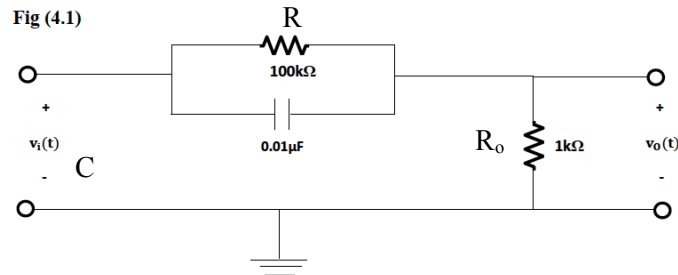


EXPERIMENT #3

Frequency Response for Circuit 1



Output voltage is obtained using voltage division between the 1 kΩ resistor (R_o) and $Z_{R||C}$.

$$Z_{R||C} = \frac{R}{1 + j\omega RC}$$

Transfer function

$$H(j\omega) = \frac{V_o(j\omega)}{V_i(j\omega)} = \frac{R_o}{R_o + Z_{R||C}} = \frac{R_o(1 + j\omega RC)}{R_o(1 + j\omega RC) + R} = \frac{R_o}{R + R_o} \frac{(1 + j\omega RC)}{(1 + \frac{j\omega R_o RC}{R + R_o})}$$

$$|H|_{dB} = 20 \log \left(\frac{R_o}{R + R_o} \right) + 20 \log(1 + j\omega RC) - 20 \log \left(1 + \frac{j\omega R_o RC}{R + R_o} \right)$$

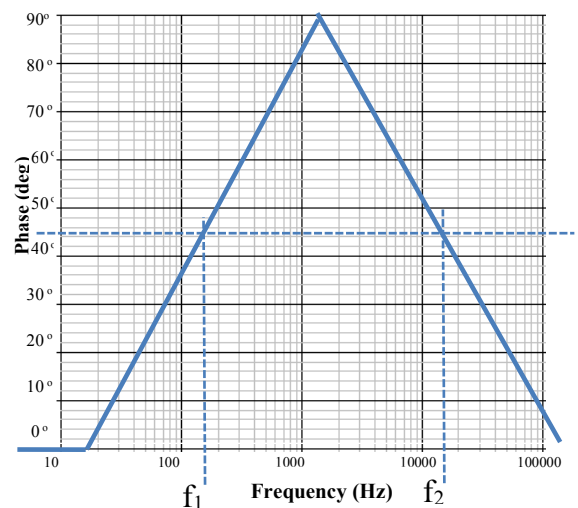
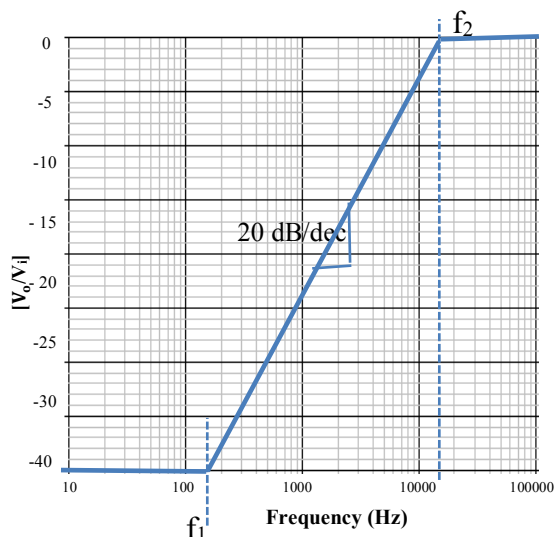
-40 dB

Corner Frequencies at

$$\omega_1 = \frac{1}{RC} = 1000 \text{ rad/s} \quad f_1 = 160 \text{ Hz} \quad (\text{zero})$$

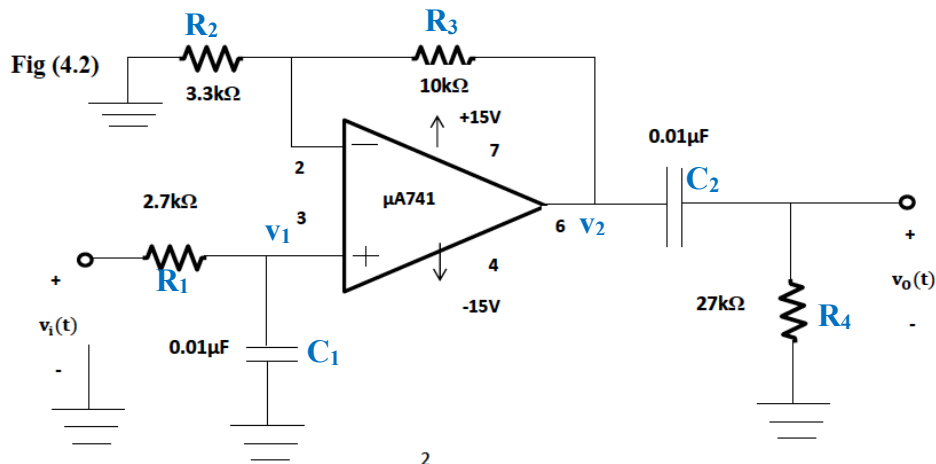
and

$$\omega_2 = \frac{R + R_o}{R_o RC} = 101,000 \text{ rad/s} \quad f_2 = 16 \times 10^3 \text{ Hz} \quad (\text{pole})$$



In the instructions, they were asked to find f_z and f_p . These are the zero and pole (corner frequencies) of the transfer function. There are 2 ways of getting them: 1. From the phase shift plot at $\pm 45^\circ$ 2. From the magnitude plot: find the corner of the asymptotic plots.

October 28, 2020 Prepared for ELE 302 TAs
Frequency Response for Circuit 2



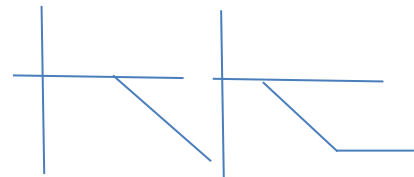
To get the transfer function $H(j\omega)$, we need to find v_1/v_i and v_2/v_1 , and v_o/v_2

$$H(j\omega) = \frac{V_o}{V_i} = \frac{V_o}{V_2} \frac{V_2}{V_1} \frac{V_1}{V_i} = H_3 H_2 H_1$$

- 1) Using voltage division to get v_1/v_i

$$H_1 = \frac{V_1}{V_i} = \frac{1}{1 + j\omega R_1 C_1}$$

corner frequency at $\omega_1 = \frac{1}{R_1 C_1} = 37 \text{ k rad/s}$ $f_1 = 5,893 \text{ Hz}$



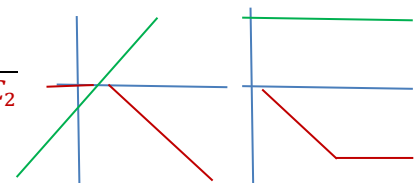
- 2) Non-inverting amplifier (or nodal analysis at Pin 2) to get v_2/v_1

$$H_2 = \frac{V_2}{V_1} = 1 + \frac{R_3}{R_2}$$

- 3) Using voltage division to get v_o/v_2

$$H_3 = \frac{V_o}{V_2} = \frac{j\omega R_4 C_2}{1 + j\omega R_4 C_2}$$

corner frequency at $\omega_2 = \frac{1}{R_4 C_2} = 3.7 \text{ k rad/s}$ $f_2 = 589 \text{ Hz}$
 and a zero at the origin

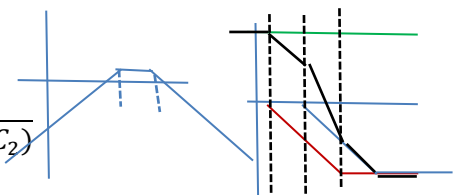


Combining all three stages together, one zero and two poles:

$$H(j\omega) = \left(1 + \frac{R_3}{R_2}\right) R_4 C_2 \frac{j\omega}{(1 + j\omega R_1 C_1)(1 + j\omega R_4 C_2)}$$

With a constant gain of $(1 + R_3/R_2)R_4 C_2 = 0.001$

$20 \log(0.001) = -60 \text{ dB}$ at $\omega = 1 \text{ rad/s}$ ($f = 0.16 \text{ Hz}$)



Time-mode phase angle: $\Delta T/T \times 360 = \Delta T \times f \times 360$ (output Leading: output at left of input is +ve)

XY-mode phase angle: Please follow the instructions from ELE 202 Experiment instruction as below:

