

# Trade Model with Endogenous Technology Choice

International Trade (PhD), Fall 2024

Ahmad Lashkaripour

Indiana University

# Overview of Lecture

- This lecture reviews a multi-industry trade model with endogenous technology choice.
  - there are multiple production technologies
  - firms sort into technologies depending on productivity profile
- Main implications
  - trade integration can encourage the adoption of more productive technologies → larger efficiency gains
  - trade can mitigate distorted technology choices (e.g., there is too little adoption of modern technologies in low-income countries due to inefficient barriers)
- Main References:
  - technology choice in efficient economies: Farrokhi and Pellegrina (2023, JPE)
  - technology choice in distorted economies: Farrokhi, Lashkaripour, Pellegrina (2024, JIE)

## Environment

- $n, i = 1, \dots, N$  countries
- $k = 1, \dots, K$  industries
- $t = 1, \dots, T$  different types of technology within each industry:
  - technologies differ in their general productivity and factor intensity
- Each industry is populated by a constant measure of managers that sort into technology types and employ their managerial capital and other inputs for production.

# Birdseye View of Model

## Demand and Supply of Final Goods

- Governed by a multi-industry gravity model, à la Eaton-Kortum or equivalently Armington.

## Key Departures from the Standard Multi-Industry Model

- Workers have heterogeneous abilities.
- Different industries within a country offer varying wages.
- Workers sort into industries to maximize their *productivity × wage*, following the Roy model.

## Demand and Preferences

- Cobb-Douglas utility aggregator across industries:

$$U_i(\mathbf{C}_i) = \prod_k \left( \frac{C_{i,k}}{\beta_{i,k}} \right)^{\beta_{i,k}}$$

implying a constant share  $\beta_{i,k}$  of expenditure on industry  $k$  goods.

- CES utility aggregator across goods sourced from various industries:

$$C_{i,k} = \left( \sum_n b_{n,k}^{\frac{1}{\sigma_k}} C_{ni,k}^{\frac{\sigma_k-1}{\sigma_k}} \right)^{\frac{\sigma_k}{\sigma_k-1}}$$

- goods are internationally differentiated but homogeneous within countries, irrespective of which technology they are developed with.

## Demand and Preferences

- Let  $p_{i,k}$  denote the competitive price of goods supplied by firms in country  $i$  within industry  $k$ .
- The price of these goods sold to destination  $n$  after applying the iceberg cost is

$$P_{in,k} = \tau_{in,k} p_{i,k}$$

- Utility maximization s.t. the budget constraint ( $\sum_i \sum_k P_{in,k} C_{in,k} = E_n$ ) implies that country  $n$ 's expenditure share on country  $i$  goods in industry  $k$  is

$$\lambda_{in,k}(p) = \frac{b_{i,k} (\tau_{in,k} p_{n,k})^{1-\sigma_k}}{\sum_\ell b_{\ell,k} (\tau_{\ell n,k} p_{\ell,k})^{1-\sigma_k}}$$

- $p \equiv \{p_{n,k}\}_n$  is a vector containing international prices in industry  $k$ .
- Total demand for goods originating from country  $i$  in industry  $k$ :

$$Q_{i,k}^D(p) \sim \sum_n d_{in,k} C_{in,k} = \frac{1}{p_{i,k}} \sum_n \lambda_{in,k}(p) \beta_{n,k} E_n$$

## Production and Supply

- Each firm  $\omega$  chooses a technology  $t \in \mathbb{T}$ .
- The technology choice determines the production function:

$$Q_{i,kt}(\omega) = A_{i,kt} \left( \underbrace{\frac{Z_{i,kt}(\omega)}{\gamma_{kt}}}_{\text{managerial productivity}} \right)^{\gamma_{kt}} \left( \underbrace{\frac{H_{i,kt}(\omega)}{1 - \gamma_{kt}}}_{\text{managerial capital}} \right)^{1 - \gamma_{kt}}$$

- Technologies differ in their general TFP ( $A$ ) and input intensity ( $\gamma$ )
- Analogous to span-of-control (Lucas, 1978)  $\Rightarrow$  Share of profits is  $\gamma_{kt}$

## Technology Choices

- Returns to managerial profit per cost minimization:

$$r_{i,kt}(\omega) = \underbrace{Z_{i,kt}(\omega)}_{\text{managerial}} \times \underbrace{a_{i,kt} p_{i,k}^{\frac{1}{\gamma_{kt}}} w_i^{\frac{\gamma_{kt}-1}{\gamma_{kt}}}}_{\substack{\text{productivity & prices} \\ \text{productivity}}}$$

- $h_{i,kt} \equiv a_{i,kt} p_{i,k}^{\frac{1}{\gamma_{kt}}} w_i^{\frac{\gamma_{kt}-1}{\gamma_{kt}}}$  is common across firms but  $Z$  is manager of firms-specific
- $a_{i,kt} \equiv (A_{i,kt})^{1/\gamma_{kt}}$  and  $w_i$  denotes wages (or the price of labor inputs)
- Every firm  $\omega$  chooses the technology that maximizes the managerial profit

$$\max \{ r_{i,kt}(\omega), \quad \text{for } t \in \mathbb{T} \}$$

## Technology Choices

- Assume  $Z_{i,kt}(\omega)$  is drawn from a Fréchet distribution with level parameter
  - Every firm chooses 1 technology
  - Integrate over the continuum of firms to recover the share
- The share of firms choosing technology  $t$  is

$$\alpha_{i,kt} = \left( \frac{a_{i,kt} (p_{i,k}/w_i)^{\frac{1}{\gamma_{kt}}}}{H_{i,k}} \right)^\theta, \quad \text{with} \quad H_{i,k} \equiv \left[ \sum_{t' \in \mathbb{T}} \left( a_{i,kt'} (p_{i,k}/w_i)^{\frac{1}{\gamma_{kt'}}} \right)^\theta \right]^{1/\theta}$$

## Production and Supply: Industry Aggregates

- Managerial profits constitute a fraction  $\gamma_{kt}$  of total sales  $\rightarrow$  total sales are

$$Y_{i,kt} = \frac{1}{\gamma_{kt}} \times \alpha_{i,kt} \times |\Omega_{i,k}| \times \mathbb{E}[Z_{i,kt}(\omega) \mid \omega \in \Omega_{i,kt}] \times a_{i,kt} p_{i,k}^{\frac{1}{\gamma_{kt}}} w_i^{\frac{\gamma_{kt}-1}{\gamma_{kt}}}$$

- where  $|\Omega_{i,k}| = 1$  is the measure of firms normalized to one and the average productivity of firms choosing technology  $t$  is

$$\mathbb{E}[Z_{i,kt}(\omega) \mid \omega \in \Omega_{ik,t}] = \alpha_{i,kt}^{-\frac{1}{\theta}}$$

- Industry-wide supply is the sum of technology-level supply functions,  $Q_{i,kt} = Y_{i,kt} / p_{i,k}$ :

$$Q_{i,k}^S(p_{i,k}) = \sum_t \frac{Y_{i,kt}}{p_{i,k}} = \sum_t \frac{a_{i,kt}}{\gamma_{kt}} \left( \frac{p_{i,k}}{w_i} \right)^{\frac{1-\gamma_{kt}}{\gamma_{kt}}} \alpha_{i,kt}(p_{i,k})^{\frac{\theta-1}{\theta}},$$

- the supply elasticity is  $\frac{\partial \ln Q_{i,k}^S(p,w)}{\partial \ln p_{i,k}} = \sum_t y_{i,kt} \left[ \frac{1-\gamma_{kt}}{\gamma_{kt}} + (\theta - 1) \left( \frac{1}{\gamma_{kt}} - \sum_{t'} \frac{\alpha_{i,kt'}}{\gamma_{kt'}} \right) \right]$ , where  $y_{i,kt} \equiv Y_{i,kt} / Y_{i,k}$  is the share of technology  $t$  in total output.

## General Equilibrium

For a set of parameters, equilibrium is a vector of wages  $w \equiv \{w_i\}$  & prices  $p \equiv \{p_{i,k}\}$  such that

- the *labor market clearing* condition is satisfied in each country:

$$w_i L_i = \sum_{k=1}^K \sum_{t \in \mathbb{T}} (1 - \gamma_{kt}) Y_{i,kt} (p, w).$$

- the *goods market clearing* condition is satisfied ( $Q^S = Q^D$ )

$$\underbrace{Y_{i,k} \sim \sum_{t=1}^T Y_{i,kt} (p, w)}_{p_{i,k} Q_{i,k}^S} = \underbrace{\sum_{n=1}^N \lambda_{in,k} (p) \beta_{n,k} E_n}_{p_{i,k} Q_{i,k}^D} \quad \text{with} \quad E_n = \sum_t \sum_k Y_{i,kt} (p, w)$$

## General Equilibrium

For a set of parameters, equilibrium is a vector of wages  $w \equiv \{w_i\}$  & prices  $p \equiv \{p_{i,k}\}$  such that

- the *labor market clearing* condition is satisfied in each country:

$$w_i L_i = \sum_{k=1}^K \sum_{t \in \mathbb{T}} (1 - \gamma_{kt}) Y_{i,kt} (p, w).$$

- the *goods market clearing* condition is satisfied ( $Q^S = Q^D$ )

$$Y_{i,k} \sim \sum_{t=1}^T Y_{i,kt} (p, w) = \sum_{n=1}^N \lambda_{in,k} (p) \beta_{n,k} E_n \quad \text{with} \quad E_n = \sum_t \sum_k Y_{i,kt} (p, w)$$

- where:

$$Y_{i,kt} (p, w) = \frac{a_{i,kt}}{\gamma_{kt}} \times \alpha_{i,kt} (p, w)^{\frac{\theta-1}{\theta}} \times p_{i,k}^{\frac{1}{\gamma_{kt}}} w_i^{\frac{\gamma_{kt}-1}{\gamma_{kt}}}$$

$$\alpha_{i,kt} (p, w) = \frac{\left( a_{i,kt} (p_{i,k}/w_i)^{\frac{1}{\gamma_{kt}}} \right)^\theta}{\sum_{t' \in \mathbb{T}} \left( a_{i,kt'} (p_{i,k}/w_i)^{\frac{1}{\gamma_{kt'}}} \right)^\theta}$$

$$\lambda_{in,k} (p) = \frac{b_{i,k} (\tau_{in,k} p_{i,k})^{1-\sigma_k}}{\sum_\ell b_{\ell,k} (\tau_{\ell n,k} p_{\ell,k})^{1-\sigma_k}}$$

## Performing Counterfactuals using Exact Hat-Algebra

- The welfare change in response to an arbitrary trade cost shock  $\{\hat{\tau}_{in,k}\}_{i,n}$ :

$$\hat{W}_i = \frac{\hat{E}_i}{\hat{P}_i} \quad \text{with} \quad \hat{P}_i = \prod_{k=1}^K \left[ \sum_{n=1}^N \lambda_{ni,k} (\hat{\tau}_{ni,k} \hat{p}_{n,k})^{1-\sigma_k} \right]^{\frac{\beta_{i,k}}{1-\sigma_k}}$$

- $\hat{E}_i$  and  $\hat{p}_{n,k}$  can be calculated given baseline data  $\{\alpha_{i,kt}, \lambda_{in,k}, \beta_{i,k}, \gamma_{i,kt}, E_i\}$  via the following system of equations ( $Y_{n,kt} = \frac{\alpha_{n,kt}/\gamma_{kt}}{\sum_{t'} \alpha_{n,kt'}/\gamma_{kt'}} Y_{n,k}$ , with  $Y_{n,k} = \sum \lambda_{ni,k} \beta_{i,k} E_i$ ):

$$\hat{w}_i w_i L_i = \sum_{k=1}^K \sum_{t=1}^T (1 - \gamma_{kt}) Y_{i,kt} \hat{Y}_{i,kt} \quad \hat{Y}_{i,kt} = \hat{\alpha}_{i,kt}^{\frac{\theta-1}{\theta}} \hat{p}_{i,k}^{\frac{1}{\gamma_{kt}}} \hat{w}_i^{\frac{\gamma_{kt}-1}{\gamma_{kt}}}$$

$$\sum_{t=1}^T Y_{i,kt} \hat{Y}_{i,kt} = \sum_{n=1}^N \lambda_{in,k} \hat{\lambda}_{in,k} \beta_{n,k} E_n \hat{E}_n, \quad E_n \hat{E}_n = \sum_k \sum_t Y_{n,kt} \hat{Y}_{n,kt}$$

$$\hat{\lambda}_{in,k} = \frac{(\hat{\tau}_{in,k} \hat{p}_{i,k})^{1-\sigma_k}}{\sum_\ell (\hat{\tau}_{\ell n,k} \hat{p}_{\ell,k})^{1-\sigma_k}}$$

$$\hat{\alpha}_{i,kt} = \frac{(\hat{p}_{i,k}/\hat{w}_i)^{\frac{\theta}{\gamma_{kt}}}}{\sum_{t'} \alpha_{i,kt'} (\hat{p}_{i,k}/\hat{w}_i)^{\frac{\theta}{\gamma_{kt'}}}}$$

## Application: Compiling Data on Technology Shares

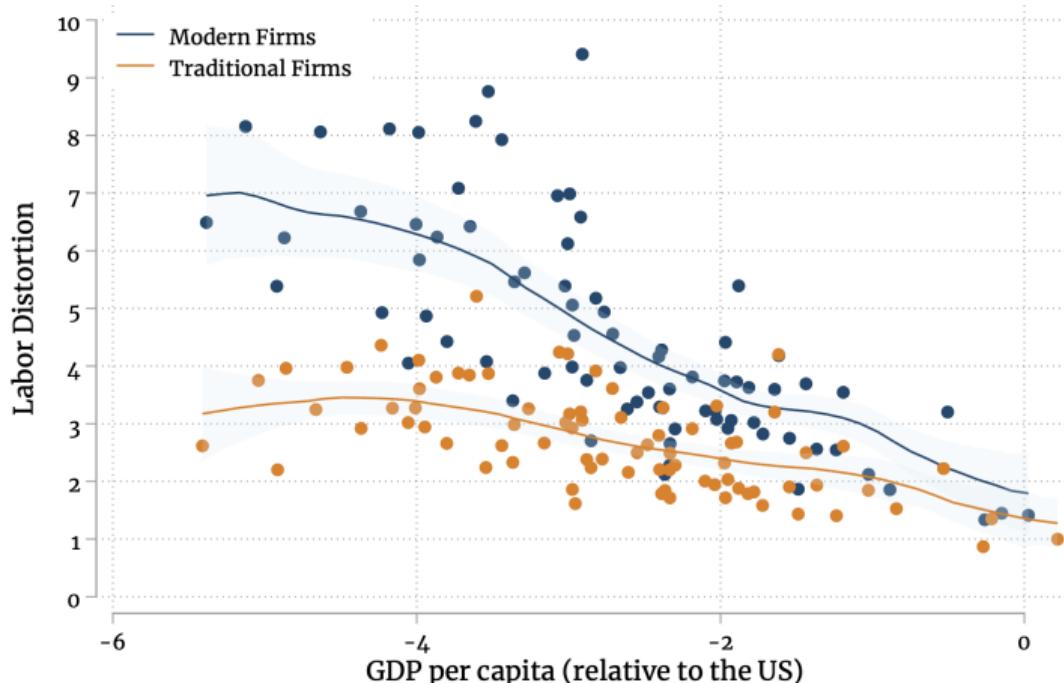
- Counterfactual simulations require data on the share  $\alpha$  of firms using various technologies.
  - technologies are characterized by two parameters: **productivity** ( $A$ ) and **factor intensity** ( $\gamma$ )
  - $(A, \gamma)$  is unobserved — technology type must be *indirectly* inferred from production/input data.

**Example** (Farrokh, Lashkaripour, Pellegrina, 2024)

- Use K-mean clustering to partition firms into two technology groups:
  1. traditional technology (low-productivity, labor intensive)
  2. modern technology (high-productivity, intensive use of traded intermediate inputs)
- The partitioning automatically determines the share  $\alpha$  of each technology type
- Technology-specific parameters ( $\gamma$  and  $A$ ) can be estimated by running a standard production function estimation on each partition of firms.

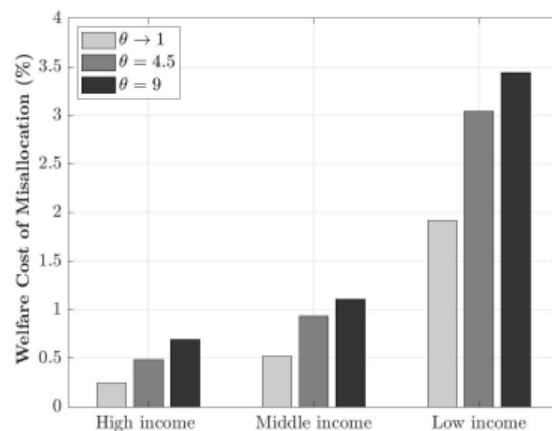
## Application: *Farrokhi, Lashkaripour, Pellegrina (2024, JIE)*

**Key Regularity:** Modern firms face more severe labor input distortions than traditional firms, with this disparity being more pronounced in low-income countries.



# Counterfactual Analysis I: Welfare Cost of Misallocation

- Labor market wedges create misallocation through:
  - Reduced adoption of modern technologies across firms (extensive margin)
  - Suboptimal resource allocation to modern firms (intensive margin)
- FLP quantify the welfare costs by simulating removal of labor input wedges across countries



- More misallocation in low-income countries due to larger gap in modern/traditional wedges
- misallocation magnifies when firms have higher technology choice flexibility (higher  $\theta$ )

# Counterfactual Analysis II: Impacts of Trade Integration

## Aggregate Welfare Effects

- Compute and decompose the welfare gains from trade under two scenarios
  1. gains from trade relative to autarky (*ex-post*)
  2. gains from piecemeal trade liberalization (*ex-ante*)
- This exercise reveals if trade integration has improved or worsened misallocation

## Labor Market Effects

- Compute the counterfactual effects of trade liberalization on *Aggregate Labor Productivity*
- This analysis can shed light on Africa's Manufacturing Puzzle ([Diao et al-2021](#))
  - Despite overall economic growth driven by trade openness, manufacturing labor productivity remains stagnant across many Sub-Saharan African nations

## Welfare Gains from Trade: Results

- Gains from Trade relative to Autarky (Ex-post)

	High income	Middle income	Low income
ACR	19.3%	18.0%	16.4%
New Model	21.3%	20.0%	19.2%

- The ACR gains describe welfare effects in a hypothetical misallocation-free economy
- Why does the new model imply larger gains:
  - trade expands access to traded intermediate inputs → increased adoption of modern technologies and reallocation towards modern firms that are intermediate-input-intensive → improvement in allocative efficiency
  - Dix Carneiro, Goldberg, Meghir, Ulyssea (2024) highlight a similar mechanism, but in the context of trade reducing the prevalence of *informality*

## Welfare Gains from Trade: Results

- Piecemeal Trade Liberalization (Ex-ante)

	ACR	Allocative Efficiency	Residual Effects
High income	90.3%	3.0%	6.7%
Middle income	86.6%	5.0%	8.4%
Low income	81.2%	9.2%	9.6%

- The logic for allocative efficiency gains is similar to what was described in the previous slide.
- These results hint that input trade liberalization can be a potentially successful form of *industrial policy* for lower income countries.
  - input tariff liberalization (e.g., tariff exemptions, duty drawback) was an integral part of Taiwan and South Korea's export-oriented industrial policy

## Structural DiD Design for Evaluating Labor Market Effects

- The goal is to quantify the effects of trade liberalization (a 20% reduction in trade costs) under the existing labor market distortions, and compare these effects to those in a hypothetical economy without such distortions:

(With Distortions :  $E_0 \rightarrow E_1$ )    versus    (Without Distortions :  $E'_0 \rightarrow E'_1$ )

		<b>Trade Barriers</b>	
		High	Low
<b>Labor</b>	High	$E_0$	$E_1$
	Low	$E'_0$	$E'_1$

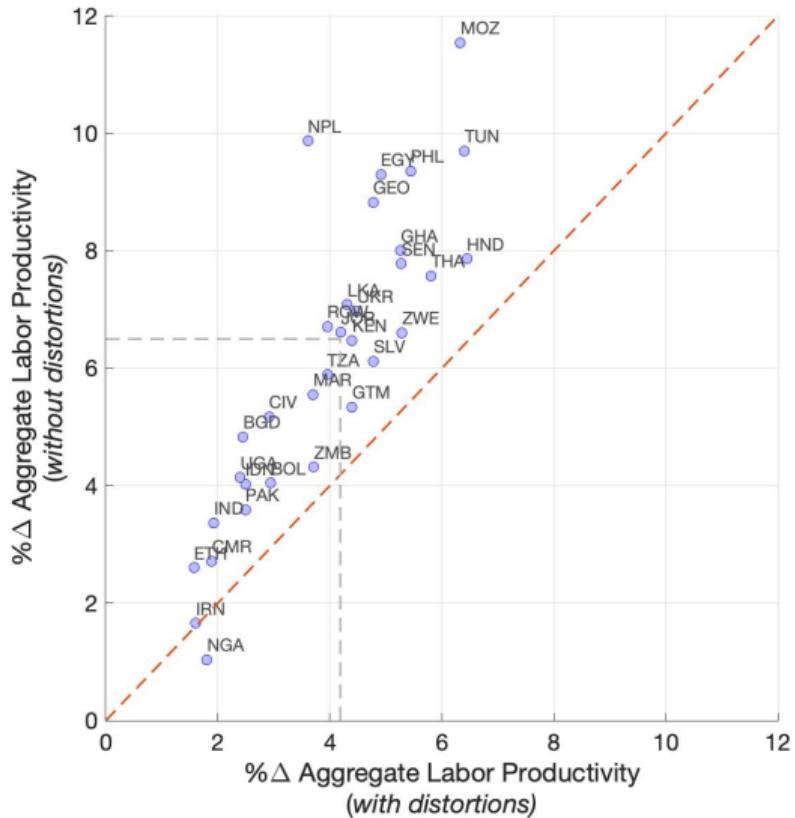
- $E_0$  represents the status quo (high trade barriers and labor wedges)
- $E_1$ ,  $E'_0$ , and  $E'_1$  represent counterfactual scenarios
- Structural *difference-in-differences*: compare  $E_0 \rightarrow E_1$  with  $E'_0 \rightarrow E'_1$

## Results: Effects of Trade Liberalization

	Trade Liberalization	
	With Distortions $(E_0 \rightarrow E_1)$	Without Distortions $(E'_0 \rightarrow E'_1)$
(a) Agg. Labor Productivity	<b>4.2%</b>	<b>6.5%</b>
(b) Real Wages	7.9%	11.3%
(c) VA per worker in Mfg	8.1%	10.6%
(d) Share of Mfg. Modern Firms	18.4%	5.4%
(e) Mfg. Employment	1.6%	-3.4%
(f) Avg. Mfg. Labor Intensity	-2.2%	-1.1%
(g) Avg. Mfg. Intrm. Input Intensity	7.5%	3.1%

- Trade liberalization spurs technological growth by encouraging modern technology adoption
- But labor market distortions dilute the link between technological growth and labor productivity

# Effects of Trade Liberalization on Aggregate Labor Productivity



- Trade increases output per worker
- **Mechanism:** trade improves access to imported intermediate inputs → directs resources toward modern technologies that are intermediate input-intensive
- However, in distorted economies, the resulting productivity gains are compromised because modern technologies are disproportionately affected by labor market distortions
- Consequently, these distortions erode 1/3 of the labor productivity gains in low-income countries