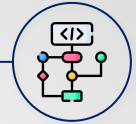


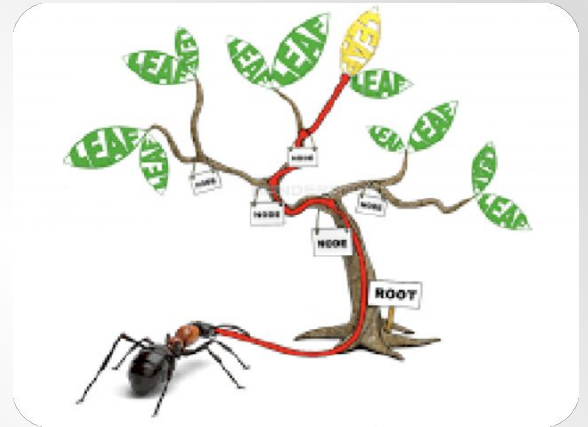
# Data structure and Algorithms



Presented by : Asmaa Ghonaim



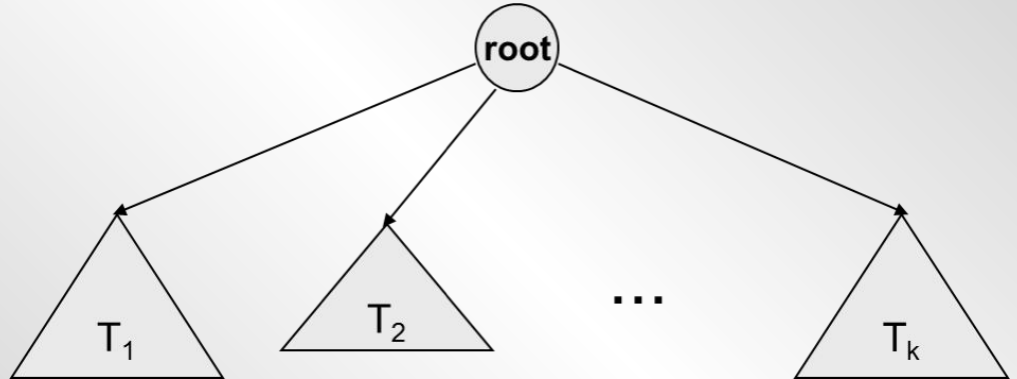
# Trees



# Trees

A **tree** is a collection of **nodes** with the following properties:

- The collection can be empty.
- Otherwise, a tree consists of a distinguished node **r**, called **root**, and **zero or more** non empty **sub-trees**  $T_1, T_2, \dots, T_k$ , each of whose roots are connected by a directed **edge[path]** from **r**.
- The **root** of each sub-tree is said to be **child of r**, and **r** is the parent of each sub-tree root.



# Trees

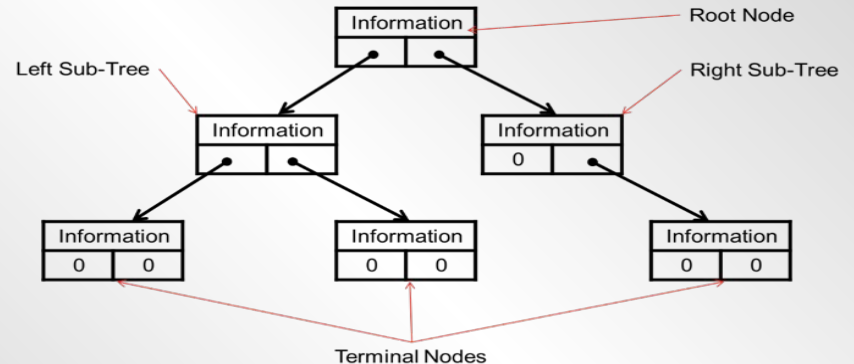
## Terminology of Trees:

- **Node** (also called a **Leaf**): is any data item in the tree.
- **Root Node**(also called **Parent Node**) : is the first item in the tree.
- **Subtree**: is any piece (i.e., branch) of thy tree.
- **Terminal Node**: is a node that has no subtrees attached to it.
- **Tree Height**: is equal to the number of layers deep that its root grows.
- If a tree is a collection of **N** nodes, then it has **N-1** edges.

N nodes = 6

$N - 1$  edges = 5

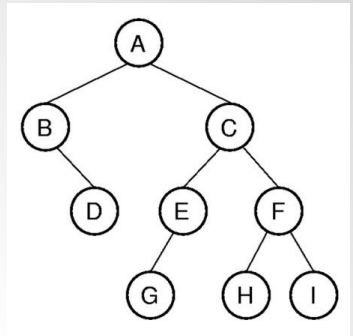
Tree Height = 3



# Trees

## Terminology of Trees:

- A **path** from node  $n_1$  to  $n_k$  is defined as a sequence of nodes  $n_1, n_2, \dots, n_k$  such that  $n_i$  is parent of  $n_{i+1}$  ( $1 \leq i < k$ )
- The **length of a path** is the **number of direct edges** on that path.
- There is a path of length **zero** from every **node to itself**.
- There is exactly **one path** from the **root** to each **node**.
- The **depth** of node  $n_i$  is the **length of the path from root to node  $n_i$**
- The **height** of node  $n_i$  is the **length of longest path** from node  $n_i$  to a leaf.



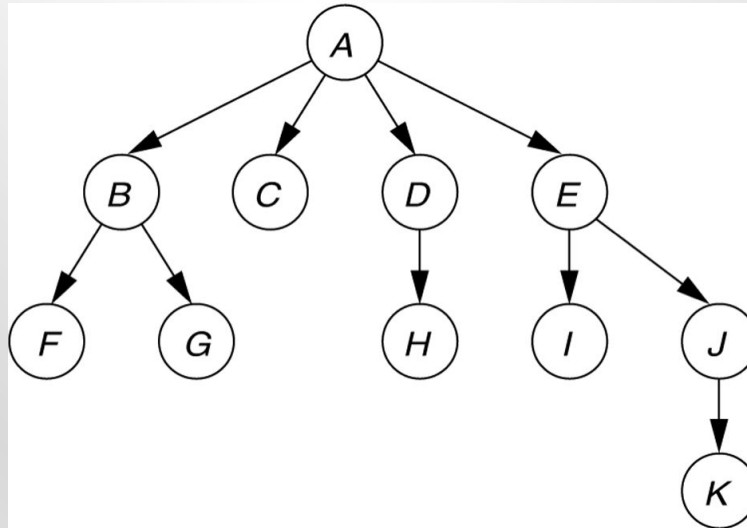
# Trees

→ A tree, with height and depth information for each Node

N nodes = **11**

N - 1 edges = **10**

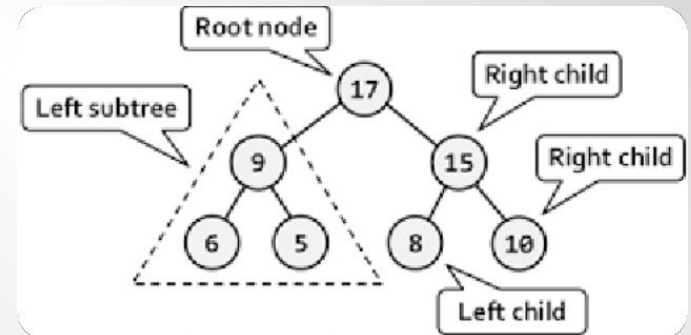
Tree Height = **4**



Node	Height	Depth
A	3	0
B	1	1
C	0	1
D	1	1
E	2	1
F	0	2
G	0	2
H	0	2
I	0	2
J	1	2
K	0	3

# Binary Trees

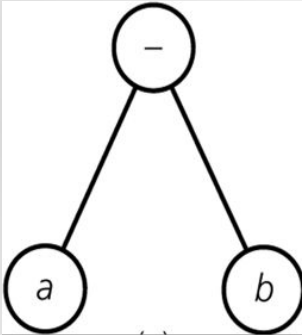
- Binary Trees are special type of Trees because, when they are sorted, they lend themselves to rapid searches, insertions, and deletions.
- Binary Tree is a non-linear and hierarchical data structure where each node has at most two children referred to as the left child and the right child.
- The Binary Tree is a special form of Linked List:
  - Items can be inserted, deleted, and accessed in any order.
  - Also, the retrieval operation is nondestructive.



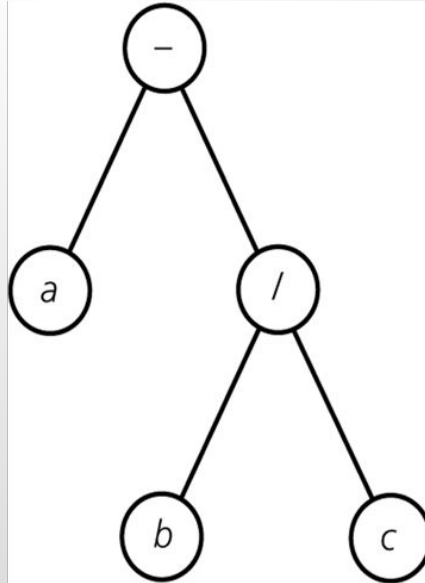
# Binary Trees

## Binary Tree – Representing Algebraic Expressions:

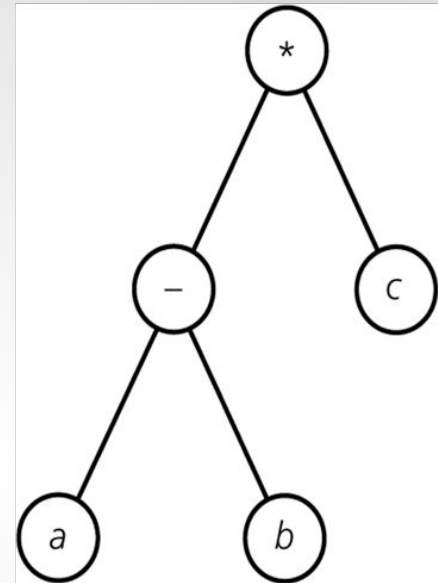
$a - b$



$a - b/c$



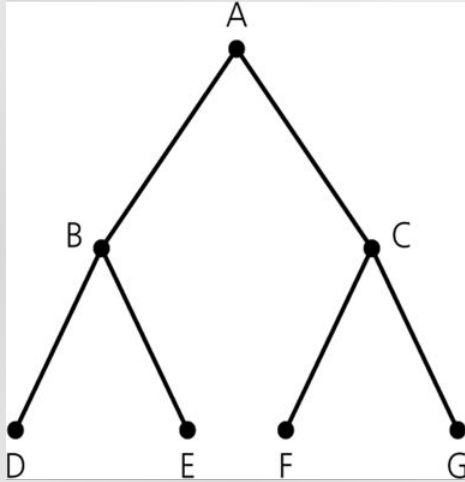
$(a - b) * c$



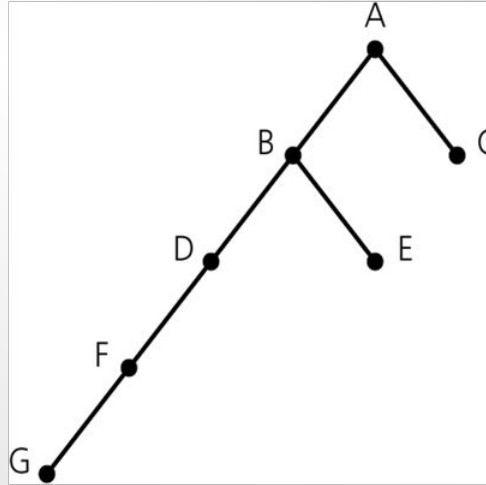


# Binary Trees

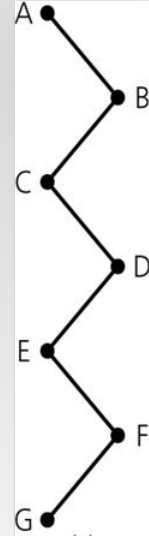
## Height of Binary Tree



3



5

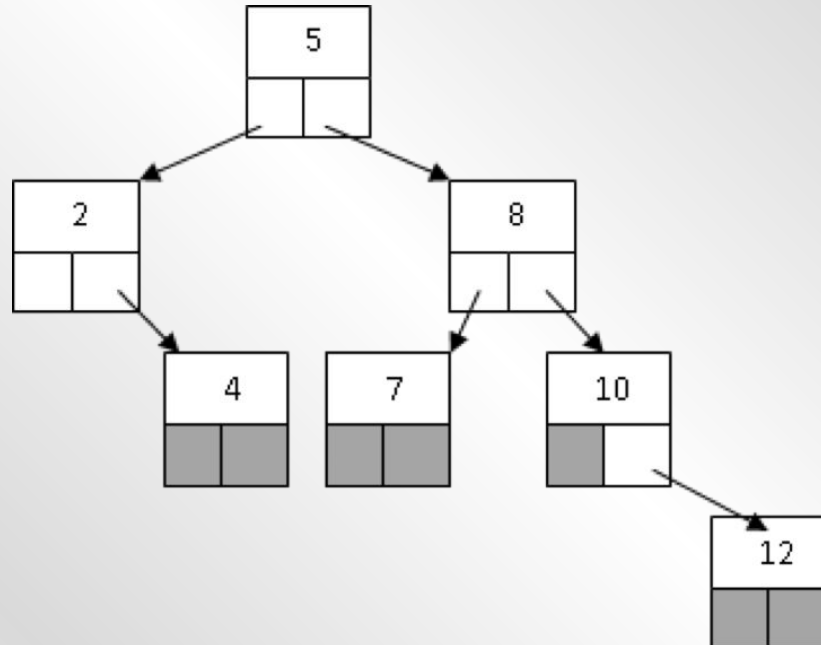


7

Binary trees with the same nodes but different heights

# Binary Trees

**Represent these values in binary tree (5, 8, 2, 4, 10, 12, 7)**



# Binary Trees

## → Traversing Binary Trees:

- ◆ is the process of accessing each node in a tree

## → Depth-first search:

- ◆ How a tree is ordered depends on how it is going to be accessed. Generally, there are three ways to traverse a tree:
- ◆ **Inorder**: you visit the **left** subtree, the **root**, and then the **right** subtree.
- ◆ **Preorder**: you visit the **root**, the **left** subtree and then the **right** subtree.
- ◆ **Postorder**: you visit the **left** subtree, the **right** subtree, and then the **root**.

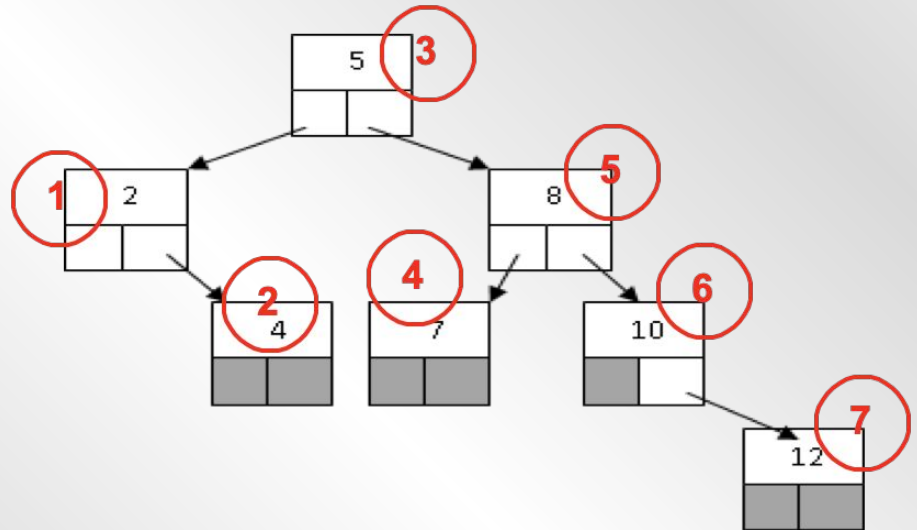
## → **Sorted Binary Tree**: **inorder** traversing is one where the subtree on the left contains nodes that are less than or equal to the root, and those on the right are greater than the root.

# Binary Trees

→ Traversing Binary Trees:

- **Inorder:** you visit the left subtree, the root, and then the right subtree.

**2,4,5,7,8,10,12**

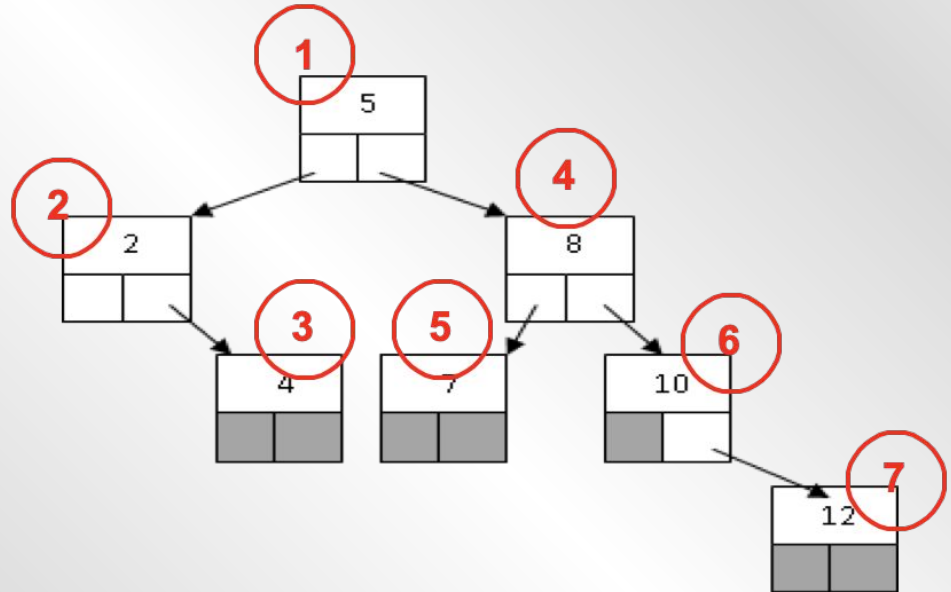


# Binary Trees

## → Traversing Binary Trees:

- **Preorder**: you visit the **root**, the **left** subtree and then the **right** subtree

**5,2,4,8,7,10,12**

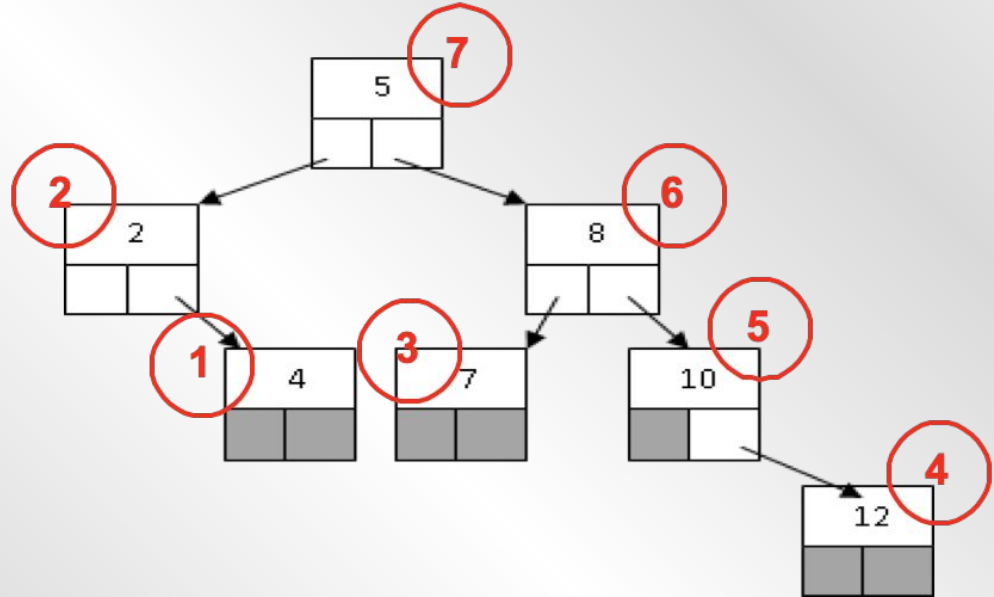


# Binary Trees

→ Traversing Binary Trees:

- **Postorder**: you visit the left subtree, the right subtree, and then the root.

**4,2,7,12,10,8,5**



# Binary Trees

## → Operations of Binary Tree

- ◆ Creating a Tree (Inserting New Nodes)
  - Case 1: insert root node.
  - Case 2: insert a leaf node.
- ◆ Traversing the Tree
  - Method 1: Inorder.
  - Method 2: Preorder.
  - Method 3: Postorder.
- ◆ Searching for a particular Node.
- ◆ Tree Height
- ◆ Deleting Nodes
  - Case 1: delete a leaf node.
  - Case 2: delete a node with one subtree.
  - Case 3: delete a node with two subtree

# Binary Trees

**Building a Binary tree using Employee as tree node:**

```
class Employee {  
    :  
    :  
    int Code;  
public:  
    Employee *pRight;  
    Employee *pLeft;  
};
```



# Binary Trees

**Building a Binary tree using Employee as tree node:**

```
class BinaryTree{  
    Employee *pParent;  
    Employee *insert(Employee *pRoot, Employee *data);  
    void inOrder(Employee *pRoot);  
    void preOrder(Employee *pRoot);  
    void postOrder(Employee *pRoot);  
    Employee * deleteT(Employee *pRoot, int key );  
    int getHeight(Employee *pRoot);  
}
```

# Binary Trees

**Building a Binary tree using Employee as tree node:**

**public:**

```
Binary(); {  
    pParent = NULL; }  
void insertNode(Employee *data);  
Employee *searchTree(int code);  
void inOrderTraverse();  
void preOrderTraverse();  
void postOrderTraverse();  
void deleteNode(int key );  
int getTreeHeight();
```

# Binary Trees

## Building a Binary tree [Insert method]:

```
public void BinaryTree::insertNode ( Employee * data){  
    pParent = insert(pParent , data); }  
  
private Employee * BinaryTree::insert ( Employee * pRoot, Employee *data){  
    // 1. If the tree is empty , return a new single node as a root of the tree  
    if (pRoot == NULL){  
        data->pRight = NULL; data->pLeft = NULL;  
        return (data); }  
    // 2. otherwise , go down to insert it in the right place  
    else { if (data->getCode() <= pRoot->getCode())  
        pRoot->pLeft = insert(pRoot->pLeft,data);  
    else  
        pRoot->pRight= insert(pRoot->pRight,data);  
    return(pRoot); // return the unchanged pParent pointer } }
```

# Binary Trees

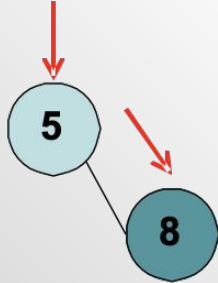
## Building a Binary tree [Insert method]

Insert 5,8,2,4

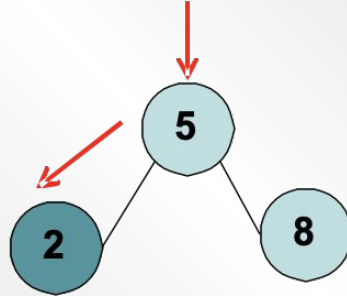
Insert 5



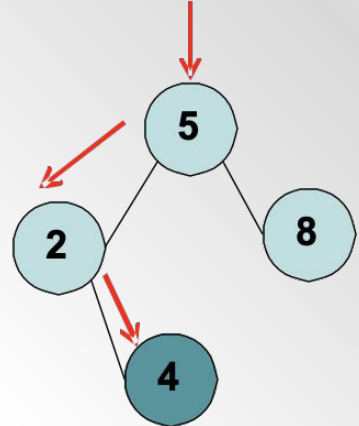
Insert 8



Insert 2



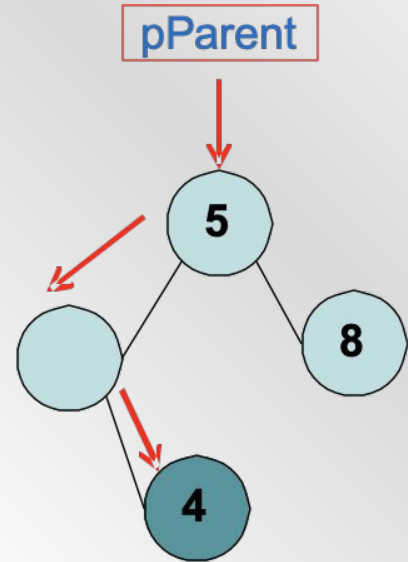
Insert 4



# Binary Trees

## Building a Binary tree [search method]:

```
public Employee * BinaryTree::searchTree( int code){  
    Employee *pRoot;  
    pRoot = pParent;  
    while (pRoot && code != pRoot->getCode()) {  
        if(code < pRoot ->getCode())  
            pRoot = pRoot -> pLeft ;  
        else  
            pRoot = pRoot -> pRight ; }  
    return pRoot; }
```

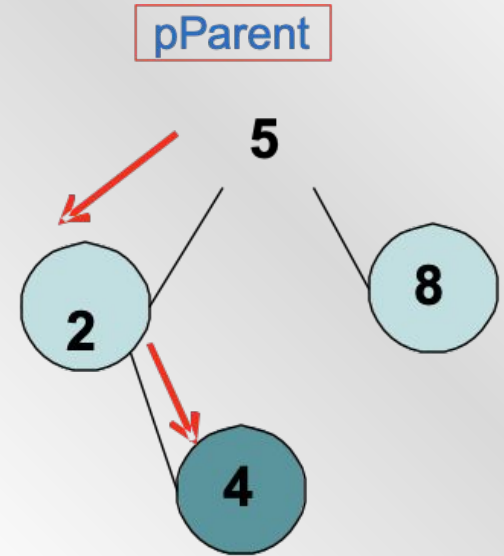


**Find 2**

# Binary Trees

## Building a Binary tree [inOrderTraverse method]:

```
public void BinaryTree::inOrderTraverse (){  
    inOrder (pParent);  
}  
  
private void BinaryTree::inOrder ( Employee * pRoot){  
    if (pRoot){  
        inOrder(pRoot ->pLeft);  
        cout<<"Code : " << pRoot ->getCode()<<endl;  
        inOrder(pRoot ->pRight);  
    }  
}
```



**Call inOrderTraverse()**

# Binary Trees

## Building a Binary tree [preOrderTraverse method]:

```
public void BinaryTree::preOrderTraverse (){  
    preOrder (pParent);  
}  
private void BinaryTree::preOrder( Employee * pRoot){  
    if (pRoot){  
        cout<<"Code : " << pRoot ->getCode()<<endl;  
        preOrder(pRoot ->pLeft);  
        preOrder(pRoot ->pRight);  
    }  
}
```

**Call preOrderTraverse()**

# Binary Trees

## Building a Binary tree [postOrderTraverse method]:

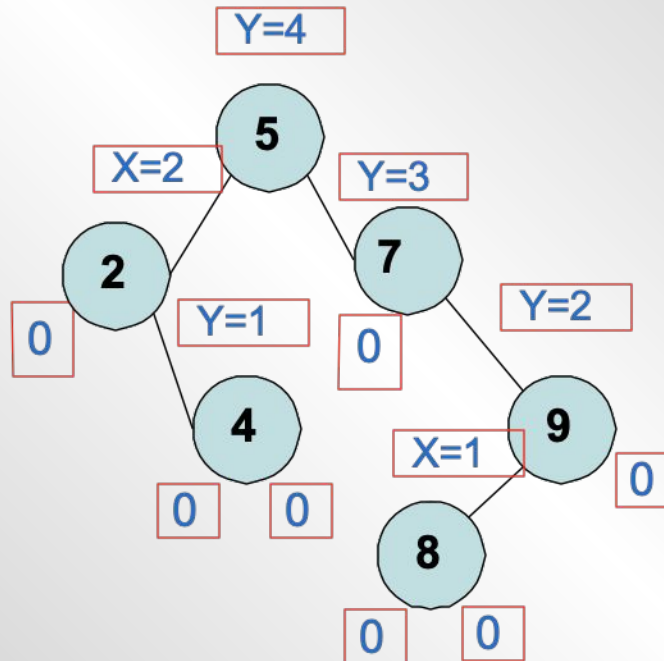
```
public void BinaryTree::postOrderTraverse (){  
  
    postOrder (pParent);  
}  
private void BinaryTree::postOrder ( Employee * pRoot){  
    if (pRoot){  
        postOrder(pRoot ->pLeft);  
        postOrder(pRoot ->pRight);  
        cout<<"Code : " << pRoot ->getCode()<<endl;  
    }  
}
```

**Call postOrderTraverse()**



# Binary Trees

**Building a Binary tree [Tree Height method]:**



# Binary Trees

## Building a Binary tree [Delete method]:

There are three cases to consider

- Case 1: delete a leaf node.

Replace the link to the deleted node by NULL.

- Case 2: delete a node with one subtree.

The node can be deleted after its parent adjusts a link to bypass the node.

- Case 3: delete a node with two subtree.

The deleted value must be replaced by an existing value that is either one of the following:

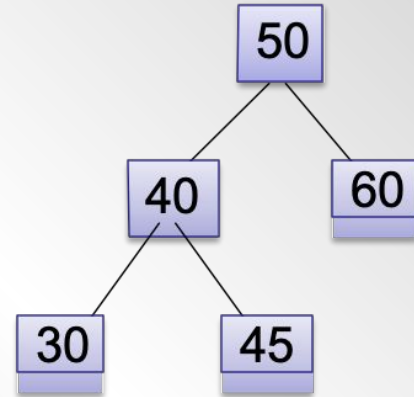
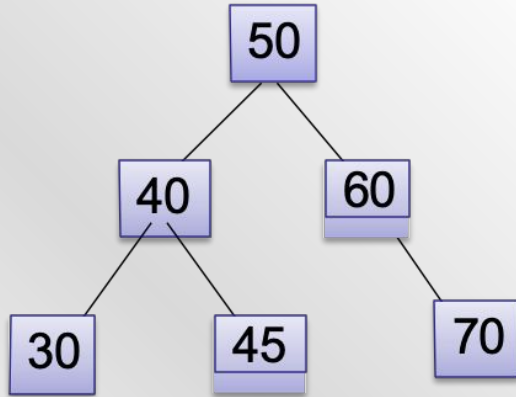
- The largest value in the deleted node's left subtree
- The smallest value in the deleted node's right subtree.

# Binary Trees

## Building a Binary tree [Delete method]:

### Case 1: delete a leaf node [70].

Replace the link to the deleted node by NULL.

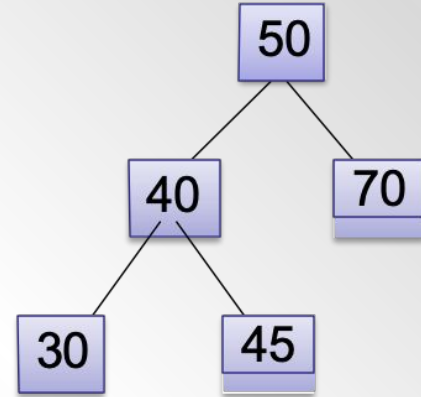
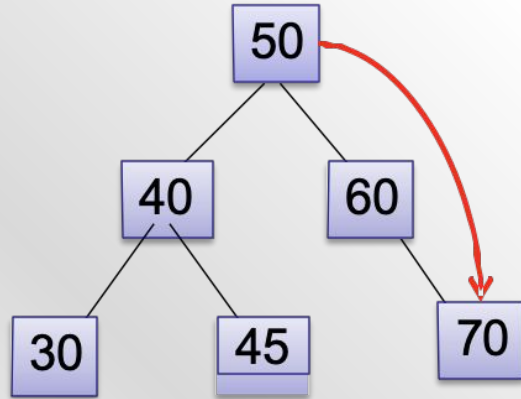


# Binary Trees

## Building a Binary tree [Delete method]:

### Case 2: delete a node with one subtree [60].

The node can be deleted after its parent adjusts a link to bypass the node.



# Binary Trees

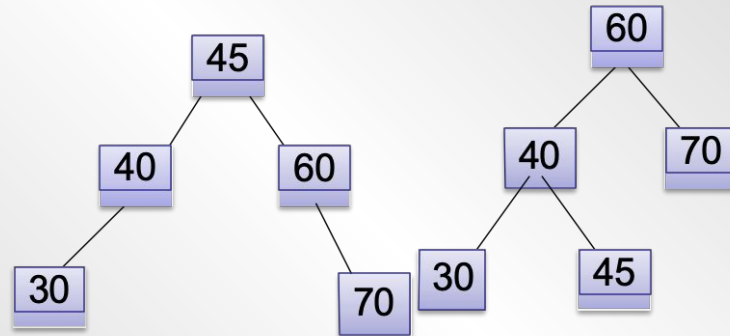
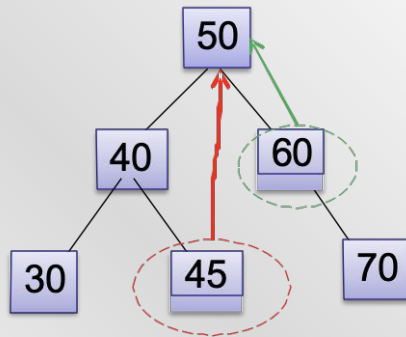
## Building a Binary tree [Delete method]:

### Case 3: delete a node with two subtree [50].

The deleted value must be replaced for its other childs by an existing value that is either one of the following:

- The largest value in the deleted node's left subtree

- The smallest value in the deleted node's right subtree.



# Lab **Exercise**

# Assignments :

- Implement delete method on Binary Tree.
- Implement and trace `getTreeHeight` function in the slide on Binary Tree
- Write a code to check if the employee linked list appears as a downward path in a binary tree.

Example:



- **Bonus:** Implement a function that will count the leaves of a binary tree.

# THANKS!