

$$\text{In}[]:= \mathbf{z2} := \mathbf{a} * \text{Exp}[-\mathbf{I} * \mathbf{c1} * \mathbf{t}] + \mathbf{b}$$

$$\text{In}[]:= \mathbf{z3} := \mathbf{r} * \text{Exp}[-\mathbf{I} * \mathbf{c1} * \mathbf{t}] + \mathbf{g}$$

$$\text{In}[]:= \mathbf{z20} := \mathbf{A} * \text{Exp}[\mathbf{I} * \mathbf{c1} * \mathbf{t}] + \mathbf{B}$$

$$\text{In}[]:= \mathbf{z30} := \mathbf{R} * \text{Exp}[\mathbf{I} * \mathbf{c1} * \mathbf{t}] + \mathbf{G}$$

$$\text{In}[]:= \mathbf{z3}$$

$$\text{Out}[]:= \mathbf{g} + e^{-i c1 t} \mathbf{r}$$

$$\text{In}[]:= \mathbf{pz2} := \mathbf{k1} * \text{Exp}[-\mathbf{I} * \mathbf{c1} * \mathbf{t} / 2] + \mathbf{I} * \mathbf{a} * \mathbf{c1} * \text{Exp}[-\mathbf{I} * \mathbf{c1} * \mathbf{t}] + \mathbf{I} * \mathbf{b} * \mathbf{c1}$$

$$\text{In}[]:= \mathbf{pz3} := \mathbf{k2} * \text{Exp}[-\mathbf{I} * \mathbf{c1} * \mathbf{t} / 2] + \mathbf{I} * \mathbf{r} * \mathbf{c1} * \text{Exp}[-\mathbf{I} * \mathbf{c1} * \mathbf{t}] + \mathbf{I} * \mathbf{g} * \mathbf{c1}$$

$$\text{In}[]:= \mathbf{Pz2} := \mathbf{K1} * \text{Exp}[\mathbf{I} * \mathbf{c1} * \mathbf{t} / 2] - \mathbf{I} * \mathbf{A} * \mathbf{c1} * \text{Exp}[\mathbf{I} * \mathbf{c1} * \mathbf{t}] - \mathbf{I} * \mathbf{B} * \mathbf{c1}$$

$$\text{In}[]:= \mathbf{Pz3} := \mathbf{K2} * \text{Exp}[\mathbf{I} * \mathbf{c1} * \mathbf{t} / 2] - \mathbf{I} * \mathbf{R} * \mathbf{c1} * \text{Exp}[\mathbf{I} * \mathbf{c1} * \mathbf{t}] - \mathbf{I} * \mathbf{G} * \mathbf{c1}$$

$$\text{In}[]:= \mathbf{deqn} := 2 * \mathbf{c0} - (\mathbf{c1} / 2) * (\mathbf{z2} * \mathbf{z20} + \mathbf{z3} * \mathbf{z30}) - (\mathbf{I} / 4) * (\mathbf{z2} * \mathbf{Pz2}) + (\mathbf{I} / 4) * (\mathbf{z20} * \mathbf{pz2}) - (\mathbf{I} / 4) * (\mathbf{z3} * \mathbf{Pz3}) + (\mathbf{I} / 4) * (\mathbf{z30} * \mathbf{pz3})$$

$$\text{In}[]:= \mathbf{DSolve}[\mathbf{y}'[\mathbf{t}] == \mathbf{deqn}, \mathbf{y}[\mathbf{t}], \mathbf{t}]$$

$$\text{Out}[]:= \left\{ \left\{ \mathbf{y}[\mathbf{t}] \rightarrow -i e^{-i c1 t} (\mathbf{a} \mathbf{B} + \mathbf{G} \mathbf{r}) - \frac{e^{-\frac{1}{2} i c1 t} (\mathbf{B} \mathbf{k1} - \mathbf{a} \mathbf{K1} + \mathbf{G} \mathbf{k2} - \mathbf{K2} \mathbf{r})}{2 c1} + i e^{i c1 t} (\mathbf{A} \mathbf{b} + \mathbf{g} \mathbf{R}) + \frac{e^{\frac{i c1 t}{2}} (\mathbf{A} \mathbf{k1} - \mathbf{b} \mathbf{K1} - \mathbf{g} \mathbf{K2} + \mathbf{k2} \mathbf{R})}{2 c1} + 2 c0 t - c1 (\mathbf{a} \mathbf{A} + \mathbf{b} \mathbf{B} + \mathbf{g} \mathbf{G} + \mathbf{r} \mathbf{R}) t + \mathbf{C}[1] \right\} \right\}$$

$$\text{In}[]:= \mathbf{y1} := -i e^{-i c1 t} (\mathbf{a} \mathbf{B} + \mathbf{G} \mathbf{r}) - \frac{1}{2 c1} e^{-\frac{1}{2} i c1 t} (\mathbf{B} \mathbf{k1} - \mathbf{a} \mathbf{K1} + \mathbf{G} \mathbf{k2} - \mathbf{K2} \mathbf{r}) + i e^{i c1 t} (\mathbf{A} \mathbf{b} + \mathbf{g} \mathbf{R}) + \frac{e^{\frac{i c1 t}{2}} (\mathbf{A} \mathbf{k1} - \mathbf{b} \mathbf{K1} - \mathbf{g} \mathbf{K2} + \mathbf{k2} \mathbf{R})}{2 c1} + 2 c0 t - c1 (\mathbf{a} \mathbf{A} + \mathbf{b} \mathbf{B} + \mathbf{g} \mathbf{G} + \mathbf{r} \mathbf{R}) t + \text{constant}$$

$$\text{In}[]:= \mathbf{y1}$$

$$\text{Out}[]:= \text{constant} - i e^{-i c1 t} (\mathbf{a} \mathbf{B} + \mathbf{G} \mathbf{r}) - \frac{e^{-\frac{1}{2} i c1 t} (\mathbf{B} \mathbf{k1} - \mathbf{a} \mathbf{K1} + \mathbf{G} \mathbf{k2} - \mathbf{K2} \mathbf{r})}{2 c1} + i e^{i c1 t} (\mathbf{A} \mathbf{b} + \mathbf{g} \mathbf{R}) + \frac{e^{\frac{i c1 t}{2}} (\mathbf{A} \mathbf{k1} - \mathbf{b} \mathbf{K1} - \mathbf{g} \mathbf{K2} + \mathbf{k2} \mathbf{R})}{2 c1} + 2 c0 t - c1 (\mathbf{a} \mathbf{A} + \mathbf{b} \mathbf{B} + \mathbf{g} \mathbf{G} + \mathbf{r} \mathbf{R}) t$$

$$\text{In}[6]:= \text{Expand}\left[\text{constant} - i e^{-i c_1 t} (a B + G r) - \frac{1}{2 c_1} e^{-\frac{1}{2} i c_1 t} (B k_1 - a K_1 + G k_2 - K_2 r) + \right. \\ \left. i e^{i c_1 t} (A b + g R) + \frac{e^{\frac{i c_1 t}{2}} (A k_1 - b K_1 - g K_2 + k_2 R)}{2 c_1} + 2 c_0 t - c_1 (a A + b B + g G + r R) t\right]$$

$$\text{Out}[6]= \text{constant} - i a B e^{-i c_1 t} + i A b e^{i c_1 t} - \frac{B e^{-\frac{1}{2} i c_1 t} k_1}{2 c_1} + \frac{A e^{\frac{i c_1 t}{2}} k_1}{2 c_1} + \\ \frac{a e^{-\frac{1}{2} i c_1 t} K_1}{2 c_1} - \frac{b e^{\frac{i c_1 t}{2}} K_1}{2 c_1} - \frac{e^{-\frac{1}{2} i c_1 t} G k_2}{2 c_1} - \frac{e^{\frac{i c_1 t}{2}} g K_2}{2 c_1} - i e^{-i c_1 t} G r + \frac{e^{-\frac{1}{2} i c_1 t} K_2 r}{2 c_1} + \\ i e^{i c_1 t} g R + \frac{e^{\frac{i c_1 t}{2}} k_2 R}{2 c_1} + 2 c_0 t - a A c_1 t - b B c_1 t - c_1 g G t - c_1 r R t$$

$$\text{In}[7]:= y1 := \text{constant} - i a B e^{-i c_1 t} + i A b e^{i c_1 t} - \frac{B e^{-\frac{1}{2} i c_1 t} k_1}{2 c_1} + \frac{A e^{\frac{i c_1 t}{2}} k_1}{2 c_1} + \\ \frac{a e^{-\frac{1}{2} i c_1 t} K_1}{2 c_1} - \frac{b e^{\frac{i c_1 t}{2}} K_1}{2 c_1} - \frac{e^{-\frac{1}{2} i c_1 t} G k_2}{2 c_1} - \frac{e^{\frac{i c_1 t}{2}} g K_2}{2 c_1} - i e^{-i c_1 t} G r + \frac{e^{-\frac{1}{2} i c_1 t} K_2 r}{2 c_1} + \\ i e^{i c_1 t} g R + \frac{e^{\frac{i c_1 t}{2}} k_2 R}{2 c_1} + 2 c_0 t - a A c_1 t - b B c_1 t - c_1 g G t - c_1 r R t$$

$$\text{In}[8]:= y1$$

$$\text{Out}[8]= \text{constant} - i a B e^{-i c_1 t} + i A b e^{i c_1 t} - \frac{B e^{-\frac{1}{2} i c_1 t} k_1}{2 c_1} + \frac{A e^{\frac{i c_1 t}{2}} k_1}{2 c_1} + \\ \frac{a e^{-\frac{1}{2} i c_1 t} K_1}{2 c_1} - \frac{b e^{\frac{i c_1 t}{2}} K_1}{2 c_1} - \frac{e^{-\frac{1}{2} i c_1 t} G k_2}{2 c_1} - \frac{e^{\frac{i c_1 t}{2}} g K_2}{2 c_1} - i e^{-i c_1 t} G r + \frac{e^{-\frac{1}{2} i c_1 t} K_2 r}{2 c_1} + \\ i e^{i c_1 t} g R + \frac{e^{\frac{i c_1 t}{2}} k_2 R}{2 c_1} + 2 c_0 t - a A c_1 t - b B c_1 t - c_1 g G t - c_1 r R t$$