

```
In[*]:= ρ := z1 + Z1 - z2 * Z2 - z3 * Z3 - g * z2^2 * Z3^2 - G * z3^2 * Z2^2
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In[*]:= ρ
```

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Out[*]:= z1 + Z1 - z2 Z2 - G Z2^2 z3^2 - z3 Z3 - g z2^2 Z3^2
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In[*]:= ρ2 := D[ρ, z2]
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In[*]:= ρ20 := D[ρ, Z2]
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In[*]:= ρ3 := D[ρ, z3]
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In[*]:= ρ30 := D[ρ, Z3]
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In[*]:= ρ22 := D[ρ, z2, Z2]
```

```
In[*]:= ρ22
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```
Out[*]:= -1
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In[*]:= ρ23 := D[ρ, z2, Z3]
```

```
In[*]:= ρ23
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```
Out[*]:= -4 g z2 Z3
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In[*]:= ρ33 := D[ρ, z3, Z3]
```

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In[*]:= ρ32 := D[ρ, z3, Z2]
```

```
In[*]:= A := {{0, I, I * ρ20, I * ρ30}, {-I, 0, 0, 0},
               {-I * ρ2, 0, 4 * ρ22, 4 * ρ23}, {-I * ρ3, 0, 4 * ρ32, 4 * ρ33}}
```

```
In[*]:= MatrixForm[A]
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```
Out[*]//MatrixForm=
```

$$\begin{pmatrix} 0 & i & i(-z2 - 2G Z2 z3^2) & i(-z3 - 2g z2^2 Z3) \\ -i & 0 & 0 & 0 \\ -i(-Z2 - 2g z2 Z3^2) & 0 & -4 & -16g z2 Z3 \\ -i(-2G Z2^2 z3 - Z3) & 0 & -16G Z2 z3 & -4 \end{pmatrix}$$

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In[*]:= B := Inverse[A]
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In[*]:= MatrixForm[B]
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Out[*]//MatrixForm=
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$$\begin{pmatrix} 0 & \frac{-16i+256igGz2Z2z3Z3}{-16+256gGz2Z2z3Z3} & \frac{16i-256igGZ2Z2z3Z3}{-16+256gGz2Z2z3Z3} & \frac{4z2Z2+4z3Z3-48gGz2^2Z2^2z3Z3-64g^2Z2Z2^3z3^3Z3-48gGz2Z2z3^2Z3^2-64g^2Gz2^3Z2z3Z3^3}{-16+256gGz2Z2z3Z3} & \frac{4z2-16i+256igGz2Z2z3Z3}{-16+256gGz2Z2z3Z3} \\ \frac{16i-256igGZ2Z2z3Z3}{-16+256gGz2Z2z3Z3} & \frac{4z2Z2+4z3Z3-48gGz2^2Z2^2z3Z3-64g^2Z2Z2^3z3^3Z3-48gGz2Z2z3^2Z3^2-64g^2Gz2^3Z2z3Z3^3}{-16+256gGz2Z2z3Z3} & \frac{4Z2-32gGz2Z2^2z3Z3-8gZ2Z3^2}{-16+256gGz2Z2z3Z3} & \frac{-8GZ2^2z3+4Z3-32gGz2Z2z3Z3^2}{-16+256gGz2Z2z3Z3} & - \\ 0 & \frac{4Z2-32gGz2Z2^2z3Z3-8gZ2Z3^2}{-16+256gGz2Z2z3Z3} & \frac{-8GZ2^2z3+4Z3-32gGz2Z2z3Z3^2}{-16+256gGz2Z2z3Z3} & - \\ 0 & \frac{-8GZ2^2z3+4Z3-32gGz2Z2z3Z3^2}{-16+256gGz2Z2z3Z3} & - & - \end{pmatrix}$$

```
In[*]:= L := {{0, I, 0, 0},
               {-I, -(z2 * Z2 + z3 * Z3) / 4, -(z2 - 2 * G * Z2 * z3^2) / 4, -(z3 - 2 * g * z2^2 * Z3) / 4},
               {0, -(Z2 - 2 * g * z2 * Z3^2) / 4, -1 / 4, g * z2 * Z3},
               {0, -(Z3 - 2 * G * Z2^2 * z3) / 4, G * Z2 * z3, -1 / 4}}
```

In[]:= **MatrixForm[L]**

Out[]:= **MatrixForm=**

$$\begin{pmatrix} 0 & i & 0 & 0 \\ -i & \frac{1}{4}(-z^2 Z^2 - z^3 Z^3) & \frac{1}{4}(-z^2 + 2 G Z^2 z^3) & \frac{1}{4}(-z^3 + 2 g z^2 Z^3) \\ 0 & \frac{1}{4}(-Z^2 + 2 g z^2 Z^3) & -\frac{1}{4} & g z^2 Z^3 \\ 0 & \frac{1}{4}(2 G Z^2 z^3 - Z^3) & G Z^2 z^3 & -\frac{1}{4} \end{pmatrix}$$

In[]:= **q := {p0, I * p1, p2, p3}**

In[]:= **Q := {p0, -I * p1, P2, P3}**

In[]:= **q.L.Q**

$$\begin{aligned} \text{Out[]}= & p_0 p_1 + P_2 \left(-\frac{p_2}{4} + G p_3 Z^2 z^3 + \frac{1}{4} i p_1 (-z^2 + 2 G Z^2 z^3) \right) + \\ & P_3 \left(-\frac{p_3}{4} + g p_2 z^2 Z^3 + \frac{1}{4} i p_1 (-z^3 + 2 g z^2 Z^3) \right) - \\ & i p_1 \left(i p_0 + \frac{1}{4} p_3 (2 G Z^2 z^3 - Z^3) + \frac{1}{4} i p_1 (-z^2 Z^2 - z^3 Z^3) + \frac{1}{4} p_2 (-Z^2 + 2 g z^2 Z^3) \right) \end{aligned}$$

$$\begin{aligned} \text{In[]}= & \text{Simplify} \left[p_0 p_1 + P_2 \left(-\frac{p_2}{4} + G p_3 Z^2 z^3 + \frac{1}{4} i p_1 (-z^2 + 2 G Z^2 z^3) \right) + \right. \\ & P_3 \left(-\frac{p_3}{4} + g p_2 z^2 Z^3 + \frac{1}{4} i p_1 (-z^3 + 2 g z^2 Z^3) \right) - \\ & \left. i p_1 \left(i p_0 + \frac{1}{4} p_3 (2 G Z^2 z^3 - Z^3) + \frac{1}{4} i p_1 (-z^2 Z^2 - z^3 Z^3) + \frac{1}{4} p_2 (-Z^2 + 2 g z^2 Z^3) \right) \right] \end{aligned}$$

$$\begin{aligned} \text{Out[]}= & 2 p_0 p_1 - \frac{1}{4} i \left(p_3 (-i P_3 + 2 G Z^2 (2 i P_2 + p_1 Z^2) z^3 - p_1 Z^3) + \right. \\ & p_2 (-i P_2 - p_1 Z^2 + 4 i g P_3 z^2 Z^3 + 2 g p_1 z^2 Z^3) + \\ & \left. p_1 (P_2 (z^2 - 2 G Z^2 z^3) + P_3 (z^3 - 2 g z^2 Z^3) - i p_1 (z^2 Z^2 + z^3 Z^3)) \right) \end{aligned}$$

$$\begin{aligned} \text{In[]}= & \text{Expand} \left[2 p_0 p_1 - \frac{1}{4} i \left(p_3 (-i P_3 + 2 G Z^2 (2 i P_2 + p_1 Z^2) z^3 - p_1 Z^3) + \right. \right. \\ & p_2 (-i P_2 - p_1 Z^2 + 4 i g P_3 z^2 Z^3 + 2 g p_1 z^2 Z^3) + \\ & \left. \left. p_1 (P_2 (z^2 - 2 G Z^2 z^3) + P_3 (z^3 - 2 g z^2 Z^3) - i p_1 (z^2 Z^2 + z^3 Z^3)) \right) \right] \end{aligned}$$

$$\begin{aligned} \text{Out[]}= & 2 p_0 p_1 - \frac{p_2 P_2}{4} - \frac{p_3 P_3}{4} - \frac{1}{4} i p_1 P_2 z^2 + \frac{1}{4} i p_1 p_2 Z^2 - \frac{1}{4} p_1^2 z^2 Z^2 - \\ & \frac{1}{4} i p_1 P_3 z^3 + G P_2 p_3 Z^2 z^3 - \frac{1}{2} i G p_1 p_3 Z^2 z^3 + \frac{1}{2} i G p_1 P_2 Z^2 z^3 + \\ & \frac{1}{4} i p_1 p_3 Z^3 + g p_2 P_3 z^2 Z^3 + \frac{1}{2} i g p_1 P_3 z^2 Z^3 - \frac{1}{4} p_1^2 z^3 Z^3 - \frac{1}{2} i g p_1 p_2 z^2 Z^3 \end{aligned}$$

$$\begin{aligned} \text{In[]}= & \text{H} := 2 p_0 p_1 - \frac{p_2 P_2}{4} - \frac{p_3 P_3}{4} - \frac{1}{4} i p_1 P_2 z^2 + \frac{1}{4} i p_1 p_2 Z^2 - \frac{1}{4} p_1^2 z^2 Z^2 - \\ & \frac{1}{4} i p_1 P_3 z^3 + G P_2 p_3 Z^2 z^3 - \frac{1}{2} i G p_1 p_3 Z^2 z^3 + \frac{1}{2} i G p_1 P_2 Z^2 z^3 + \\ & \frac{1}{4} i p_1 p_3 Z^3 + g p_2 P_3 z^2 Z^3 + \frac{1}{2} i g p_1 P_3 z^2 Z^3 - \frac{1}{4} p_1^2 z^3 Z^3 - \frac{1}{2} i g p_1 p_2 z^2 Z^3 \end{aligned}$$

In[]:= **Collect**[H, p1 * P2]

$$\begin{aligned} \text{Out[]}= & 2 p_0 p_1 - \frac{p_2 P_2}{4} - \frac{p_3 P_3}{4} + \frac{1}{4} i p_1 p_2 Z_2 - \frac{1}{4} p_1^2 z_2 Z_2 - \frac{1}{4} i p_1 P_3 z_3 + \\ & G P_2 p_3 Z_2 z_3 - \frac{1}{2} i G p_1 p_3 Z_2^2 z_3 + p_1 P_2 \left(-\frac{i z_2}{4} + \frac{1}{2} i G Z_2 z_3^2 \right) + \frac{1}{4} i p_1 p_3 Z_3 + \\ & g p_2 P_3 z_2 Z_3 + \frac{1}{2} i g p_1 P_3 z_2^2 Z_3 - \frac{1}{4} p_1^2 z_3 Z_3 - \frac{1}{2} i g p_1 p_2 z_2 Z_3^2 \end{aligned}$$

In[]:= **H**

In[]:= **ClearAll**[H]

$$\begin{aligned} \text{In[]:= } H := & 2 p_0 p_1 - \frac{p_2 P_2}{4} - \frac{p_3 P_3}{4} - \frac{1}{4} i p_1 P_2 z_2 + \frac{1}{4} i p_1 p_2 Z_2 - \frac{1}{4} p_1^2 z_2 Z_2 - \\ & \frac{1}{4} i p_1 P_3 z_3 + G P_2 p_3 Z_2 z_3 - \frac{1}{2} i G p_1 p_3 Z_2^2 z_3 + \frac{1}{2} i G p_1 P_2 Z_2 z_3^2 + \\ & \frac{1}{4} i p_1 p_3 Z_3 + g p_2 P_3 z_2 Z_3 + \frac{1}{2} i g p_1 P_3 z_2^2 Z_3 - \frac{1}{4} p_1^2 z_3 Z_3 - \frac{1}{2} i g p_1 p_2 z_2 Z_3^2 \end{aligned}$$

In[]:= **H**

$$\begin{aligned} \text{Out[]}= & 2 p_0 p_1 - \frac{p_2 P_2}{4} - \frac{p_3 P_3}{4} - \frac{1}{4} i p_1 P_2 z_2 + \frac{1}{4} i p_1 p_2 Z_2 - \frac{1}{4} p_1^2 z_2 Z_2 - \\ & \frac{1}{4} i p_1 P_3 z_3 + G P_2 p_3 Z_2 z_3 - \frac{1}{2} i G p_1 p_3 Z_2^2 z_3 + \frac{1}{2} i G p_1 P_2 Z_2 z_3^2 + \\ & \frac{1}{2} i G p_1 P_3 Z_2 z_3^2 + \frac{1}{4} i p_1 p_3 Z_3 + g p_2 P_3 z_2 Z_3 - \frac{1}{4} p_1^2 z_3 Z_3 - \frac{1}{2} i g p_1 p_2 z_2 Z_3^2 \end{aligned}$$

In[]:= **Collect**[H, p1 * P2]

$$\begin{aligned} \text{Out[]}= & 2 p_0 p_1 - \frac{p_2 P_2}{4} - \frac{p_3 P_3}{4} + \frac{1}{4} i p_1 p_2 Z_2 - \frac{1}{4} p_1^2 z_2 Z_2 - \frac{1}{4} i p_1 P_3 z_3 + \\ & G P_2 p_3 Z_2 z_3 - \frac{1}{2} i G p_1 p_3 Z_2^2 z_3 + p_1 P_2 \left(-\frac{i z_2}{4} + \frac{1}{2} i G Z_2 z_3^2 \right) + \frac{1}{4} i p_1 p_3 Z_3 + \\ & g p_2 P_3 z_2 Z_3 + \frac{1}{2} i g p_1 P_3 z_2^2 Z_3 - \frac{1}{4} p_1^2 z_3 Z_3 - \frac{1}{2} i g p_1 p_2 z_2 Z_3^2 \end{aligned}$$

In[]:= **Collect**[H, p1 * P3]

$$\begin{aligned} \text{Out[]}= & 2 p_0 p_1 - \frac{p_2 P_2}{4} - \frac{p_3 P_3}{4} - \frac{1}{4} i p_1 P_2 z_2 + \frac{1}{4} i p_1 p_2 Z_2 - \frac{1}{4} p_1^2 z_2 Z_2 + \\ & G P_2 p_3 Z_2 z_3 - \frac{1}{2} i G p_1 p_3 Z_2^2 z_3 + \frac{1}{2} i G p_1 P_2 Z_2 z_3^2 + \frac{1}{4} i p_1 p_3 Z_3 + \\ & g p_2 P_3 z_2 Z_3 - \frac{1}{4} p_1^2 z_3 Z_3 - \frac{1}{2} i g p_1 p_2 z_2 Z_3^2 + p_1 P_3 \left(-\frac{i z_3}{4} + \frac{1}{2} i g z_2^2 Z_3 \right) \end{aligned}$$

In[]:= **Collect[H, p2 * P2]**

$$\begin{aligned} \text{Out[]}= & 2 p_0 p_1 - \frac{p_2^2 P_2}{4} - \frac{p_3 P_3}{4} - \frac{1}{4} i p_1 P_2 z_2 + \frac{1}{4} i p_1 p_2 Z_2 - \frac{1}{4} p_1^2 z_2 Z_2 - \\ & \frac{1}{4} i p_1 P_3 z_3 + G P_2 p_3 Z_2 z_3 - \frac{1}{2} i G p_1 p_3 Z_2^2 z_3 + \frac{1}{2} i G p_1 P_2 Z_2 z_3^2 + \\ & \frac{1}{4} i p_1 p_3 Z_3 + g p_2 P_3 z_2 Z_3 + \frac{1}{2} i g p_1 P_3 z_2^2 Z_3 - \frac{1}{4} p_1^2 z_3 Z_3 - \frac{1}{2} i g p_1 p_2 z_2 Z_3^2 \end{aligned}$$

In[]:= **Collect[H, p2 * P3]**

$$\begin{aligned} \text{Out[]}= & 2 p_0 p_1 - \frac{p_2^2 P_2}{4} - \frac{p_3 P_3}{4} - \frac{1}{4} i p_1 P_2 z_2 + \frac{1}{4} i p_1 p_2 Z_2 - \frac{1}{4} p_1^2 z_2 Z_2 - \\ & \frac{1}{4} i p_1 P_3 z_3 + G P_2 p_3 Z_2 z_3 - \frac{1}{2} i G p_1 p_3 Z_2^2 z_3 + \frac{1}{2} i G p_1 P_2 Z_2 z_3^2 + \\ & \frac{1}{4} i p_1 p_3 Z_3 + g p_2 P_3 z_2 Z_3 + \frac{1}{2} i g p_1 P_3 z_2^2 Z_3 - \frac{1}{4} p_1^2 z_3 Z_3 - \frac{1}{2} i g p_1 p_2 z_2 Z_3^2 \end{aligned}$$

In[]:= **Collect[H, p1 * p2]**

$$\begin{aligned} \text{Out[]}= & 2 p_0 p_1 - \frac{p_2^2 P_2}{4} - \frac{p_3 P_3}{4} - \frac{1}{4} i p_1 P_2 z_2 - \frac{1}{4} p_1^2 z_2 Z_2 - \frac{1}{4} i p_1 P_3 z_3 + \\ & G P_2 p_3 Z_2 z_3 - \frac{1}{2} i G p_1 p_3 Z_2^2 z_3 + \frac{1}{2} i G p_1 P_2 Z_2 z_3^2 + \frac{1}{4} i p_1 p_3 Z_3 + \\ & g p_2 P_3 z_2 Z_3 + \frac{1}{2} i g p_1 P_3 z_2^2 Z_3 - \frac{1}{4} p_1^2 z_3 Z_3 + p_1 p_2 \left(\frac{i Z_2}{4} - \frac{1}{2} i g z_2 Z_3^2 \right) \end{aligned}$$

In[]:= **Collect[H, p1 * p3]**

$$\begin{aligned} \text{Out[]}= & 2 p_0 p_1 - \frac{p_2^2 P_2}{4} - \frac{p_3 P_3}{4} - \frac{1}{4} i p_1 P_2 z_2 + \frac{1}{4} i p_1 p_2 Z_2 - \frac{1}{4} p_1^2 z_2 Z_2 - \\ & \frac{1}{4} i p_1 P_3 z_3 + G P_2 p_3 Z_2 z_3 + \frac{1}{2} i G p_1 P_2 Z_2 z_3^2 + p_1 p_3 \left(-\frac{1}{2} i G Z_2^2 z_3 + \frac{i Z_3}{4} \right) + \\ & g p_2 P_3 z_2 Z_3 + \frac{1}{2} i g p_1 P_3 z_2^2 Z_3 - \frac{1}{4} p_1^2 z_3 Z_3 - \frac{1}{2} i g p_1 p_2 z_2 Z_3^2 \end{aligned}$$

In[]:= **Collect[H, P2 * p3]**

$$\begin{aligned} \text{Out[]}= & 2 p_0 p_1 - \frac{p_2^2 P_2}{4} - \frac{p_3 P_3}{4} - \frac{1}{4} i p_1 P_2 z_2 + \frac{1}{4} i p_1 p_2 Z_2 - \frac{1}{4} p_1^2 z_2 Z_2 - \\ & \frac{1}{4} i p_1 P_3 z_3 + G P_2 p_3 Z_2 z_3 - \frac{1}{2} i G p_1 p_3 Z_2^2 z_3 + \frac{1}{2} i G p_1 P_2 Z_2 z_3^2 + \\ & \frac{1}{4} i p_1 p_3 Z_3 + g p_2 P_3 z_2 Z_3 + \frac{1}{2} i g p_1 P_3 z_2^2 Z_3 - \frac{1}{4} p_1^2 z_3 Z_3 - \frac{1}{2} i g p_1 p_2 z_2 Z_3^2 \end{aligned}$$

In[]:= **dz2 := 2 * D[H, P2]**

In[]:= **dz2**

$$\text{Out[]}= 2 \left(-\frac{p_2}{4} - \frac{i p_1 z_2}{4} + G p_3 Z_2 z_3 + \frac{1}{2} i G p_1 Z_2 z_3^2 \right)$$

$$\text{In}[*]:= \text{Expand}\left[2\left(-\frac{p2}{4}-\frac{i p1 z2}{4}+G p3 Z2 z3+\frac{1}{2} i G p1 Z2 z3^2\right)\right]$$

$$\text{Out}[*]= -\frac{p2}{2}-\frac{i p1 z2}{2}+2 G p3 Z2 z3+i G p1 Z2 z3^2$$

$$\text{In}[*]:= \text{Collect}[\%, p1]$$

$$\text{Out}[*]= -\frac{p2}{2}+2 G p3 Z2 z3+p1\left(-\frac{i z2}{2}+i G Z2 z3^2\right)$$

$$\text{In}[*]:= \text{dp2} := -2 * D[H, Z2]$$

$$\text{In}[*]:= \text{dp2}$$

$$\text{Out}[*]= -2\left(\frac{i p1 p2}{4}-\frac{p1^2 z2}{4}+G P2 p3 z3-i G p1 p3 Z2 z3+\frac{1}{2} i G p1 P2 z3^2\right)$$

$$\text{In}[*]:= \text{Expand}\left[-2\left(\frac{i p1 p2}{4}-\frac{p1^2 z2}{4}+G P2 p3 z3-i G p1 p3 Z2 z3+\frac{1}{2} i G p1 P2 z3^2\right)\right]$$

$$\text{Out}[*]= -\frac{1}{2} i p1 p2+\frac{p1^2 z2}{2}-2 G P2 p3 z3+2 i G p1 p3 Z2 z3-i G p1 P2 z3^2$$

$$\text{In}[*]:= \text{dz3} := 2 * D[H, P3]$$

$$\text{In}[*]:= \text{dz3}$$

$$\text{Out}[*]= 2\left(-\frac{p3}{4}-\frac{i p1 z3}{4}+g p2 z2 Z3+\frac{1}{2} i g p1 z2^2 Z3\right)$$

$$\text{In}[*]:= \text{Expand}\left[2\left(-\frac{p3}{4}-\frac{i p1 z3}{4}+g p2 z2 Z3+\frac{1}{2} i g p1 z2^2 Z3\right)\right]$$

$$\text{Out}[*]= -\frac{p3}{2}-\frac{i p1 z3}{2}+2 g p2 z2 Z3+i g p1 z2^2 Z3$$

$$\text{In}[*]:= \text{Collect}[\%, p1]$$

$$\text{Out}[*]= -\frac{p3}{2}+2 g p2 z2 Z3+p1\left(-\frac{i z3}{2}+i g z2^2 Z3\right)$$

$$\text{In}[*]:= \text{dp3} := -2 * D[H, Z3]$$

$$\text{In}[*]:= \text{dp3}$$

$$\text{Out}[*]= -2\left(\frac{i p1 p3}{4}+g p2 P3 z2+\frac{1}{2} i g p1 P3 z2^2-\frac{p1^2 z3}{4}-i g p1 p2 z2 Z3\right)$$

$$\text{In}[*]:= \text{Expand}\left[-2\left(\frac{i p1 p3}{4}+g p2 P3 z2+\frac{1}{2} i g p1 P3 z2^2-\frac{p1^2 z3}{4}-i g p1 p2 z2 Z3\right)\right]$$

$$\text{Out}[*]= -\frac{1}{2} i p1 p3-2 g p2 P3 z2-i g p1 P3 z2^2+\frac{p1^2 z3}{2}+2 i g p1 p2 z2 Z3$$

$$\text{In}[*]:= \text{z2st} := s * \text{Exp}[I * t] + s^3 * v2$$

In[]:= **z2st**

Out[]:= $e^{i t} s + s^3 v2$

In[]:= **p2st := s * w21 + s^3 * w23**

In[]:= **p2st**

Out[]:= $s w21 + s^3 w23$

In[]:= **p1 := -1**

In[]:= **H**

Out[]:=
$$-2 p0 - \frac{p2 P2}{4} - \frac{p3 P3}{4} + \frac{i P2 z2}{4} - \frac{i p2 Z2}{4} - \frac{z2 Z2}{4} + \frac{i P3 z3}{4} + G P2 p3 Z2 z3 + \frac{1}{2} i G p3 Z2^2 z3 - \frac{1}{2} i G P2 Z2 z3^2 - \frac{i p3 Z3}{4} + g p2 P3 z2 Z3 - \frac{1}{2} i g P3 z2^2 Z3 - \frac{z3 Z3}{4} + \frac{1}{2} i g p2 z2 Z3^2$$

In[]:= **dz2 /. {z2 → z2st, Z2 → s * Exp[-I * t] + s^3 * V2, p2 → p2st, P2 → s * W21 + s^3 * W23}**

Out[]:=
$$2 \left(\frac{1}{4} i (e^{i t} s + s^3 v2) + \frac{1}{4} (-s w21 - s^3 w23) + G p3 (e^{-i t} s + s^3 V2) z3 - \frac{1}{2} i G (e^{-i t} s + s^3 V2) z3^2 \right)$$

In[]:= **Expand[2 (**
$$\frac{1}{4} i (e^{i t} s + s^3 v2) + \frac{1}{4} (-s w21 - s^3 w23) + G p3 (e^{-i t} s + s^3 V2) z3 - \frac{1}{2} i G (e^{-i t} s + s^3 V2) z3^2)$$
]

Out[]:=
$$\frac{1}{2} i e^{i t} s + \frac{1}{2} i s^3 v2 - \frac{s w21}{2} - \frac{s^3 w23}{2} + 2 e^{-i t} G p3 s z3 + 2 G p3 s^3 V2 z3 - i e^{-i t} G s z3^2 - i G s^3 V2 z3^2$$

In[]:= **Collect[%, s]**

Out[]:=
$$s \left(\frac{1}{2} i e^{i t} - \frac{w21}{2} + 2 e^{-i t} G p3 z3 - i e^{-i t} G z3^2 \right) + s^3 \left(\frac{i v2}{2} - \frac{w23}{2} + 2 G p3 V2 z3 - i G V2 z3^2 \right)$$

In[]:= **z3st := c * s + s^3 * v3**

In[]:= **p3st := s * w31 + s^3 * w33**

In[]:= **dz2 /. {z2 → z2st, Z2 → s * Exp[-I * t] + s^3 * V2, p2 → p2st, P2 → s * W21 + s^3 * W23, z3 → z3st, Z3 → k * s + s^3 * V3, p3 → p3st, P3 → s * W31 + s^3 * W33}**

Out[]:=
$$2 \left(\frac{1}{4} i (e^{i t} s + s^3 v2) - \frac{1}{2} i G (e^{-i t} s + s^3 V2) (c s + s^3 v3)^2 + \frac{1}{4} (-s w21 - s^3 w23) + G (e^{-i t} s + s^3 V2) (c s + s^3 v3) (s w31 + s^3 w33) \right)$$

$$\text{In}[*]:= \text{Expand}\left[2 \left(\frac{1}{4} \text{I} \left(\text{e}^{\text{I} t} s + s^3 v2\right) - \frac{1}{2} \text{I} G \left(\text{e}^{-\text{I} t} s + s^3 V2\right) \left(c s + s^3 v3\right)^2 + \frac{1}{4} \left(-s w21 - s^3 w23\right) + G \left(\text{e}^{-\text{I} t} s + s^3 V2\right) \left(c s + s^3 v3\right) \left(s w31 + s^3 w33\right)\right)\right]$$

$$\text{Out}[*]= \frac{1}{2} \text{I} \text{e}^{\text{I} t} s - \text{I} c^2 \text{e}^{-\text{I} t} G s^3 + \frac{1}{2} \text{I} s^3 v2 - \text{I} c^2 G s^5 V2 - 2 \text{I} c \text{e}^{-\text{I} t} G s^5 v3 - 2 \text{I} c G s^7 V2 v3 - \text{I} \text{e}^{-\text{I} t} G s^7 v3^2 - \text{I} G s^9 V2 v3^2 - \frac{s w21}{2} - \frac{s^3 w23}{2} + 2 c \text{e}^{-\text{I} t} G s^3 w31 + 2 c G s^5 V2 w31 + 2 \text{e}^{-\text{I} t} G s^5 v3 w31 + 2 G s^7 V2 v3 w31 + 2 c \text{e}^{-\text{I} t} G s^5 w33 + 2 c G s^7 V2 w33 + 2 \text{e}^{-\text{I} t} G s^7 v3 w33 + 2 G s^9 V2 v3 w33$$

$$\text{In}[*]:= \text{Collect}[\%, s]$$

$$\text{Out}[*]= s \left(\frac{1}{2} \text{I} \text{e}^{\text{I} t} - \frac{w21}{2}\right) + s^3 \left(-\text{I} c^2 \text{e}^{-\text{I} t} G + \frac{\text{I} v2}{2} - \frac{w23}{2} + 2 c \text{e}^{-\text{I} t} G w31\right) + s^5 \left(-\text{I} c^2 G V2 - 2 \text{I} c \text{e}^{-\text{I} t} G v3 + 2 c G V2 w31 + 2 \text{e}^{-\text{I} t} G v3 w31 + 2 c \text{e}^{-\text{I} t} G w33\right) + s^7 \left(-2 \text{I} c G V2 v3 - \text{I} \text{e}^{-\text{I} t} G v3^2 + 2 G V2 v3 w31 + 2 c G V2 w33 + 2 \text{e}^{-\text{I} t} G v3 w33\right) + s^9 \left(-\text{I} G V2 v3^2 + 2 G V2 v3 w33\right)$$

$$\text{In}[*]:= \text{dp2} /. \{z2 \rightarrow z2st, Z2 \rightarrow s * \text{Exp}[-\text{I} * t] + s^3 * V2, p2 \rightarrow p2st, P2 \rightarrow s * W21 + s^3 * W23, z3 \rightarrow z3st, Z3 \rightarrow k * s + s^3 * V3, p3 \rightarrow p3st, P3 \rightarrow s * W31 + s^3 * W33\}$$

$$\text{Out}[*]= -2 \left(\frac{1}{4} \left(-\text{e}^{\text{I} t} s - s^3 v2\right) - \frac{1}{4} \text{I} \left(s w21 + s^3 w23\right) - \frac{1}{2} \text{I} G \left(c s + s^3 v3\right)^2 \left(s w21 + s^3 w23\right) + \text{I} G \left(\text{e}^{-\text{I} t} s + s^3 V2\right) \left(c s + s^3 v3\right) \left(s w31 + s^3 w33\right) + G \left(c s + s^3 v3\right) \left(s w21 + s^3 w23\right) \left(s w31 + s^3 w33\right)\right)$$

$$\text{In}[*]:= \text{Expand}\left[-2 \left(\frac{1}{4} \left(-\text{e}^{\text{I} t} s - s^3 v2\right) - \frac{1}{4} \text{I} \left(s w21 + s^3 w23\right) - \frac{1}{2} \text{I} G \left(c s + s^3 v3\right)^2 \left(s w21 + s^3 w23\right) + \text{I} G \left(\text{e}^{-\text{I} t} s + s^3 V2\right) \left(c s + s^3 v3\right) \left(s w31 + s^3 w33\right) + G \left(c s + s^3 v3\right) \left(s w21 + s^3 w23\right) \left(s w31 + s^3 w33\right)\right)\right]$$

$$\text{Out}[*]= \frac{1}{2} \text{e}^{\text{I} t} s + \frac{s^3 v2}{2} + \frac{\text{I} s w21}{2} + \text{I} c^2 G s^3 W21 + 2 \text{I} c G s^5 v3 W21 + \text{I} G s^7 v3^2 W21 + \frac{1}{2} \text{I} s^3 w23 + \text{I} c^2 G s^5 W23 + 2 \text{I} c G s^7 v3 W23 + \text{I} G s^9 v3^2 W23 - 2 \text{I} c \text{e}^{-\text{I} t} G s^3 w31 - 2 \text{I} c G s^5 V2 w31 - 2 \text{I} \text{e}^{-\text{I} t} G s^5 v3 w31 - 2 \text{I} G s^7 V2 v3 w31 - 2 c G s^3 W21 w31 - 2 G s^5 v3 W21 w31 - 2 c G s^5 W23 w31 - 2 G s^7 v3 W23 w31 - 2 \text{I} c \text{e}^{-\text{I} t} G s^5 w33 - 2 \text{I} c G s^7 V2 w33 - 2 \text{I} \text{e}^{-\text{I} t} G s^7 v3 w33 - 2 \text{I} G s^9 V2 v3 w33 - 2 c G s^5 W21 w33 - 2 G s^7 v3 W21 w33 - 2 c G s^7 W23 w33 - 2 G s^9 v3 W23 w33$$

In[*]:= **Collect**[% , s]

$$\begin{aligned} \text{Out[*]} = & s \left(\frac{e^{it}}{2} + \frac{i w_{21}}{2} \right) + s^3 \left(\frac{v_2}{2} + i c^2 G W_{21} + \frac{i w_{23}}{2} - 2 i c e^{-it} G w_{31} - 2 c G W_{21} w_{31} \right) + \\ & s^5 \left(2 i c G v_3 W_{21} + i c^2 G W_{23} - 2 i c G V_2 w_{31} - 2 i e^{-it} G v_3 w_{31} - \right. \\ & \quad \left. 2 G v_3 W_{21} w_{31} - 2 c G W_{23} w_{31} - 2 i c e^{-it} G w_{33} - 2 c G W_{21} w_{33} \right) + \\ & s^7 \left(i G v_3^2 W_{21} + 2 i c G v_3 W_{23} - 2 i G V_2 v_3 w_{31} - 2 G v_3 W_{23} w_{31} - \right. \\ & \quad \left. 2 i c G V_2 w_{33} - 2 i e^{-it} G v_3 w_{33} - 2 G v_3 W_{21} w_{33} - 2 c G W_{23} w_{33} \right) + \\ & s^9 \left(i G v_3^2 W_{23} - 2 i G V_2 v_3 w_{33} - 2 G v_3 W_{23} w_{33} \right) \end{aligned}$$

In[*]:= **w21 := -I * Exp[I * t]**

In[*]:= **dz2**

$$\text{Out[*]} = 2 \left(-\frac{p_2}{4} + \frac{i z_2}{4} + G p_3 Z_2 z_3 - \frac{1}{2} i G Z_2 z_3^2 \right)$$

$$\text{In[*]} = s \left(\frac{1}{2} i e^{it} - \frac{w_{21}}{2} \right) + s^3 \left(-i c^2 e^{-it} G + \frac{i v_2}{2} - \frac{w_{23}}{2} + 2 c e^{-it} G w_{31} \right)$$

$$\text{Out[*]} = i e^{it} s + s^3 \left(-i c^2 e^{-it} G + \frac{i v_2}{2} - \frac{w_{23}}{2} + 2 c e^{-it} G w_{31} \right)$$

$$\text{In[*]} = s \left(\frac{e^{it}}{2} + \frac{i w_{21}}{2} \right) + s^3 \left(\frac{v_2}{2} + i c^2 G W_{21} + \frac{i w_{23}}{2} - 2 i c e^{-it} G w_{31} - 2 c G W_{21} w_{31} \right)$$

$$\text{Out[*]} = e^{it} s + s^3 \left(\frac{v_2}{2} + i c^2 G W_{21} + \frac{i w_{23}}{2} - 2 i c e^{-it} G w_{31} - 2 c G W_{21} w_{31} \right)$$

In[*]:= **W21 := I * Exp[-I * t]**

In[*]:= **dz3 /. {z2 -> z2st, Z2 -> s * Exp[-I * t] + s^3 * V2,
p2 -> p2st, P2 -> s * W21 + s^3 * W23, z3 -> z3st,
Z3 -> k * s + s^3 * V3, p3 -> p3st, P3 -> s * W31 + s^3 * W33}**

$$\begin{aligned} \text{Out[*]} = & 2 \left(\frac{1}{4} i (c s + s^3 v_3) - \frac{1}{2} i g (e^{it} s + s^3 v_2)^2 (k s + s^3 V_3) + \right. \\ & \quad \left. g (e^{it} s + s^3 v_2) (k s + s^3 V_3) (-i e^{it} s + s^3 w_{23}) + \frac{1}{4} (-s w_{31} - s^3 w_{33}) \right) \end{aligned}$$

$$\begin{aligned} \text{In[*]} = & \text{Expand} \left[2 \left(\frac{1}{4} i (c s + s^3 v_3) - \frac{1}{2} i g (e^{it} s + s^3 v_2)^2 (k s + s^3 V_3) + \right. \right. \\ & \quad \left. \left. g (e^{it} s + s^3 v_2) (k s + s^3 V_3) (-i e^{it} s + s^3 w_{23}) + \frac{1}{4} (-s w_{31} - s^3 w_{33}) \right) \right] \end{aligned}$$

$$\begin{aligned} \text{Out[*]} = & \frac{i c s}{2} - 3 i e^{2it} g k s^3 - 4 i e^{it} g k s^5 v_2 - i g k s^7 v_2^2 + \frac{1}{2} i s^3 v_3 - \\ & 3 i e^{2it} g s^5 V_3 - 4 i e^{it} g s^7 v_2 V_3 - i g s^9 v_2^2 V_3 + 2 e^{it} g k s^5 w_{23} + \\ & 2 g k s^7 v_2 w_{23} + 2 e^{it} g s^7 V_3 w_{23} + 2 g s^9 v_2 V_3 w_{23} - \frac{s w_{31}}{2} - \frac{s^3 w_{33}}{2} \end{aligned}$$

In[8]:= Collect[%, s]

$$\begin{aligned} \text{Out[8]} = & s^5 \left(-4 i e^{i t} g k v2 - 3 i e^{2 i t} g V3 + 2 e^{i t} g k w23 \right) + \\ & s^7 \left(-i g k v2^2 - 4 i e^{i t} g v2 V3 + 2 g k v2 w23 + 2 e^{i t} g V3 w23 \right) + \\ & s^9 \left(-i g v2^2 V3 + 2 g v2 V3 w23 \right) + s \left(\frac{i c}{2} - \frac{w31}{2} \right) + s^3 \left(-3 i e^{2 i t} g k + \frac{i v3}{2} - \frac{w33}{2} \right) \end{aligned}$$

In[9]:= dp3 /. {z2 → z2st, Z2 → s * Exp[-I * t] + s^3 * V2,
p2 → p2st, P2 → s * W21 + s^3 * W23, z3 → z3st,
Z3 → k * s + s^3 * V3, p3 → p3st, P3 → s * W31 + s^3 * W33}

$$\begin{aligned} \text{Out[9]} = & -2 \left(\frac{1}{4} \left(-c s - s^3 v3 \right) + i g \left(e^{i t} s + s^3 v2 \right) \left(k s + s^3 V3 \right) \left(-i e^{i t} s + s^3 w23 \right) - \frac{1}{4} i \left(s w31 + s^3 w33 \right) - \right. \\ & \left. \frac{1}{2} i g \left(e^{i t} s + s^3 v2 \right)^2 \left(s w31 + s^3 w33 \right) + g \left(e^{i t} s + s^3 v2 \right) \left(-i e^{i t} s + s^3 w23 \right) \left(s w31 + s^3 w33 \right) \right) \end{aligned}$$

In[10]:= Expand[%99]

$$\begin{aligned} \text{Out[10]} = & \frac{c s}{2} - 2 e^{2 i t} g k s^3 - 2 e^{i t} g k s^5 v2 + \frac{s^3 v3}{2} - 2 e^{2 i t} g s^5 V3 - 2 e^{i t} g s^7 v2 V3 - 2 i e^{i t} g k s^5 w23 - \\ & 2 i g k s^7 v2 w23 - 2 i e^{i t} g s^7 V3 w23 - 2 i g s^9 v2 V3 w23 + \frac{i s w31}{2} + 3 i e^{2 i t} g s^3 W31 + \\ & 4 i e^{i t} g s^5 v2 W31 + i g s^7 v2^2 W31 - 2 e^{i t} g s^5 w23 W31 - 2 g s^7 v2 w23 W31 + \frac{1}{2} i s^3 w33 + \\ & 3 i e^{2 i t} g s^5 W33 + 4 i e^{i t} g s^7 v2 W33 + i g s^9 v2^2 W33 - 2 e^{i t} g s^7 w23 W33 - 2 g s^9 v2 w23 W33 \end{aligned}$$

In[11]:= Collect[%, s]

$$\begin{aligned} \text{Out[11]} = & s \left(\frac{c}{2} + \frac{i w31}{2} \right) + s^3 \left(-2 e^{2 i t} g k + \frac{v3}{2} + 3 i e^{2 i t} g W31 + \frac{i w33}{2} \right) + \\ & s^5 \left(-2 e^{i t} g k v2 - 2 e^{2 i t} g V3 - 2 i e^{i t} g k w23 + \right. \\ & \left. 4 i e^{i t} g v2 W31 - 2 e^{i t} g w23 W31 + 3 i e^{2 i t} g W33 \right) + \\ & s^7 \left(-2 e^{i t} g v2 V3 - 2 i g k v2 w23 - 2 i e^{i t} g V3 w23 + i g v2^2 W31 - 2 g v2 w23 W31 + \right. \\ & \left. 4 i e^{i t} g v2 W33 - 2 e^{i t} g w23 W33 \right) + s^9 \left(-2 i g v2 V3 w23 + i g v2^2 W33 - 2 g v2 w23 W33 \right) \end{aligned}$$

In[12]:= w31 := I * c

In[13]:= W31 := -I * k

In[14]:= dz3 /. {z2 → z2st, Z2 → s * Exp[-I * t] + s^3 * V2,
p2 → p2st, P2 → s * W21 + s^3 * W23, z3 → z3st,
Z3 → k * s + s^3 * V3, p3 → p3st, P3 → s * W31 + s^3 * W33}

$$\begin{aligned} \text{Out[14]} = & 2 \left(\frac{1}{4} i \left(c s + s^3 v3 \right) - \frac{1}{2} i g \left(e^{i t} s + s^3 v2 \right)^2 \left(k s + s^3 V3 \right) + \right. \\ & \left. g \left(e^{i t} s + s^3 v2 \right) \left(k s + s^3 V3 \right) \left(-i e^{i t} s + s^3 w23 \right) + \frac{1}{4} \left(-i c s - s^3 w33 \right) \right) \end{aligned}$$

$$\begin{aligned} \text{In}[] := & \text{Expand}\left[2\left(\frac{1}{4}i(c s + s^3 v3) - \frac{1}{2}i g (e^{it} s + s^3 v2)^2 (k s + s^3 V3) + \right.\right. \\ & \left.\left. g (e^{it} s + s^3 v2) (k s + s^3 V3) (-i e^{it} s + s^3 w23) + \frac{1}{4}(-i c s - s^3 w33)\right)\right] \\ \text{Out}[] = & -3i e^{2it} g k s^3 - 4i e^{it} g k s^5 v2 - i g k s^7 v2^2 + \frac{1}{2}i s^3 v3 - 3i e^{2it} g s^5 V3 - 4i e^{it} g s^7 v2 V3 - \\ & i g s^9 v2^2 V3 + 2i e^{it} g k s^5 w23 + 2 g k s^7 v2 w23 + 2 e^{it} g s^7 V3 w23 + 2 g s^9 v2 V3 w23 - \frac{s^3 w33}{2} \end{aligned}$$

In[] := Collect[%, s]

$$\begin{aligned} \text{Out}[] = & s^5 (-4i e^{it} g k v2 - 3i e^{2it} g V3 + 2 e^{it} g k w23) + \\ & s^7 (-i g k v2^2 - 4i e^{it} g v2 V3 + 2 g k v2 w23 + 2 e^{it} g V3 w23) + \\ & s^9 (-i g v2^2 V3 + 2 g v2 V3 w23) + s^3 \left(-3i e^{2it} g k + \frac{i v3}{2} - \frac{w33}{2}\right) \end{aligned}$$

**In[] := dp3 /. {z2 → z2st, Z2 → s*Exp[-I*t] + s^3*V2,
p2 → p2st, P2 → s*W21 + s^3*W23, z3 → z3st,
Z3 → k*s + s^3*V3, p3 → p3st, P3 → s*W31 + s^3*W33}**

$$\begin{aligned} \text{Out}[] = & -2\left(\frac{1}{4}(-c s - s^3 v3) + i g (e^{it} s + s^3 v2) (k s + s^3 V3) (-i e^{it} s + s^3 w23) - \right. \\ & \frac{1}{4}i(i c s + s^3 w33) - \frac{1}{2}i g (e^{it} s + s^3 v2)^2 (-i k s + s^3 w33) + \\ & \left. g (e^{it} s + s^3 v2) (-i e^{it} s + s^3 w23) (-i k s + s^3 w33)\right) \end{aligned}$$

In[] := Expand[%107]

$$\begin{aligned} \text{Out}[] = & e^{2it} g k s^3 + 2 e^{it} g k s^5 v2 + g k s^7 v2^2 + \frac{s^3 v3}{2} - 2 e^{2it} g s^5 V3 - 2 e^{it} g s^7 v2 V3 - \\ & 2i e^{it} g s^7 V3 w23 - 2i g s^9 v2 V3 w23 + \frac{1}{2}i s^3 w33 + 3i e^{2it} g s^5 W33 + \\ & 4i e^{it} g s^7 v2 W33 + i g s^9 v2^2 W33 - 2 e^{it} g s^7 w23 W33 - 2 g s^9 v2 w23 W33 \end{aligned}$$

In[] := Collect[%, s]

$$\begin{aligned} \text{Out}[] = & s^3 \left(e^{2it} g k + \frac{v3}{2} + \frac{i w33}{2}\right) + s^5 (2 e^{it} g k v2 - 2 e^{2it} g V3 + 3i e^{2it} g W33) + \\ & s^7 (g k v2^2 - 2 e^{it} g v2 V3 - 2i e^{it} g V3 w23 + 4i e^{it} g v2 W33 - 2 e^{it} g w23 W33) + \\ & s^9 (-2i g v2 V3 w23 + i g v2^2 W33 - 2 g v2 w23 W33) \end{aligned}$$

In[] := dz2trunc := s \left(\frac{1}{2}i e^{it} - \frac{w21}{2}\right) + s^3 \left(-i c^2 e^{-it} G + \frac{i v2}{2} - \frac{w23}{2} + 2 c e^{-it} G w31\right)

In[] := dz2trunc

$$\text{Out}[] = i e^{it} s + s^3 \left(i c^2 e^{-it} G + \frac{i v2}{2} - \frac{w23}{2}\right)$$

In[] := dp2trunc := s \left(\frac{e^{it}}{2} + \frac{i w21}{2}\right) + s^3 \left(\frac{v2}{2} + i c^2 G W21 + \frac{i w23}{2} - 2i c e^{-it} G w31 - 2 c G W21 w31\right)

In[]:= **dp2trunc**

$$\text{Out[]}:= e^{i t} s + s^3 \left(3 c^2 e^{-i t} G + \frac{v2}{2} + \frac{i w23}{2} \right)$$

In[]:= **dz3trunc :=** $s \left(\frac{i c}{2} - \frac{w31}{2} \right) + s^3 \left(-3 i e^{2 i t} g k + \frac{i v3}{2} - \frac{w33}{2} \right)$

In[]:= **dz3trunc**

$$\text{Out[]}:= s^3 \left(-3 i e^{2 i t} g k + \frac{i v3}{2} - \frac{w33}{2} \right)$$

In[]:= **dp3trunc :=** $s^3 \left(e^{2 i t} g k + \frac{v3}{2} + \frac{i w33}{2} \right)$

In[]:= **dp3trunc**

$$\text{Out[]}:= s^3 \left(e^{2 i t} g k + \frac{v3}{2} + \frac{i w33}{2} \right)$$

In[]:= **DSolve**[{ $l'[t] == i c^2 e^{-i t} G + \frac{i l[t]}{2} - \frac{m[t]}{2}$,

$$m'[t] == 3 c^2 e^{-i t} G + \frac{l[t]}{2} + \frac{i m[t]}{2}$$
}, { $l[t]$, $m[t]$ }, t]

$$\begin{aligned} \text{Out[]}:= & \left\{ \left\{ l[t] \rightarrow c^2 e^{-\frac{3 i t}{2}} (-1 + e^{i t}) G \cos\left[\frac{t}{2}\right] + e^{\frac{i t}{2}} C[1] \cos\left[\frac{t}{2}\right] - \right. \right. \\ & i c^2 e^{-\frac{3 i t}{2}} (1 + e^{i t}) G \sin\left[\frac{t}{2}\right] - e^{\frac{i t}{2}} C[2] \sin\left[\frac{t}{2}\right], m[t] \rightarrow i c^2 e^{-\frac{3 i t}{2}} (1 + e^{i t}) G \cos\left[\frac{t}{2}\right] + \\ & \left. e^{\frac{i t}{2}} C[2] \cos\left[\frac{t}{2}\right] + c^2 e^{-\frac{3 i t}{2}} (-1 + e^{i t}) G \sin\left[\frac{t}{2}\right] + e^{\frac{i t}{2}} C[1] \sin\left[\frac{t}{2}\right] \right\} \right\} \end{aligned}$$

In[]:= $c^2 e^{-\frac{3 i t}{2}} (-1 + e^{i t}) G \cos\left[\frac{t}{2}\right] - i c^2 e^{-\frac{3 i t}{2}} (1 + e^{i t}) G \sin\left[\frac{t}{2}\right]$

$$\text{Out[]}:= c^2 e^{-\frac{3 i t}{2}} (-1 + e^{i t}) G \cos\left[\frac{t}{2}\right] - i c^2 e^{-\frac{3 i t}{2}} (1 + e^{i t}) G \sin\left[\frac{t}{2}\right]$$

In[]:= **TrigReduce**[$c^2 e^{-\frac{3 i t}{2}} (-1 + e^{i t}) G \cos\left[\frac{t}{2}\right] - i c^2 e^{-\frac{3 i t}{2}} (1 + e^{i t}) G \sin\left[\frac{t}{2}\right]$]

$$\text{Out[]}:= 0$$

In[]:= $c^2 e^{-\frac{3 i t}{2}} (-1 + e^{i t}) G \cos\left[\frac{t}{2}\right] + e^{\frac{i t}{2}} C[1] \cos\left[\frac{t}{2}\right] - i c^2 e^{-\frac{3 i t}{2}} (1 + e^{i t}) G \sin\left[\frac{t}{2}\right] - e^{\frac{i t}{2}} C[2] \sin\left[\frac{t}{2}\right]$

$$\text{Out[]}:= c^2 e^{-\frac{3 i t}{2}} (-1 + e^{i t}) G \cos\left[\frac{t}{2}\right] + e^{\frac{i t}{2}} C[1] \cos\left[\frac{t}{2}\right] - i c^2 e^{-\frac{3 i t}{2}} (1 + e^{i t}) G \sin\left[\frac{t}{2}\right] - e^{\frac{i t}{2}} C[2] \sin\left[\frac{t}{2}\right]$$

In[]:= **TrigReduce**[$c^2 e^{-\frac{3 i t}{2}} (-1 + e^{i t}) G \cos\left[\frac{t}{2}\right] +$

$$e^{\frac{i t}{2}} C[1] \cos\left[\frac{t}{2}\right] - i c^2 e^{-\frac{3 i t}{2}} (1 + e^{i t}) G \sin\left[\frac{t}{2}\right] - e^{\frac{i t}{2}} C[2] \sin\left[\frac{t}{2}\right]]$$

$$\text{Out[]}:= \frac{1}{2} \left(C[1] + e^{i t} C[1] - i C[2] + i e^{i t} C[2] \right)$$

$$\text{In}[*]:= \text{I} \, c^2 \, e^{-\frac{3 \, \text{I} \, t}{2}} \left(1 + e^{\text{I} \, t} \right) \text{G Cos}\left[\frac{t}{2}\right] + c^2 \, e^{-\frac{3 \, \text{I} \, t}{2}} \left(-1 + e^{\text{I} \, t} \right) \text{G Sin}\left[\frac{t}{2}\right]$$

$$\text{Out}[*]= \text{I} \, c^2 \, e^{-\frac{3 \, \text{I} \, t}{2}} \left(1 + e^{\text{I} \, t} \right) \text{G Cos}\left[\frac{t}{2}\right] + c^2 \, e^{-\frac{3 \, \text{I} \, t}{2}} \left(-1 + e^{\text{I} \, t} \right) \text{G Sin}\left[\frac{t}{2}\right]$$

$$\text{In}[*]:= \text{TrigReduce}\left[\text{I} \, c^2 \, e^{-\frac{3 \, \text{I} \, t}{2}} \left(1 + e^{\text{I} \, t} \right) \text{G Cos}\left[\frac{t}{2}\right] + c^2 \, e^{-\frac{3 \, \text{I} \, t}{2}} \left(-1 + e^{\text{I} \, t} \right) \text{G Sin}\left[\frac{t}{2}\right]\right]$$

$$\text{Out}[*]= 2 \, \text{I} \, c^2 \, e^{-\text{I} \, t} \text{G}$$