

# Options for Large-Eddy Simulations of Hurricane Boundary Layers in CM1 (and Other Numerical Models)

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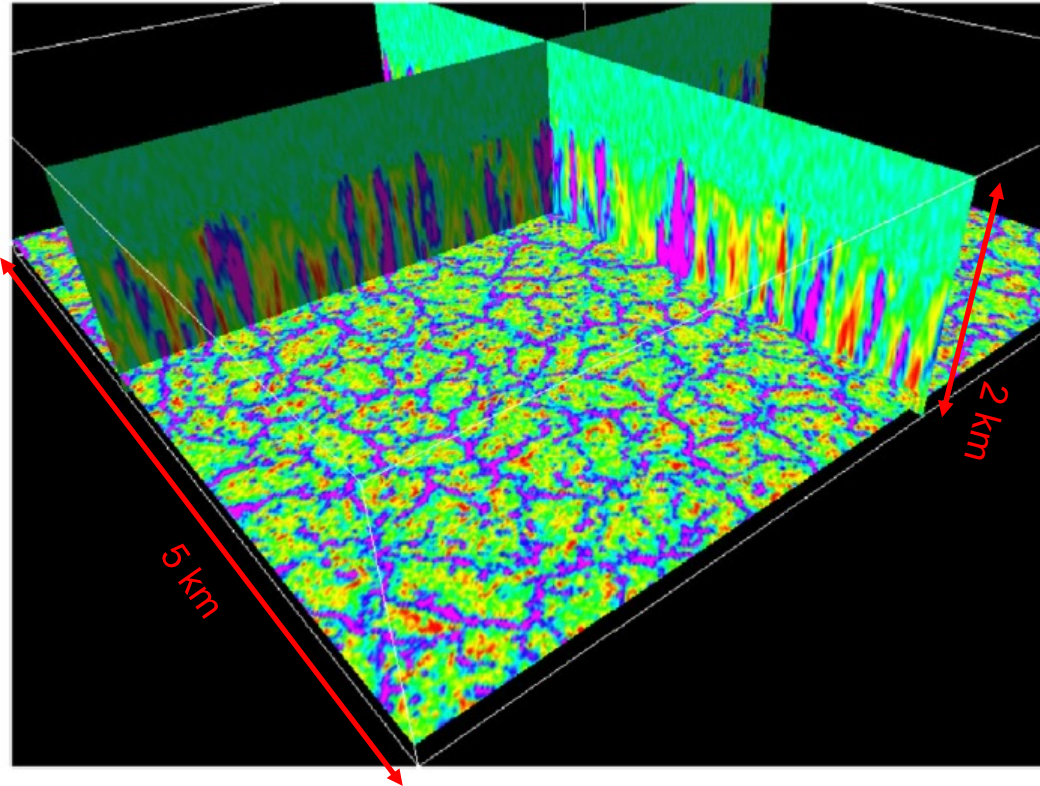
Acknowledgements: NSF PREEVENTS, ONR TCRI

(also thanks to Dan Stern, Rich Rotunno, Xiaomin Chen, ...)



# Large-Eddy Simulation (LES)

Vertical velocity, convective boundary layer



Moeng and Sullivan (2015)  
(*Encyclopedia of Atmospheric Sciences*)

- Integrate governing equations using turbulence-permitting resolution
  - $\Delta x$  of  $\sim 100$  m or less
- Advantage:
  - A more accurate representation of turbulent processes
- Disadvantages:
  - Need to account for larger scales
  - High resolution (even  $\Delta x < 10$  m) doesn't solve everything

## Three Options in CM1:

1. Small-domain, high-resolution “patch”
2. The “eddy recycling” method
3. Subgrid turbulence model

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Problem:

- Hurricanes are huge! (hundreds of km)
- So, 100 m grid spacing for ~2-day simulation requires millions of supercomputer core-hours



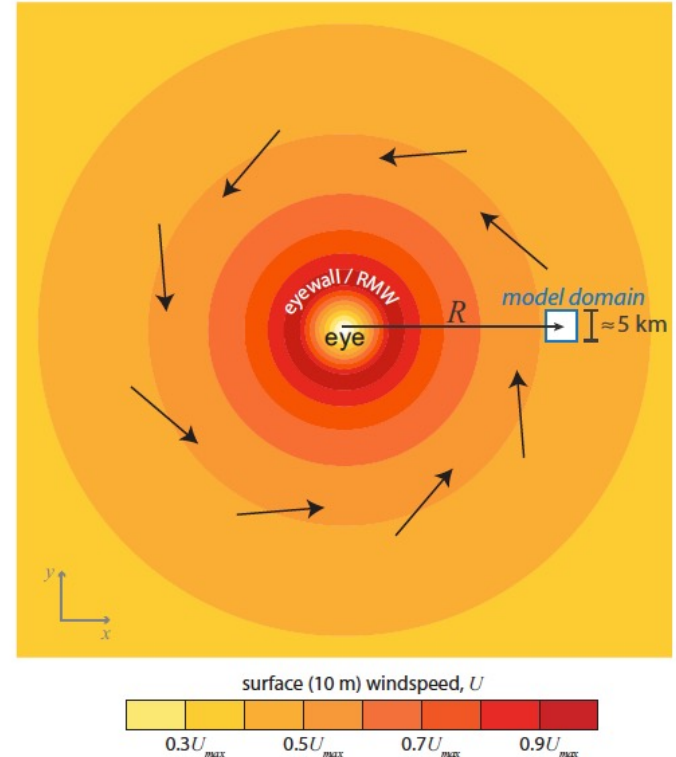
### Problem:

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### Solution:

Simulate a “patch” of the TC boundary layer





Bryan et al. (2017a, BLM)

$$\begin{aligned} \text{radial velocity: } \frac{\partial u}{\partial t} &= \dots + \langle v \rangle \frac{V}{R} + \frac{\langle u \rangle^2}{R} - \left( fV + \frac{V^2}{R} \right) \\ \text{tangential velocity: } \frac{\partial v}{\partial t} &= \dots - \langle u \rangle \frac{V}{R} - \langle u \rangle \frac{\partial V}{\partial R} \end{aligned}$$

centrifugal acceleration  
& radial advection  
& pressure-gradient acceleration

User must specify 3 terms:

- $R$  (radius from center of TC)
- $V(z)$  (“gradient wind”)
- $dV/dR(z)$  (radial gradient of  $V$ )

Caveat: applies only *outside eyewall* ( $r > \text{RMW}$ )

Chen et al. (2021, JAS)

$$\begin{aligned} \frac{\partial \theta}{\partial t} &= \dots + \frac{\theta_{\text{ref}} - \langle \theta \rangle}{\tau_n} \\ \frac{\partial q_v}{\partial t} &= \dots + \frac{q_{\text{ref}} - \langle q_v \rangle}{\tau_n} \end{aligned}$$

These “nudging” terms account crudely for radial advection, subsidence, microphysics, radiation...

User must specify vertical profiles of  $\theta$  and  $q_v$

CM1 default (LES Hurricane test case):

- $\theta$ : constant lapse rate
- $q_v$ : constant relative humidity

Angled brackets:  $\langle \rangle$  denotes horizontal average

Horizontal windspeed ( $\text{m s}^{-1}$ )  
at 100 m ASL

CM1:

$\Delta x = \Delta y = 10 \text{ m}$ ,

$\Delta z = 5 \text{ m}$

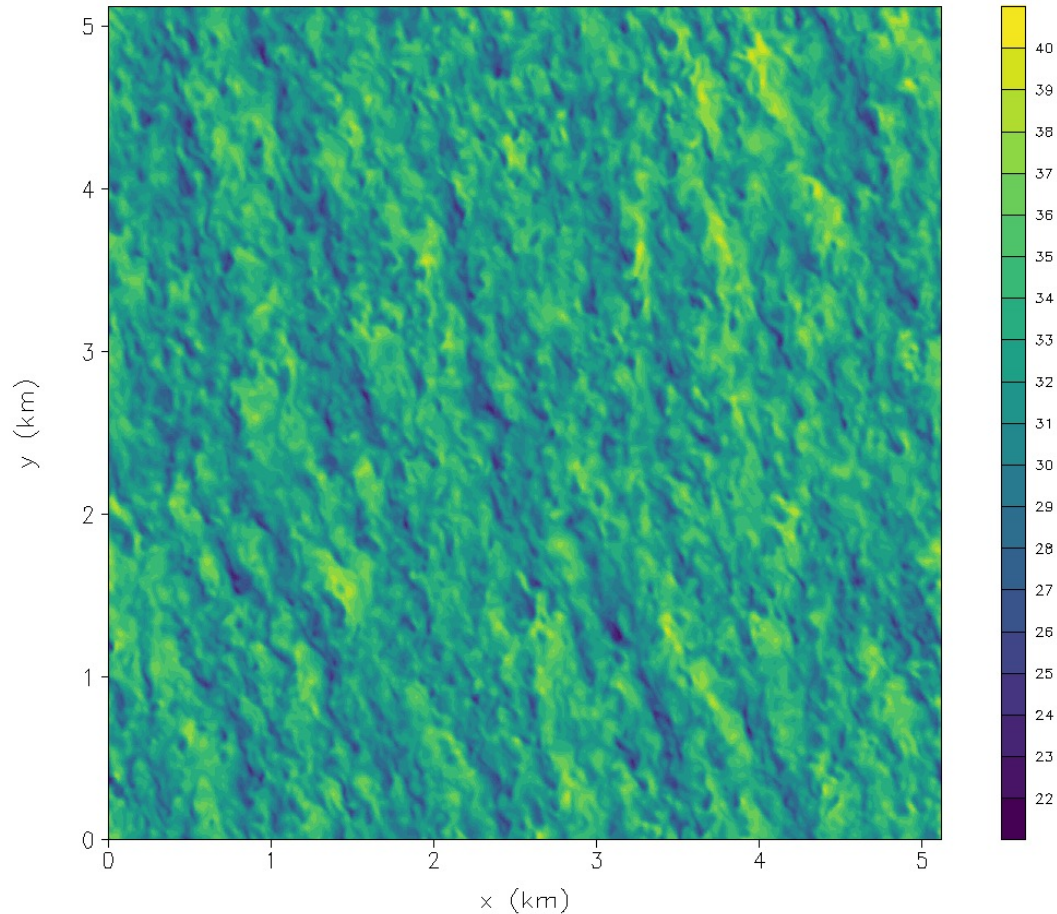
Input parameters:

$R = 40 \text{ km}$

$V = 38 \text{ m s}^{-1}$

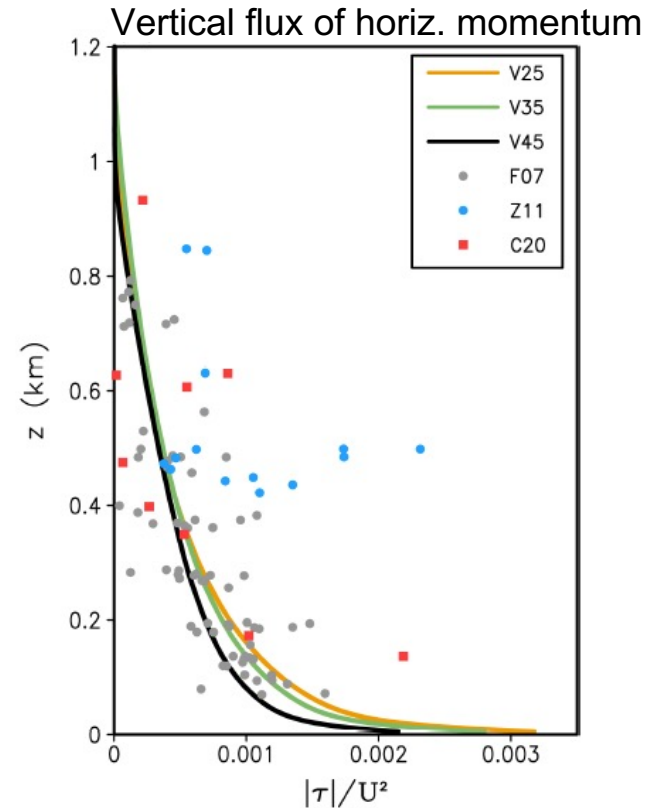
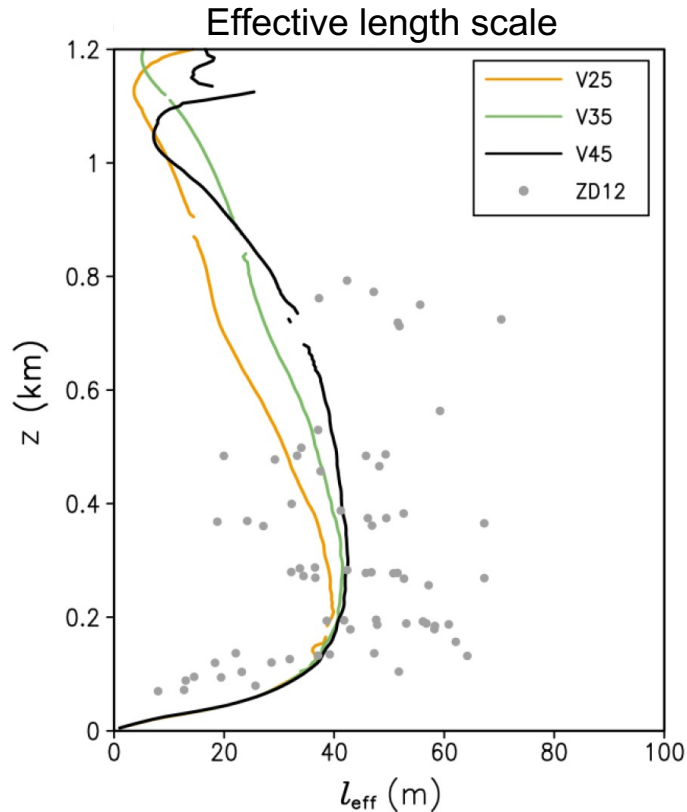
$dV/dR = -8 \times 10^{-4} \text{ s}^{-1}$

(radial decay parameter  $n = 0.8$ )



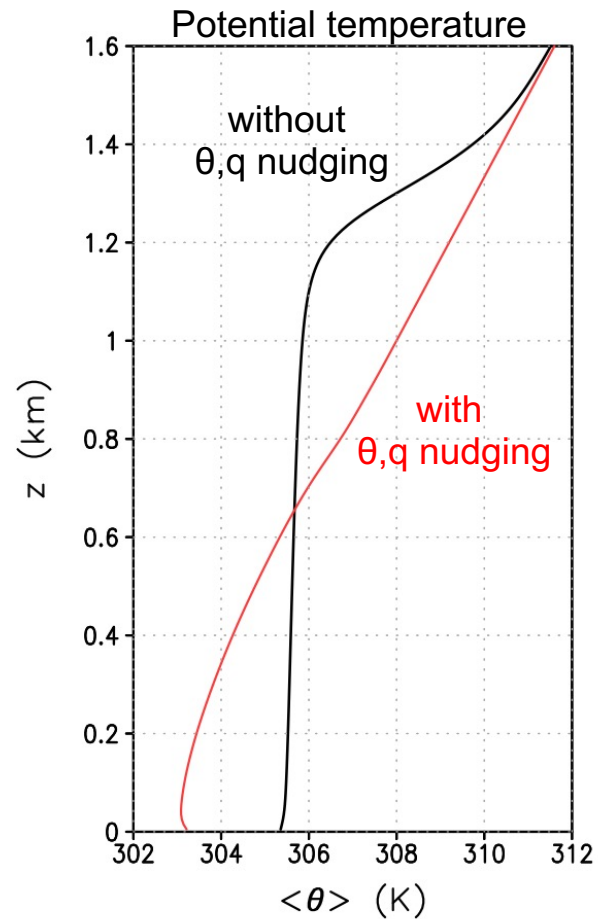
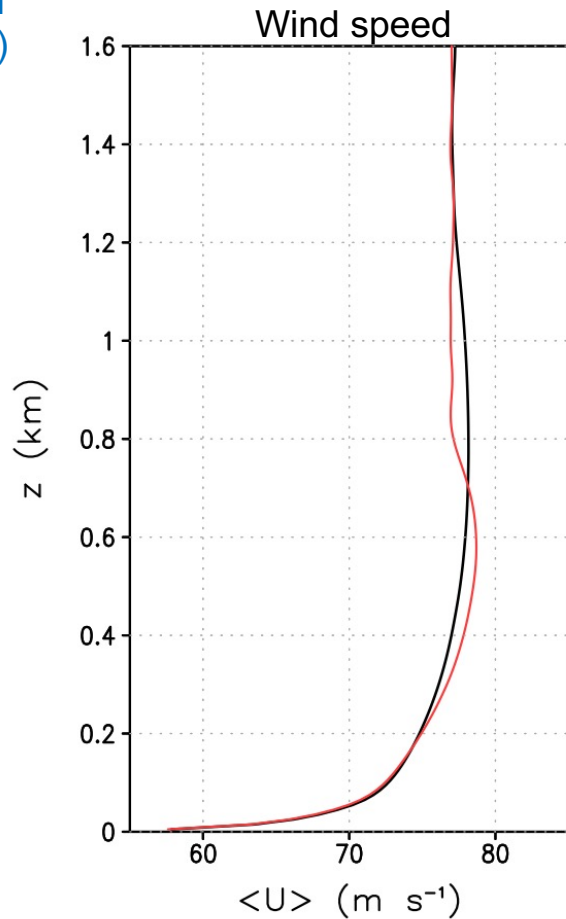


Simulations (colored lines) compare well with obs. (dots)



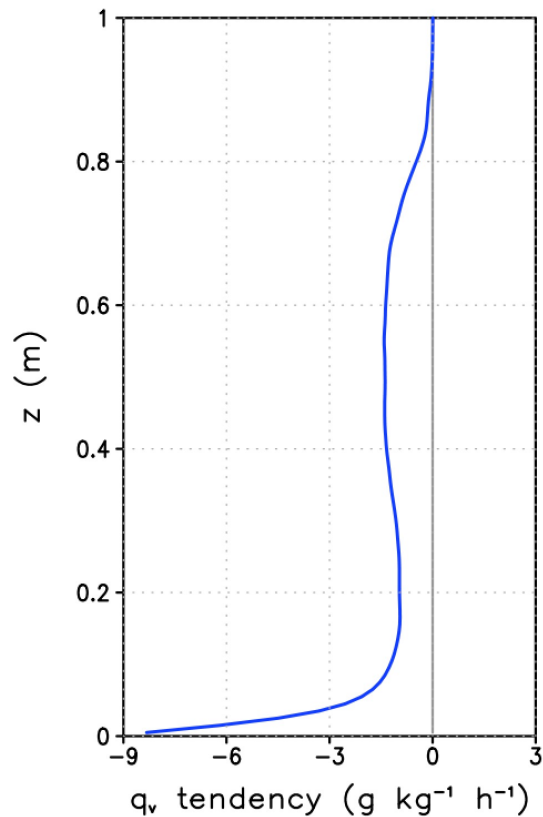
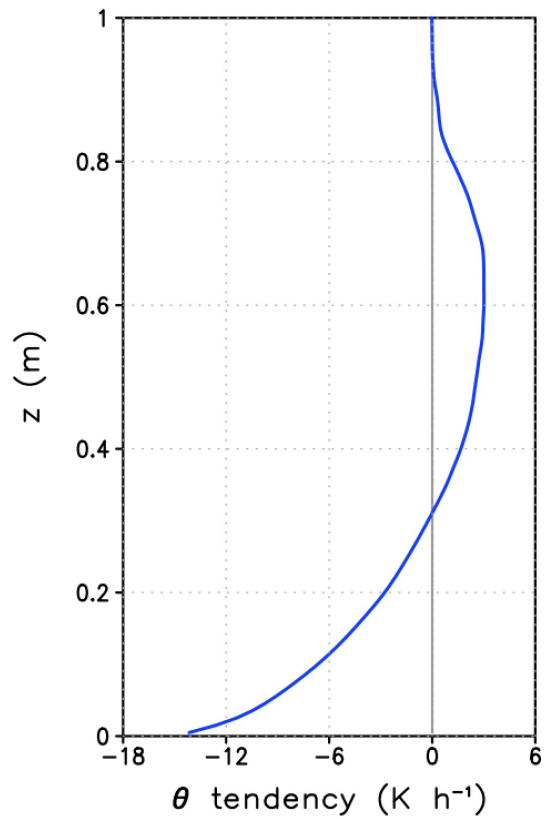
see Bryan et al. (2017a), Chen et al. (2021, JAS) (also, the next talk!)

- simulations from Chen et al. (2021)



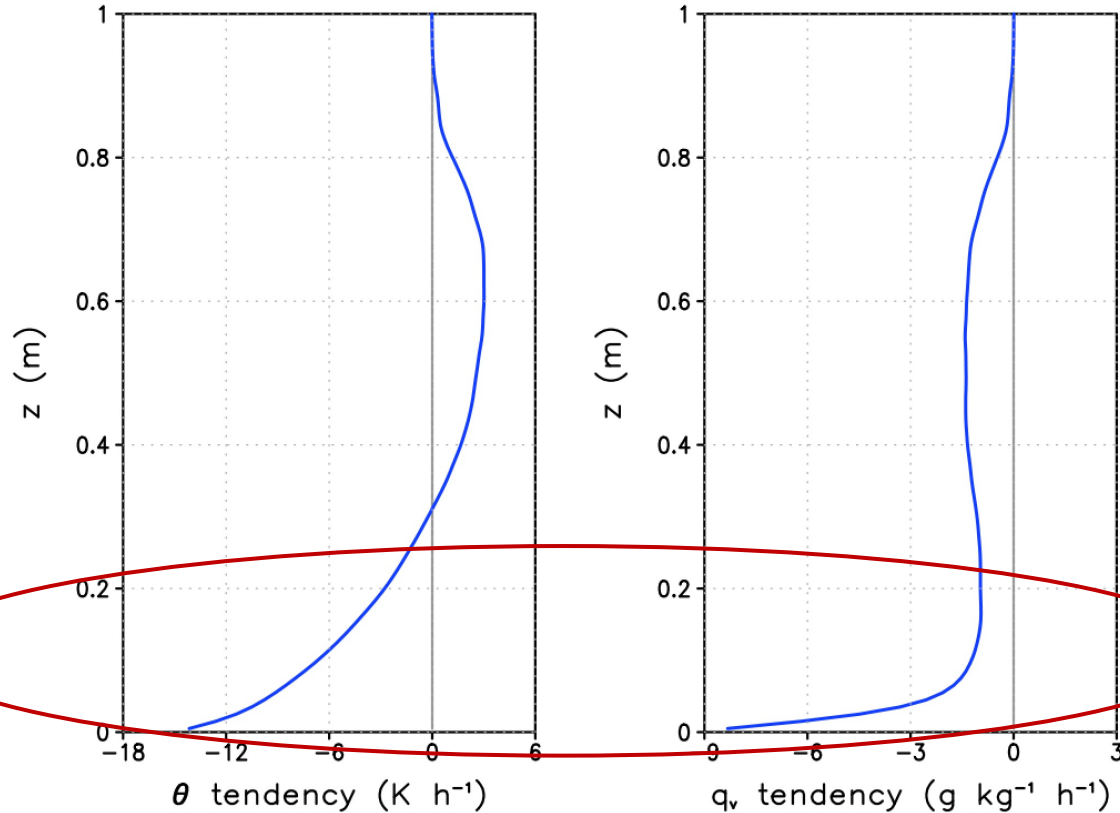
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## Nudging tendencies



- simulations from Chen et al. (2021)

## Nudging tendencies

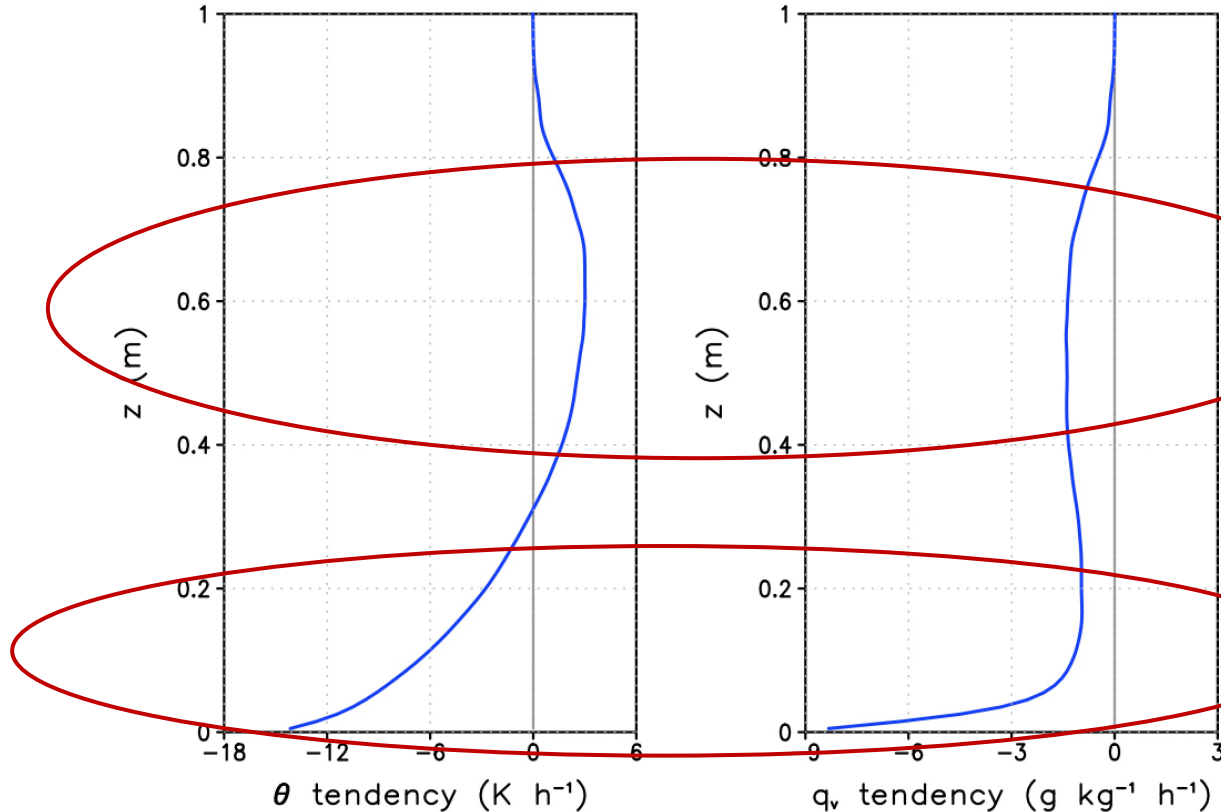


Cooling and drying in lower PBL:

- Radial Advection
- Evaporation (for  $\theta$ )

- simulations from Chen et al. (2021)

## Nudging tendencies



Consistent with  
Kepert et al. (2016)

Warming and drying in  
upper PBL:

- Clouds/convection
- Subsidence

Cooling and drying in  
lower PBL:

- Radial Advection
- Evaporation

# The Small-Domain (“patch”) Hurricane LES Technique

## CM1

- Pre-configured namelists in “run/config\_files”
- Since `cm1r21`: user settings are now in “namelist.input” file (eg, `hurr_vg`)
- Can rotate winds & mesoscale-tendency terms (`hurr_rotate`)

## Other models:

- Should be easy to add
- Primarily need “mesoscale tendency terms”
  - Horizontal winds: Bryan et al. (2017a, BLM)
  - Temperature, moisture: Chen et al. (2021, JAS)
- Code to calculate domain-average profiles:  
`<u>`, `<v>`, `<theta>`, `<qv>`

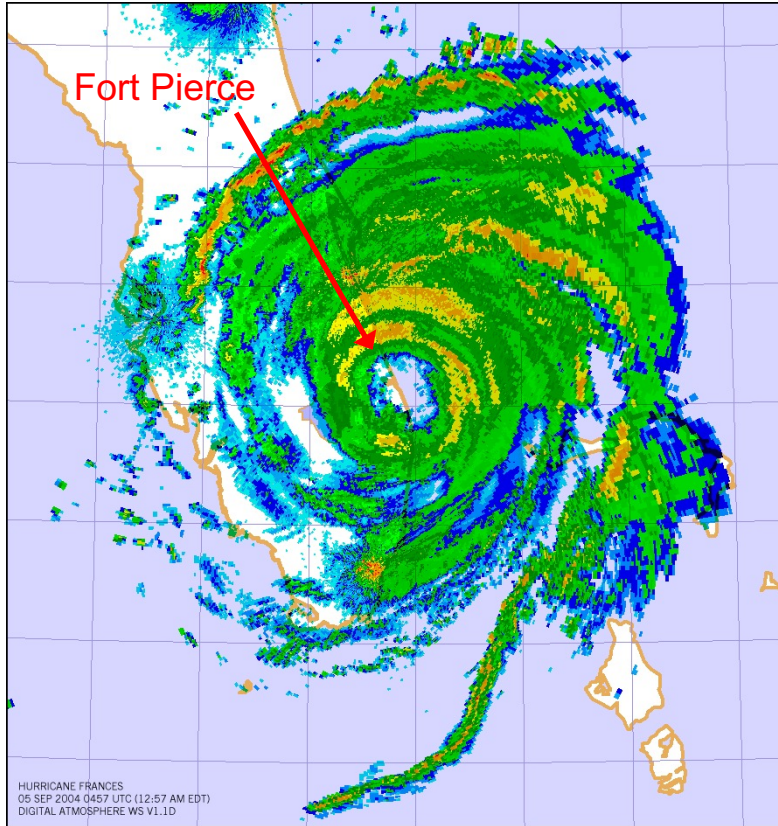


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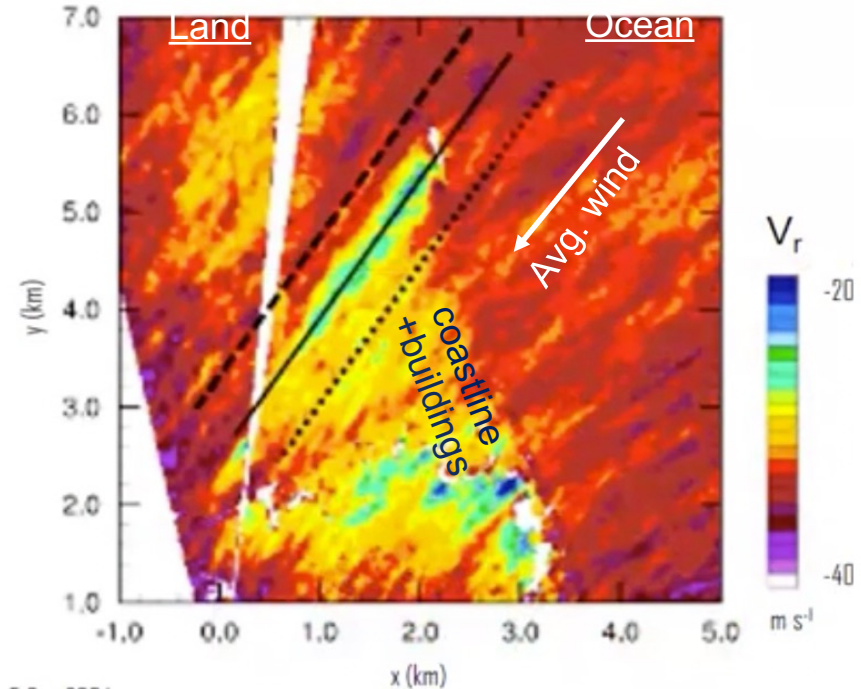
# Inhomogeneous Conditions

## Hurricane Frances (2004)

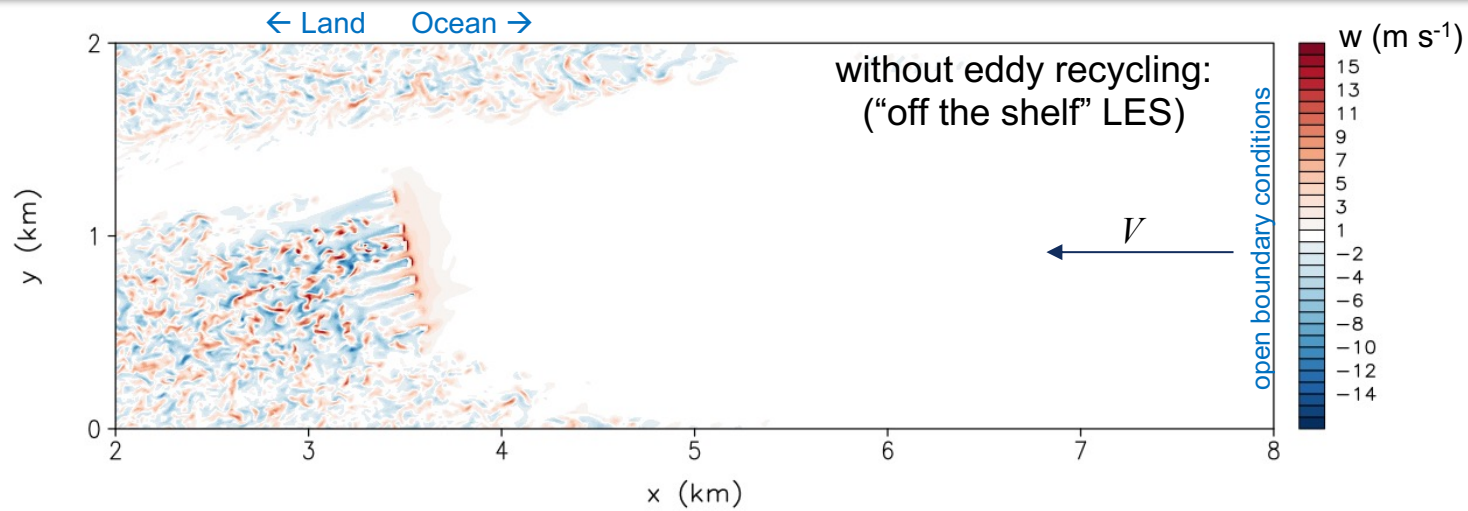


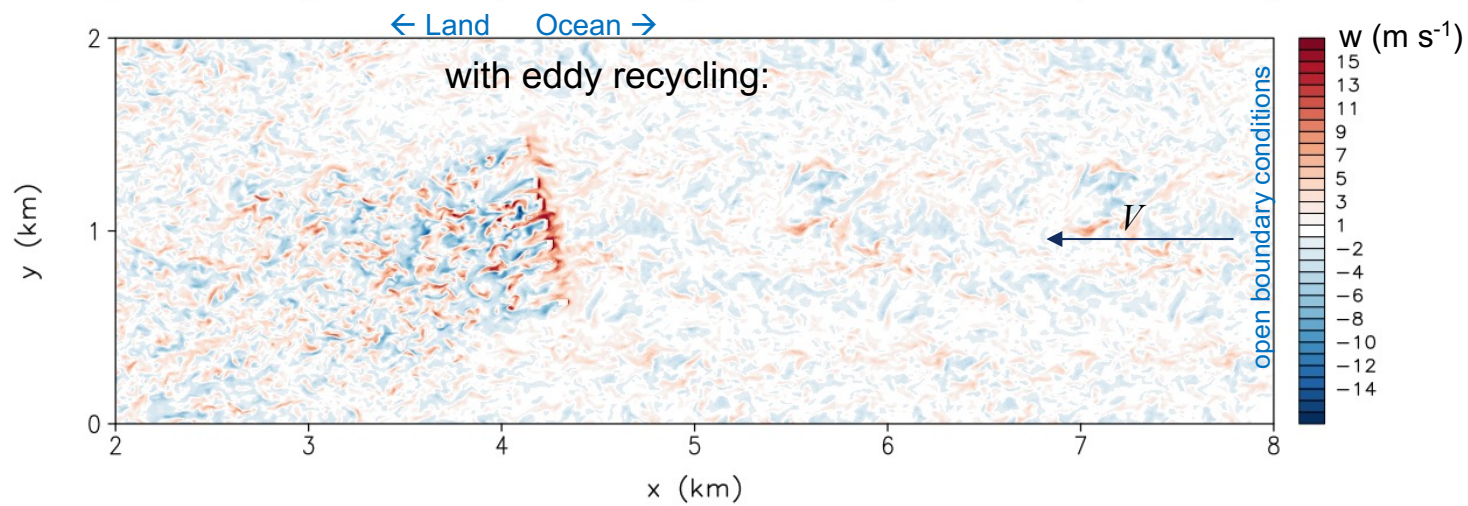
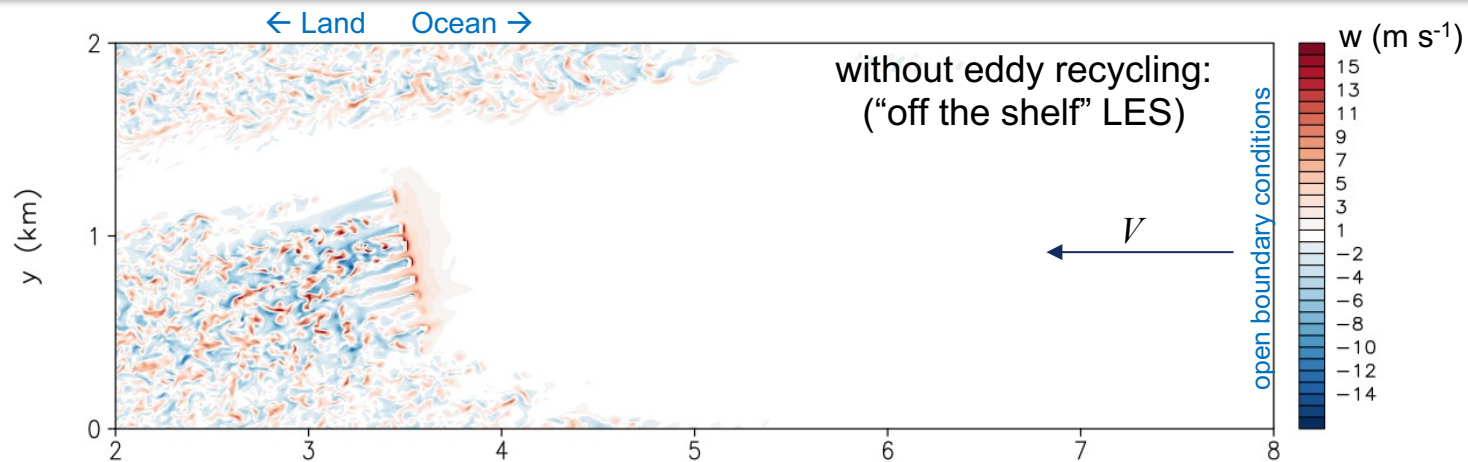
Kosiba (2014, Hurricanes Conf.)  
Doppler on Wheels radial velocity:

Average radial velocity 0358-0428 hr

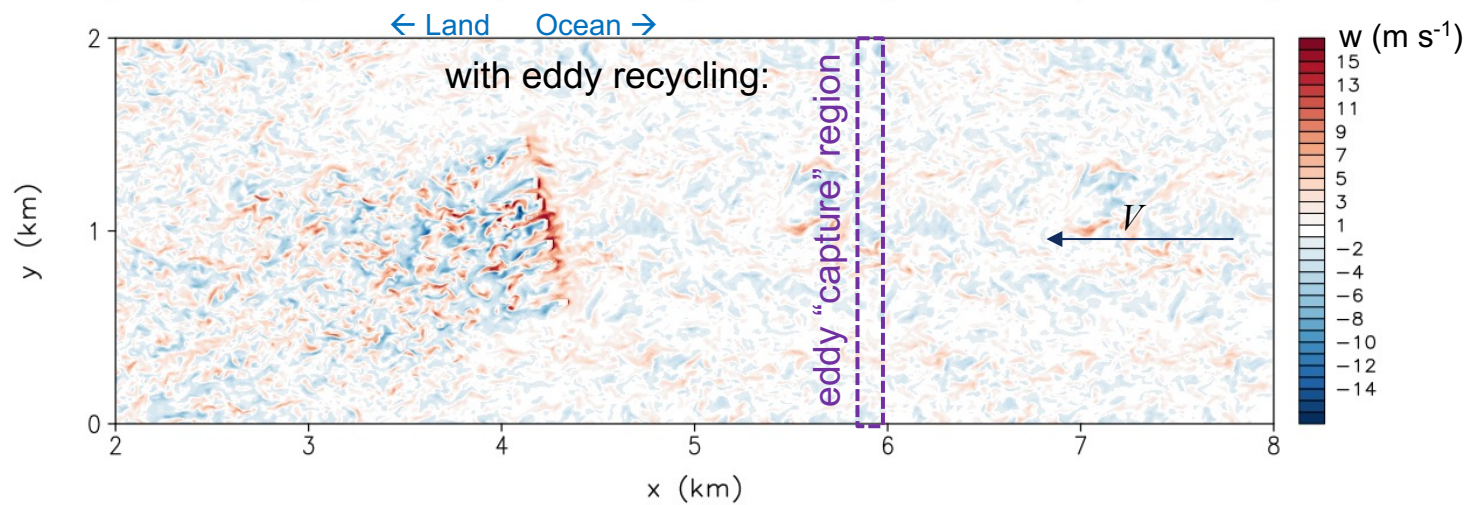
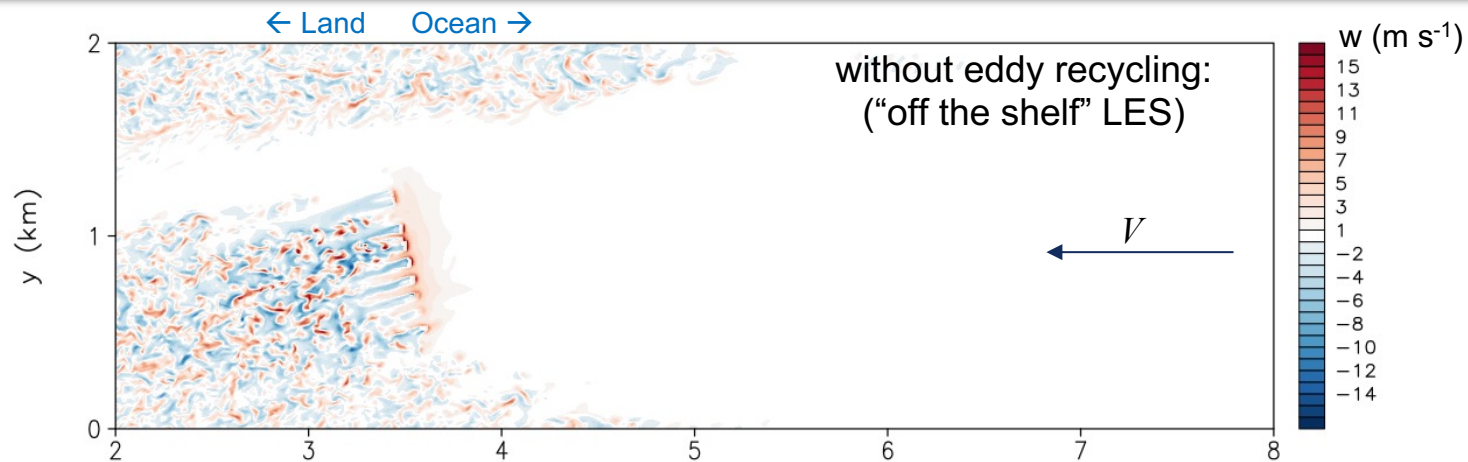


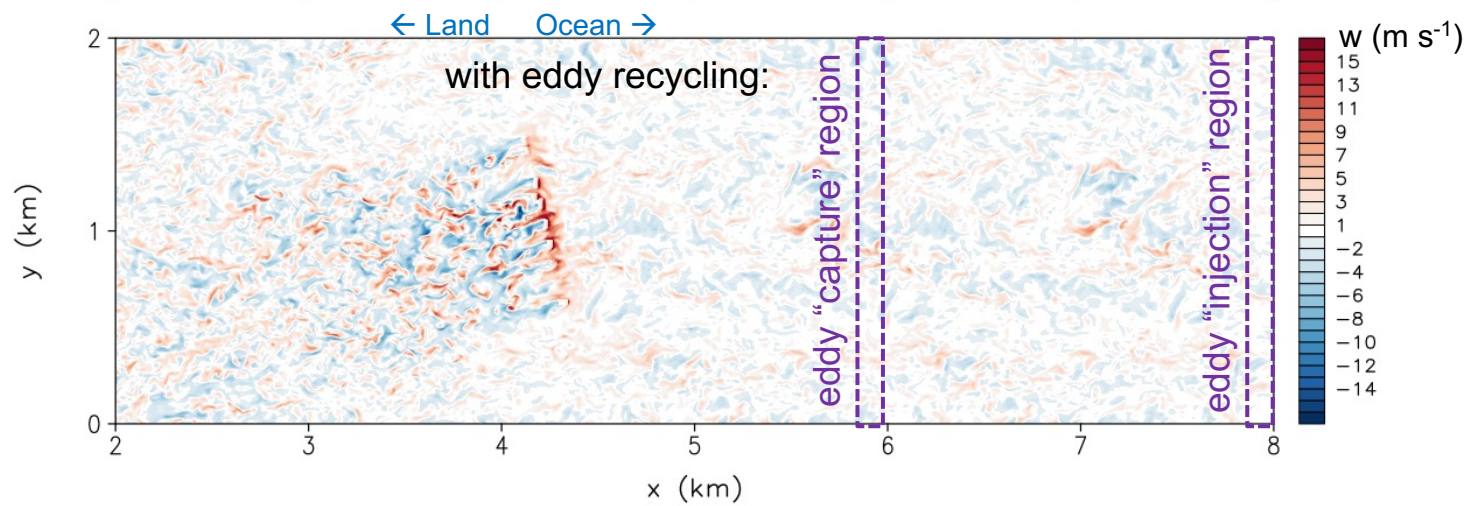
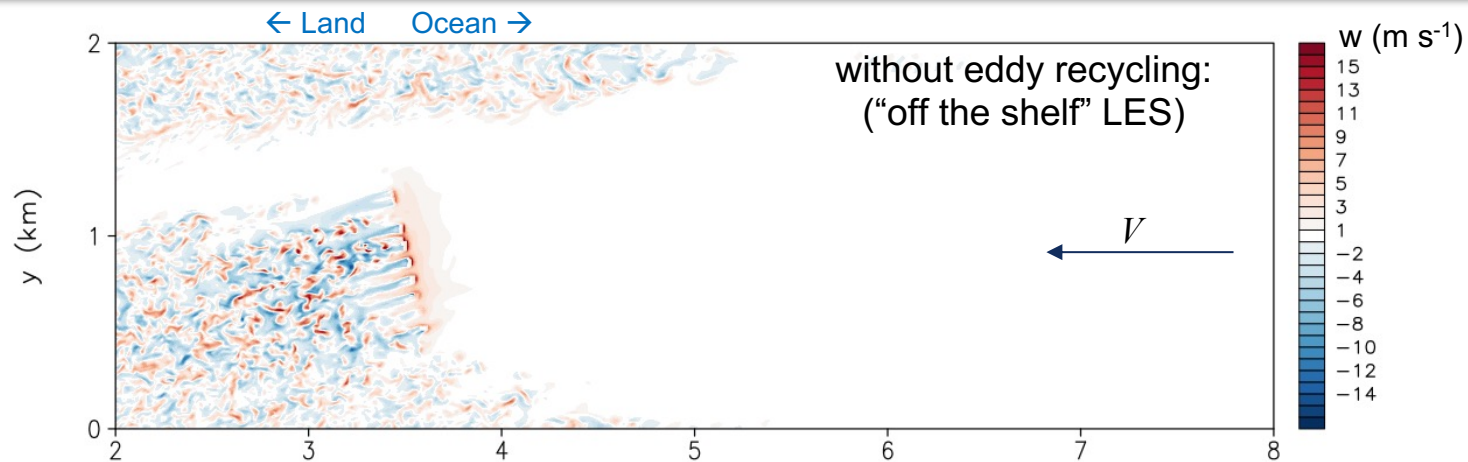
- Not suitable for periodic lateral boundary conditions!





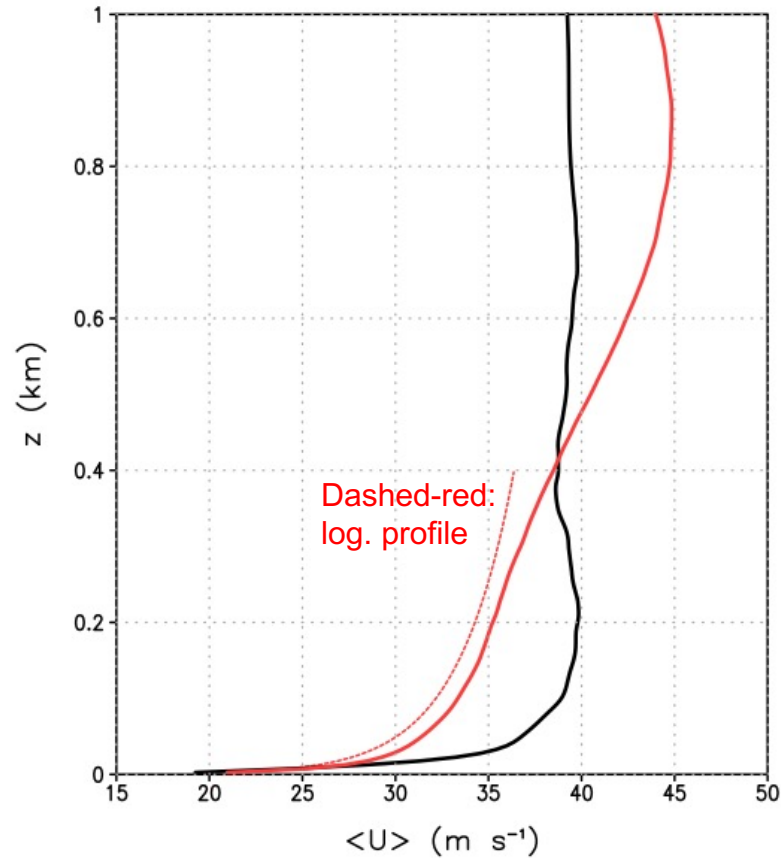








Average wind speed,  $x=6-7$  km (over ocean)



Black:  
without eddy injection

Red:  
with eddy injection

Dashed-red:  
log. profile

# The “Eddy Recycling” Technique


## CM1

- Available in `cm1r21.0`
- See pre-configured namelists:  
`config_files/hurricane_les_within_mm`  
`config_files/les_HurrCoast`
- A work in progress; feedback welcome

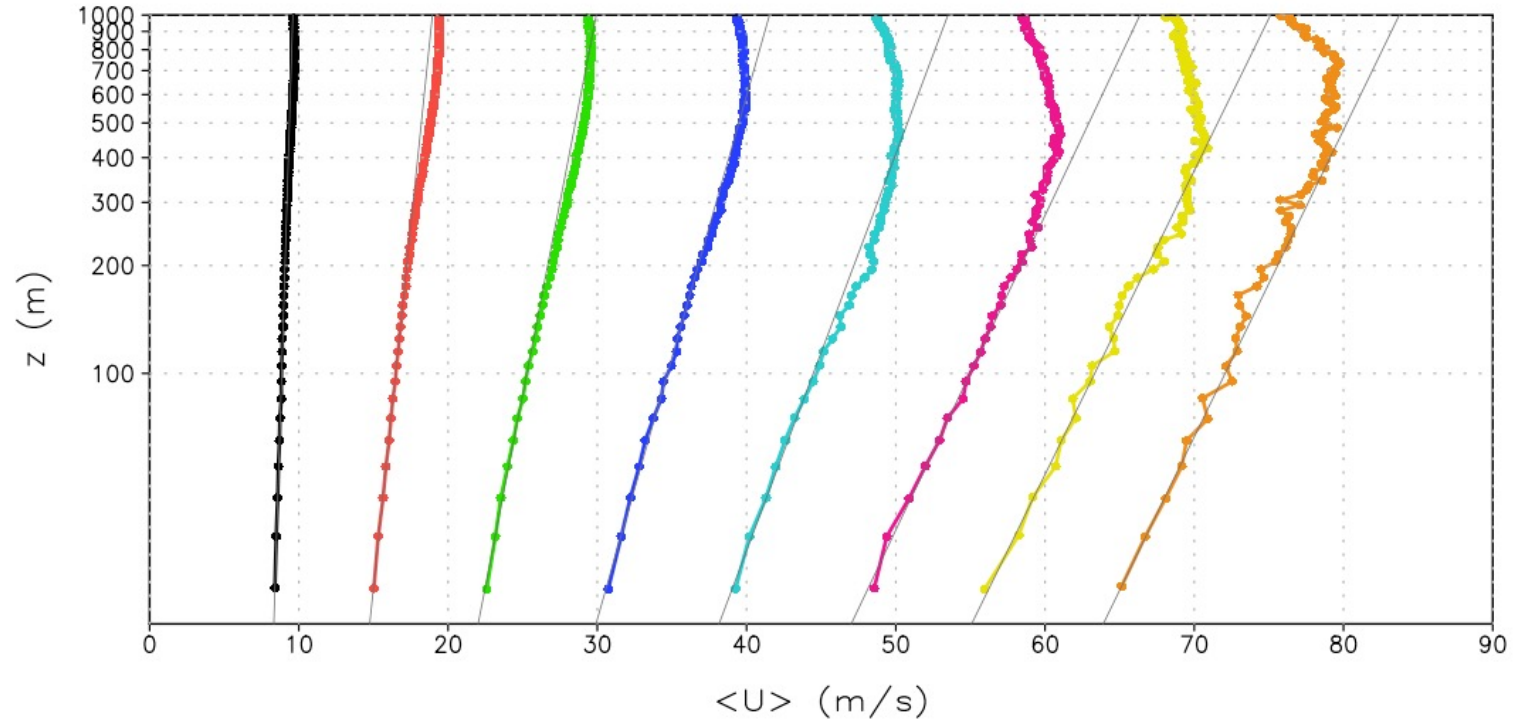
## Other models:

- Not easy to add...
- Need code to identify eddy “capture” and “injection” zones
- Need code to apply tendencies in “injection” zone
- Distributed-memory (MPI) communication can be a real hassle

## Three Options in CM1:

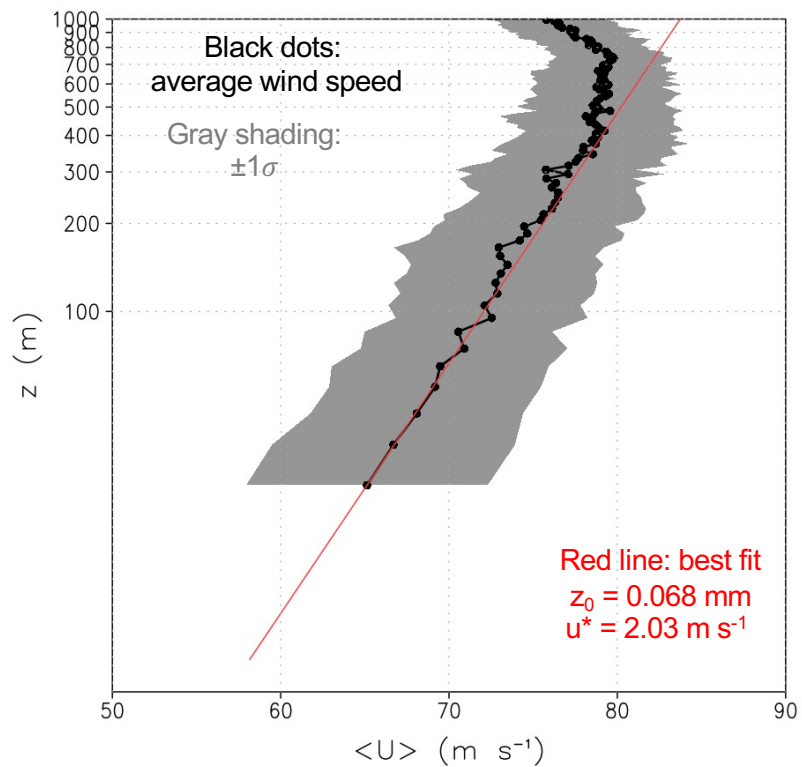
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- 

Composites: average wind speed  
(uses database from Wang et al. 2015, BAMS)

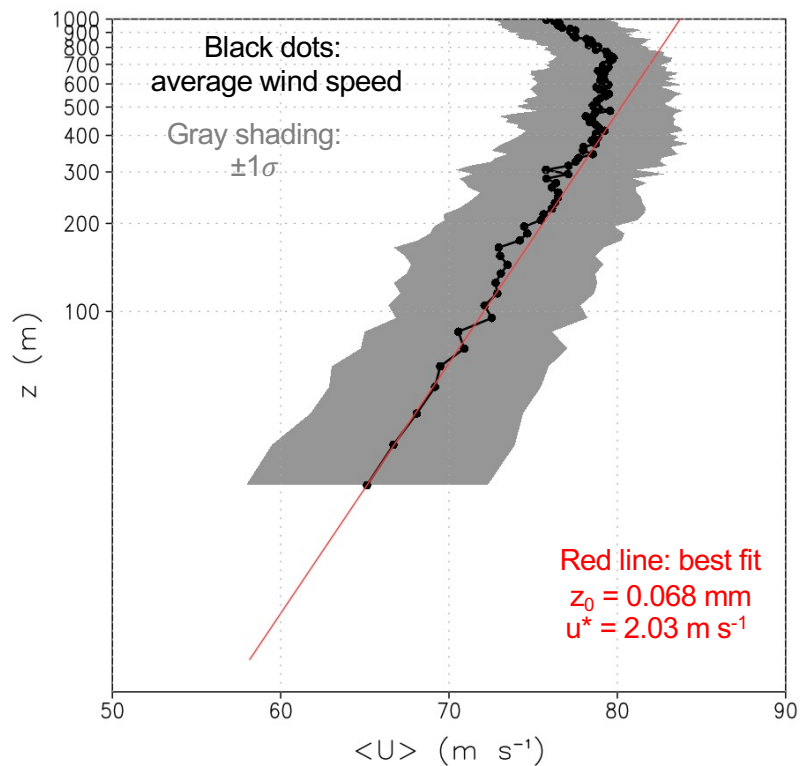


see also Richter et al. (2021, JAS)

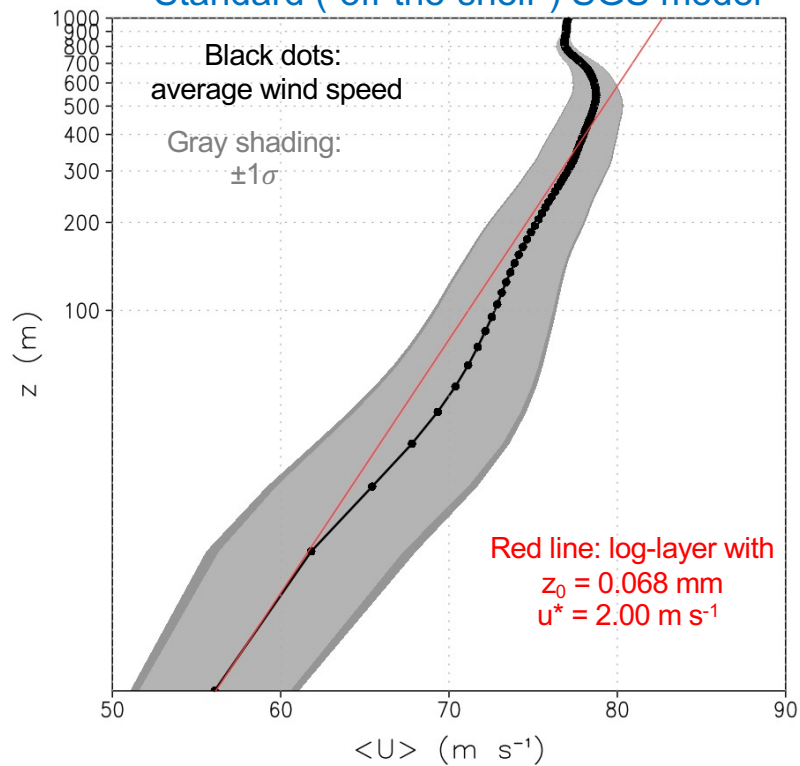
## Composite wind speed from dropsondes (N = 98)



## Composite wind speed from dropsondes (N = 98)



## Average wind speed from CM1-LES ( $\Delta x = 20 \text{ m}$ ) Standard (“off-the-shelf”) SGS model



- Overprediction of shear near surface is a common problem with LES (eg, Brasseur and Wei, 2010)



See Appendix of Bryan et al. (2017a, BLM)

(motivated by Sullivan et al., 1994, BLM)

For subgrid turbulence terms

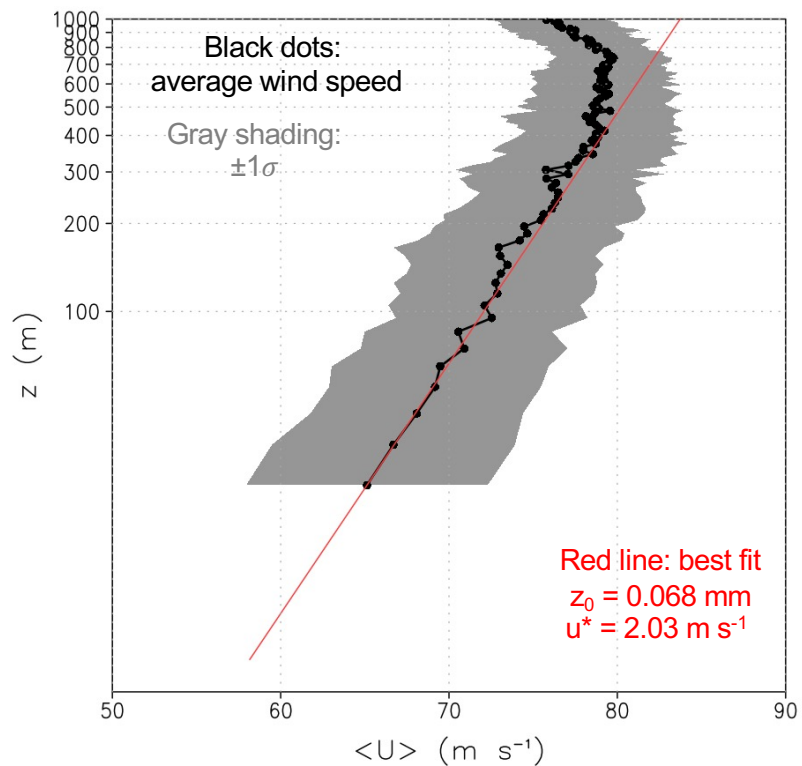
$$\frac{\partial u_i}{\partial t} = -u_j \frac{\partial u_i}{\partial x_j} - c_p \theta \frac{\partial \pi'}{\partial x_i} + \delta_{i3} g \frac{\theta'}{\theta_0} + \varepsilon_{ij3} u_j f + \boxed{\frac{1}{\rho} \frac{\partial \tau_{ij}^t}{\partial x_j}}$$

... add a second eddy viscosity term

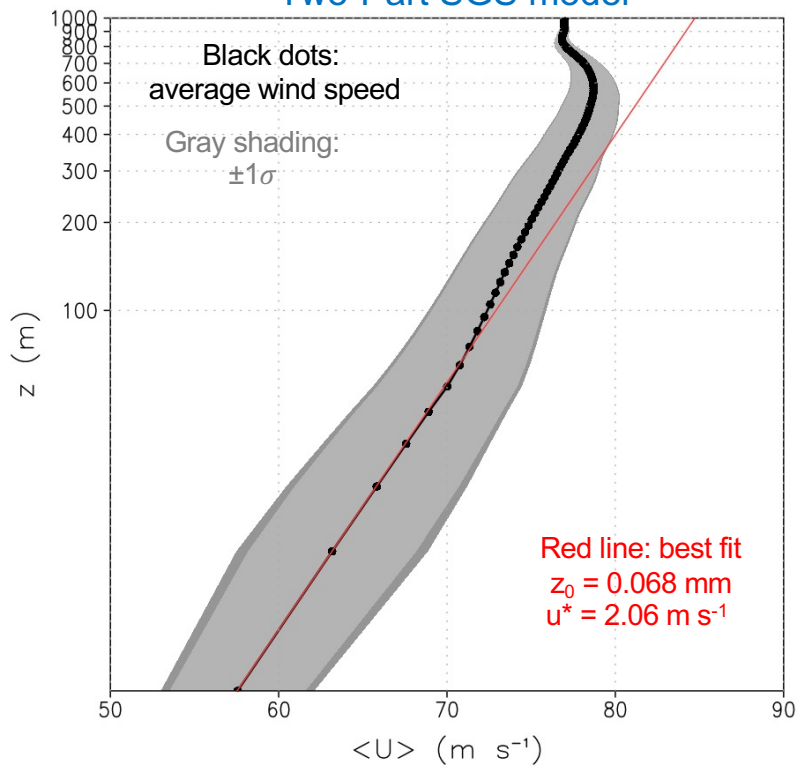
$$\begin{aligned} \tau_{13}^t &= \rho K_m \gamma \left( \frac{\partial u}{\partial z} + \frac{\partial w}{\partial x} \right) + \boxed{\rho K_w \frac{\partial \tilde{u}}{\partial z}}, \\ \tau_{23}^t &= \rho K_m \gamma \left( \frac{\partial v}{\partial z} + \frac{\partial w}{\partial y} \right) + \boxed{\rho K_w \frac{\partial \tilde{v}}{\partial z}}, \end{aligned}$$

$K_w$  is determined diagnostically so that  $\langle U \rangle$  is logarithmic near surface ( $z < 100$  m)

Composite wind speed from dropsondes (N = 98)



Average wind speed from CM1-LES ( $\Delta x = 20 \text{ m}$ )  
Two-Part SGS model



# The “Two-Part” Subgrid Turbulence Model

## CM1

- Available since `cm1r20`
- `sgsmodel = 4`
- Since `cm1r21` can use time-average instead of space-average (`t2p_avg = 2`)
  - So we can use it for non-homogeneous cases

## Other models:

- Should be fairly easy to add
- Need code to calculate average fields
  - Either spatial averages or time averages
- Code to calculate  $K_w$  is not complicated
  - (happy to share CM1 code)
- Minor addition to subgrid turbulence code

Thanks!

CM1 webpage: <https://www2.mmm.ucar.edu/people/bryan/cm1>  
(or just google “CM1”)

[These slides are now available on the CM1 webpage]

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