

$$\text{In[*]:= } \rho := z_1 + Z_1 - z_2 Z_2 - G z_3^2 Z_2^2 - z_3 Z_3 - g z_2^2 Z_3^2 - a \left( z_2^2 Z_2^2 - 4 z_2 z_3 Z_2 Z_3 + z_3^2 Z_3^2 \right)$$

$$\text{In[*]:= } \rho^2$$

$$\text{Out[*]= } \rho^2$$

$$\text{In[*]:= } \rho^2 := D[\rho, z_2]$$

$$\text{In[*]:= } \text{:=} \text{eho}^2$$

$$\text{Out[*]= } 2 \text{ eho}^2$$

$$\text{In[*]:= } \rho^2$$

$$\text{Out[*]= } -Z_2 - 2 g z_2 Z_3^2 - a \left( 2 z_2 Z_2^2 - 4 z_3 Z_2 Z_3 \right)$$

$$\text{In[*]:= } \rho^2 \theta := D[\rho, Z_2]$$

$$\text{In[*]:= } \rho^3 := D[\rho, z_3]$$

$$\text{In[*]:= } \rho^3 \theta := D[\rho, Z_3]$$

$$\text{In[*]:= } \rho^3 \theta$$

$$\text{Out[*]= } -z_3 - 2 g z_2^2 Z_3 - a \left( -4 z_2 z_3 Z_2 + 2 z_3^2 Z_3 \right)$$

$$\text{In[*]:= } x_2 := e^{i t} s + s^3 \left( a e^{i t} + 2 a c^2 e^{i t} - 4 i a e^{i t} t \right)$$

$$\text{In[*]:= } x_3 := c * s + \left( -2 a c - a c^3 - 2 c e^{2 i t} g \right) * s^3$$

$$\text{In[*]:= } y_2 := (x_2) / (\text{Exp}[I * t] * s)$$

$$\text{In[*]:= } y_2$$

$$\text{Out[*]= } \frac{1}{s} e^{-i t} \left( e^{i t} s + s^3 \left( a e^{i t} + 2 a c^2 e^{i t} - 4 i a e^{i t} t \right) \right)$$

$$\text{In[*]:= } \text{Simplify} \left[ \frac{1}{s} e^{-i t} \left( e^{i t} s + s^3 \left( a e^{i t} + 2 a c^2 e^{i t} - 4 i a e^{i t} t \right) \right) \right]$$

$$\text{Out[*]= } 1 + a s^2 \left( 1 + 2 c^2 - 4 i t \right)$$

$$\text{In[*]:= } y_2 := \%$$

$$\text{In[*]:= } y_2$$

$$\text{In[*]:= } y_2$$

$$\text{In[*]:= } y_2 := 1 + a s^2 \left( 1 + 2 c^2 - 4 i t \right)$$

$$\text{In[*]:= } y_2$$

$$\text{Out[*]= } 1 + a s^2 \left( 1 + 2 c^2 - 4 i t \right)$$

$$\text{In[*]:= } y_3 := (x_3) / (c * s)$$

$$\text{In[*]:= } y_3$$

$$\text{Out[*]= } \frac{1}{c s} \left( c s + \left( -2 a c - a c^3 - 2 c e^{2 i t} g \right) s^3 \right)$$

In[\*]:= Simplify[ $\frac{1}{c s} (c s + (-2 a c - a c^3 - 2 c e^{2 i t} g) s^3)$ ]

Out[\*]=  $1 - a (2 + c^2) s^2 - 2 e^{2 i t} g s^2$

In[\*]:= y3 :=  $1 - a (2 + c^2) s^2 - 2 e^{2 i t} g s^2$

In[\*]:= Collect[ $1 - a (2 + c^2) s^2 - 2 e^{2 i t} g s^2, s$ ]

Out[\*]=  $1 + (-a (2 + c^2) - 2 e^{2 i t} g) s^2$

In[\*]:= y3 :=  $1 - a (2 + c^2) s^2 - 2 e^{2 i t} g s^2$

In[\*]:= y3 :=  $1 + (-a (2 + c^2) - 2 e^{2 i t} g) s^2$

In[\*]:= y3

Out[\*]=  $1 + (-a (2 + c^2) - 2 e^{2 i t} g) s^2$

In[\*]:= y2J :=  $1 + a * J * s^2 (1 + 2 c^2 - 4 i t)$

In[\*]:= y2J

Out[\*]=  $1 + a J s^2 (1 + 2 c^2 - 4 i t)$

In[\*]:= y2

Out[\*]=  $1 + a s^2 (1 + 2 c^2 - 4 i t)$

In[\*]:= y3J :=  $1 + (-a (2 + c^2) - 2 e^{2 i t} g) * J * s^2$

In[\*]:= A := Sum[bJ \* Exp[I \* J \* t], {J, -6, 6}]

In[\*]:= A

Out[\*]=  $e^{-6 i t} b_{-6} + e^{-5 i t} b_{-5} + e^{-4 i t} b_{-4} + e^{-3 i t} b_{-3} + e^{-2 i t} b_{-2} + e^{-i t} b_{-1} + b_0 + e^{i t} b_1 + e^{2 i t} b_2 + e^{3 i t} b_3 + e^{4 i t} b_4 + e^{5 i t} b_5 + e^{6 i t} b_6$

In[\*]:= dz2 := D[x2, t]

In[\*]:= dz2

Out[\*]=  $i e^{i t} s + s^3 (-3 i a e^{i t} + 2 i a c^2 e^{i t} + 4 a e^{i t} t)$

In[\*]:= y23

Out[\*]= y23

In[\*]:= Sum[y2J, {J, -1, 1}]

Out[\*]= 3

In[\*]:= y2J /. J -> 3

Out[\*]=  $1 + 3 a s^2 (1 + 2 c^2 - 4 i t)$

In[\*]:= y2J /. J -> k

Out[\*]=  $1 + a k s^2 (1 + 2 c^2 - 4 i t)$

```
In[ ]:= I1 := Exp[I * J * t] * y2J * A * dz2
```

```
In[ ]:= I1
```

```
Out[ ]:= e^{i J t} (1 + a J s^2 (1 + 2 c^2 - 4 i t)) (i e^{i t} s + s^3 (-3 i a e^{i t} + 2 i a c^2 e^{i t} + 4 a e^{i t} t))
(e^{-6 i t} b_{-6} + e^{-5 i t} b_{-5} + e^{-4 i t} b_{-4} + e^{-3 i t} b_{-3} + e^{-2 i t} b_{-2} +
e^{-i t} b_{-1} + b_0 + e^{i t} b_1 + e^{2 i t} b_2 + e^{3 i t} b_3 + e^{4 i t} b_4 + e^{5 i t} b_5 + e^{6 i t} b_6)
```

```
In[ ]:= Simplify[%51]
```

```
Out[ ]:= %51
```

```
In[ ]:= Expand[%52]
```

```
Out[ ]:= %52
```

```
In[ ]:= % / s
```

```
Out[ ]:= \frac{%52}{s}
```

```
In[ ]:= Simplify[%54]
```

```
Out[ ]:= %54
```

```
In[ ]:= n := Expand[%55]
```

```
In[ ]:= Collect[%, Exp[I * t]]
```

```
In[ ]:= % /. J -> -Infinity
```

```
In[ ]:= Collect[%57, Exp[I * J * t]]
```

```
Out[ ]:= %57
```

```
In[ ]:= n
```

```
Out[ ]:= %55
```

```
In[ ]:= FullSimplify[%62]
```

```
Out[ ]:= %62
```

```
In[ ]:= n /. J -> 1
```

```
Out[ ]:= %55
```

```
In[ ]:= Collect[%, Exp[I * t]]
```

```
Out[ ]:= %55
```

```
In[ ]:= I1new := i b_{-2} - 2 i a s^2 b_{-2} + 4 i a c^2 s^2 b_{-2} - 3 i a^2 s^4 b_{-2} - 4 i a^2 c^2 s^4 b_{-2} +
4 i a^2 c^4 s^4 b_{-2} + 8 a s^2 t b_{-2} - 8 a^2 s^4 t b_{-2} + 16 a^2 c^2 s^4 t b_{-2} - 16 i a^2 s^4 t^2 b_{-2}
```

```
In[ ]:= Collect[I1new, s]
```

```
Out[ ]:= i b_{-2} + s^2 (-2 i a b_{-2} + 4 i a c^2 b_{-2} + 8 a t b_{-2}) +
s^4 (-3 i a^2 b_{-2} - 4 i a^2 c^2 b_{-2} + 4 i a^2 c^4 b_{-2} - 8 a^2 t b_{-2} + 16 a^2 c^2 t b_{-2} - 16 i a^2 t^2 b_{-2})
```

In[\*]:= **I1new1 := i b<sub>-2</sub> + s<sup>2</sup> (-2 i a b<sub>-2</sub> + 4 i a c<sup>2</sup> b<sub>-2</sub> + 8 a t b<sub>-2</sub>)**

In[\*]:= **n /. J -> 2**

Out[\*]:= **i b<sub>-2</sub> - 2 i a s<sup>2</sup> b<sub>-2</sub> + 4 i a c<sup>2</sup> s<sup>2</sup> b<sub>-2</sub> - 3 i a<sup>2</sup> s<sup>4</sup> b<sub>-2</sub> - 4 i a<sup>2</sup> c<sup>2</sup> s<sup>4</sup> b<sub>-2</sub> +  
4 i a<sup>2</sup> c<sup>4</sup> s<sup>4</sup> b<sub>-2</sub> + 8 a s<sup>2</sup> t b<sub>-2</sub> - 8 a<sup>2</sup> s<sup>4</sup> t b<sub>-2</sub> + 16 a<sup>2</sup> c<sup>2</sup> s<sup>4</sup> t b<sub>-2</sub> - 16 i a<sup>2</sup> s<sup>4</sup> t<sup>2</sup> b<sub>-2</sub>**

In[\*]:= **Collect[%, Exp[I \* t]]**

Out[\*]:= **i b<sub>-2</sub> - 2 i a s<sup>2</sup> b<sub>-2</sub> + 4 i a c<sup>2</sup> s<sup>2</sup> b<sub>-2</sub> - 3 i a<sup>2</sup> s<sup>4</sup> b<sub>-2</sub> - 4 i a<sup>2</sup> c<sup>2</sup> s<sup>4</sup> b<sub>-2</sub> +  
4 i a<sup>2</sup> c<sup>4</sup> s<sup>4</sup> b<sub>-2</sub> + 8 a s<sup>2</sup> t b<sub>-2</sub> - 8 a<sup>2</sup> s<sup>4</sup> t b<sub>-2</sub> + 16 a<sup>2</sup> c<sup>2</sup> s<sup>4</sup> t b<sub>-2</sub> - 16 i a<sup>2</sup> s<sup>4</sup> t<sup>2</sup> b<sub>-2</sub>**

In[\*]:= **i b<sub>-3</sub> - i a s<sup>2</sup> b<sub>-3</sub> + 6 i a c<sup>2</sup> s<sup>2</sup> b<sub>-3</sub> - 6 i a<sup>2</sup> s<sup>4</sup> b<sub>-3</sub> - 8 i a<sup>2</sup> c<sup>2</sup> s<sup>4</sup> b<sub>-3</sub> +  
8 i a<sup>2</sup> c<sup>4</sup> s<sup>4</sup> b<sub>-3</sub> + 12 a s<sup>2</sup> t b<sub>-3</sub> - 16 a<sup>2</sup> s<sup>4</sup> t b<sub>-3</sub> + 32 a<sup>2</sup> c<sup>2</sup> s<sup>4</sup> t b<sub>-3</sub> - 32 i a<sup>2</sup> s<sup>4</sup> t<sup>2</sup> b<sub>-3</sub>**

Out[\*]:= **i b<sub>-3</sub> - i a s<sup>2</sup> b<sub>-3</sub> + 6 i a c<sup>2</sup> s<sup>2</sup> b<sub>-3</sub> - 6 i a<sup>2</sup> s<sup>4</sup> b<sub>-3</sub> - 8 i a<sup>2</sup> c<sup>2</sup> s<sup>4</sup> b<sub>-3</sub> +  
8 i a<sup>2</sup> c<sup>4</sup> s<sup>4</sup> b<sub>-3</sub> + 12 a s<sup>2</sup> t b<sub>-3</sub> - 16 a<sup>2</sup> s<sup>4</sup> t b<sub>-3</sub> + 32 a<sup>2</sup> c<sup>2</sup> s<sup>4</sup> t b<sub>-3</sub> - 32 i a<sup>2</sup> s<sup>4</sup> t<sup>2</sup> b<sub>-3</sub>**

In[\*]:= **Collect[%, s]**

Out[\*]:= **i b<sub>-3</sub> + s<sup>2</sup> (-i a b<sub>-3</sub> + 6 i a c<sup>2</sup> b<sub>-3</sub> + 12 a t b<sub>-3</sub>) +  
s<sup>4</sup> (-6 i a<sup>2</sup> b<sub>-3</sub> - 8 i a<sup>2</sup> c<sup>2</sup> b<sub>-3</sub> + 8 i a<sup>2</sup> c<sup>4</sup> b<sub>-3</sub> - 16 a<sup>2</sup> t b<sub>-3</sub> + 32 a<sup>2</sup> c<sup>2</sup> t b<sub>-3</sub> - 32 i a<sup>2</sup> t<sup>2</sup> b<sub>-3</sub>)**

In[\*]:= **I1new2 := i b<sub>-3</sub> + s<sup>2</sup> (-i a b<sub>-3</sub> + 6 i a c<sup>2</sup> b<sub>-3</sub> + 12 a t b<sub>-3</sub>)**

In[\*]:= **n /. J -> 3**

Out[\*]:= **i b<sub>-2</sub> - 2 i a s<sup>2</sup> b<sub>-2</sub> + 4 i a c<sup>2</sup> s<sup>2</sup> b<sub>-2</sub> - 3 i a<sup>2</sup> s<sup>4</sup> b<sub>-2</sub> - 4 i a<sup>2</sup> c<sup>2</sup> s<sup>4</sup> b<sub>-2</sub> +  
4 i a<sup>2</sup> c<sup>4</sup> s<sup>4</sup> b<sub>-2</sub> + 8 a s<sup>2</sup> t b<sub>-2</sub> - 8 a<sup>2</sup> s<sup>4</sup> t b<sub>-2</sub> + 16 a<sup>2</sup> c<sup>2</sup> s<sup>4</sup> t b<sub>-2</sub> - 16 i a<sup>2</sup> s<sup>4</sup> t<sup>2</sup> b<sub>-2</sub>**

In[\*]:= **Collect[%, Exp[I \* t]]**

Out[\*]:= **i b<sub>-2</sub> - 2 i a s<sup>2</sup> b<sub>-2</sub> + 4 i a c<sup>2</sup> s<sup>2</sup> b<sub>-2</sub> - 3 i a<sup>2</sup> s<sup>4</sup> b<sub>-2</sub> - 4 i a<sup>2</sup> c<sup>2</sup> s<sup>4</sup> b<sub>-2</sub> +  
4 i a<sup>2</sup> c<sup>4</sup> s<sup>4</sup> b<sub>-2</sub> + 8 a s<sup>2</sup> t b<sub>-2</sub> - 8 a<sup>2</sup> s<sup>4</sup> t b<sub>-2</sub> + 16 a<sup>2</sup> c<sup>2</sup> s<sup>4</sup> t b<sub>-2</sub> - 16 i a<sup>2</sup> s<sup>4</sup> t<sup>2</sup> b<sub>-2</sub>**

In[\*]:= **i b<sub>-4</sub> + 8 i a c<sup>2</sup> s<sup>2</sup> b<sub>-4</sub> - 9 i a<sup>2</sup> s<sup>4</sup> b<sub>-4</sub> - 12 i a<sup>2</sup> c<sup>2</sup> s<sup>4</sup> b<sub>-4</sub> + 12 i a<sup>2</sup> c<sup>4</sup> s<sup>4</sup> b<sub>-4</sub> +  
16 a s<sup>2</sup> t b<sub>-4</sub> - 24 a<sup>2</sup> s<sup>4</sup> t b<sub>-4</sub> + 48 a<sup>2</sup> c<sup>2</sup> s<sup>4</sup> t b<sub>-4</sub> - 48 i a<sup>2</sup> s<sup>4</sup> t<sup>2</sup> b<sub>-4</sub>**

Out[\*]:= **i b<sub>-4</sub> + 8 i a c<sup>2</sup> s<sup>2</sup> b<sub>-4</sub> - 9 i a<sup>2</sup> s<sup>4</sup> b<sub>-4</sub> - 12 i a<sup>2</sup> c<sup>2</sup> s<sup>4</sup> b<sub>-4</sub> + 12 i a<sup>2</sup> c<sup>4</sup> s<sup>4</sup> b<sub>-4</sub> +  
16 a s<sup>2</sup> t b<sub>-4</sub> - 24 a<sup>2</sup> s<sup>4</sup> t b<sub>-4</sub> + 48 a<sup>2</sup> c<sup>2</sup> s<sup>4</sup> t b<sub>-4</sub> - 48 i a<sup>2</sup> s<sup>4</sup> t<sup>2</sup> b<sub>-4</sub>**

In[\*]:= **Collect[%, s]**

Out[\*]:= **i b<sub>-4</sub> + s<sup>2</sup> (8 i a c<sup>2</sup> b<sub>-4</sub> + 16 a t b<sub>-4</sub>) +  
s<sup>4</sup> (-9 i a<sup>2</sup> b<sub>-4</sub> - 12 i a<sup>2</sup> c<sup>2</sup> b<sub>-4</sub> + 12 i a<sup>2</sup> c<sup>4</sup> b<sub>-4</sub> - 24 a<sup>2</sup> t b<sub>-4</sub> + 48 a<sup>2</sup> c<sup>2</sup> t b<sub>-4</sub> - 48 i a<sup>2</sup> t<sup>2</sup> b<sub>-4</sub>)**

In[\*]:= **I1new3 := i b<sub>-4</sub> + s<sup>2</sup> (8 i a c<sup>2</sup> b<sub>-4</sub> + 16 a t b<sub>-4</sub>)**

In[\*]:= **I1new2**

Out[\*]:= **i b<sub>-3</sub> + s<sup>2</sup> (-i a b<sub>-3</sub> + 6 i a c<sup>2</sup> b<sub>-3</sub> + 12 a t b<sub>-3</sub>)**

In[\*]:= **I1new3**

Out[\*]:= **i b<sub>-4</sub> + s<sup>2</sup> (8 i a c<sup>2</sup> b<sub>-4</sub> + 16 a t b<sub>-4</sub>)**

$$\text{In}[*]:= \mathbf{i} \, \mathbf{b}_{-4} + \mathbf{s}^2 \left( 8 \, \mathbf{i} \, \mathbf{a} \, \mathbf{c}^2 \, \mathbf{b}_{-4} + 16 \, \mathbf{a} \, \mathbf{t} \, \mathbf{b}_{-4} \right)$$

$$\text{Out}[*]= \mathbf{i} \, \mathbf{b}_{-4} + \mathbf{s}^2 \left( 8 \, \mathbf{i} \, \mathbf{a} \, \mathbf{c}^2 \, \mathbf{b}_{-4} + 16 \, \mathbf{a} \, \mathbf{t} \, \mathbf{b}_{-4} \right)$$

$$\text{In}[*]:= \mathbf{I1new1}$$

$$\text{Out}[*]= \mathbf{i} \, \mathbf{b}_{-2} + \mathbf{s}^2 \left( -2 \, \mathbf{i} \, \mathbf{a} \, \mathbf{b}_{-2} + 4 \, \mathbf{i} \, \mathbf{a} \, \mathbf{c}^2 \, \mathbf{b}_{-2} + 8 \, \mathbf{a} \, \mathbf{t} \, \mathbf{b}_{-2} \right)$$

$$\text{In}[*]:= \mathbf{a} := \mathbf{0}$$

$$\text{In}[*]:= \rho 2$$

$$\text{Out}[*]= -Z_2 - 2 \, g \, z_2 \, Z_3^2$$

$$\text{In}[*]:= \mathbf{x3}$$

$$\text{Out}[*]= \mathbf{c} \, \mathbf{s} - 2 \, \mathbf{c} \, \mathbf{e}^{2 \, \mathbf{i} \, \mathbf{t}} \, \mathbf{g} \, \mathbf{s}^3$$

$$\text{In}[*]:= \mathbf{X3} := \mathbf{c} \, \mathbf{s} - 2 \, \mathbf{c} \, \mathbf{e}^{-2 \, \mathbf{i} \, \mathbf{t}} * \mathbf{G} * \mathbf{s}^3$$

$$\text{In}[*]:= \mathbf{x2}$$

$$\text{Out}[*]= \mathbf{e}^{\mathbf{i} \, \mathbf{t}} \, \mathbf{s}$$

$$\text{In}[*]:= \mathbf{X2} := \mathbf{s} * \text{Exp}[-\mathbf{I} * \mathbf{t}]$$

$$\text{In}[*]:= \mathbf{q2} := \rho 2 /. \{z_2 \rightarrow x2, Z_2 \rightarrow X2, Z_3 \rightarrow X3\}$$

$$\text{In}[*]:= \mathbf{q2}$$

$$\text{Out}[*]= -\mathbf{e}^{-\mathbf{i} \, \mathbf{t}} \, \mathbf{s} - 2 \, \mathbf{e}^{\mathbf{i} \, \mathbf{t}} \, \mathbf{g} \, \mathbf{s} \left( \mathbf{c} \, \mathbf{s} - 2 \, \mathbf{c} \, \mathbf{e}^{-2 \, \mathbf{i} \, \mathbf{t}} \, \mathbf{G} \, \mathbf{s}^3 \right)^2$$

$$\text{In}[*]:= \text{FullSimplify}[-\mathbf{e}^{-\mathbf{i} \, \mathbf{t}} \, \mathbf{s} - 2 \, \mathbf{e}^{\mathbf{i} \, \mathbf{t}} \, \mathbf{g} \, \mathbf{s} \left( \mathbf{c} \, \mathbf{s} - 2 \, \mathbf{c} \, \mathbf{e}^{-2 \, \mathbf{i} \, \mathbf{t}} \, \mathbf{G} \, \mathbf{s}^3 \right)^2]$$

$$\text{Out}[*]= \mathbf{e}^{-\mathbf{i} \, \mathbf{t}} \, \mathbf{s} \left( -1 - 2 \, \mathbf{c}^2 \, \mathbf{e}^{2 \, \mathbf{i} \, \mathbf{t}} \, \mathbf{g} \left( \mathbf{s} - 2 \, \mathbf{e}^{-2 \, \mathbf{i} \, \mathbf{t}} \, \mathbf{G} \, \mathbf{s}^3 \right)^2 \right)$$

$$\text{In}[*]:= \text{Expand}[\mathbf{e}^{-\mathbf{i} \, \mathbf{t}} \, \mathbf{s} \left( -1 - 2 \, \mathbf{c}^2 \, \mathbf{e}^{2 \, \mathbf{i} \, \mathbf{t}} \, \mathbf{g} \left( \mathbf{s} - 2 \, \mathbf{e}^{-2 \, \mathbf{i} \, \mathbf{t}} \, \mathbf{G} \, \mathbf{s}^3 \right)^2 \right)]$$

$$\text{Out}[*]= -\mathbf{e}^{-\mathbf{i} \, \mathbf{t}} \, \mathbf{s} - 2 \, \mathbf{c}^2 \, \mathbf{e}^{\mathbf{i} \, \mathbf{t}} \, \mathbf{g} \, \mathbf{s}^3 + 8 \, \mathbf{c}^2 \, \mathbf{e}^{-\mathbf{i} \, \mathbf{t}} \, \mathbf{g} \, \mathbf{G} \, \mathbf{s}^5 - 8 \, \mathbf{c}^2 \, \mathbf{e}^{-3 \, \mathbf{i} \, \mathbf{t}} \, \mathbf{g} \, \mathbf{G}^2 \, \mathbf{s}^7$$

$$\text{In}[*]:= \mathbf{q2t} := -\mathbf{e}^{-\mathbf{i} \, \mathbf{t}} \, \mathbf{s} - 2 \, \mathbf{c}^2 \, \mathbf{e}^{\mathbf{i} \, \mathbf{t}} \, \mathbf{g} \, \mathbf{s}^3$$

$$\text{In}[*]:= \mathbf{I2} := \text{Exp}[\mathbf{I} * \mathbf{J} * \mathbf{t}] * \mathbf{y2J} * \mathbf{A} * \mathbf{dz2} * \mathbf{q2t}$$

$$\text{In}[*]:= \mathbf{I2}$$

$$\text{Out}[*]= \mathbf{i} \, \mathbf{e}^{\mathbf{i} \, \mathbf{t} + \mathbf{i} \, \mathbf{J} \, \mathbf{t}} \, \mathbf{s} \left( -\mathbf{e}^{-\mathbf{i} \, \mathbf{t}} \, \mathbf{s} - 2 \, \mathbf{c}^2 \, \mathbf{e}^{\mathbf{i} \, \mathbf{t}} \, \mathbf{g} \, \mathbf{s}^3 \right) \\ \left( \mathbf{e}^{-6 \, \mathbf{i} \, \mathbf{t}} \, \mathbf{b}_{-6} + \mathbf{e}^{-5 \, \mathbf{i} \, \mathbf{t}} \, \mathbf{b}_{-5} + \mathbf{e}^{-4 \, \mathbf{i} \, \mathbf{t}} \, \mathbf{b}_{-4} + \mathbf{e}^{-3 \, \mathbf{i} \, \mathbf{t}} \, \mathbf{b}_{-3} + \mathbf{e}^{-2 \, \mathbf{i} \, \mathbf{t}} \, \mathbf{b}_{-2} + \mathbf{e}^{-\mathbf{i} \, \mathbf{t}} \, \mathbf{b}_{-1} + \right. \\ \left. \mathbf{b}_0 + \mathbf{e}^{\mathbf{i} \, \mathbf{t}} \, \mathbf{b}_1 + \mathbf{e}^{2 \, \mathbf{i} \, \mathbf{t}} \, \mathbf{b}_2 + \mathbf{e}^{3 \, \mathbf{i} \, \mathbf{t}} \, \mathbf{b}_3 + \mathbf{e}^{4 \, \mathbf{i} \, \mathbf{t}} \, \mathbf{b}_4 + \mathbf{e}^{5 \, \mathbf{i} \, \mathbf{t}} \, \mathbf{b}_5 + \mathbf{e}^{6 \, \mathbf{i} \, \mathbf{t}} \, \mathbf{b}_6 \right)$$

In[ ]:= **ExpandAll[%]**

Out[ ]:= 
$$\begin{aligned} & -i e^{-6it+iJt} s^2 b_{-6} - 2i c^2 e^{-4it+iJt} g s^4 b_{-6} - i e^{-5it+iJt} s^2 b_{-5} - \\ & 2i c^2 e^{-3it+iJt} g s^4 b_{-5} - i e^{-4it+iJt} s^2 b_{-4} - 2i c^2 e^{-2it+iJt} g s^4 b_{-4} - \\ & i e^{-3it+iJt} s^2 b_{-3} - 2i c^2 e^{-it+iJt} g s^4 b_{-3} - i e^{-2it+iJt} s^2 b_{-2} - 2i c^2 e^{it+iJt} g s^4 b_{-2} - \\ & i e^{-it+iJt} s^2 b_{-1} - 2i c^2 e^{it+iJt} g s^4 b_{-1} - i e^{it+iJt} s^2 b_0 - 2i c^2 e^{2it+iJt} g s^4 b_0 - \\ & i e^{it+iJt} s^2 b_1 - 2i c^2 e^{3it+iJt} g s^4 b_1 - i e^{2it+iJt} s^2 b_2 - 2i c^2 e^{4it+iJt} g s^4 b_2 - \\ & i e^{3it+iJt} s^2 b_3 - 2i c^2 e^{5it+iJt} g s^4 b_3 - i e^{4it+iJt} s^2 b_4 - 2i c^2 e^{6it+iJt} g s^4 b_4 - \\ & i e^{5it+iJt} s^2 b_5 - 2i c^2 e^{7it+iJt} g s^4 b_5 - i e^{6it+iJt} s^2 b_6 - 2i c^2 e^{8it+iJt} g s^4 b_6 \end{aligned}$$

In[ ]:= **Collect[%, s]**

Out[ ]:= 
$$\begin{aligned} & s^2 \left( -i e^{-6it+iJt} b_{-6} - i e^{-5it+iJt} b_{-5} - i e^{-4it+iJt} b_{-4} - \right. \\ & \quad i e^{-3it+iJt} b_{-3} - i e^{-2it+iJt} b_{-2} - i e^{-it+iJt} b_{-1} - i e^{it+iJt} b_0 - i e^{it+iJt} b_1 - \\ & \quad i e^{2it+iJt} b_2 - i e^{3it+iJt} b_3 - i e^{4it+iJt} b_4 - i e^{5it+iJt} b_5 - i e^{6it+iJt} b_6 \left. \right) + \\ & s^4 \left( -2i c^2 e^{-4it+iJt} g b_{-6} - 2i c^2 e^{-3it+iJt} g b_{-5} - 2i c^2 e^{-2it+iJt} g b_{-4} - \right. \\ & \quad 2i c^2 e^{-it+iJt} g b_{-3} - 2i c^2 e^{it+iJt} g b_{-2} - 2i c^2 e^{it+iJt} g b_{-1} - 2i c^2 e^{2it+iJt} g b_0 - \\ & \quad 2i c^2 e^{3it+iJt} g b_1 - 2i c^2 e^{4it+iJt} g b_2 - 2i c^2 e^{5it+iJt} g b_3 - \\ & \quad \left. 2i c^2 e^{6it+iJt} g b_4 - 2i c^2 e^{7it+iJt} g b_5 - 2i c^2 e^{8it+iJt} g b_6 \right) \end{aligned}$$

In[ ]:= **%/s^2**

Out[ ]:= 
$$\begin{aligned} & \frac{1}{s^2} \left( s^2 \left( -i e^{-6it+iJt} b_{-6} - i e^{-5it+iJt} b_{-5} - i e^{-4it+iJt} b_{-4} - \right. \right. \\ & \quad i e^{-3it+iJt} b_{-3} - i e^{-2it+iJt} b_{-2} - i e^{-it+iJt} b_{-1} - i e^{it+iJt} b_0 - i e^{it+iJt} b_1 - \\ & \quad i e^{2it+iJt} b_2 - i e^{3it+iJt} b_3 - i e^{4it+iJt} b_4 - i e^{5it+iJt} b_5 - i e^{6it+iJt} b_6 \left. \right) + \\ & s^4 \left( -2i c^2 e^{-4it+iJt} g b_{-6} - 2i c^2 e^{-3it+iJt} g b_{-5} - 2i c^2 e^{-2it+iJt} g b_{-4} - \right. \\ & \quad 2i c^2 e^{-it+iJt} g b_{-3} - 2i c^2 e^{it+iJt} g b_{-2} - 2i c^2 e^{it+iJt} g b_{-1} - 2i c^2 e^{2it+iJt} g b_0 - \\ & \quad 2i c^2 e^{3it+iJt} g b_1 - 2i c^2 e^{4it+iJt} g b_2 - 2i c^2 e^{5it+iJt} g b_3 - \\ & \quad \left. 2i c^2 e^{6it+iJt} g b_4 - 2i c^2 e^{7it+iJt} g b_5 - 2i c^2 e^{8it+iJt} g b_6 \right) \left. \right) \end{aligned}$$

In[ ]:= **Simplify[%100]**

Out[ ]:= %100

In[ ]:= **Expand[%101]**

Out[ ]:= %101

In[ ]:= **% /. J → 1**

Out[ ]:= %101

In[ ]:= **Collect[%, Exp[I \* t]]**

Out[ ]:= %101

$$\begin{aligned} \text{In}[*]:= \mathbf{m} := & -i e^{i(-6+J)t} b_{-6} - 2 i c^2 e^{2 i t+i(-6+J)t} g s^2 b_{-6} - \\ & i e^{i t+i(-6+J)t} b_{-5} - 2 i c^2 e^{3 i t+i(-6+J)t} g s^2 b_{-5} - i e^{2 i t+i(-6+J)t} b_{-4} - \\ & 2 i c^2 e^{4 i t+i(-6+J)t} g s^2 b_{-4} - i e^{3 i t+i(-6+J)t} b_{-3} - 2 i c^2 e^{5 i t+i(-6+J)t} g s^2 b_{-3} - \\ & i e^{4 i t+i(-6+J)t} b_{-2} - 2 i c^2 e^{6 i t+i(-6+J)t} g s^2 b_{-2} - i e^{5 i t+i(-6+J)t} b_{-1} - \\ & 2 i c^2 e^{7 i t+i(-6+J)t} g s^2 b_{-1} - i e^{6 i t+i(-6+J)t} b_0 - 2 i c^2 e^{8 i t+i(-6+J)t} g s^2 b_0 - \\ & i e^{7 i t+i(-6+J)t} b_1 - 2 i c^2 e^{9 i t+i(-6+J)t} g s^2 b_1 - i e^{8 i t+i(-6+J)t} b_2 - \\ & 2 i c^2 e^{10 i t+i(-6+J)t} g s^2 b_2 - i e^{9 i t+i(-6+J)t} b_3 - 2 i c^2 e^{11 i t+i(-6+J)t} g s^2 b_3 - \\ & i e^{10 i t+i(-6+J)t} b_4 - 2 i c^2 e^{12 i t+i(-6+J)t} g s^2 b_4 - i e^{11 i t+i(-6+J)t} b_5 - \\ & 2 i c^2 e^{13 i t+i(-6+J)t} g s^2 b_5 - i e^{12 i t+i(-6+J)t} b_6 - 2 i c^2 e^{14 i t+i(-6+J)t} g s^2 b_6 \end{aligned}$$

$$\text{In}[*]:= \mathbf{m} /. J \rightarrow 2$$

$$\begin{aligned} \text{Out}[*]= & -i e^{-4 i t} b_{-6} - 2 i c^2 e^{-2 i t} g s^2 b_{-6} - i e^{-3 i t} b_{-5} - 2 i c^2 e^{-i t} g s^2 b_{-5} - i e^{-2 i t} b_{-4} - \\ & 2 i c^2 g s^2 b_{-4} - i e^{-i t} b_{-3} - 2 i c^2 e^{i t} g s^2 b_{-3} - i b_{-2} - 2 i c^2 e^{2 i t} g s^2 b_{-2} - i e^{i t} b_{-1} - \\ & 2 i c^2 e^{3 i t} g s^2 b_{-1} - i e^{2 i t} b_0 - 2 i c^2 e^{4 i t} g s^2 b_0 - i e^{3 i t} b_1 - 2 i c^2 e^{5 i t} g s^2 b_1 - \\ & i e^{4 i t} b_2 - 2 i c^2 e^{6 i t} g s^2 b_2 - i e^{5 i t} b_3 - 2 i c^2 e^{7 i t} g s^2 b_3 - i e^{6 i t} b_4 - \\ & 2 i c^2 e^{8 i t} g s^2 b_4 - i e^{7 i t} b_5 - 2 i c^2 e^{9 i t} g s^2 b_5 - i e^{8 i t} b_6 - 2 i c^2 e^{10 i t} g s^2 b_6 \end{aligned}$$

$$\text{In}[*]:= \text{Collect}[\%, \text{Exp}[I * t]]$$

$$\begin{aligned} \text{Out}[*]= & -i e^{-4 i t} b_{-6} - i e^{-3 i t} b_{-5} + e^{-2 i t} (-2 i c^2 g s^2 b_{-6} - i b_{-4}) - 2 i c^2 g s^2 b_{-4} + \\ & e^{-i t} (-2 i c^2 g s^2 b_{-5} - i b_{-3}) - i b_{-2} + e^{i t} (-2 i c^2 g s^2 b_{-3} - i b_{-1}) + \\ & e^{2 i t} (-2 i c^2 g s^2 b_{-2} - i b_0) + e^{3 i t} (-2 i c^2 g s^2 b_{-1} - i b_1) + e^{4 i t} (-2 i c^2 g s^2 b_0 - i b_2) + \\ & e^{5 i t} (-2 i c^2 g s^2 b_1 - i b_3) + e^{6 i t} (-2 i c^2 g s^2 b_2 - i b_4) + e^{7 i t} (-2 i c^2 g s^2 b_3 - i b_5) - \\ & 2 i c^2 e^{9 i t} g s^2 b_5 + e^{8 i t} (-2 i c^2 g s^2 b_4 - i b_6) - 2 i c^2 e^{10 i t} g s^2 b_6 \end{aligned}$$

$$\text{In}[*]:= \mathbf{m} /. J \rightarrow 3$$

$$\begin{aligned} \text{Out}[*]= & -i e^{-3 i t} b_{-6} - 2 i c^2 e^{-i t} g s^2 b_{-6} - i e^{-2 i t} b_{-5} - 2 i c^2 g s^2 b_{-5} - i e^{-i t} b_{-4} - \\ & 2 i c^2 e^{i t} g s^2 b_{-4} - i b_{-3} - 2 i c^2 e^{2 i t} g s^2 b_{-3} - i e^{i t} b_{-2} - 2 i c^2 e^{3 i t} g s^2 b_{-2} - i e^{2 i t} b_{-1} - \\ & 2 i c^2 e^{4 i t} g s^2 b_{-1} - i e^{3 i t} b_0 - 2 i c^2 e^{5 i t} g s^2 b_0 - i e^{4 i t} b_1 - 2 i c^2 e^{6 i t} g s^2 b_1 - \\ & i e^{5 i t} b_2 - 2 i c^2 e^{7 i t} g s^2 b_2 - i e^{6 i t} b_3 - 2 i c^2 e^{8 i t} g s^2 b_3 - i e^{7 i t} b_4 - \\ & 2 i c^2 e^{9 i t} g s^2 b_4 - i e^{8 i t} b_5 - 2 i c^2 e^{10 i t} g s^2 b_5 - i e^{9 i t} b_6 - 2 i c^2 e^{11 i t} g s^2 b_6 \end{aligned}$$

$$\text{In}[*]:= \text{Collect}[\%, \text{Exp}[I * t]]$$

$$\begin{aligned} \text{Out}[*]= & -i e^{-3 i t} b_{-6} - i e^{-2 i t} b_{-5} - 2 i c^2 g s^2 b_{-5} + e^{-i t} (-2 i c^2 g s^2 b_{-6} - i b_{-4}) - \\ & i b_{-3} + e^{i t} (-2 i c^2 g s^2 b_{-4} - i b_{-2}) + e^{2 i t} (-2 i c^2 g s^2 b_{-3} - i b_{-1}) + \\ & e^{3 i t} (-2 i c^2 g s^2 b_{-2} - i b_0) + e^{4 i t} (-2 i c^2 g s^2 b_{-1} - i b_1) + e^{5 i t} (-2 i c^2 g s^2 b_0 - i b_2) + \\ & e^{6 i t} (-2 i c^2 g s^2 b_1 - i b_3) + e^{7 i t} (-2 i c^2 g s^2 b_2 - i b_4) + e^{8 i t} (-2 i c^2 g s^2 b_3 - i b_5) - \\ & 2 i c^2 e^{10 i t} g s^2 b_5 + e^{9 i t} (-2 i c^2 g s^2 b_4 - i b_6) - 2 i c^2 e^{11 i t} g s^2 b_6 \end{aligned}$$

$$\text{In}[*]:= \mathbf{y2J}$$

$$\text{Out}[*]= 1$$

$$\text{In}[*]:= \rho 3$$

$$\text{Out}[*]= -2 G z_3 Z_2^2 - Z_3$$

$$\text{In}[*]:= \mathbf{q3} := \rho 3 /. \{Z_2 \rightarrow X2, z_3 \rightarrow x3, Z_3 \rightarrow X3\}$$

In[\*]:= **q3**

Out[\*]:=  $-c s + 2 c e^{-2 i t} G s^3 - 2 e^{-2 i t} G s^2 (c s - 2 c e^{2 i t} g s^3)$

In[\*]:= **Simplify** $[-c s + 2 c e^{-2 i t} G s^3 - 2 e^{-2 i t} G s^2 (c s - 2 c e^{2 i t} g s^3)]$

Out[\*]:=  $c s (-1 + 4 g G s^4)$

In[\*]:= **ρ3**

Out[\*]:=  $z_1 + Z_1 - z_2 Z_2 - G z_3^2 Z_2^2 - z_3 Z_3 - g z_2^2 Z_{33}^2$

In[\*]:= **ρ3**

Out[\*]:=  $-2 G z_3 Z_2^2 - Z_3$

In[\*]:= **x2**

Out[\*]:=  $e^{i t} s$

In[\*]:= **X2**

Out[\*]:=  $e^{-i t} s$

In[\*]:= **x3**

Out[\*]:=  $c s - 2 c e^{2 i t} g s^3$

In[\*]:= **X3**

Out[\*]:=  $c s - 2 c e^{-2 i t} G s^3$

In[\*]:= **X3n := k \* s - 2 k e<sup>-2 i t</sup> \* G \* s<sup>3</sup>**

In[\*]:= **q3 := ρ3 /. {Z<sub>2</sub> → X2, z<sub>3</sub> → x3, Z<sub>3</sub> → X3n}**

In[\*]:= **q3**

Out[\*]:=  $-k s + 2 e^{-2 i t} G k s^3 - 2 e^{-2 i t} G s^2 (c s - 2 c e^{2 i t} g s^3)$

In[\*]:= **Simplify** $[-k s + 2 e^{-2 i t} G k s^3 - 2 e^{-2 i t} G s^2 (c s - 2 c e^{2 i t} g s^3)]$

Out[\*]:=  $-k s + 2 e^{-2 i t} G (-c + k) s^3 + 4 c g G s^5$

In[\*]:= **q3t := -k s + 2 e<sup>-2 i t</sup> G (-c + k) s<sup>3</sup>**

In[\*]:= **I3 := (Exp[I \* J \* t] \* y2J \* A \* dz2 \* q3t) / s<sup>2</sup>**

In[\*]:= **I3**

Out[\*]:=  $\frac{1}{s} i e^{i t + i J t} (-k s + 2 e^{-2 i t} G (-c + k) s^3) (e^{-6 i t} b_{-6} + e^{-5 i t} b_{-5} + e^{-4 i t} b_{-4} + e^{-3 i t} b_{-3} + e^{-2 i t} b_{-2} + e^{-i t} b_{-1} + b_0 + e^{i t} b_1 + e^{2 i t} b_2 + e^{3 i t} b_3 + e^{4 i t} b_4 + e^{5 i t} b_5 + e^{6 i t} b_6)$

In[\*]:= **Simplify[%112]**

Out[\*]:=  $-i e^{i (-7 + J) t} (e^{2 i t} k + 2 G (c - k) s^2) (b_{-6} + e^{i t} b_{-5} + e^{2 i t} b_{-4} + e^{3 i t} b_{-3} + e^{4 i t} b_{-2} + e^{5 i t} b_{-1} + e^{6 i t} b_0 + e^{7 i t} b_1 + e^{8 i t} b_2 + e^{9 i t} b_3 + e^{10 i t} b_4 + e^{11 i t} b_5 + e^{12 i t} b_6)$



In[\*]:= Expand[%]

$$\begin{aligned} \text{Out[*]} = & -i e^{2i t+i(-7+J)} t k b_{-6} - 2i c e^{i(-7+J)} t G s^2 b_{-6} + 2i e^{i(-7+J)} t G k s^2 b_{-6} - \\ & i e^{3i t+i(-7+J)} t k b_{-5} - 2i c e^{i t+i(-7+J)} t G s^2 b_{-5} + 2i e^{i t+i(-7+J)} t G k s^2 b_{-5} - \\ & i e^{4i t+i(-7+J)} t k b_{-4} - 2i c e^{2i t+i(-7+J)} t G s^2 b_{-4} + 2i e^{2i t+i(-7+J)} t G k s^2 b_{-4} - \\ & i e^{5i t+i(-7+J)} t k b_{-3} - 2i c e^{3i t+i(-7+J)} t G s^2 b_{-3} + 2i e^{3i t+i(-7+J)} t G k s^2 b_{-3} - \\ & i e^{6i t+i(-7+J)} t k b_{-2} - 2i c e^{4i t+i(-7+J)} t G s^2 b_{-2} + 2i e^{4i t+i(-7+J)} t G k s^2 b_{-2} - \\ & i e^{7i t+i(-7+J)} t k b_{-1} - 2i c e^{5i t+i(-7+J)} t G s^2 b_{-1} + 2i e^{5i t+i(-7+J)} t G k s^2 b_{-1} - \\ & i e^{8i t+i(-7+J)} t k b_0 - 2i c e^{6i t+i(-7+J)} t G s^2 b_0 + 2i e^{6i t+i(-7+J)} t G k s^2 b_0 - \\ & i e^{9i t+i(-7+J)} t k b_1 - 2i c e^{7i t+i(-7+J)} t G s^2 b_1 + 2i e^{7i t+i(-7+J)} t G k s^2 b_1 - \\ & i e^{10i t+i(-7+J)} t k b_2 - 2i c e^{8i t+i(-7+J)} t G s^2 b_2 + 2i e^{8i t+i(-7+J)} t G k s^2 b_2 - \\ & i e^{11i t+i(-7+J)} t k b_3 - 2i c e^{9i t+i(-7+J)} t G s^2 b_3 + 2i e^{9i t+i(-7+J)} t G k s^2 b_3 - \\ & i e^{12i t+i(-7+J)} t k b_4 - 2i c e^{10i t+i(-7+J)} t G s^2 b_4 + 2i e^{10i t+i(-7+J)} t G k s^2 b_4 - \\ & i e^{13i t+i(-7+J)} t k b_5 - 2i c e^{11i t+i(-7+J)} t G s^2 b_5 + 2i e^{11i t+i(-7+J)} t G k s^2 b_5 - \\ & i e^{14i t+i(-7+J)} t k b_6 - 2i c e^{12i t+i(-7+J)} t G s^2 b_6 + 2i e^{12i t+i(-7+J)} t G k s^2 b_6 \end{aligned}$$

In[\*]:= Simplify[%]

$$\begin{aligned} \text{Out[*]} = & -i e^{i(-7+J)} t \left( e^{2i t} k + 2 G (c - k) s^2 \right) \left( b_{-6} + e^{i t} b_{-5} + e^{2i t} b_{-4} + e^{3i t} \right. \\ & \left. (b_{-3} + e^{i t} b_{-2} + e^{2i t} b_{-1} + e^{3i t} b_0 + e^{4i t} b_1 + e^{5i t} b_2 + e^{6i t} b_3 + e^{7i t} b_4 + e^{8i t} b_5 + e^{9i t} b_6) \right) \end{aligned}$$

In[\*]:= Expand[%]

$$\begin{aligned} \text{Out[*]} = & -i e^{2i t+i(-7+J)} t k b_{-6} - 2i c e^{i(-7+J)} t G s^2 b_{-6} + 2i e^{i(-7+J)} t G k s^2 b_{-6} - \\ & i e^{3i t+i(-7+J)} t k b_{-5} - 2i c e^{i t+i(-7+J)} t G s^2 b_{-5} + 2i e^{i t+i(-7+J)} t G k s^2 b_{-5} - \\ & i e^{4i t+i(-7+J)} t k b_{-4} - 2i c e^{2i t+i(-7+J)} t G s^2 b_{-4} + 2i e^{2i t+i(-7+J)} t G k s^2 b_{-4} - \\ & i e^{5i t+i(-7+J)} t k b_{-3} - 2i c e^{3i t+i(-7+J)} t G s^2 b_{-3} + 2i e^{3i t+i(-7+J)} t G k s^2 b_{-3} - \\ & i e^{6i t+i(-7+J)} t k b_{-2} - 2i c e^{4i t+i(-7+J)} t G s^2 b_{-2} + 2i e^{4i t+i(-7+J)} t G k s^2 b_{-2} - \\ & i e^{7i t+i(-7+J)} t k b_{-1} - 2i c e^{5i t+i(-7+J)} t G s^2 b_{-1} + 2i e^{5i t+i(-7+J)} t G k s^2 b_{-1} - \\ & i e^{8i t+i(-7+J)} t k b_0 - 2i c e^{6i t+i(-7+J)} t G s^2 b_0 + 2i e^{6i t+i(-7+J)} t G k s^2 b_0 - \\ & i e^{9i t+i(-7+J)} t k b_1 - 2i c e^{7i t+i(-7+J)} t G s^2 b_1 + 2i e^{7i t+i(-7+J)} t G k s^2 b_1 - \\ & i e^{10i t+i(-7+J)} t k b_2 - 2i c e^{8i t+i(-7+J)} t G s^2 b_2 + 2i e^{8i t+i(-7+J)} t G k s^2 b_2 - \\ & i e^{11i t+i(-7+J)} t k b_3 - 2i c e^{9i t+i(-7+J)} t G s^2 b_3 + 2i e^{9i t+i(-7+J)} t G k s^2 b_3 - \\ & i e^{12i t+i(-7+J)} t k b_4 - 2i c e^{10i t+i(-7+J)} t G s^2 b_4 + 2i e^{10i t+i(-7+J)} t G k s^2 b_4 - \\ & i e^{13i t+i(-7+J)} t k b_5 - 2i c e^{11i t+i(-7+J)} t G s^2 b_5 + 2i e^{11i t+i(-7+J)} t G k s^2 b_5 - \\ & i e^{14i t+i(-7+J)} t k b_6 - 2i c e^{12i t+i(-7+J)} t G s^2 b_6 + 2i e^{12i t+i(-7+J)} t G k s^2 b_6 \end{aligned}$$

In[\*]:= % /. J -> 1

$$\begin{aligned} \text{Out[*]} = & -i e^{-4i t} k b_{-6} - 2i c e^{-6i t} G s^2 b_{-6} + 2i e^{-6i t} G k s^2 b_{-6} - i e^{-3i t} k b_{-5} - 2i c e^{-5i t} G s^2 b_{-5} + \\ & 2i e^{-5i t} G k s^2 b_{-5} - i e^{-2i t} k b_{-4} - 2i c e^{-4i t} G s^2 b_{-4} + 2i e^{-4i t} G k s^2 b_{-4} - \\ & i e^{-i t} k b_{-3} - 2i c e^{-3i t} G s^2 b_{-3} + 2i e^{-3i t} G k s^2 b_{-3} - i k b_{-2} - 2i c e^{-2i t} G s^2 b_{-2} + \\ & 2i e^{-2i t} G k s^2 b_{-2} - i e^{i t} k b_{-1} - 2i c e^{-i t} G s^2 b_{-1} + 2i e^{-i t} G k s^2 b_{-1} - i e^{2i t} k b_0 - \\ & 2i c G s^2 b_0 + 2i G k s^2 b_0 - i e^{3i t} k b_1 - 2i c e^{i t} G s^2 b_1 + 2i e^{i t} G k s^2 b_1 - \\ & i e^{4i t} k b_2 - 2i c e^{2i t} G s^2 b_2 + 2i e^{2i t} G k s^2 b_2 - i e^{5i t} k b_3 - 2i c e^{3i t} G s^2 b_3 + \\ & 2i e^{3i t} G k s^2 b_3 - i e^{6i t} k b_4 - 2i c e^{4i t} G s^2 b_4 + 2i e^{4i t} G k s^2 b_4 - i e^{7i t} k b_5 - \\ & 2i c e^{5i t} G s^2 b_5 + 2i e^{5i t} G k s^2 b_5 - i e^{8i t} k b_6 - 2i c e^{6i t} G s^2 b_6 + 2i e^{6i t} G k s^2 b_6 \end{aligned}$$

In[ ]:= **Collect**[% , Exp[I \* t]]

$$\begin{aligned} \text{Out[ ]}= & e^{-6 i t} \left( -2 i c G s^2 b_{-6} + 2 i G k s^2 b_{-6} \right) + e^{-5 i t} \left( -2 i c G s^2 b_{-5} + 2 i G k s^2 b_{-5} \right) + \\ & e^{-4 i t} \left( -i k b_{-6} - 2 i c G s^2 b_{-4} + 2 i G k s^2 b_{-4} \right) + e^{-3 i t} \left( -i k b_{-5} - 2 i c G s^2 b_{-3} + 2 i G k s^2 b_{-3} \right) - \\ & i k b_{-2} + e^{-2 i t} \left( -i k b_{-4} - 2 i c G s^2 b_{-2} + 2 i G k s^2 b_{-2} \right) + \\ & e^{-i t} \left( -i k b_{-3} - 2 i c G s^2 b_{-1} + 2 i G k s^2 b_{-1} \right) - 2 i c G s^2 b_0 + 2 i G k s^2 b_0 + \\ & e^{i t} \left( -i k b_{-1} - 2 i c G s^2 b_1 + 2 i G k s^2 b_1 \right) + e^{2 i t} \left( -i k b_0 - 2 i c G s^2 b_2 + 2 i G k s^2 b_2 \right) + \\ & e^{3 i t} \left( -i k b_1 - 2 i c G s^2 b_3 + 2 i G k s^2 b_3 \right) + e^{4 i t} \left( -i k b_2 - 2 i c G s^2 b_4 + 2 i G k s^2 b_4 \right) - \\ & i e^{7 i t} k b_5 + e^{5 i t} \left( -i k b_3 - 2 i c G s^2 b_5 + 2 i G k s^2 b_5 \right) - \\ & i e^{8 i t} k b_6 + e^{6 i t} \left( -i k b_4 - 2 i c G s^2 b_6 + 2 i G k s^2 b_6 \right) \end{aligned}$$

In[ ]:= % / s ^ 2

$$\begin{aligned} \text{Out[ ]}= & \frac{1}{s^2} \left( e^{-6 i t} \left( -2 i c G s^2 b_{-6} + 2 i G k s^2 b_{-6} \right) + e^{-5 i t} \left( -2 i c G s^2 b_{-5} + 2 i G k s^2 b_{-5} \right) + \right. \\ & e^{-4 i t} \left( -i k b_{-6} - 2 i c G s^2 b_{-4} + 2 i G k s^2 b_{-4} \right) + e^{-3 i t} \left( -i k b_{-5} - 2 i c G s^2 b_{-3} + 2 i G k s^2 b_{-3} \right) - \\ & i k b_{-2} + e^{-2 i t} \left( -i k b_{-4} - 2 i c G s^2 b_{-2} + 2 i G k s^2 b_{-2} \right) + \\ & e^{-i t} \left( -i k b_{-3} - 2 i c G s^2 b_{-1} + 2 i G k s^2 b_{-1} \right) - 2 i c G s^2 b_0 + 2 i G k s^2 b_0 + \\ & e^{i t} \left( -i k b_{-1} - 2 i c G s^2 b_1 + 2 i G k s^2 b_1 \right) + e^{2 i t} \left( -i k b_0 - 2 i c G s^2 b_2 + 2 i G k s^2 b_2 \right) + \\ & e^{3 i t} \left( -i k b_1 - 2 i c G s^2 b_3 + 2 i G k s^2 b_3 \right) + e^{4 i t} \left( -i k b_2 - 2 i c G s^2 b_4 + 2 i G k s^2 b_4 \right) - \\ & i e^{7 i t} k b_5 + e^{5 i t} \left( -i k b_3 - 2 i c G s^2 b_5 + 2 i G k s^2 b_5 \right) - \\ & \left. i e^{8 i t} k b_6 + e^{6 i t} \left( -i k b_4 - 2 i c G s^2 b_6 + 2 i G k s^2 b_6 \right) \right) \end{aligned}$$

In[ ]:= **Simplify**[%]

$$\begin{aligned} \text{Out[ ]}= & -\frac{1}{s^2} i e^{-6 i t} \left( e^{2 i t} k + 2 G (c - k) s^2 \right) \left( b_{-6} + e^{i t} b_{-5} + e^{2 i t} b_{-4} + e^{3 i t} \right. \\ & \left. \left( b_{-3} + e^{i t} b_{-2} + e^{2 i t} b_{-1} + e^{3 i t} b_0 + e^{4 i t} b_1 + e^{5 i t} b_2 + e^{6 i t} b_3 + e^{7 i t} b_4 + e^{8 i t} b_5 + e^{9 i t} b_6 \right) \right) \end{aligned}$$

In[ ]:= **Ahmad** := %139

In[ ]:= **Ahmad**

Out[ ]:= %139

In[ ]:= **Ahmad** /. J → 1

Out[ ]:= %139

In[ ]:= **Collect**[% , Exp[I \* t]]

Out[ ]:= %139