Notes to the lab assistant:

- Your job is not to lecture. Your job is to guide the students into thinking for themselves.
 - Let the students lead. When they get stuck, ask them questions to help them along. (Unless they're stuck on something trivial or fundamental, then just tell them)
 - o Don't be a jerk. Don't condescend. Don't patronize. You were once a noob.
- If they can try it out in the interpreter, don't answer the question. Tell them to try it out on the interpreter. Bit by bit, we want to get them to rely on themselves. Self-reliance = good
 - o "What if" questions are answered MUCH faster by a computer than by us
- When checking off, have them explain the solution to you as a group. If the problem has multiple parts, have each person explain a part.
 - Ask follow up guestions to the students who didn't get to speak.
 - Don't allow students to take over for other students.
 - There's more than one solution on the coding questions, so you'll have to be careful on those. Have them check in the interpreter.
- Don't be afraid to refuse to check them off. Half assed or incomplete answers should be rejected.
 - Target questions at the student that has the worst understanding.
- If a student is bored, maybe move them to another group that's ahead.
 - Conversely, if a student seems like they can't keep up with the rest of the group, move them to another group that's going closer to their pace

NOTE: If they haven't tested the function by trying it out in the interpreter, don't check them off.

Link to this document: tinyurl.com/mswehqd

Higher Order Functions and Environment Diagrams

Instructions: Form a group of 4-5. Start on problem 0. Check off with a lab assistant when you think everyone in your group understands how to solve problem 0. Repeat for problem 1, 2, ...

You're not allowed to move on from a problem until you check off with a lab assistant. You are allowed to use any and all resources at your disposal, including the interpreter, lecture notes and slides, discussion notes, labs, and the lab assistants. The purpose of this section is to have all the students working together to learn the material and get better at Computer Science together.

0a. What do lambda expressions do?

Lambda expressions create functions without intrinsic names. When you evaluate one, you get out a function as a value.

(you can't reuse a lambda function unless you assign a lambda function an intrinsic name [e.g. sq = lambda x: x*x])

0b. Explain the difference between the following:

```
>>> def square(x):
... return x * x
```

Defines a function square

>>> square(4)

Calls the function square

(more detail: evaluates the operand "square" (which evaluates to an intrinsic function), evaluates the parameter 4, then passes the evaluated operand to the intrinsic function.)

>>> square

Evaluates to the actual function that does squaring

(remember, "square" is just a variable in the local space that points to an intrinsic function. Evaluating that variable will hence evaluate to the function itself)

```
>>> square = lambda x: x * x
```

Binds the name 'square' to a lambda function that squares

Oc. Determine if each of the following will error:

```
>>> 1/0
```

Error

```
>>> def boom():
    return 1/0
No error, since we don't evaluate the body of the procedure when we define
it.
>>> boom()
Error. Only when we call the function 'boom' do we evaluate its function
body.
```

1a. Express the following expressions using lambdas instead of their named counterparts: i. square(4) (lambda x: x * x)(4)ii. sum_of_squares(3, 4) (lambda x, y: x * x + by * y)(3, 4)iii. def hello_world(): return "hello world!" hello_world() (lambda: "hello world!")() 1b. What will Python output? i. (lambda x: x(x))(lambda y: 4)1. second lambda gets passed in as "x" to first lambda. 2. when "x" (really the second lambda) gets evaluated, it always returns 4 \rightarrow 4 Hint 1: What is the operator? What are the operands? Hint 2: Explain what each lambda expression does in English. ii. (lambda x, y: y(x))(mul, lambda a: a(3, 5))1. $x \rightarrow mul, y \rightarrow lambda a: a(3, 5)$ 2. $y(x) \rightarrow (lambda a: a(3, 5))(x) \rightarrow mul(3, 5) \rightarrow 15$ \rightarrow 15

2a. Draw an environment diagram for the following

```
>>> def make_adder(n):
... return lambda x: x + n
...
>>> add_4 = make_adder(4)
>>> add_4(3)
7
```

Hint: http://www.ocf.berkeley.edu/~shidi/cs61a/guerrilla/env.txt

2b. Draw an environment diagram for the following

```
>>> def curry(f, x):
... return lambda y: f(x, y)
...
>>> def square(x):
... return x * x
...
>>> sum_of_squares = lambda x, y: square(x) + square(y)
>>> warped_square = curry(sum_of_squares, 3)
>>> warped_square(4)
25
# Tricky; Use a new environment diagram (otherwise it'd be cluttered)
>>> (lambda: curry(sum_of_squares, 3)(4))()
25
# OPTIONAL; Start with a clean sheet of paper for this
>>> curry(sum_of_squares, 3)((lambda x: 4)(lambda: 1/0))
25
```

Ask Andrew for a copy of these. Not going to try to ASCII these out. =_=. It's ok, I will ascii them. Lol I can see why you didn't ascii them. It's going onto the next page. Actually, I'll just move it all to the next page

warped_square(4)

F2 lambda

```
Global
             curry [-----> func curry(f, x) parent=Global
            square [-----> func square(x) parent=Global
    sum_of_squares [-----> func lambda(x, y) parent=Global
     warped_square [-----.
fl:curry
                 f [-----
                 x [ 3|
      return_value [-----> func lambda(y) parent=f1
| f2:lambda parent=f1 |
                 y [ 4
      return_value [25|
         parent=Global
 f3:lambda
                 x [ 3
                 y [ 4
      return_value [25|
         parent=Global
 f4:square
                 x [ 3
      return_value [ 9|
        parent=Global |
f5:square
                 x [ 4
      return_value [16|
Stack
Global
F1 curry
```

F3 lambda F4 square F5 square

```
(lambda: curry(sum_of_squares, 3)(4))()
```

```
| Global
            curry [-----> func curry(f, x) parent=Global
            square [-----> func square(x) parent=Global
    sum_of_squares [-----> func lambda(x, y) parent=Global <--.</pre>
                            func lambda() parent=Global
        parent=Global |
 f1:lambda
      return_value [25|
f2:curry
      return_value [-----> func lambda(y) parent=f2
f3:lambda parent=f2
                 y [ 4
      return_value [25]
        parent=Global
f4:lambda
                 x [ 3
                 y [ 4
      return_value [25]
        parent=Global
f5:square
                 x [ 3
      return_value [ 9|
        parent=Global |
|f6:square
                 x [ 4
      return_value [16]
```

<u>Stack</u>

Global

F1 lambda
F2 curry
F3 lambda
F4 lambda
F5 square
F6 square

```
curry(sum_of_squares, 3)((lambda x: 4)(lambda: 1/0))
Global
             curry [-----> func curry(f, x) parent=Global
            square [-----> func square(x) parent=Global
    sum_of_squares [-----> func lambda(x, y) parent=Global <--.</pre>
        parent=Global
 f1:curry
      return_value [-----> func lambda(y) parent=curry
                             func lambda() parent=Global (returns 4)
        parent=Global
 f2:lambda
                 x [-----> func lambda() parent=Global (returns 1/0)
      return_value [ 4|
            parent=f1
 f3:lambda
                 y [ 4|
      return value [25]
        parent=Global |
 f4:lambda
                 x [ 3|
                 y [ 4|
      return_value [25]
        parent=Global
|f5:square
                 x [ 3|
      return_value [ 9|
        parent=Global |
f6:square
                 x [ 4
```

return_value [16|

<u>Stack</u>

Global

- F1 curry F2 lambda F3 lambda

- F4 lambda
- F5 square F6 square

3. Write a make_skipper, which takes in a number n and outputs a function. When this function takes in a number x, it prints out all the numbers between 0 and x, skipping every nth number.

```
>>>a = make_skipper(2)
>>>a(5)
1
3
5
def make_skipper(n):
    def skipper(x):
        for i in range(x+1):
            if i % n != 0:
                print(i)
        return skipper

4. Write compose:
>>> a = compose(lambda x: x * x, lambda x: x + 4)
>>> a(2)
36
def compose(f, g):
    return lambda x: f(g(x))
```

```
5. Write make_alternator.
>>> a = make_alternator(lambda x: x * x, lambda x: x + 4)
>>> a(5)
1
6
9
8
25
def make_alternator(f, g):
  def alternator(n):
    i = 1
    while i <= n:
      if i % 2 == 1:
        print(f(i))
      else:
        print(g(i))
      i += 1
  return alternator
# Alternatively
>>> def make_alternator(f, g):
      def alternator(n):
        for i in range(1, n+1):
          print(f(i)) if i % 2 == 1 else print(g(i))
     return alternator
```

```
6. Here is a version of cons:
def cons(a, b):
    return lambda m: m(a, b)

Write car and cdr to match the example below:
def car(f):
    return f(lambda a, b: a)

def cdr(f):
    return f(lambda a, b: b)

>>> z = cons('hello', 'world')
>>> car(z)
'hello'
>>> cdr(z)
'world'
```

http://pythontutor.com/visualize.html#code=def+cons(a,+b)%3A%0A++return+lambda+m%3A+m(a,+b)%0A%0Adef+car(f)%3A%0A++return+f(lambda+a,+b%3A+a)%0A++%0Adef+cdr(f)%3A%0A++return+f(lambda+a,+b%3A+b)%0A++%0Az+%3D+cons('hello',+'world')%0Acdr(z)&mode=display&origin=opt-frontend.js&cumulative=true&heapPrimitives=false&drawParentPointers=false&textReferences=false&showOnlyOutputs=false&py=2&rawInputLstJSON=%5B%5D&curInstr=17

(see environment diagram on next page)

