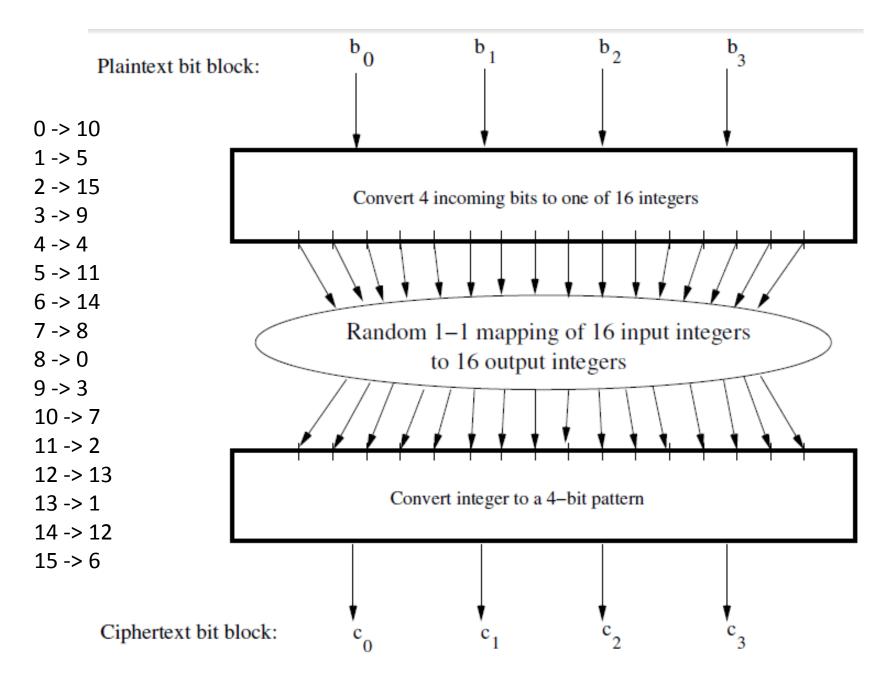
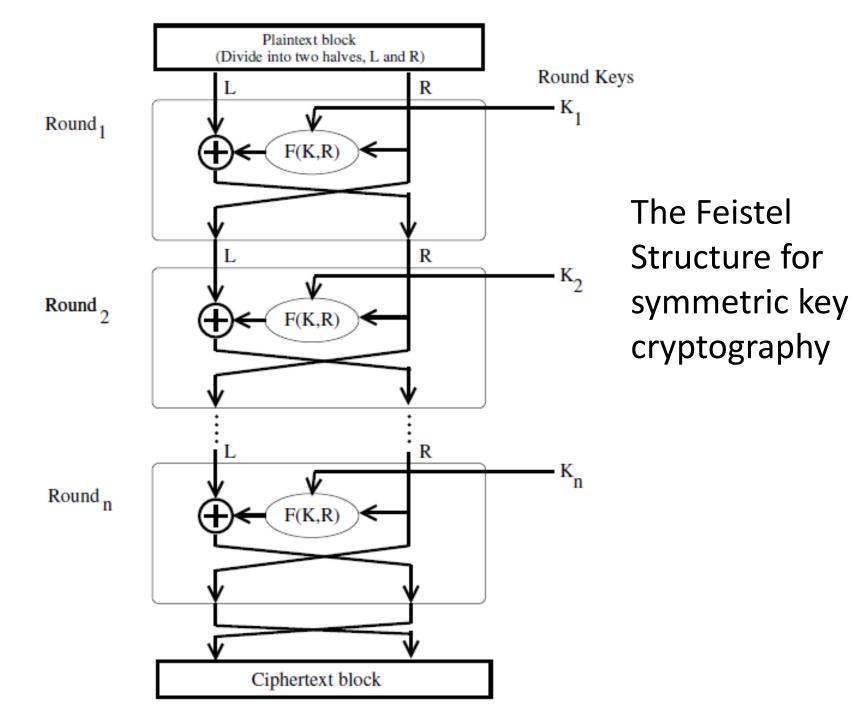
Data and Network Security

Course Code: IT-4542



The Feistel Structure For Block Ciphers

- Named after the IBM cryptographer Horst Feistel and first implemented in the Lucifer cipher by Horst Feistel and Don Coppersmith.
- There are multiple rounds of processing of the plaintext, with each round consisting of a substitution step followed by a permutation step.
- The block, R goes through unchanged. The left half, L, goes through an operation. The operation carried out on L is referred to as the Feistel Function.
- The permutation step: swapping the modified L and R.
- Examples: DES, Blowfish, CAST-128, and KASUMI



• Let LE_i and RE_i denote the output half-blocks at the end of the ith round of processing. The letter E' denotes encryption.

$$LE_i = RE_{i-1}$$

 $RE_i = LE_{i-1} \oplus F(RE_{i-1}, K_i)$

- F denotes the operation that "scrambles" RE_{i-1} of the previous round with the round key K_i .
- For Example, 16th rounds of processing

$$LE_{16} = RE_{15}$$

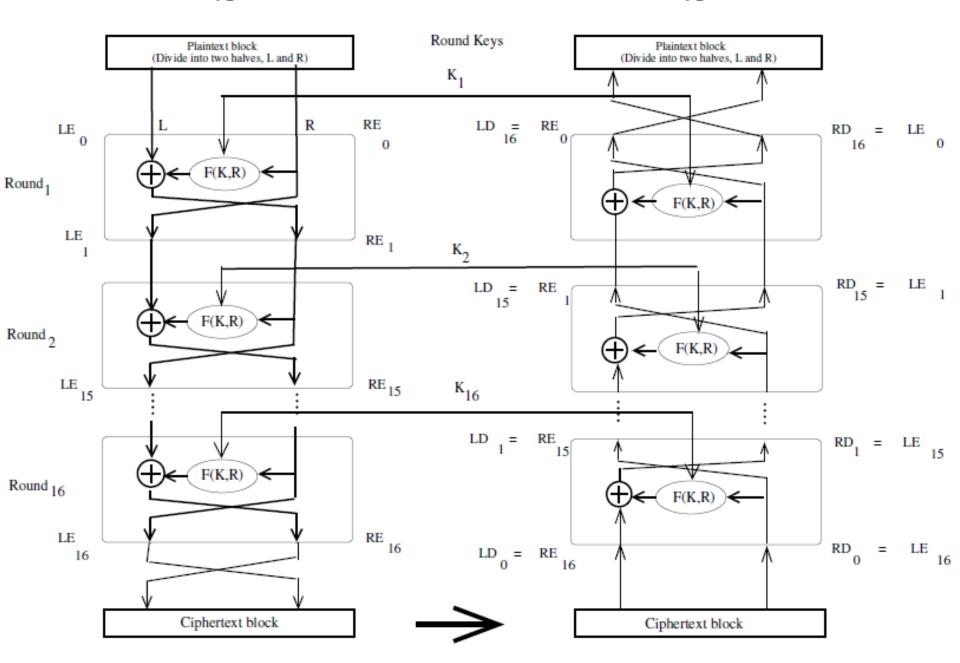
 $RE_{16} = LE_{15} \oplus F(RE_{15}, K_{16})$

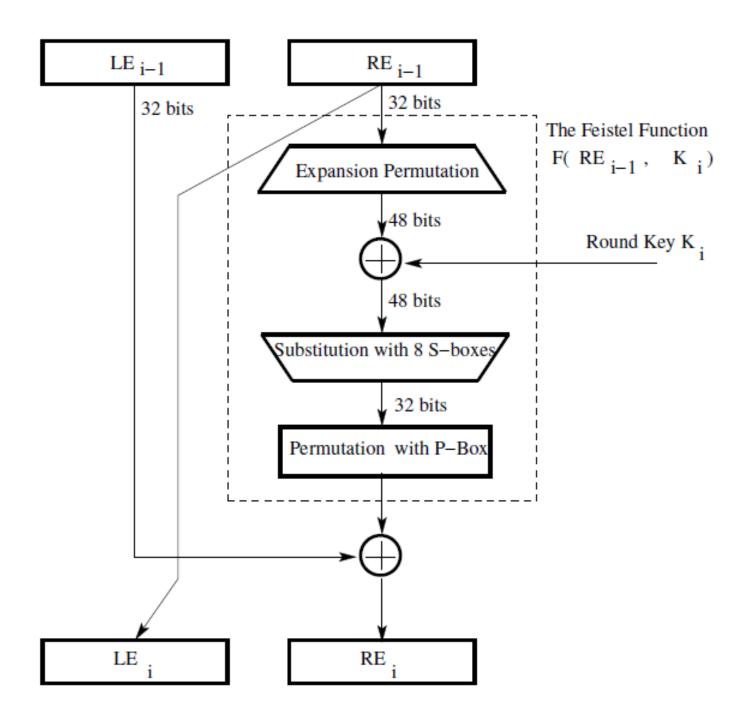
Decryption in Ciphers Based on the Feistel Structure

 The decryption algorithm is exactly the same as the encryption algorithm with the only difference that the round keys are used in the reverse order.

Encryption

Decryption





Data Encryption Algorithm

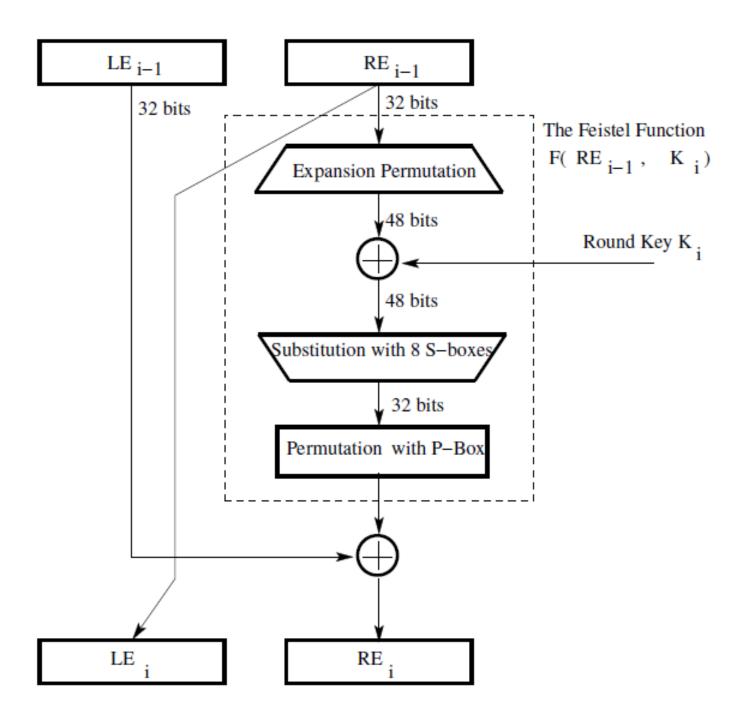
- The Expansion step:
 - first divide the 32-bit block into eight 4-bit words
 - attach an additional bit on the left to each 4-bit word that is the last bit of the previous 4-bit word
 - attach an additional bit to the right of each 4-bit word that is the beginning bit of the next 4-bit word.
 - Example: 1010 1010 1111010101

Data Encryption Algorithm

- The Expansion step:
 - first divide the 32-bit block into eight 4-bit words
 - attach an additional bit on the left to each 4-bit word that is the last bit of the previous 4-bit word
 - attach an additional bit to the right of each 4-bit word that is the beginning bit of the next 4-bit word.
 - Example: 1010 1010 1111010101

Data Encryption Algorithm

- The Expansion step:
 - first divide the 32-bit block into eight 4-bit words
 - attach an additional bit on the left to each 4-bit word that is the last bit of the previous 4-bit word
 - attach an additional bit to the right of each 4-bit word that is the beginning bit of the next 4-bit word.
 - Example: 1010 1010 1111010101



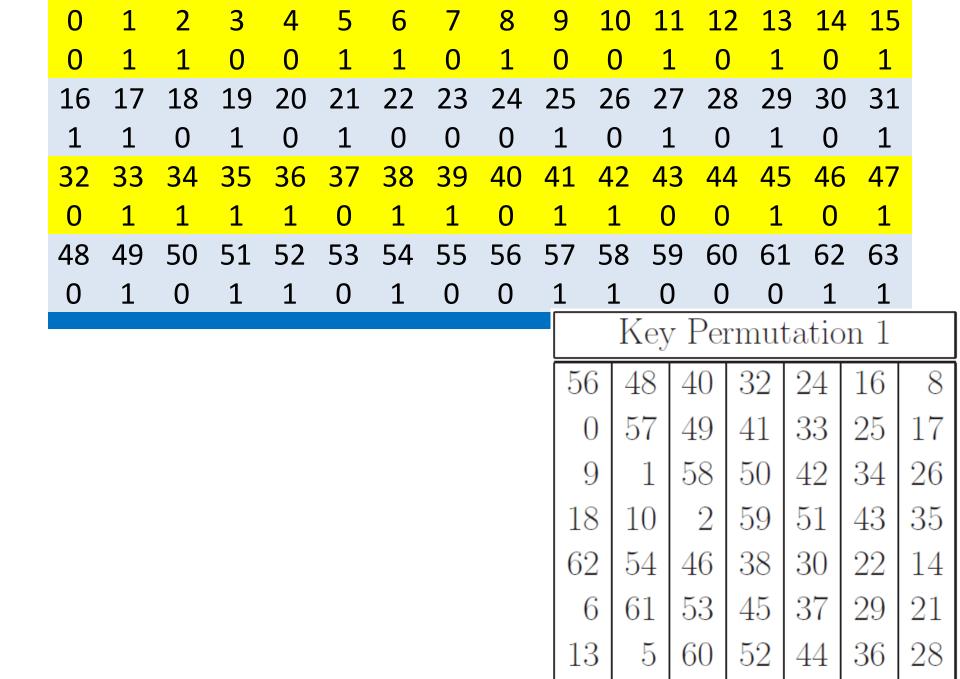
The DES Key Schedule: Generating the Round Keys

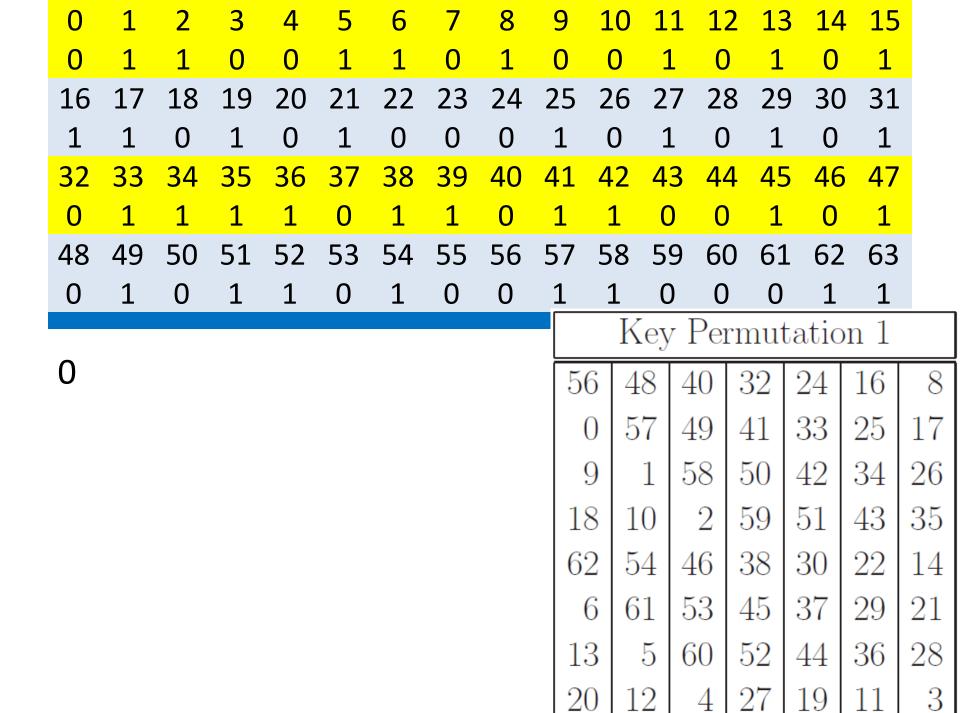
- The 56-bit encryption key is represented by 8 bytes, with the last bit (the least significant bit) of each byte used as a parity bit.
- The relevant 56 bits are subject to a permutation at the beginning before any round keys are generated. This is referred to as Key Permutation 1.
- At the beginning of each round, we divide the 56 relevant key bits into two 28 bit halves and circularly shift to the left each half by one or two bits, depending on the round.

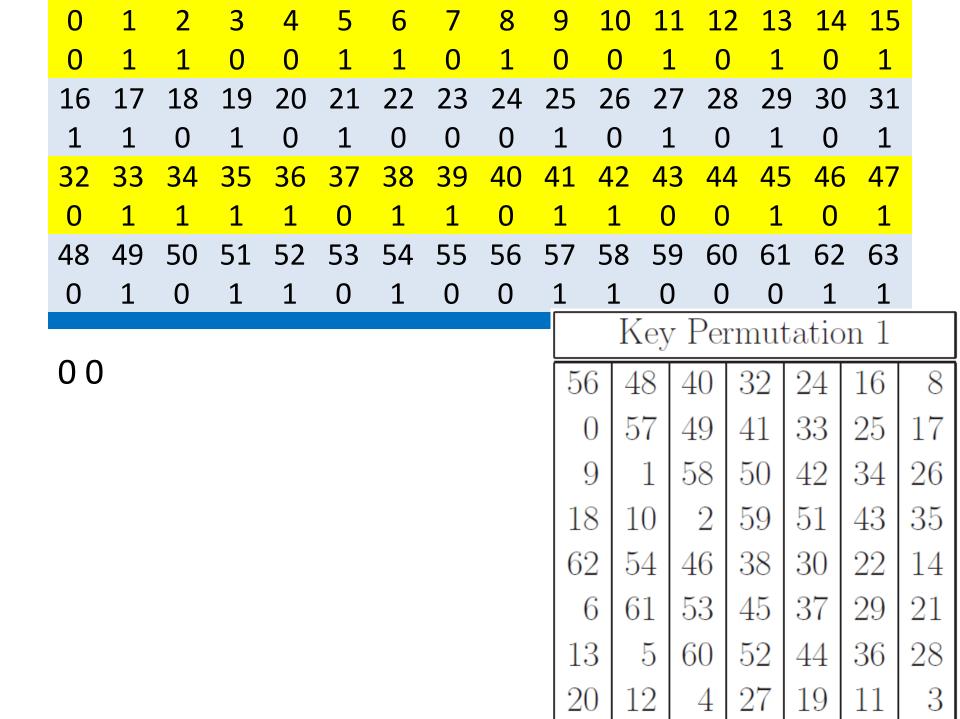
Key with even parity

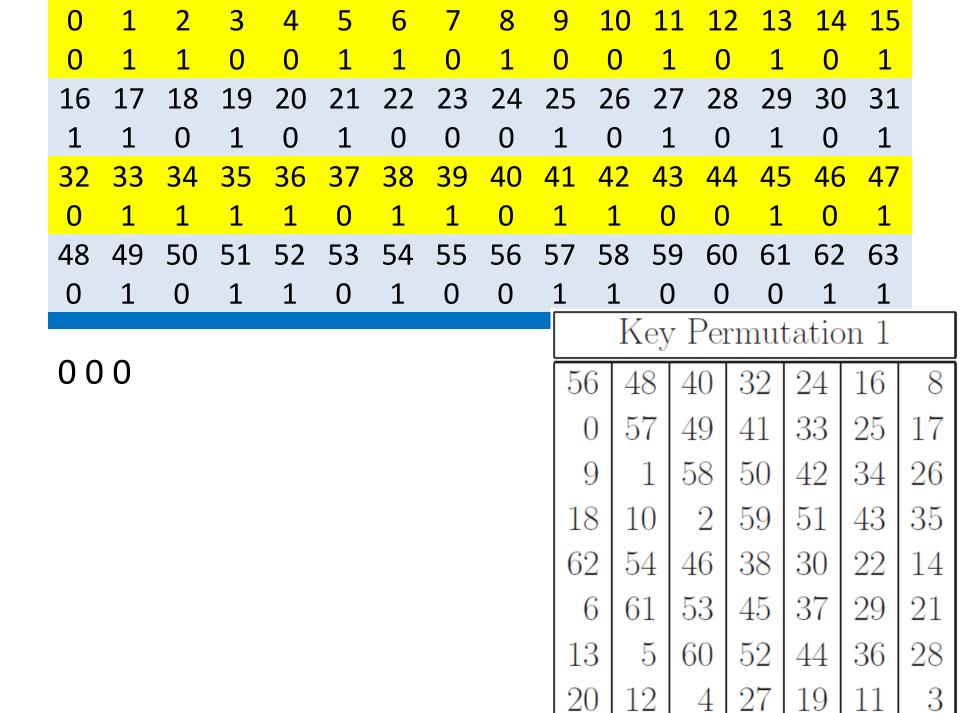
```
01100110 10010101 11010100 01010101
01111011 01100101 01011010 01100011
```

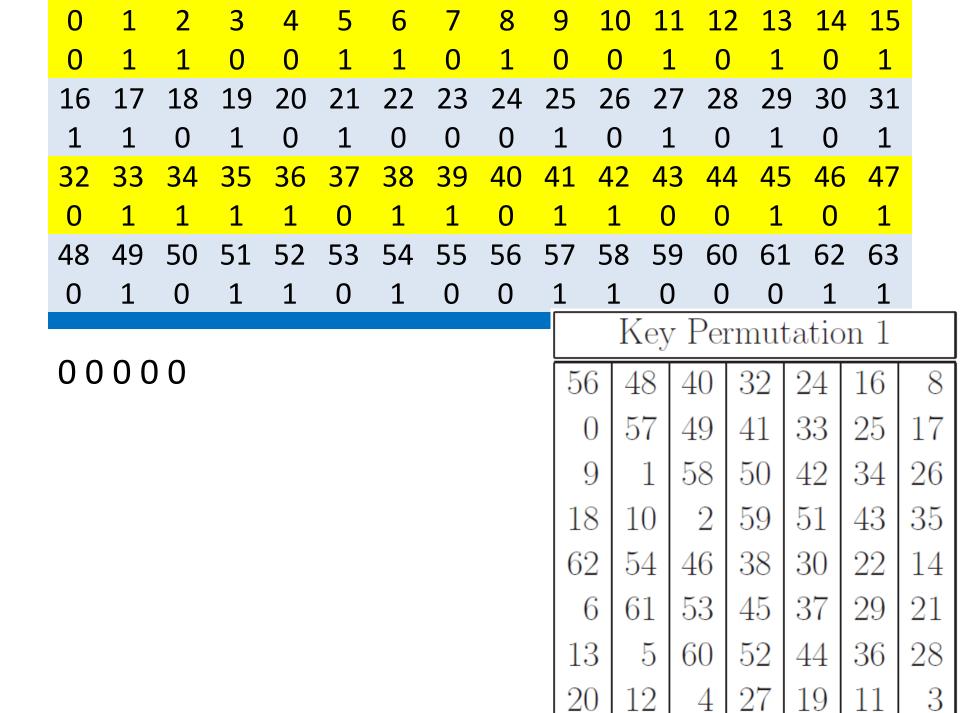
```
0
                           5
                                 6
                                            8
                                                 9
                                                      10
                                                           11
                                                                12
                                                                      13
                                 1
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                      0
                                      0
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\mathbf{O}
                                                 0
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16
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                                     23
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                                                                      45
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                                                            \mathbf{0}
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48
                          53
                                54
                                     55
                                          56
                                                     58
                                                           59
          50
                51
                     52
                                                57
                                                                60
                                                                      61
                                                                           62
                                                                                63
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                           0
                                      0
                                           0
                                                                 0
                                                                      0
```

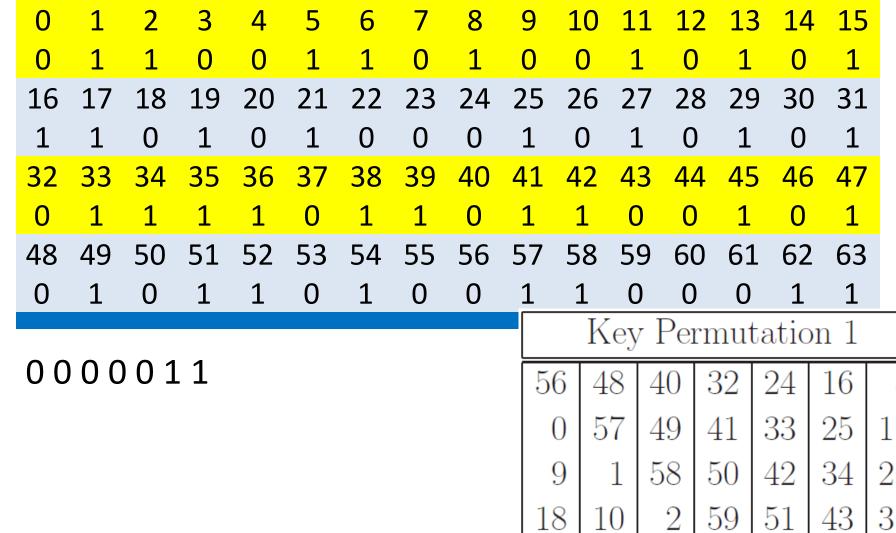


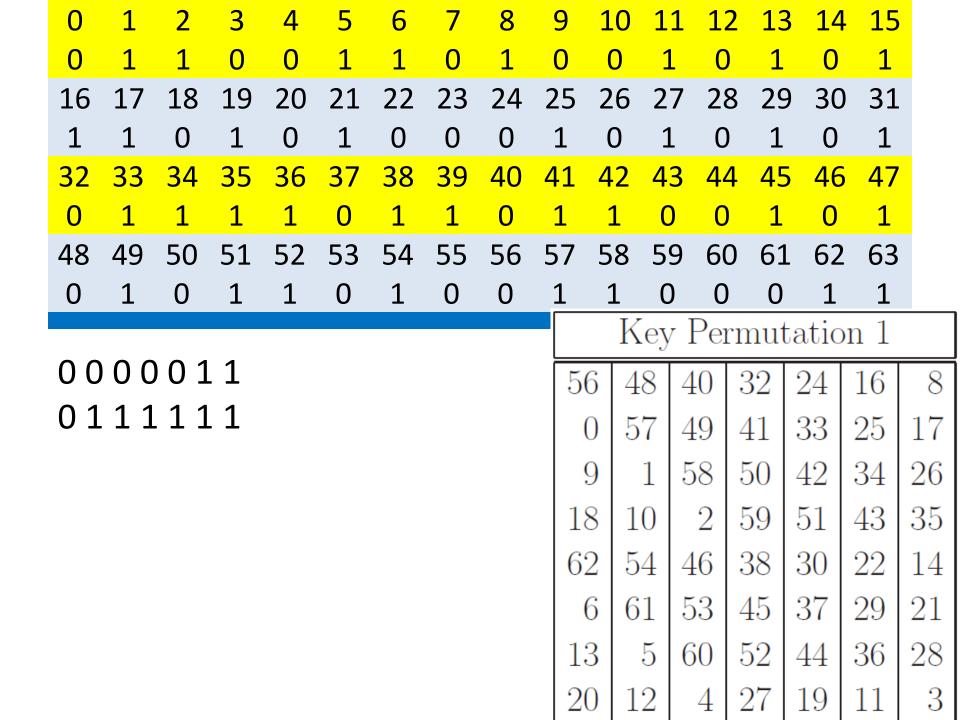


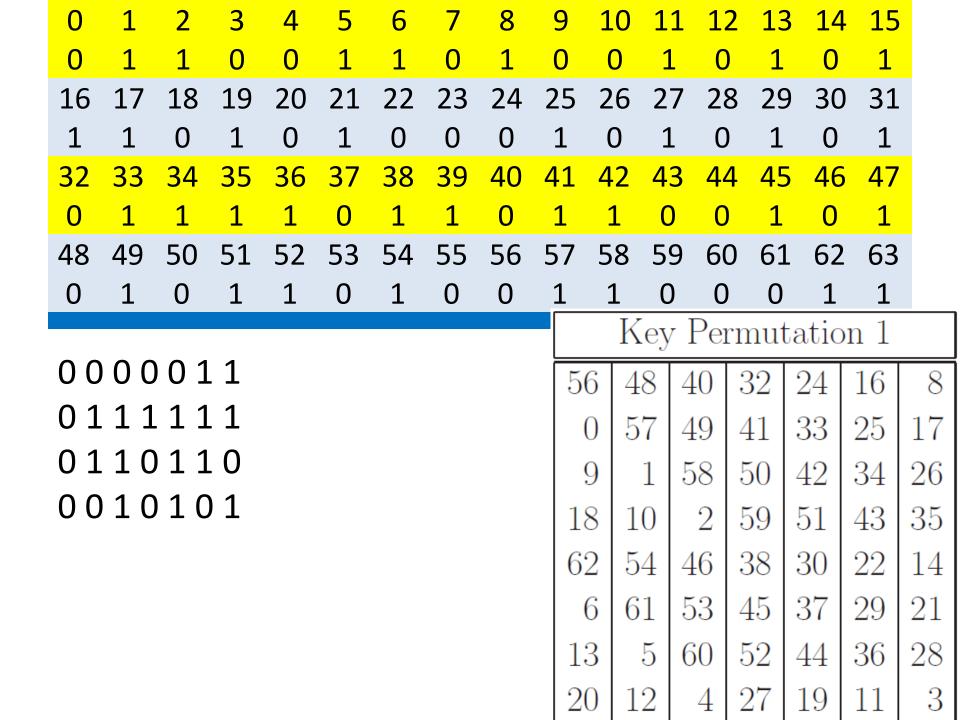


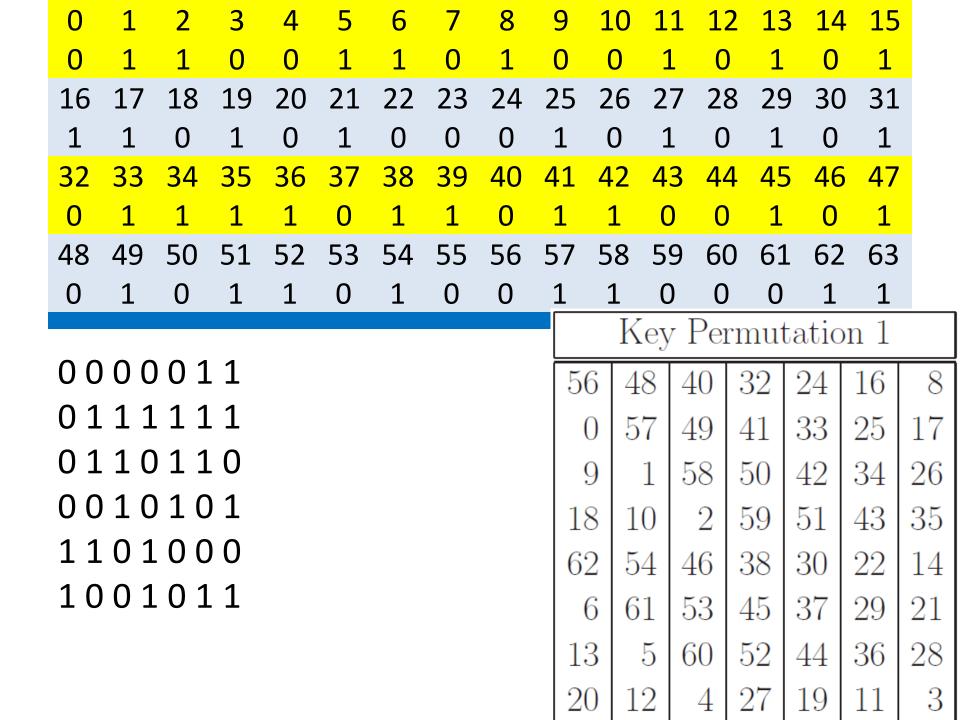


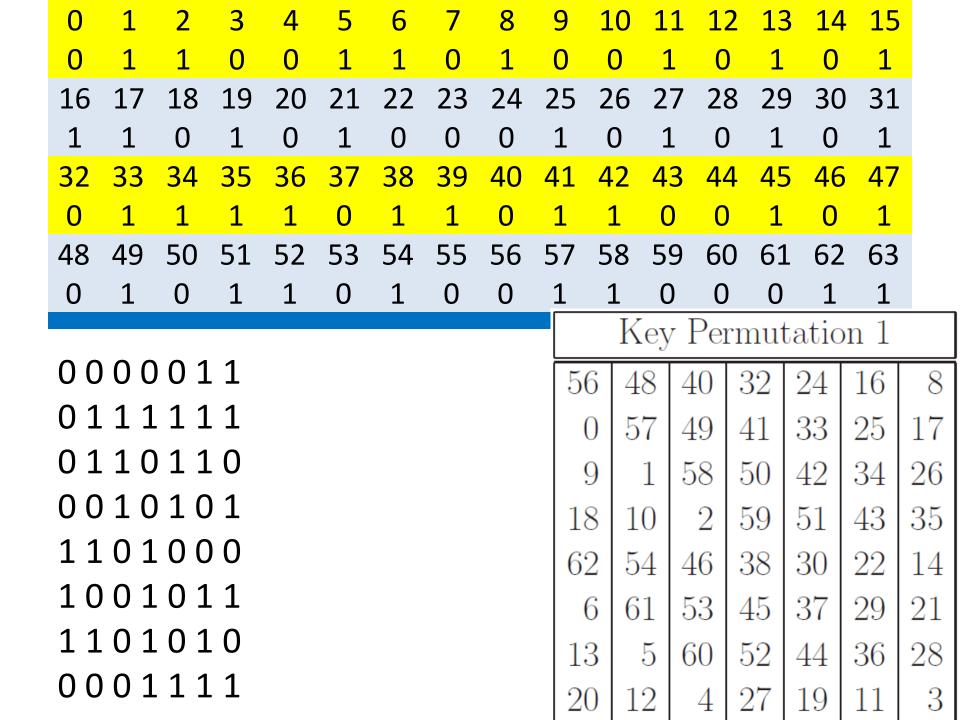












	0	1	2	3	4	5	6	7	8	9	10	11	12	13
	0	0	0	0	0	1	1	0	1	1	1	1	1	1
1	14	15	16	17	18	19	20	21	22	23	24	25	26	27
	0	1	1	0	1	1	0	0	0	1	0	1	0	1
2	28	29	30	31	32	33	34	35	36	37	38	39	40	41
	1	1	0	1	0	0	0	1	0	0	1	0	1	1
4	12	43	44	45	46	47	48	49	50	51	52	53	54	55
	1	1	0	1	0	1	0	0	0	0	1	1	1	1

0	1	2	3	4	5	6	7	8	9	10	11	12	13
0	0	0	0	0	1	1	0	1	1	1	1	1	1
14	15	16	17	18	19	20	21	22	23	24	25	26	27
0	1	1	0	1	1	0	0	0	1	0	1	0	1
28	29	30	31	32	33	34	35	36	37	38	39	40	41
1	1	0	1	0	0	0	1	0	0	1	0	1	1
42	43	44	45	46	47	48	49	50	51	52	53	54	55
1	1	0	1	0	1	0	0	0	0	1	1	1	1

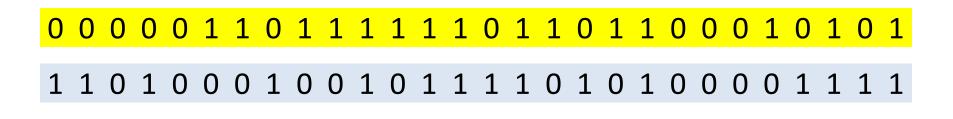
Round Number	Number of left shifts
1	1
2	1
3	2
4	2
5	2
6	2
7	2
8	2
9	1
10	2
11	2
12	2
13	2
14	2
15	2
16	1

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The DES Key Schedule: Generating the Round Keys

 Contraction-Permutation: Join together the two halves and apply a 56 bit to 48 bit contracting permutation (this is referred to as Permutation Choice 2).

	Key Permutation 2														
13 16 10 23 0 4 2 27															
14	5	20	9	22	18	11	3								
25	7	15	6	26	19	12	1								
40	51	30	36	46	54	29	39								
50	44	32	47	43	48	38	55								
33	52	45	41	49	35	28	31								



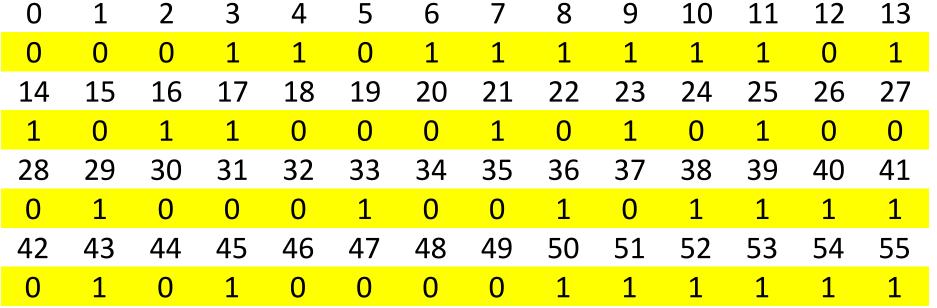
0 0 0 1 1 0 1 1 1 1 1 1 0 1 1 0 1 1 0 0 0 1 0 1 0 1 0 0

0	1	2	3	4	5	6	7	8	9	10	11	12	13
0	0	0	1	1	0	1	1	1	1	1	1	0	1
14	15	16	17	18	19	20	21	22	23	24	25	26	27
1	0	1	1	0	0	0	1	0	1	0	1	0	0
28	29	30	31	32	33	34	35	36	37	38	39	40	41
0	1	0	0	0	1	0	0	1	0	1	1	1	1
42	43	44	45	46	47	48	49	50	51	52	53	54	55
0	1	0	1	0	0	0	0	1	1	1	1	1	1

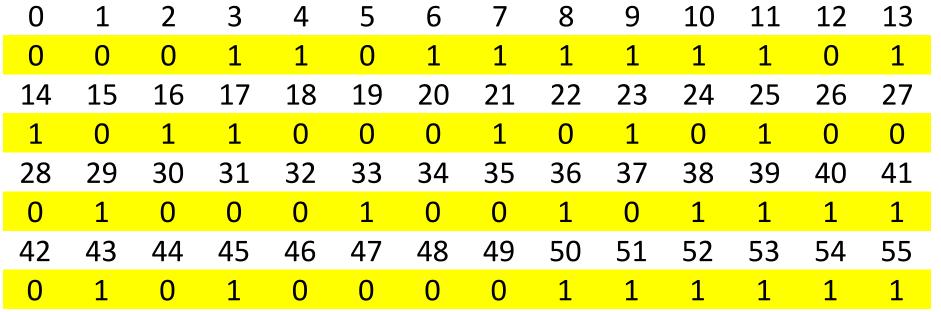
0	1	2	3	4	5	6	7	8	9	10	11	12	13
0	0	0	1	1	0	1	1	1	1	1	1	0	1
14	15	16	17	18	19	20	21	22	23	24	25	26	27
1	0	1	1	0	0	0	1	0	1	0	1	0	0
28	29	30	31	32	33	34	35	36	37	38	39	40	41
0	1	0	0	0	1	0	0	1	0	1	1	1	1
42	43	44	45	46	47	48	49	50	51	52	53	54	55
0	1	0	1	0	0	0	0	1	1	1	1	1	1

:														
	Key Permutation 2													
	13													
	14	5	20	9	22	18	11	3						
	25	7	15	6	26	19	12	1						
	40	51	30	36	46	54	29	39						
	50	44	32	47	43	48	38	55						
	33	52	45	41	49	35	28	31						

Key Permutation 2 ()



Key Permutation 2													
13	16	10	23	0	4	2	27						
14	5	20	9	22	18	11	3						
25	7	15	6	26	19	12	1						
40	51	30	36	46	54	29	39						
50	44	32	47	43	48	38	55						
33	52	45	41	49	35	28	31						

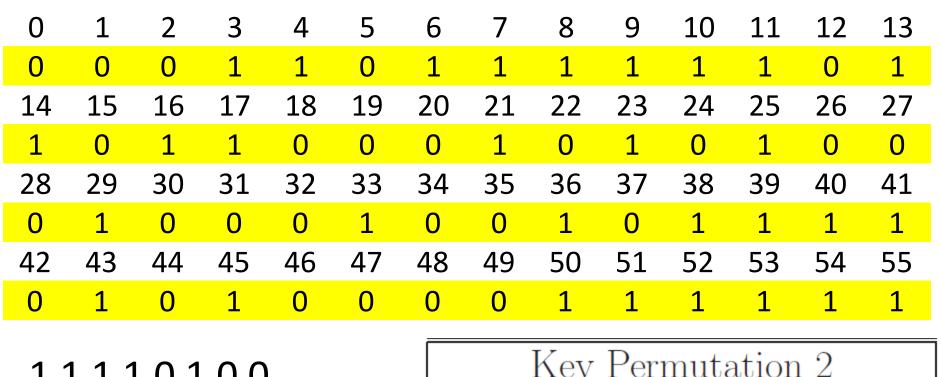


,														
	Key Permutation 2													
	13	16	10	23	0	4	2	27						
	14	5	20	9	22	18	11	3						
	25	7	15	6	26	19	12	1						
	40	51	30	36	46	54	29	39						
	50	44	32	47	43	48	38	55						
	33	52	45	41	49	35	28	31						

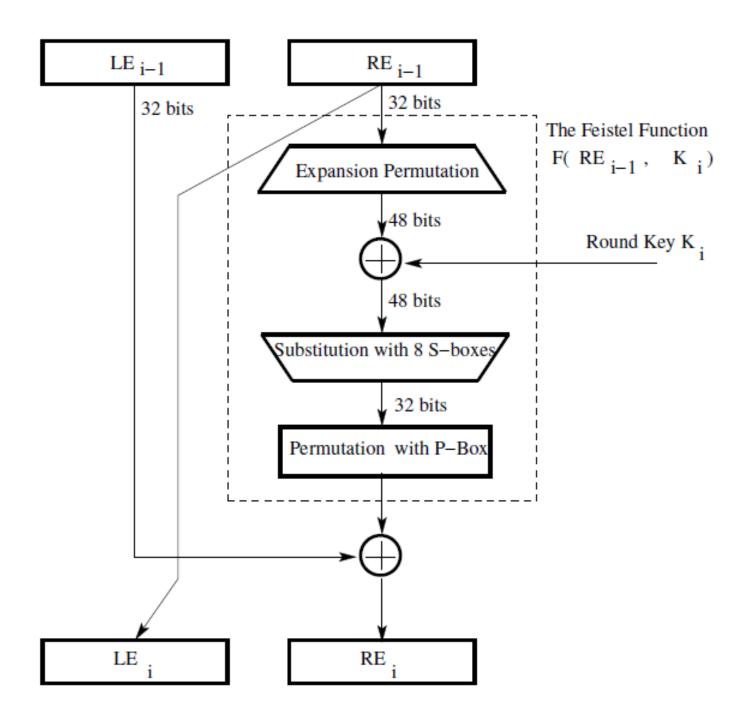


1	1	1	1	0	1	0	0
1	0	0	1	0	0	1	1
1	1	0	1	0	0	0	0
1	1	0	1	0	1	1	1
1	0	0	0	1	0	1	1
1	1	1	1	0	0	0	0

,														
	Key Permutation 2													
	13	16	10	23	0	4	2	27						
	14	5	20	9	22	18	11	3						
	25	7	15	6	26	19	12	1						
	40	51	30	36	46	54	29	39						
	50	44	32	47	43	48	38	55						
	33	52	45	41	49	35	28	31						



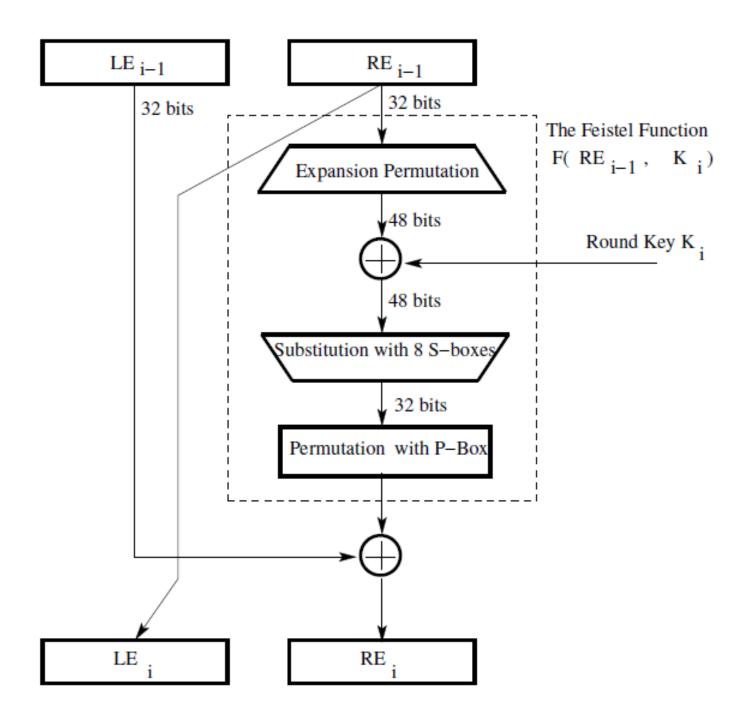
11110100	Key Permutation 2									
100100	13	16	10	23	0	4	2	27		
1101000	14	5	20	9	22	18	11	3		
1101000	25	7	15	6	26	19	12	1		
1001011	40	51	30	36	46	54	29	39		
11110100	50	44	32	47	43	48	38	55		



Data:

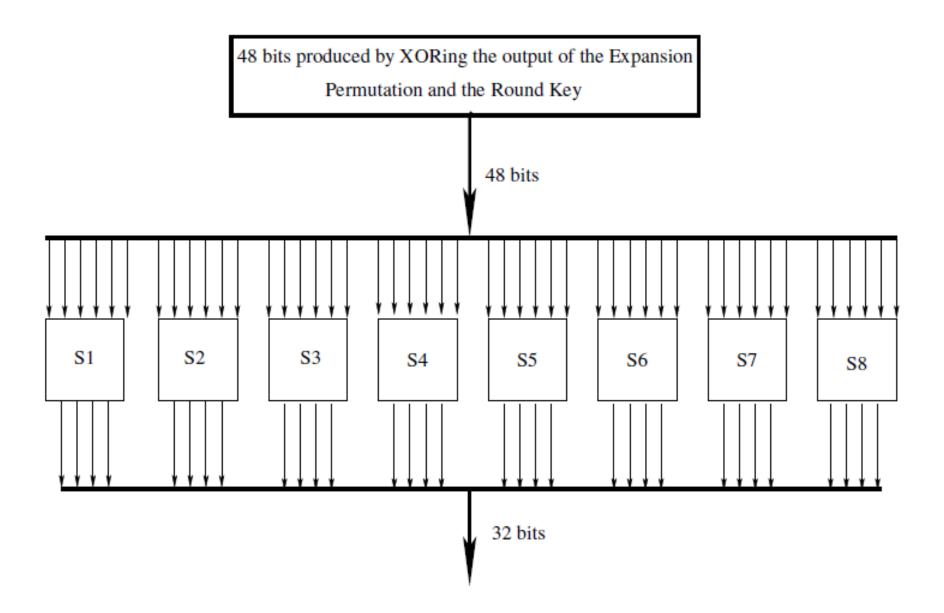
Key:

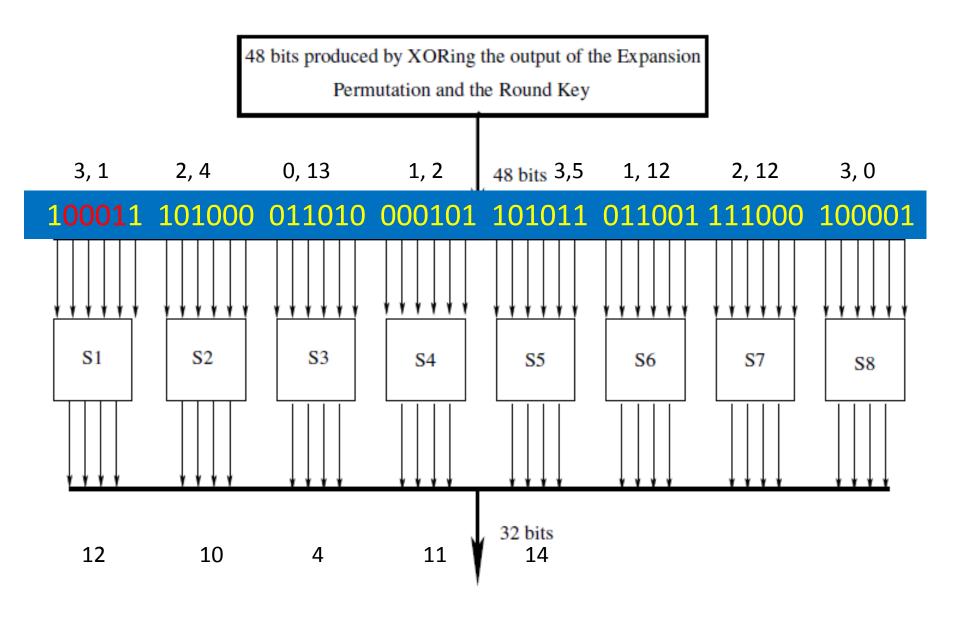
Data XOR Key:



The S-Box for the Substitution Step in Each Round

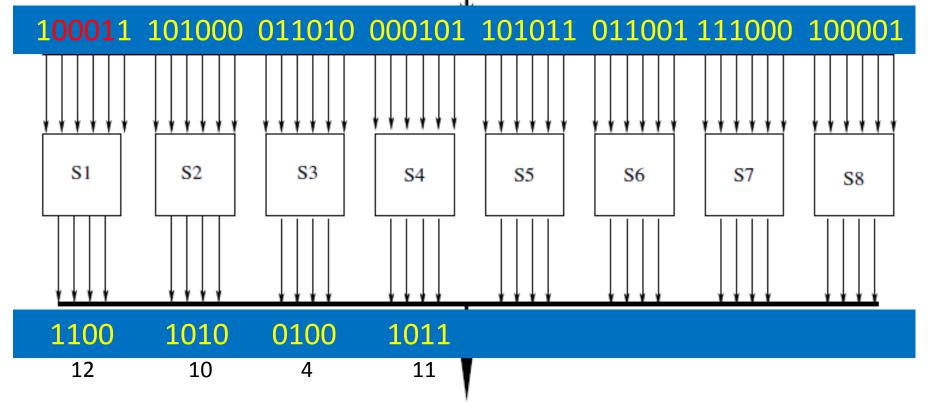
- the 48-bit input word is divided into eight 6-bit words and each 6-bit word fed into a separate Sbox. Each S-box produces a 4-bit output.
- Each of the eight S-boxes consists of a 4 × 16 table lookup for an output 4-bit word. The first and the last bit of the 6-bit input word are decoded into one of 4 rows and the middle 4 bits decoded into one of 16 columns for the table lookup.
- The S-boxes were tuned to enhance the resistance of DES to what is known as the differential cryptanalysis attack





48 bits produced by XORing the output of the Expansion
Permutation and the Round Key

48 bits



			Th	e 4 >	< 16	subst	ituti	on ta	able i	for S	-box	S_1			
14	4	13	1	2	15	11	8	3	10	6	12	5	9	0	7
0	15	7	4	14	2	13	1	10	6	12	11	9	5	3	8
4	1	14	8	13	6	2	11	15	12	9	7	3	10	5	0
15	12	8	2	4	9	1	7	5	11	3	14	10	0	6	13
	S-box S_2														
15	1	8	14	6	11	3	4	9	7	2	13	12	0	5	10
3	13	4	7	15	2	8	14	12	0	1	10	6	9	11	5
0	14	7	11	10	4	13	1	5	8	12	6	9	3	2	15
13	8	10	1	3	15	4	2	11	6	7	12	0	5	14	9
							S-bo	$\times S_3$							
10	0	9	14	6	3	15	5	1	13	12	7	11	4	2	8
13	7	0	9	3	4	6	10	2	8	5	14	12	11	15	1
13	6	4	9	8	15	3	0	11	1	2	12	5	10	14	7
1	10	13	0	6	9	8	7	4	15	14	3	11	5	2	12
							S-bo	$\times S_4$							
7	13	14	3	0	6	9	10	1	2	8	5	11	12	4	15
13	8	11	5	6	15	0	3	4	7	2	12	1	10	14	9
10	6	9	0	12	11	7	13	15	1	3	14	5	2	8	4
3	15	0	6	10	1	13	8	9	4	5	11	12	7	2	14

100011 101000 011010 000101 101011 011001 111000 100001

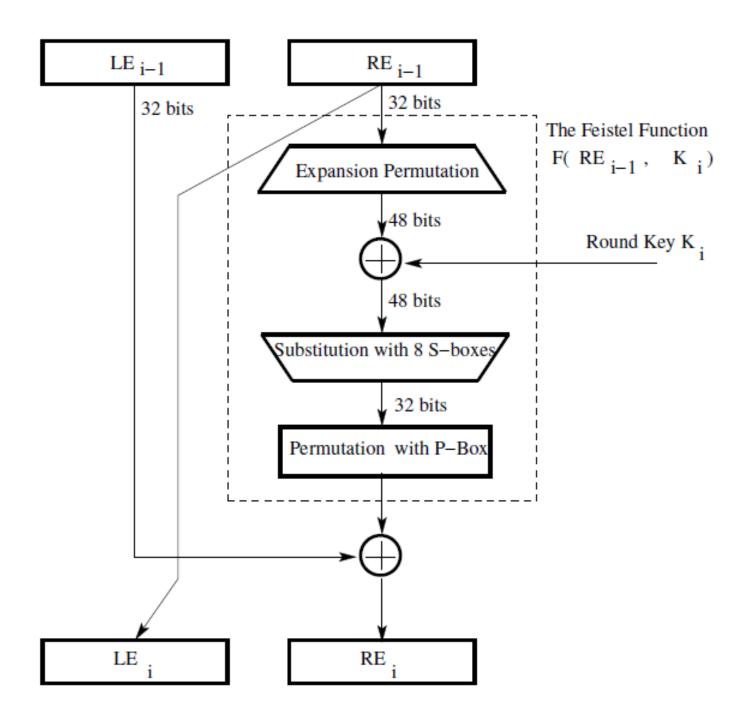
1	100011	11	3	12	1100	
		0001	1			
2	101000	10	2	10	1010	
	101000	0100	4		1010	
3	011010	00	0	4	0100	
3	011010	1101	13	4	0100	
1	000101	01	1	11	1011	
4	000101	0010	2	11	1011	
5	101011	11	3	14	1110	
	101011	0101	5	14		
6	011001	01	1	0	0000	
0	011001	1100	12	0	0000	
7	111000	10	2	0	0000	
/	111000	1100	12	U		
8	100001	11	3	<u> </u>	0010	
0	100001	0000	0	2	0010	

							S-bo	$\times S_5$							
2	12	4	1	7	10	11	6	8	5	3	15	13	0	14	9
14	11	2	12	4	7	13	1	5	0	15	10	3	9	8	6
4	2	1	11	10	13	7	8	15	9	12	5	6	3	0	14
11	8	12	7	1	14	2	13	6	15	0	9	10	4	5	3
S-box S_6															
12	1	10	15	9	2	6	8	0	13	3	4	14	7	5	11
10	15	4	2	7	12	9	5	6	1	13	14	0	11	3	8
9	14	15	5	2	8	12	3	7	0	4	10	1	13	11	6
4	3	2	12	9	5	15	10	11	14	1	7	6	0	8	13
							S-bo	$\times S_7$							
4	11	2	14	15	0	8	13	3	12	9	7	5	10	6	1
13	0	11	7	4	9	1	10	14	3	5	12	2	15	8	6
1	4	11	19	12	3	7	1.4	4.0			0	0		_	0
		11	13	14	3	(14	10	15	6	8	0	5	9	2
6	11	13	8	1	4	10	$\frac{14}{7}$	10 9	15 5	6	8 15	14	5 2	9	12 12
1 1	ı					10		9			_	_			
1 1	ı					10	7	9			_	_			
6	11	13	8	1	4	10	7 S-bo	9 x S ₈	5	0	15	14	2	3	12
13	2	8	4	6	15	10	7 S-bo	$\frac{9}{\times S_8}$	5 9	3	15	5	0	12	7

100011 101000 011010 000101 101011 011001 111000 100001

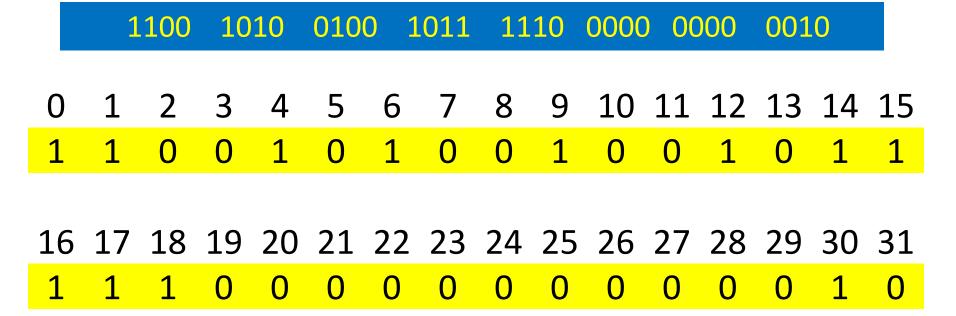
1	100011	11	3	12	1100	
		0001	1			
2	101000	10	2	10	1010	
	101000	0100	4		1010	
3	011010	00	0	4	0100	
3	011010	1101	13	4	0100	
1	000101	01	1	11	1011	
4	000101	0010	2	11	1011	
5	101011	11	3	14	1110	
	101011	0101	5	14		
6	011001	01	1	0	0000	
0	011001	1100	12	0	0000	
7	111000	10	2	0	0000	
/	111000	1100	12	U		
8	100001	11	3	<u> </u>	0010	
0	100001	0000	0	2	0010	

1	100011	11 0001	3	12	1100	
	101000	10	2	4.0	1010	
2	101000	0100	4	10	1010	
3	011010	00	0	4	0100	
<u> </u>	011010	1101	13		0100	
4	000101	01	1	11	1011	
4	000101	0010	2		1011	
5	101011	11	3	14	1110	
	101011	0101	5			
6	011001	01	1	0	0000	
	011001	1100	12			
7	111000	10	2	0	0000	
,	111000	1100	12			
8	100001	11	3	2	0010	
	100001	0000	0	~	0010	



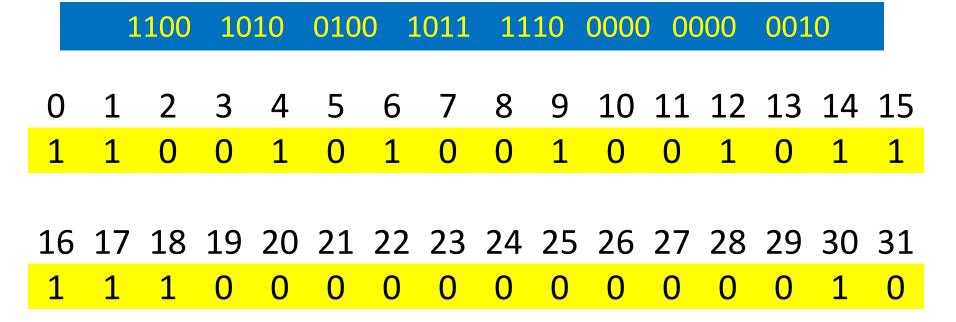
Permutation with P-Box

	P-Box Permutation											
15	15 6 19 20 28 11 27 16											
0	14	22	25	4	17	30	9					
1	1 7 23 13 31 26 2 8											
18	12	29	5	21	10	3	24					

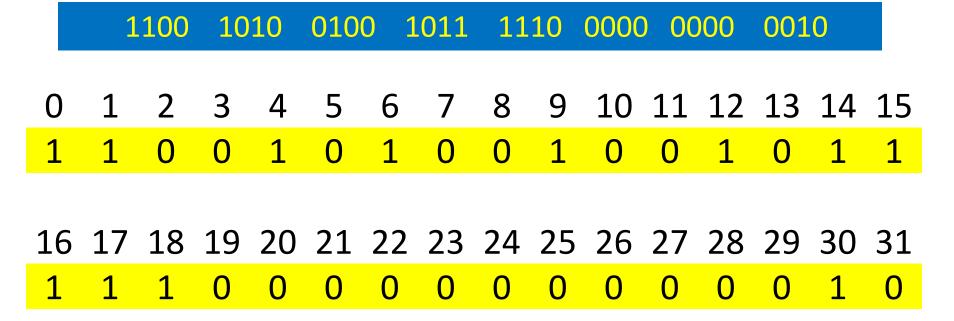




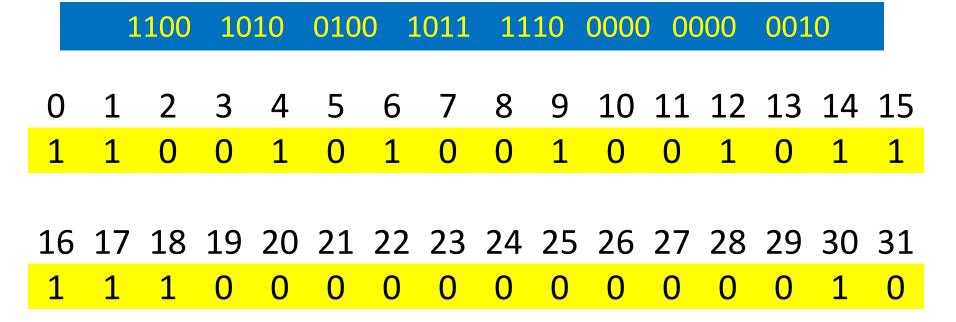
P-Box Permutation												
15	5 6 19 20 28 11 27 16											
0	14	22	25	4	17	30	9					
1	7	23	13	31	26	2	8					
18	12	29	5	21	10	3	24					



	P-Box Permutation											
15	6	19	20	28	11	27	16					
0	14	22	25	4	17	30	9					
1	7	23	13	31	26	2	8					
18	12	29	5	21	10	3	24					



	P-Box Permutation											
15	6	19	20	28	11	27	16					
0	14	22	25	4	17	30	9					
1	7	23	13	31	26	2	8					
18	12	29	5	21	10	3	24					



1100 00011100 1111

	P-Box Permutation											
15	6	19	20	28	11	27	16					
0	14	22	25	4	17	30	9					
1	7	23	13	31	26	2	8					
18	12	29	5	21	10	3	24					

1100 1010 0100 1011 1110 0000 0000 5 6 7 8 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31

1100 00011100 11111000 0000

	P-Box Permutation											
15	6	19	20	28	11	27	16					
0	14	22	25	4	17	30	9					
1	7	23	13	31	26	2	8					
18	12	29	5	21	10	3	24					

0100 1011 1110 0000 0000 1100 1010 5 6 7 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31

	P-Box Permutation											
15	6	19	20	28	11	27	16					
0	14	22	25	4	17	30	9					
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