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$$f(x, y, z) = (x+y)z \quad \text{eval at } x = -3$$

$$y = 9$$

$$z = -2$$

a)

$$\begin{array}{l} x_{-3} \quad -2 \\ y_9 \quad -2 \\ z_{-2} \quad 6 \end{array} \quad \begin{array}{c} (+) \quad 6 \quad -2 \\ (*) \quad f \quad -12 \end{array}$$

blue = gradient

$$\frac{da}{dx} = 1 \quad \frac{da}{dy} = 1$$

$$\frac{\partial f}{\partial a} = z \quad \frac{\partial f}{\partial z} = a$$

b) standard:  $h'(x) = f'(g(x))g'(x)$

modified:  $h'(x) = g'(f(x))f'(x)$

$$\frac{\partial f}{\partial y} = \frac{\partial f}{\partial a} \frac{da}{dy} \quad \frac{\partial f}{\partial x} = \frac{\partial f}{\partial a} \frac{da}{dx}$$

↑ upstream    ↑ local

standard:  $\frac{dh}{dx} = \frac{df}{dg} \cdot \frac{dg}{dx}$

modified:  $\frac{dh}{dx} = \frac{dg}{df} \cdot \frac{df}{dx}$

$$\frac{dg}{df} = z$$

$$\frac{df}{dx} = 1$$

$$\frac{dh}{dx} = \frac{dg}{df} \cdot \frac{df}{dx} = (-2)(1) = -2$$

$$\frac{dg}{dz} = a$$

$$\frac{df}{dy} = 1$$

$$\frac{dh}{dy} = \frac{dg}{df} \cdot \frac{df}{dy} = (-2)(1) = -2$$

$$\frac{dh}{dz} = \frac{dg}{dz} = 6$$

answers: -2, -2, 6

Note:  $g'(f(x))$  doesn't make sense because

$(x+y)z \rightarrow z$  is independent from  $x$  and  $y$ .

$f(x)$  is a linear function so it's the same,

but for something like  $\log(x)$ , it fails.