

$$\ln[*]:= \mathbf{z2st} := \mathbf{s} * \mathbf{z21} + \mathbf{s}^3 * \mathbf{z23}$$

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$$\text{Out[*]}= \mathbf{s} \mathbf{z21} + \mathbf{s}^3 \mathbf{z23}$$

$$\ln[*]:= \mathbf{p2st} := \mathbf{s} * \mathbf{p21} + \mathbf{s}^3 * \mathbf{p23}$$

$$\ln[*]:= \mathbf{z3st} := \mathbf{s} * \mathbf{z31} + \mathbf{s}^3 * \mathbf{z33}$$

$$\ln[*]:= \mathbf{p3st} := \mathbf{s} * \mathbf{p31} + \mathbf{s}^3 * \mathbf{p33}$$

$$\ln[*]:= \mathbf{dz2} := -\frac{\mathbf{p2}}{2} - \frac{\mathbf{i} \mathbf{p1} \mathbf{z2}}{2} + 2 \mathbf{G} \mathbf{p3} \mathbf{Z2} \mathbf{z3} + \mathbf{i} \mathbf{G} \mathbf{p1} \mathbf{Z2} \mathbf{z3}^2$$

$$\ln[*]:= \mathbf{dz2}$$

$$\text{Out[*]}= -\frac{\mathbf{p2}}{2} - \frac{\mathbf{i} \mathbf{p1} \mathbf{z2}}{2} + 2 \mathbf{G} \mathbf{p3} \mathbf{Z2} \mathbf{z3} + \mathbf{i} \mathbf{G} \mathbf{p1} \mathbf{Z2} \mathbf{z3}^2$$

$$\ln[*]:= \mathbf{dp2} := -\frac{1}{2} \mathbf{i} \mathbf{p1} \mathbf{p2} + \frac{\mathbf{p1}^2 \mathbf{z2}}{2} - 2 \mathbf{G} \mathbf{P2} \mathbf{p3} \mathbf{z3} + 2 \mathbf{i} \mathbf{G} \mathbf{p1} \mathbf{p3} \mathbf{Z2} \mathbf{z3} - \mathbf{i} \mathbf{G} \mathbf{p1} \mathbf{P2} \mathbf{z3}^2$$

$$\ln[*]:= \mathbf{dp2}$$

$$\text{Out[*]}= -\frac{1}{2} \mathbf{i} \mathbf{p1} \mathbf{p2} + \frac{\mathbf{p1}^2 \mathbf{z2}}{2} - 2 \mathbf{G} \mathbf{P2} \mathbf{p3} \mathbf{z3} + 2 \mathbf{i} \mathbf{G} \mathbf{p1} \mathbf{p3} \mathbf{Z2} \mathbf{z3} - \mathbf{i} \mathbf{G} \mathbf{p1} \mathbf{P2} \mathbf{z3}^2$$

$$\ln[*]:= \mathbf{dz3} := -\frac{\mathbf{p3}}{2} - \frac{\mathbf{i} \mathbf{p1} \mathbf{z3}}{2} + 2 \mathbf{g} \mathbf{p2} \mathbf{z2} \mathbf{Z3} + \mathbf{i} \mathbf{g} \mathbf{p1} \mathbf{z2}^2 \mathbf{Z3}$$

$$\ln[*]:= \mathbf{dz3}$$

$$\text{Out[*]}= -\frac{\mathbf{p3}}{2} - \frac{\mathbf{i} \mathbf{p1} \mathbf{z3}}{2} + 2 \mathbf{g} \mathbf{p2} \mathbf{z2} \mathbf{Z3} + \mathbf{i} \mathbf{g} \mathbf{p1} \mathbf{z2}^2 \mathbf{Z3}$$

$$\ln[*]:= \mathbf{dp3} := -\frac{1}{2} \mathbf{i} \mathbf{p1} \mathbf{p3} - 2 \mathbf{g} \mathbf{p2} \mathbf{P3} \mathbf{z2} - \mathbf{i} \mathbf{g} \mathbf{p1} \mathbf{P3} \mathbf{z2}^2 + \frac{\mathbf{p1}^2 \mathbf{z3}}{2} + 2 \mathbf{i} \mathbf{g} \mathbf{p1} \mathbf{p2} \mathbf{z2} \mathbf{Z3}$$

$$\ln[*]:= \mathbf{dp3}$$

$$\text{Out[*]}= -\frac{1}{2} \mathbf{i} \mathbf{p1} \mathbf{p3} - 2 \mathbf{g} \mathbf{p2} \mathbf{P3} \mathbf{z2} - \mathbf{i} \mathbf{g} \mathbf{p1} \mathbf{P3} \mathbf{z2}^2 + \frac{\mathbf{p1}^2 \mathbf{z3}}{2} + 2 \mathbf{i} \mathbf{g} \mathbf{p1} \mathbf{p2} \mathbf{z2} \mathbf{Z3}$$

$$\ln[*]:= \mathbf{Z2st} := \mathbf{s} * \mathbf{Z21} + \mathbf{s}^3 * \mathbf{Z23}$$

$$\ln[*]:= \mathbf{Z3st} := \mathbf{s} * \mathbf{Z31} + \mathbf{s}^3 * \mathbf{Z33}$$

$$\ln[*]:= \mathbf{P2st} := \mathbf{s} * \mathbf{P21} + \mathbf{s}^3 * \mathbf{P23}$$

$$\ln[*]:= \mathbf{P3st} := \mathbf{s} * \mathbf{P31} + \mathbf{s}^3 * \mathbf{P33}$$

$$\ln[*]:= \mathbf{dz2} /. \{\mathbf{z2} \rightarrow \mathbf{z2st}, \mathbf{z3} \rightarrow \mathbf{z3st}, \mathbf{Z2} \rightarrow \mathbf{Z2st}, \mathbf{Z3} \rightarrow \mathbf{Z3st}, \mathbf{p2} \rightarrow \mathbf{p2st}, \mathbf{p3} \rightarrow \mathbf{p3st}, \mathbf{P2} \rightarrow \mathbf{P2st}, \mathbf{P3} \rightarrow \mathbf{P3st}\}$$

$$\text{Out[*]}= \frac{1}{2} \left(-\mathbf{p21} \mathbf{s} - \mathbf{p23} \mathbf{s}^3 \right) - \frac{1}{2} \mathbf{i} \mathbf{p1} \left(\mathbf{s} \mathbf{z21} + \mathbf{s}^3 \mathbf{z23} \right) + 2 \mathbf{G} \left(\mathbf{p31} \mathbf{s} + \mathbf{p33} \mathbf{s}^3 \right) \left(\mathbf{s} \mathbf{Z21} + \mathbf{s}^3 \mathbf{Z23} \right) \left(\mathbf{s} \mathbf{z31} + \mathbf{s}^3 \mathbf{z33} \right) + \mathbf{i} \mathbf{G} \mathbf{p1} \left(\mathbf{s} \mathbf{Z21} + \mathbf{s}^3 \mathbf{Z23} \right) \left(\mathbf{s} \mathbf{z31} + \mathbf{s}^3 \mathbf{z33} \right)^2$$

$$\text{In[]:= Expand}\left[\frac{1}{2}(-p_{21}s - p_{23}s^3) - \frac{1}{2}i p_1 (s z_{21} + s^3 z_{23}) + \right. \\ \left. 2 G (p_{31}s + p_{33}s^3) (s Z_{21} + s^3 Z_{23}) (s z_{31} + s^3 z_{33}) + i G p_1 (s Z_{21} + s^3 Z_{23}) (s z_{31} + s^3 z_{33})^2\right]$$

$$\text{Out[]:= } -\frac{p_{21}s}{2} - \frac{p_{23}s^3}{2} - \frac{1}{2}i p_1 s z_{21} - \frac{1}{2}i p_1 s^3 z_{23} + 2 G p_{31} s^3 Z_{21} z_{31} + 2 G p_{33} s^5 Z_{21} z_{31} + \\ 2 G p_{31} s^5 Z_{23} z_{31} + 2 G p_{33} s^7 Z_{23} z_{31} + i G p_1 s^3 Z_{21} z_{31}^2 + i G p_1 s^5 Z_{23} z_{31}^2 + \\ 2 G p_{31} s^5 Z_{21} z_{33} + 2 G p_{33} s^7 Z_{21} z_{33} + 2 G p_{31} s^7 Z_{23} z_{33} + 2 G p_{33} s^9 Z_{23} z_{33} + \\ 2 i G p_1 s^5 Z_{21} z_{31} z_{33} + 2 i G p_1 s^7 Z_{23} z_{31} z_{33} + i G p_1 s^7 Z_{21} z_{33}^2 + i G p_1 s^9 Z_{23} z_{33}^2$$

$$\text{In[]:= Collect[%, s]}$$

$$\text{Out[]:= } s \left(-\frac{p_{21}}{2} - \frac{i p_1 z_{21}}{2} \right) + s^3 \left(-\frac{p_{23}}{2} - \frac{i p_1 z_{23}}{2} + 2 G p_{31} Z_{21} z_{31} + i G p_1 Z_{21} z_{31}^2 \right) + \\ s^5 \left(2 G p_{33} Z_{21} z_{31} + 2 G p_{31} Z_{23} z_{31} + i G p_1 Z_{23} z_{31}^2 + 2 G p_{31} Z_{21} z_{33} + 2 i G p_1 Z_{21} z_{31} z_{33} \right) + \\ s^7 \left(2 G p_{33} Z_{23} z_{31} + 2 G p_{33} Z_{21} z_{33} + 2 G p_{31} Z_{23} z_{33} + 2 i G p_1 Z_{23} z_{31} z_{33} + i G p_1 Z_{21} z_{33}^2 \right) + \\ s^9 \left(2 G p_{33} Z_{23} z_{33} + i G p_1 Z_{23} z_{33}^2 \right)$$

$$\text{In[]:= dp2 /. \{z2 \to z2st, z3 \to z3st, Z2 \to Z2st, \\ Z3 \to Z3st, p2 \to p2st, p3 \to p3st, P2 \to P2st, P3 \to P3st\}}$$

$$\text{Out[]:= } -\frac{1}{2}i p_1 (p_{21}s + p_{23}s^3) + \frac{1}{2}p_1^2 (s z_{21} + s^3 z_{23}) - \\ 2 G (P_{21}s + P_{23}s^3) (p_{31}s + p_{33}s^3) (s z_{31} + s^3 z_{33}) + \\ 2 i G p_1 (p_{31}s + p_{33}s^3) (s Z_{21} + s^3 Z_{23}) (s z_{31} + s^3 z_{33}) - \\ i G p_1 (P_{21}s + P_{23}s^3) (s z_{31} + s^3 z_{33})^2$$

$$\text{In[]:= Expand}\left[-\frac{1}{2}i p_1 (p_{21}s + p_{23}s^3) + \frac{1}{2}p_1^2 (s z_{21} + s^3 z_{23}) - \right.$$

$$\left. 2 G (P_{21}s + P_{23}s^3) (p_{31}s + p_{33}s^3) (s z_{31} + s^3 z_{33}) + 2 i G p_1 (p_{31}s + p_{33}s^3) \right. \\ \left. (s Z_{21} + s^3 Z_{23}) (s z_{31} + s^3 z_{33}) - i G p_1 (P_{21}s + P_{23}s^3) (s z_{31} + s^3 z_{33})^2\right]$$

$$\text{Out[]:= } -\frac{1}{2}i p_1 p_{21} s - \frac{1}{2}i p_1 p_{23} s^3 + \frac{1}{2}p_1^2 s z_{21} + \frac{1}{2}p_1^2 s^3 z_{23} - \\ 2 G P_{21} p_{31} s^3 z_{31} - 2 G P_{23} p_{31} s^5 z_{31} - 2 G P_{21} p_{33} s^5 z_{31} - 2 G P_{23} p_{33} s^7 z_{31} + \\ 2 i G p_1 p_{31} s^3 Z_{21} z_{31} + 2 i G p_1 p_{33} s^5 Z_{21} z_{31} + 2 i G p_1 p_{31} s^5 Z_{23} z_{31} + \\ 2 i G p_1 p_{33} s^7 Z_{23} z_{31} - i G p_1 P_{21} s^3 z_{31}^2 - i G p_1 P_{23} s^5 z_{31}^2 - 2 G P_{21} p_{31} s^5 z_{33} - \\ 2 G P_{23} p_{31} s^7 z_{33} - 2 G P_{21} p_{33} s^7 z_{33} - 2 G P_{23} p_{33} s^9 z_{33} + 2 i G p_1 p_{31} s^5 Z_{21} z_{33} + \\ 2 i G p_1 p_{33} s^7 Z_{21} z_{33} + 2 i G p_1 p_{31} s^7 Z_{23} z_{33} + 2 i G p_1 p_{33} s^9 Z_{23} z_{33} - \\ 2 i G p_1 P_{21} s^5 z_{31} z_{33} - 2 i G p_1 P_{23} s^7 z_{31} z_{33} - i G p_1 P_{21} s^7 z_{33}^2 - i G p_1 P_{23} s^9 z_{33}^2$$

In[*]:= Collect[%, s]

$$\begin{aligned} \text{Out[*]} = & s \left(-\frac{1}{2} i p_1 p_{21} + \frac{p_1^2 z_{21}}{2} \right) + \\ & s^3 \left(-\frac{1}{2} i p_1 p_{23} + \frac{p_1^2 z_{23}}{2} - 2 G P_{21} p_{31} z_{31} + 2 i G p_1 p_{31} Z_{21} z_{31} - i G p_1 P_{21} z_{31}^2 \right) + \\ & s^5 \left(-2 G P_{23} p_{31} z_{31} - 2 G P_{21} p_{33} z_{31} + 2 i G p_1 p_{33} Z_{21} z_{31} + 2 i G p_1 p_{31} Z_{23} z_{31} - \right. \\ & \quad \left. i G p_1 P_{23} z_{31}^2 - 2 G P_{21} p_{31} z_{33} + 2 i G p_1 p_{31} Z_{21} z_{33} - 2 i G p_1 P_{21} z_{31} z_{33} \right) + \\ & s^7 \left(-2 G P_{23} p_{33} z_{31} + 2 i G p_1 p_{33} Z_{23} z_{31} - 2 G P_{23} p_{31} z_{33} - 2 G P_{21} p_{33} z_{33} + \right. \\ & \quad \left. 2 i G p_1 p_{33} Z_{21} z_{33} + 2 i G p_1 p_{31} Z_{23} z_{33} - 2 i G p_1 P_{23} z_{31} z_{33} - i G p_1 P_{21} z_{33}^2 \right) + \\ & s^9 \left(-2 G P_{23} p_{33} z_{33} + 2 i G p_1 p_{33} Z_{23} z_{33} - i G p_1 P_{23} z_{33}^2 \right) \end{aligned}$$

In[*]:= DSolve[{l'[t] == -\frac{m[t]}{2} - \frac{i p_1 * l[t]}{2},

$$m'[t] == -\frac{1}{2} i p_1 * m[t] + \frac{p_1^2 * l[t]}{2}], \{l[t], m[t]\}, t]$$

$$\begin{aligned} \text{Out[*]} = & \left\{ \left\{ l[t] \rightarrow \frac{1}{2} e^{-i p_1 t} (1 + e^{i p_1 t}) C[1] + \frac{i e^{-i p_1 t} (-1 + e^{i p_1 t}) C[2]}{2 p_1}, \right. \right. \\ & \left. \left. m[t] \rightarrow -\frac{1}{2} i e^{-i p_1 t} (-1 + e^{i p_1 t}) p_1 C[1] + \frac{1}{2} e^{-i p_1 t} (1 + e^{i p_1 t}) C[2] \right\} \right\} \end{aligned}$$

$$\text{In[*]} := \frac{1}{2} e^{-i p_1 t} (1 + e^{i p_1 t}) C[1] + \frac{i e^{-i p_1 t} (-1 + e^{i p_1 t}) C[2]}{2 p_1}$$

$$\text{Out[*]} = \frac{1}{2} e^{-i p_1 t} (1 + e^{i p_1 t}) C[1] + \frac{i e^{-i p_1 t} (-1 + e^{i p_1 t}) C[2]}{2 p_1}$$

$$\text{In[*]} := \text{Expand} \left[\frac{1}{2} e^{-i p_1 t} (1 + e^{i p_1 t}) C[1] + \frac{i e^{-i p_1 t} (-1 + e^{i p_1 t}) C[2]}{2 p_1} \right]$$

$$\text{Out[*]} = \frac{C[1]}{2} + \frac{1}{2} e^{-i p_1 t} C[1] + \frac{i C[2]}{2 p_1} - \frac{i e^{-i p_1 t} C[2]}{2 p_1}$$

In[*]:= dz3 /. {z2 -> z2st, z3 -> z3st, Z2 -> Z2st,
Z3 -> Z3st, p2 -> p2st, p3 -> p3st, P2 -> P2st, P3 -> P3st}

$$\begin{aligned} \text{Out[*]} = & \frac{1}{2} (-p_{31} s - p_{33} s^3) - \frac{1}{2} i p_1 (s z_{31} + s^3 z_{33}) + \\ & 2 g (p_{21} s + p_{23} s^3) (s z_{21} + s^3 z_{23}) (s Z_{31} + s^3 Z_{33}) + i g p_1 (s z_{21} + s^3 z_{23})^2 (s Z_{31} + s^3 Z_{33}) \end{aligned}$$

$$\begin{aligned} \text{In[*]} := & \text{Expand} \left[\frac{1}{2} (-p_{31} s - p_{33} s^3) - \frac{1}{2} i p_1 (s z_{31} + s^3 z_{33}) + \right. \\ & \left. 2 g (p_{21} s + p_{23} s^3) (s z_{21} + s^3 z_{23}) (s Z_{31} + s^3 Z_{33}) + i g p_1 (s z_{21} + s^3 z_{23})^2 (s Z_{31} + s^3 Z_{33}) \right] \end{aligned}$$

$$\begin{aligned} \text{Out[*]} = & -\frac{p_{31} s}{2} - \frac{p_{33} s^3}{2} - \frac{1}{2} i p_1 s z_{31} + 2 g p_{21} s^3 z_{21} Z_{31} + 2 g p_{23} s^5 z_{21} Z_{31} + i g p_1 s^3 z_{21}^2 Z_{31} + \\ & 2 g p_{21} s^5 z_{23} Z_{31} + 2 g p_{23} s^7 z_{23} Z_{31} + 2 i g p_1 s^5 z_{21} z_{23} Z_{31} + i g p_1 s^7 z_{23}^2 Z_{31} - \\ & \frac{1}{2} i p_1 s^3 z_{33} + 2 g p_{21} s^5 z_{21} Z_{33} + 2 g p_{23} s^7 z_{21} Z_{33} + i g p_1 s^5 z_{21}^2 Z_{33} + \\ & 2 g p_{21} s^7 z_{23} Z_{33} + 2 g p_{23} s^9 z_{23} Z_{33} + 2 i g p_1 s^7 z_{21} z_{23} Z_{33} + i g p_1 s^9 z_{23}^2 Z_{33} \end{aligned}$$

In[]:= **Collect**[% , s]

$$\text{Out[]}= s \left(-\frac{p_{31}}{2} - \frac{i p_1 z_{31}}{2} \right) + s^3 \left(-\frac{p_{33}}{2} + 2 g p_{21} z_{21} Z_{31} + i g p_1 z_{21}^2 Z_{31} - \frac{i p_1 z_{33}}{2} \right) +$$

$$s^5 \left(2 g p_{23} z_{21} Z_{31} + 2 g p_{21} z_{23} Z_{31} + 2 i g p_1 z_{21} z_{23} Z_{31} + 2 g p_{21} z_{21} Z_{33} + i g p_1 z_{21}^2 Z_{33} \right) +$$

$$s^7 \left(2 g p_{23} z_{23} Z_{31} + i g p_1 z_{23}^2 Z_{31} + 2 g p_{23} z_{21} Z_{33} + 2 g p_{21} z_{23} Z_{33} + 2 i g p_1 z_{21} z_{23} Z_{33} \right) +$$

$$s^9 \left(2 g p_{23} z_{23} Z_{33} + i g p_1 z_{23}^2 Z_{33} \right)$$

In[]:= **dp3 /. {z2 → z2st, z3 → z3st, Z2 → Z2st,**
Z3 → Z3st, p2 → p2st, p3 → p3st, P2 → P2st, P3 → P3st}

$$\text{Out[]}= -\frac{1}{2} i p_1 \left(p_{31} s + p_{33} s^3 \right) - 2 g \left(p_{21} s + p_{23} s^3 \right) \left(P_{31} s + P_{33} s^3 \right) \left(s z_{21} + s^3 z_{23} \right) -$$

$$i g p_1 \left(P_{31} s + P_{33} s^3 \right) \left(s z_{21} + s^3 z_{23} \right)^2 + \frac{1}{2} p_1^2 \left(s z_{31} + s^3 z_{33} \right) +$$

$$2 i g p_1 \left(p_{21} s + p_{23} s^3 \right) \left(s z_{21} + s^3 z_{23} \right) \left(s Z_{31} + s^3 Z_{33} \right)$$

In[]:= **Expand** $\left[-\frac{1}{2} i p_1 \left(p_{31} s + p_{33} s^3 \right) - 2 g \left(p_{21} s + p_{23} s^3 \right) \left(P_{31} s + P_{33} s^3 \right) \left(s z_{21} + s^3 z_{23} \right) - \right.$
 $\left. i g p_1 \left(P_{31} s + P_{33} s^3 \right) \left(s z_{21} + s^3 z_{23} \right)^2 + \frac{1}{2} p_1^2 \left(s z_{31} + s^3 z_{33} \right) + \right.$
 $\left. 2 i g p_1 \left(p_{21} s + p_{23} s^3 \right) \left(s z_{21} + s^3 z_{23} \right) \left(s Z_{31} + s^3 Z_{33} \right) \right]$

$$\text{Out[]}= -\frac{1}{2} i p_1 p_{31} s - \frac{1}{2} i p_1 p_{33} s^3 - 2 g p_{21} P_{31} s^3 z_{21} - 2 g p_{23} P_{31} s^5 z_{21} -$$

$$2 g p_{21} P_{33} s^5 z_{21} - 2 g p_{23} P_{33} s^7 z_{21} - i g p_1 P_{31} s^3 z_{21}^2 - i g p_1 P_{33} s^5 z_{21}^2 -$$

$$2 g p_{21} P_{31} s^5 z_{23} - 2 g p_{23} P_{31} s^7 z_{23} - 2 g p_{21} P_{33} s^7 z_{23} - 2 g p_{23} P_{33} s^9 z_{23} -$$

$$2 i g p_1 P_{31} s^5 z_{21} z_{23} - 2 i g p_1 P_{33} s^7 z_{21} z_{23} - i g p_1 P_{31} s^7 z_{23}^2 -$$

$$i g p_1 P_{33} s^9 z_{23}^2 + \frac{1}{2} p_1^2 s z_{31} + 2 i g p_1 p_{21} s^3 z_{21} Z_{31} + 2 i g p_1 p_{23} s^5 z_{21} Z_{31} +$$

$$2 i g p_1 p_{21} s^5 z_{23} Z_{31} + 2 i g p_1 p_{23} s^7 z_{23} Z_{31} + \frac{1}{2} p_1^2 s^3 z_{33} + 2 i g p_1 p_{21} s^5 z_{21} Z_{33} +$$

$$2 i g p_1 p_{23} s^7 z_{21} Z_{33} + 2 i g p_1 p_{21} s^7 z_{23} Z_{33} + 2 i g p_1 p_{23} s^9 z_{23} Z_{33}$$

In[]:= **Collect**[% , s]

$$\text{Out[]}= s \left(-\frac{1}{2} i p_1 p_{31} + \frac{p_1^2 z_{31}}{2} \right) +$$

$$s^3 \left(-\frac{1}{2} i p_1 p_{33} - 2 g p_{21} P_{31} z_{21} - i g p_1 P_{31} z_{21}^2 + 2 i g p_1 p_{21} z_{21} Z_{31} + \frac{p_1^2 z_{33}}{2} \right) +$$

$$s^5 \left(-2 g p_{23} P_{31} z_{21} - 2 g p_{21} P_{33} z_{21} - i g p_1 P_{33} z_{21}^2 - 2 g p_{21} P_{31} z_{23} - \right.$$

$$\left. 2 i g p_1 P_{31} z_{21} z_{23} + 2 i g p_1 p_{23} z_{21} Z_{31} + 2 i g p_1 p_{21} z_{23} Z_{31} + 2 i g p_1 p_{21} z_{21} Z_{33} \right) +$$

$$s^7 \left(-2 g p_{23} P_{33} z_{21} - 2 g p_{23} P_{31} z_{23} - 2 g p_{21} P_{33} z_{23} - 2 i g p_1 P_{33} z_{21} z_{23} - \right.$$

$$\left. i g p_1 P_{31} z_{23}^2 + 2 i g p_1 p_{23} z_{23} Z_{31} + 2 i g p_1 p_{23} z_{21} Z_{33} + 2 i g p_1 p_{21} z_{23} Z_{33} \right) +$$

$$s^9 \left(-2 g p_{23} P_{33} z_{23} - i g p_1 P_{33} z_{23}^2 + 2 i g p_1 p_{23} z_{23} Z_{33} \right)$$

$$\text{In}[*]:= \text{DSolve}\left[\left\{\ell'[t] == -\frac{m[t]}{2} - \frac{i p1 * \ell[t]}{2},\right.\right.$$

$$\left. m'[t] == -\frac{1}{2} i p1 * m[t] + \frac{p1^2 * \ell[t]}{2}\right\}, \{\ell[t], m[t]\}, t]$$

$$\text{Out}[*]:= \left\{\left\{\ell[t] \rightarrow \frac{1}{2} e^{-i p1 t} (1 + e^{i p1 t}) C[1] + \frac{i e^{-i p1 t} (-1 + e^{i p1 t}) C[2]}{2 p1},\right.\right.$$

$$\left. m[t] \rightarrow -\frac{1}{2} i e^{-i p1 t} (-1 + e^{i p1 t}) p1 C[1] + \frac{1}{2} e^{-i p1 t} (1 + e^{i p1 t}) C[2]\right\}$$

$$\text{In}[*]:= -\frac{1}{2} i e^{-i p1 t} (-1 + e^{i p1 t}) p1 C[1] + \frac{1}{2} e^{-i p1 t} (1 + e^{i p1 t}) C[2]$$

$$\text{Out}[*]:= -\frac{1}{2} i e^{-i p1 t} (-1 + e^{i p1 t}) p1 C[1] + \frac{1}{2} e^{-i p1 t} (1 + e^{i p1 t}) C[2]$$

$$\text{In}[*]:= -\frac{1}{2} i e^{-i p1 t} (-1 + e^{i p1 t}) p1 C[1] + \frac{1}{2} e^{-i p1 t} (1 + e^{i p1 t}) C[2]$$

$$\text{Out}[*]:= -\frac{1}{2} i e^{-i p1 t} (-1 + e^{i p1 t}) p1 C[1] + \frac{1}{2} e^{-i p1 t} (1 + e^{i p1 t}) C[2]$$

$$\text{In}[*]:= p1 := -1$$

$$\text{In}[*]:= z21$$

$$\text{Out}[*]:= z21$$

$$\text{In}[*]:= z21 := \frac{1}{2} e^{-i p1 t} (1 + e^{i p1 t}) * c1 + \frac{i e^{-i p1 t} (-1 + e^{i p1 t}) * c2}{2 p1}$$

$$\text{In}[*]:= z21$$

$$\text{Out}[*]:= -\frac{1}{2} i c2 e^{i t} (-1 + e^{-i t}) + \frac{1}{2} c1 e^{i t} (1 + e^{-i t})$$

$$\text{In}[*]:= Z21 := \frac{1}{2} i * C2 * e^{-i t} (-1 + e^{i t}) + \frac{1}{2} C1 * e^{-i t} (1 + e^{i t})$$

$$\text{In}[*]:= p21 := -\frac{1}{2} i e^{-i p1 t} (-1 + e^{i p1 t}) * p1 * c1 + \frac{1}{2} e^{-i p1 t} (1 + e^{i p1 t}) * c2$$

$$\text{In}[*]:= p21$$

$$\text{Out}[*]:= \frac{1}{2} i c1 e^{i t} (-1 + e^{-i t}) + \frac{1}{2} c2 e^{i t} (1 + e^{-i t})$$

$$\text{In}[*]:= P21 := -\frac{1}{2} i * C1 * e^{-i t} (-1 + e^{i t}) + \frac{1}{2} * C2 * e^{-i t} (1 + e^{i t})$$

$$\text{In}[*]:= z31 := \frac{1}{2} e^{-i p1 t} (1 + e^{i p1 t}) * d1 + \frac{i e^{-i p1 t} (-1 + e^{i p1 t}) * d2}{2 p1}$$

$$\text{In}[*]:= z31$$

$$\text{Out}[*]:= -\frac{1}{2} i d2 e^{i t} (-1 + e^{-i t}) + \frac{1}{2} d1 e^{i t} (1 + e^{-i t})$$

$$\text{In}[*]:= \text{Z31} := \frac{1}{2} \text{i} * \text{D2} * \text{e}^{-\text{i} t} (-1 + \text{e}^{\text{i} t}) + \frac{1}{2} * \text{D2} * \text{e}^{-\text{i} t} (1 + \text{e}^{\text{i} t})$$

$$\text{In}[*]:= \text{p31} := -\frac{1}{2} \text{i} \text{e}^{-\text{i} \text{p1} t} (-1 + \text{e}^{\text{i} \text{p1} t}) \text{p1} * \text{d1} + \frac{1}{2} \text{e}^{-\text{i} \text{p1} t} (1 + \text{e}^{\text{i} \text{p1} t}) * \text{d2}$$

$$\text{In}[*]:= \text{p31}$$

$$\text{Out}[*]= \frac{1}{2} \text{i} \text{d1} \text{e}^{\text{i} t} (-1 + \text{e}^{-\text{i} t}) + \frac{1}{2} \text{d2} \text{e}^{\text{i} t} (1 + \text{e}^{-\text{i} t})$$

$$\text{In}[*]:= \text{P31} := -\frac{1}{2} \text{i} * \text{D1} * \text{e}^{-\text{i} t} (-1 + \text{e}^{\text{i} t}) + \frac{1}{2} * \text{D2} * \text{e}^{-\text{i} t} (1 + \text{e}^{\text{i} t})$$

$$\text{In}[*]:= \text{z2st}$$

$$\text{Out}[*]= \left(-\frac{1}{2} \text{i} \text{c2} \text{e}^{\text{i} t} (-1 + \text{e}^{-\text{i} t}) + \frac{1}{2} \text{c1} \text{e}^{\text{i} t} (1 + \text{e}^{-\text{i} t}) \right) \text{s} + \text{s}^3 \text{z23}$$

$$\text{In}[*]:= \text{Expand} \left[\left(-\frac{1}{2} \text{i} \text{c2} \text{e}^{\text{i} t} (-1 + \text{e}^{-\text{i} t}) + \frac{1}{2} \text{c1} \text{e}^{\text{i} t} (1 + \text{e}^{-\text{i} t}) \right) \text{s} + \text{s}^3 \text{z23} \right]$$

$$\text{Out}[*]= \frac{\text{c1} \text{s}}{2} - \frac{\text{i} \text{c2} \text{s}}{2} + \frac{1}{2} \text{c1} \text{e}^{\text{i} t} \text{s} + \frac{1}{2} \text{i} \text{c2} \text{e}^{\text{i} t} \text{s} + \text{s}^3 \text{z23}$$

$$\text{In}[*]:= \text{Collect}[\%, \text{s}]$$

$$\text{Out}[*]= \left(\frac{\text{c1}}{2} - \frac{\text{i} \text{c2}}{2} + \frac{1}{2} \text{c1} \text{e}^{\text{i} t} + \frac{1}{2} \text{i} \text{c2} \text{e}^{\text{i} t} \right) \text{s} + \text{s}^3 \text{z23}$$

$$\text{In}[*]:= \text{Z2st}$$

$$\text{Out}[*]= \left(\frac{1}{2} \text{i} \text{C2} \text{e}^{-\text{i} t} (-1 + \text{e}^{\text{i} t}) + \frac{1}{2} \text{C1} \text{e}^{-\text{i} t} (1 + \text{e}^{\text{i} t}) \right) \text{s} + \text{s}^3 \text{Z23}$$

$$\text{In}[*]:= \text{Expand} \left[\left(\frac{1}{2} \text{i} \text{C2} \text{e}^{-\text{i} t} (-1 + \text{e}^{\text{i} t}) + \frac{1}{2} \text{C1} \text{e}^{-\text{i} t} (1 + \text{e}^{\text{i} t}) \right) \text{s} + \text{s}^3 \text{Z23} \right]$$

$$\text{Out}[*]= \frac{\text{C1} \text{s}}{2} + \frac{\text{i} \text{C2} \text{s}}{2} + \frac{1}{2} \text{C1} \text{e}^{-\text{i} t} \text{s} - \frac{1}{2} \text{i} \text{C2} \text{e}^{-\text{i} t} \text{s} + \text{s}^3 \text{Z23}$$

$$\text{In}[*]:= \text{Collect}[\%, \text{s}]$$

$$\text{Out}[*]= \left(\frac{\text{C1}}{2} + \frac{\text{i} \text{C2}}{2} + \frac{1}{2} \text{C1} \text{e}^{-\text{i} t} - \frac{1}{2} \text{i} \text{C2} \text{e}^{-\text{i} t} \right) \text{s} + \text{s}^3 \text{Z23}$$

$$\text{In}[*]:= \text{dz2}$$

$$\text{Out}[*]= -\frac{\text{p2}}{2} + \frac{\text{i} \text{z2}}{2} + 2 \text{G} \text{p3} \text{Z2} \text{z3} - \text{i} \text{G} \text{Z2} \text{z3}^2$$

In[*]:= dz2 /. {z2 → z2st, z3 → z3st, Z2 → Z2st,
Z3 → Z3st, p2 → p2st, p3 → p3st, P2 → P2st, P3 → P3st}

$$\begin{aligned} \text{Out[*]} = & \frac{1}{2} \left(- \left(\frac{1}{2} \, i \, c1 \, e^{i t} (-1 + e^{-i t}) + \frac{1}{2} \, c2 \, e^{i t} (1 + e^{-i t}) \right) s - p23 \, s^3 \right) + \\ & \frac{1}{2} \, i \left(\left(- \frac{1}{2} \, i \, c2 \, e^{i t} (-1 + e^{-i t}) + \frac{1}{2} \, c1 \, e^{i t} (1 + e^{-i t}) \right) s + s^3 \, z23 \right) + \\ & 2 \, G \left(\left(\frac{1}{2} \, i \, d1 \, e^{i t} (-1 + e^{-i t}) + \frac{1}{2} \, d2 \, e^{i t} (1 + e^{-i t}) \right) s + p33 \, s^3 \right) \\ & \left(\left(\frac{1}{2} \, i \, C2 \, e^{-i t} (-1 + e^{i t}) + \frac{1}{2} \, C1 \, e^{-i t} (1 + e^{i t}) \right) s + s^3 \, Z23 \right) \\ & \left(\left(- \frac{1}{2} \, i \, d2 \, e^{i t} (-1 + e^{-i t}) + \frac{1}{2} \, d1 \, e^{i t} (1 + e^{-i t}) \right) s + s^3 \, z33 \right) - \\ & i \, G \left(\left(\frac{1}{2} \, i \, C2 \, e^{-i t} (-1 + e^{i t}) + \frac{1}{2} \, C1 \, e^{-i t} (1 + e^{i t}) \right) s + s^3 \, Z23 \right) \\ & \left(\left(- \frac{1}{2} \, i \, d2 \, e^{i t} (-1 + e^{-i t}) + \frac{1}{2} \, d1 \, e^{i t} (1 + e^{-i t}) \right) s + s^3 \, z33 \right)^2 \end{aligned}$$

In[*]:= Expand[%60]

$$\begin{aligned} \text{Out[*]} = & \frac{1}{2} \, i \, c1 \, e^{i t} s - \frac{1}{2} \, c2 \, e^{i t} s - \frac{1}{8} \, i \, C1 \, d1^2 \, G \, s^3 - \frac{3}{8} \, C2 \, d1^2 \, G \, s^3 + \frac{1}{4} \, C1 \, d1 \, d2 \, G \, s^3 + \frac{1}{4} \, i \, C2 \, d1 \, d2 \, G \, s^3 - \\ & \frac{3}{8} \, i \, C1 \, d2^2 \, G \, s^3 - \frac{1}{8} \, C2 \, d2^2 \, G \, s^3 + \frac{1}{8} \, i \, C1 \, d1^2 \, e^{-i t} \, G \, s^3 + \frac{1}{8} \, C2 \, d1^2 \, e^{-i t} \, G \, s^3 + \frac{1}{4} \, C1 \, d1 \, d2 \, e^{-i t} \, G \, s^3 - \\ & \frac{1}{4} \, i \, C2 \, d1 \, d2 \, e^{-i t} \, G \, s^3 - \frac{1}{8} \, i \, C1 \, d2^2 \, e^{-i t} \, G \, s^3 - \frac{1}{8} \, C2 \, d2^2 \, e^{-i t} \, G \, s^3 - \frac{5}{8} \, i \, C1 \, d1^2 \, e^{i t} \, G \, s^3 - \\ & \frac{1}{8} \, C2 \, d1^2 \, e^{i t} \, G \, s^3 + \frac{3}{4} \, C1 \, d1 \, d2 \, e^{i t} \, G \, s^3 - \frac{3}{4} \, i \, C2 \, d1 \, d2 \, e^{i t} \, G \, s^3 + \frac{1}{8} \, i \, C1 \, d2^2 \, e^{i t} \, G \, s^3 + \\ & \frac{5}{8} \, C2 \, d2^2 \, e^{i t} \, G \, s^3 - \frac{3}{8} \, i \, C1 \, d1^2 \, e^{2 i t} \, G \, s^3 + \frac{3}{8} \, C2 \, d1^2 \, e^{2 i t} \, G \, s^3 + \frac{3}{4} \, C1 \, d1 \, d2 \, e^{2 i t} \, G \, s^3 + \\ & \frac{3}{4} \, i \, C2 \, d1 \, d2 \, e^{2 i t} \, G \, s^3 + \frac{3}{8} \, i \, C1 \, d2^2 \, e^{2 i t} \, G \, s^3 - \frac{3}{8} \, C2 \, d2^2 \, e^{2 i t} \, G \, s^3 - \frac{p23 \, s^3}{2} + C1 \, d1 \, G \, p33 \, s^5 + \\ & C2 \, d2 \, G \, p33 \, s^5 + \frac{1}{2} \, C1 \, d1 \, e^{-i t} \, G \, p33 \, s^5 - \frac{1}{2} \, i \, C2 \, d1 \, e^{-i t} \, G \, p33 \, s^5 - \frac{1}{2} \, i \, C1 \, d2 \, e^{-i t} \, G \, p33 \, s^5 - \\ & \frac{1}{2} \, C2 \, d2 \, e^{-i t} \, G \, p33 \, s^5 + \frac{1}{2} \, C1 \, d1 \, e^{i t} \, G \, p33 \, s^5 + \frac{1}{2} \, i \, C2 \, d1 \, e^{i t} \, G \, p33 \, s^5 + \frac{1}{2} \, i \, C1 \, d2 \, e^{i t} \, G \, p33 \, s^5 - \\ & \frac{1}{2} \, C2 \, d2 \, e^{i t} \, G \, p33 \, s^5 + \frac{1}{2} \, i \, s^3 \, z23 + \frac{1}{4} \, i \, d1^2 \, G \, s^5 \, Z23 + \frac{1}{2} \, d1 \, d2 \, G \, s^5 \, Z23 - \frac{1}{4} \, i \, d2^2 \, G \, s^5 \, Z23 - \\ & \frac{1}{2} \, i \, d1^2 \, e^{i t} \, G \, s^5 \, Z23 - \frac{1}{2} \, i \, d2^2 \, e^{i t} \, G \, s^5 \, Z23 - \frac{3}{4} \, i \, d1^2 \, e^{2 i t} \, G \, s^5 \, Z23 + \frac{3}{2} \, d1 \, d2 \, e^{2 i t} \, G \, s^5 \, Z23 + \\ & \frac{3}{4} \, i \, d2^2 \, e^{2 i t} \, G \, s^5 \, Z23 + d1 \, G \, p33 \, s^7 \, Z23 - i \, d2 \, G \, p33 \, s^7 \, Z23 + d1 \, e^{i t} \, G \, p33 \, s^7 \, Z23 + \\ & i \, d2 \, e^{i t} \, G \, p33 \, s^7 \, Z23 - i \, C1 \, d1 \, G \, s^5 \, z33 - C2 \, d1 \, G \, s^5 \, z33 + C1 \, d2 \, G \, s^5 \, z33 - i \, C2 \, d2 \, G \, s^5 \, z33 - \\ & i \, C1 \, d1 \, e^{i t} \, G \, s^5 \, z33 + C2 \, d1 \, e^{i t} \, G \, s^5 \, z33 + C1 \, d2 \, e^{i t} \, G \, s^5 \, z33 + i \, C2 \, d2 \, e^{i t} \, G \, s^5 \, z33 + \\ & C1 \, G \, p33 \, s^7 \, z33 + i \, C2 \, G \, p33 \, s^7 \, z33 + C1 \, e^{-i t} \, G \, p33 \, s^7 \, z33 - i \, C2 \, e^{-i t} \, G \, p33 \, s^7 \, z33 - \\ & 2 \, i \, d1 \, e^{i t} \, G \, s^7 \, Z23 \, z33 + 2 \, d2 \, e^{i t} \, G \, s^7 \, Z23 \, z33 + 2 \, G \, p33 \, s^9 \, Z23 \, z33 - \frac{1}{2} \, i \, C1 \, G \, s^7 \, z33^2 + \\ & \frac{1}{2} \, C2 \, G \, s^7 \, z33^2 - \frac{1}{2} \, i \, C1 \, e^{-i t} \, G \, s^7 \, z33^2 - \frac{1}{2} \, C2 \, e^{-i t} \, G \, s^7 \, z33^2 - i \, G \, s^9 \, Z23 \, z33^2 \end{aligned}$$

In[]:= **Collect**[% , s]

$$\begin{aligned}
 \text{Out[]}= & \left(\frac{1}{2} \, \text{i} \, c1 \, e^{\text{i} \, t} - \frac{1}{2} \, c2 \, e^{\text{i} \, t} \right) s + \\
 & s^3 \left(-\frac{1}{8} \, \text{i} \, C1 \, d1^2 \, G - \frac{3}{8} \, C2 \, d1^2 \, G + \frac{1}{4} \, C1 \, d1 \, d2 \, G + \frac{1}{4} \, \text{i} \, C2 \, d1 \, d2 \, G - \frac{3}{8} \, \text{i} \, C1 \, d2^2 \, G - \frac{1}{8} \, C2 \, d2^2 \, G + \right. \\
 & \quad \frac{1}{8} \, \text{i} \, C1 \, d1^2 \, e^{-\text{i} \, t} \, G + \frac{1}{8} \, C2 \, d1^2 \, e^{-\text{i} \, t} \, G + \frac{1}{4} \, C1 \, d1 \, d2 \, e^{-\text{i} \, t} \, G - \frac{1}{4} \, \text{i} \, C2 \, d1 \, d2 \, e^{-\text{i} \, t} \, G - \\
 & \quad \frac{1}{8} \, \text{i} \, C1 \, d2^2 \, e^{-\text{i} \, t} \, G - \frac{1}{8} \, C2 \, d2^2 \, e^{-\text{i} \, t} \, G - \frac{5}{8} \, \text{i} \, C1 \, d1^2 \, e^{\text{i} \, t} \, G - \frac{1}{8} \, C2 \, d1^2 \, e^{\text{i} \, t} \, G + \frac{3}{4} \, C1 \, d1 \, d2 \, e^{\text{i} \, t} \, G - \\
 & \quad \frac{3}{4} \, \text{i} \, C2 \, d1 \, d2 \, e^{\text{i} \, t} \, G + \frac{1}{8} \, \text{i} \, C1 \, d2^2 \, e^{\text{i} \, t} \, G + \frac{5}{8} \, C2 \, d2^2 \, e^{\text{i} \, t} \, G - \frac{3}{8} \, \text{i} \, C1 \, d1^2 \, e^{2 \, \text{i} \, t} \, G + \frac{3}{8} \, C2 \, d1^2 \, e^{2 \, \text{i} \, t} \, G + \\
 & \quad \left. \frac{3}{4} \, C1 \, d1 \, d2 \, e^{2 \, \text{i} \, t} \, G + \frac{3}{4} \, \text{i} \, C2 \, d1 \, d2 \, e^{2 \, \text{i} \, t} \, G + \frac{3}{8} \, \text{i} \, C1 \, d2^2 \, e^{2 \, \text{i} \, t} \, G - \frac{3}{8} \, C2 \, d2^2 \, e^{2 \, \text{i} \, t} \, G - \frac{p23}{2} + \frac{\text{i} \, z23}{2} \right) + \\
 & s^5 \left(C1 \, d1 \, G \, p33 + C2 \, d2 \, G \, p33 + \frac{1}{2} \, C1 \, d1 \, e^{-\text{i} \, t} \, G \, p33 - \frac{1}{2} \, \text{i} \, C2 \, d1 \, e^{-\text{i} \, t} \, G \, p33 - \right. \\
 & \quad \frac{1}{2} \, \text{i} \, C1 \, d2 \, e^{-\text{i} \, t} \, G \, p33 - \frac{1}{2} \, C2 \, d2 \, e^{-\text{i} \, t} \, G \, p33 + \frac{1}{2} \, C1 \, d1 \, e^{\text{i} \, t} \, G \, p33 + \frac{1}{2} \, \text{i} \, C2 \, d1 \, e^{\text{i} \, t} \, G \, p33 + \\
 & \quad \frac{1}{2} \, \text{i} \, C1 \, d2 \, e^{\text{i} \, t} \, G \, p33 - \frac{1}{2} \, C2 \, d2 \, e^{\text{i} \, t} \, G \, p33 + \frac{1}{4} \, \text{i} \, d1^2 \, G \, Z23 + \frac{1}{2} \, d1 \, d2 \, G \, Z23 - \frac{1}{4} \, \text{i} \, d2^2 \, G \, Z23 - \\
 & \quad \frac{1}{2} \, \text{i} \, d1^2 \, e^{\text{i} \, t} \, G \, Z23 - \frac{1}{2} \, \text{i} \, d2^2 \, e^{\text{i} \, t} \, G \, Z23 - \frac{3}{4} \, \text{i} \, d1^2 \, e^{2 \, \text{i} \, t} \, G \, Z23 + \frac{3}{2} \, d1 \, d2 \, e^{2 \, \text{i} \, t} \, G \, Z23 + \\
 & \quad \frac{3}{4} \, \text{i} \, d2^2 \, e^{2 \, \text{i} \, t} \, G \, Z23 - \text{i} \, C1 \, d1 \, G \, z33 - C2 \, d1 \, G \, z33 + C1 \, d2 \, G \, z33 - \text{i} \, C2 \, d2 \, G \, z33 - \\
 & \quad \left. \text{i} \, C1 \, d1 \, e^{\text{i} \, t} \, G \, z33 + C2 \, d1 \, e^{\text{i} \, t} \, G \, z33 + C1 \, d2 \, e^{\text{i} \, t} \, G \, z33 + \text{i} \, C2 \, d2 \, e^{\text{i} \, t} \, G \, z33 \right) + \\
 & s^7 \left(d1 \, G \, p33 \, Z23 - \text{i} \, d2 \, G \, p33 \, Z23 + d1 \, e^{\text{i} \, t} \, G \, p33 \, Z23 + \text{i} \, d2 \, e^{\text{i} \, t} \, G \, p33 \, Z23 + C1 \, G \, p33 \, z33 + \right. \\
 & \quad \text{i} \, C2 \, G \, p33 \, z33 + C1 \, e^{-\text{i} \, t} \, G \, p33 \, z33 - \text{i} \, C2 \, e^{-\text{i} \, t} \, G \, p33 \, z33 - 2 \, \text{i} \, d1 \, e^{\text{i} \, t} \, G \, Z23 \, z33 + \\
 & \quad \left. 2 \, d2 \, e^{\text{i} \, t} \, G \, Z23 \, z33 - \frac{1}{2} \, \text{i} \, C1 \, G \, z33^2 + \frac{1}{2} \, C2 \, G \, z33^2 - \frac{1}{2} \, \text{i} \, C1 \, e^{-\text{i} \, t} \, G \, z33^2 - \frac{1}{2} \, C2 \, e^{-\text{i} \, t} \, G \, z33^2 \right) + \\
 & s^9 \left(2 \, G \, p33 \, Z23 \, z33 - \text{i} \, G \, Z23 \, z33^2 \right)
 \end{aligned}$$

In[*]:= **dp2 /. {z2 → z2st, z3 → z3st, Z2 → Z2st,
Z3 → Z3st, p2 → p2st, p3 → p3st, P2 → P2st, P3 → P3st}**

$$\begin{aligned}
 \text{Out[*]} = & \frac{1}{2} i \left(\left(\frac{1}{2} i c1 e^{i t} (-1 + e^{-i t}) + \frac{1}{2} c2 e^{i t} (1 + e^{-i t}) \right) s + p23 s^3 \right) + \\
 & \frac{1}{2} \left(\left(-\frac{1}{2} i c2 e^{i t} (-1 + e^{-i t}) + \frac{1}{2} c1 e^{i t} (1 + e^{-i t}) \right) s + s^3 z23 \right) - \\
 & 2 G \left(\left(-\frac{1}{2} i C1 e^{-i t} (-1 + e^{i t}) + \frac{1}{2} C2 e^{-i t} (1 + e^{i t}) \right) s + P23 s^3 \right) \\
 & \left(\left(\frac{1}{2} i d1 e^{i t} (-1 + e^{-i t}) + \frac{1}{2} d2 e^{i t} (1 + e^{-i t}) \right) s + p33 s^3 \right) \\
 & \left(\left(-\frac{1}{2} i d2 e^{i t} (-1 + e^{-i t}) + \frac{1}{2} d1 e^{i t} (1 + e^{-i t}) \right) s + s^3 z33 \right) - \\
 & 2 i G \left(\left(\frac{1}{2} i d1 e^{i t} (-1 + e^{-i t}) + \frac{1}{2} d2 e^{i t} (1 + e^{-i t}) \right) s + p33 s^3 \right) \\
 & \left(\left(\frac{1}{2} i C2 e^{-i t} (-1 + e^{i t}) + \frac{1}{2} C1 e^{-i t} (1 + e^{i t}) \right) s + s^3 Z23 \right) \\
 & \left(\left(-\frac{1}{2} i d2 e^{i t} (-1 + e^{-i t}) + \frac{1}{2} d1 e^{i t} (1 + e^{-i t}) \right) s + s^3 z33 \right) + \\
 & i G \left(\left(-\frac{1}{2} i C1 e^{-i t} (-1 + e^{i t}) + \frac{1}{2} C2 e^{-i t} (1 + e^{i t}) \right) s + P23 s^3 \right) \\
 & \left(\left(-\frac{1}{2} i d2 e^{i t} (-1 + e^{-i t}) + \frac{1}{2} d1 e^{i t} (1 + e^{-i t}) \right) s + s^3 z33 \right)^2
 \end{aligned}$$

In[]:= Expand[%63]

$$\begin{aligned}
\text{Out[]}= & \frac{1}{2} c_1 e^{i t} s + \frac{1}{2} i c_2 e^{i t} s - \frac{1}{8} C_1 d_1^2 G s^3 + \frac{3}{8} i C_2 d_1^2 G s^3 - \frac{1}{4} i C_1 d_1 d_2 G s^3 + \\
& \frac{1}{4} C_2 d_1 d_2 G s^3 - \frac{3}{8} C_1 d_2^2 G s^3 + \frac{1}{8} i C_2 d_2^2 G s^3 + \frac{3}{8} C_1 d_1^2 e^{-i t} G s^3 - \frac{3}{8} i C_2 d_1^2 e^{-i t} G s^3 - \\
& \frac{3}{4} i C_1 d_1 d_2 e^{-i t} G s^3 - \frac{3}{4} C_2 d_1 d_2 e^{-i t} G s^3 - \frac{3}{8} C_1 d_2^2 e^{-i t} G s^3 + \frac{3}{8} i C_2 d_2^2 e^{-i t} G s^3 - \\
& \frac{3}{8} C_1 d_1^2 e^{i t} G s^3 + \frac{7}{8} i C_2 d_1^2 e^{i t} G s^3 - \frac{5}{4} i C_1 d_1 d_2 e^{i t} G s^3 - \frac{5}{4} C_2 d_1 d_2 e^{i t} G s^3 + \\
& \frac{7}{8} C_1 d_2^2 e^{i t} G s^3 - \frac{3}{8} i C_2 d_2^2 e^{i t} G s^3 + \frac{1}{8} C_1 d_1^2 e^{2 i t} G s^3 + \frac{1}{8} i C_2 d_1^2 e^{2 i t} G s^3 + \\
& \frac{1}{4} i C_1 d_1 d_2 e^{2 i t} G s^3 - \frac{1}{4} C_2 d_1 d_2 e^{2 i t} G s^3 - \frac{1}{8} C_1 d_2^2 e^{2 i t} G s^3 - \frac{1}{8} i C_2 d_2^2 e^{2 i t} G s^3 + \\
& \frac{1}{2} i p_{23} s^3 - \frac{1}{4} i d_1^2 G P_{23} s^5 - \frac{1}{2} d_1 d_2 G P_{23} s^5 + \frac{1}{4} i d_2^2 G P_{23} s^5 + \frac{1}{2} i d_1^2 e^{i t} G P_{23} s^5 + \\
& \frac{1}{2} i d_2^2 e^{i t} G P_{23} s^5 + \frac{3}{4} i d_1^2 e^{2 i t} G P_{23} s^5 - \frac{3}{2} d_1 d_2 e^{2 i t} G P_{23} s^5 - \frac{3}{4} i d_2^2 e^{2 i t} G P_{23} s^5 - \\
& i C_1 d_1 G p_{33} s^5 - C_2 d_1 G p_{33} s^5 + C_1 d_2 G p_{33} s^5 - i C_2 d_2 G p_{33} s^5 - i C_1 d_1 e^{-i t} G p_{33} s^5 - \\
& C_2 d_1 e^{-i t} G p_{33} s^5 - C_1 d_2 e^{-i t} G p_{33} s^5 + i C_2 d_2 e^{-i t} G p_{33} s^5 - d_1 G P_{23} p_{33} s^7 + \\
& i d_2 G P_{23} p_{33} s^7 - d_1 e^{i t} G P_{23} p_{33} s^7 - i d_2 e^{i t} G P_{23} p_{33} s^7 + \frac{s^3 z_{23}}{2} + \frac{1}{2} d_1^2 G s^5 Z_{23} - \\
& i d_1 d_2 G s^5 Z_{23} - \frac{1}{2} d_2^2 G s^5 Z_{23} - \frac{1}{2} d_1^2 e^{2 i t} G s^5 Z_{23} - i d_1 d_2 e^{2 i t} G s^5 Z_{23} + \\
& \frac{1}{2} d_2^2 e^{2 i t} G s^5 Z_{23} - i d_1 G p_{33} s^7 Z_{23} - d_2 G p_{33} s^7 Z_{23} - i d_1 e^{i t} G p_{33} s^7 Z_{23} + \\
& d_2 e^{i t} G p_{33} s^7 Z_{23} - C_1 d_1 G s^5 z_{33} + 2 i C_2 d_1 G s^5 z_{33} - 2 i C_1 d_2 G s^5 z_{33} - \\
& C_2 d_2 G s^5 z_{33} + \frac{1}{2} C_1 d_1 e^{-i t} G s^5 z_{33} - \frac{1}{2} i C_2 d_1 e^{-i t} G s^5 z_{33} - \frac{1}{2} i C_1 d_2 e^{-i t} G s^5 z_{33} - \\
& \frac{1}{2} C_2 d_2 e^{-i t} G s^5 z_{33} + \frac{1}{2} C_1 d_1 e^{i t} G s^5 z_{33} + \frac{1}{2} i C_2 d_1 e^{i t} G s^5 z_{33} + \frac{1}{2} i C_1 d_2 e^{i t} G s^5 z_{33} - \\
& \frac{1}{2} C_2 d_2 e^{i t} G s^5 z_{33} + 2 i d_1 e^{i t} G P_{23} s^7 z_{33} - 2 d_2 e^{i t} G P_{23} s^7 z_{33} - 2 i C_1 e^{-i t} G p_{33} s^7 z_{33} - \\
& 2 C_2 e^{-i t} G p_{33} s^7 z_{33} - 2 G P_{23} p_{33} s^9 z_{33} + d_1 G s^7 Z_{23} z_{33} - i d_2 G s^7 Z_{23} z_{33} - \\
& d_1 e^{i t} G s^7 Z_{23} z_{33} - i d_2 e^{i t} G s^7 Z_{23} z_{33} - 2 i G p_{33} s^9 Z_{23} z_{33} + \frac{1}{2} C_1 G s^7 z_{33}^2 + \\
& \frac{1}{2} i C_2 G s^7 z_{33}^2 - \frac{1}{2} C_1 e^{-i t} G s^7 z_{33}^2 + \frac{1}{2} i C_2 e^{-i t} G s^7 z_{33}^2 + i G P_{23} s^9 z_{33}^2
\end{aligned}$$

In[]:= Collect[%, s]

$$\begin{aligned}
 \text{Out[]}= & \left(\frac{1}{2} c1 e^{i t} + \frac{1}{2} i c2 e^{i t} \right) s + \\
 & s^3 \left(-\frac{1}{8} C1 d1^2 G + \frac{3}{8} i C2 d1^2 G - \frac{1}{4} i C1 d1 d2 G + \frac{1}{4} C2 d1 d2 G - \frac{3}{8} C1 d2^2 G + \frac{1}{8} i C2 d2^2 G + \right. \\
 & \quad \frac{3}{8} C1 d1^2 e^{-i t} G - \frac{3}{8} i C2 d1^2 e^{-i t} G - \frac{3}{4} i C1 d1 d2 e^{-i t} G - \frac{3}{4} C2 d1 d2 e^{-i t} G - \\
 & \quad \frac{3}{8} C1 d2^2 e^{-i t} G + \frac{3}{8} i C2 d2^2 e^{-i t} G - \frac{3}{8} C1 d1^2 e^{i t} G + \frac{7}{8} i C2 d1^2 e^{i t} G - \frac{5}{4} i C1 d1 d2 e^{i t} G - \\
 & \quad \frac{5}{4} C2 d1 d2 e^{i t} G + \frac{7}{8} C1 d2^2 e^{i t} G - \frac{3}{8} i C2 d2^2 e^{i t} G + \frac{1}{8} C1 d1^2 e^{2 i t} G + \frac{1}{8} i C2 d1^2 e^{2 i t} G + \\
 & \quad \left. \frac{1}{4} i C1 d1 d2 e^{2 i t} G - \frac{1}{4} C2 d1 d2 e^{2 i t} G - \frac{1}{8} C1 d2^2 e^{2 i t} G - \frac{1}{8} i C2 d2^2 e^{2 i t} G + \frac{i p23}{2} + \frac{z23}{2} \right) + \\
 & s^5 \left(-\frac{1}{4} i d1^2 G P23 - \frac{1}{2} d1 d2 G P23 + \frac{1}{4} i d2^2 G P23 + \frac{1}{2} i d1^2 e^{i t} G P23 + \frac{1}{2} i d2^2 e^{i t} G P23 + \right. \\
 & \quad \frac{3}{4} i d1^2 e^{2 i t} G P23 - \frac{3}{2} d1 d2 e^{2 i t} G P23 - \frac{3}{4} i d2^2 e^{2 i t} G P23 - i C1 d1 G p33 - \\
 & \quad C2 d1 G p33 + C1 d2 G p33 - i C2 d2 G p33 - i C1 d1 e^{-i t} G p33 - C2 d1 e^{-i t} G p33 - \\
 & \quad C1 d2 e^{-i t} G p33 + i C2 d2 e^{-i t} G p33 + \frac{1}{2} d1^2 G Z23 - i d1 d2 G Z23 - \frac{1}{2} d2^2 G Z23 - \\
 & \quad \frac{1}{2} d1^2 e^{2 i t} G Z23 - i d1 d2 e^{2 i t} G Z23 + \frac{1}{2} d2^2 e^{2 i t} G Z23 - C1 d1 G z33 + \\
 & \quad 2 i C2 d1 G z33 - 2 i C1 d2 G z33 - C2 d2 G z33 + \frac{1}{2} C1 d1 e^{-i t} G z33 - \\
 & \quad \frac{1}{2} i C2 d1 e^{-i t} G z33 - \frac{1}{2} i C1 d2 e^{-i t} G z33 - \frac{1}{2} C2 d2 e^{-i t} G z33 + \\
 & \quad \left. \frac{1}{2} C1 d1 e^{i t} G z33 + \frac{1}{2} i C2 d1 e^{i t} G z33 + \frac{1}{2} i C1 d2 e^{i t} G z33 - \frac{1}{2} C2 d2 e^{i t} G z33 \right) + \\
 & s^7 \left(-d1 G P23 p33 + i d2 G P23 p33 - d1 e^{i t} G P23 p33 - i d2 e^{i t} G P23 p33 - \right. \\
 & \quad i d1 G p33 Z23 - d2 G p33 Z23 - i d1 e^{i t} G p33 Z23 + d2 e^{i t} G p33 Z23 + \\
 & \quad 2 i d1 e^{i t} G P23 z33 - 2 d2 e^{i t} G P23 z33 - 2 i C1 e^{-i t} G p33 z33 - 2 C2 e^{-i t} G p33 z33 + \\
 & \quad d1 G Z23 z33 - i d2 G Z23 z33 - d1 e^{i t} G Z23 z33 - i d2 e^{i t} G Z23 z33 + \\
 & \quad \left. \frac{1}{2} C1 G z33^2 + \frac{1}{2} i C2 G z33^2 - \frac{1}{2} C1 e^{-i t} G z33^2 + \frac{1}{2} i C2 e^{-i t} G z33^2 \right) + \\
 & s^9 \left(-2 G P23 p33 z33 - 2 i G p33 Z23 z33 + i G P23 z33^2 \right)
 \end{aligned}$$

$$\begin{aligned}
In[*]:= & \text{dz2trunc} := \left(\frac{1}{2} \, i \, c1 \, e^{i t} - \frac{1}{2} \, c2 \, e^{i t} \right) s + \\
& s^3 \left(-\frac{1}{8} \, i \, C1 \, d1^2 \, G - \frac{3}{8} \, C2 \, d1^2 \, G + \frac{1}{4} \, C1 \, d1 \, d2 \, G + \frac{1}{4} \, i \, C2 \, d1 \, d2 \, G - \frac{3}{8} \, i \, C1 \, d2^2 \, G - \frac{1}{8} \, C2 \, d2^2 \, G + \right. \\
& \frac{1}{8} \, i \, C1 \, d1^2 \, e^{-i t} \, G + \frac{1}{8} \, C2 \, d1^2 \, e^{-i t} \, G + \frac{1}{4} \, C1 \, d1 \, d2 \, e^{-i t} \, G - \frac{1}{4} \, i \, C2 \, d1 \, d2 \, e^{-i t} \, G - \\
& \frac{1}{8} \, i \, C1 \, d2^2 \, e^{-i t} \, G - \frac{1}{8} \, C2 \, d2^2 \, e^{-i t} \, G - \frac{5}{8} \, i \, C1 \, d1^2 \, e^{i t} \, G - \frac{1}{8} \, C2 \, d1^2 \, e^{i t} \, G + \frac{3}{4} \, C1 \, d1 \, d2 \, e^{i t} \, G - \\
& \frac{3}{4} \, i \, C2 \, d1 \, d2 \, e^{i t} \, G + \frac{1}{8} \, i \, C1 \, d2^2 \, e^{i t} \, G + \frac{5}{8} \, C2 \, d2^2 \, e^{i t} \, G - \frac{3}{8} \, i \, C1 \, d1^2 \, e^{2 i t} \, G + \frac{3}{8} \, C2 \, d1^2 \, e^{2 i t} \, G + \\
& \left. \frac{3}{4} \, C1 \, d1 \, d2 \, e^{2 i t} \, G + \frac{3}{4} \, i \, C2 \, d1 \, d2 \, e^{2 i t} \, G + \frac{3}{8} \, i \, C1 \, d2^2 \, e^{2 i t} \, G - \frac{3}{8} \, C2 \, d2^2 \, e^{2 i t} \, G - \frac{p23}{2} + \frac{i \, z23}{2} \right)
\end{aligned}$$

In[*]:= dz2trunc

$$\begin{aligned}
Out[*]:= & \left(\frac{1}{2} \, i \, c1 \, e^{i t} - \frac{1}{2} \, c2 \, e^{i t} \right) s + \\
& s^3 \left(-\frac{1}{8} \, i \, C1 \, d1^2 \, G - \frac{3}{8} \, C2 \, d1^2 \, G + \frac{1}{4} \, C1 \, d1 \, d2 \, G + \frac{1}{4} \, i \, C2 \, d1 \, d2 \, G - \frac{3}{8} \, i \, C1 \, d2^2 \, G - \frac{1}{8} \, C2 \, d2^2 \, G + \right. \\
& \frac{1}{8} \, i \, C1 \, d1^2 \, e^{-i t} \, G + \frac{1}{8} \, C2 \, d1^2 \, e^{-i t} \, G + \frac{1}{4} \, C1 \, d1 \, d2 \, e^{-i t} \, G - \frac{1}{4} \, i \, C2 \, d1 \, d2 \, e^{-i t} \, G - \\
& \frac{1}{8} \, i \, C1 \, d2^2 \, e^{-i t} \, G - \frac{1}{8} \, C2 \, d2^2 \, e^{-i t} \, G - \frac{5}{8} \, i \, C1 \, d1^2 \, e^{i t} \, G - \frac{1}{8} \, C2 \, d1^2 \, e^{i t} \, G + \frac{3}{4} \, C1 \, d1 \, d2 \, e^{i t} \, G - \\
& \frac{3}{4} \, i \, C2 \, d1 \, d2 \, e^{i t} \, G + \frac{1}{8} \, i \, C1 \, d2^2 \, e^{i t} \, G + \frac{5}{8} \, C2 \, d2^2 \, e^{i t} \, G - \frac{3}{8} \, i \, C1 \, d1^2 \, e^{2 i t} \, G + \frac{3}{8} \, C2 \, d1^2 \, e^{2 i t} \, G + \\
& \left. \frac{3}{4} \, C1 \, d1 \, d2 \, e^{2 i t} \, G + \frac{3}{4} \, i \, C2 \, d1 \, d2 \, e^{2 i t} \, G + \frac{3}{8} \, i \, C1 \, d2^2 \, e^{2 i t} \, G - \frac{3}{8} \, C2 \, d2^2 \, e^{2 i t} \, G - \frac{p23}{2} + \frac{i \, z23}{2} \right)
\end{aligned}$$

$$In[*]:= \text{dp2trunc} := \left(\frac{1}{2} \, c1 \, e^{i t} + \frac{1}{2} \, i \, c2 \, e^{i t} \right) s +$$

$$\begin{aligned}
& s^3 \left(-\frac{1}{8} \, C1 \, d1^2 \, G + \frac{3}{8} \, i \, C2 \, d1^2 \, G - \frac{1}{4} \, i \, C1 \, d1 \, d2 \, G + \frac{1}{4} \, C2 \, d1 \, d2 \, G - \frac{3}{8} \, C1 \, d2^2 \, G + \frac{1}{8} \, i \, C2 \, d2^2 \, G + \right. \\
& \frac{3}{8} \, C1 \, d1^2 \, e^{-i t} \, G - \frac{3}{8} \, i \, C2 \, d1^2 \, e^{-i t} \, G - \frac{3}{4} \, i \, C1 \, d1 \, d2 \, e^{-i t} \, G - \frac{3}{4} \, C2 \, d1 \, d2 \, e^{-i t} \, G - \\
& \frac{3}{8} \, C1 \, d2^2 \, e^{-i t} \, G + \frac{3}{8} \, i \, C2 \, d2^2 \, e^{-i t} \, G - \frac{3}{8} \, C1 \, d1^2 \, e^{i t} \, G + \frac{7}{8} \, i \, C2 \, d1^2 \, e^{i t} \, G - \frac{5}{4} \, i \, C1 \, d1 \, d2 \, e^{i t} \, G - \\
& \frac{5}{4} \, C2 \, d1 \, d2 \, e^{i t} \, G + \frac{7}{8} \, C1 \, d2^2 \, e^{i t} \, G - \frac{3}{8} \, i \, C2 \, d2^2 \, e^{i t} \, G + \frac{1}{8} \, C1 \, d1^2 \, e^{2 i t} \, G + \frac{1}{8} \, i \, C2 \, d1^2 \, e^{2 i t} \, G + \\
& \left. \frac{1}{4} \, i \, C1 \, d1 \, d2 \, e^{2 i t} \, G - \frac{1}{4} \, C2 \, d1 \, d2 \, e^{2 i t} \, G - \frac{1}{8} \, C1 \, d2^2 \, e^{2 i t} \, G - \frac{1}{8} \, i \, C2 \, d2^2 \, e^{2 i t} \, G + \frac{i \, p23}{2} + \frac{z23}{2} \right)
\end{aligned}$$

In[]:= **dp2trunc**

$$\begin{aligned}
 \text{Out[]}= & \left(\frac{1}{2} c1 e^{i t} + \frac{1}{2} i c2 e^{i t} \right) s + \\
 & s^3 \left(-\frac{1}{8} C1 d1^2 G + \frac{3}{8} i C2 d1^2 G - \frac{1}{4} i C1 d1 d2 G + \frac{1}{4} C2 d1 d2 G - \frac{3}{8} C1 d2^2 G + \frac{1}{8} i C2 d2^2 G + \right. \\
 & \quad \frac{3}{8} C1 d1^2 e^{-i t} G - \frac{3}{8} i C2 d1^2 e^{-i t} G - \frac{3}{4} i C1 d1 d2 e^{-i t} G - \frac{3}{4} C2 d1 d2 e^{-i t} G - \\
 & \quad \frac{3}{8} C1 d2^2 e^{-i t} G + \frac{3}{8} i C2 d2^2 e^{-i t} G - \frac{3}{8} C1 d1^2 e^{i t} G + \frac{7}{8} i C2 d1^2 e^{i t} G - \frac{5}{4} i C1 d1 d2 e^{i t} G - \\
 & \quad \frac{5}{4} C2 d1 d2 e^{i t} G + \frac{7}{8} C1 d2^2 e^{i t} G - \frac{3}{8} i C2 d2^2 e^{i t} G + \frac{1}{8} C1 d1^2 e^{2 i t} G + \frac{1}{8} i C2 d1^2 e^{2 i t} G + \\
 & \quad \left. \frac{1}{4} i C1 d1 d2 e^{2 i t} G - \frac{1}{4} C2 d1 d2 e^{2 i t} G - \frac{1}{8} C1 d2^2 e^{2 i t} G - \frac{1}{8} i C2 d2^2 e^{2 i t} G + \frac{i p23}{2} + \frac{z23}{2} \right)
 \end{aligned}$$

In[]:= DSolve[

$$\begin{aligned}
\{l'[t] = & -\frac{1}{8}i C1 d1^2 G - \frac{3}{8} C2 d1^2 G + \frac{1}{4} C1 d1 d2 G + \frac{1}{4}i C2 d1 d2 G - \frac{3}{8}i C1 d2^2 G - \frac{1}{8} C2 d2^2 G + \\
& \frac{1}{8}i C1 d1^2 e^{-it} G + \frac{1}{8} C2 d1^2 e^{-it} G + \frac{1}{4} C1 d1 d2 e^{-it} G - \frac{1}{4}i C2 d1 d2 e^{-it} G - \\
& \frac{1}{8}i C1 d2^2 e^{-it} G - \frac{1}{8} C2 d2^2 e^{-it} G - \frac{5}{8}i C1 d1^2 e^{it} G - \frac{1}{8} C2 d1^2 e^{it} G + \\
& \frac{3}{4} C1 d1 d2 e^{it} G - \frac{3}{4}i C2 d1 d2 e^{it} G + \frac{1}{8}i C1 d2^2 e^{it} G + \\
& \frac{5}{8} C2 d2^2 e^{it} G - \frac{3}{8}i C1 d1^2 e^{2it} G + \frac{3}{8} C2 d1^2 e^{2it} G + \frac{3}{4} C1 d1 d2 e^{2it} G + \\
& \frac{3}{4}i C2 d1 d2 e^{2it} G + \frac{3}{8}i C1 d2^2 e^{2it} G - \frac{3}{8} C2 d2^2 e^{2it} G - \frac{m[t]}{2} + \frac{i * l[t]}{2}, \\
m'[t] = & -\frac{1}{8} C1 d1^2 G + \frac{3}{8}i C2 d1^2 G - \frac{1}{4}i C1 d1 d2 G + \frac{1}{4} C2 d1 d2 G - \frac{3}{8} C1 d2^2 G + \\
& \frac{1}{8}i C2 d2^2 G + \frac{3}{8} C1 d1^2 e^{-it} G - \frac{3}{8}i C2 d1^2 e^{-it} G - \frac{3}{4}i C1 d1 d2 e^{-it} G - \\
& \frac{3}{4} C2 d1 d2 e^{-it} G - \frac{3}{8} C1 d2^2 e^{-it} G + \frac{3}{8}i C2 d2^2 e^{-it} G - \frac{3}{8} C1 d1^2 e^{it} G + \frac{7}{8}i C2 d1^2 e^{it} G - \\
& \frac{5}{4}i C1 d1 d2 e^{it} G - \frac{5}{4} C2 d1 d2 e^{it} G + \frac{7}{8} C1 d2^2 e^{it} G - \frac{3}{8}i C2 d2^2 e^{it} G + \\
& \frac{1}{8} C1 d1^2 e^{2it} G + \frac{1}{8}i C2 d1^2 e^{2it} G + \frac{1}{4}i C1 d1 d2 e^{2it} G - \frac{1}{4} C2 d1 d2 e^{2it} G - \\
& \frac{1}{8} C1 d2^2 e^{2it} G - \frac{1}{8}i C2 d2^2 e^{2it} G + \frac{i * m[t]}{2} + \frac{l[t]}{2}\}, \{l[t], m[t]\}, t]
\end{aligned}$$

$$\begin{aligned}
Out[] = & \left\{ \left\{ l[t] \rightarrow \frac{1}{8} e^{\frac{it}{2}} G \left(2 \left(-2i C2 d1 + C1 (d1 + i d2) \right) (d1 - i d2) e^{-it} + \right. \right. \\
& 2 \left(-i d1 + d2 \right) \left(-i C1 d1 + 2 C2 d1 - C1 d2 \right) e^{it} - (C1 - i C2) (d1 - i d2)^2 e^{-2it} - \\
& (C1 + i C2) (d1 + i d2)^2 e^{2it} - 4 (i C1 + C2) (d1 + i d2)^2 t \right) \cos\left[\frac{t}{2}\right] + \\
& e^{\frac{it}{2}} C[1] \cos\left[\frac{t}{2}\right] + \frac{1}{8} e^{\frac{it}{2}} G \left(2 (d1 - i d2) (C2 (d1 + i d2) - 2 C1 d2) e^{-it} - \right. \\
& 2 (d1 + i d2) (C2 (d1 - i d2) - 2 C1 d2) e^{it} - i (C1 - i C2) (d1 - i d2)^2 e^{-2it} + \\
& i (C1 + i C2) (d1 + i d2)^2 e^{2it} + 4 (C1 - i C2) (d1 + i d2)^2 t \right) \sin\left[\frac{t}{2}\right] - e^{\frac{it}{2}} C[2] \sin\left[\frac{t}{2}\right], \\
m[t] \rightarrow & -\frac{1}{8} e^{\frac{it}{2}} G \left(2 (d1 - i d2) (C2 (d1 + i d2) - 2 C1 d2) e^{-it} - \right. \\
& 2 (d1 + i d2) (C2 (d1 - i d2) - 2 C1 d2) e^{it} - i (C1 - i C2) (d1 - i d2)^2 e^{-2it} + \\
& i (C1 + i C2) (d1 + i d2)^2 e^{2it} + 4 (C1 - i C2) (d1 + i d2)^2 t \right) \cos\left[\frac{t}{2}\right] + \\
& e^{\frac{it}{2}} C[2] \cos\left[\frac{t}{2}\right] + \frac{1}{8} e^{\frac{it}{2}} G \left(2 \left(-2i C2 d1 + C1 (d1 + i d2) \right) (d1 - i d2) e^{-it} + \right. \\
& 2 \left(-i d1 + d2 \right) \left(-i C1 d1 + 2 C2 d1 - C1 d2 \right) e^{it} - (C1 - i C2) (d1 - i d2)^2 e^{-2it} - \\
& (C1 + i C2) (d1 + i d2)^2 e^{2it} - 4 (i C1 + C2) (d1 + i d2)^2 t \right) \sin\left[\frac{t}{2}\right] + e^{\frac{it}{2}} C[1] \sin\left[\frac{t}{2}\right] \} \}
\end{aligned}$$

$$\begin{aligned}
In[*]:= & \frac{1}{8} e^{\frac{i t}{2}} G \left(2 \left(-2 i C2 d1 + C1 (d1 + i d2) \right) (d1 - i d2) e^{-i t} + \right. \\
& 2 \left(-i d1 + d2 \right) \left(-i C1 d1 + 2 C2 d1 - C1 d2 \right) e^{i t} - (C1 - i C2) (d1 - i d2)^2 e^{-2 i t} - \\
& (C1 + i C2) (d1 + i d2)^2 e^{2 i t} - 4 (i C1 + C2) (d1 + i d2)^2 t \Big) \cos\left[\frac{t}{2}\right] + \\
& e^{\frac{i t}{2}} C[1] \cos\left[\frac{t}{2}\right] + \frac{1}{8} e^{\frac{i t}{2}} G \left(2 (d1 - i d2) (C2 (d1 + i d2) - 2 C1 d2) e^{-i t} - \right. \\
& 2 (d1 + i d2) (C2 (d1 - i d2) - 2 C1 d2) e^{i t} - i (C1 - i C2) (d1 - i d2)^2 e^{-2 i t} + \\
& i (C1 + i C2) (d1 + i d2)^2 e^{2 i t} + 4 (C1 - i C2) (d1 + i d2)^2 t \Big) \sin\left[\frac{t}{2}\right] - e^{\frac{i t}{2}} C[2] \sin\left[\frac{t}{2}\right]
\end{aligned}$$

$$\begin{aligned}
Out[*]:= & \frac{1}{8} e^{\frac{i t}{2}} G \left(2 \left(-2 i C2 d1 + C1 (d1 + i d2) \right) (d1 - i d2) e^{-i t} + \right. \\
& 2 \left(-i d1 + d2 \right) \left(-i C1 d1 + 2 C2 d1 - C1 d2 \right) e^{i t} - (C1 - i C2) (d1 - i d2)^2 e^{-2 i t} - \\
& (C1 + i C2) (d1 + i d2)^2 e^{2 i t} - 4 (i C1 + C2) (d1 + i d2)^2 t \Big) \cos\left[\frac{t}{2}\right] + \\
& e^{\frac{i t}{2}} C[1] \cos\left[\frac{t}{2}\right] + \frac{1}{8} e^{\frac{i t}{2}} G \left(2 (d1 - i d2) (C2 (d1 + i d2) - 2 C1 d2) e^{-i t} - \right. \\
& 2 (d1 + i d2) (C2 (d1 - i d2) - 2 C1 d2) e^{i t} - i (C1 - i C2) (d1 - i d2)^2 e^{-2 i t} + \\
& i (C1 + i C2) (d1 + i d2)^2 e^{2 i t} + 4 (C1 - i C2) (d1 + i d2)^2 t \Big) \sin\left[\frac{t}{2}\right] - e^{\frac{i t}{2}} C[2] \sin\left[\frac{t}{2}\right]
\end{aligned}$$

`In[*]:= TrigReduce[%71]`

$$\begin{aligned}
Out[*]:= & \frac{1}{8} C1 d1^2 G - \frac{3}{8} i C2 d1^2 G + \frac{1}{4} i C1 d1 d2 G - \frac{1}{4} C2 d1 d2 G + \frac{3}{8} C1 d2^2 G - \frac{1}{8} i C2 d2^2 G - \\
& \frac{1}{8} C1 d1^2 e^{i t} G - \frac{3}{8} i C2 d1^2 e^{i t} G + \frac{1}{4} i C1 d1 d2 e^{i t} G + \frac{1}{4} C2 d1 d2 e^{i t} G - \\
& \frac{3}{8} C1 d2^2 e^{i t} G - \frac{1}{8} i C2 d2^2 e^{i t} G - \frac{1}{4} C1 d1^2 e^{2 i t} G - \frac{1}{4} i C2 d1^2 e^{2 i t} G - \\
& \frac{1}{2} i C1 d1 d2 e^{2 i t} G + \frac{1}{2} C2 d1 d2 e^{2 i t} G + \frac{1}{4} C1 d2^2 e^{2 i t} G + \frac{1}{4} i C2 d2^2 e^{2 i t} G - \\
& \frac{1}{2} i C1 d1^2 e^{i t} G t - \frac{1}{2} C2 d1^2 e^{i t} G t + C1 d1 d2 e^{i t} G t - i C2 d1 d2 e^{i t} G t + \\
& \frac{1}{2} i C1 d2^2 e^{i t} G t + \frac{1}{2} C2 d2^2 e^{i t} G t + \frac{C[1]}{2} + \frac{1}{2} e^{i t} C[1] - \frac{1}{2} i C[2] + \frac{1}{2} i e^{i t} C[2]
\end{aligned}$$

$$\begin{aligned}
In[*]:= & \frac{1}{8} C1 d1^2 G - \frac{3}{8} \text{I} C2 d1^2 G + \frac{1}{4} \text{I} C1 d1 d2 G - \frac{1}{4} C2 d1 d2 G + \frac{3}{8} C1 d2^2 G - \frac{1}{8} \text{I} C2 d2^2 G - \\
& \frac{1}{8} C1 d1^2 e^{\text{I} t} G - \frac{3}{8} \text{I} C2 d1^2 e^{\text{I} t} G + \frac{1}{4} \text{I} C1 d1 d2 e^{\text{I} t} G + \frac{1}{4} C2 d1 d2 e^{\text{I} t} G - \frac{3}{8} C1 d2^2 e^{\text{I} t} G - \\
& \frac{1}{8} \text{I} C2 d2^2 e^{\text{I} t} G - \frac{1}{4} C1 d1^2 e^{2 \text{I} t} G - \frac{1}{4} \text{I} C2 d1^2 e^{2 \text{I} t} G - \frac{1}{2} \text{I} C1 d1 d2 e^{2 \text{I} t} G + \\
& \frac{1}{2} C2 d1 d2 e^{2 \text{I} t} G + \frac{1}{4} C1 d2^2 e^{2 \text{I} t} G + \frac{1}{4} \text{I} C2 d2^2 e^{2 \text{I} t} G - \frac{1}{2} \text{I} C1 d1^2 e^{\text{I} t} G t - \\
& \frac{1}{2} C2 d1^2 e^{\text{I} t} G t + C1 d1 d2 e^{\text{I} t} G t - \text{I} C2 d1 d2 e^{\text{I} t} G t + \frac{1}{2} \text{I} C1 d2^2 e^{\text{I} t} G t + \frac{1}{2} C2 d2^2 e^{\text{I} t} G t \\
Out[*]= & \frac{1}{8} C1 d1^2 G - \frac{3}{8} \text{I} C2 d1^2 G + \frac{1}{4} \text{I} C1 d1 d2 G - \frac{1}{4} C2 d1 d2 G + \frac{3}{8} C1 d2^2 G - \frac{1}{8} \text{I} C2 d2^2 G - \\
& \frac{1}{8} C1 d1^2 e^{\text{I} t} G - \frac{3}{8} \text{I} C2 d1^2 e^{\text{I} t} G + \frac{1}{4} \text{I} C1 d1 d2 e^{\text{I} t} G + \frac{1}{4} C2 d1 d2 e^{\text{I} t} G - \frac{3}{8} C1 d2^2 e^{\text{I} t} G - \\
& \frac{1}{8} \text{I} C2 d2^2 e^{\text{I} t} G - \frac{1}{4} C1 d1^2 e^{2 \text{I} t} G - \frac{1}{4} \text{I} C2 d1^2 e^{2 \text{I} t} G - \frac{1}{2} \text{I} C1 d1 d2 e^{2 \text{I} t} G + \\
& \frac{1}{2} C2 d1 d2 e^{2 \text{I} t} G + \frac{1}{4} C1 d2^2 e^{2 \text{I} t} G + \frac{1}{4} \text{I} C2 d2^2 e^{2 \text{I} t} G - \frac{1}{2} \text{I} C1 d1^2 e^{\text{I} t} G t - \\
& \frac{1}{2} C2 d1^2 e^{\text{I} t} G t + C1 d1 d2 e^{\text{I} t} G t - \text{I} C2 d1 d2 e^{\text{I} t} G t + \frac{1}{2} \text{I} C1 d2^2 e^{\text{I} t} G t + \frac{1}{2} C2 d2^2 e^{\text{I} t} G t
\end{aligned}$$

In[*]:= **Simplify[%73]**

$$\begin{aligned}
Out[*]= & -\frac{1}{8} G \left(C1 \left(-d2^2 \left(3 + 2 e^{2 \text{I} t} + e^{\text{I} t} \left(-3 + 4 \text{I} t \right) \right) + \right. \right. \\
& \left. \left. 2 \text{I} d1 d2 \left(-1 + 2 e^{2 \text{I} t} + e^{\text{I} t} \left(-1 + 4 \text{I} t \right) \right) + d1^2 \left(-1 + 2 e^{2 \text{I} t} + e^{\text{I} t} \left(1 + 4 \text{I} t \right) \right) \right) + \right. \\
& \left. C2 \left(-\text{I} d2^2 \left(-1 + 2 e^{2 \text{I} t} + e^{\text{I} t} \left(-1 - 4 \text{I} t \right) \right) - 2 d1 d2 \left(-1 + 2 e^{2 \text{I} t} + e^{\text{I} t} \left(1 - 4 \text{I} t \right) \right) + \right. \right. \\
& \left. \left. d1^2 \left(3 \text{I} + 2 \text{I} e^{2 \text{I} t} + e^{\text{I} t} \left(3 \text{I} + 4 t \right) \right) \right) \right)
\end{aligned}$$

$$\begin{aligned}
In[*]:= & \frac{1}{8} C1 d1^2 G - \frac{3}{8} i C2 d1^2 G + \frac{1}{4} i C1 d1 d2 G - \frac{1}{4} C2 d1 d2 G + \frac{3}{8} C1 d2^2 G - \frac{1}{8} i C2 d2^2 G - \\
& \frac{1}{8} C1 d1^2 e^{i t} G - \frac{3}{8} i C2 d1^2 e^{i t} G + \frac{1}{4} i C1 d1 d2 e^{i t} G + \frac{1}{4} C2 d1 d2 e^{i t} G - \frac{3}{8} C1 d2^2 e^{i t} G - \\
& \frac{1}{8} i C2 d2^2 e^{i t} G - \frac{1}{4} C1 d1^2 e^{2 i t} G - \frac{1}{4} i C2 d1^2 e^{2 i t} G - \frac{1}{2} i C1 d1 d2 e^{2 i t} G + \\
& \frac{1}{2} C2 d1 d2 e^{2 i t} G + \frac{1}{4} C1 d2^2 e^{2 i t} G + \frac{1}{4} i C2 d2^2 e^{2 i t} G - \frac{1}{2} i C1 d1^2 e^{i t} G t - \\
& \frac{1}{2} C2 d1^2 e^{i t} G t + C1 d1 d2 e^{i t} G t - i C2 d1 d2 e^{i t} G t + \frac{1}{2} i C1 d2^2 e^{i t} G t + \frac{1}{2} C2 d2^2 e^{i t} G t \\
Out[*]= & \frac{1}{8} C1 d1^2 G - \frac{3}{8} i C2 d1^2 G + \frac{1}{4} i C1 d1 d2 G - \frac{1}{4} C2 d1 d2 G + \frac{3}{8} C1 d2^2 G - \frac{1}{8} i C2 d2^2 G - \\
& \frac{1}{8} C1 d1^2 e^{i t} G - \frac{3}{8} i C2 d1^2 e^{i t} G + \frac{1}{4} i C1 d1 d2 e^{i t} G + \frac{1}{4} C2 d1 d2 e^{i t} G - \frac{3}{8} C1 d2^2 e^{i t} G - \\
& \frac{1}{8} i C2 d2^2 e^{i t} G - \frac{1}{4} C1 d1^2 e^{2 i t} G - \frac{1}{4} i C2 d1^2 e^{2 i t} G - \frac{1}{2} i C1 d1 d2 e^{2 i t} G + \\
& \frac{1}{2} C2 d1 d2 e^{2 i t} G + \frac{1}{4} C1 d2^2 e^{2 i t} G + \frac{1}{4} i C2 d2^2 e^{2 i t} G - \frac{1}{2} i C1 d1^2 e^{i t} G t - \\
& \frac{1}{2} C2 d1^2 e^{i t} G t + C1 d1 d2 e^{i t} G t - i C2 d1 d2 e^{i t} G t + \frac{1}{2} i C1 d2^2 e^{i t} G t + \frac{1}{2} C2 d2^2 e^{i t} G t
\end{aligned}$$

In[*]:= Collect[%, t * Exp[I * t]]

$$\begin{aligned}
Out[*]= & \frac{1}{8} C1 d1^2 G - \frac{3}{8} i C2 d1^2 G + \frac{1}{4} i C1 d1 d2 G - \frac{1}{4} C2 d1 d2 G + \frac{3}{8} C1 d2^2 G - \frac{1}{8} i C2 d2^2 G - \\
& \frac{1}{8} C1 d1^2 e^{i t} G - \frac{3}{8} i C2 d1^2 e^{i t} G + \frac{1}{4} i C1 d1 d2 e^{i t} G + \frac{1}{4} C2 d1 d2 e^{i t} G - \\
& \frac{3}{8} C1 d2^2 e^{i t} G - \frac{1}{8} i C2 d2^2 e^{i t} G - \frac{1}{4} C1 d1^2 e^{2 i t} G - \frac{1}{4} i C2 d1^2 e^{2 i t} G - \\
& \frac{1}{2} i C1 d1 d2 e^{2 i t} G + \frac{1}{2} C2 d1 d2 e^{2 i t} G + \frac{1}{4} C1 d2^2 e^{2 i t} G + \frac{1}{4} i C2 d2^2 e^{2 i t} G + \\
& e^{i t} \left(-\frac{1}{2} i C1 d1^2 G - \frac{1}{2} C2 d1^2 G + C1 d1 d2 G - i C2 d1 d2 G + \frac{1}{2} i C1 d2^2 G + \frac{1}{2} C2 d2^2 G \right) t
\end{aligned}$$

$$In[*]:= -\frac{1}{2} i C1 d1^2 G - \frac{1}{2} C2 d1^2 G + C1 d1 d2 G - i C2 d1 d2 G + \frac{1}{2} i C1 d2^2 G + \frac{1}{2} C2 d2^2 G$$

$$Out[*]= -\frac{1}{2} i C1 d1^2 G - \frac{1}{2} C2 d1^2 G + C1 d1 d2 G - i C2 d1 d2 G + \frac{1}{2} i C1 d2^2 G + \frac{1}{2} C2 d2^2 G$$