

28-7-2021

Mo

1) What is Hashing?

Hashing is a data structure is a two-step process. The hash function converts the item into a small integer or hash value.

This integer is used as an index to store the original data. It stores the data in hash table. You can use a hash key to locate data quickly.

2) What is collision?

A collision occurs when more than one value to be hashed by a particular hash function hash to be same slot in the table or data structure (hash being generated by the hash function).

3) What is different type of collision

- 1) Open hashing / Chaining
- 2) Close Hashing / Open addressing

Different types of hashing function

- 1) $K \bmod 10$
- 2) $K \bmod N$
- 3) Mid Square
- 4) Folding Method

42, 16, 91, 33, 18, 27, 36, 62

42 mod 10

$$\begin{array}{r} 10 \overline{) 42} \\ 40 \\ \hline 2 \end{array}$$

$$\begin{array}{r} 10 \overline{) 91} \\ 90 \\ \hline 1 \end{array}$$

$$\begin{array}{r} 10 \overline{) 33} \\ 30 \\ \hline 3 \end{array}$$

$$\begin{array}{r} 10 \overline{) 18} \\ 10 \\ \hline 8 \end{array}$$

$$\begin{array}{r} 10 \overline{) 27} \\ 20 \\ \hline 7 \end{array}$$

k mod 10

36	0
91	1
42	2
33	3
	4
	5
16	6
27	7
18	8
1	9

$$RK_0 = (RK + i^2) \bmod 10$$

$$(6 + 1^2) \bmod 10$$

$$(6 + 1) \bmod 10$$

$$7 \bmod 10$$

$$RK_1 = (RK + i^2) \bmod 10$$

$$(7 + 2^2) \bmod 10$$

$$11 \bmod 10$$

$$\begin{array}{r} 10 \overline{) 11} \\ 10 \\ \hline 1 \end{array}$$

2

$$RK_2 = (RK + i^2) \bmod 10$$

$$(1 + 3^2) \bmod 10$$

$$10 \bmod 10$$

$$0$$

$$RK_3 = (RK + i^2) \bmod 10$$

$$(0 + 4^2) \bmod 10$$

$$16 \bmod 10$$

$$RK_4 = (RK + i^2) \bmod 10$$

$$(16 + 5^2) \bmod 10$$

$$41 \bmod 10$$

$$RK_5 = (RK + i^2) \bmod 10$$

$$(1 + 6^2) \bmod 10$$

$$1$$

Part Paper

Insert the following keys in hash table using hash function

$$h(x) = (2x+3) \bmod 10$$

7, 10, 11, 17, 20, 22, 25, 36, 42.

Chain

$$h(x) = 2x+3 \bmod 10$$

$$\bmod 2 \quad n-1$$

$$10-129$$

① 7

$$(2(7)+3) \bmod 10$$

$$(14+3) \bmod 10$$

$$17 \bmod 10$$

$$10 \overline{) 17}$$

② 10

$$(2(10)+3) \bmod 10$$

$$(20+3) \bmod 10$$

$$23 \bmod 10$$

$$10 \overline{) 23}$$

③ 11

$$(2(11)+3) \bmod 10$$

$$(22+3) \bmod 10$$

$$25 \bmod 10$$

$$10 \overline{) 25}$$

4) 17

$$(2(17)+3) \bmod 10$$

$$(34+3) \bmod 10$$

$$37 \bmod 10$$

$$10 \overline{) 37}$$

$$RK = (RK + 1) \bmod 10$$

5) 20

$$(2(20)+3) \bmod 10$$

$$(40+3) \bmod 10$$

$$43 \bmod 10$$

$$10 \overline{) 43}$$

6) 22

$$(2(22)+3) \bmod 10$$

$$(44+3) \bmod 10$$

$$47 \bmod 10$$

	0
	1
	2
Collision	10, 20, 30, 40
	4
Collision	11, 21
	5
Collision	7, 17, 27, 37, 47
	6
	7
	8
	9

$$10 \overline{) 17}$$



7) 21

$$(2(21)+3) \bmod 6$$

$$(42+3) \bmod 6$$

$$45 \bmod 6$$

$$10 \overline{) 45}$$

$$\underline{42}$$

8) 25

$$(2(25)+3) \bmod 6$$

$$(50+3) \bmod 6$$

$$53 \bmod 6$$

$$10 \overline{) 53}$$

$$\underline{50}$$

$$\underline{3}$$

9) 35

$$(2(35)+3) \bmod 6$$

$$(70+3) \bmod 6$$

$$10 \overline{) 73}$$

$$\underline{70}$$

$$\underline{3}$$

42

$$2(42)+3 \bmod 6$$

$$(84+3) \bmod 6$$

$$10 \overline{) 87}$$

$$\underline{80}$$

$$\underline{7}$$

Linear

Linear.

7, 10, 13, 17, 20, 23, 27, 30, 33, 37, 42

22

0	$h(n) = (2x+3) \bmod 10$	25	0
	$(2(7)+3) \bmod 10$		1
	$(14+3) \bmod 10$		2
	$17 \bmod 10$	10, 18, 26	3
10	$(2(10)+3) \bmod 10$	20	4
	$(20+3) \bmod 10$	4, 24	5
	$23 \bmod 10$	21	6
		7, 27	7
11	$(2(11)+3) \bmod 10$	17	8
	$(22+3) \bmod 10$	22	9
	$25 \bmod 10$		
	5		
17	$(2(17)+3) \bmod 10$		
	$(34+3) \bmod 10$		
	$37 \bmod 10$		

Linear.

7

$RK_2(RK+i) \bmod 10$

$(7+i) \bmod 10$

$8 \bmod 10$

8

20 $(2(20)+3) \bmod 10$

$(40+3) \bmod 10$

$43 \bmod 10$

$RK_2(RK+0) \bmod 10$

$(3+1) \bmod 10$

4 mod 10

22

$(2(22)+3) \bmod 10$

$44+3 \bmod 10$

47 mod 10

29-7-2021

Double hashing

$$h_1(k) = k \bmod 11$$

$$h_2(k) = 8 - (k \bmod 8) \quad \text{--- chote ho karna}$$

collision
formula

$$\text{Formula: } (h_1(k) + 2 \cdot h_2(k)) \bmod 11$$

20, 34, 45, 70, 86

$$h_1 = k \bmod 11$$

$$20 \bmod 11$$

$$\begin{array}{r} 11 \overline{) 20} \\ 11 \\ \hline 9 \end{array}$$

$$h_1 = 34 \bmod 11$$

$$\begin{array}{r} 3 \\ 11 \overline{) 34} \\ 33 \\ \hline 1 \end{array}$$

using h_2 formula

$$8 - (k \bmod 8)$$

$$8 - (5)$$

$$3$$

$$(1 + 2 \cdot (3)) \bmod 11$$

$$(7 + 6) \bmod 11$$

$$13 \bmod 11$$

$$2$$

34
56
45
70
20

$$70$$

$$20 \bmod 11$$

$$\begin{array}{r} 11 \overline{) 70} \\ 66 \\ \hline 4 \end{array}$$

$$\begin{array}{r} 11 \overline{) 20} \\ 11 \\ \hline 9 \end{array}$$

$$8 - (k \bmod 8)$$

$$8 - (70 \bmod 8) \quad 70 \div 8$$

$$8 - 6$$

$$2$$

$$2$$

$$(4 + 1 \cdot 2) \bmod 11$$

$$(6) \bmod 11$$

$$6$$

$$\begin{array}{r} 9 \\ 11 \overline{) 70} \\ 63 \\ \hline 7 \end{array}$$

$$\begin{array}{r} 11 \overline{) 70} \\ 66 \\ \hline 4 \end{array}$$

$$\underline{56}$$

$$\begin{array}{r} 56 \bmod 11 \\ 11 \overline{) 56} \\ \underline{55} \\ 1 \end{array}$$

$$\begin{array}{r} 8 \overline{) 56} \\ \underline{56} \\ 0 \end{array}$$

$$8 - (56 \bmod 8) \\ 8 - 0 = 8$$

$$(4 + 1 \cdot 8) \bmod 11$$

$$12 \bmod 11$$

$$1 \bmod 11$$

$$\begin{array}{r} 1 \overline{) 11} \\ \underline{11} \\ 0 \end{array}$$

$$11 \overline{) 11}$$

$$(6 + 2 \cdot 0) \bmod 11$$

$$(1 + 2 \cdot 8) \bmod 11 \\ 17 \bmod 11$$

$$\begin{array}{r} 1 \overline{) 17} \\ \underline{17} \\ 0 \end{array}$$

$$\frac{11}{6}$$

$$(1 + 3 \cdot 8) \bmod 11$$

$$(1 + 24) \bmod 11$$

$$25 \bmod 11$$

$$\begin{array}{r} 2 \overline{) 25} \\ \underline{22} \\ 3 \end{array}$$

Double

20, 34, 45, 70, 56

$$h_1(k) = k \bmod 11$$

$$h_2(k) = 8 - (k \bmod 8)$$

$$\text{Formula } (h_1(k) + i \cdot h_2(k)) \bmod 11$$

$$h_1(20) = 20 \bmod 11$$

$$\begin{array}{r} 11 \overline{) 20} \\ 11 \\ \hline 9 \end{array}$$

$$h_1(34) = 34 \bmod 11$$

$$\begin{array}{r} 3 \\ 11 \overline{) 34} \\ 33 \\ \hline 1 \end{array}$$

$$45 \bmod 11$$

$$\begin{array}{r} 4 \\ 11 \overline{) 45} \\ 44 \\ \hline 1 \end{array}$$

$$8 - (45 \bmod 8)$$

$$8 - 5$$

$$= 3$$

$$\begin{array}{r} 5 \\ 8 \overline{) 45} \\ 40 \\ \hline 5 \end{array}$$

$$(1 + (1 \cdot 3)) \bmod 4$$

$$(1 + 3) \bmod 4$$

$$4 \bmod 11$$

$$4$$

$$70 \bmod 11$$

$$\begin{array}{r} 6 \\ 11 \overline{) 70} \\ 66 \\ \hline 4 \end{array}$$

$$\begin{array}{r} 8 \\ 8 \overline{) 70} \\ 64 \\ \hline 6 \end{array}$$

$$70 \bmod 11$$

$$8 - (70 \bmod 8)$$

$$(8 - 6)$$

$$2$$

$$(4 + 1 \cdot 2) \bmod 11$$

$$6 \bmod 11 = 6$$

	0
34	1
	2
56	3
45	4
	5
70	6
	7
	8
20	9
	10

$$56$$

$$56 \bmod 11$$

$$\begin{array}{r} 5 \\ 11 \overline{) 56} \\ \underline{55} \\ 1 \end{array}$$

$$(5 - 1) \cdot 11 = 44$$

$$8 - 56 \bmod 8$$

$$8 - 0$$

$$8$$

$$\begin{array}{r} 7 \\ 8 \overline{) 56} \\ \underline{56} \\ 0 \end{array}$$

$$\begin{array}{r} 2 \\ 11 \overline{) 22} \\ \underline{22} \\ 0 \end{array}$$

$$(1 + (1 \cdot 8)) \bmod 4$$

$$(1 + 8) \bmod 4$$

$$(9) \bmod 11$$

$$9$$

$$1 + (2 \cdot 8) \bmod 11$$

$$17 \bmod 11$$

$$1 + (3 \cdot 8) \bmod 4$$

$$25 \bmod 4$$

$$\begin{array}{r} 1 \\ 11 \overline{) 11} \\ \underline{11} \\ 0 \end{array}$$

$$\begin{array}{r} 2 \\ 11 \overline{) 22} \\ \underline{22} \\ 0 \end{array}$$

26-7-2021

Ques

Hashing

∴ eg.
tags

database for used
data/entries of used pointer
used.

- 1) store data
- 2) Retrieve data

Different function are used to apply
hashing/mapping

↓
because value are stored
smaller.

Hashing

- 2, 4, 3, 2, 1) 1) Key (Search Key)
- 2) hash table
- 3) Hash function

$$K \bmod 10$$

$$n = 10$$

$$10 - 1$$

General function

ex. ex
(24, 16, 8, 9, 11)

$$24 \bmod 10$$

$$\begin{array}{r} 2 \\ 10 \overline{) 24} \\ \underline{20} \\ 4 \end{array}$$

$$11 \bmod 10$$

$$\begin{array}{r} 1 \\ 10 \overline{) 11} \\ \underline{10} \\ 1 \end{array}$$

11	0
	1
	2
	3
20	4
	5
16	6
	7
08	8
9	9

- 1) What is hashing
- 2) What is collision
- 3) What is different types of collision
- 4) Different function of hashing

Function

- 1) $K \text{ Mode } 10 \rightarrow 2-1$ values
- 2) $K \text{ Mode } N \rightarrow N+1$
- 3) Mid square $2(2)2 \rightarrow 2^2 = 4$
- 4) Folding Method

↓ If add of double

1 2 3 4 5 6

$$\begin{array}{r} 123 \\ 456 \\ \hline 579 \end{array}$$

Types of collision

- 1) Chaining / open hashing
- 2) Open addressing (close hashing)
 - (1) Linear
 - 2) Quadratic
 - 3) Double.

Chaining

42, 19, 10, 12, 22, 32, 34
K mode 5

42 mode

$$\begin{array}{r} 7 \\ 6 \overline{)42} \\ \underline{42} \\ 0 \end{array}$$

$$\begin{array}{r} 19 \\ 6 \overline{)19} \\ \underline{12} \\ 7 \end{array}$$

$$\begin{array}{r} 10 \\ 6 \overline{)10} \\ \underline{6} \\ 4 \end{array}$$

$$\begin{array}{r} 12 \\ 6 \overline{)12} \\ \underline{12} \\ 0 \end{array}$$

$$\begin{array}{r} 22 \\ 6 \overline{)22} \\ \underline{18} \\ 4 \end{array}$$

$$\begin{array}{r} 32 \\ 6 \overline{)32} \\ \underline{30} \\ 2 \end{array}$$

$$\begin{array}{r} 34 \\ 6 \overline{)34} \\ \underline{30} \\ 4 \end{array}$$

42, 12	0
19	1
10, 32	2
	3
10, 22, 34	4

42, 12	0	→	42	→	12
19	1	→	19		
10, 32	2	→	32		
	3				
10, 22, 34	4	→	10	→	22

Solved

42, 19, 10, 12, 22, 32, 34

K modes

6-125

42, 12	0	12
19	1	
32	2	
	3	
10, 22, 34	4	

→ Linear

42, 19, 10, 12, 22, 32, 34, 40, 77

K mode

$$\begin{array}{r} 42 \\ 10 \overline{) 42} \\ \underline{40} \\ 2 \end{array}$$

10	0
40	1
42	2
12	3
22	4
32	5
34	6
40	7
77	8
19	9

Formula
not good approach
Array divide
open hashing
class Linear map

Formula

Linear

$RK \pm (RK + i) \text{ mode } 10$

Example

43, 135, 72, 23, 99, 19, 82

$RK = (RK + 1) \text{ mod } 10$

43

$(43 + 1) \text{ mod } 10$

44 mod 10

$10 \overline{) 44}$
40
4

135

$(135 + 1) \text{ mod } 10$

136 mod 10

$10 \overline{) 136}$
100
36
2 36

$10 \overline{) 23}$
20
3

23

$RK = (RK + 1) \text{ mod } 10$

$(23 + 1) \text{ mod } 10$

24 mod 10

4

$10 \overline{) 24}$
20
4

99

$RK = (RK + 1) \text{ mod } 10$

$(99 + 1) \text{ mod } 10$

100 mod 10

82

$RK = (RK + 1) \text{ mod } 10$

$(82 + 1) \text{ mod } 10$

83 mod 10

3

99	0
	1
72	2
43	3
48 23	4
135	5
32	6
	7
	8
99	9

$20 \overline{) 23}$
20
3

$10 \overline{) 99}$
90
9

$10 \overline{) 100}$
100
0

$10 \overline{) 82}$
80
2

$$(2+2) \bmod 10$$

$$84 \bmod 10$$

$$\begin{array}{r} 8 \\ 10 \overline{) 84} \\ \underline{80} \\ 4 \end{array}$$

$$(2+4) \bmod 10$$

$$6 \bmod 10$$

(RK)

is C/addr of its key

- its value index

The keys 1, 3, 12, 4, 25, 6, 18, 20, 8 are inserted into empty hash table of length 10 using open addressing with hash function $H(i) = i^2 \text{ mod } 10$ and linear probing.

What is the resultant hash table and find the maximum probe value?

$$H(i) = i^2 \text{ mod } 10$$

20	9
1	1
	2
3	3
12, 18	4
25	5
4	6
6	7
8	8
3	9

$$1 \text{ mod } 10$$

$$3 \text{ mod } 10$$

$$12 \text{ mod } 10$$

$$10 \text{ mod } 10$$

$$H(1) = 1^2 \text{ mod } 10$$

$$H(3) = 3^2 \text{ mod } 10$$

$$3 = 1^2 \text{ mod } 10$$

$$9 \text{ mod } 10$$

$$12 = 12^2 \text{ mod } 10$$

$$144 \text{ mod } 10$$

$$4 = 4^2 \bmod 10$$

$$16 \bmod 10$$

$$10 \overline{) 16}$$

$$\underline{10}$$

$$6$$

$$\begin{array}{r} 28 \\ 28 \\ \hline 125 \\ 80 \\ \hline 628 \end{array}$$

6

$$25 = 25^2 \bmod 10$$

$$625 \bmod 10$$

$$= 5$$

$$10 \overline{) 625}$$

$$\underline{600}$$

$$25$$

$$6 = 6^2 \bmod 10$$

$$36 \bmod 10$$

$$10 \overline{) 36}$$

$$\underline{30}$$

$$6$$

$$6 = (RK + 1) \bmod 10$$

$$(6 + 1) \bmod 10$$

$$7 \bmod 10$$

$$= 7$$

$$12 = 12^2 \bmod 10$$

$$324 \bmod 10$$

$$10 \overline{) 324}$$

$$\underline{320}$$

$$4$$

$$\begin{array}{r} 32 \\ 32 \\ \hline 00 \\ 300 \\ \hline 320 \end{array}$$

(4+1)

$$20 = 20^2 \bmod 10$$

$$400 \bmod 10$$

$$10 \overline{) 400}$$

$$\underline{400}$$

$$0$$

(5+1)

$$2 = 2^2 \bmod 10$$

$$4 \bmod 10$$

$$10 \overline{) 4}$$

$$4$$

$$RK = (RK + 1) \bmod 10$$

$$(4 + 1) \bmod 10$$

$$5 \bmod 10$$

$$RK \neq (RK + 1) \bmod 10$$

$$4 = (4 + 2) \bmod 10$$

$$6 \bmod 10$$

20
1
8
12
25
4
6
17
3

Advantages of Hashing

- 1) more reliable and flexible method of data retrieval than any other data structure.
- 2) faster than searching arrays and lists.
- 3) Same space it can store in n probes
- any stored in a tree that will otherwise take $\log n$ probes.
- 4) does not allow null values like hash ^{map} ~~map~~

Disadvantages of Hashing

Hash collisions are practically unavoidable when hashing a random subset of a large set.

- 2) not effective when number of entries are very small
- 3) take constant time on average,