Homework 4 R Script

Alexander Hernandez

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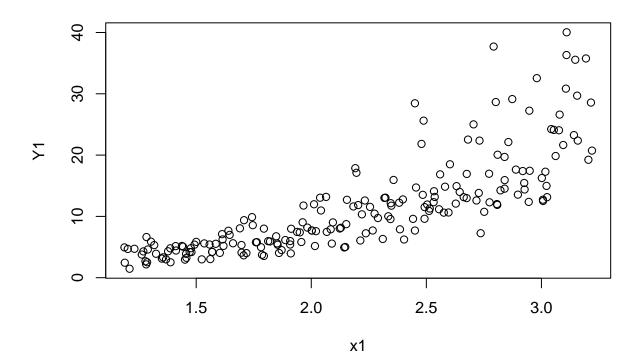
```
library(PASWR)
## Loading required package: lattice
library(MASS)
library(ISLR)
## Warning: package 'ISLR' was built under R version 4.2.2
library(UsingR)
## Loading required package: HistData
## Loading required package: Hmisc
## Loading required package: survival
## Loading required package: Formula
## Loading required package: ggplot2
##
## Attaching package: 'Hmisc'
## The following objects are masked from 'package:base':
##
##
       format.pval, units
##
## Attaching package: 'UsingR'
## The following object is masked from 'package:survival':
##
##
       cancer
```

1) SimDataST

a) Import the data in R and draw a scatterplot using x1 and Y1

```
attach(SimDataST)
plot(x1, Y1,
    main = "SimDataST variables Y1 vs x1")
```

SimDataST variables Y1 vs x1

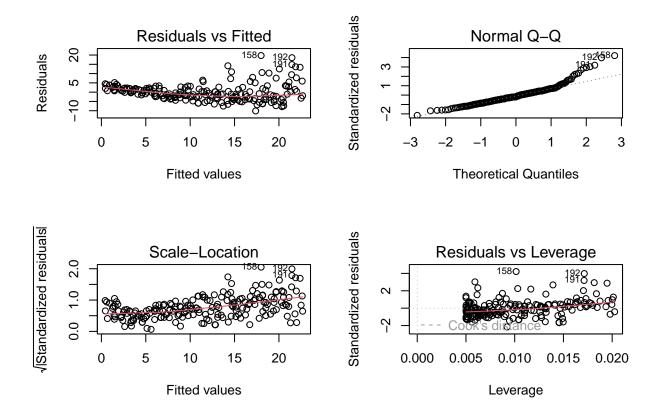


b) Fit a simple linear regression model using Y1 as response and x1 as regressor. Assess the residual plots of the model

```
model1b = lm(Y1 \sim x1)
summary(model1b)
##
## Call:
## lm(formula = Y1 \sim x1)
##
## Residuals:
       Min
##
                1Q Median
                                 ЗQ
## -10.123 -2.918 -0.826
                              1.996
                                    19.713
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -12.5720
                             1.2980 -9.686
                                               <2e-16 ***
## x1
                10.9452
                             0.5702 19.194
                                              <2e-16 ***
```

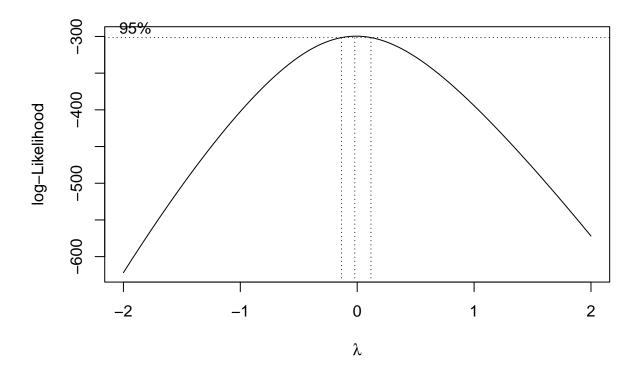
```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.708 on 198 degrees of freedom
## Multiple R-squared: 0.6504, Adjusted R-squared: 0.6487
## F-statistic: 368.4 on 1 and 198 DF, p-value: < 2.2e-16
# Y1 = -12.5720 + 10.9452(x1)

par(mfrow=c(2,2))
plot(model1b)</pre>
```



The residual plots do not look valid.

c) Determine a lambda value using Box-Cox transformation to improve the model boxcox(model1b)



A lambda value around 0.1 would improve the model

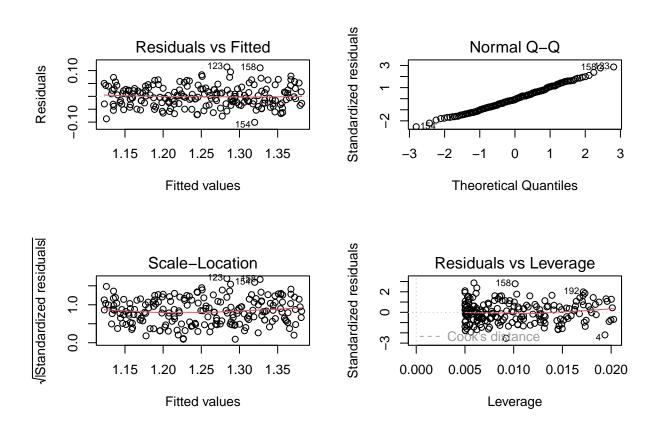
d) Fit a simple regression model after transformation

```
model1d = lm(Y1**0.1 ~ x1)
summary(model1d)
##
## Call:
## lm(formula = Y1^0.1 \sim x1)
##
## Residuals:
##
         Min
                    1Q
                          Median
                                         3Q
   -0.100724 -0.028771 -0.003729 0.025765 0.114189
##
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.971612
                          0.011021
                                      88.16
                                              <2e-16 ***
                          0.004842
                                      26.29
## x1
               0.127278
                                              <2e-16 ***
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
## Residual standard error: 0.03998 on 198 degrees of freedom
## Multiple R-squared: 0.7773, Adjusted R-squared: 0.7761
## F-statistic: 690.9 on 1 and 198 DF, p-value: < 2.2e-16
```

```
# Y1 = -12.5720 + 10.9452(x1)
```

e) Compare the results in b and d. Was the transformation worth it?

par(mfrow=c(2,2))
plot(model1d)



The plots have improved and thus the transformation is worth it

2) Cars93

a) How many variables are included in the dataset

```
names (Cars93)
   [1] "Manufacturer"
                              "Model"
                                                    "Type"
##
                              "Price"
   [4] "Min.Price"
                                                    "Max.Price"
  [7] "MPG.city"
                              "MPG.highway"
                                                    "AirBags"
## [10] "DriveTrain"
                              "Cylinders"
                                                    "EngineSize"
## [13] "Horsepower"
                              "RPM"
                                                    "Rev.per.mile"
## [16] "Man.trans.avail"
                              "Fuel.tank.capacity"
                                                    "Passengers"
## [19] "Length"
                              "Wheelbase"
                                                    "Width"
## [22] "Turn.circle"
                              "Rear.seat.room"
                                                    "Luggage.room"
## [25] "Weight"
                              "Origin"
                                                    "Make"
length(names(Cars93))
## [1] 27
```

b) Fit a regression model for MPG.city using the numerical variables EngineZie, Weight, Passengers, and Price

```
attach(Cars93)
model2b = lm(MPG.city ~ EngineSize +
                        Weight +
                        Passengers +
                        Price)
model2b
##
## Call:
## lm(formula = MPG.city ~ EngineSize + Weight + Passengers + Price)
## Coefficients:
## (Intercept)
                 EngineSize
                                   Weight
                                            Passengers
                                                               Price
                   0.196119
                                -0.008207
                                              0.269622
     46.389413
                                                           -0.035804
##
\# MPG.city = 46.389 + 0.196(EngineSize) - 0.008(Weight) +
             0.270(Passengers) - 0.036(Price)
```

c) Which variables are marked as statistically significant by the marginal t-test?

```
summary(model2b)

##

## Call:

## Im(formula = MPG.city ~ EngineSize + Weight + Passengers + Price)

##

## Residuals:

## Min 1Q Median 3Q Max
```

##
Coefficients:

-6.1207 -1.9098 0.0522 1.1294 13.9580

```
Estimate Std. Error t value Pr(>|t|)
## (Intercept) 46.389413 2.097516 22.116 < 2e-16 ***
## EngineSize 0.196119 0.588880 0.333
                                         0.740
## Weight
             ## Passengers 0.269622 0.424951
                                0.634
                                         0.527
## Price
            -0.035804 0.049179 -0.728
                                         0.469
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 3.06 on 88 degrees of freedom
## Multiple R-squared: 0.7165, Adjusted R-squared: 0.7036
## F-statistic: 55.59 on 4 and 88 DF, p-value: < 2.2e-16
# Weight is the only variable marked as statistically significant
```

d) Which model is selected by AIC criteria?

```
model2d = lm(MPG.city ~ Weight)

AIC(model2b, k=5)

## [1] 496.7923

AIC(model2d, k=2)

## [1] 474.6028

# 496.7923 and 474.6028

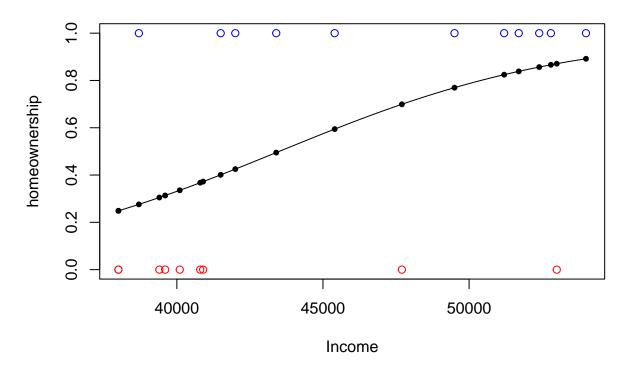
# Given two models, one using EngineSize, Weight, Passengers, and Price and # another using only the statistically significant variable Weight, # the model containing only Weight has a lower AIC and thus is chosen.
```

3) Home Ownership to Family Income

a) Fit a simple logistic regression model for the subject data and display with the scatterplot

```
homedata = read.csv("C:\\repos\\STAT 50001\\Homework 4\\Homedata.csv")
homedata
##
      Income homeownership
## 1
       38000
## 2
       51200
                         1
## 3
       39600
                         0
## 4
       43400
                         1
## 5
       47700
                         0
## 6
                         0
      53000
## 7
      41500
                         1
## 8
       40800
                         0
## 9
       45400
                         1
## 10 52400
                         1
## 11 38700
                         1
## 12 40100
                         0
## 13 49500
                         1
## 14 38000
                         0
## 15 42000
                         1
## 16 54000
## 17 51700
                         1
## 18 39400
                         0
## 19 40900
                         0
## 20 52800
attach(homedata)
model3 = glm(homeownership ~ Income,
                     family = binomial(logit))
model3
##
## Call: glm(formula = homeownership ~ Income, family = binomial(logit))
##
## Coefficients:
## (Intercept)
                     Income
   -8.7395139
                  0.0002009
##
##
## Degrees of Freedom: 19 Total (i.e. Null); 18 Residual
## Null Deviance:
                        27.53
## Residual Deviance: 22.43
                                AIC: 26.43
# homeownership = [1 + exp(8.7395139 - 0.0002009(Income))]^{-1}
plot(homedata, main = "Homeownership vs Income",
     col=ifelse(homeownership==0, "red", "blue"),
)
curve(predict(model3, data.frame(Income=x), type="resp"), add=TRUE)
points(Income, fitted(model3), pch=20)
```

Homeownership vs Income



b) What is the estimated porbability that a family with an income of \$45,000 owns a house?

```
predict(model3, data.frame(Income=45000), type="resp")

## 1
## 0.5747456

# There is a 0.5747 chance a family of income $45,000 owns a house.
```

4) Defaulting on a Credit Card Versus Annual Income and Balance

```
attach(Default)
model4 = glm(default ~ balance,
            family = binomial(logit))
model4
##
## Call: glm(formula = default ~ balance, family = binomial(logit))
##
## Coefficients:
## (Intercept)
                  balance
## -10.651331
                  0.005499
## Degrees of Freedom: 9999 Total (i.e. Null); 9998 Residual
## Null Deviance:
                       2921
## Residual Deviance: 1596 AIC: 1600
# default = [1 + exp( 10.651331 - 0.005499(balance) )]^-1
```

- 5) KeepKidsHealthy fetal smoking and malnutrition on premature births
- a) Extract the variables of interest: gestation, smoking status, mother's height and weight, and birth weight of the babies

```
b = babies[ , c("gestation", "smoke", "ht", "wt1", "wt1", "wt")]
attach(b)
```

b) Clean the data set as there are some missing values coded as 9, 99, or 999

```
bedit = b
is.na(bedit) = bedit == 9 | bedit == 99 | bedit == 999
bedit = na.omit(bedit)
```

c) Calculate the BMI of mothers

```
bedit["BMI"] = (bedit["wt1"] * 0.453592) / (bedit["ht"] * 0.0254)
head(bedit["BMI"], 5)

## BMI
## 1 28.80315
## 2 37.66912
## 3 32.08851
## 5 33.31708
## 6 26.78693
```

d) Create indicator variable (1 for premature and 0 for not premature) babies

```
bedit["premature"] = with(bedit, ifelse(bedit["gestation"] < 259, 1, 0))</pre>
```

e) Fit a logistic regression model with smoke and BMI as a predictor variable and premature as a response variable

```
attach(bedit)
## The following objects are masked from b:
##
       gestation, ht, smoke, wt, wt1
model5 = glm(premature ~ smoke + BMI,
             family = binomial(logit))
model5
## Call: glm(formula = premature ~ smoke + BMI, family = binomial(logit))
## Coefficients:
## (Intercept)
                                     BMI
                      smoke
##
      -3.43570
                    0.09376
                                 0.02491
## Degrees of Freedom: 1152 Total (i.e. Null); 1150 Residual
## Null Deviance:
                        636.8
```

Residual Deviance: 634.6 AIC: 640.6

homeownership = $[1 + exp(3.53570 - 0.09376(smoke) - 0.02491(BMI))]^-1$