

LAB 3: Discrete-Time Fourier Series

Objective

In Lab 3, you will learn about discrete-time Fourier series (DTFS). You will implement DFTS and discrete-time Fourier series (IDFTS) by MATLAB. You also will examine some properties of DFTS.

Discrete-Time Fourier Series

The Discrete-time Fourier series D_r for a periodic signal $x[n]$ with the fundamental period N_0 is defined as follows

$$x[n] = \sum_{r=0}^{N_0-1} D_r e^{jr\Omega_0 n}$$

$$D_r = \frac{1}{N_0} \sum_{n=0}^{N_0-1} x[n] e^{-jr\Omega_0 n}$$

where, $\Omega_0 = \frac{2\pi}{N_0}$ is the fundamental frequency.

Preparation

- Read chapter 9, specially section 9.1, from *Linear Signals and Systems* by B.P. Lathi.
- Work through Computer Example 9.2 of the text.
- Work through Computer Example 9.7-1, and 9.7-2 of the text.

Lab Assignment

A. Discrete-Time Fourier Series

In this assignment, you will find the discrete-time Fourier series of the signal $x[n]$.

$$x[n] = 4 \cos(2.4\pi n) + 2 \sin(3.2\pi n)$$

- 1) Find the fundamental period N_0 and fundamental frequency Ω_0 of $x[n]$.
- 2) Use MATLAB to compute the DTFS of the signal $x[n]$ by implementing Eq. (9.4) from the textbook. Plot $x[n]$, the magnitude $|D_r|$ and phase $\angle D_r$ spectra with respect to r .
- 3) Repeat steps 1 and 2 for the signal $y[n]$ depicted in Figure 1.

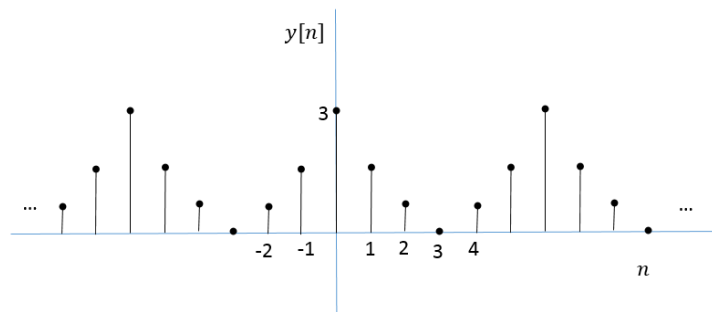


Figure 1

B. Inverse DTFS and time shifting property

In this assignment, you will compute the inverse discrete Fourier transform and examine the time shifting property.

- 1) The Fourier series spectrum of a periodic discrete signal is shown in Figure 2. Use MATLAB to implement the inverse DTFS and find the $x[n]$. Plot $x[n]$ with respect to n .

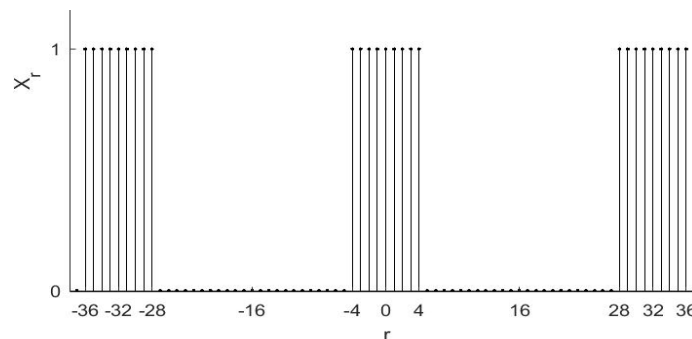


Figure 2

- 2) Multiply $X[r]$ to $e^{-j5\Omega_0 r}$ and find the inverse DTFS of the product. Plot the result and explain how it differs from $x[n]$ in part 1.

C. System Response

In this assignment, you will compute the response of an LTID system to an input signal using DTFS.

- 1) Consider an LTID system with frequency response $H[r]$ as depicted in Figure 3. For $N_0 = 32$ and $\Omega_0 = 2\pi/N_0$, plot $H[r]$ with respect to Ω_0 .

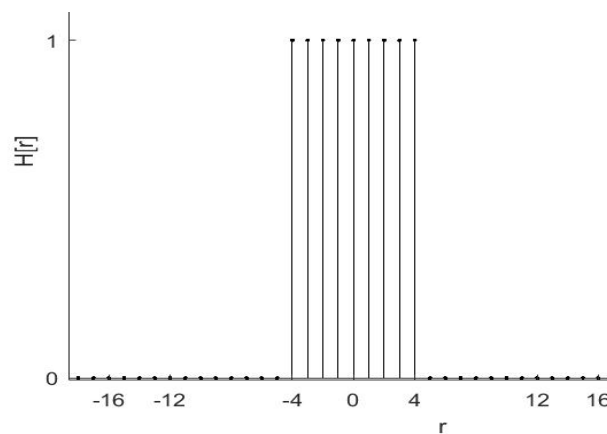


Figure 3

- 2) Find and plot the output $y_1[n]$ if the input $x_1[n]$ is applied to the system. For this purpose, find the DTFS of signal $x[n]$ and then compute $Y_1[r] = X_1[r]H[r]$.

$$x_1[n] = 4 \cos(\pi n / 8)$$

- 3) Repeat part 2 for the signal $x_2[n]$ defined below,

$$x_2[n] = 4 \cos(\pi n / 2)$$

- 4) Compare the results in part 1 and 2 and discuss why they are different.