

RSA

In RSA, if $P=3$ & $q=11$, $M=31$
Compute Encryption & Decryption.

Step 1:-

Calculate $n = p \times q$

$$n = 3 \times 11$$

$$n = 33$$

Step 2:-

Calculate $\phi(n) = (p-1) \times (q-1)$

$$= (3-1) \times (11-1)$$

$$= 2 \times 10$$

$$\phi(n) = 20$$

Step 3:-

Choose "e" such that $1 < e < \phi(n)$

e is co-prime to $\phi(n)$, $\gcd(e, \phi(n)) = 1$

$$1 < e < \phi(n)$$

$$1 < e < 20$$

$$e = 3$$

Step 4:-

Calculate d, such that

$$de = 1 \pmod{\phi(n)}$$

$$d = de \pmod{\phi(n)} = 1$$

$$= d \times 3 \pmod{\phi(n)} = 1$$

$$\therefore d = \frac{1 + k\phi(n)}{e}$$

$$d = \frac{1 + 1(20)}{3} \Rightarrow \frac{21}{3} = 7$$

$$d = \frac{1 + 2(20)}{3} \Rightarrow \frac{41}{3} = 13.66$$

$$d = \frac{1 + 4(20)}{3} = 27$$

$$d = 7$$

$$\text{Public Key} = \{e, n\} = \{3, 33\}$$

$$\text{Private Key} = \{d, n\} = \{7, 33\}$$

► Given $M = 31$

For Encryption:-

$$C = M^e \bmod n$$

$$C = 31^3 \bmod 33$$

$$31 \bmod 33 = 31$$

$$31^2 \bmod 33 = 4$$

$$124 \bmod 33 = 25$$

$$\boxed{C = 25}$$

For Decryption:-

$$M = C^d \bmod 33$$

$$= 25^7 \bmod 33$$

$$25 \bmod 33 = 25 \quad 25^2 \bmod 33 = 31$$

$$25^4 \bmod 33 = 4$$

$$25 \times 31 \times 4 = 3100$$

$$3100 \bmod 33 =$$

$$\boxed{D = 31}$$

In RSA, if $e = 13$ & $n = 100$, Encrypt the message "HAPPY" using 0-25 for A to Z

Step 1:-

Choose two large prime numbers

$$p = 7, q = 11$$

Step 2:-

Given

$$n = 100$$

Step 3:-

$$\text{Calculate } \phi(n) = (p-1) * (q-1)$$

$$= (7-1) * (11-1)$$

$$= 6 * 10$$

$$\phi(n) = 60$$

Step 4:-

Given

$$e = 13$$

► H A P P Y

$$7 + 0 + 15 + 15 + 24$$

$$M = 61$$

For Encryption:-

$$C = M^e \text{ mod } n$$

$$= 61^{13} \text{ mod } n$$

$$61 \bmod 100 = 61$$

$$61^2 \bmod 100 = 21$$

$$61^4 \bmod 100 = 41$$

$$61^8 \bmod 100 = 1.9170$$

$$61 \times 41 \times 21 \times 1.9170 = 1.006865$$

$$C = 1.006865$$