University of Sargodha

BS 3rd Semester/Term Exam 2021 Subject: Information Technology Time Allowed: 02:30 Hours Paper: Linear Algebra (MATH-203) Note: Objective part is compulsory. Attempt any three questions from subjective part. Maximum Marks: 80

Objective Part

Write short answers of the following in 2-3 lines each on your answer sheet. i.

For what value of K the vectors (1,-2,K) in \mathbb{R}^3 be a linear combination of vectors (3,0,-2) and ii.

Let $S = \{u = (1,2,1), v = (2,9,0), w = (3,3,4)\}$ form bases for R^3 . Find the vector v in R^3 whose iii. iv. ν.

Use Wronskian to show that $f_1 = 1$, $f_2 = e^x$ and $f_3 = e^{2x}$ are linearly independent. vi.

If A is invertible matrix and n is nonnegative integer, then show that $(A^n)^{-1} = (A^{-1})^n$. Define Null space.

vii.

Show that matrix P is orthogonal if and only if P^T is orthogonal. viii. ix.

State Calay's Hamilton theorem.

Show that matrix $A = \begin{bmatrix} 1 & 2 \\ 3 & -4 \end{bmatrix}$ is zero of $g(x) = x^2 + 3x - 10$. xi.

If A is symmetric then show that $(A^{-1})^T = (A^T)^{-1}$. xii.

Normalize the vector v = (1,2,4,5). xiii.

Consider the vector u = (1, -5, 3) and find $||u||_{\infty}$, $||u||_{1}$, $||u||_{2}$. xiv.

Show that set of all symmetric matrices is subspace of vector space of all $n \times n$ matrices.

 $\begin{bmatrix} -1 \\ b \end{bmatrix}$, & $A^2 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ find a & b.

xvi. Write the basis and dimension of vector space V of all $M_{2\times 2}$ matrices.

a) Find Eigen values and bases for Eigen spaces of $A = \begin{bmatrix} -2 & -1 \\ 5 & 2 \end{bmatrix}$. Q.2.

b) Determine whether the vectors in R^4 are linear independent or linear dependent

a) Determine whether the vector v = (3,3,-4) is a linear combination of Q.3. (1,2,3), y = (2,3,7), z = (3,5,6).

(1,2,3),
$$y = (2,3)$$

b) Find the inverse of matrix $A = \begin{bmatrix} 1 & 1 & 1 \\ 0 & 1 & 2 \\ 1 & 2 & 4 \end{bmatrix}$

a) Solve the system by Gauss elimination method Q.4.

$$3x_1 + x_2 - x_3 = -4$$

$$x_1 + x_2 - 2x_3 = -4$$

$$-x_1 + 2x_2 - x_3 = 1$$
linearly in $\frac{1}{2}$

b) Show that the set $\{1,i\}$ in \mathbb{C} is linearly independent over \mathbb{R} but linearly dependent over \mathbb{C} .

b) Show that the set $v = \mathbb{R}^n$ with standard addition and scalar multiplication defined as $v = \mathbb{R}^n$ where $v = \mathbb{R}^n$. Check whether the set $v = \mathbb{R}^n$ over $v = \mathbb{R}^n$ for $v = \mathbb{R}^n$. a) Consider the set $v = \mathbb{R}$. Check whether the set V over F forms a vector space or not? Q.5.

b) Compute the determinant of 2 7 0 6 0 6 3 0 7 3 1 -5

a) Apply the Gram Schmidt process to transform the basis vectors $u_1 = (1,1,1), u_2 = (0,1,1)$ and (0,0,1) into an orthogonal basis and then normalize the orthogonal basis vectors to the orthogonal basis and the orthogonal basis vectors to the orthog a) Apply the Gram Schmidt process to transform the vectors $u_1 = (1,1,1), u_2 = (0,1,1)$ are $u_3 = (0,0,1)$ into an orthogonal basis and then normalize the orthogonal basis vectors to obtain Q 6.

b) Show that the matrix 0 1 2 cannot be diagonalized. Visit tShahab.com for more.