

Today

- More relational algebra
 - Division
 - Examples
- SQL
 - Review
 - Examples

Division

- Let R be a relation with fields x, y
- Let S be a relation with field y
- R/S returns one column corresponding to certain x values
- R/S is the set of all x values such that ***for every y value*** in S , there is a tuple (x,y) in R
- Stated another way, for each x value in R , consider the set of all y values in R that correspond to that x value. If this set contains all the values in S , then x is in R/S
- R/S is the largest relation instance Q such that $Q \times S \subseteq R$

Division

R

Supplier_no	Part_no
s1	p1
s1	p2
s1	p3
s1	p4
s2	p1
s2	p2
s3	p2
s4	p2
s4	p4

S1

Part_no
p2

S2

Part_no
p2
p4

S3

Part_no
p1
p2
p4

R/S1

Supplier_no
s1
s2
s3
s4

R/S2

Supplier_no
s1
s4

R/S3

Supplier_no
s1

R / S computes the suppliers who supply all the parts in S

Division

- Generalizing to to a set of attributes
- Let R be a relation with fields $A_1, A_2, \dots, A_k, A_{k+1}, A_{k+2}, \dots A_{k+n}$
- Let S be a relation with fields $A_{k+1}, A_{k+2}, \dots A_{k+n}$
- R/S results in a relation with fields A_1, A_2, \dots, A_k
- R/S is the set of all A_1, A_2, \dots, A_k such that *for every* $A_{k+1}, A_{k+2}, \dots A_{k+n}$ in S, there is a tuple in R

sid	sname	rating	age
22	Dustin	7	45.0
29	Brutus	1	33.0
31	Lubber	8	55.5
32	Andy	8	25.5
58	Rusty	10	35.0
64	Horatio	7	35.0
71	Zorba	10	16.0
74	Horatio	9	35.0
85	Art	3	25.5
95	Bob	3	63.5

S3 (Sailors)

sid	bid	day
22	101	10/10/98
22	102	10/10/98
22	103	10/8/98
22	104	10/7/98
31	102	11/10/98
31	103	11/6/98
31	104	11/12/98
64	101	9/5/98
64	102	9/8/98
74	103	9/8/98

R2 (Reserves)

bid	bname	color
101	Interlake	blue
102	Interlake	red
103	Clipper	green
104	Marine	red

B1 (Boats)

Q1: Find the names of sailors who have reserved boat 103

A1: $\pi_{sname}(\sigma_{bid=103}(Reserves) \bowtie Sailors)$

sid	sname	rating	age
22	Dustin	7	45.0
29	Brutus	1	33.0
31	Lubber	8	55.5
32	Andy	8	25.5
58	Rusty	10	35.0
64	Horatio	7	35.0
71	Zorba	10	16.0
74	Horatio	9	35.0
85	Art	3	25.5
95	Bob	3	63.5

S3 (Sailors)

sid	bid	day
22	101	10/10/98
22	102	10/10/98
22	103	10/8/98
22	104	10/7/98
31	102	11/10/98
31	103	11/6/98
31	104	11/12/98
64	101	9/5/98
64	102	9/8/98
74	103	9/8/98

R2 (Reserves)

bid	bname	color
101	Interlake	blue
102	Interlake	red
103	Clipper	green
104	Marine	red

B1 (Boats)

Q2: Find the names of sailors who have reserved a red boat.

A2: $\pi_{sname}(\sigma_{color=red}(Boats) \bowtie Reserves \bowtie Sailors)$

sid	sname	rating	age
22	Dustin	7	45.0
29	Brutus	1	33.0
31	Lubber	8	55.5
32	Andy	8	25.5
58	Rusty	10	35.0
64	Horatio	7	35.0
71	Zorba	10	16.0
74	Horatio	9	35.0
85	Art	3	25.5
95	Bob	3	63.5

S3 (Sailors)

sid	bid	day
22	101	10/10/98
22	102	10/10/98
22	103	10/8/98
22	104	10/7/98
31	102	11/10/98
31	103	11/6/98
31	104	11/12/98
64	101	9/5/98
64	102	9/8/98
74	103	9/8/98

R2 (Reserves)

bid	bname	color
101	Interlake	blue
102	Interlake	red
103	Clipper	green
104	Marine	red

B1 (Boats)

Q3: Find the names of sailors who have reserved a red or a green boat.

A3: $\rho\left(tempboats, (\sigma_{color=red}(Boats) \cup (\sigma_{color=green}(Boats))\right)$
 $\pi_{sname}(tempboats) \bowtie Reserves \bowtie Sailors$

sid	sname	rating	age
22	Dustin	7	45.0
29	Brutus	1	33.0
31	Lubber	8	55.5
32	Andy	8	25.5
58	Rusty	10	35.0
64	Horatio	7	35.0
71	Zorba	10	16.0
74	Horatio	9	35.0
85	Art	3	25.5
95	Bob	3	63.5

S3 (Sailors)

sid	bid	day
22	101	10/10/98
22	102	10/10/98
22	103	10/8/98
22	104	10/7/98
31	102	11/10/98
31	103	11/6/98
31	104	11/12/98
64	101	9/5/98
64	102	9/8/98
74	103	9/8/98

R2 (Reserves)

bid	bname	color
101	Interlake	blue
102	Interlake	red
103	Clipper	green
104	Marine	red

B1 (Boats)

Q4: Find the colors of boats reserved by Lubber.

A4: $\pi_{color}(\sigma_{sname=Lubber}(Sailors) \bowtie Reserves \bowtie Boats)$

sid	sname	rating	age
22	Dustin	7	45.0
29	Brutus	1	33.0
31	Lubber	8	55.5
32	Andy	8	25.5
58	Rusty	10	35.0
64	Horatio	7	35.0
71	Zorba	10	16.0
74	Horatio	9	35.0
85	Art	3	25.5
95	Bob	3	63.5

S3 (Sailors)

sid	bid	day
22	101	10/10/98
22	102	10/10/98
22	103	10/8/98
22	104	10/7/98
31	102	11/10/98
31	103	11/6/98
31	104	11/12/98
64	101	9/5/98
64	102	9/8/98
74	103	9/8/98

R2 (Reserves)

bid	bname	color
101	Interlake	blue
102	Interlake	red
103	Clipper	green
104	Marine	red

B1 (Boats)

Q5: Find the names of sailors who have reserved a red and a green boat.

A5: $\rho(tempred, \pi_{sid}((\sigma_{color=red}(Boats)) \bowtie Reserves))$
 $\rho(tempgreen, \pi_{sid}((\sigma_{color=green}(Boats)) \bowtie Reserves))$
 $\pi_{sname}(tempred \cap tempgreen) \bowtie Sailors$

sid	sname	rating	age
22	Dustin	7	45.0
29	Brutus	1	33.0
31	Lubber	8	55.5
32	Andy	8	25.5
58	Rusty	10	35.0
64	Horatio	7	35.0
71	Zorba	10	16.0
74	Horatio	9	35.0
85	Art	3	25.5
95	Bob	3	63.5

S3 (Sailors)

sid	bid	day
22	101	10/10/98
22	102	10/10/98
22	103	10/8/98
22	104	10/7/98
31	102	11/10/98
31	103	11/6/98
31	104	11/12/98
64	101	9/5/98
64	102	9/8/98
74	103	9/8/98

R2 (Reserves)

bid	bname	color
101	Interlake	blue
102	Interlake	red
103	Clipper	green
104	Marine	red

B1 (Boats)

Q: Find the names of sailors who have reserved at least one boat.

A: $\pi_{sname}(Sailors \bowtie Reserves)$

sid	sname	rating	age
22	Dustin	7	45.0
29	Brutus	1	33.0
31	Lubber	8	55.5
32	Andy	8	25.5
58	Rusty	10	35.0
64	Horatio	7	35.0
71	Zorba	10	16.0
74	Horatio	9	35.0
85	Art	3	25.5
95	Bob	3	63.5

S3 (Sailors)

sid	bid	day
22	101	10/10/98
22	102	10/10/98
22	103	10/8/98
22	104	10/7/98
31	102	11/10/98
31	103	11/6/98
31	104	11/12/98
64	101	9/5/98
64	102	9/8/98
74	103	9/8/98

R2 (Reserves)

bid	bname	color
101	Interlake	blue
102	Interlake	red
103	Clipper	green
104	Marine	red

B1 (Boats)

Q: Find the names of sailors who have reserved at least two boats.

A: $\rho\left(reservations, \pi_{sid, name, bid}(Sailors \bowtie Reserves)\right)$
 $\rho(reservationPairs(1 \rightarrow sid1, 2 \rightarrow sname1, 3 \rightarrow bid1, 4 \rightarrow sid2,$
 $5 \rightarrow sname2, 6 \rightarrow bid2), reservations \times reservations)$
 $\pi_{sname1}(\sigma_{sid1=sid2 \wedge (bid1 \neq bid2)}(reservationPairs))$

sid	sname	rating	age
22	Dustin	7	45.0
29	Brutus	1	33.0
31	Lubber	8	55.5
32	Andy	8	25.5
58	Rusty	10	35.0
64	Horatio	7	35.0
71	Zorba	10	16.0
74	Horatio	9	35.0
85	Art	3	25.5
95	Bob	3	63.5

S3 (Sailors)

sid	bid	day
22	101	10/10/98
22	102	10/10/98
22	103	10/8/98
22	104	10/7/98
31	102	11/10/98
31	103	11/6/98
31	104	11/12/98
64	101	9/5/98
64	102	9/8/98
74	103	9/8/98

R2 (Reserves)

bid	bname	color
101	Interlake	blue
102	Interlake	red
103	Clipper	green
104	Marine	red

B1 (Boats)

Q: Find the sids of sailors with age over 20 who have not reserved a red boat

A: $\pi_{sid}(\sigma_{age>20}Sailors) - \pi_{sid}(\sigma_{color=red}(Boats) \bowtie Reserves \bowtie Sailors)$

sid	sname	rating	age
22	Dustin	7	45.0
29	Brutus	1	33.0
31	Lubber	8	55.5
32	Andy	8	25.5
58	Rusty	10	35.0
64	Horatio	7	35.0
71	Zorba	10	16.0
74	Horatio	9	35.0
85	Art	3	25.5
95	Bob	3	63.5

S3 (Sailors)

sid	bid	day
22	101	10/10/98
22	102	10/10/98
22	103	10/8/98
22	104	10/7/98
31	102	11/10/98
31	103	11/6/98
31	104	11/12/98
64	101	9/5/98
64	102	9/8/98
74	103	9/8/98

R2 (Reserves)

bid	bname	color
101	Interlake	blue
102	Interlake	red
103	Clipper	green
104	Marine	red

B1 (Boats)

Q: Find the names of sailors who have reserved all boats

A: $\rho(\text{tempsids}, \pi_{sid, bid} \text{Reserves} / \pi_{bid} \text{Boats})$
 $\pi_{sname}(\text{tempsids} \bowtie \text{Sailors})$

sid	sname	rating	age
22	Dustin	7	45.0
29	Brutus	1	33.0
31	Lubber	8	55.5
32	Andy	8	25.5
58	Rusty	10	35.0
64	Horatio	7	35.0
71	Zorba	10	16.0
74	Horatio	9	35.0
85	Art	3	25.5
95	Bob	3	63.5

S3 (Sailors)

sid	bid	day
22	101	10/10/98
22	102	10/10/98
22	103	10/8/98
22	104	10/7/98
31	102	11/10/98
31	103	11/6/98
31	104	11/12/98
64	101	9/5/98
64	102	9/8/98
74	103	9/8/98

R2 (Reserves)

bid	bname	color
101	Interlake	blue
102	Interlake	red
103	Clipper	green
104	Marine	red

B1 (Boats)

Q: Find the names of sailors who have reserved all boats called Interlake

sid	sname	rating	age
22	Dustin	7	45.0
29	Brutus	1	33.0
31	Lubber	8	55.5
32	Andy	8	25.5
58	Rusty	10	35.0
64	Horatio	7	35.0
71	Zorba	10	16.0
74	Horatio	9	35.0
85	Art	3	25.5
95	Bob	3	63.5

S3 (Sailors)

sid	bid	day
22	101	10/10/98
22	102	10/10/98
22	103	10/8/98
22	104	10/7/98
31	102	11/10/98
31	103	11/6/98
31	104	11/12/98
64	101	9/5/98
64	102	9/8/98
74	103	9/8/98

R2 (Reserves)

bid	bname	color
101	Interlake	blue
102	Interlake	red
103	Clipper	green
104	Marine	red

B1 (Boats)

Q: Find the names of sailors who have reserved all boats called Interlake

A: $\rho(\text{tempsids}, \pi_{sid, bid} \text{Reserves} / \pi_{bid}(\sigma_{bname = \text{"Interlake"}}(\text{Boats})))$
 $\pi_{sname}(\text{tempsids} \bowtie \text{Sailors})$

SQL

- Basic form:

```
SELECT [DISTINCT] <select-list>  
FROM <from-list>  
WHERE <qualification>
```

- from-list: names of tables to query from. A table name can be followed by a range variable (“as <alias>”)
- select-list: list of column names or expressions involving common names of tables named in the from-list. Can be prefixed by a range variable (alias.<column_name>)
- qualification: Boolean combination of conditions in the form:
 - “expression op expression”
 - Op is one of the comparison operators {<, <=, =, <>, >=, >}
 - Expression is a column name, constant, or an expression
- DISTINCT (optional) makes results unique (a set) -> results to SQL queries contain duplicates by default!

sid	sname	rating	age
22	Dustin	7	45.0
29	Brutus	1	33.0
31	Lubber	8	55.5
32	Andy	8	25.5
58	Rusty	10	35.0
64	Horatio	7	35.0
71	Zorba	10	16.0
74	Horatio	9	35.0
85	Art	3	25.5
95	Bob	3	63.5

S3 (Sailors)

sid	bid	day
22	101	10/10/98
22	102	10/10/98
22	103	10/8/98
22	104	10/7/98
31	102	11/10/98
31	103	11/6/98
31	104	11/12/98
64	101	9/5/98
64	102	9/8/98
74	103	9/8/98

R2 (Reserves)

bid	bname	color
101	Interlake	blue
102	Interlake	red
103	Clipper	green
104	Marine	red

B1 (Boats)

Q: Find the names and ages of all sailors.

sid	sname	rating	age
22	Dustin	7	45.0
29	Brutus	1	33.0
31	Lubber	8	55.5
32	Andy	8	25.5
58	Rusty	10	35.0
64	Horatio	7	35.0
71	Zorba	10	16.0
74	Horatio	9	35.0
85	Art	3	25.5
95	Bob	3	63.5

S3 (Sailors)

sid	bid	day
22	101	10/10/98
22	102	10/10/98
22	103	10/8/98
22	104	10/7/98
31	102	11/10/98
31	103	11/6/98
31	104	11/12/98
64	101	9/5/98
64	102	9/8/98
74	103	9/8/98

R2 (Reserves)

bid	bname	color
101	Interlake	blue
102	Interlake	red
103	Clipper	green
104	Marine	red

B1 (Boats)

Q: Find the names and ages of all sailors.

```
SELECT DISTINCT S.name, S.age
FROM Sailors S
```

What if we don't include DISTINCT?

sid	sname	rating	age
22	Dustin	7	45.0
29	Brutus	1	33.0
31	Lubber	8	55.5
32	Andy	8	25.5
58	Rusty	10	35.0
64	Horatio	7	35.0
71	Zorba	10	16.0
74	Horatio	9	35.0
85	Art	3	25.5
95	Bob	3	63.5

S3 (Sailors)

sid	bid	day
22	101	10/10/98
22	102	10/10/98
22	103	10/8/98
22	104	10/7/98
31	102	11/10/98
31	103	11/6/98
31	104	11/12/98
64	101	9/5/98
64	102	9/8/98
74	103	9/8/98

R2 (Reserves)

bid	bname	color
101	Interlake	blue
102	Interlake	red
103	Clipper	green
104	Marine	red

B1 (Boats)

Q: Find all sailors with a rating above 7.

sid	sname	rating	age
22	Dustin	7	45.0
29	Brutus	1	33.0
31	Lubber	8	55.5
32	Andy	8	25.5
58	Rusty	10	35.0
64	Horatio	7	35.0
71	Zorba	10	16.0
74	Horatio	9	35.0
85	Art	3	25.5
95	Bob	3	63.5

S3 (Sailors)

sid	bid	day
22	101	10/10/98
22	102	10/10/98
22	103	10/8/98
22	104	10/7/98
31	102	11/10/98
31	103	11/6/98
31	104	11/12/98
64	101	9/5/98
64	102	9/8/98
74	103	9/8/98

R2 (Reserves)

bid	bname	color
101	Interlake	blue
102	Interlake	red
103	Clipper	green
104	Marine	red

B1 (Boats)

Q: Find all sailors with a rating above 7.

```
SELECT S.sid, S.sname, S.rating, S.age
FROM Sailors as S
WHERE S.rating > 7
```

Can also use SELECT *

SQL – Set operations

- ***UNION***: Set union
- ***INTERSECT***: Set intersection
- ***EXCEPT***: Set difference
- In contrast to other SQL queries, these operations remove duplicates by default. To include duplicates, need to include **ALL** keyword:
 - UNION ALL
 - INTERSECT ALL
 - EXCEPT ALL

sid	sname	rating	age
22	Dustin	7	45.0
29	Brutus	1	33.0
31	Lubber	8	55.5
32	Andy	8	25.5
58	Rusty	10	35.0
64	Horatio	7	35.0
71	Zorba	10	16.0
74	Horatio	9	35.0
85	Art	3	25.5
95	Bob	3	63.5

S3 (Sailors)

sid	bid	day
22	101	10/10/98
22	102	10/10/98
22	103	10/8/98
22	104	10/7/98
31	102	11/10/98
31	103	11/6/98
31	104	11/12/98
64	101	9/5/98
64	102	9/8/98
74	103	9/8/98

R2 (Reserves)

bid	bname	color
101	Interlake	blue
102	Interlake	red
103	Clipper	green
104	Marine	red

B1 (Boats)

Q3: Find the names of sailors who have reserved a red or a green boat.

```

SELECT S.sname
FROM   Sailors S, Reserves R, Boats B
WHERE  S.sid = R.sid AND R.bid = B.bid
       AND (B.color = 'red' OR B.color = 'green')

```

sid	sname	rating	age
-----	-------	--------	-----

S3 (Sailors)

sid	bid	day
-----	-----	-----

R2 (Reserves)

bid	bname	color
-----	-------	-------

B1 (Boats)

Q5: Find the names of sailors who have reserved a red and a green boat.

```
SELECT S.sname
FROM Sailors S, Reserves R, Boats B
WHERE S.sid = R.sid AND R.bid = B.bid AND B.color = 'red'
UNION
SELECT S2.sname
FROM Sailors S2, Boats B2, Reserves H2
WHERE S2.sid = H2.sid AND H2.bid = B2.bid AND B2.color =
'green'
```

Nested Queries

- A nested query is a query with another query embedded in it
- Also known as a “subquery”
- Useful to break complicated queries into smaller queries

sid	sname	rating	age
-----	-------	--------	-----

S3 (Sailors)

sid	bid	day
-----	-----	-----

R2 (Reserves)

bid	bname	color
-----	-------	-------

B1 (Boats)

Q1: Find the names of sailors who have reserved boat 103

```
SELECT S.name
FROM Sailors S
WHERE S.sid IN (SELECT R.sid
                FROM Reserves R
                WHERE R.bid = 103)
```


Aggregate Operators

- COUNT ([DISTINCT A]): The number of [unique] values in column A
- SUM ([DISTINCT A]): The sum of all [unique] values in column A
- AVG ([DISTINCT A]): The average of all [unique] values in column A
- MAX (A): The maximum of all values in column A
- MIN (A): The minimum of all values in column A

sid	sname	rating	age
-----	-------	--------	-----

S3 (Sailors)

sid	bid	day
-----	-----	-----

R2 (Reserves)

bid	bname	color
-----	-------	-------

B1 (Boats)

Find the average age of all sailors.

```
SELECT AVG(S.age) FROM SAILORS S
```

Find the average age of sailors with a rating of 10

```
SELECT AVG(S.age) FROM SAILORS S WHERE S.rating = 10
```

Find the name and age of the oldest sailor

```
SELECT S.sname, S.age
FROM Sailors S
WHERE S.age = (SELECT MAX(S2.age) FROM SAILOR s2)
```

Count the number of sailors

```
SELECT COUNT(*) FROM Sailors S
```

Count the number of different sailor names.

```
SELECT COUNT(DISTINCT S.sname) FROM Sailors S
```

GROUP BY and HAVING

- `SELECT [DISTINCT] <select-list>`
- `FROM <from-list>`
- `WHERE <qualification>`
- `GROUP BY <grouping-list>`
- `HAVING <group-qualification>`

- `<grouping-list>`: Used when we want to apply aggregate operations to each member of a group of rows in a relation. Specifies the list of fields we want to group by.
- `<group-qualification>`: condition on the grouping

sid	sname	rating	age
-----	-------	--------	-----

S3 (Sailors)

sid	bid	day
-----	-----	-----

R2 (Reserves)

bid	bname	color
-----	-------	-------

B1 (Boats)

Find the age of the youngest sailor for each rating level.

```
SELECT min(S.age)
FROM Sailors S
WHERE S.rating = i
```

Need to specify $i = 1, 2, 3, \dots, 10$. Another way:

```
SELECT S.rating, MIN(S.age) as min_age
FROM Sailors S
GROUP BY S.rating
```

If we only want to include rows where the minimum age is > 40

```
SELECT S.rating, MIN(S.age) as min_age
FROM Sailors S
GROUP BY S.rating
HAVING min_age > 40
```