In[\*]:= l[t]
Out[\*]= l[t]

$$\begin{split} & \text{In}(*) = \text{Solve} \Big[ \\ & \left\{ l^{\, !} [t] = 2\, \dot{a}\, a\, c + \dot{a}\, a\, c^{\, 3} - \frac{1}{2}\, \dot{a}\, B\, c^{\, 2}\, e^{-\dot{a}\, t} - \frac{3}{2}\, \dot{a}\, b\, e^{\dot{a}\, t} + \dot{a}\, b\, c^{\, 2}\, e^{\dot{a}\, t} - 3\, \dot{a}\, c\, e^{2\, \dot{a}\, t}\, g\, + \frac{\dot{a}\, 1\, [t]}{2} + \frac{\dot{a}\, m\, [t]}{2} \right\}, \, \{l[t], \\ & m^{\, !} [t] = 2\, a\, c + a\, c^{\, 3} - \frac{3}{2}\, B\, c^{\, 2}\, e^{-\dot{a}\, t} - \frac{5}{2}\, b\, e^{\dot{a}\, t} - b\, c^{\, 2}\, e^{\dot{a}\, t} + c\, e^{2\, \dot{a}\, t}\, g\, + \frac{\dot{a}\, 1\, [t]}{2} + \frac{\dot{a}\, m\, [t]}{2} \right\}, \, \{l[t], \\ & m[t]), \, t \Big] \\ & c_{i}(t) = \frac{1}{2}\, \dot{a}\, e^{\frac{\dot{a}\, t}{2}} \\ & (i\, c\, (A\, a + B\, b\, c + 2\, a\, c^{\, 2})\, e^{-\dot{a}\, t} - \dot{a}\, B\, c^{\, 2}\, e^{-2\, \dot{a}\, t}\, + 2\, \dot{a}\, c\, e^{2\, \dot{a}\, t}\, g\, - 2\, \dot{a}\, e^{2\, \dot{a}\, t}$$

$$\textit{Out[*]} = \frac{1}{2} \left( 2 \, \mathsf{B} \, \mathsf{C} + \mathsf{B} \, \mathsf{C}^3 + 2 \, \mathsf{a} \, \mathsf{e}^{\mathsf{i} \, \mathsf{t}} + 4 \, \mathsf{a} \, \mathsf{C}^2 \, \mathsf{e}^{\mathsf{i} \, \mathsf{t}} - 2 \, \mathsf{b} \, \mathsf{C} \, \mathsf{e}^{\mathsf{2} \, \mathsf{i} \, \mathsf{t}} - 8 \, \mathsf{i} \, \mathsf{a} \, \mathsf{e}^{\mathsf{i} \, \mathsf{t}} \, \mathsf{t} + \mathsf{C} \, [1] \, + \, \mathsf{e}^{\mathsf{i} \, \mathsf{t}} \, \mathsf{C} \, [2] \, + \, \mathsf{i} \, \, \mathsf{e}^{\mathsf{i} \, \mathsf{t}} \, \mathsf{C} \, [2] \right)$$

$$\begin{aligned} & \text{FullSimplify} \Big[ \frac{1}{2} \, \left( 2 \, \text{B} \, \text{c} + \text{B} \, \text{c}^3 + 2 \, \text{a} \, \text{e}^{\, \text{i} \, \text{t}} + 4 \, \text{a} \, \text{c}^2 \, \text{e}^{\, \text{i} \, \text{t}} - 2 \, \text{b} \, \text{c} \, \text{e}^{2 \, \, \text{i} \, \text{t}} - 8 \, \, \text{i} \, \text{a} \, \text{e}^{\, \text{i} \, \text{t}} \, \text{t} + \text{C} \, [1] + \text{e}^{\, \text{i} \, \text{t}} \, \text{C} \, [2] + \, \, \text{i} \, \, \text{e}^{\, \text{i} \, \text{t}} \, \text{C} \, [2] \right) \Big] \\ & \text{Out}_{[^a]^{\equiv}} \, \frac{1}{2} \, \left( \text{B} \, \text{C} \, \left( 2 + \text{C}^2 \right) - 2 \, \text{b} \, \text{C} \, \, \text{e}^{2 \, \, \text{i} \, \text{t}} + \text{C} \, [1] + \text{e}^{\, \text{i} \, \text{t}} \, \left( \text{a} \, \left( 2 + 4 \, \text{C}^2 - 8 \, \, \text{i} \, \, \text{t} \right) + \text{C} \, [1] + \, \, \text{i} \, \, \text{C} \, [2] \right) - \, \, \text{i} \, \, \text{C} \, [2] \right) \end{aligned}$$

$$\begin{aligned} & \text{Out}[*] = \ B \ C \ e^{-\frac{i \, t}{2}} \ Cos\left[\frac{t}{2}\right] + \frac{1}{2} \ B \ C^3 \ e^{-\frac{i \, t}{2}} \ Cos\left[\frac{t}{2}\right] + a \ e^{\frac{3 \, i \, t}{2}} \ Cos\left[\frac{t}{2}\right] - \frac{1}{2} \ b \ c \ e^{\frac{3 \, i \, t}{2}} \ Cos\left[\frac{t}{2}\right] + \\ & 2 \ a \ c^2 \ e^{\frac{3 \, i \, t}{2}} \ Cos\left[\frac{t}{2}\right] - \frac{1}{2} \ b \ c \ e^{\frac{5 \, i \, t}{2}} \ Cos\left[\frac{t}{2}\right] + c^2 \ e^{-\frac{i \, t}{2}} \ G \ Cos\left[\frac{t}{2}\right] - c^2 \ e^{-\frac{3 \, i \, t}{2}} \ G \ Cos\left[\frac{t}{2}\right] - \\ & 4 \ \dot{\mathbb{1}} \ a \ e^{\frac{i \, t}{2}} \ t \ Cos\left[\frac{t}{2}\right] + e^{\frac{i \, t}{2}} \ C[1] \ Cos\left[\frac{t}{2}\right] + \dot{\mathbb{1}} \ B \ c \ e^{-\frac{i \, t}{2}} \ Sin\left[\frac{t}{2}\right] + \frac{1}{2} \ \dot{\mathbb{1}} \ B \ c^3 \ e^{-\frac{i \, t}{2}} \ Sin\left[\frac{t}{2}\right] - \\ & \dot{\mathbb{1}} \ a \ e^{\frac{3 \, i \, t}{2}} \ Sin\left[\frac{t}{2}\right] - \frac{1}{2} \ \dot{\mathbb{1}} \ b \ c \ e^{\frac{3 \, i \, t}{2}} \ Sin\left[\frac{t}{2}\right] - 2 \ \dot{\mathbb{1}} \ a \ c^2 \ e^{\frac{3 \, i \, t}{2}} \ Sin\left[\frac{t}{2}\right] + \frac{1}{2} \ \dot{\mathbb{1}} \ b \ c \ e^{\frac{5 \, i \, t}{2}} \ Sin\left[\frac{t}{2}\right] - \\ & \dot{\mathbb{1}} \ c^2 \ e^{-\frac{i \, t}{2}} \ G \ Sin\left[\frac{t}{2}\right] - \dot{\mathbb{1}} \ c^2 \ e^{-\frac{3 \, i \, t}{2}} \ G \ Sin\left[\frac{t}{2}\right] + 4 \ a \ e^{\frac{i \, t}{2}} \ t \ Sin\left[\frac{t}{2}\right] - e^{\frac{i \, t}{2}} \ C[2] \ Sin\left[\frac{t}{2}\right] \end{aligned}$$

$$\begin{aligned} & \textit{Out}[*]_{=} & -\frac{1}{2} \, \, \, \dot{\mathbb{E}} \, \, \, \, \dot{\mathbb{E}} \, \, \dot{\mathbb{E}} \, \, \dot{\mathbb{E}} \, \, \, \dot{\mathbb{$$

## In[\*]:= TrigReduce[%16]

$$\textit{Out[*]} = \frac{1}{2} \left( 2 \; B \; c \; + \; B \; c^3 \; + \; 2 \; a \; e^{i \; t} \; + \; 4 \; a \; c^2 \; e^{i \; t} \; - \; 2 \; b \; c \; e^{2 \; i \; t} \; - \; 8 \; i \; a \; e^{i \; t} \; t \; + \; C \; [1] \; + \; e^{i \; t} \; C \; [2] \; + \; i \; e^{i \; t} \; C \; [2] \; \right)$$

## In[\*]:= ExpandAll[%]

$$\textit{Out[*]$= B $C$ + $\frac{B \ C^3}{2}$ + a $e^{i \ t}$ + 2 a $c^2$ $e^{i \ t}$ - b $c$ $e^{2 \ i \ t}$ - 4 i a $e^{i \ t}$ $t$ + $\frac{C \ [1]}{2}$ + $\frac{1}{2}$ $e^{i \ t}$ $C \ [1]$ - $\frac{1}{2}$ i $C \ [2]$ + $\frac{1}{2}$ i $e^{i \ t}$ $C \ [2]$ + $\frac{1}{2$$

$$ln[@]:= V_3[t_] := l[t] /. sol_3[[1]]$$

$$In[\bullet]:= V_3 := V_3[t]$$

## In[\*]:= TrigReduce[%21]

$$\begin{array}{l} \text{Out}(*) = & \frac{1}{2} \\ & & \\ & \left( -4 \text{ a c} - 2 \text{ a c}^3 + b \ \text{e}^{\text{i t}} + 2 \text{ b c}^2 \ \text{e}^{\text{i t}} - 4 \text{ c e}^{2 \text{ i t}} \ \text{g} - 4 \text{ i b e}^{\text{i t}} \ \text{t} + \text{C[1]} + \text{e}^{\text{i t}} \ \text{C[1]} - \text{i C[2]} + \text{i e}^{\text{i t}} \ \text{C[2]} \right) \end{array}$$

Info]:= ExpandAll[%]

$$\begin{aligned} & \textit{Out}[\,^{\,\text{o}}]_{=} & -2 \; a \; c \; - \; a \; c^{3} \; + \; \frac{1}{2} \; b \; e^{i \; t} \; + \; b \; c^{2} \; e^{i \; t} \; - \; 2 \; c \; e^{2 \; i \; t} \; g \; - \\ & 2 \; i \; b \; e^{i \; t} \; t \; + \; \frac{C \, [\, 1\,]}{2} \; + \; \frac{1}{2} \; e^{i \; t} \; C \, [\, 1\,] \; - \; \frac{1}{2} \; i \; C \, [\, 2\,] \; + \; \frac{1}{2} \; i \; e^{i \; t} \; C \, [\, 2\,] \end{aligned}$$

$$ln[@] := b := 0$$

$$\begin{array}{l} \textit{Out}[*] = & \frac{1}{2} \, \, \dot{\mathbb{E}} \, \, \dot{\mathbb{E}} \, \, \,$$

In[\*]:= TrigReduce[%26]

$$\textit{Out[*]} = \frac{1}{2} \left( -4 \ a \ c - 2 \ a \ c^3 - 4 \ c \ e^{2 \ i \ t} \ g + C \ [1] \ + e^{i \ t} \ C \ [1] \ - \ \dot{i} \ C \ [2] \ + \ \dot{i} \ e^{i \ t} \ C \ [2] \right)$$

$$ln[\bullet] := \mathbf{C[1]} := \mathbf{0}$$

SetDelayed: Tag C in C[1] is Protected.

Out[\*]= \$Failed

$$\ln[*]:= V_2 := B c + \frac{B c^3}{2} + a e^{it} + 2 a c^2 e^{it} - b c e^{2it} - 4 i a e^{it} t$$

Out 
$$0 = a e^{it} + 2 a c^2 e^{it} - 4 i a e^{it}$$

$$log_{\hat{e}} := V_3 := -2 a c - a c^3 + \frac{1}{2} b e^{it} + b c^2 e^{it} - 2 c e^{2it} g - 2 i b e^{it} t$$

$$Out[\bullet] = -2 a c - a c^3 - 2 c e^{2 i t} g$$

$$||f||_{x=1}^{x=1} = (Exp[I*t])*s + (ae^{it} + 2ac^2e^{it} - 4iae^{it})*s^3$$

$$I_{n[\cdot]:=} J_2 := (Exp[-I*t]) *s + (a e^{-it} + 2 a c^2 e^{-it} + 4 i a e^{-it} t) *s^3$$

$$ln[*]:= j_3 := c * s + (-2 a c - a c^3 - 2 c e^{2 i t} g) * s^3$$

$$I_{n[\cdot]} := J_3 := c * s + (-2 a c - a c^3 - 2 c e^{-2 i t} * G) * s^3$$

$$\begin{array}{ll} \ln[*] := & \rho := z_1 + Z_1 - z_2 \ Z_2 - G \ z_3^2 \ Z_2^2 - z_3 \ Z_3 - g \ z_2^2 \ Z_3^2 - \\ & \left( B \ z_3 \ Z_2 + b \ z_2 \ Z_3 \right) \ \left( z_2 \ Z_2 - z_3 \ Z_3 \right) - a \ \left( z_2^2 \ Z_2^2 - 4 \ z_2 \ z_3 \ Z_2 \ Z_3 + z_3^2 \ Z_3^2 \right) \end{array}$$

4  $(c s + (-2 a c - a c^3 - 2 c e^{2 i t} g) s^3) (c s + (-2 a c - a c^3 - 2 c e^{-2 i t} G) s^3)$ 

 $s^{3}\,\left(a\,\,\mathrm{e}^{\mathrm{i}\,\,t}\,+\,2\,\,a\,\,c^{2}\,\,\mathrm{e}^{\mathrm{i}\,\,t}\,-\,4\,\,\mathrm{i}\,\,a\,\,\mathrm{e}^{\mathrm{i}\,\,t}\,\,t\right)\,\right)\,+\,\left(\mathrm{e}^{-\mathrm{i}\,\,t}\,\,s\,+\,s^{3}\,\,\left(a\,\,\mathrm{e}^{-\mathrm{i}\,\,t}\,+\,2\,\,a\,\,c^{2}\,\,\mathrm{e}^{-\mathrm{i}\,\,t}\,+\,4\,\,\mathrm{i}\,\,a\,\,\mathrm{e}^{-\mathrm{i}\,\,t}\,\,t\right)\,\right)^{\,2}$ 

 $(e^{-it}s + s^3(ae^{-it} + 2ac^2e^{-it} + 4iae^{-it}t))(e^{it}s +$ 

 $(e^{it}s + s^3(ae^{it} + 2ac^2e^{it} - 4iae^{it}))^2) + z_1 + Z_1)$