

Inclusion-Exclusion Principle:

→ Let A & B be any finite sets, then:

$$n(A \cup B) = n(A) + n(B) - n(A \cap B) \rightarrow (i)$$

→ For any finite sets; A, B & C .

$$n(A \cup B \cup C) = n(A) + n(B) + n(C) - n(A \cap B) - n(B \cap C) - n(A \cap C) + n(A \cap B \cap C) \rightarrow (ii)$$

* Group of 80 peoples; 60 likes Eggs & 30 likes fish; find Percentage of Peoples like both.

$$n(E) = 60$$

$$n(F) = 30$$

$$n(E \cap F) = ?$$

$$n(E \cup F) = 80$$

$$n(E \cup F) = n(E) + n(F) - n(E \cap F)$$

$$80 = 60 + 30 - n(E \cap F).$$

$$(10) = n(E \cap F).$$

* 200 students; 50 take math, 140 took economics & 24 took both. How many of them not took any of the course.

$$n(M) = 50$$

$$n(E) = 140$$

$$n(M \cap E) = 24$$

$$n(M \cup E) = 50 + 140 - 24.$$

$$= 166.$$

$$200 - 166 = (34)$$

* In a survey of usage of three toothpaste A, B, C . It is found that 60 people likes A , 55 like B , 40 likes C , 20 likes A & B , 35 likes B & C , 15 likes A & C and 10 likes all. Find no. of persons included in the survey?

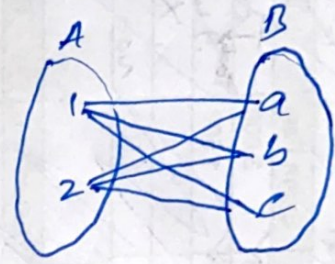
Relations and their Properties:

→ Relations: Relation is derived from cartesian product of sets. i.e:

$$A = \{1, 2\}, B = \{a, b, c\}$$

$$A \times B = \{(1, a), (1, b), (1, c), (2, a), (2, b), (2, c)\}$$

Cartesian product
of A & B .



Defination: Let A and B be two non-empty sets, then a relation R from A to B is a subset of $A \times B$ (cartesian product).

$$\therefore R \subseteq A \times B.$$

Example: $A = \{1, 2\}$ and $B = \{1, 2, 3\}$

$$R_1 = \{(1, 1), (1, 3), (2, 2), (2, 3)\}$$

↳ Relation Because.

$$R_1 \subseteq A \times B.$$

Some important points of relation:

$$R_{\text{MAX}} = A \times B, R_{\text{MIN}} = \emptyset, \text{Total}$$

Binary Relation: A binary relation ' R ' from A to B , is a set of ordered pairs where first element is from set A and second element is from set B .

Example: $A = \{a, b\}, B = \{1, 2, 3\}$.

$$\vec{A}RB = \{(a, 1), (a, 2), (b, 3)\}.$$