

General Procedure For Testing hypothesis  
About  $\mu$  or Mean.  $\sigma$  (known):-

(i) Formulation of Hypothesis:

null hyp  $H_0: \mu = \mu_0$  general notation  
alternative hyp  $H_1: \mu \neq \mu_0$ .

(ii) Level of Significance:

$$\alpha = 0.05 \text{ or } 5\%$$

(iii) Test Statistic:

$$Z = \frac{\bar{X} - \mu_0}{\sigma / \sqrt{n}}$$

(iii) Test Statistic:

$$Z = \frac{\bar{x} - \mu_0}{s / \sqrt{n}}$$

(iv) Critical Region:

Reject  $H_0$  if  
 $Z_{(cal)} \geq 1 > Z/2$

(v) Calculation:

(vi) Conclusion:

Example:

10 devices cell is taken voltage test gives the following result 1.52, 1.53, 1.49, 1.48, 1.47, 1.49, 1.51, 1.50, 1.45, 1.46. The mean voltage of the cells when store volts 1.51 volts. Assuming the S.D to remain unchanged at 0.02V is there reason to believe that the cell has deteriorated are  $\alpha = 0.05$ .

(1) Formation of hypothesis:-

Null hypothesis:-

$$H_0: \mu = 1.51$$

Alternative hypothesis:

$$H_1: \mu \neq 1.51$$



$$H_0: \mu = 1.51$$

Alternative hypothesis:

$$H_1: \mu \neq 1.51$$

(2) level of significance:

$$\alpha = 0.05$$

(3) Test Statistic:

$$Z = \frac{\bar{X} - \mu_0}{\sigma / \sqrt{n}}$$

(4) Critical region:

Reject  $H_0$  if

$$|Z_{\text{cal}}| \geq Z_{\alpha/2}$$

$$|Z_{\text{cal}}| \geq Z_{(0.05/2)}$$

$$|z_{\text{calc}}| \geq z_{0.0025}$$

$$|z_{\text{calc}}| \geq 1.96$$

(5) Calculation:

$$n = 10, \quad \sigma = 0.02, \quad \mu_0 = 1.51$$

$$\bar{x} = ?$$

$$\bar{x} = \frac{\sum x_i}{n}$$

$$\bar{x} = 1.49$$

$$z = \frac{1.49 - 1.51}{0.02 / \sqrt{10}}$$

$$z = -3.162.$$

$$Z_{\alpha} = \frac{0.02}{\sqrt{10}} = -3.162.$$

### (6) Conclusion:

From the provided evidence  
 $3.162 \geq 1.96$  So we  
 reject  $H_0$  and concluded that  
 result are significant.

### Example:

A home heating oil delivery  
 Company would like to estimate the  
 annual usage for its customers who  
 lives in single family home. A  
 sample 100 customers indicated an  
 average annual usage of 1103 gallons  
 on a sample S.D of 327.8 gallons  
 At the 100% level of significant  
 is the evidence that the annual



Usage exceeds 1000 gallons Per year?

(1) Formation of Hypothesis:

Null :  $H_0 : \mu \leq 1000$

Alternative :  $H_1 : \mu > 1000$ .

(2) Level of Significance:

$$\alpha = 0.01$$

(3) Test Statistic:

$$Z = \frac{\bar{X} - \mu}{S.D / \sqrt{n}}$$

$$s.d / \sqrt{n}$$

nce

(4) Critical region:

Reject  $H_0$  if

$$Z_{(cal)} \geq Z_{\alpha}$$

$$Z_{(cal)} \geq Z_{0.01}$$

$$Z_{(cal)} \geq 2.326$$

(5) Calculation:

$$n = 100, \bar{x} = 1103, s = 327.8$$

$$Z = \frac{1103 - 1000}{327.8 / \sqrt{100}}$$

$$Z = 3.14$$

(6) Conclusion:



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From the provided evidence.

$3.14 > 2.326$  so we  
reject  $H_0$  and concluded that results  
are significant.

# One Sample z test for testing mean

$\sigma$  known

$$Z = \frac{\bar{X} - \mu_0}{\sigma / \sqrt{n}}$$

$\sigma$  known  $n > 30$

$$Z = \frac{\bar{X} - \mu_0}{\sigma / \sqrt{n}}$$

## One Sample t-test for testing mean

$\sigma$  - known

$$t = \frac{\bar{X} - \mu_0}{s / \sqrt{n}} \text{ with } (n-1) \text{ d.f.}$$

## Formulas for Small & Capital "S"

$$S = \sqrt{\frac{\sum x^2}{n} - \left(\frac{\sum x}{n}\right)^2}$$

$$S = \sqrt{\frac{1}{n-1} \left( \sum x^2 - \left(\frac{\sum x}{n}\right)^2 \right)}$$

$$s = \sqrt{\frac{1}{n-1} (\sum x^2 - \frac{(\sum x)^2}{n})}$$

Q: General Procedure for testing mean when  $\sigma$  is unknown.

(1) Formation of hypothesis:

Null hypothesis  $H_0: \mu = \mu_0$

Alternative hypothesis  $H_1: \mu \neq \mu_0$

Level of Significance:

$$\alpha = 0.05$$



Test Statistic:

$$t = \frac{\bar{x} - \mu_0}{s/\sqrt{n}} \text{ with } v = n-1 \text{ df}$$

Critical region:

$$|t_{\text{calc}}| \geq t_{\alpha/2}(v) \Rightarrow (\text{new})$$

Calculation:

Conclusion:

One tail test

$$H_0: \mu \geq \mu_0$$

$$H_1: \mu \leq \mu_0$$

$$t_{\text{calc}} \leq t_{\alpha}(v)$$

## : Exercise:

Q:1

(1) Formation of hypothesis:-

Null hypothesis:  $H_0: \mu = 67.39$

Alternate hypothesis:  $H_1: \mu > 67.39$

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(2) Level of Significance:

$$\alpha = 0.05$$

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(3) Test Statistics:-

$$Z = \frac{\bar{X} - \mu_0}{S / \sqrt{n}}$$

v)

(4) Critical region:-

Reg  $H_0$  if

$$|Z_{cal}| \geq Z_{0.05}$$

$$|Z_{cal}| \geq 1.645$$

$$|Z_{\text{cal}}| \geq Z_{\alpha/2}$$

$$|Z_{\text{cal}}| \geq 1.645$$

(5) Calculation:

Data:

$$\mu_0 = 67.39, \quad \sigma = 1.30$$

$$n = 400, \quad \bar{x} = 67.47$$

$$Z = \frac{67.47 - 67.39}{1.30 / \sqrt{400}}$$

$$Z = 1.23$$



From provided evidence  $1.645 > 1.28$   
So we <sup>don't reject</sup> accept  $H_0$  and results are insignificant.

Q: 2 A sample of 100 observation from a population with  $\sigma = 2$  inches has  $\bar{x} = 66.5$  inches. Test the null hypothesis  $H_0: \mu = 67$  against the alternative hypothesis  $H_1: \mu \neq 67$  use 1% level of hypc.

Formation of hypothesis:

Null Hypothesis:  $H_0: \mu = 67$

Alternate hypothesis:  $H_1: \mu \neq 67$

Null Hypothesis:  $H_0 : \mu = 67$   
Alternate hypothesis:  $H_1 : \mu \neq 67$

(2) Level of Significance:

$$\alpha = 0.01$$

(3) Test Statistics:-

$$Z = \frac{\bar{X} - \mu_0}{\sigma / \sqrt{n}}$$

(4) Critical region:

Reject  $H_0$  if

$$|Z_{\text{cal}}| \geq Z_{0.01}$$

$$|Z_{\text{cal}}| \geq 2.575$$

Q:3 A Sample of 900 plants is found to have a mean of 34 cm. Can it is reasonable regarded as a random sample from a large population with mean 32 cm and Standard deviation 23 cm. Use 5% level of Significance.

Formation of hypothesis:

Null hypothesis:  $H_0 : \mu = 32$

Alternative hypothesis:  $H_1 : \mu \neq 32$ .

(2) Level of Significance:

$$\alpha = 0.05$$

(3) Test Statistics:

$$Z = \frac{\bar{X} - \mu_0}{S.D / \sqrt{n}}$$

$$S.D / \sqrt{n}$$



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(4) Critical region:

Reject  $H_0$  if:

$$|z_{\text{calc}}| \geq z_{0.05}$$

$$|z_{\text{calc}}| \geq 1.645.$$

(i) Calculation:

Data:

$$n = 900, \bar{x} = 34, s.D = 23$$

$$z = \frac{34 - 32}{23 / \sqrt{900}}$$

$$z = 2.61$$

## CHAPTER # 17

(10) outline:

Testing hypothesis about variance of a normal population:

(1) Formation of hypothesis:

$$H_0 : \sigma^2 = \sigma_0^2 \quad \text{and} \quad H_1 : \sigma^2 \neq \sigma_0^2$$

$$H_0 : \sigma^2 \leq \sigma_0^2 \quad \text{and} \quad H_1 : \sigma^2 > \sigma_0^2$$

$$H_0 : \sigma^2 \geq \sigma_0^2 \quad \text{and} \quad H_1 : \sigma^2 \leq \sigma_0^2$$

(2) Level of Significance:

$$\alpha = 5\%, 2\%, 1\%$$

(3) Test Statistic

$$\chi^2 = n s^2$$

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Calculation:  
Conclusion:

$$S^2 = \frac{\sum x^2}{n} - \left( \frac{\sum x}{n} \right)^2$$

$$S = \sqrt{\frac{\sum x^2}{n} - \left( \frac{\sum x}{n} \right)^2}$$



Q:1 A sample of 25 observation has  $S^2 = 12.6$  would you accept or reject at the 5% level of significance the hypothesis that  $\sigma^2 = 20$ .

Null hypothesis:  $H_0 : \sigma^2 = 20$

Alternative hypothesis:  $H_1 : \sigma^2 \neq 20$

level of significant

$$\alpha = 0.05$$

Test Statistic:

$$\chi^2 = \frac{n S^2}{\sigma_0^2}$$

$$v = (n-1) df$$

$$v = (n-1)df$$

Critical region:

$$\chi^2 \leq \chi^2_{1 - \frac{\alpha}{2}(n-1)}, \quad \chi^2 \leq \chi^2_{1 - \frac{0.05}{2}(24)}$$

$$\chi^2 \geq \chi^2_{\frac{\alpha}{2}(n-1)}, \quad \chi^2 \geq \chi^2_{\frac{0.05}{2}(24)}$$

Calculation:

$$\chi^2 = \frac{ns^2}{\sigma_0^2}$$

Since  $n = 25$ ,  $s^2 = 12.6$ ,  $\sigma^2 = 20$

$$\chi^2 = \frac{25(12.6)}{20} = \frac{316}{20} = 15.8$$

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Conclusion:

From the provided evidence  
 $15.8 \neq 12.40$  so, we don't reject  
 $H_0$  and concluded that the results are  
insignificant.

Q:2 A sample of 9 parts produced



$$\alpha = 5\%, 2\%, 1\%$$

### (3) Test Statistic

$$\chi^2 = \frac{n s^2}{\sigma_0^2}$$

$$\chi^2 = \frac{\sum (x - \bar{x})^2}{\sigma_0^2}$$

with  $v = (n-1)df$

### (4) Critical region:

Reject  $H_0$  if

$$(i) \chi^2_{(cal)} \leq \chi^2_{1 - \frac{\alpha}{2}, (n-1)} \text{ and } \chi^2_{(cal)} \geq \chi^2_{\frac{\alpha}{2}, (n-1)}$$

$$(ii) \chi^2_{(cal)} \geq \chi^2_{\alpha, (n-1)}$$

$$(iii) \chi^2_{(cal)} \leq \chi^2_{1-\alpha, (n-1)}$$

$$|z_{\alpha/2}| \geq 1.645.$$

e) Calculation:

Data:

$$n = 900, \bar{x} = 34, s.D = 23$$

$$z = \frac{34 - 32}{23 / \sqrt{900}}$$

$$z = 2.61$$

Conclusion:

From Provided evidence

$2.61 \geq 1.645$ , So we reject  $H_0$ ,  
and the result are significant.

Calculation:

Data:  $b = 2$  ,  $\bar{X} = 66.5$   
 $n = 100$  ,  $\mu = 67$

$$Z = \frac{66.5 - 67}{2 / \sqrt{100}}$$

$$Z = -2.5$$

Conclusion:

From providing evidence  
 $2.5 \neq 2.575$  don't reject  $H_0$  and the  
 result are insignificant.

Q:3 A sample of 900 plants is found to