### Data Communication Assignment 1

### 1 Generate a sine wave of specific frequency for specified time duration.

Sine waves represent periodic oscillations.

Sine waves have the shape of sine curve.

The X-axis of the sine curve represents the time.

The Y-axis of the sine curve represents the amplitude of the sine wave.

The amplitude of the sine wave at any point in Y is proportional to the sine of a variable.

The sine wave is given by the equation

#### A sin(ft)

A - Amplitude t - Time f - Frequency

The sine curve goes through origin.

A cycle of sine wave is complete when the position of the sine wave starts from a position and comes to the same position after attaining its maximum and minimum amplitude during its course.

The time taken to complete one cycle is called the period of the sine wave.

The frequency of the sine wave is given by number of cycles per second.

'A' denotes amplitude of a sine wave.

The distance covered by a cycle measures the wavelength of the sine wave.

The wavelength of the sine wave is denoted by  $\lambda$ .

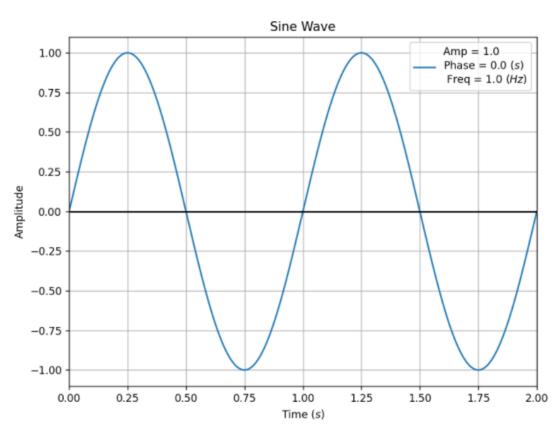
Examples of sine waves include the oscillations produced by the suspended weight on spring and the alternating current.

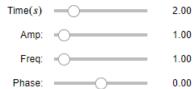
NumPy has the sin() function, which takes an array of values and provides the sine value for them.

Using the numpy sin() function and the matplotlib plot()a sine wave can be drawn.

```
[1]: import matplotlib.pyplot as plt
     import numpy as np
     import ipywidgets as wd
     from IPython.display import display
     %matplotlib nbagg
[2]: fig, ax = plt.subplots(1, figsize=(8, 6))
     def draw_plot(time_duration, A, f, phase):
         ax.clear()
        t = np.linspace(0,time duration,1000)
         ##### t= np.arange(0,10,0.01);
         y = A * np.sin(2 * np.pi * f * t + phase * 2 * np.pi)
         units = 'Amp = {} \nPhase = {} $(s)$ \n Freq = {} $(Hz)$'
         plt.plot(t, y, label=units.format(A, phase, f))
         plt.legend(loc=1)
         ax.set_xlim(t[0], t[-1])
         plt.grid(True)
         plt.axhline(y=0, color='k')
         plt.xlabel('Time $(s)$')
         plt.ylabel('Amplitude')
         plt.title("Sine Wave")
         plt.show()
     time_duration = wd.FloatSlider(min=0, max=10, value=2, description = "Time$(s)$")
     A = wd.FloatSlider(min=0, max=10, value=1, description="Amp:")
     f = wd.FloatSlider(min=0, max=10, value=1, description="Freq:")
     phase = wd.FloatSlider(min=-5, max=5, value=0, description="Phase:")
```

wd.interactive(draw\_plot,time\_duration=time\_duration, A=A, f=f, phase=phase)





#### 2 Generate a sine wave with noise.

```
[8]: import matplotlib.pyplot as plt
import numpy as np

import ipywidgets as wd
from IPython.display import display

%matplotlib nbagg
```

```
[9]: fig, ax = plt.subplots(1, figsize=(8, 6))
     def draw plot(time duration, A, f, phase):
         plt.clf()
         # Sampling rate 1000 hz / second
         t = np.linspace(0, time duration, 1000, endpoint = True)
         y = A * np.sin(2 * np.pi * f * t + phase * 2 * np.pi)
         noise = np.random.rand(len(y))
         corrupt = y + noise
          units = 'Amp = \{\}\ \nPhase = \{\}\ \s(s)\ \n Freq = \{\}\ \s(Hz)\ \s'
          plt.plot(t, y, label=units.format(A, phase, f))
          plt.legend(loc=1)
         plt.subplot (3,1,1)
         plt.title (" SINE WAVE ")
         plt.plot (t,y)
         plt.grid (which= "Both")
         plt.axhline(y=0, color='k')
         plt.subplot (3,1,2)
         plt.title (" NOISE ")
         plt.plot(t,noise)
         plt.grid (which= "Both")
         plt.axhline(y=0, color='k')
         plt.subplot (3,1,3)
```

```
plt.title (" NOISY SIGNAL ")
plt.plot (t,corrupt)
plt.grid (which= "Both")
plt.axhline(y=0, color='k')

plt.xlabel('Time $(s)$')
plt.ylabel('Amplitude')

plt.tight_layout()
plt.show()

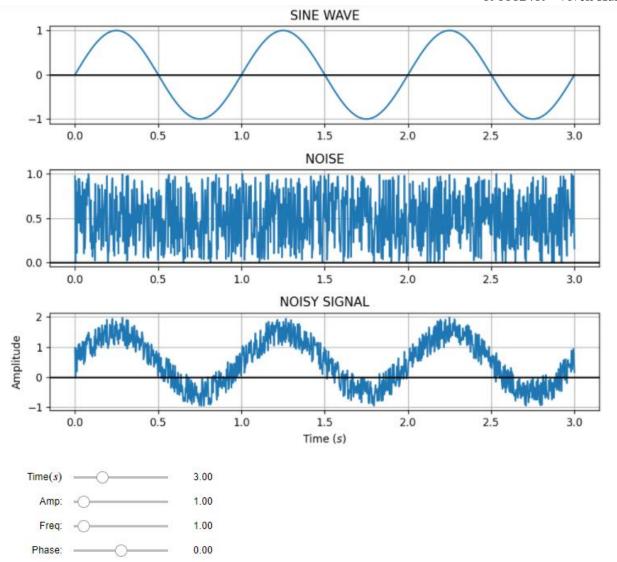
time_duration = wd.FloatSlider(min=0, max=10, value=2, description = "Time$(s)$")

A = wd.FloatSlider(min=0, max=10, value=1, description="Amp:")

f = wd.FloatSlider(min=0, max=10, value=1, description="Freq:")
phase = wd.FloatSlider(min=-5, max=5, value=0, description="Phase:")

wd.interactive(draw_plot,time_duration=time_duration, A=A, f=f, phase=phase)
```

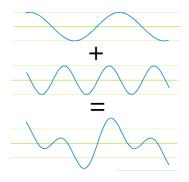
<IPython.core.display.Javascript object>



## 3 Construct a square wave using multiple sine waves.

Sine and cosine waves can make other functions!

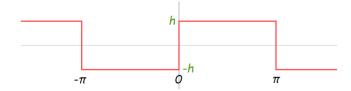
Here two different sine waves add together to make a new wave:



## **Square Wave**

Can we use sine waves to make a **square wave**?

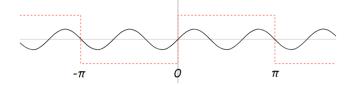
Our target is this square wave:



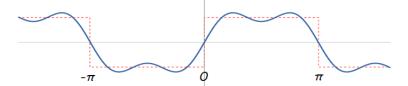
Start with **sin(x)**:



Then take sin(3x)/3:

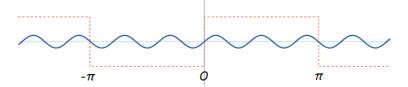


And add it to make sin(x)+sin(3x)/3:



Can you see how it starts to look a little like a square wave?

Now take sin(5x)/5:



Add it also, to make sin(x)+sin(3x)/3+sin(5x)/5:



Getting better! Let's add a lot more sine waves.

Using 20 sine waves we get sin(x)+sin(3x)/3+sin(5x)/5+...+sin(39x)/39:



Using 100 sine waves we get  $\sin(x) + \sin(3x)/3 + \sin(5x)/5 + ... + \sin(199x)/199$ :



And if we could add infinite sine waves in that pattern we would have a square wave!

So we can say that:

a square wave = 
$$\sin(x) + \sin(3x)/3 + \sin(5x)/5 + \dots$$
 (infinitely)

That is the idea of a Fourier series.

By adding infinite sine (and or cosine) waves we can make other functions, even if they are a bit weird.

# **Finding the Coefficients**

How did we know to use  $\sin(3x)/3$ ,  $\sin(5x)/5$ , etc?

There are formulas!

First let us write down a full series of sines and cosines, with a name for all coefficients:

$$f(x) = a_0 + \sum_{n=1}^{\infty} a_n \cos(nx \frac{\pi}{L}) + \sum_{n=1}^{\infty} b_n \sin(nx \frac{\pi}{L})$$

#### Where:

- f(x) is the function we want (such as a square wave)
- L is half of the period of the function
- a<sub>0</sub>, a<sub>n</sub> and b<sub>n</sub> are coefficients that we need to calculate!

To find the coefficients  $a_0$ ,  $a_n$  and  $b_n$  we use these formulas:

$$a_0 = \frac{1}{2L} \int_{-L}^{L} f(x) dx$$

$$a_n = \frac{1}{L} \int_{-L}^{L} f(x) \cos(nx \frac{\pi}{L}) dx$$

$$b_n = \frac{1}{L} \int_{-L}^{L} f(x) \sin(nx \frac{\pi}{L}) dx$$

```
[5]: import matplotlib.pyplot as plt
import numpy as np

import ipywidgets as wd
from IPython.display import display

%matplotlib nbagg
```

```
[7]: fig, ax = plt.subplots(1, figsize=(8, 6))
              def draw_plot(time_duration, A, f, phase, harmonics):
                         ax.clear()
                         t = np.linspace(0,time_duration,1000)
                         ##### t= np.arange(0,10,0.01);
                        y=0
                         for ham in range(1,2*harmonics,2):
                          y = A * np.sin(2 * np.pi * f * t + phase * 2 * np.pi)
                                    y = y + (1/ham) * A * np.sin(2 * np.pi * ham * f * t + phase * 2 * np.pi)
                         units = 'Amp = {} \n = {} \n
                         ax.plot(t, y, label=units.format(A,f,phase,harmonics ))
                         ax.legend(loc=1)
                         ax.set_xlim(t[0], t[-1])
                         plt.grid(True)
                         plt.axhline(y=0, color='k')
                         plt.xlabel('Time t$(s)$')
                         plt.ylabel('Amplitude A')
                         plt.title("Sine Wave")
                         plt.show()
              time_duration = wd.FloatSlider(min=0,max=10,value=2,description = "Time$(s)$")
              A = wd.FloatSlider(min=0, max=10, value=1, description="Amp:")
              f = wd.FloatSlider(min=0, max=10, value=1, description="Freq:")
              phase = wd.FloatSlider(min=-5, max=5, value=0, description="Phase:")
              harmonics = wd.IntSlider(min=1, max=100, value=10, description="Harmonics:")
              wd.interactive(draw_plot,time_duration=time_duration, A=A, f=f,__
                →phase=phase, harmonics=harmonics)
```

<IPython.core.display.Javascript object>

