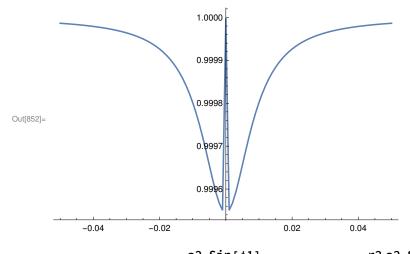
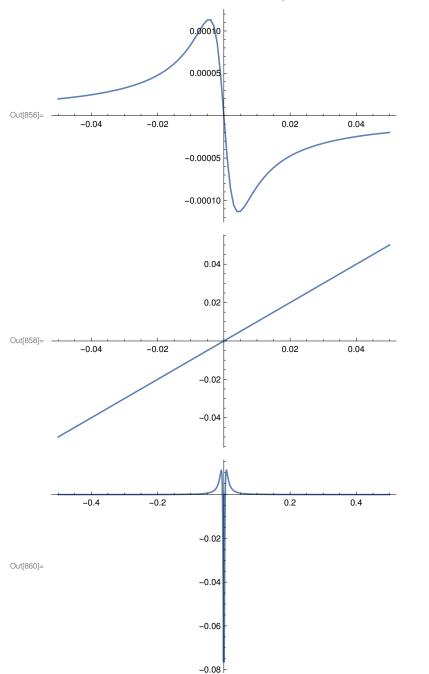
```
In[2]:= r12 := \frac{r2 - a2 \ Exp[I \phi 2]}{1 - r2 \ a2 \ Exp[I \phi 2]}
trans := \frac{r1 - r12 \ a1 \ Exp[I \phi 1]}{1 - r1 \ r12 \ a1 \ Exp[I \phi 1]}
ln[829]:= n := 3.45;
         c := 299792458;
         R1 := 10 \times 10^{(-6)};
         R2 := 10 \times 10^{(-6)};
         d1 := 2 Pi R1
         d2 := 2 Pi R2
         \lambda := 1550 \times 10^{(-9)}; (* resonant wavelength *)
         Q1 := 1 \times 10^{5};
         Q2 := 1 \times 10^{6};
         g1 := 0.0
         g2 := 1500
         \alpha 1 := \frac{2 \operatorname{Pi} n}{\lambda \operatorname{Q} 1}
         \alpha 2 := \frac{2 \operatorname{Pi} n}{\lambda \operatorname{Q} 2}
         a1 := Exp[g1 - \alpha 1 d1]
         a2 := Exp[g2 - \alpha 2 d2]
         t1 := \sqrt{1 - r1^2}
         t2 := \sqrt{1 - r2^2}
         t3 := \sqrt{1 - r3^2}
         r1:= 0.999999
         r2:= 0.999999
 ln[24]:= \phi 2 := \phi 1
```

```
ln[849] = \phi 1min := -0.05;
      \phi1max := 0.05;
      transdata := Table[\{\phi 1, Abs[trans]^2\}, \{\phi 1, \phi 1min, \phi 1max, 0.001\}]
      ListLinePlot[transdata, PlotRange → All]
```



$$\begin{split} & \text{In} [780] \text{:=} & \phi 12 \text{ :=} & -\text{ArcTan} \Big[ \frac{\text{a2 Sin}[\phi 1]}{\text{r2} - \text{a2 Cos}[\phi 1]} \Big] + \text{ArcTan} \Big[ \frac{\text{r2 a2 Sin}[\phi 1]}{1 - \text{r2 a2 Cos}[\phi 1]} \Big] \\ & \phi \text{eff :=} \\ & -\text{ArcTan} \Big[ \frac{\text{a1 Abs}[\text{r12}] \, \text{Sin}[\phi 1 + \phi 12]}{\text{r1} - \text{a1 Abs}[\text{r12}] \, \text{Cos}[\phi 1 + \phi 12]} \Big] + \text{ArcTan} \Big[ \frac{\text{r1 a1 Abs}[\text{r12}] \, \text{Sin}[\phi 1 + \phi 12]}{1 - \text{r1 a1 Abs}[\text{r12}] \, \text{Cos}[\phi 1 + \phi 12]} \Big] \\ & \text{vg :=} & (\text{n/c}) \, \Big( \Big( \text{a1} \, \Big( -1 + \text{r1}^2 \Big) \, \text{Abs}[\text{r12}] \\ & \Big( -\text{a1} \, \Big( 1 + \text{r1}^2 \Big) \, \text{Abs}[\text{r12}] + \text{r1 Cos}[\phi 1 + \phi 12] + \text{a1}^2 \, \text{r1 Abs}[\text{r12}]^2 \, \text{Cos}[\phi 1 + \phi 12] \Big) \Big) \Big/ \\ & \Big( \Big( \text{r1}^2 + \text{a1}^2 \, \text{Abs}[\text{r12}]^2 - 2 \, \text{a1} \, \text{r1 Abs}[\text{r12}] \, \text{Cos}[\phi 1 + \phi 12] \Big) \Big) \Big) \Big) \end{aligned}$$

```
ln[853] := \phi 1min := -0.05;
      \phi1max := 0.05;
      transdata := Table[\{\phi 1, \phi eff\}, \{\phi 1, \phi 1 min, \phi 1 max, 0.001\}]
      ListLinePlot[transdata, PlotRange → All]
      transdata := Table [\{\phi 1, \phi 12\}, \{\phi 1, \phi 1 min, \phi 1 max, 0.001\}]
      ListLinePlot[transdata, PlotRange → All]
      transdata := Table[\{\phi 1, c vg\}, \{\phi 1, -0.5, 0.5, 0.001\}]
      ListLinePlot[transdata, PlotRange → All]
```



ln[791]:= r1 - Abs[r12] a1 /.  $\phi$ 1  $\rightarrow$  0

r1 - r2 a1

r2 - a2

Out[791] = 0.00874665

Out[792]= **0.00874863** 

 $\text{Out} \texttt{[793]=} -2.762747754502644 \times 10^{651}$ 

 $ln[861]:= (1 / vg) /. \phi1 \rightarrow 0$ 

 $\text{Out[861]= } -3.35405\times10^9$