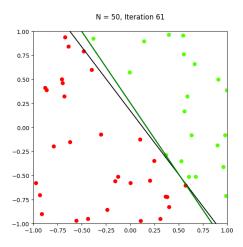
CS 4340 - Project PLA

Austin Hester September 14, 2017

Introduction



Animated GIF of PLA in Action

The Code

```
# Austin Hester
# 09/13/2017
# PLA Python Implementation
# Trains with 50 linearly seperable points
# Tests against 30
import numpy as np
import random
import matplotlib.pyplot as plt
class Perceptron:
    \mathbf{def} __init___(self, N):
        x1, y1, x2, y2 = [random.uniform(-1, 1) for i in
            range(4)
        # for generating linearly seperable data (V)
        self.V = np.array([x2*y1-x1*y2, y2-y1, x1-x2])
        self.X = self.generatePoints(N)
        self.iterations = 0
    def generatePoints(self, N):
        X = []
        for i in range (N):
            x1, x2 = [random.uniform(-1, 1) for i in
                range(2)
            x_{-} = np.array([1, x1, x2])
            # classify based on V, our PLA does not know
                this line
            s = int(np.sign(self.V.T.dot(x_-)))
            x_{-} = np.append(x_{-}, [s])
            X.append(x_{-})
        return np. array (X)
    def plot(self, testPts=None, w_=None, save=False):
        fig = plt. figure (figsize = (6,6))
        plt.xlim(-1,1)
        plt.ylim(-1,1)
        plt.title('N = %s, Iteration %s \ ' % (str(len(
            self.X)), str(self.iterations)))
        # draw line pla is searching for
        V = self.V
        a, b = -V[1]/V[2], -V[0]/V[2]
        l = np. linspace(-1,1)
        plt.plot(1, a*l+b, 'k-')
        ax = fig.add\_subplot(1,1,1)
```

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ax.scatter(self.X[:,1:2], self.X[:,2:3], c=self.X
        [:,3:4], cmap='prism')
    if (w_{-} \text{ is not None and } w_{-}[2] != 0):
         # draw training line
         aa \,, \;\; bb \, = \, -w_-[\, 1\, ] \, / \, w_-[\, 2\, ] \,\,, \;\; -w_-[\, 0\, ] \, / \, w_-[\, 2\, ]
         plt.plot(1, aa*l+bb, 'g-', lw=2)
    if (testPts is not None):
         # draw test points
         ax.scatter(testPts[:,1:2], testPts[:,2:3], c=
             testPts[:,3:4], cmap='cool')
    if save:
         plt.savefig('.\gifs\p_N\%s' \% (str(len(self.X)
             )), dpi=100, bbox_inches='tight')
    else:
         plt.show()
# returns percentage of missed points
def classify Error (self, w<sub>-</sub>, pts=None):
    if pts is None:
         pts = self.X[:,:3]
         S = self.X[:,3:4]
    else:
         S = pts[:,3:4]
         pts = pts[:,:3]
    M = len(pts)
    n_{mispts} = 0
    for x_-, s in zip(pts, S):
         if int(np.sign(w_{-}.T.dot(x_{-}))) != s:
             n_mispts += 1
    print("Missed points: %d" % (n_mispts))
    print("w_: ", w_)
    err = n_mispts / float(M)
    return err
# Pick a random misclassified pt (according to given
   w_{-})
def pickMisclPoint(self, w_):
    pts = self.X[:,:3]
    S = self.X[:, 3:4]
    mispts = []
    for x,d in zip(pts, S):
         if int(np.sign(w_{-}.T.dot(x))) != d:
             mispts.append((x, d))
    return mispts [random.randrange(0, len(mispts))]
# Run PLA on data contained in self.X
```

```
def pla(self, c=0.01, save=False):
        X = self.X[:,:3]
        N = len(X)
        w_{-} = np.zeros(len(X[0]))
        it = 0
        print("Iteration %d: " % (it))
        # Run while there are misclassified points
        # or we get to 1,000 iterations
        while self.classifyError(w_-) != 0 or it > 1000:
            it += 1
            print("Iteration %d: " % (it))
            # pick mispicked pt
            x, d = self.pickMisclPoint(w_{-})
            w_- += c*d*x
            if save:
                 self.plot(vec=w_, save=True)
                 plt.title('N = %s, Iteration %s \ n' % (str
                    (N), \mathbf{str}(it))
                 plt.savefig('.\gifs\p_N\%s_it%s' % (str(N)
                    str(it)), dpi=100, bbox_inches='tight',
        self.w = w_{-}
        self.iterations = it
    # Test our test points using classifyError
    def checkTestPoints(self, testPts, w_):
        print ("-----
        print("Test Info")
        print ("-----
        return self.classifyError(w_, pts=testPts)
\mathbf{def} \ \operatorname{testPLA}(p, M):
    testPts = p.generatePoints(M)
    print("—
    print("Testing data:\n", testPts)
    testError = p.checkTestPoints(testPts, p.w)
    print("Test Error:", round(testError * 100, 3), "%")
    print("-----
    return testPts, testError
# initialize perceptron with 50 training points
train = 50
test = 30
save = False
```

```
p = Perceptron(train)
print("_______")
print("Training data:\n", p.X)
print("______")
p. pla(save=save) # run pla, save=True to generate gif

testPts, testErr = testPLA(p, test)

if not save:
    p. plot(testPts=testPts, w_=p.w)
```

Notes