

# Optical Properties of Gain incorporating Photonic Resonators



*by*

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CIIT/FA15-BPH-019/ISB

BS Thesis  
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Optical Properties of Gain incorporating Photonic Resonators

A Thesis Presented to

**COMSATS University Islamabad**

In partial fulfillment

of the requirement for the degree of

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by

Ahmad Bilal

CUI/FA15-BPH-019/ISB

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# Optical Properties of Gain incorporating Photonic Resonators

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A Under Graduate Thesis submitted to the Department of Physics as partial fulfillment of the requirement for the award of Degree of BS (Physics).

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## Optical Properties of Gain incorporating Photonic Resonators

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## Declaration

I **Ahmad Bilal** (CIIT/FA15-BPH-019/ISB) hereby declare that this project neither as a whole nor as a part there of has been copied out from any source. It is further declared that I have developed this thesis and the accompanied report entirely on the basis of my personal efforts made under the sincere guidance of my supervisors. No portion of the work presented in this report has been submitted in support of any other degree of qualification of this or any other University or Institute of learning, if found I shall stand responsible.

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# Certificate

It is certified that Ahmad Bilal (Registration No. CIIT/FA156-BPH-019/ISB) has carried out all the work related to this thesis under my supervision at the Department of Physics, COMSATS University Islamabad and the work fulfills the requirement for award of BS degree.

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# Abstract

In this project, we extended the research on optical ring resonators for such mediums in which there is gain. First we studied normally the optical properties of passive resonators and measured the effects of EIT and EIA in them (details later discussed). Then we moved over focus on active resonators varrying different parameters to acheive EIT and EIA in gain incorporating photonic resonators which have extensive amount of applications. The main focus for this project was to model the characteristics and properties of active resonators and compare it with the results of passive resonators. Due to the gain property of active resonators, similar effects can be seen here as in passive resonators but without losses involved. The main idea was to establish a photonic device that could work efficiently as passive resonators and also have more output.

# Dedication

This thesis is dedicated to my mother who brought me up all by herself and made me the gentleman I am today.



*Indeed, in the creation of the heavens,  
and the earth and the alternation of  
the night and the day, are signs for  
those of understanding.*

*The Noble Quran [3:190]*

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## Acknowledgements

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In the name of Allah, who is the most beneficent and merciful. I would like to thank all  
the

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# Chapter 1

## Introduction

### Resonators

Most of the time, using `mpmath` is simply a matter of setting the desired precision and entering a formula. For verification purposes, a quite (but not always!) reliable technique is to calculate the same thing a second time at a higher precision and verifying that the results agree.

### Explanation

To perform more advanced calculations, it is important to have some understanding of how `mpmath` works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis. Most of the time, using `mpmath` is simply a matter of setting the desired precision and entering a formula. For verification purposes, a quite (but not always!) reliable technique is to calculate the same thing a second time at a higher precision and verifying that the results agree.

### Optical Resonators

To perform more advanced calculations, it is important to have some understanding of how `mpmath` works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis. Most of the time, using `mpmath`

## Different Geometeries

is simply a matter of setting the desired precision and entering a formula. For verification purposes, a quite (but not always!) reliable technique is to calculate the same thing a second time at a higher precision and verifying that the results agree.

## Fabry-Perot Resonators

To perform more advanced calculations, it is important to have some understanding of how mpmath works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis.

## Explanation

To perform more advanced calculations, it is important to have some understanding of how mpmath works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis.

## Ring Resonators

To perform more advanced calculations, it is important to have some understanding of how mpmath works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis.

## All-Pass

To perform more advanced calculations, it is important to have some understanding of how mpmath works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis.

## Add drop

To perform more advanced calculations, it is important to have some understanding of how mpmath works internally and what the possible sources of error are. This section gives an

overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis.

## **Coupled Ring**

To perform more advanced calculations, it is important to have some understanding of how mpmath works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis.

## **References**

To perform more advanced calculations, it is important to have some understanding of how mpmath works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis. To perform more advanced calculations, it is important to have some understanding of how mpmath works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis.

# Chapter 2

## Area of Study

### The Fabry-Perot Interferometer

Most of the time, using `mpmath` is simply a matter of setting the desired precision and entering a formula. For verification purposes, a quite (but not always!) reliable technique is to calculate the same thing a second time at a higher precision and verifying that the results agree.

### Theory of Fabry-Perot interferometer

To perform more advanced calculations, it is important to have some understanding of how `mpmath` works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis. Most of the time, using `mpmath` is simply a matter of setting the desired precision and entering a formula. For verification purposes, a quite (but not always!) reliable technique is to calculate the same thing a second time at a higher precision and verifying that the results agree.

### Finesse, Q-factor

To perform more advanced calculations, it is important to have some understanding of how `mpmath` works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis. Most of the time, using `mpmath` is simply a matter of setting the desired precision and entering a formula. For verification purposes, a quite (but not always!) reliable technique is to calculate the same thing a second time at a higher precision and verifying that the results agree.



## Gain incorporation in Resonators

To perform more advanced calculations, it is important to have some understanding of how `mpmath` works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision

### Beer's Law

binary floating-point arithmetic and some concepts from numerical analysis. Most of the time, using `mpmath` is simply a matter of setting the desired precision and entering a formula. For verification purposes, a quite (but not always!) reliable technique is to calculate the same thing a second time at a higher precision and verifying that the results agree.

### Beer's law study as gain

To perform more advanced calculations, it is important to have some understanding of how `mpmath` works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis. Most of the time, using `mpmath` is simply a matter of setting the desired precision and entering a formula. For verification purposes, a quite (but not always!) reliable technique is to calculate the same thing a second time at a higher precision and verifying that the results agree.

### Gain medium

To perform more advanced calculations, it is important to have some understanding of how `mpmath` works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis.

# Chapter 3

## Coupled Resonators with Gain

### Coupled resontaor with Gain medium

Most of the time, using `mpmath` is simply a matter of setting the desired precision and entering a formula. For verification purposes, a quite (but not always!) reliable technique is to calculate the same thing a second time at a higher precision and verifying that the results agree.

### Gain element

To perform more advanced calculations, it is important to have some understanding of how `mpmath` works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis. Most of the time, using `mpmath` is simply a matter of setting the desired precision and entering a formula. For verification purposes, a quite (but not always!) reliable technique is to calculate the same thing a second time at a higher precision and verifying that the results agree.

### Calculation/Equations

To perform more advanced calculations, it is important to have some understanding of how `mpmath` works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis. Most of the time, using `mpmath` is simply a matter of setting the desired precision and entering a formula. For verification purposes, a quite (but not always!) reliable technique is to calculate the same thing a second time at a higher precision and verifying that the results agree.

## For single

To perform more advanced calculations, it is important to have some understanding of how `mpmath` works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis. Most of the time, using `mpmath` is simply a matter of setting the desired precision and entering a formula. For verification purposes, a quite (but not always!) reliable technique is to calculate the same thing a second time at a higher precision and verifying that the results agree.

## For coupled

To perform more advanced calculations, it is important to have some understanding of how `mpmath` works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis. Most of the time, using `mpmath` is simply a matter of setting the desired precision and entering a formula. For verification purposes, a quite (but not always!) reliable technique is to calculate the same thing a second time at a higher precision and verifying that the results agree.

## For triple

To perform more advanced calculations, it is important to have some understanding of how `mpmath` works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis.

## Coupling Regimes

To perform more advanced calculations, it is important to have some understanding of how `mpmath` works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis. To perform more advanced calculations, it is important to have some understanding of how `mpmath` works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis.

# Chapter 4

## Electromagnetically Induced Transparency

### EIT in Atoms

Most of the time, using `mpmath` is simply a matter of setting the desired precision and entering a formula. For verification purposes, a quite (but not always!) reliable technique is to calculate the same thing a second time at a higher precision and verifying that the results agree.

### Two level Atoms

To perform more advanced calculations, it is important to have some understanding of how `mpmath` works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis. Most of the time, using `mpmath` is simply a matter of setting the desired precision and entering a formula. For verification purposes, a quite (but not always!) reliable technique is to calculate the same thing a second time at a higher precision and verifying that the results agree.

### EIT in ring resonators

To perform more advanced calculations, it is important to have some understanding of how `mpmath` works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis. Most of the time, using `mpmath` is simply a matter of setting the desired

precision and entering a formula. For verification purposes, a quite (but not always!) reliable technique is to calculate the same thing a second time at a higher precision and verifying that the results agree.

## EIT in Coupled resonators(CRIT)

To perform more advanced calculations, it is important to have some understanding of how mpmath works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis. Most of the time, using mpmath is simply a matter of setting the desired precision and entering a formula. For verification purposes, a quite (but not always!) reliable technique is to calculate the same thing a second time at a higher precision and verifying that the results agree.

## CRIT with gain

To perform more advanced calculations, it is important to have some understanding of how mpmath works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis. Most of the time, using mpmath is simply a matter of setting the desired precision and entering a formula. For verification purposes, a quite (but not always!) reliable technique is to calculate the same thing a second time at a higher precision and verifying that the results agree.

## Results

To perform more advanced calculations, it is important to have some understanding of how mpmath works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis. Most of the time, using mpmath is simply a matter of setting the desired precision and entering a formula. For verification purposes, a quite (but not always!) reliable technique is to calculate the same thing a second time at a higher precision and verifying that the results agree.

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# Chapter 5

## Electromagnetically Induced Absorbption

### EIA concepts

To perform more advanced calculations, it is important to have some understanding of how mpmath works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis. To perform more advanced calculations, it is important to have some

### EIA in atoms

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### EIA Quantum phenomena

This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis. To perform more advanced calculations, it is important to have some understanding of how mpmath works internally and what the possible sources of error are. This section gives an overview of arbitrary-precision binary floating-point arithmetic and some concepts from numerical analysis. To perform more advanced calculations, it is important to have some understanding of how mpmath works internally

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## **EIA in resonators**

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## **Coupled resonators induced Absorption**

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## **CRIA with gain**

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# Chapter 6

## Conclusion

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# Appendix A

## Abbreviations

EIT Electromagnetically Induced Transparency

EIA Electromagnetically Induced Absorption

CRIT Coupled Resonator Induced Transparency

CRIA Coupled Resonator Induced Absorption

FSR Free Spectral Range

MRR Micro Ring Resonator

MZI Mach Zehnder Interferometer

FWHM Full width at half maximum

CMT Coupled Mode Theory