

# **IMPORTANT CONCEPTS Part-I**

**1. The word Statistics :** is used in three meanings:-

- i) The aggregate of numerical facts in any field of enquiry. Word 'data' is meant in this sense.
- ii) The Science of systematic collection, presentation, analysis and interpretation of data. In other words the "subject of statistics" is meant by it.
- iii) It is used as the plural of the word 'Statistic' a term used to define any value extracted from the sample, a part of the population.

**2. Primary data :** are the most original data which are collected for the first time and have not undergone any statistical treatment.

**3. Secondary data :** are the data which have undergone at least once any statistical treatment.

**4. Grouped data :** are data arranged form in classes or groups along with their corresponding frequencies.

**5. Variable :** is any quantitative characteristic which varies from one individual or object to another.

**6. Constant :** is any value which does not change but remains fixed.

**7. Discrete Variable :** is a variable which takes countable or countably infinite number of values.

**8. An Array :** is an arrangement of data in ascending or descending order.

**9. Classification :** is the process of arranging data in classes according to their similarities.

**10. Tabulation :** is the process of arranging data in rows and columns.

**11. Freq. Distribution :** is the tabular arrangement of data in to groups according to size or magnitude.

**12. Class Limits :** are the values defining the classes or groups the smaller value is called lower class limit and the greater one is called upper class limit.

**13. Class-boundaries (C.Bs) :** are precise or true class limits. These values separate the class limits. The smaller value is called lower class boundary and the greater one is called upper class boundary.

**14. Class mark/Mid point/Middle Value :** is the mean of lower and upper class limits or boundaries.

**15. Size of Class Interval :** is the difference between the upper and lower class boundaries of a class.

16. **Frequency** : is the no. of individuals or objects in a class.
17. **Cummulative freq.** : is the total frequency of all less then the upper C.B. of a given class.
18. **Simple Bar Diagram** : is a chart consisting of vertical or horizontal bars of equal width with heights equal to the corresponding frequencies.
19. **Multiple Bar Diagram** : is a grouped bar diagram used to the represent two or more sets of inter-related data.
20. **Pie Chart** : is the sub-division of a circle into sectors whose areas are proportional to the different angles of the total area of a circle i.e.  $360^{\circ}$ .
21. **Historigram** : is the graphic representation of a time-series.
22. **Histogram** : is the graphic representation of freq. dist. by a set of adjacent rectangles in which area of each rectangle is proportional to the corresponding class frequencies.
23. **Frequency Polygon** : (A closed shape with many corners) is the graphic form of a frrequency dist. obtained by joining the mid-points of the types of each rectangle of the histogram and the end points are joined to the mid-points of arbitrary classes taken at the start and at the end on x-axis.
24. **Cummulative frequency curve or ogive** : is a graphic representation obtained by plotting cummulative frequencies against the upper C.B. and by joining the points smoothly.
25. **Average** : is a balancing point of a set of data or it is a central value representing the entire data.
26. **Measures of Central Tendency or Measures of Location** : are measures which tend to lie in centre or measures used to locate the centre of the data.
27. **Arithmatic Mean (A.M.)** : is a value obtained by dividing the sum of all the values by their total number.
28. **G.M.** : is the  $\eta$ th positive root of the product of non-zero and non-negative values.
29. **H.M.** : is the reciprocal of the A.M.. of reciprocals of the non-zero values.
30. **Mode** : is a value which occurs most of the times the data.
31. **Median** : is the most middle value of the data.
32. **When an average should be used :**
- A.M. should be used when data are relatively homogeneous.

**G.M.** should be used when data are ratios of change.

**H.M.** should be used when data are rates of change.

**Mode** should be used when data have a predominated figure.

**Median** should be used when data are heterogeneous.

**33. Quartiles** : are the values that divide the data into four equal parts.

**34. Deciles** : are the values that divide the data into ten equal parts.

**35. Percentiles** : are the values that divide the data into hundred equal parts.

**36. Dispersion** : is the scatterness of values about some central value of the data.

**37. Measure of dispersion** : is a value that measures the dispersion or scatterness of data about some central value.

**38. Absolute measure of dispersion** : is measure of dispersion expressed in the same units as of the data.

**39. Relative measure of dispersion** : is measure of dispersion expressed in the form of co-efficient and is unitless.

**40. Range** : is the difference between maximum and minimum values of the data.

**41. Mean Deviation** : is the mean of the absolute deviations from any measure of central tendency.

**42. Variance** : is the mean of squared deviations of values from their arithmetic mean.

**43. Co-efficient of variation (C.V.)** : is the percentage of S.D. with respect to mean.

**44. Co-efficient of S.D.** : is the ratio of S.D to mean.

**45. Moments** : are the means of  $r^{\text{th}}$  powered-deviations.

**46. Skewness** : is the lack of symmetry.

**47. Kurtosis** : is the peakedness or flatness of the uni modal curve.

**48. Index Nos.** : are the economic barometers to know relative change in a variable or a group of related variables with respect to time or space.

**49. Simple I/No.** : is a number that measures relative change in a single variable with respect to time or space.

50. **Composite I/No.** : is a number that measures a relative change in a group of related variables with respect to time or space.

51. The main steps used in the construction of I/No. are : (I) Purpose & Scope (ii) Selection of Commodities (iii) Collection of prices (iv) Selection of base period (v) Choice of average (vi) Selection of appropriate weights.

52. **Fixed base method** : is a method in which a particular economically stable year or average of some years is taken as base.

53. **Chain base Method** : is a method in which a particular year is not fixed but goes on changing with the given year i.e. the relatives are computed with the immediately preceding year as a base.

54.  $\eta$  Factorial : is product of first n natural numbers.

55. **Permutation** : is an arrangement of all or some of a set of objects in a definite order.

56. **Combination** : is an arrangement of objects without regard to their order.

57. **Experiment** : is any process of obtaining an observation.

58. **Random Experiment** : is an experiment which produces different outcomes even though it is repeated under the similar conditions.

59. **Trial** : is the single performance of an experiment.

60. **Outcomes** : are the results obtained from an experiment.

61. **Sample Space** : is a complete list of all possible outcomes obtained from random experiment.

62. **Sample Points** : are the elements of a sample Space.

63. **Event** : is a subset of a Sample Space.

64. **Simple Event** : is the event that consists of only one sample point of the Sample Space.

65. **Composite Event** : is the event that consists of more than one sample point of the Sample Space.

66. **Equally likely events** : are the events that have the same no. of sample points of the sample space.

67. **Mutually Exclusive Events** : are the events that have no common sample points of the sample space.

68. **Independent Event** : are those events which do not effect each other with respect to their occurrence.

69. **Dependent Event** : are those events which effect each other with respect to their occurrence.

70. **Exhaustive Events** : are the disjoint events that constitute the entire sample space.

71. **The Classical OR "a priori" definition of probability** : "If a random experiment can be performed in 'n' mutually exclusive, equally likely, exhaustive number of sample points and "m" of these are favourable to the occurrence of a certain event A, then the probability of the occurrence of the event A ( $P(A)$ ) is the ratio  $m/n$ . i.e.  $P(A) = m/n$

72. **Relative frequency OR "a posteriori" OR Statistical OR empirical definition of probability** : If a random experiment is repeated a large number of times, say, 'n' under the similar condition, if an event A is observed to occur 'm' times, then the probability of occurrence of event A  $P(A)$  is defined as the limit of the relative frequency  $m/n$  as tends to infinity. i.e.  $P(A) = \lim_{n \rightarrow \infty} \frac{m}{n}$

73. **Axiomatic definition of probability** : Let the Sample Space S has the Sample Points  $E_1, E_2, E_3, \dots, E_i, \dots, E_n$ . Each Sample point is assigned a real number  $P(E_1), P(E_2), P(E_3), \dots, P(E_i), P(E_n)$  which are called the probabilities of the points. The probability of any point denoted by  $P(E_i)$  must obey the following the axioms.

i)  $0 < P(E_i) < 1$

: ( $i = 1, 2, 3, \dots, n$ )

ii)  $P(S) = 1$

iii) For the mutually exclusive events  $E_1$  and  $E_2$ ,  $P(E_1 \cup E_2) = P(E_1) + P(E_2)$

74. **Random Numbers** : are the nos. obtained by some random process (manual or mechanical) from a discrete uniform distribution of basic numbers 0, 1, 2, 3, 4, 5, 6, 7, 8, 9.

75. **Random Variable (r.v.)** : is the set of numerical values obtained from the outcomes of a random experiment.

76. **Discrete r.v.** : are the variables that can assume finite or countably infinite values in a sample space.

77. **Continuous r.v.** : are the variables that can assume value in an interval  $[a, b]$ , where  $a < b$ .

78. **Probability Distribution OR Probability function** : is an arrangement of values of r.v. along with their corresponding probabilities in the form of pairs, table, graph or formula.

79. **Discrete Probability Distribution is defined as** : If  $X$  is a discrete r.v. assuming the values  $x_1, x_2, x_3, \dots, x_i, \dots, x_n$ , with their corresponding probabilities  $P(X = x_i) = f(x_i) = P(x_i)$   $i = 1, 2, 3, \dots, n$  is called discrete probability distribution.

80. **Continuous probability distribution function (p.d.f) is defined as** : If  $X$  is a continuous r.v.

defined in an interval  $[a, b]$  then the p.d.f of  $X$  is defined as  $P(a \leq x \leq b) = \int_a^b f(x) dx$

81. **Binomial Experiment:** if in an experiment  
 i) Each trial results either in success or failure.  
 ii) The trials are independent.  
 iii) The probability of success remains constant from trial to trial, and  
 iv) The experiment is repeated a fixed number of times.
82. **Binomial probability distribution:** if  $p$  is the probability of success of an event in a single trial then the probability of exactly  $x$  success in ' $n$ ' independent trials of a 'Binomial Experiment' is given by

$$f(x) = \binom{n}{x} p^x q^{n-x} \quad \text{for } x = 0, 1, 2, \dots, n$$

83. **Binomial random variable:** is a random variable  $X$  that follows binomial probability distribution.
84. **Binomial Frequency distribution:** if  $N$ , the number of sets or experiments multiplies basic binomial probability function, the result is Binomial Frequency distribution.
85. **Hypergeometric Experiment:** if in an experiment  
 i) Each trial results either in success or failure.  
 ii) The successive trials are dependent.  
 iii) The probability of success changes from trial to trial, and  
 iv) The experiment is repeated a fixed number of times.
86. **Hypergeometric probability distribution:**  
 If ' $N$ ' is number of elements in a population, from which ' $K$ ' are success and a sample of size ' $n$ ' is selected from the population then the probability of ' $x$ ' successes at  $X=x$  given by

$$f(x) = \frac{\binom{k}{x} \binom{N-k}{n-x}}{\binom{N}{n}} \quad \begin{aligned} &\text{for } x = 0, 1, 2, \dots, n \\ &N \geq n \\ &K \geq x \\ &n \geq x \end{aligned}$$

87. **Hypergeometric random variable:** is a random ' $x$ ' that follows the hypergeometric probability distribution:

# IMPORTANT FORMULAE Part-I

## 1. MEASURES OF CENTRAL TENDENCY

### (a) Arithmatic Mean (Mean) ( $\bar{X}$ )

	<u>Ungrouped data</u>	<u>Grouped data</u>
Direct Method	$\bar{X} = \frac{\sum X}{n}$	$\bar{X} = \frac{\sum fX}{\sum f}$
Short cut Method	$\bar{X} = a + \frac{\sum D}{n}$	$\bar{X} = a + \frac{\sum fD}{\sum f}$
Coding Method	—	$\bar{X} = a + \frac{\sum fU}{\sum f} \times h$

Where 'a' an assumed value (Provisional Mean)

'D' Deviation of 'x' from the value 'a' i.e.  $D = x - a$

'h' Class Interval Size (Uniform)

$$U = \frac{X - a}{h} \quad \text{or} \quad U = \frac{D}{h}$$

Sum of deviations from the A.M. is always Zero i.e.  $\sum(X - \bar{X}) = 0$  and  $\sum f(X - \bar{X}) = 0$

### (b) Weighted Mean ( $\bar{X}_w$ )

Here use weights instead of frequencies,  $\bar{X}_w = \frac{\sum XW}{\sum W}$

### (c) Combined Mean ( $\bar{X}_c$ )

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If  $\bar{X}_1, \bar{X}_2, \dots, \bar{X}_k$ , are the Means of the numbers in each

$k$  - the group  $n_1, n_2, \dots, n_k$  then  $\bar{X}_c = \frac{\sum n_i \bar{X}_i}{\sum n_i}$

### (d) Geometric Mean (G.M.)

#### Ungrouped data

$$\text{G.M.} = (X_1 \times X_2 \times \dots \times X_n)^{\frac{1}{n}}$$

$$\text{G.M.} = \text{Antilog} \left[ \frac{\sum \log x}{n} \right]$$

#### Grouped data

$$\text{G.M.} = \text{Antilog} \left[ \frac{\sum f \log x}{\sum f} \right]$$

### (e) Harmonic Mean (H.M.)

$$\text{H.M.} = \frac{n}{\sum (\frac{1}{x})}$$

$$\text{H.M.} = \frac{\sum f}{\sum (\frac{f}{x})} \quad \text{or} \quad \text{H.M.} = \frac{\sum f}{\sum f(\frac{1}{x})}$$

### Relation between (AM, GM, and HM)

$$(i) \quad GM = \sqrt{(A.M.) (H.M.)}$$

$$(ii) \quad A.M. \geq G.M \geq H.M$$

### **(e) Median :**

Median = The value of  $\frac{n+1}{2}$ th item of (arranged data) (ungrouped data)

$$\text{Median} = L + \frac{h}{f} \left( \frac{N}{2} - c \right)$$

(Grouped data)

Where  $N = \sum f$ ,

$\frac{N}{2}$  = Median group (M.G.)

'L' = the lower boundary of the M.G.

'f' = the frequency of the M.G.

'c' = the preceding cumulative frequency of the M.G.

'h' = the class interval size of the M.G.

### Quartiles : (Q)

$$Q_i = \text{The value of } i \left( \frac{n+1}{4} \right) \text{ th item}$$

(Ungrouped data)

$$Q_i = L + \frac{h}{f} \left( \frac{iN}{4} - c \right)$$

(Grouped data)

Where  $i = 1, 2, 3$

### Deciles : (D)

$$D_j = \text{The value of } j \left( \frac{n+1}{10} \right) \text{ th item}$$

(Ungrouped data)

$$D_j = L + \frac{h}{f} \left( \frac{jN}{10} - c \right)$$

(Grouped data)

Where  $j = 1, 2, 3, \dots, 9$

### Percentiles : (P)

$$P_k = \text{The value of } k \left( \frac{n+1}{100} \right) \text{ th item}$$

(Ungrouped data)

$$P_k = L + \frac{h}{f} \left( \frac{KN}{100} - c \right)$$

(Grouped data)

Where  $K = 1, 2, 3, \dots, 99$

Note: Median =  $Q_2 = D_5 = P_{50}$  and  $D_1 = P_{10}$   $D_2 = P_{20}$  .....  $D_{10} = P_{100}$

Also  $Q_1 = P_{25}$  and  $Q_3 = P_{75}$

## Mode :

$$\text{Mode} = L + \frac{f_m - f_1}{(f_m - f_1) + (f_m - f_2)} \times h$$

$$\text{Mode} = x + \frac{f_2 - f_1}{(f_m - f_1) + (f_m - f_2)} \times \frac{h}{2}$$

Mode = 3 Median - 2 Mean (approximately) (Empirical Relation)

Where,

$f_m$  = the frequency of the Model Class or (group) (M.G.)

$f_1$  = the preceding frequency of the (M.G.)

$f_2$  = the proceeding frequency of the (M.G.)

$L$  = the lower boundary of the M.G.

$h$  = the class interval size of M.G

$x$  = the mid point of M.G.

If, Mean = Median = Mode, the Distribution will be symmetrical

If, Mean > Median > Mode, the Distribution will positively skewed

If, Mean < Median < Mode, the Distribution will negatively skewed

## (2) MEASURES OF DISPERSION

### (A) ABSOLUTE MEASURES OF DISPERSION :

#### (a) Range: (R)

$$R = X_m - X_o \quad \text{Where } X_m = \text{Maximum Value}, \quad X_o = \text{Minimum Value}$$

#### (b) Interquartile Range (I.Q.R.)

$$I.Q.R. = Q_3 - Q_1 \quad \text{Where } Q_3 = \text{Upper quartile}, \quad Q_1 = \text{Lower quartile}$$

#### (c) Semi-Interquartile Range (S.I.Q.R.) OR Quartile Deviation (Q.D.)

$$Q.D. = \frac{Q_3 - Q_1}{2}$$

#### (d) Mean Deviation (Average Deviation) (M.D.)

##### Ungrouped data

$$M.D. (\text{Mean}) = \frac{\sum |X - \bar{X}|}{n}$$

$$M.D. (\text{Median}) = \frac{\sum |X - \text{Median}|}{n}$$

$$M.D. (\text{Mode}) = \frac{\sum |X - \text{Mode}|}{n}$$

##### Grouped data

$$M.D. = \frac{\sum f|X - \bar{X}|}{\sum f}$$

$$M.D. = \frac{\sum f|X - \text{Median}|}{\sum f}$$

$$M.D. = \frac{\sum f|X - \text{Mode}|}{\sum f}$$

#### (e) Standard deviation (S) and variance ( $S^2$ )

##### Ungrouped data

$$\text{Direct Method} \quad S = \sqrt{\frac{\sum (X - \bar{X})^2}{n}}$$

$$\text{Indirect Method} \quad S = \sqrt{\frac{\sum X^2}{n} - \left(\frac{\sum X}{n}\right)^2}$$

$$\text{Shortcut Method} \quad S = \sqrt{\frac{\sum D^2}{n} - \left(\frac{\sum D}{n}\right)^2}$$

$$\text{Coding Method} \quad \text{_____}$$

##### Grouped data

$$S = \sqrt{\frac{\sum f(X - \bar{X})^2}{\sum f}}$$

$$S = \sqrt{\frac{\sum fX^2}{\sum f} - \left(\frac{\sum fX}{\sum f}\right)^2}$$

$$S = \sqrt{\frac{\sum fD^2}{\sum f} - \left(\frac{\sum fD}{\sum f}\right)^2}$$

$$S = \sqrt{\frac{\sum fU^2}{\sum f} - \left(\frac{\sum fU}{\sum f}\right)^2} \times h$$

### (B) RELATIVE MEASURES OF DISPERSION:

$$(i) \quad \text{Co-efficient of Dispersion} = \frac{X_m - X_o}{X_m + X_o}$$

$$(i) \quad \text{Co-efficient of Q.D.} = \frac{Q_3 - Q_1}{Q_3 + Q_1}$$

$$(iii) \quad \text{Mean Co-efficient of Dispersion} = \frac{\text{M.D.}}{\text{Mean}}$$

Median Co-efficient of Dispersion =  $\frac{\text{M.D.}}{\text{Median}}$

Mode Co-efficient of Dispersion =  $\frac{\text{M.D.}}{\text{Mode}}$

(iv) Co-efficient of S.D. =  $\frac{\text{S.D.}}{\text{Mean}}$

(v) Co-efficient of variation (C.V.) =  $\frac{\text{S.D.}}{\text{Mean}} \times 100$

### **(f) Combined Variance**

If  $n_1, n_2, \dots, n_k$ , are the Nos. of k-th groups having Means

$\bar{X}_1, \bar{X}_2, \dots, \bar{X}_k$ , and variances,  $S_1^2, S_2^2, \dots, S_k^2$  then Combined

$$\text{Mean } \bar{X}_c = \frac{n_1 \bar{X}_1 + n_2 \bar{X}_2 + \dots + n_k \bar{X}_k}{n_1 + n_2 + \dots + n_k} = \frac{\sum n_i \bar{X}_i}{\sum n_i}$$

and Combined Variance

$$S_{(\text{comb})}^2 = \frac{1}{n} \left[ \sum_{i=1}^k n_i \{ S_i^2 + (\bar{X}_i - \bar{X}_c)^2 \} \right] \quad n = \sum n_i$$

$$\text{Co-efficient of variation (comb)} = \frac{S_{(\text{comb})}}{\bar{X}_c} \times 100$$

### **(g) Corrected variance**

$$S_{(\text{corrected})}^2 = S^2 - \frac{h^2}{12}$$

$$\text{Co-efficient of variation (corrected)} = \frac{S_{(\text{corrected})}}{\bar{X}} \times 100$$

## **(C) PROPERTIES OF VARIANCE**

If a and b are any two constants, and x, y, be

Independent variables, then

$$(i) \text{Var}(a) = 0$$

$$(ii) \text{Var}(x \pm a) = \text{Var}(x)$$

$$(iii) \text{Var}(ax) = a^2 \text{var}(x)$$

$$(iv) \text{Var}(ax \pm b) = a^2 \text{var}(x)$$

$$(v) \text{Var}(x \pm y) = \text{Var}(x) + \text{Var}(y)$$

### (3) MOMENTS

#### i) Moments about Arithmetic Mean:

##### Ungrouped data

$$m_1 = \frac{\sum(X - \bar{X})}{n} = 0$$

$$m_2 = \frac{\sum(X - \bar{X})^2}{n} = S^2$$

$$m_3 = \frac{\sum(X - \bar{X})^3}{n}$$

$$m_4 = \frac{\sum(X - \bar{X})^4}{n}$$

##### Grouped data

$$m_1 = \frac{\sum f(X - \bar{X})}{\sum f} = 0$$

$$m_2 = \frac{\sum f(X - \bar{X})^2}{\sum f} = S^2$$

$$m_3 = \frac{\sum f(X - \bar{X})^3}{\sum f}$$

$$m_4 = \frac{\sum f(X - \bar{X})^4}{\sum f}$$

#### ii) Moments about origin ( $x=a$ ) P.M.

$$m'_1 = \frac{\sum(x - a)}{n} = \frac{\sum D}{n}$$

$$m'_2 = \frac{\sum D^2}{n}$$

$$m'_3 = \frac{\sum D^3}{n}$$

$$m'_4 = \frac{\sum D^4}{n}$$

$$m'_1 = \frac{\sum f(x - a)}{\sum f} = \frac{\sum fD}{\sum f}$$

$$m'_2 = \frac{\sum fD^2}{\sum f}$$

$$m'_3 = \frac{\sum fD^3}{\sum f}$$

$$m'_4 = \frac{\sum fD^4}{\sum f}$$

#### iii) Moments about Zero ( $x=0$ )

$$m'_1 = \frac{\sum X}{n} = \bar{X}$$

$$m'_2 = \frac{\sum X^2}{n}$$

$$m'_3 = \frac{\sum X^3}{n}$$

$$m'_4 = \frac{\sum X^4}{n}$$

$$m'_1 = \frac{\sum fX}{\sum f} = \bar{X}$$

$$m'_2 = \frac{\sum fX^2}{\sum f}$$

$$m'_3 = \frac{\sum fX^3}{\sum f}$$

$$m'_4 = \frac{\sum fX^4}{\sum f}$$

#### iv) Moments about Coding Method : $U = \frac{(x - a)}{h}$

$$m'_1 = \frac{\sum fU}{\sum f} \times h$$

$$m'_3 = \frac{\sum fU^3}{\sum f} \times h^3$$

$$m'_2 = \frac{\sum fU^2}{\sum f} \times h^2$$

$$m'_4 = \frac{\sum fU^4}{\sum f} \times h^4$$

Grouped data

#### v) Moments about A.M. in terms of P.M.

$$m_1 = 0$$

$$m_3 = m'_3 - 3m'_1m'_2 + 2(m'_1)^3$$

$$m_2 = m'_2 - (m'_1)^2 \rightarrow \text{variance}$$

$$m_4 = m'_4 - 4m'_1m'_3 + 6m'_1m'_2 - 3(m'_1)^4$$

### **vi) Moment Ratios : $\beta_1$ , $\beta_2$ or $b_1$ , $b_2$**

$$\beta_1 = b_1 = \frac{(m_3)^2}{(m_2)^3} \quad \beta_2 = b_2 = \frac{m_4}{(m_2)^2}$$

If  $\beta_1 = 0$ , the distribution will be symmetrical  
otherwise positively or negatively skewed

If  $\beta_2 = 3$ , the distribution will be Normal (Mesokurtic)

If  $\beta_2 > 3$ , the distribution will be Leptokurtic

If  $\beta_2 < 3$ , the distribution will be Platykurtic

### **vii) Co-efficient of skewness : (Sk)**

Karl Pearson Co-efficient of Skewness

$$Sk = \frac{\text{Mean} - \text{Mode}}{\text{S.D.}} \quad \text{and} \quad Sk = \frac{3(\text{Mean} - \text{Median})}{\text{S.D.}}$$

Bowleys (Quartiles) Co-efficient of Skewness

$$Sk = \frac{Q_3 + Q_1 - 2 \text{ Median}}{Q_3 - Q_1}$$

If  $Sk = 0$ , the distribution will be symmetrical

If  $Sk$  or  $\sqrt{\beta_1} > 0$ , the distribution will be Positively Skewed

If  $Sk$  or  $\sqrt{\beta_1} < 0$ , the distribution will be Negatively Skewed

### **viii) Sheppard's Correction : (Corrected moments)**

$$\bar{m}_2 = m_2 - \frac{h^2}{12} \quad (\text{Corrected Variance})$$

$$\bar{m}_4 = m_4 - \frac{h^2}{2} m_2 + \frac{7}{240} \times h^4$$

### **ix) Relationship between different Measures of dispersion**

$$Q.D. = \frac{2}{3} (\text{S.D.}) \quad \text{app.}$$

$$M.D. = \frac{4}{5} (\text{S.D.}) \quad \text{app.}$$

$$Q.D. = \frac{5}{6} (\text{S.D.}) \quad \text{app.}$$

## (4) INDEX NUMBER

$$\text{Price Relative } P_{on} = \frac{P_n}{P_o} \times 100$$

$$\text{Link Relative } P(n-1, n) = \frac{P_n}{P_{n-1}} \times 100$$

Where  $P_n$  = Price for the current (given) year

$P_o$  = Price for the base year.

$q_n$  = Quantity for the current (given) year

$q_o$  = Quantity for the base year

### a) Unweighted Index Numbers : (Two Methods)

i) Simple aggregate Method,  $P_{on} = \frac{\sum P_n}{\sum P_o} \times 100$

ii) Simple average of Relative Method

$$P_{on} = \frac{1}{k} \sum \left[ \left( \frac{P_n}{P_o} \right) \times 100 \right] \quad (\text{A.M. as average})$$

$$P_{on} = \left[ \prod \left( \frac{P_n}{P_o} \right) \right]^{\frac{1}{k}} \times 100 \quad (\text{G.M. as average})$$

Where  $\prod$  = product sign

K = No. of Commodities

Median as usual, the middle most relative for each year is taken as Median

### a) Weighted Index Numbers : (Two Methods)

i) Weighted aggregative Index

ii) Weighted average of Relative Index

#### i) Weighted aggregate Price Index Numbers :

Computed by the formulae

$$\text{Laspeyre's Index } P_{on} = \frac{\sum P_n q_o}{\sum P_o q_o} \times 100$$

$$\text{Paasche's Index } P_{on} = \frac{\sum P_n q_n}{\sum P_o q_n} \times 100$$

$$\text{Fisher Ideal Index } P_{on} = \sqrt{\frac{\sum P_n q_o}{\sum P_o q_o} \times \frac{\sum P_n q_n}{\sum P_o q_n}} \times 100$$

OR

$$P_{on} = \sqrt{Lasp(Pon) \times Paash(Pon)}$$

Marshal Edgeworth Index  $P_{on} = \frac{\sum P_n (q_o + q_n)}{\sum P_o (q_o + q_n)} \times 100$

OR  $P_{on} = \frac{\sum P_n q_o + \sum P_n q_n}{\sum P_o q_o + \sum P_o q_n} \times 100$

i) Weighted aggregate Quantity Index Numbers :

Laspeyres Index  $Q_{on} = \frac{\sum q_n P_o}{\sum q_o P_o} \times 100$

Paasche's Index  $Q_{on} = \frac{\sum q_n P_n}{\sum q_o P_n} \times 100$

Fisher Ideal Index  $Q_{on} = \sqrt{\frac{\sum q_n P_o}{\sum q_o P_o} \times \frac{\sum q_n P_o}{\sum q_o P_n}} \times 100$

OR

$$Q_{on} = \sqrt{Lasp (Q_{on}) \times Paash (Q_{on})}$$

Marshal Edgeworth Index  $Q_{on} = \left[ \frac{\sum q_n (P_o + P_n)}{\sum q_o (P_o + P_n)} \right] \times 100$

$$Q_{on} = \frac{\sum q_n P_o + \sum q_n P_n}{\sum q_o P_o + \sum q_o P_n} \times 100$$

i) Weighted average of Relative Price Index :

$$P_{on} = \frac{\sum \left( \frac{P_n}{P_o} \right) \times P_o q_o}{\sum P_o q_o} \times 100$$

OR

$$P_{on} = \frac{\sum \left( \frac{P_n}{P_o} \right) \times w}{\sum w} \times 100$$

OR

$$P_{on} = \frac{\sum I W}{\sum W} \quad \text{Where } I = \frac{P_n}{P_o} \times 100 \quad W = P_o q_o$$

Consumer's Price Index Numbers : (CPI)

Aggregative Expenditure Method.  $P_{on} = \frac{\sum P_n q_o}{\sum P_o q_o} \times 100$

Family (Household) Budget Method.  $P_{on} = \frac{\sum I W}{\sum W} \times 100$

## (5) PROBABILITY

Factorial:  $n! = n(n - 1)(n - 2) \dots 3.2.1 \quad (0! = 1)$

eg  $6! = 6 \times 5 \times 4 \times 3 \times 2 \times 1 = 720$

Permutation: (P)  $P_r^n = \frac{n!}{(n - r)!}$

$$P = \frac{n!}{n_1! n_2! \dots n_k!} \quad \sum_{k=1}^r nk = n$$

When all objects taken at a time having different types or kinds

Combination  $C_r^n = \frac{n!}{(n - r)! r!}$

### Laws of Probability :

If A and B are any two events, then

#### i) Addition Theorem : (Law)

$$P(A \cup B) = P(A) + P(B) \quad (\text{Events are Mutually exclusives})$$

$$P(A \cup B) = P(A) + P(B) - P(A \cap B) \quad (\text{Events are not Mutually exclusives})$$

#### ii) Multiplication Theorem : (Law)

$$P(A \cap B) = P(A) \cdot P(B) \quad (\text{Events are Independent})$$

$$P(A \cap B) = P(A) \cdot P(B/A) \quad (\text{Events are Dependent})$$

$$P(A \cap B) = P(B) \cdot P(A/B) \quad (\text{Events are Dependent})$$

#### iii) Conditional Probability : (Law)

$$P(A/B) = \frac{P(A \cap B)}{P(B)} \quad ; \quad P(B) > 0$$

$$P(B/A) = \frac{P(A \cap B)}{P(A)} \quad ; \quad P(A) > 0$$

#### iv) Complement Law of Probability :

$$P(A) + P(\bar{A}) = 1$$

## (6) RANDOM VARIABLE AND PROBABILITY DISTRIBUTION

**PROPERTIES OF :** (i) Discrete Probability Distribution:

$$\text{i) } f(x) > 0 \quad \text{ii) } \sum P(x_i) = 1$$

(ii) Continuous Probability density function:

$$\text{i) } f(x) > 0 \quad \text{ii) } \int f(x) dx = 1$$

OR Total Area =  $\frac{1}{2}$  [ sum of ordinates  $x = 1$

**Properties of Expectation :**

If  $a$  and  $b$  are two constants and  $x, y$  are tow independent variables, then

- |   |                               |
|---|-------------------------------|
| i) $E(a) = a$                             | ii) $E(x + a) = E(x) + a$     |
| iii) $E(ax) = aE(x)$                      | iv) $E(ax + b) = aE(x) + b$   |
| v) $E(x + y) = E(x) + E(y)$               | vi) $E(xy) = E(x) \cdot E(y)$ |
| vii) $E[x - E(x)] = E(x) - E(x)$<br>=Zero |                               |

## BINOMIAL AND HYPERGEOMETRIC DISTRIBUTION

P.d.f of Binomial distribution:-

$$f(x) = \binom{n}{x} p^x q^{n-x} \quad \text{for } x = 0, 1, 2, \dots, n$$

Mean of the binomial distribution =  $np$

Variance of the binomial distribution =  $npq$

S.D. of the binomial distribution =  $\sqrt{npq}$

P.d.f. of Hypergeometric distribution is :-

$$f(x) = \frac{\binom{k}{x} \binom{N-k}{n-x}}{\binom{N}{n}} \quad \text{for } x = 0, 1, 2, \dots, n$$

Mean of the Hypergeometric distribution =  $\frac{nK}{N}$

Variance of the Hypergeometric distribution =  $\frac{nK}{N} \left( \frac{N-K}{N} \right) \left( \frac{N-n}{N-1} \right)$