

```
In[*]:= ρ := z1 + Z1 - z2 * Z2 - z3 * Z3 - g * z2^2 * Z3^2 - G * z3^2 * Z2^2
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In[*]:= ρ
```

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Out[*]:= z1 + Z1 - z2 Z2 - G Z2^2 z3^2 - z3 Z3 - g z2^2 Z3^2
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In[*]:= ρ2 := D[ρ, z2]
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In[*]:= ρ20 := D[ρ, Z2]
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In[*]:= ρ3 := D[ρ, z3]
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In[*]:= ρ30 := D[ρ, Z3]
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In[*]:= ρ22 := D[ρ, z2, Z2]
```

```
In[*]:= ρ22
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```
Out[*]:= -1
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```
In[*]:= ρ23 := D[ρ, z2, Z3]
```

```
In[*]:= ρ23
```

```
Out[*]:= -4 g z2 Z3
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In[*]:= ρ33 := D[ρ, z3, Z3]
```

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In[*]:= ρ32 := D[ρ, z3, Z2]
```

```
In[*]:= A := {{0, I, I * ρ20, I * ρ30}, {-I, 0, 0, 0},
               {-I * ρ2, 0, 4 * ρ22, 4 * ρ23}, {-I * ρ3, 0, 4 * ρ32, 4 * ρ33}}
```

```
In[*]:= MatrixForm[A]
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```
Out[*]//MatrixForm=
```

$$\begin{pmatrix} 0 & i & i(-z2 - 2G Z2 z3^2) & i(-z3 - 2g z2^2 Z3) \\ -i & 0 & 0 & 0 \\ -i(-Z2 - 2g z2 Z3^2) & 0 & -4 & -16g z2 Z3 \\ -i(-2G Z2^2 z3 - Z3) & 0 & -16G Z2 z3 & -4 \end{pmatrix}$$

```
In[*]:= B := Inverse[A]
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In[*]:= MatrixForm[B]
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```
Out[*]//MatrixForm=
```

$$\begin{pmatrix} 0 & \frac{-16i+256igGz2Z2z3Z3}{-16+256gGz2Z2z3Z3} & \frac{16i-256igGz2Z2z3Z3}{-16+256gGz2Z2z3Z3} & \frac{4z2Z2+4z3Z3-48gGz2^2Z2^2z3Z3-64g^2Z2Z2^3z3^3Z3-48gGz2Z2z3^2Z3^2-64g^2Gz2^3Z2z3Z3^3}{-16+256gGz2Z2z3Z3} & \frac{4z2-16i+256igGz2Z2z3Z3}{-16+256gGz2Z2z3Z3} \\ \frac{16i-256igGz2Z2z3Z3}{-16+256gGz2Z2z3Z3} & \frac{4z2Z2+4z3Z3-48gGz2^2Z2^2z3Z3-64g^2Z2Z2^3z3^3Z3-48gGz2Z2z3^2Z3^2-64g^2Gz2^3Z2z3Z3^3}{-16+256gGz2Z2z3Z3} & \frac{4Z2-32gGz2Z2^2z3Z3-8gZ2Z3^2}{-16+256gGz2Z2z3Z3} & \frac{-8GZ2^2z3+4Z3-32gGz2Z2z3Z3^2}{-16+256gGz2Z2z3Z3} & - \\ 0 & \frac{4Z2-32gGz2Z2^2z3Z3-8gZ2Z3^2}{-16+256gGz2Z2z3Z3} & \frac{-8GZ2^2z3+4Z3-32gGz2Z2z3Z3^2}{-16+256gGz2Z2z3Z3} & - \\ 0 & \frac{-8GZ2^2z3+4Z3-32gGz2Z2z3Z3^2}{-16+256gGz2Z2z3Z3} & - & - \end{pmatrix}$$

```
In[*]:= L := {{0, I, 0, 0},
               {-I, -(z2 * Z2 + z3 * Z3) / 4, -(z2 - 2 * G * Z2 * z3^2) / 4, -(z3 - 2 * g * z2^2 * Z3) / 4},
               {0, -(Z2 - 2 * g * z2 * Z3^2) / 4, -1 / 4, g * z2 * Z3},
               {0, -(Z3 - 2 * G * Z2^2 * z3) / 4, G * Z2 * z3, -1 / 4}}
```

In[]:= **MatrixForm**[L]

Out[]:= **MatrixForm**=

$$\begin{pmatrix} 0 & i & 0 & 0 \\ -i & \frac{1}{4}(-z^2 Z^2 - z^3 Z^3) & \frac{1}{4}(-z^2 + 2 G Z^2 z^3) & \frac{1}{4}(-z^3 + 2 g z^2 Z^3) \\ 0 & \frac{1}{4}(-Z^2 + 2 g z^2 Z^3) & -\frac{1}{4} & g z^2 Z^3 \\ 0 & \frac{1}{4}(2 G Z^2 z^3 - Z^3) & G Z^2 z^3 & -\frac{1}{4} \end{pmatrix}$$

In[]:= **q** := {p0, I * p1, p2, p3}

In[]:= **Q** := {p0, -I * p1, P2, P3}

In[]:= **q.L.Q**

$$\begin{aligned} \text{Out[]} = & p_0 p_1 + P_2 \left(-\frac{p_2}{4} + G p_3 Z^2 z^3 + \frac{1}{4} i p_1 (-z^2 + 2 G Z^2 z^3) \right) + \\ & P_3 \left(-\frac{p_3}{4} + g p_2 z^2 Z^3 + \frac{1}{4} i p_1 (-z^3 + 2 g z^2 Z^3) \right) - \\ & i p_1 \left(i p_0 + \frac{1}{4} p_3 (2 G Z^2 z^3 - Z^3) + \frac{1}{4} i p_1 (-z^2 Z^2 - z^3 Z^3) + \frac{1}{4} p_2 (-Z^2 + 2 g z^2 Z^3) \right) \end{aligned}$$

$$\begin{aligned} \text{In[]} = & \text{Simplify} \left[p_0 p_1 + P_2 \left(-\frac{p_2}{4} + G p_3 Z^2 z^3 + \frac{1}{4} i p_1 (-z^2 + 2 G Z^2 z^3) \right) + \right. \\ & P_3 \left(-\frac{p_3}{4} + g p_2 z^2 Z^3 + \frac{1}{4} i p_1 (-z^3 + 2 g z^2 Z^3) \right) - \\ & \left. i p_1 \left(i p_0 + \frac{1}{4} p_3 (2 G Z^2 z^3 - Z^3) + \frac{1}{4} i p_1 (-z^2 Z^2 - z^3 Z^3) + \frac{1}{4} p_2 (-Z^2 + 2 g z^2 Z^3) \right) \right] \end{aligned}$$

$$\begin{aligned} \text{Out[]} = & 2 p_0 p_1 - \frac{1}{4} i \left(p_3 (-i P_3 + 2 G Z^2 (2 i P_2 + p_1 Z^2) z^3 - p_1 Z^3) + \right. \\ & p_2 (-i P_2 - p_1 Z^2 + 4 i g P_3 z^2 Z^3 + 2 g p_1 z^2 Z^3) + \\ & \left. p_1 (P_2 (z^2 - 2 G Z^2 z^3) + P_3 (z^3 - 2 g z^2 Z^3) - i p_1 (z^2 Z^2 + z^3 Z^3)) \right) \end{aligned}$$

$$\begin{aligned} \text{In[]} = & \text{Expand} \left[2 p_0 p_1 - \frac{1}{4} i \left(p_3 (-i P_3 + 2 G Z^2 (2 i P_2 + p_1 Z^2) z^3 - p_1 Z^3) + \right. \right. \\ & p_2 (-i P_2 - p_1 Z^2 + 4 i g P_3 z^2 Z^3 + 2 g p_1 z^2 Z^3) + \\ & \left. \left. p_1 (P_2 (z^2 - 2 G Z^2 z^3) + P_3 (z^3 - 2 g z^2 Z^3) - i p_1 (z^2 Z^2 + z^3 Z^3)) \right) \right] \end{aligned}$$

$$\begin{aligned} \text{Out[]} = & 2 p_0 p_1 - \frac{p_2 P_2}{4} - \frac{p_3 P_3}{4} - \frac{1}{4} i p_1 P_2 z^2 + \frac{1}{4} i p_1 p_2 Z^2 - \frac{1}{4} p_1^2 z^2 Z^2 - \\ & \frac{1}{4} i p_1 P_3 z^3 + G P_2 p_3 Z^2 z^3 - \frac{1}{2} i G p_1 p_3 Z^2 z^3 + \frac{1}{2} i G p_1 P_2 Z^2 z^3 + \\ & \frac{1}{4} i p_1 p_3 Z^3 + g p_2 P_3 z^2 Z^3 + \frac{1}{2} i g p_1 P_3 z^2 Z^3 - \frac{1}{4} p_1^2 z^3 Z^3 - \frac{1}{2} i g p_1 p_2 z^2 Z^3 \end{aligned}$$

$$\begin{aligned} \text{In[]} = & \text{H} := 2 p_0 p_1 - \frac{p_2 P_2}{4} - \frac{p_3 P_3}{4} - \frac{1}{4} i p_1 P_2 z^2 + \frac{1}{4} i p_1 p_2 Z^2 - \frac{1}{4} p_1^2 z^2 Z^2 - \\ & \frac{1}{4} i p_1 P_3 z^3 + G P_2 p_3 Z^2 z^3 - \frac{1}{2} i G p_1 p_3 Z^2 z^3 + \frac{1}{2} i G p_1 P_2 Z^2 z^3 + \\ & \frac{1}{4} i p_1 p_3 Z^3 + g p_2 P_3 z^2 Z^3 + \frac{1}{2} i g p_1 P_3 z^2 Z^3 - \frac{1}{4} p_1^2 z^3 Z^3 - \frac{1}{2} i g p_1 p_2 z^2 Z^3 \end{aligned}$$

In[]:= **Collect**[H, p1 * P2]

$$\begin{aligned} \text{Out[]}= & 2 p_0 p_1 - \frac{p_2 P_2}{4} - \frac{p_3 P_3}{4} + \frac{1}{4} i p_1 p_2 Z_2 - \frac{1}{4} p_1^2 z_2 Z_2 - \frac{1}{4} i p_1 P_3 z_3 + \\ & G P_2 p_3 Z_2 z_3 - \frac{1}{2} i G p_1 p_3 Z_2^2 z_3 + p_1 P_2 \left(-\frac{i z_2}{4} + \frac{1}{2} i G Z_2 z_3^2 \right) + \frac{1}{4} i p_1 p_3 Z_3 + \\ & g p_2 P_3 z_2 Z_3 + \frac{1}{2} i g p_1 P_3 z_2^2 Z_3 - \frac{1}{4} p_1^2 z_3 Z_3 - \frac{1}{2} i g p_1 p_2 z_2 Z_3^2 \end{aligned}$$

In[]:= **H**

In[]:= **ClearAll**[H]

$$\begin{aligned} \text{In[]:= } H := & 2 p_0 p_1 - \frac{p_2 P_2}{4} - \frac{p_3 P_3}{4} - \frac{1}{4} i p_1 P_2 z_2 + \frac{1}{4} i p_1 p_2 Z_2 - \frac{1}{4} p_1^2 z_2 Z_2 - \\ & \frac{1}{4} i p_1 P_3 z_3 + G P_2 p_3 Z_2 z_3 - \frac{1}{2} i G p_1 p_3 Z_2^2 z_3 + \frac{1}{2} i G p_1 P_2 Z_2 z_3^2 + \\ & \frac{1}{4} i p_1 p_3 Z_3 + g p_2 P_3 z_2 Z_3 + \frac{1}{2} i g p_1 P_3 z_2^2 Z_3 - \frac{1}{4} p_1^2 z_3 Z_3 - \frac{1}{2} i g p_1 p_2 z_2 Z_3^2 \end{aligned}$$

In[]:= **H**

$$\begin{aligned} \text{Out[]}= & 2 p_0 p_1 - \frac{p_2 P_2}{4} - \frac{p_3 P_3}{4} - \frac{1}{4} i p_1 P_2 z_2 + \frac{1}{4} i p_1 p_2 Z_2 - \frac{1}{4} p_1^2 z_2 Z_2 - \\ & \frac{1}{4} i p_1 P_3 z_3 + G P_2 p_3 Z_2 z_3 - \frac{1}{2} i G p_1 p_3 Z_2^2 z_3 + \frac{1}{2} i G p_1 P_2 Z_2 z_3^2 + \\ & \frac{1}{2} i G p_1 P_3 Z_2 z_3^2 + \frac{1}{4} i p_1 p_3 Z_3 + g p_2 P_3 z_2 Z_3 - \frac{1}{4} p_1^2 z_3 Z_3 - \frac{1}{2} i g p_1 p_2 z_2 Z_3^2 \end{aligned}$$

In[]:= **Collect**[H, p1 * P2]

$$\begin{aligned} \text{Out[]}= & 2 p_0 p_1 - \frac{p_2 P_2}{4} - \frac{p_3 P_3}{4} + \frac{1}{4} i p_1 p_2 Z_2 - \frac{1}{4} p_1^2 z_2 Z_2 - \frac{1}{4} i p_1 P_3 z_3 + \\ & G P_2 p_3 Z_2 z_3 - \frac{1}{2} i G p_1 p_3 Z_2^2 z_3 + p_1 P_2 \left(-\frac{i z_2}{4} + \frac{1}{2} i G Z_2 z_3^2 \right) + \frac{1}{4} i p_1 p_3 Z_3 + \\ & g p_2 P_3 z_2 Z_3 + \frac{1}{2} i g p_1 P_3 z_2^2 Z_3 - \frac{1}{4} p_1^2 z_3 Z_3 - \frac{1}{2} i g p_1 p_2 z_2 Z_3^2 \end{aligned}$$

In[]:= **Collect**[H, p1 * P3]

$$\begin{aligned} \text{Out[]}= & 2 p_0 p_1 - \frac{p_2 P_2}{4} - \frac{p_3 P_3}{4} - \frac{1}{4} i p_1 P_2 z_2 + \frac{1}{4} i p_1 p_2 Z_2 - \frac{1}{4} p_1^2 z_2 Z_2 + \\ & G P_2 p_3 Z_2 z_3 - \frac{1}{2} i G p_1 p_3 Z_2^2 z_3 + \frac{1}{2} i G p_1 P_2 Z_2 z_3^2 + \frac{1}{4} i p_1 p_3 Z_3 + \\ & g p_2 P_3 z_2 Z_3 - \frac{1}{4} p_1^2 z_3 Z_3 - \frac{1}{2} i g p_1 p_2 z_2 Z_3^2 + p_1 P_3 \left(-\frac{i z_3}{4} + \frac{1}{2} i g z_2^2 Z_3 \right) \end{aligned}$$

In[]:= **Collect[H, p2 * P2]**

$$\begin{aligned} \text{Out[]}= & 2 p_0 p_1 - \frac{p_2 P_2}{4} - \frac{p_3 P_3}{4} - \frac{1}{4} i p_1 P_2 z_2 + \frac{1}{4} i p_1 p_2 Z_2 - \frac{1}{4} p_1^2 z_2 Z_2 - \\ & \frac{1}{4} i p_1 P_3 z_3 + G P_2 p_3 Z_2 z_3 - \frac{1}{2} i G p_1 p_3 Z_2^2 z_3 + \frac{1}{2} i G p_1 P_2 Z_2 z_3^2 + \\ & \frac{1}{4} i p_1 p_3 Z_3 + g p_2 P_3 z_2 Z_3 + \frac{1}{2} i g p_1 P_3 z_2^2 Z_3 - \frac{1}{4} p_1^2 z_3 Z_3 - \frac{1}{2} i g p_1 p_2 z_2 Z_3^2 \end{aligned}$$

In[]:= **Collect[H, p2 * P3]**

$$\begin{aligned} \text{Out[]}= & 2 p_0 p_1 - \frac{p_2 P_2}{4} - \frac{p_3 P_3}{4} - \frac{1}{4} i p_1 P_2 z_2 + \frac{1}{4} i p_1 p_2 Z_2 - \frac{1}{4} p_1^2 z_2 Z_2 - \\ & \frac{1}{4} i p_1 P_3 z_3 + G P_2 p_3 Z_2 z_3 - \frac{1}{2} i G p_1 p_3 Z_2^2 z_3 + \frac{1}{2} i G p_1 P_2 Z_2 z_3^2 + \\ & \frac{1}{4} i p_1 p_3 Z_3 + g p_2 P_3 z_2 Z_3 + \frac{1}{2} i g p_1 P_3 z_2^2 Z_3 - \frac{1}{4} p_1^2 z_3 Z_3 - \frac{1}{2} i g p_1 p_2 z_2 Z_3^2 \end{aligned}$$

In[]:= **Collect[H, p1 * p2]**

$$\begin{aligned} \text{Out[]}= & 2 p_0 p_1 - \frac{p_2 P_2}{4} - \frac{p_3 P_3}{4} - \frac{1}{4} i p_1 P_2 z_2 - \frac{1}{4} p_1^2 z_2 Z_2 - \frac{1}{4} i p_1 P_3 z_3 + \\ & G P_2 p_3 Z_2 z_3 - \frac{1}{2} i G p_1 p_3 Z_2^2 z_3 + \frac{1}{2} i G p_1 P_2 Z_2 z_3^2 + \frac{1}{4} i p_1 p_3 Z_3 + \\ & g p_2 P_3 z_2 Z_3 + \frac{1}{2} i g p_1 P_3 z_2^2 Z_3 - \frac{1}{4} p_1^2 z_3 Z_3 + p_1 p_2 \left(\frac{i Z_2}{4} - \frac{1}{2} i g z_2 Z_3^2 \right) \end{aligned}$$

In[]:= **Collect[H, p1 * p3]**

$$\begin{aligned} \text{Out[]}= & 2 p_0 p_1 - \frac{p_2 P_2}{4} - \frac{p_3 P_3}{4} - \frac{1}{4} i p_1 P_2 z_2 + \frac{1}{4} i p_1 p_2 Z_2 - \frac{1}{4} p_1^2 z_2 Z_2 - \\ & \frac{1}{4} i p_1 P_3 z_3 + G P_2 p_3 Z_2 z_3 + \frac{1}{2} i G p_1 P_2 Z_2 z_3^2 + p_1 p_3 \left(-\frac{1}{2} i G Z_2^2 z_3 + \frac{i Z_3}{4} \right) + \\ & g p_2 P_3 z_2 Z_3 + \frac{1}{2} i g p_1 P_3 z_2^2 Z_3 - \frac{1}{4} p_1^2 z_3 Z_3 - \frac{1}{2} i g p_1 p_2 z_2 Z_3^2 \end{aligned}$$

In[]:= **Collect[H, P2 * p3]**

$$\begin{aligned} \text{Out[]}= & 2 p_0 p_1 - \frac{p_2 P_2}{4} - \frac{p_3 P_3}{4} - \frac{1}{4} i p_1 P_2 z_2 + \frac{1}{4} i p_1 p_2 Z_2 - \frac{1}{4} p_1^2 z_2 Z_2 - \\ & \frac{1}{4} i p_1 P_3 z_3 + G P_2 p_3 Z_2 z_3 - \frac{1}{2} i G p_1 p_3 Z_2^2 z_3 + \frac{1}{2} i G p_1 P_2 Z_2 z_3^2 + \\ & \frac{1}{4} i p_1 p_3 Z_3 + g p_2 P_3 z_2 Z_3 + \frac{1}{2} i g p_1 P_3 z_2^2 Z_3 - \frac{1}{4} p_1^2 z_3 Z_3 - \frac{1}{2} i g p_1 p_2 z_2 Z_3^2 \end{aligned}$$

In[]:= **dz2 := 2 * D[H, P2]**

In[]:= **dz2**

$$\text{Out[]}= 2 \left(-\frac{p_2}{4} - \frac{i p_1 z_2}{4} + G p_3 Z_2 z_3 + \frac{1}{2} i G p_1 Z_2 z_3^2 \right)$$

$$\text{In}[*]:= \text{Expand}\left[2\left(-\frac{p2}{4}-\frac{i p1 z2}{4}+G p3 Z2 z3+\frac{1}{2} i G p1 Z2 z3^2\right)\right]$$

$$\text{Out}[*]= -\frac{p2}{2}-\frac{i p1 z2}{2}+2 G p3 Z2 z3+i G p1 Z2 z3^2$$

$$\text{In}[*]:= \text{Collect}[\%, p1]$$

$$\text{Out}[*]= -\frac{p2}{2}+2 G p3 Z2 z3+p1\left(-\frac{i z2}{2}+i G Z2 z3^2\right)$$

$$\text{In}[*]:= \text{dp2} := -2 * D[H, Z2]$$

$$\text{In}[*]:= \text{dp2}$$

$$\text{Out}[*]= -2\left(\frac{i p1 p2}{4}-\frac{p1^2 z2}{4}+G P2 p3 z3-i G p1 p3 Z2 z3+\frac{1}{2} i G p1 P2 z3^2\right)$$

$$\text{In}[*]:= \text{Expand}\left[-2\left(\frac{i p1 p2}{4}-\frac{p1^2 z2}{4}+G P2 p3 z3-i G p1 p3 Z2 z3+\frac{1}{2} i G p1 P2 z3^2\right)\right]$$

$$\text{Out}[*]= -\frac{1}{2} i p1 p2+\frac{p1^2 z2}{2}-2 G P2 p3 z3+2 i G p1 p3 Z2 z3-i G p1 P2 z3^2$$

$$\text{In}[*]:= \text{dz3} := 2 * D[H, P3]$$

$$\text{In}[*]:= \text{dz3}$$

$$\text{Out}[*]= 2\left(-\frac{p3}{4}-\frac{i p1 z3}{4}+g p2 z2 Z3+\frac{1}{2} i g p1 z2^2 Z3\right)$$

$$\text{In}[*]:= \text{Expand}\left[2\left(-\frac{p3}{4}-\frac{i p1 z3}{4}+g p2 z2 Z3+\frac{1}{2} i g p1 z2^2 Z3\right)\right]$$

$$\text{Out}[*]= -\frac{p3}{2}-\frac{i p1 z3}{2}+2 g p2 z2 Z3+i g p1 z2^2 Z3$$

$$\text{In}[*]:= \text{Collect}[\%, p1]$$

$$\text{Out}[*]= -\frac{p3}{2}+2 g p2 z2 Z3+p1\left(-\frac{i z3}{2}+i g z2^2 Z3\right)$$

$$\text{In}[*]:= \text{dp3} := -2 * D[H, Z3]$$

$$\text{In}[*]:= \text{dp3}$$

$$\text{Out}[*]= -2\left(\frac{i p1 p3}{4}+g p2 P3 z2+\frac{1}{2} i g p1 P3 z2^2-\frac{p1^2 z3}{4}-i g p1 p2 z2 Z3\right)$$

$$\text{In}[*]:= \text{Expand}\left[-2\left(\frac{i p1 p3}{4}+g p2 P3 z2+\frac{1}{2} i g p1 P3 z2^2-\frac{p1^2 z3}{4}-i g p1 p2 z2 Z3\right)\right]$$

$$\text{Out}[*]= -\frac{1}{2} i p1 p3-2 g p2 P3 z2-i g p1 P3 z2^2+\frac{p1^2 z3}{2}+2 i g p1 p2 z2 Z3$$

$$\text{In}[*]:= \text{z2st} := s * \text{Exp}[I * t] + s^3 * v2$$

In[]:= **z2st**

Out[]:= $e^{i t} s + s^3 v2$

In[]:= **p2st := s * w21 + s^3 * w23**

In[]:= **p2st**

Out[]:= $s w21 + s^3 w23$

In[]:= **p1 := -1**

In[]:= **H**

Out[]:=
$$-2 p0 - \frac{p2 P2}{4} - \frac{p3 P3}{4} + \frac{i P2 z2}{4} - \frac{i p2 Z2}{4} - \frac{z2 Z2}{4} + \frac{i P3 z3}{4} + G P2 p3 Z2 z3 + \frac{1}{2} i G p3 Z2^2 z3 - \frac{1}{2} i G P2 Z2 z3^2 - \frac{i p3 Z3}{4} + g p2 P3 z2 Z3 - \frac{1}{2} i g P3 z2^2 Z3 - \frac{z3 Z3}{4} + \frac{1}{2} i g p2 z2 Z3^2$$

In[]:= **dz2 /. {z2 → z2st, Z2 → s * Exp[-I * t] + s^3 * V2, p2 → p2st, P2 → s * W21 + s^3 * W23}**

Out[]:=
$$2 \left(\frac{1}{4} i (e^{i t} s + s^3 v2) + \frac{1}{4} (-s w21 - s^3 w23) + G p3 (e^{-i t} s + s^3 V2) z3 - \frac{1}{2} i G (e^{-i t} s + s^3 V2) z3^2 \right)$$

In[]:= **Expand[2 (**
$$\frac{1}{4} i (e^{i t} s + s^3 v2) + \frac{1}{4} (-s w21 - s^3 w23) + G p3 (e^{-i t} s + s^3 V2) z3 - \frac{1}{2} i G (e^{-i t} s + s^3 V2) z3^2$$
)]

Out[]:=
$$\frac{1}{2} i e^{i t} s + \frac{1}{2} i s^3 v2 - \frac{s w21}{2} - \frac{s^3 w23}{2} + 2 e^{-i t} G p3 s z3 + 2 G p3 s^3 V2 z3 - i e^{-i t} G s z3^2 - i G s^3 V2 z3^2$$

In[]:= **Collect[%, s]**

Out[]:=
$$s \left(\frac{1}{2} i e^{i t} - \frac{w21}{2} + 2 e^{-i t} G p3 z3 - i e^{-i t} G z3^2 \right) + s^3 \left(\frac{i v2}{2} - \frac{w23}{2} + 2 G p3 V2 z3 - i G V2 z3^2 \right)$$

In[]:= **z3st := c * s + s^3 * v3**

In[]:= **p3st := s * w31 + s^3 * w33**

In[]:= **dz2 /. {z2 → z2st, Z2 → s * Exp[-I * t] + s^3 * V2, p2 → p2st, P2 → s * W21 + s^3 * W23, z3 → z3st, Z3 → k * s + s^3 * V3, p3 → p3st, P3 → s * W31 + s^3 * W33}**

Out[]:=
$$2 \left(\frac{1}{4} i (e^{i t} s + s^3 v2) - \frac{1}{2} i G (e^{-i t} s + s^3 V2) (c s + s^3 v3)^2 + \frac{1}{4} (-s w21 - s^3 w23) + G (e^{-i t} s + s^3 V2) (c s + s^3 v3) (s w31 + s^3 w33) \right)$$

$$\text{In}[*]:= \text{Expand}\left[2\left(\frac{1}{4}\mathfrak{i}\left(\mathfrak{e}^{\mathfrak{i}t}s+s^3v2\right)-\frac{1}{2}\mathfrak{i}G\left(\mathfrak{e}^{-\mathfrak{i}t}s+s^3V2\right)\left(cs+s^3v3\right)^2+\right.\right. \\ \left.\left.\frac{1}{4}\left(-sw21-s^3w23\right)+G\left(\mathfrak{e}^{-\mathfrak{i}t}s+s^3V2\right)\left(cs+s^3v3\right)\left(sw31+s^3w33\right)\right)\right]$$

$$\text{Out}[*]= \frac{1}{2}\mathfrak{i}\mathfrak{e}^{\mathfrak{i}t}s-\mathfrak{i}c^2\mathfrak{e}^{-\mathfrak{i}t}Gs^3+\frac{1}{2}\mathfrak{i}s^3v2-\mathfrak{i}c^2Gs^5V2-2\mathfrak{i}c\mathfrak{e}^{-\mathfrak{i}t}Gs^5v3- \\ 2\mathfrak{i}cGs^7V2v3-\mathfrak{i}\mathfrak{e}^{-\mathfrak{i}t}Gs^7v3^2-\mathfrak{i}Gs^9V2v3^2-\frac{sw21}{2}-\frac{s^3w23}{2}+ \\ 2c\mathfrak{e}^{-\mathfrak{i}t}Gs^3w31+2cGs^5V2w31+2\mathfrak{e}^{-\mathfrak{i}t}Gs^5v3w31+2Gs^7V2v3w31+ \\ 2c\mathfrak{e}^{-\mathfrak{i}t}Gs^5w33+2cGs^7V2w33+2\mathfrak{e}^{-\mathfrak{i}t}Gs^7v3w33+2Gs^9V2v3w33$$

$$\text{In}[*]:= \text{Collect}[\%, s]$$

$$\text{Out}[*]= s\left(\frac{1}{2}\mathfrak{i}\mathfrak{e}^{\mathfrak{i}t}-\frac{w21}{2}\right)+s^3\left(-\mathfrak{i}c^2\mathfrak{e}^{-\mathfrak{i}t}G+\frac{\mathfrak{i}v2}{2}-\frac{w23}{2}+2c\mathfrak{e}^{-\mathfrak{i}t}Gw31\right)+ \\ s^5\left(-\mathfrak{i}c^2GV2-2\mathfrak{i}c\mathfrak{e}^{-\mathfrak{i}t}Gv3+2cGV2w31+2\mathfrak{e}^{-\mathfrak{i}t}Gv3w31+2c\mathfrak{e}^{-\mathfrak{i}t}Gw33\right)+ \\ s^7\left(-2\mathfrak{i}cGV2v3-\mathfrak{i}\mathfrak{e}^{-\mathfrak{i}t}Gv3^2+2GV2v3w31+2cGV2w33+2\mathfrak{e}^{-\mathfrak{i}t}Gv3w33\right)+ \\ s^9\left(-\mathfrak{i}GV2v3^2+2GV2v3w33\right)$$

$$\text{In}[*]:= \text{dp2} /. \{z2 \rightarrow z2st, Z2 \rightarrow s * \text{Exp}[-I * t] + s^3 * V2, \\ p2 \rightarrow p2st, P2 \rightarrow s * W21 + s^3 * W23, z3 \rightarrow z3st, \\ Z3 \rightarrow k * s + s^3 * V3, p3 \rightarrow p3st, P3 \rightarrow s * W31 + s^3 * W33\}$$

$$\text{Out}[*]= -2\left(\frac{1}{4}\left(-\mathfrak{e}^{\mathfrak{i}t}s-s^3v2\right)-\frac{1}{4}\mathfrak{i}\left(sw21+s^3w23\right)-\right. \\ \left.\frac{1}{2}\mathfrak{i}G\left(cs+s^3v3\right)^2\left(sw21+s^3w23\right)+\mathfrak{i}G\left(\mathfrak{e}^{-\mathfrak{i}t}s+s^3V2\right)\left(cs+s^3v3\right)\left(sw31+s^3w33\right)+\right. \\ \left.G\left(cs+s^3v3\right)\left(sw21+s^3w23\right)\left(sw31+s^3w33\right)\right)$$

$$\text{In}[*]:= \text{Expand}\left[-2\left(\frac{1}{4}\left(-\mathfrak{e}^{\mathfrak{i}t}s-s^3v2\right)-\frac{1}{4}\mathfrak{i}\left(sw21+s^3w23\right)-\right.\right. \\ \left.\left.\frac{1}{2}\mathfrak{i}G\left(cs+s^3v3\right)^2\left(sw21+s^3w23\right)+\mathfrak{i}G\left(\mathfrak{e}^{-\mathfrak{i}t}s+s^3V2\right)\left(cs+s^3v3\right)\left(sw31+s^3w33\right)+\right.\right. \\ \left.\left.G\left(cs+s^3v3\right)\left(sw21+s^3w23\right)\left(sw31+s^3w33\right)\right)\right]$$

$$\text{Out}[*]= \frac{1}{2}\mathfrak{e}^{\mathfrak{i}t}s+\frac{s^3v2}{2}+\frac{\mathfrak{i}sw21}{2}+\mathfrak{i}c^2Gs^3W21+2\mathfrak{i}cGs^5v3W21+\mathfrak{i}Gs^7v3^2W21+\frac{1}{2}\mathfrak{i}s^3w23+ \\ \mathfrak{i}c^2Gs^5W23+2\mathfrak{i}cGs^7v3W23+\mathfrak{i}Gs^9v3^2W23-2\mathfrak{i}c\mathfrak{e}^{-\mathfrak{i}t}Gs^3w31-2\mathfrak{i}cGs^5V2w31- \\ 2\mathfrak{i}\mathfrak{e}^{-\mathfrak{i}t}Gs^5v3w31-2\mathfrak{i}Gs^7V2v3w31-2cGs^3W21w31-2Gs^5v3W21w31-2cGs^5W23w31- \\ 2Gs^7v3W23w31-2\mathfrak{i}c\mathfrak{e}^{-\mathfrak{i}t}Gs^5w33-2\mathfrak{i}cGs^7V2w33-2\mathfrak{i}\mathfrak{e}^{-\mathfrak{i}t}Gs^7v3w33- \\ 2\mathfrak{i}Gs^9V2v3w33-2cGs^5W21w33-2Gs^7v3W21w33-2cGs^7W23w33-2Gs^9v3W23w33$$

In[]:= **Collect**[% , s]

$$\begin{aligned} \text{Out[]} = & s \left(\frac{e^{it}}{2} + \frac{i w_{21}}{2} \right) + s^3 \left(\frac{v_2}{2} + i c^2 G W_{21} + \frac{i w_{23}}{2} - 2 i c e^{-it} G w_{31} - 2 c G W_{21} w_{31} \right) + \\ & s^5 \left(2 i c G v_3 W_{21} + i c^2 G W_{23} - 2 i c G V_2 w_{31} - 2 i e^{-it} G v_3 w_{31} - \right. \\ & \quad \left. 2 G v_3 W_{21} w_{31} - 2 c G W_{23} w_{31} - 2 i c e^{-it} G w_{33} - 2 c G W_{21} w_{33} \right) + \\ & s^7 \left(i G v_3^2 W_{21} + 2 i c G v_3 W_{23} - 2 i G V_2 v_3 w_{31} - 2 G v_3 W_{23} w_{31} - \right. \\ & \quad \left. 2 i c G V_2 w_{33} - 2 i e^{-it} G v_3 w_{33} - 2 G v_3 W_{21} w_{33} - 2 c G W_{23} w_{33} \right) + \\ & s^9 \left(i G v_3^2 W_{23} - 2 i G V_2 v_3 w_{33} - 2 G v_3 W_{23} w_{33} \right) \end{aligned}$$

In[]:= **w21** := **-I * Exp[I * t]**

In[]:= **dz2**

$$\text{Out[]} = 2 \left(-\frac{p_2}{4} + \frac{i z_2}{4} + G p_3 Z_2 z_3 - \frac{1}{2} i G Z_2 z_3^2 \right)$$

$$\text{In[]} = s \left(\frac{1}{2} i e^{it} - \frac{w_{21}}{2} \right) + s^3 \left(-i c^2 e^{-it} G + \frac{i v_2}{2} - \frac{w_{23}}{2} + 2 c e^{-it} G w_{31} \right)$$

$$\text{Out[]} = i e^{it} s + s^3 \left(-i c^2 e^{-it} G + \frac{i v_2}{2} - \frac{w_{23}}{2} + 2 c e^{-it} G w_{31} \right)$$

$$\text{In[]} = s \left(\frac{e^{it}}{2} + \frac{i w_{21}}{2} \right) + s^3 \left(\frac{v_2}{2} + i c^2 G W_{21} + \frac{i w_{23}}{2} - 2 i c e^{-it} G w_{31} - 2 c G W_{21} w_{31} \right)$$

$$\text{Out[]} = e^{it} s + s^3 \left(\frac{v_2}{2} + i c^2 G W_{21} + \frac{i w_{23}}{2} - 2 i c e^{-it} G w_{31} - 2 c G W_{21} w_{31} \right)$$

In[]:= **W21** := **I * Exp[-I * t]**

In[]:= **dz3 /. {z2 → z2st, Z2 → s * Exp[-I * t] + s^3 * V2,**
p2 → p2st, P2 → s * W21 + s^3 * W23, z3 → z3st,
Z3 → k * s + s^3 * V3, p3 → p3st, P3 → s * W31 + s^3 * W33}

$$\begin{aligned} \text{Out[]} = & 2 \left(\frac{1}{4} i (c s + s^3 v_3) - \frac{1}{2} i g (e^{it} s + s^3 v_2)^2 (k s + s^3 V_3) + \right. \\ & \quad \left. g (e^{it} s + s^3 v_2) (k s + s^3 V_3) (-i e^{it} s + s^3 w_{23}) + \frac{1}{4} (-s w_{31} - s^3 w_{33}) \right) \end{aligned}$$

$$\begin{aligned} \text{In[]} = & \text{Expand} \left[2 \left(\frac{1}{4} i (c s + s^3 v_3) - \frac{1}{2} i g (e^{it} s + s^3 v_2)^2 (k s + s^3 V_3) + \right. \right. \\ & \quad \left. \left. g (e^{it} s + s^3 v_2) (k s + s^3 V_3) (-i e^{it} s + s^3 w_{23}) + \frac{1}{4} (-s w_{31} - s^3 w_{33}) \right) \right] \end{aligned}$$

$$\begin{aligned} \text{Out[]} = & \frac{i c s}{2} - 3 i e^{2it} g k s^3 - 4 i e^{it} g k s^5 v_2 - i g k s^7 v_2^2 + \frac{1}{2} i s^3 v_3 - \\ & 3 i e^{2it} g s^5 V_3 - 4 i e^{it} g s^7 v_2 V_3 - i g s^9 v_2^2 V_3 + 2 e^{it} g k s^5 w_{23} + \\ & 2 g k s^7 v_2 w_{23} + 2 e^{it} g s^7 V_3 w_{23} + 2 g s^9 v_2 V_3 w_{23} - \frac{s w_{31}}{2} - \frac{s^3 w_{33}}{2} \end{aligned}$$

In[8]:= Collect[%, s]

$$\begin{aligned} \text{Out[8]} = & s^5 \left(-4 i e^{i t} g k v2 - 3 i e^{2 i t} g V3 + 2 e^{i t} g k w23 \right) + \\ & s^7 \left(-i g k v2^2 - 4 i e^{i t} g v2 V3 + 2 g k v2 w23 + 2 e^{i t} g V3 w23 \right) + \\ & s^9 \left(-i g v2^2 V3 + 2 g v2 V3 w23 \right) + s \left(\frac{i c}{2} - \frac{w31}{2} \right) + s^3 \left(-3 i e^{2 i t} g k + \frac{i v3}{2} - \frac{w33}{2} \right) \end{aligned}$$

In[9]:= dp3 /. {z2 → z2st, Z2 → s * Exp[-I * t] + s^3 * V2,
p2 → p2st, P2 → s * W21 + s^3 * W23, z3 → z3st,
Z3 → k * s + s^3 * V3, p3 → p3st, P3 → s * W31 + s^3 * W33}

$$\begin{aligned} \text{Out[9]} = & -2 \left(\frac{1}{4} \left(-c s - s^3 v3 \right) + i g \left(e^{i t} s + s^3 v2 \right) \left(k s + s^3 V3 \right) \left(-i e^{i t} s + s^3 w23 \right) - \frac{1}{4} i \left(s w31 + s^3 w33 \right) - \right. \\ & \left. \frac{1}{2} i g \left(e^{i t} s + s^3 v2 \right)^2 \left(s w31 + s^3 w33 \right) + g \left(e^{i t} s + s^3 v2 \right) \left(-i e^{i t} s + s^3 w23 \right) \left(s w31 + s^3 w33 \right) \right) \end{aligned}$$

In[10]:= Expand[%99]

$$\begin{aligned} \text{Out[10]} = & \frac{c s}{2} - 2 e^{2 i t} g k s^3 - 2 e^{i t} g k s^5 v2 + \frac{s^3 v3}{2} - 2 e^{2 i t} g s^5 V3 - 2 e^{i t} g s^7 v2 V3 - 2 i e^{i t} g k s^5 w23 - \\ & 2 i g k s^7 v2 w23 - 2 i e^{i t} g s^7 V3 w23 - 2 i g s^9 v2 V3 w23 + \frac{i s w31}{2} + 3 i e^{2 i t} g s^3 W31 + \\ & 4 i e^{i t} g s^5 v2 W31 + i g s^7 v2^2 W31 - 2 e^{i t} g s^5 w23 W31 - 2 g s^7 v2 w23 W31 + \frac{1}{2} i s^3 w33 + \\ & 3 i e^{2 i t} g s^5 W33 + 4 i e^{i t} g s^7 v2 W33 + i g s^9 v2^2 W33 - 2 e^{i t} g s^7 w23 W33 - 2 g s^9 v2 w23 W33 \end{aligned}$$

In[11]:= Collect[%, s]

$$\begin{aligned} \text{Out[11]} = & s \left(\frac{c}{2} + \frac{i w31}{2} \right) + s^3 \left(-2 e^{2 i t} g k + \frac{v3}{2} + 3 i e^{2 i t} g W31 + \frac{i w33}{2} \right) + \\ & s^5 \left(-2 e^{i t} g k v2 - 2 e^{2 i t} g V3 - 2 i e^{i t} g k w23 + \right. \\ & \left. 4 i e^{i t} g v2 W31 - 2 e^{i t} g w23 W31 + 3 i e^{2 i t} g W33 \right) + \\ & s^7 \left(-2 e^{i t} g v2 V3 - 2 i g k v2 w23 - 2 i e^{i t} g V3 w23 + i g v2^2 W31 - 2 g v2 w23 W31 + \right. \\ & \left. 4 i e^{i t} g v2 W33 - 2 e^{i t} g w23 W33 \right) + s^9 \left(-2 i g v2 V3 w23 + i g v2^2 W33 - 2 g v2 w23 W33 \right) \end{aligned}$$

In[12]:= w31 := I * c

In[13]:= W31 := -I * k

In[14]:= dz3 /. {z2 → z2st, Z2 → s * Exp[-I * t] + s^3 * V2,
p2 → p2st, P2 → s * W21 + s^3 * W23, z3 → z3st,
Z3 → k * s + s^3 * V3, p3 → p3st, P3 → s * W31 + s^3 * W33}

$$\begin{aligned} \text{Out[14]} = & 2 \left(\frac{1}{4} i \left(c s + s^3 v3 \right) - \frac{1}{2} i g \left(e^{i t} s + s^3 v2 \right)^2 \left(k s + s^3 V3 \right) + \right. \\ & \left. g \left(e^{i t} s + s^3 v2 \right) \left(k s + s^3 V3 \right) \left(-i e^{i t} s + s^3 w23 \right) + \frac{1}{4} \left(-i c s - s^3 w33 \right) \right) \end{aligned}$$

$$\begin{aligned} \text{In}[*]:= & \text{Expand}\left[2\left(\frac{1}{4}\mathfrak{i}\left(\mathfrak{c}\mathfrak{s}+\mathfrak{s}^3\mathfrak{v}3\right)-\frac{1}{2}\mathfrak{i}\mathfrak{g}\left(\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{s}+\mathfrak{s}^3\mathfrak{v}2\right)^2\left(\mathfrak{k}\mathfrak{s}+\mathfrak{s}^3\mathfrak{V}3\right)+\right.\right. \\ & \left.\left.\mathfrak{g}\left(\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{s}+\mathfrak{s}^3\mathfrak{v}2\right)\left(\mathfrak{k}\mathfrak{s}+\mathfrak{s}^3\mathfrak{V}3\right)\left(-\mathfrak{i}\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{s}+\mathfrak{s}^3\mathfrak{w}23\right)+\frac{1}{4}\left(-\mathfrak{i}\mathfrak{c}\mathfrak{s}-\mathfrak{s}^3\mathfrak{w}33\right)\right)\right] \\ \text{Out}[*]= & -3\mathfrak{i}\mathfrak{e}^{2\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{k}\mathfrak{s}^3-4\mathfrak{i}\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{k}\mathfrak{s}^5\mathfrak{v}2-\mathfrak{i}\mathfrak{g}\mathfrak{k}\mathfrak{s}^7\mathfrak{v}2^2+\frac{1}{2}\mathfrak{i}\mathfrak{s}^3\mathfrak{v}3-3\mathfrak{i}\mathfrak{e}^{2\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{s}^5\mathfrak{V}3-4\mathfrak{i}\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{s}^7\mathfrak{v}2\mathfrak{V}3- \\ & \mathfrak{i}\mathfrak{g}\mathfrak{s}^9\mathfrak{v}2^2\mathfrak{V}3+2\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{k}\mathfrak{s}^5\mathfrak{w}23+2\mathfrak{g}\mathfrak{k}\mathfrak{s}^7\mathfrak{v}2\mathfrak{w}23+2\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{s}^7\mathfrak{V}3\mathfrak{w}23+2\mathfrak{g}\mathfrak{s}^9\mathfrak{v}2\mathfrak{V}3\mathfrak{w}23-\frac{\mathfrak{s}^3\mathfrak{w}33}{2} \end{aligned}$$

In[*]:= Collect[%, s]

$$\begin{aligned} \text{Out}[*]= & \mathfrak{s}^5\left(-4\mathfrak{i}\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{k}\mathfrak{v}2-3\mathfrak{i}\mathfrak{e}^{2\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{V}3+2\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{k}\mathfrak{w}23\right)+ \\ & \mathfrak{s}^7\left(-\mathfrak{i}\mathfrak{g}\mathfrak{k}\mathfrak{v}2^2-4\mathfrak{i}\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{v}2\mathfrak{V}3+2\mathfrak{g}\mathfrak{k}\mathfrak{v}2\mathfrak{w}23+2\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{V}3\mathfrak{w}23\right)+ \\ & \mathfrak{s}^9\left(-\mathfrak{i}\mathfrak{g}\mathfrak{v}2^2\mathfrak{V}3+2\mathfrak{g}\mathfrak{v}2\mathfrak{V}3\mathfrak{w}23\right)+\mathfrak{s}^3\left(-3\mathfrak{i}\mathfrak{e}^{2\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{k}+\frac{\mathfrak{i}\mathfrak{v}3}{2}-\frac{\mathfrak{w}33}{2}\right) \end{aligned}$$

**In[*]:= dp3 /. {z2 → z2st, Z2 → s*Exp[-I*t] + s^3*V2,
p2 → p2st, P2 → s*W21 + s^3*W23, z3 → z3st,
Z3 → k*s + s^3*V3, p3 → p3st, P3 → s*W31 + s^3*W33}**

$$\begin{aligned} \text{Out}[*]= & -2\left(\frac{1}{4}\left(-\mathfrak{c}\mathfrak{s}-\mathfrak{s}^3\mathfrak{v}3\right)+\mathfrak{i}\mathfrak{g}\left(\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{s}+\mathfrak{s}^3\mathfrak{v}2\right)\left(\mathfrak{k}\mathfrak{s}+\mathfrak{s}^3\mathfrak{V}3\right)\left(-\mathfrak{i}\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{s}+\mathfrak{s}^3\mathfrak{w}23\right)-\right. \\ & \frac{1}{4}\mathfrak{i}\left(\mathfrak{i}\mathfrak{c}\mathfrak{s}+\mathfrak{s}^3\mathfrak{w}33\right)-\frac{1}{2}\mathfrak{i}\mathfrak{g}\left(\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{s}+\mathfrak{s}^3\mathfrak{v}2\right)^2\left(-\mathfrak{i}\mathfrak{k}\mathfrak{s}+\mathfrak{s}^3\mathfrak{W}33\right)+ \\ & \left.\mathfrak{g}\left(\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{s}+\mathfrak{s}^3\mathfrak{v}2\right)\left(-\mathfrak{i}\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{s}+\mathfrak{s}^3\mathfrak{w}23\right)\left(-\mathfrak{i}\mathfrak{k}\mathfrak{s}+\mathfrak{s}^3\mathfrak{W}33\right)\right) \end{aligned}$$

In[*]:= Expand[%107]

$$\begin{aligned} \text{Out}[*]= & \mathfrak{e}^{2\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{k}\mathfrak{s}^3+2\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{k}\mathfrak{s}^5\mathfrak{v}2+\mathfrak{g}\mathfrak{k}\mathfrak{s}^7\mathfrak{v}2^2+\frac{\mathfrak{s}^3\mathfrak{v}3}{2}-2\mathfrak{e}^{2\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{s}^5\mathfrak{V}3-2\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{s}^7\mathfrak{v}2\mathfrak{V}3- \\ & 2\mathfrak{i}\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{s}^7\mathfrak{V}3\mathfrak{w}23-2\mathfrak{i}\mathfrak{g}\mathfrak{s}^9\mathfrak{v}2\mathfrak{V}3\mathfrak{w}23+\frac{1}{2}\mathfrak{i}\mathfrak{s}^3\mathfrak{w}33+3\mathfrak{i}\mathfrak{e}^{2\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{s}^5\mathfrak{W}33+ \\ & 4\mathfrak{i}\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{s}^7\mathfrak{v}2\mathfrak{W}33+\mathfrak{i}\mathfrak{g}\mathfrak{s}^9\mathfrak{v}2^2\mathfrak{W}33-2\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{s}^7\mathfrak{w}23\mathfrak{W}33-2\mathfrak{g}\mathfrak{s}^9\mathfrak{v}2\mathfrak{w}23\mathfrak{W}33 \end{aligned}$$

In[*]:= Collect[%, s]

$$\begin{aligned} \text{Out}[*]= & \mathfrak{s}^3\left(\mathfrak{e}^{2\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{k}+\frac{\mathfrak{v}3}{2}+\frac{\mathfrak{i}\mathfrak{w}33}{2}\right)+\mathfrak{s}^5\left(2\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{k}\mathfrak{v}2-2\mathfrak{e}^{2\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{V}3+3\mathfrak{i}\mathfrak{e}^{2\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{W}33\right)+ \\ & \mathfrak{s}^7\left(\mathfrak{g}\mathfrak{k}\mathfrak{v}2^2-2\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{v}2\mathfrak{V}3-2\mathfrak{i}\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{V}3\mathfrak{w}23+4\mathfrak{i}\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{v}2\mathfrak{W}33-2\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{g}\mathfrak{w}23\mathfrak{W}33\right)+ \\ & \mathfrak{s}^9\left(-2\mathfrak{i}\mathfrak{g}\mathfrak{v}2\mathfrak{V}3\mathfrak{w}23+\mathfrak{i}\mathfrak{g}\mathfrak{v}2^2\mathfrak{W}33-2\mathfrak{g}\mathfrak{v}2\mathfrak{w}23\mathfrak{W}33\right) \end{aligned}$$

In[*]:= dz2trunc := s $\left(\frac{1}{2}\mathfrak{i}\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}-\frac{\mathfrak{w}21}{2}\right)+\mathfrak{s}^3\left(-\mathfrak{i}\mathfrak{c}^2\mathfrak{e}^{-\mathfrak{i}\mathfrak{t}}\mathfrak{G}+\frac{\mathfrak{i}\mathfrak{v}2}{2}-\frac{\mathfrak{w}23}{2}+2\mathfrak{c}\mathfrak{e}^{-\mathfrak{i}\mathfrak{t}}\mathfrak{G}\mathfrak{w}31\right)$

In[*]:= dz2trunc

$$\text{Out}[*]= \mathfrak{i}\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}\mathfrak{s}+\mathfrak{s}^3\left(\mathfrak{i}\mathfrak{c}^2\mathfrak{e}^{-\mathfrak{i}\mathfrak{t}}\mathfrak{G}+\frac{\mathfrak{i}\mathfrak{v}2}{2}-\frac{\mathfrak{w}23}{2}\right)$$

In[*]:= dp2trunc := s $\left(\frac{\mathfrak{e}^{\mathfrak{i}\mathfrak{t}}}{2}+\frac{\mathfrak{i}\mathfrak{w}21}{2}\right)+\mathfrak{s}^3\left(\frac{\mathfrak{v}2}{2}+\mathfrak{i}\mathfrak{c}^2\mathfrak{G}\mathfrak{W}21+\frac{\mathfrak{i}\mathfrak{w}23}{2}-2\mathfrak{i}\mathfrak{c}\mathfrak{e}^{-\mathfrak{i}\mathfrak{t}}\mathfrak{G}\mathfrak{w}31-2\mathfrak{c}\mathfrak{G}\mathfrak{W}21\mathfrak{w}31\right)$

In[]:= **dp2trunc**

$$\text{Out[]}:= e^{i t} s + s^3 \left(3 c^2 e^{-i t} G + \frac{v2}{2} + \frac{i w23}{2} \right)$$

$$\text{In[]}:= \text{dz3trunc} := s \left(\frac{i c}{2} - \frac{w31}{2} \right) + s^3 \left(-3 i e^{2 i t} g k + \frac{i v3}{2} - \frac{w33}{2} \right)$$

In[]:= **dz3trunc**

$$\text{Out[]}:= s^3 \left(-3 i e^{2 i t} g k + \frac{i v3}{2} - \frac{w33}{2} \right)$$

$$\text{In[]}:= \text{dp3trunc} := s^3 \left(e^{2 i t} g k + \frac{v3}{2} + \frac{i w33}{2} \right)$$

In[]:= **dp3trunc**

$$\text{Out[]}:= s^3 \left(e^{2 i t} g k + \frac{v3}{2} + \frac{i w33}{2} \right)$$

$$\text{In[]}:= \text{DSolve}[\{l'[t] == i c^2 e^{-i t} G + \frac{i l[t]}{2} - \frac{m[t]}{2},$$

$$m'[t] == 3 c^2 e^{-i t} G + \frac{l[t]}{2} + \frac{i m[t]}{2}\}, \{l[t], m[t]\}, t]$$

$$\text{Out[]}:= \left\{ \left\{ l[t] \rightarrow c^2 e^{-\frac{3 i t}{2}} (-1 + e^{i t}) G \cos\left[\frac{t}{2}\right] + e^{\frac{i t}{2}} C[1] \cos\left[\frac{t}{2}\right] - \right. \right. \\ \left. i c^2 e^{-\frac{3 i t}{2}} (1 + e^{i t}) G \sin\left[\frac{t}{2}\right] - e^{\frac{i t}{2}} C[2] \sin\left[\frac{t}{2}\right], m[t] \rightarrow i c^2 e^{-\frac{3 i t}{2}} (1 + e^{i t}) G \cos\left[\frac{t}{2}\right] + \right. \\ \left. e^{\frac{i t}{2}} C[2] \cos\left[\frac{t}{2}\right] + c^2 e^{-\frac{3 i t}{2}} (-1 + e^{i t}) G \sin\left[\frac{t}{2}\right] + e^{\frac{i t}{2}} C[1] \sin\left[\frac{t}{2}\right] \right\} \right\}$$

$$\text{In[]}:= c^2 e^{-\frac{3 i t}{2}} (-1 + e^{i t}) G \cos\left[\frac{t}{2}\right] - i c^2 e^{-\frac{3 i t}{2}} (1 + e^{i t}) G \sin\left[\frac{t}{2}\right]$$

$$\text{Out[]}:= c^2 e^{-\frac{3 i t}{2}} (-1 + e^{i t}) G \cos\left[\frac{t}{2}\right] - i c^2 e^{-\frac{3 i t}{2}} (1 + e^{i t}) G \sin\left[\frac{t}{2}\right]$$

$$\text{In[]}:= \text{TrigReduce}\left[c^2 e^{-\frac{3 i t}{2}} (-1 + e^{i t}) G \cos\left[\frac{t}{2}\right] - i c^2 e^{-\frac{3 i t}{2}} (1 + e^{i t}) G \sin\left[\frac{t}{2}\right]\right]$$

$$\text{Out[]}:= 0$$

$$\text{In[]}:= c^2 e^{-\frac{3 i t}{2}} (-1 + e^{i t}) G \cos\left[\frac{t}{2}\right] + e^{\frac{i t}{2}} C[1] \cos\left[\frac{t}{2}\right] - i c^2 e^{-\frac{3 i t}{2}} (1 + e^{i t}) G \sin\left[\frac{t}{2}\right] - e^{\frac{i t}{2}} C[2] \sin\left[\frac{t}{2}\right]$$

$$\text{Out[]}:= c^2 e^{-\frac{3 i t}{2}} (-1 + e^{i t}) G \cos\left[\frac{t}{2}\right] + e^{\frac{i t}{2}} C[1] \cos\left[\frac{t}{2}\right] - i c^2 e^{-\frac{3 i t}{2}} (1 + e^{i t}) G \sin\left[\frac{t}{2}\right] - e^{\frac{i t}{2}} C[2] \sin\left[\frac{t}{2}\right]$$

$$\text{In[]}:= \text{TrigReduce}\left[c^2 e^{-\frac{3 i t}{2}} (-1 + e^{i t}) G \cos\left[\frac{t}{2}\right] + \right.$$

$$\left. e^{\frac{i t}{2}} C[1] \cos\left[\frac{t}{2}\right] - i c^2 e^{-\frac{3 i t}{2}} (1 + e^{i t}) G \sin\left[\frac{t}{2}\right] - e^{\frac{i t}{2}} C[2] \sin\left[\frac{t}{2}\right]\right]$$

$$\text{Out[]}:= \frac{1}{2} \left(C[1] + e^{i t} C[1] - i C[2] + i e^{i t} C[2] \right)$$

$$\text{In}[*]:= \text{I} \, c^2 \, e^{-\frac{3 \text{I} t}{2}} \left(1 + e^{\text{I} t}\right) \text{G Cos}\left[\frac{t}{2}\right] + c^2 \, e^{-\frac{3 \text{I} t}{2}} \left(-1 + e^{\text{I} t}\right) \text{G Sin}\left[\frac{t}{2}\right]$$

$$\text{Out}[*]= \text{I} \, c^2 \, e^{-\frac{3 \text{I} t}{2}} \left(1 + e^{\text{I} t}\right) \text{G Cos}\left[\frac{t}{2}\right] + c^2 \, e^{-\frac{3 \text{I} t}{2}} \left(-1 + e^{\text{I} t}\right) \text{G Sin}\left[\frac{t}{2}\right]$$

$$\text{In}[*]:= \text{TrigReduce}\left[\text{I} \, c^2 \, e^{-\frac{3 \text{I} t}{2}} \left(1 + e^{\text{I} t}\right) \text{G Cos}\left[\frac{t}{2}\right] + c^2 \, e^{-\frac{3 \text{I} t}{2}} \left(-1 + e^{\text{I} t}\right) \text{G Sin}\left[\frac{t}{2}\right]\right]$$

$$\text{Out}[*]= 2 \, \text{I} \, c^2 \, e^{-\text{I} t} \text{G}$$