

Photo Album

by Ahmed Ibrahim

The Hough Transform



- **The Hough Transform** is a technique which is used to **isolate curves of a given shape in an image**.
- Any curve defined in **parametric form** may be found using the Hough Transform.
- Curves such as lines, circles and ellipses are very easy to find.
- In industry most manufactured parts have such boundaries, so these curves may serve the purpose.
- This transform technique is relatively **unaffected by noise**.

The Hough Transform



Line Detection

- Equation of straight line given in parametric form is:

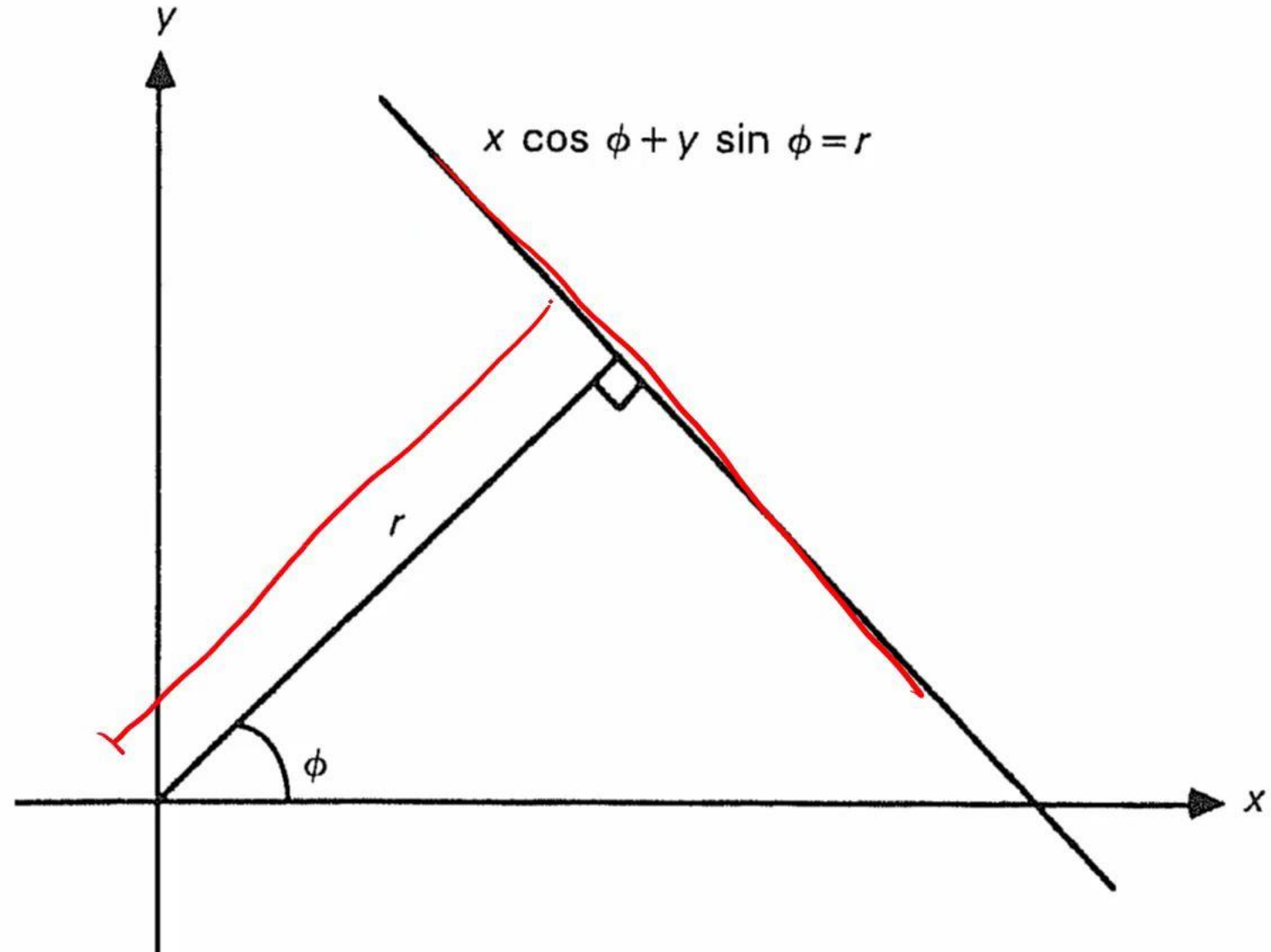
$$x \cos \phi + y \sin \phi = \underline{r}$$

- Where ' r ' is the length of a normal to the line from the origin and ' ϕ ' is the angle this normal makes with the X-axis

The Hough Transform



Line Detection



The Hough Transform



Line Detection

- If we have a point (x_i, y_i) on this line, then:

$$\underline{x_i} \cos \phi + \underline{y_i} \sin \phi = \underline{r}$$

- A line will have some constant value of ' \underline{r} ' and ' $\underline{\phi}$ '.
- Suppose, however, that we do not know which line we are considering, but we **do know the coordinates of the point(s)** on the line.
- Now we can consider ' \underline{r} ' and ' $\underline{\phi}$ ' as variables and point (x_i, y_i) as constants.

The Hough Transform



Line Detection

- In this case the equation

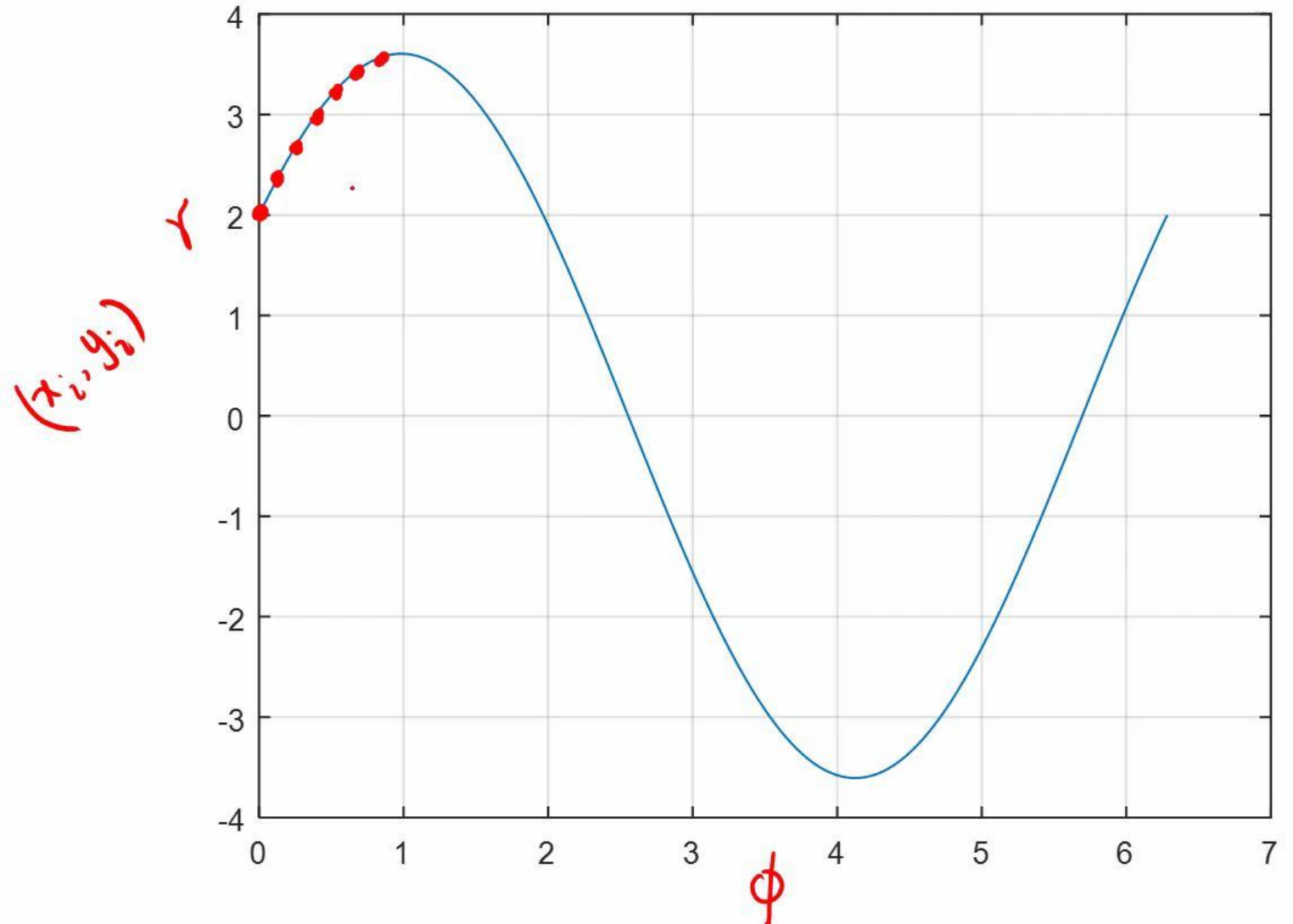
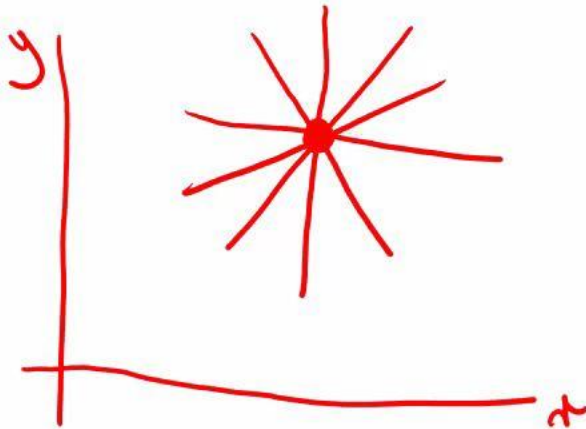
$$x_i \cos \phi + y_i \sin \phi = r$$

- Defines the values of '**r**' and '**ϕ**' such that the line passes through the point (x_i, y_i) .
- If we plot the values of '**r**' and '**ϕ**' for this given point then we will get a sinusoidal curve in **(r-ϕ) space**.

The Hough Transform



Line Detection

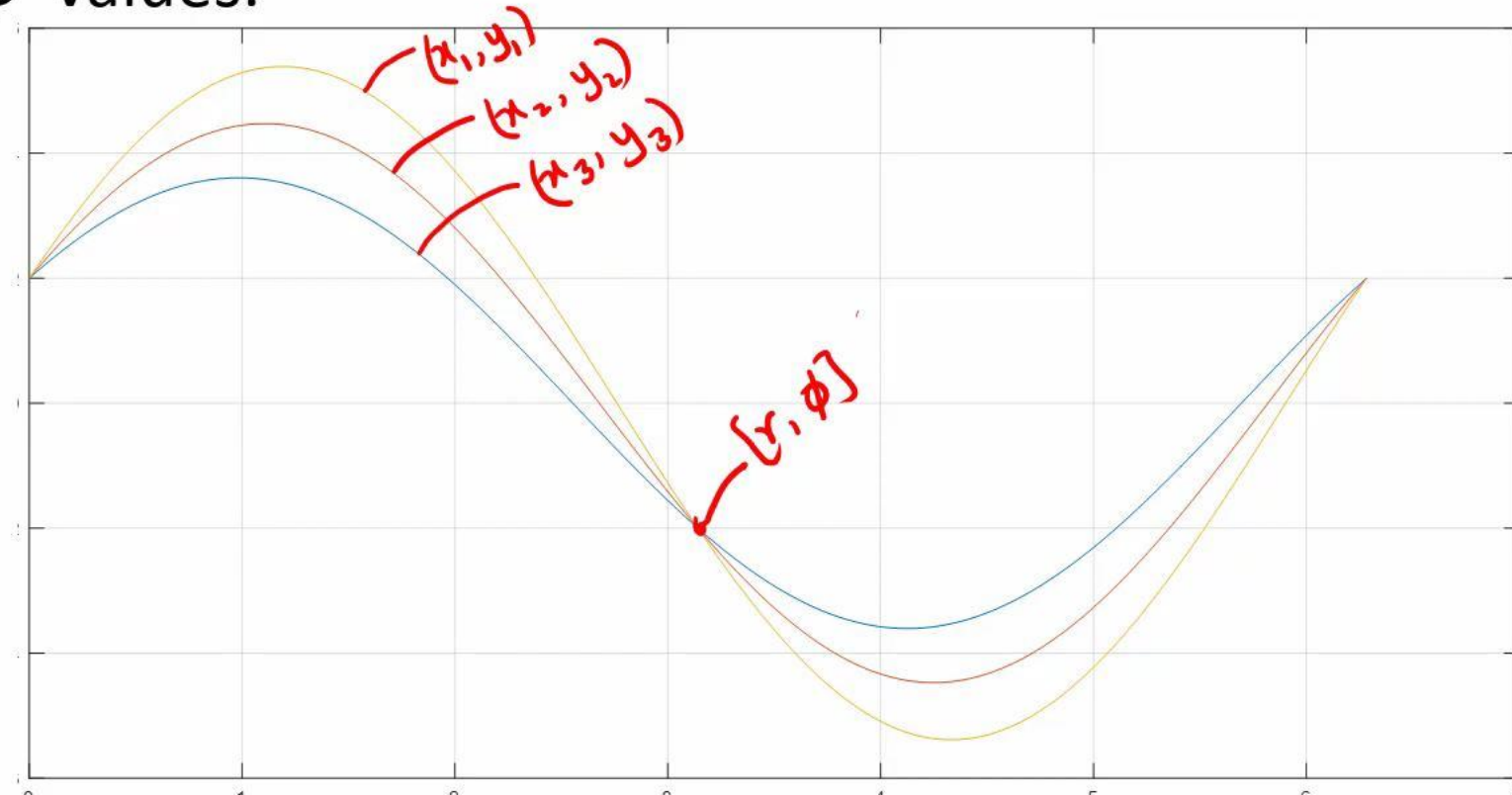


The Hough Transform



Line Detection

- All points which are **collinear** to this point will correspond to one common pair of ' r ' and ' ϕ ' values.

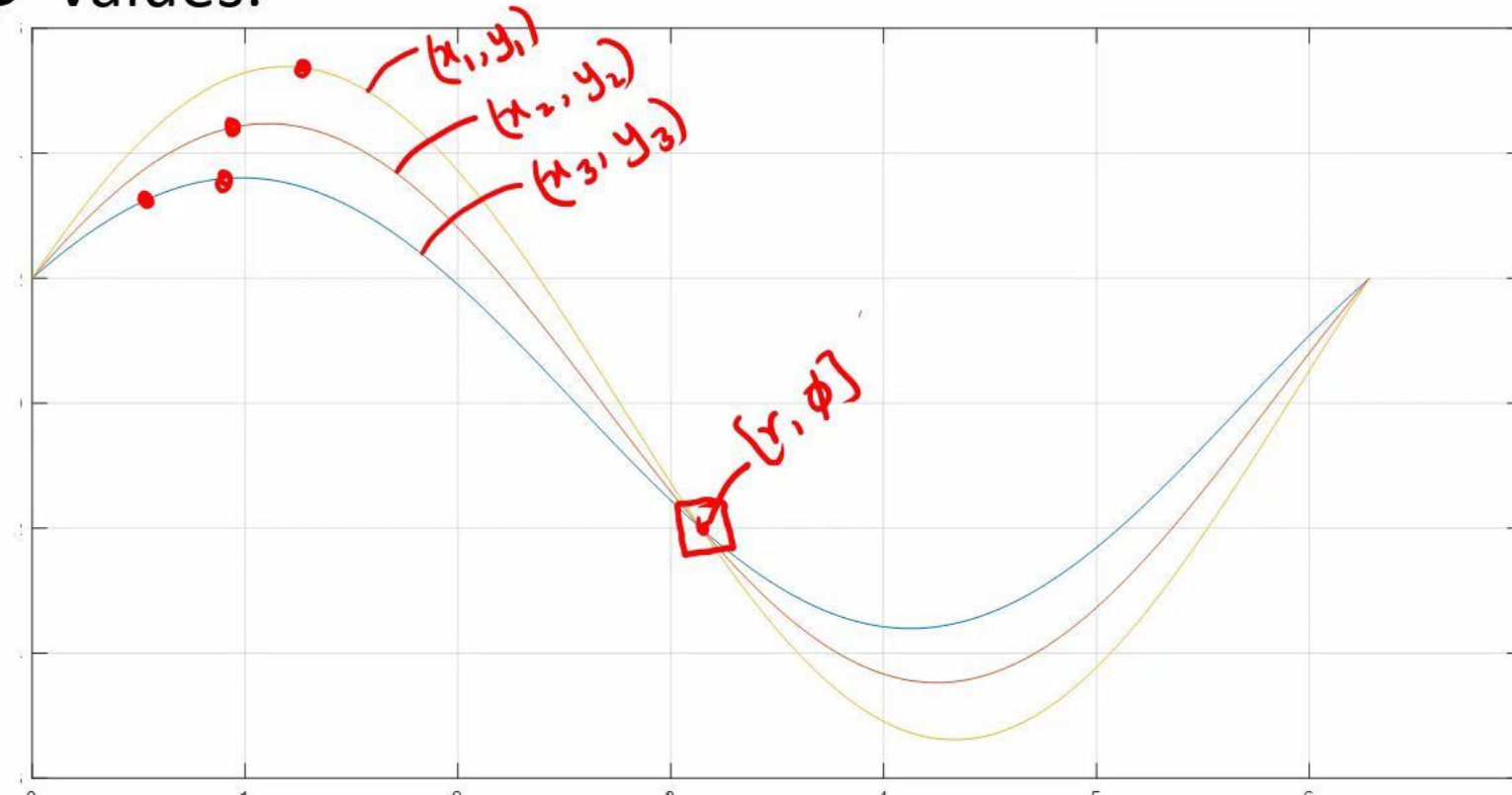


The Hough Transform

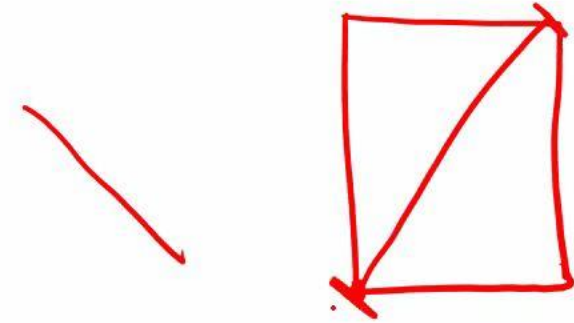


Line Detection

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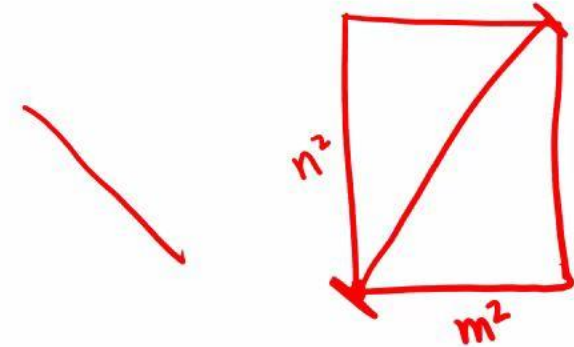
The Hough Transform



Line Detection

- Since now we have two variables ' r ' and ' ϕ ' we need to discretize them.
- Φ is ranging from '0' to '180' and if we use a resolution of 1 deg. then we will have 180 discrete values of ϕ .
- For ' r ' maximum distance from the origin may be a limit, which effectively will be the pixel location that is farthest from the origin, i.e. $\text{sqrt}(m^2+n^2)$.

The Hough Transform



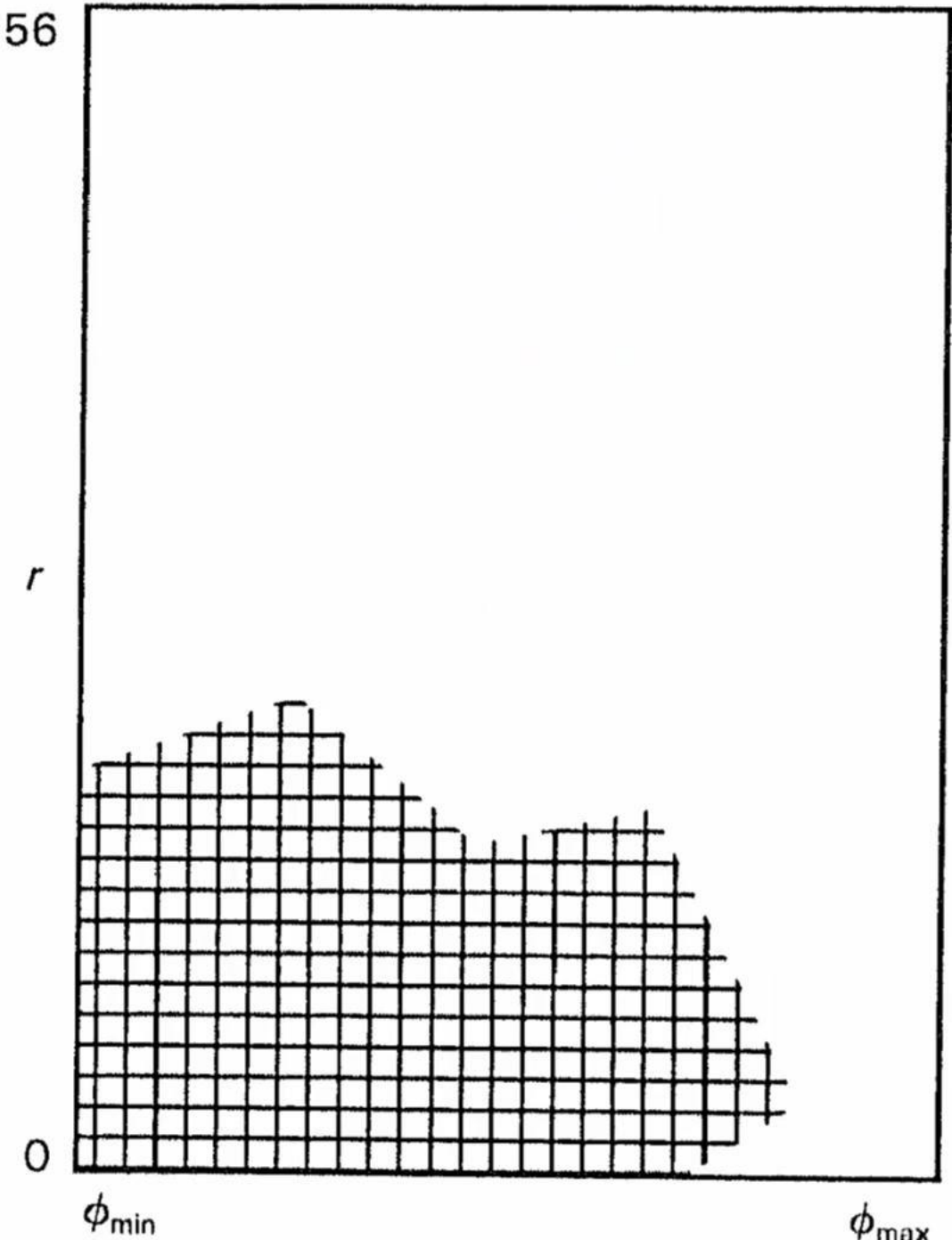
Line Detection

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- ϕ is ranging from '0' to '180' and if we use a resolution of 1 deg. then we will have 180 discrete values of ϕ .
- For ' r ' maximum distance from the origin may be a limit, which effectively will be the pixel location that is farthest from the origin, i.e. $\text{sqrt}(m^2+n^2)$.
- Our representation of $(r-\phi)$ space is now simply a 2-dimensional array of size, let 300x180, each element corresponding to a pair of ' r ' and ' ϕ '.

The Hough Transform

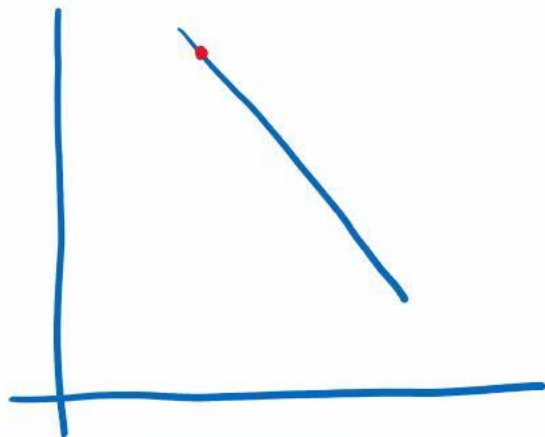
Line Detection

- This is called an **accumulator** since we are going to accumulate evidence of curves given by particular boundary points (x,y) in the image plane.



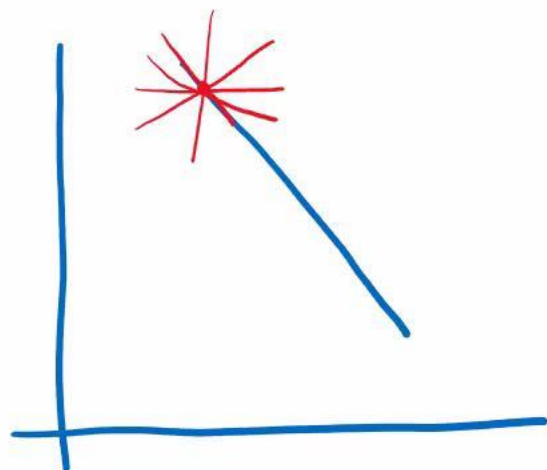


Hough Transform



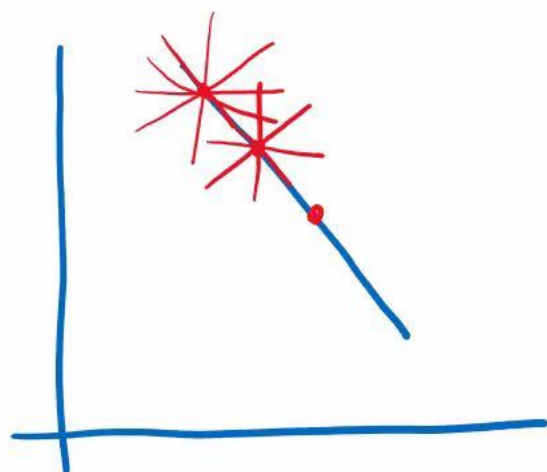


Hough Transform



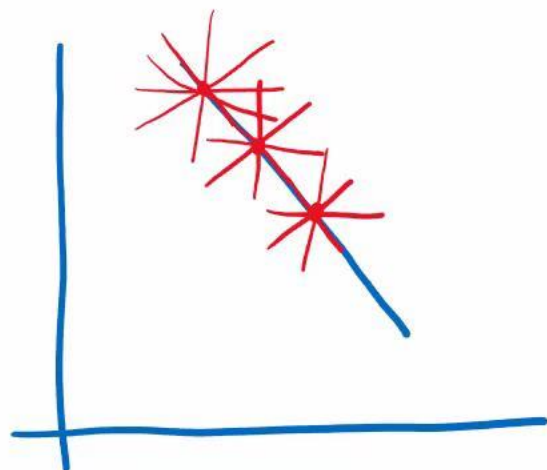


Hough Transform



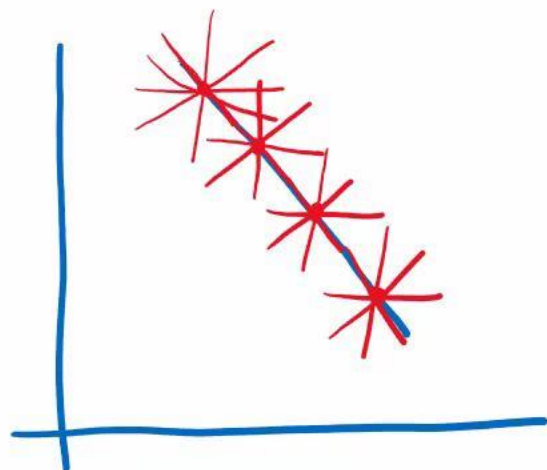


Hough Transform



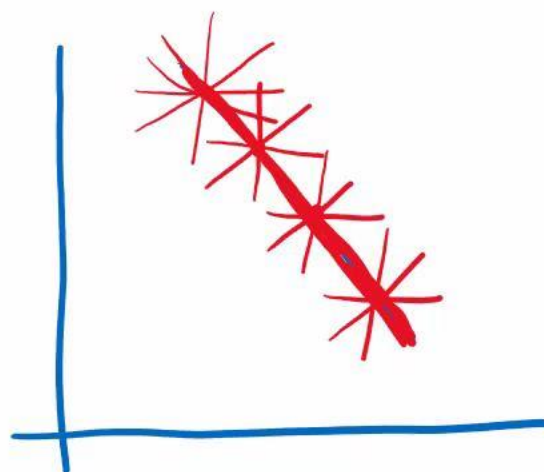


Hough Transform



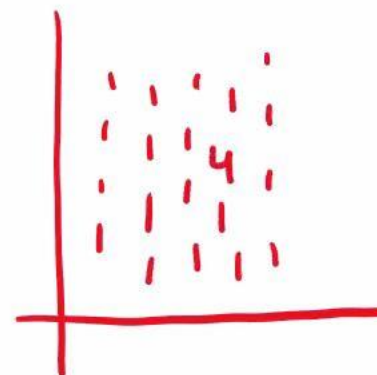
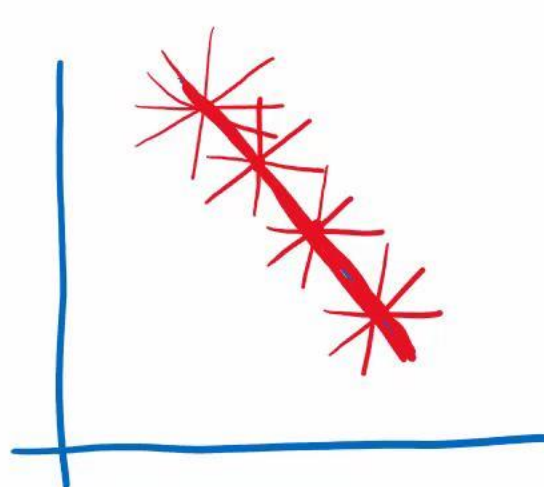


Hough Transform



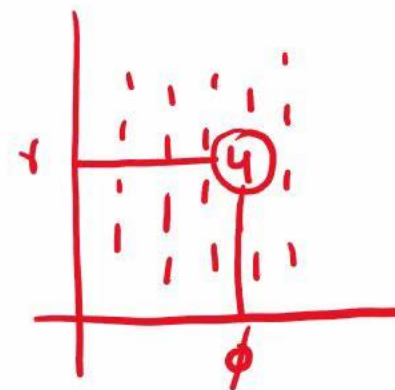
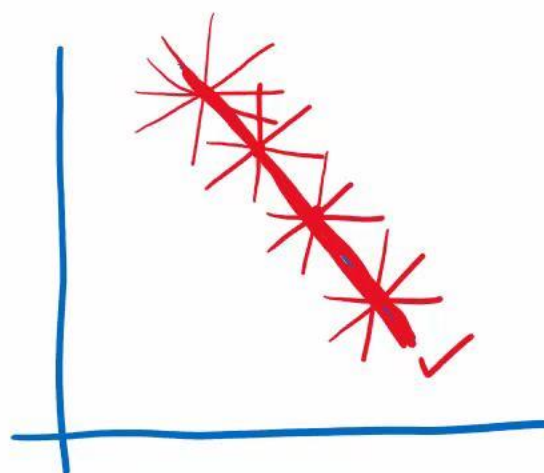


Hough Transform





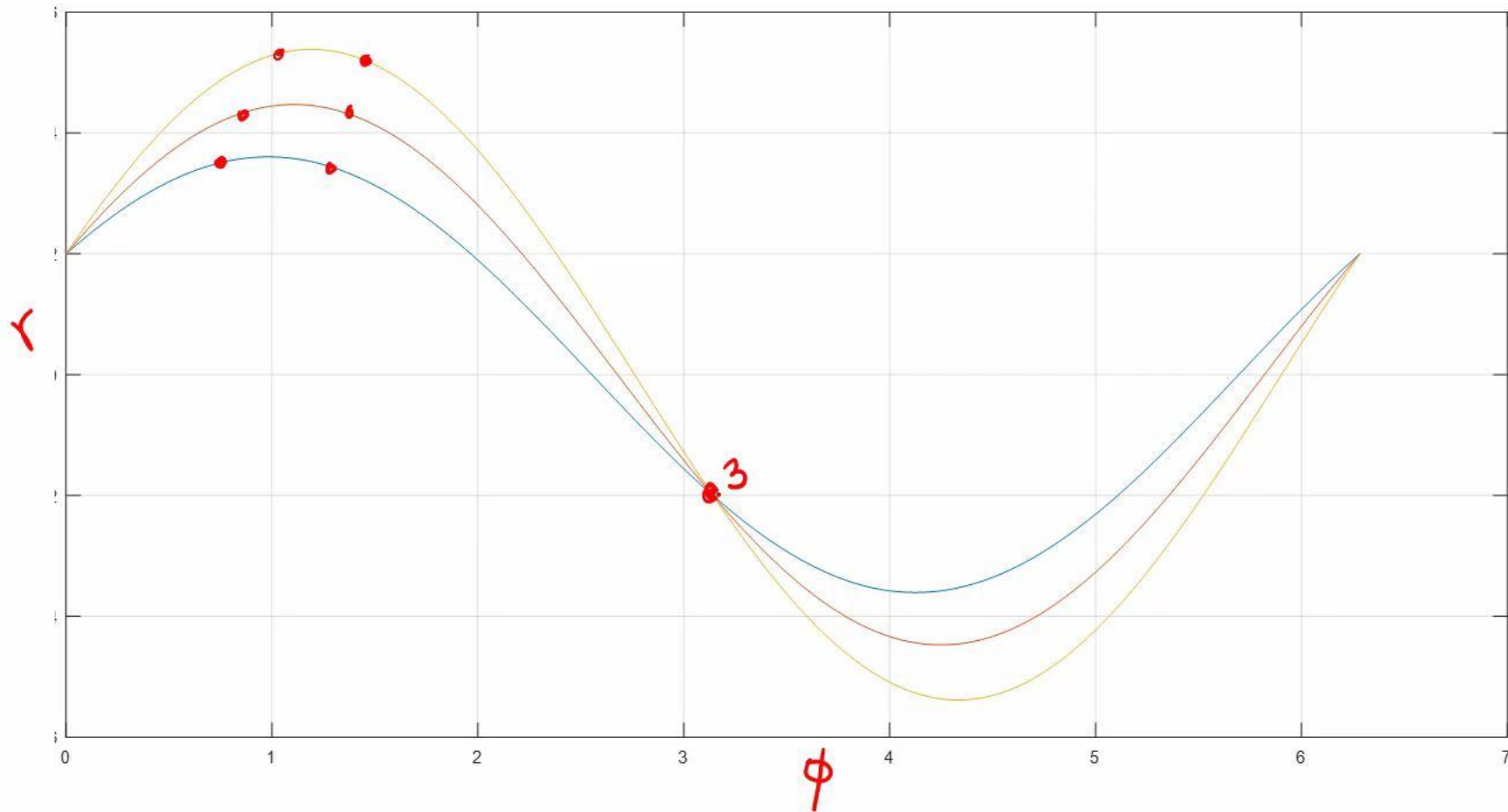
Hough Transform



The Hough Transform



Line Detection



The Hough Transform



Circle Detection

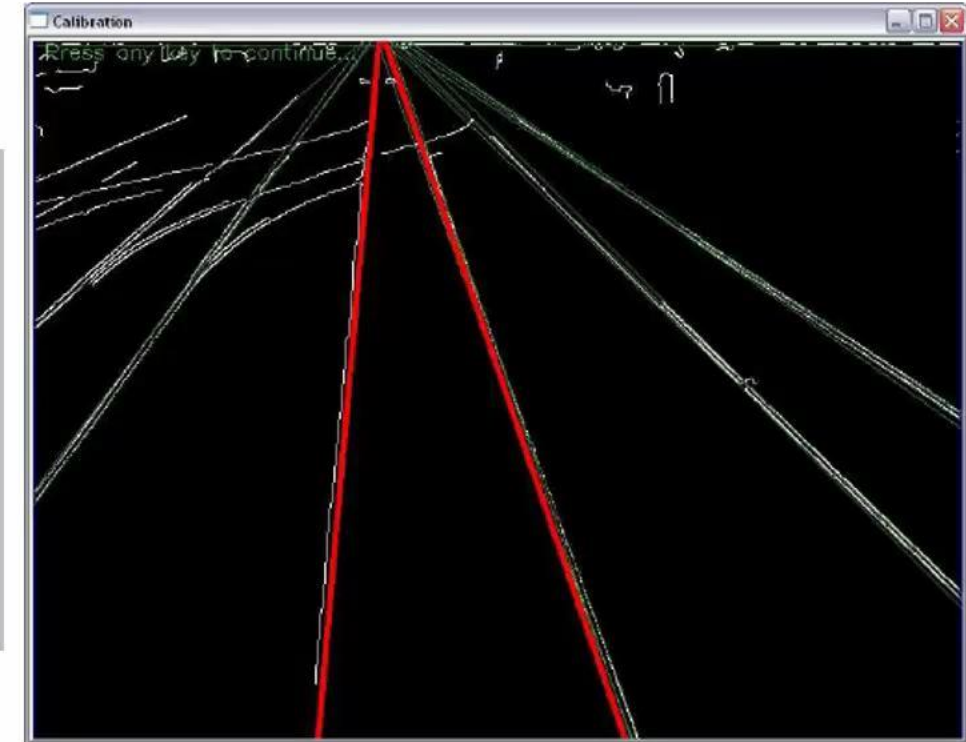
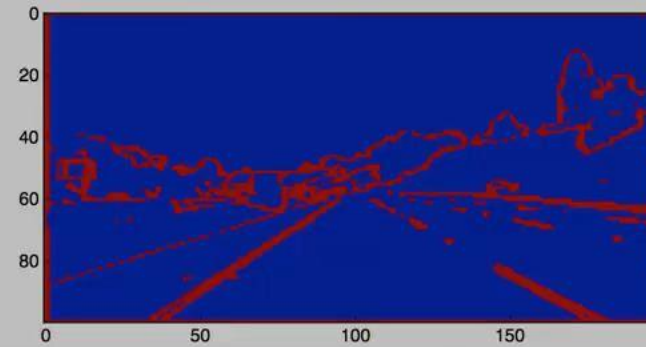
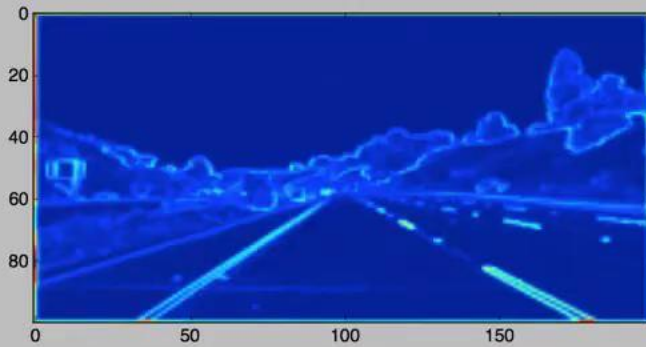
- Parametric equation of a circle is given as

$$(x - a)^2 + (y - b)^2 = r^2$$

The Hough Transform



Line Detection



The Hough Transform



Circle Detection

