	COURSE: FORMAL METHODS		MARKS: /100
	TOPIC: Basic Sets, Propositions & Predicates	CODE: BCS 2213	
	ASSESSMENT: Tutorial 2	NO: 2	
		DURATION: 2 Hour	

STUDENT'S INFORMATION

MATRIC NO : _____

Name : _____

Instructions: Answer all the questions

- Examine the following descriptions of sets so that you understand which members they contain (Z – is a set of all integer values). Is it true that a) corresponds to c) and b) correspond to d)? Rewrite c) and d) in more strict way.
 - $\{-5, -3, -1, 1, 3, 5, \dots\}$
 - $\{0, 2, 4, 6, \dots\}$
 - $\{n \mid m \text{ is an integer and } n = 2m-1\}$
 - $\{n \mid n = 2m \text{ for some } m \text{ in } Z\}$
- Write formal description of the following sets.
 - The set containing the numbers 1, 10, 100 and 1000.
 - The set containing all natural numbers that are less than 5.
 - The set containing nothing at all.

For the question 3 and 4, consider the following sets.

$$EU = \left\{ \begin{array}{l} \text{Belgium, France, Germany, Italy, Luxemburg, Netherlands, Denmark, Greece, Ireland, UK,} \\ \text{Spain, Portugal} \end{array} \right\}$$

$$NATO = \left\{ \begin{array}{l} \text{Belgium, Canada, Denmark, France, Iceland, Italy, Luxemburg, Netherlands, Norway,} \\ \text{Portugal, UK, US, Greece, Turkey, Spain, Germany} \end{array} \right\}$$

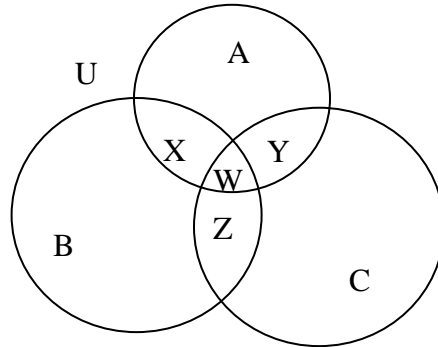
$$Scandinavia = \{Denmark, Finland, Norway, Sweden, Iceland\}$$

$$Benelux = \{Belgium, Netherlands, Luxemburg\}$$

$$CentralAmerica = \{CostaRica, Honduras, ElSavador, Guatemala, Nicaragua, Belize, Panama\}$$

- Form the following sets:
 - $Scandinavia \setminus NATO$
 - $CentralAmerica \cap Benelux$
 - $(EU \cap NATO) \cap Scandinavia$
 - $EU \cap (NATO \cap Scandinavia)$
- Supply arguments for the following rules. Illustrate the rules using sets EU, NATO and Scandinavia.
 - $A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$
 - $(A \cap B) \cup (A \setminus B) = A$

5. The diagram below is what is known as a Venn diagram. Use the letters on the diagram to describe the area corresponding to the following
- $A \cap (B \cup C)$
 - $(A \cap B) \cup (A \cap C)$
 - $(A \cup B) \setminus C$
 - $(A \setminus C) \cup (B \setminus C)$



6. Let X be the set $\{1,2,3,4,5\}$ and Y be the set $\{6,7,8,9,10\}$. The unary function $f : X \rightarrow Y$ and the binary function $g : X \times Y \rightarrow Y$ are described as following tables.

n	$F(n)$
1	6
2	7
3	6
4	7
5	6

g	6	7	8	9	10
1	10	10	10	10	10
2	7	8	9	10	6
3	7	7	8	8	9
4	9	8	7	6	10
5	6	6	6	6	6

- What are value of $f(2)$?
 - What is the range of f ?
 - What is the range of g ?
 - What is the value of $g(2,10)$?
 - What is the value of $g(4, f(4))$?
7. Show that $p \Leftrightarrow q$ is equivalent to $(p \Rightarrow q) \wedge (q \Rightarrow p)$
8. Show that $\neg p \vee (p \wedge q) \Leftrightarrow \neg p \vee q$

9. How do you interpret the two sentences below, and how would you write them using the logical symbols.

- If it's a sunny day then we will go for a picnic
- If you work hard you will pass your examinations