

- **Unit Vectors:** Those vectors whose magnitude is equals to 1 are called unit vectors.

• **Norm:** Norm is a function from the real or complex vector space to a non-negative real number which can be used in many ways such as distance from the origin.

- **Hermitian:** The sum of a square matrix  $A$  and its conjugate transpose is called Hermitian.

- **Skew-Hermitian:** The difference between a square matrix  $A$  and its conjugate transpose is called skew Hermitian.

- **Unitary matrix:** Unitary matrix are the matrix whose inverse equals to its conjugate transpose. The unitary matrix is the complex analogue of real orthogonal matrices.



• **Fourier Series:** separates a periodic function  $f(x)$  in a combination of all of its basis functions  $\sin(nx)$  and  $\cos(nx)$ .

• **Similar Matrices:** If  $A$  and  $B$  are two matrices then we say that  $B$  is similar to  $A$  if there is an invertible matrix  $P$  such that:-

$$B = P^{-1}AP.$$

• **Subspace:** A subset  $W$  of a vector space  $V$  is called subspace of  $V$ , if  $W$  is itself under the addition and scalar multiplication in  $V$ .

• **Orthogonal matrices:** Two matrices are said to be orthogonal if they are perpendicular. i.e.: their dot product is zero.

• **Equal matrix:** Two matrices are said to be equal if they have same dimensions or order and their corresponding elements are identical.



• **Row Space**:- If  $A$  is a  $m \times n$  matrix then, the subspace of  $\mathbb{R}^n$  spanned by its row vectors are called the row space.

• **Column Space**:- If  $A$  is a  $m \times n$  matrix, then the subspace of  $\mathbb{R}^n$  spanned by its column vectors are called the column space.

• **Null Space**:- The solution of homogeneous system of equations  $Ax=0$ , ~~span where~~ which is the subspace is spanned by of  $\mathbb{R}^n$  is called the null space.

• **Linear Combination**:- If  $w$  is a vector in vector space  $V$  then  $w$  is called the linear combinations of vectors  $\{v_1, v_2, v_3, \dots, v_n\}$  in  $V$ , if  $w$  can be represented in form :-  
$$w = k_1 v_1 + k_2 v_2 + k_3 v_3 + \dots + k_n v_n$$
where  $\{k_1, k_2, k_3, \dots, k_n\}$  are the scalars.

• **Linear Independence**:- Let  $S = \{v_1, v_2, v_3, \dots, v_n\}$  is the set of two or more vectors in vector space  $V$  then they are <sup>no</sup> vector in called linear Independence set if  $\uparrow S$  cannot be expressed as linear combination of others.

• **Linear dependent**:- The set that can be expressed as linear combination of others and not linear independent is called linear dependent set.

• **Cross product**:- The cross product or inner or scalar product of two matrices  $u$  and  $v$  is given and denoted as-

$$UV = U_1 V_1 + U_2 V_2 + U_3 V_3 + \dots + U_n V_n$$

and also:-

$$U \cdot V = |U||V|\cos\theta$$

• **Magnitude**:- If  $V = \{v_1, v_2, v_3, \dots, v_n\}$  is a vector in  $R^n$  then the magnitude of  $V$  denoted as  $\|V\|$  and defined as:-

$$\|V\| = \sqrt{v_1^2 + v_2^2 + v_3^2 + \dots + v_n^2}$$



• **Rank:-** The common dimensions of row space and column space of matrix  $A$  is called its rank. And is denoted by  $\text{rank}(A)$ .

• **Nullity:-** The dimensions of the null space of a matrix  $A$  is called its nullity.

• D/f b/w Echelon and reduced Echelon?

Echelon	Reduced Echelon
• The solution of the row echelon is not unique	• The solutions of the reduced row echelon is unique.

• Infinite solutions.	• Only one solution
• Contains non-zero element at upper right corner only.	• Every column contains one and zero only.

• **Orthogonal Basis:-** The row of an orthogonal matrix are its orthogonal basis.

If the length of row is 1 then they are mutually perpendicular.

Similarly, the column of an orthogonal matrix are its orthogonal basis.

• **Basis:-** If  $S = \{v_1, v_2, v_3, \dots, v_n\}$  is a vector in finite-dimensional vector space  $V$  then  $S$



• **Dimensions:** The dimension of a finite-dimensional vector space denotes as  $\dim(V)$  and defined to be the number of vectors in Basis of  $V$ .

• **Eigen Value:**  $Ax = \lambda x$  for some scalar  $\lambda$ .  
The scalar  $\lambda$  is called the eigen value.

Eigen value = Characteristic value.

• **Eigen Vector:** If  $A$  is an  $m \times n$  matrix then the non-zero vector  $x$  in  $\mathbb{R}^n$  are called its eigen vector.

In eq.  $Ax = \lambda x$ ,  $x$  is called corresponding eigen vector.

Eigen vector = Characteristics vector.

• **Positive definite:** A positive definite matrix is a symmetric matrix with all possible eigenvalues.

• **Complex matrices:** Matrices whose values are real ~~as~~ ~~well~~ or complex are called complex matrices.

• **Characteristic Equation:** The equation which we solve to get the / find the matrix's eigen values.

$$|\lambda I - A| = 0$$



• L-U Factorization / Decomposition:- The factorization of a square matrix  $A$  as

$$A = LU$$

where  $L$  is the lower triangle and  $U$  is the upper triangle is called L-U factorization.

• Standard Basis:-

• Argumented Matrix:-