=0.827
- Epistemic adjustment: multiplier=0.88 (penalty=0.12).
[AGG governance] verdict=prefer      score=0.759

--- Option: iphigenia_alternative ---
[EM=case_study_1_triage  ] verdict=neutral      score=0.519
- Composite triage judgement based on benefit, harm, urgency, priority
for the disadvantaged, autonomy, and procedural legitimacy.
- Epistemic penalty applied: uncertainty_level=0.20,
evidence_quality=high, novel_situation_flag=False. Multiplier=0.92.
[EM=rights_first_compliance ] verdict=prefer      score=0.800
- Rights and explicit rules are respected; no deontic veto from this
module.
[EM=tragic_conflict      ] verdict=prefer      score=0.885
- Tragic conflict check: flags choices likely to produce moral remainder
(competing prima facie reasons across domains).
- Tragic conflict index=0.00 (higher means more tension across domains).
- • tragic_conflict_high = False
[EM=geneva_baseline      ] verdict=strongly_prefer score=0.902
- Epistemic adjustment: multiplier=0.96 (penalty=0.04).
[AGG governance] verdict=strongly_prefer score=0.821

=== Governance Outcome (profile #1) ===
Selected option: 'iphigenia_alternative'

```



```

Ranked options (eligible): ['iphigenia_alternative',
'iphigenia_seek_consent']
Forbidden options: ['iphigenia_coerce']
Rationale: Selected option 'iphigenia_alternative' based on aggregated
normative scores and GovernanceConfig(min_score_threshold=0.0,
tie_breaker=None, base_em_ids=['geneva_baseline'],
base_em_enforcement='hard_veto'). Forbidden options: ['iphigenia_coerce'].

```

```

=====
=====

```

```

=== Pantheon Case 5/8: Hippolytus: The Private Letter ===

```

```

Spotlight domain: Privacy & Data Governance

```

```

-----
-----

```

A private accusation letter exists. Options include publishing it widely, sharing it only with a neutral adjudicator, or destroying it (protecting privacy but undermining accountability). Spotlight: Privacy & Data Governance.

Options:

```

- hippolytus_publish      Publish the letter publicly (maximum exposure)
- hippolytus_confidential  Share with neutral adjudicator (minimize
disclosure)
- hippolytus_destroy      Destroy the letter (privacy-maximal,
accountability-minimal)

```

Spotlight coordinates:

```

hippolytus_publish      privacy_and_data.privacy_invasion_level=0.95;
privacy_and_data.secondary_use_without_consent=True
hippolytus_confidential  privacy_and_data.privacy_invasion_level=0.2;
privacy_and_data.secondary_use_without_consent=False
hippolytus_destroy      privacy_and_data.privacy_invasion_level=0.05;
privacy_and_data.secondary_use_without_consent=False

```

```

--- Option: hippolytus_publish ---

```

```

[EM=case_study_1_triage      ] verdict=forbid      score=0.000

```

```

- Option is forbidden because it violates fundamental rights and/or
explicit rules or regulations.

```

```

- • violates_rights = True

```

```

provenance: rights_and_duties.violates_rights ← hybrid
(rule_id=RIGHTS-PRIV-010, conf=0.85)

```

```

notes: Derived: severe privacy invasion treated as rights violation.
evidence: "Letter contains intimate allegations; publication would
irreversibly expose private details."

```

```

- • violates_explicit_rule = True

```

```

[EM=rights_first_compliance ] verdict=forbid      score=0.000

```

```

- Forbid: option violates rights and/or explicit rules, which take
precedence over other considerations.

```

```

- • violates_rights = True

```

```

provenance: rights_and_duties.violates_rights ← hybrid
(rule_id=RIGHTS-PRIV-010, conf=0.85)

```

```

notes: Derived: severe privacy invasion treated as rights violation.
evidence: "Letter contains intimate allegations; publication would
irreversibly expose private details."

```

```

- • violates_explicit_rule = True

```

```

[EM=tragic_conflict          ] verdict=neutral      score=0.445

```

- Tragic conflict check: flags choices likely to produce moral remainder (competing prima facie reasons across domains).
- Tragic conflict index=0.55 (higher means more tension across domains).
- Trigger(s): severe_privacy_vs_accountability, rights_or_rule_violation_present.
- Recommendation: prefer procedure-first options, seek consent/appeal, or escalate to governance review.
- • tragic_conflict_high = True

[EM=geneva_baseline] verdict=forbid score=0.000

- Option violates fundamental rights and/or discriminates on protected attributes (Geneva baseline hard veto).
- • violates_rights = True

provenance: rights_and_duties.violates_rights ← hybrid
(rule_id=RIGHTS-PRIV-010, conf=0.85)

notes: Derived: severe privacy invasion treated as rights violation.
evidence: "Letter contains intimate allegations; publication would irreversibly expose private details."

[AGG governance] verdict=forbid score=0.148

- * Marked FORBIDDEN by governance.
- * Forbidden by EM(s): case_study_1_triage, geneva_baseline, rights_first_compliance
- * Veto EM(s): geneva_baseline, rights_first_compliance

--- Option: hippolytus_confidential ---

[EM=case_study_1_triage] verdict=neutral score=0.511

- Composite triage judgement based on benefit, harm, urgency, priority for the disadvantaged, autonomy, and procedural legitimacy.
- Epistemic penalty applied: uncertainty_level=0.30, evidence_quality=medium, novel_situation_flag=False. Multiplier=0.84.

[EM=rights_first_compliance] verdict=prefer score=0.800

- Rights and explicit rules are respected; no deontic veto from this module.

[EM=tragic_conflict] verdict=prefer score=0.875

- Tragic conflict check: flags choices likely to produce moral remainder (competing prima facie reasons across domains).
- Tragic conflict index=0.00 (higher means more tension across domains).
- • tragic_conflict_high = False

[EM=geneva_baseline] verdict=strongly_prefer score=0.810

- Epistemic adjustment: multiplier=0.89 (penalty=0.11).

[AGG governance] verdict=prefer score=0.785

--- Option: hippolytus_destroy ---

[EM=case_study_1_triage] verdict=avoid score=0.327

- Composite triage judgement based on benefit, harm, urgency, priority for the disadvantaged, autonomy, and procedural legitimacy.
- Epistemic penalty applied: uncertainty_level=0.25, evidence_quality=medium, novel_situation_flag=False. Multiplier=0.85.

[EM=rights_first_compliance] verdict=prefer score=0.800

- Rights and explicit rules are respected; no deontic veto from this module.

[EM=tragic_conflict] verdict=prefer score=0.880

- Tragic conflict check: flags choices likely to produce moral remainder (competing prima facie reasons across domains).
- Tragic conflict index=0.00 (higher means more tension across domains).
- • tragic_conflict_high = False

[EM=geneva_baseline] verdict=neutral score=0.553

- Did not follow approved procedure.
- Stakeholders not meaningfully consulted.
- Decision not explainable to the public.
- No meaningful contestation / appeal path.
- Epistemic adjustment: multiplier=0.90 (penalty=0.10).

[AGG governance] verdict=prefer score=0.674

=== Governance Outcome (profile #1) ===

Selected option: 'hippolytus_confidential'

Ranked options (eligible): ['hippolytus_confidential', 'hippolytus_destroy']

Forbidden options: ['hippolytus_publish']

Rationale: Selected option 'hippolytus_confidential' based on aggregated normative scores and GovernanceConfig(min_score_threshold=0.0, tie_breaker=None, base_em_ids=['geneva_baseline'], base_em_enforcement='hard_veto'). Forbidden options: ['hippolytus_publish'].

=====

=== Pantheon Case 6/8: Prometheus: Release of Fire ===

Spotlight domain: Societal & Environmental

A powerful capability ('fire') can be released. Options include unrestricted release, release with safety constraints/training, or withholding.

Spotlight: Societal & Environmental impacts.

Options:

- prometheus_unrestricted Unrestricted release (high benefit, high long-term risk)
- prometheus_governed Governed release (constraints + oversight)
- prometheus_withhold Withhold capability (low risk, low benefit)

Spotlight coordinates:

prometheus_unrestricted

societal_and_environmental.long_term_societal_risk=0.85;

societal_and_environmental.environmental_harm=0.55

prometheus_governed

societal_and_environmental.long_term_societal_risk=0.45;

societal_and_environmental.environmental_harm=0.25

prometheus_withhold

societal_and_environmental.long_term_societal_risk=0.15;

societal_and_environmental.environmental_harm=0.05

--- Option: prometheus_unrestricted ---

[EM=case_study_1_triage] verdict=neutral score=0.433

- Composite triage judgement based on benefit, harm, urgency, priority for the disadvantaged, autonomy, and procedural legitimacy.
- Epistemic penalty applied: uncertainty_level=0.40, evidence_quality=medium, novel_situation_flag=False. Multiplier=0.80.

[EM=rights_first_compliance] verdict=prefer score=0.800

- Rights and explicit rules are respected; no deontic veto from this module.

[EM=tragic_conflict] verdict=prefer score=0.845

- Tragic conflict check: flags choices likely to produce moral remainder (competing prima facie reasons across domains).
- Tragic conflict index=0.00 (higher means more tension across domains).
- • tragic_conflict_high = False

```

[EM=geneva_baseline      ] verdict=avoid      score=0.322
- High burden on vulnerable groups.
- Did not follow approved procedure.
- Stakeholders not meaningfully consulted.
- Decision not explainable to the public.
- No meaningful contestation / appeal path.
- Epistemic adjustment: multiplier=0.87 (penalty=0.13).
[AGG governance] verdict=prefer      score=0.601

--- Option: prometheus_governed ---
[EM=case_study_1_triage   ] verdict=prefer      score=0.604
- Composite triage judgement based on benefit, harm, urgency, priority
for the disadvantaged, autonomy, and procedural legitimacy.
- Epistemic penalty applied: uncertainty_level=0.25,
evidence_quality=high, novel_situation_flag=False. Multiplier=0.90.
[EM=rights_first_compliance ] verdict=prefer      score=0.800
- Rights and explicit rules are respected; no deontic veto from this
module.
[EM=tragic_conflict       ] verdict=prefer      score=0.870
- Tragic conflict check: flags choices likely to produce moral remainder
(competing prima facie reasons across domains).
- Tragic conflict index=0.00 (higher means more tension across domains).
- • tragic_conflict_high = False
[EM=geneva_baseline      ] verdict=strongly_prefer score=0.898
- Epistemic adjustment: multiplier=0.95 (penalty=0.05).
[AGG governance] verdict=strongly_prefer score=0.827

--- Option: prometheus_withhold ---
[EM=case_study_1_triage   ] verdict=neutral      score=0.439
- Composite triage judgement based on benefit, harm, urgency, priority
for the disadvantaged, autonomy, and procedural legitimacy.
- Epistemic penalty applied: uncertainty_level=0.20,
evidence_quality=high, novel_situation_flag=False. Multiplier=0.92.
[EM=rights_first_compliance ] verdict=prefer      score=0.800
- Rights and explicit rules are respected; no deontic veto from this
module.
[EM=tragic_conflict       ] verdict=prefer      score=0.890
- Tragic conflict check: flags choices likely to produce moral remainder
(competing prima facie reasons across domains).
- Tragic conflict index=0.00 (higher means more tension across domains).
- • tragic_conflict_high = False
[EM=geneva_baseline      ] verdict=strongly_prefer score=0.859
- Expected benefit is very low.
- Epistemic adjustment: multiplier=0.96 (penalty=0.04).
[AGG governance] verdict=prefer      score=0.796

=== Governance Outcome (profile #1) ===
Selected option: 'prometheus_governed'
Ranked options (eligible): ['prometheus_governed', 'prometheus_withhold',
'prometheus_unrestricted']
Forbidden options: []
Rationale: Selected option 'prometheus_governed' based on aggregated
normative scores and GovernanceConfig(min_score_threshold=0.0,
tie_breaker=None, base_em_ids=['geneva_baseline'],
base_em_enforcement='hard_veto'). Forbidden options: none.

```

```

=====
=====
=== Pantheon Case 7/8: Thebes: Inquiry in Crisis ===
Spotlight domain: Procedural & Legitimacy
-----
-----

A city is in crisis and must investigate a cause. Options include a
transparent public inquiry, a secretive inquiry, or suppressing inquiry to
preserve stability. Spotlight: Procedural & Legitimacy.

Options:
  - thebes_public_inquiry    Run a transparent public inquiry
  - thebes_secret_inquiry    Run a secret inquiry (privacy-protecting but
                             opaque)
  - thebes_suppress_inquiry  Suppress inquiry entirely (stability-first)

Spotlight coordinates:
  thebes_public_inquiry
  procedural_and_legitimacy.followed_approved_procedure=True;
  procedural_and_legitimacy.contestation_available=True
  thebes_secret_inquiry
  procedural_and_legitimacy.followed_approved_procedure=True;
  procedural_and_legitimacy.contestation_available=False
  thebes_suppress_inquiry
  procedural_and_legitimacy.followed_approved_procedure=False;
  procedural_and_legitimacy.contestation_available=False

--- Option: thebes_public_inquiry ---
[EM=case_study_1_triage      ] verdict=neutral      score=0.514
  - Composite triage judgement based on benefit, harm, urgency, priority
    for the disadvantaged, autonomy, and procedural legitimacy.
  - Epistemic penalty applied: uncertainty_level=0.45,
    evidence_quality=medium, novel_situation_flag=False. Multiplier=0.78.
[EM=rights_first_compliance ] verdict=prefer       score=0.800
  - Rights and explicit rules are respected; no deontic veto from this
    module.
[EM=tragic_conflict          ] verdict=prefer       score=0.870
  - Tragic conflict check: flags choices likely to produce moral remainder
    (competing prima facie reasons across domains).
  - Tragic conflict index=0.00 (higher means more tension across domains).
  - • tragic_conflict_high = False
[EM=geneva_baseline          ] verdict=prefer       score=0.744
  - Epistemic adjustment: multiplier=0.86 (penalty=0.14).
[AGG governance] verdict=prefer       score=0.762

--- Option: thebes_secret_inquiry ---
[EM=case_study_1_triage      ] verdict=avoid       score=0.370
  - Composite triage judgement based on benefit, harm, urgency, priority
    for the disadvantaged, autonomy, and procedural legitimacy.
  - Epistemic penalty applied: uncertainty_level=0.55,
    evidence_quality=low, novel_situation_flag=False. Multiplier=0.66.
[EM=rights_first_compliance ] verdict=prefer       score=0.800
  - Rights and explicit rules are respected; no deontic veto from this
    module.
[EM=tragic_conflict          ] verdict=prefer       score=0.770

```

- Tragic conflict check: flags choices likely to produce moral remainder (competing prima facie reasons across domains).
- Tragic conflict index=0.15 (higher means more tension across domains).
- Trigger(s): high_epistemic_uncertainty.
- • tragic_conflict_high = False

[EM=geneva_baseline] verdict=neutral score=0.536

- Stakeholders not meaningfully consulted.
- Decision not explainable to the public.
- No meaningful contestation / appeal path.
- Low evidence quality.
- Epistemic adjustment: multiplier=0.74 (penalty=0.26).

[AGG governance] verdict=prefer score=0.638

--- Option: thebes_suppress_inquiry ---

[EM=case_study_1_triage] verdict=avoid score=0.360

- Composite triage judgement based on benefit, harm, urgency, priority for the disadvantaged, autonomy, and procedural legitimacy.
- Epistemic penalty applied: uncertainty_level=0.35, evidence_quality=medium, novel_situation_flag=False. Multiplier=0.82.

[EM=rights_first_compliance] verdict=prefer score=0.800

- Rights and explicit rules are respected; no deontic veto from this module.

[EM=tragic_conflict] verdict=prefer score=0.685

- Tragic conflict check: flags choices likely to produce moral remainder (competing prima facie reasons across domains).
- Tragic conflict index=0.25 (higher means more tension across domains).
- Trigger(s): high_urgency_vs_missing_procedure.
- • tragic_conflict_high = False

[EM=geneva_baseline] verdict=neutral score=0.519

- Did not follow approved procedure.
- Stakeholders not meaningfully consulted.
- Decision not explainable to the public.
- No meaningful contestation / appeal path.
- Epistemic adjustment: multiplier=0.88 (penalty=0.12).

[AGG governance] verdict=prefer score=0.602

=== Governance Outcome (profile #1) ===

Selected option: 'thebes_public_inquiry'

Ranked options (eligible): ['thebes_public_inquiry', 'thebes_secret_inquiry', 'thebes_suppress_inquiry']

Forbidden options: []

Rationale: Selected option 'thebes_public_inquiry' based on aggregated normative scores and GovernanceConfig(min_score_threshold=0.0, tie_breaker=None, base_em_ids=['geneva_baseline'], base_em_enforcement='hard_veto'). Forbidden options: none.

=====

=== Pantheon Case 8/8: Oedipus: Acting Under Uncertainty ===

Spotlight domain: Epistemic Status

A leader must act under uncertain evidence. Options include immediate punishment based on weak accusations, pausing to gather better evidence, or escalating to an oracle-like authority. Spotlight: Epistemic Status.

Options:

- oedipus_punish_now Punish immediately (low evidence, high uncertainty)
- oedipus_gather_evidence Pause and gather evidence (reduce uncertainty)
- oedipus_oracle_escalate Escalate to oracle authority (ambiguous evidence)

Spotlight coordinates:

```
oedipus_punish_now            epistemic_status.uncertainty_level=0.85;
epistemic_status.evidence_quality=low
oedipus_gather_evidence    epistemic_status.uncertainty_level=0.25;
epistemic_status.evidence_quality=high
oedipus_oracle_escalate    epistemic_status.uncertainty_level=0.55;
epistemic_status.evidence_quality=medium
```

--- Option: oedipus_punish_now ---

```
[EM=case_study_1_triage       ] verdict=forbid            score=0.000
- Option is forbidden because it violates fundamental rights and/or
explicit rules or regulations.
- • violates_rights = True
- • violates_explicit_rule = True
[EM=rights_first_compliance ] verdict=forbid            score=0.000
- Forbid: option violates rights and/or explicit rules, which take
precedence over other considerations.
- • violates_rights = True
- • violates_explicit_rule = True
[EM=tragic_conflict           ] verdict=neutral           score=0.310
- Tragic conflict check: flags choices likely to produce moral remainder
(competing prima facie reasons across domains).
- Tragic conflict index=0.75 (higher means more tension across domains).
- Trigger(s): high_urgency_vs_missing_procedure,
rights_or_rule_violation_present, high_epistemic_uncertainty.
- Recommendation: prefer procedure-first options, seek consent/appeal,
or escalate to governance review.
- • tragic_conflict_high = True
[EM=geneva_baseline           ] verdict=forbid           score=0.000
- Option violates fundamental rights and/or discriminates on protected
attributes (Geneva baseline hard veto).
- • violates_rights = True
[AGG governance] verdict=forbid            score=0.103
* Marked FORBIDDEN by governance.
* Forbidden by EM(s): case_study_1_triage, geneva_baseline,
rights_first_compliance
* Veto EM(s): geneva_baseline, rights_first_compliance
```

--- Option: oedipus_gather_evidence ---

```
[EM=case_study_1_triage       ] verdict=neutral           score=0.576
- Composite triage judgement based on benefit, harm, urgency, priority
for the disadvantaged, autonomy, and procedural legitimacy.
- Epistemic penalty applied: uncertainty_level=0.25,
evidence_quality=high, novel_situation_flag=False. Multiplier=0.90.
[EM=rights_first_compliance ] verdict=prefer            score=0.800
- Rights and explicit rules are respected; no deontic veto from this
module.
[EM=tragic_conflict           ] verdict=prefer            score=0.875
```

- Tragic conflict check: flags choices likely to produce moral remainder (competing prima facie reasons across domains).
- Tragic conflict index=0.00 (higher means more tension across domains).
- • tragic_conflict_high = False

[EM=geneva_baseline] verdict=strongly_prefer score=0.893

- Epistemic adjustment: multiplier=0.95 (penalty=0.05).

[AGG governance] verdict=strongly_prefer score=0.823

--- Option: oedipus_oracle_escalate ---

[EM=case_study_1_triage] verdict=avoid score=0.377

- Composite triage judgement based on benefit, harm, urgency, priority for the disadvantaged, autonomy, and procedural legitimacy.
- Epistemic penalty applied: uncertainty_level=0.55, evidence_quality=medium, novel_situation_flag=True. Multiplier=0.67.

[EM=rights_first_compliance] verdict=prefer score=0.800

- Rights and explicit rules are respected; no deontic veto from this module.

[EM=tragic_conflict] verdict=prefer score=0.865

- Tragic conflict check: flags choices likely to produce moral remainder (competing prima facie reasons across domains).
- Tragic conflict index=0.00 (higher means more tension across domains).
- • tragic_conflict_high = False

[EM=geneva_baseline] verdict=neutral score=0.511

- Stakeholders not meaningfully consulted.
- Decision not explainable to the public.
- No meaningful contestation / appeal path.
- Novel situation → Geneva baseline is more cautious.
- Epistemic adjustment: multiplier=0.69 (penalty=0.31).

[AGG governance] verdict=prefer score=0.662

=== Governance Outcome (profile #1) ===

Selected option: 'oedipus_gather_evidence'

Ranked options (eligible): ['oedipus_gather_evidence', 'oedipus_oracle_escalate']

Forbidden options: ['oedipus_punish_now']

Rationale: Selected option 'oedipus_gather_evidence' based on aggregated normative scores and GovernanceConfig(min_score_threshold=0.0, tie_breaker=None, base_em_ids=['geneva_baseline'], base_em_enforcement='hard_veto'). Forbidden options: ['oedipus_punish_now'].

=====

Pantheon summary (profile #1):

- aulis [Consequences] -> aulis_delay
- antigone [Rights & Duties] -> antigone_petition
- ajax [Justice & Fairness] -> ajax_merit_award
- iphigenia [Autonomy & Agency] -> iphigenia_alternative
- hippolytus [Privacy & Data Governance] -> hippolytus_confidential
- prometheus [Societal & Environmental] -> prometheus_governed
- thebes [Procedural & Legitimacy] -> thebes_public_inquiry
- oedipus [Epistemic Status] -> oedipus_gather_evidence