CHAPTER 1

SOLUTIONS

2 CHAPTER solutions

CHAPTER 1

Exercise 1.1

(a) Biologists study cells at many levels. The cells are built from organelles such as the mitochondria, ribosomes, and chloroplasts. Organelles are built of macromolecules such as proteins, lipids, nucleic acids, and carbohydrates. These biochemical macromolecules are built simpler molecules such as carbon chains and amino acids. When studying at one of these levels of abstraction, biologists are usually interested in the levels above and below: what the structures at that level are used to build, and how the structures themselves are built.

(b) The fundamental building blocks of chemistry are electrons, protons, and neutrons (physicists are interested in how the protons and neutrons are built). These blocks combine to form atoms. Atoms combine to form molecules. For example, when chemists study molecules, they can abstract away the lower levels of detail so that they can describe the general properties of a molecule such as benzene without having to calculate the motion of the individual electrons in the molecule.

Exercise 1.3

Ben can use a hierarchy to design the house. First, he can decide how many bedrooms, bathrooms, kitchens, and other rooms he would like. He can then jump up a level of hierarchy to decide the overall layout and dimensions of the house. At the top-level of the hierarchy, he material he would like to use, what kind of roof, etc. He can then jump to an even lower level of hierarchy to decide the specific layout of each room, where he would like to place the doors, windows, etc. He can use the principle of regularity in planning the framing of the house. By using the same type of material, he can scale the framing depending on the dimensions of each room. He can also use regularity to choose the same (or a small set of) doors and windows for each room. That way, when he places

a new door or window he need not redesign the size, material, layout specifica-
tions from scratch. This is also an example of modularity: once he has designed
the specifications for the windows in one room, for example, he need not re-
specify them when he uses the same windows in another room. This will save
him both design time and, thus, money. He could also save by buying some
items (like windows) in bulk.

Exercise 1.5

(a) The hour hand can be resolved to $12 * 4 = 48$ positions, which represents
$\log_2 48 = 5.58$ bits of information. (b) Knowing whether it is before or after noon
adds one more bit.

Exercise 1.7

$2^{16} = 65,536$ numbers.

Exercise 1.9

(a) $2^{16}-1 = 65535$; (b) $2^{15}-1 = 32767$; (c) $2^{15}-1 = 32767$

Exercise 1.11

(a) 0; (b) $-2^{15} = -32768$; (c) $-(2^{15}-1) = -32767$

Exercise 1.13

(a) 10; (b) 54; (c) 240; (d) 6311

Exercise 1.15

(a) A; (b) 36; (c) F0; (d) 18A7

Exercise 1.17

(a) 165; (b) 59; (c) 65535; (d) 3489660928

Exercise 1.19

(a) 10100101; (b) 00111011; (c) 1111111111111111;
(d) 11010000000000000000000000000000

Exercise 1.21

(a) -6; (b) -10; (c) 112; (d) -97

Exercise 1.23

(a) -2; (b) -22; (c) 112; (d) -31

Exercise 1.25

(a) 101010; (b) 111111; (c) 11100101; (d) 1101001101

Exercise 1.27

(a) 2A; (b) 3F; (c) E5; (d) 34D

Exercise 1.29

(a) 00101010; (b) 11000001; (c) 01111100; (d) 10000000; (e) overflow

Exercise 1.31

00101010; (b) 10111111; (c) 01111100; (d) overflow; (e) overflow

Exercise 1.33

(a) 00000101; (b) 11111010

Exercise 1.35

(a) 00000101; (b) 00001010

Exercise 1.37

(a) 52; (b) 77; (c) 345; (d) 1515

Exercise 1.39

(a) 100010_2, 22_{16}, 34_{10}; (b) 110011_2, 33_{16}, 51_{10}; (c) 010101101_2, AD_{16}, 173_{10}; (d) 011000100111_2, 627_{16}, 1575_{10}

Exercise 1.41

15 greater than 0, 16 less than 0; 15 greater and 15 less for sign/magnitude

Exercise 1.43

4, 8

Exercise 1.45

5,760,000

EExercise 1.47

46.566 gigabytes

Exercise 1.49

128 kbits

Exercise 1.51

	-2	-1	0	1	2	3	
Unsigned			00	01	10	11	
	10	11	00	01			Two's Complement
		11	00 10	01			Sign/Magnitude

Exercise 1.53

(a) 11011101; (b) 110001000 (overflows)

Exercise 1.55

(a) 11011101; (b) 110001000

Exercise 1.57

(a) 000111 + 001101 = 010100
(b) 010001 + 011001 = 101010, overflow
(c) 100110 + 001000 = 101110

(d) $011111 + 110010 = 010001$
(e) $101101 + 101010 = 010111$, overflow
(f) $111110 + 100011 = 100001$

Exercise 1.59

(a) 0x2A; (b) 0x9F; (c) 0xFE; (d) 0x66, overflow

Exercise 1.61

(a) $010010 + 110100 = 000110$; (b) $011110 + 110111 = 010101$; (c) $100100 + 111101 = 100001$; (d) $110000 + 101011 = 011011$, overflow

Exercise 1.63

Biased
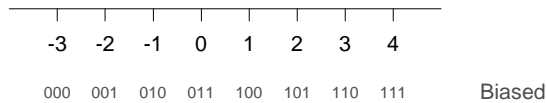
Exercise 1.65

(a) 0011 0111 0001
(b) 187
(c) $95 = 1011111$
(d) Addition of BCD numbers doesn't work directly. Also, the representation doesn't maximize the amount of information that can be stored; for example 2 BCD digits requires 8 bits and can store up to 100 values (0-99) - unsigned 8-bit binary can store 28 (256) values.

Exercise 1.67

Both of them are full of it. $42_{10} = 101010_2$, which has 3 1's in its representation.

Exercise 1.69

```
#include <stdio.h>

void main(void)
{
  char bin[80];
  int i = 0, dec = 0;

  printf("Enter binary number: ");
  scanf("%s", bin);
```
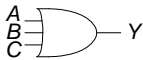
```
while (bin[i] != 0) {
   if (bin[i] == '0') dec = dec * 2;
   else if (bin[i] == '1') dec = dec * 2 + 1;
   else printf("Bad character %c in the number.\n", bin[i]);
   i = i + 1;
}
printf("The decimal equivalent is %d\n", dec);
```
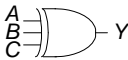
Exercise 1.71

OR3

$$Y = A+B+C$$

A	B	C	Y
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	1
1	1	0	1
1	1	1	1

(a)

XOR3
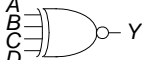
$$Y = A \oplus B \oplus C$$

A	B	C	Y
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1

(b)

XNOR4

$$Y = \overline{A \oplus B \oplus C \oplus D}$$

A	C	B	D	Y
0	0	0	0	1
0	0	0	1	0
0	0	1	0	0
0	0	1	1	1
0	1	0	0	0
0	1	0	1	1
0	1	1	0	1
0	1	1	1	0
1	0	0	0	0
1	0	0	1	1
1	0	1	0	1
1	0	1	1	0
1	1	0	0	1
1	1	0	1	0
1	1	1	0	0
1	1	1	1	1

(c)

Exercise 1.73

A	B	C	Y
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1

Exercise 1.75

A	B	C	Y
0	0	0	1
0	0	1	1
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	0

Exercise 1.77

$$2^{2^N}$$

Exercise 1.79

No, there is no legal set of logic levels. The slope of the transfer characteristic never is better than -1, so the system never has any gain to compensate for noise.
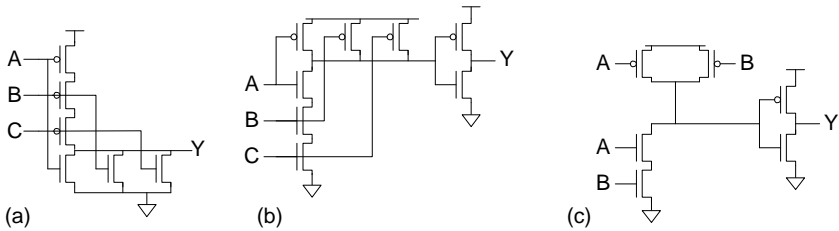
Exercise 1.81

The circuit functions as a buffer with logic levels $V_{IL} = 1.5$; $V_{IH} = 1.8$; $V_{OL} = 1.2$; $V_{OH} = 3.0$. It can receive inputs from LVCMOS and LVTTL gates because their output logic levels are compatible with this gate's input levels. However, it cannot drive LVCMOS or LVTTL gates because the 1.2 V_{OL} exceeds the V_{IL} of LVCMOS and LVTTL.

Exercise 1.83

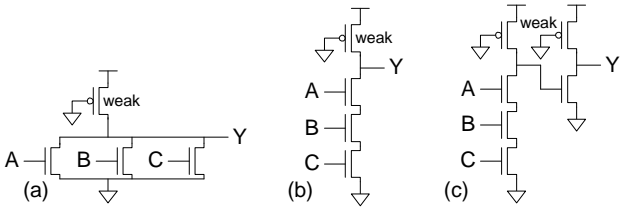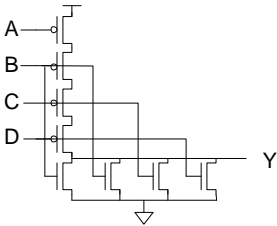(a) XOR gate; (b) $V_{IL} = 1.25$; $V_{IH} = 2$; $V_{OL} = 0$; $V_{OH} = 3$

Exercise 1.85

(a)   (b)   (c)

Exercise 1.87

XOR

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	0

Exercise 1.89

(a)   (b)   (c)

Question 1.1

Question 1.3

17 minutes: (1) designer and freshman cross (2 minutes); (2) freshman returns (1 minute); (3) professor and TA cross (10 minutes); (4) designer returns (2 minutes); (5) designer and freshman cross (2 minutes).

CHAPTER 2

Exercise 2.1

(a) $Y = \overline{A}\,\overline{B} + A\overline{B} + AB$

(b) $Y = \overline{A}\,\overline{B}\,\overline{C} + ABC$

(c) $Y = \overline{A}\,\overline{B}\,\overline{C} + \overline{A}\,B\,\overline{C} + A\overline{B}\,\overline{C} + AB\overline{C} + ABC$

(d)

$Y = \overline{A}\,\overline{B}\,\overline{C}\,\overline{D} + \overline{A}\,\overline{B}\,C\,\overline{D} + \overline{A}\,B\,\overline{C}\,D + A\overline{B}\,\overline{C}\,D + A\overline{B}\,\overline{C}\,\overline{D} + AB\overline{C}\,\overline{D} + ABC\overline{D}$

(e)

$Y = \overline{A}\,\overline{B}\,\overline{C}\,\overline{D} + \overline{A}\,\overline{B}\,CD + \overline{A}\,B\,\overline{C}\,D + \overline{A}\,BCD + A\overline{B}\,\overline{C}\,D + A\overline{B}\,C\,\overline{D} + AB\overline{C}\,D + ABCD$

Exercise 2.3

(a) $Y = (A + \overline{B})$

(b)

$Y = (A + B + \overline{C})(A + \overline{B} + C)(A + \overline{B} + \overline{C})(\overline{A} + B + C)(\overline{A} + B + \overline{C})(\overline{A} + \overline{B} + C)$

(c) $Y = (A + B + \overline{C})(A + \overline{B} + \overline{C})(\overline{A} + \overline{B} + C)$

(d)

$Y = (A + \overline{B} + C + D)(A + \overline{B} + C + \overline{D})(A + \overline{B} + \overline{C} + D)(A + \overline{B} + \overline{C} + \overline{D})(\overline{A} + B + C + \overline{D})$
$(\overline{A} + B + \overline{C} + \overline{D})(\overline{A} + \overline{B} + C + D)(\overline{A} + \overline{B} + C + \overline{D})(\overline{A} + \overline{B} + \overline{C} + \overline{D})$

(e)

$Y = (A + B + C + \overline{D})(A + B + \overline{C} + \overline{D})(A + \overline{B} + C + D)(A + \overline{B} + \overline{C} + \overline{D})(\overline{A} + B + C + D)$
$(\overline{A} + B + \overline{C} + \overline{D})(\overline{A} + \overline{B} + C + \overline{D})(\overline{A} + \overline{B} + \overline{C} + D)$

Exercise 2.5

(a) $Y = A + \overline{B}$

(b) $Y = \overline{A}\,\overline{B}\,\overline{C} + ABC$

(c) $Y = \overline{A}\,\overline{C} + A\overline{B} + AC$

(d) $Y = \overline{A}\,\overline{B} + \overline{B}\,\overline{D} + AC\overline{D}$

(e)

$Y = \overline{A}\,\overline{B}\,\overline{C}\,\overline{D} + \overline{A}\,\overline{B}CD + \overline{A}B\overline{C}D + \overline{A}BC\overline{D} + A\overline{B}\,\overline{C}D + A\overline{B}C\overline{D} + AB\overline{C}\,\overline{D} + ABCD$

This can also be expressed as:

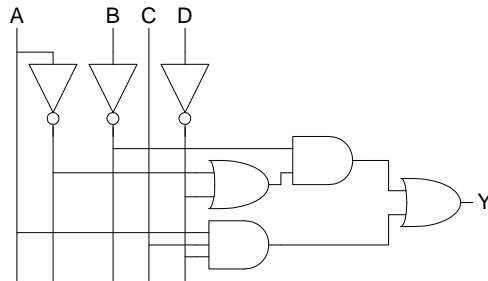$Y = \overline{(A \oplus B)}\,\overline{(C \oplus D)} + (A \oplus B)(C \oplus D)$
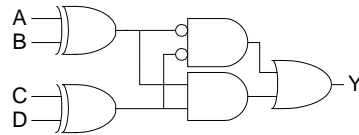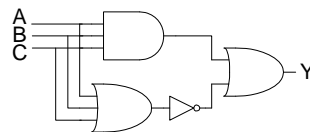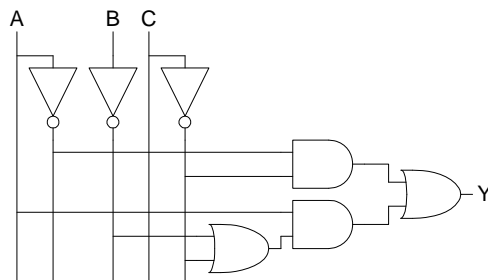
Exercise 2.7

(a)
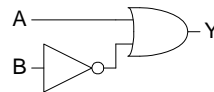
(b)
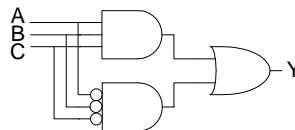
(c)
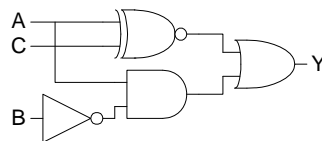
(d)

(e)

Exercise 2.9

(a) Same as 2.7(a)
(b)

(c)

(d)

(e)

Exercise 2.11

(a)
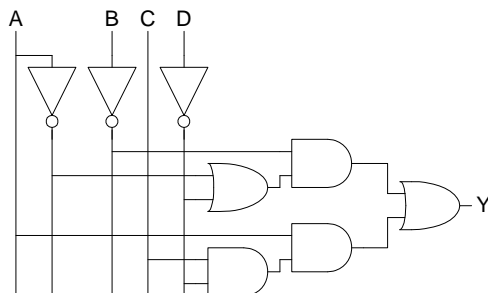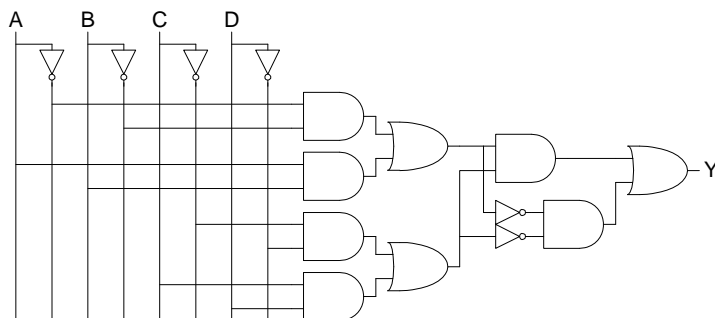

(b)
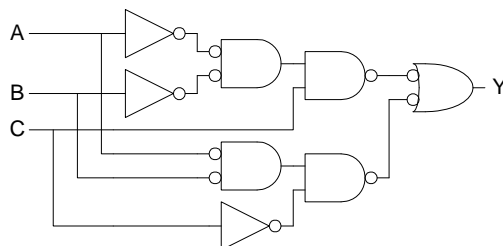
(c)

(d)

(e)

Exercise 2.13

(a) $Y = AC + \overline{B}C$
(b) $Y = \overline{A}$
(c) $Y = \overline{A} + \overline{B}\,\overline{C} + \overline{B}\,\overline{D} + BD$

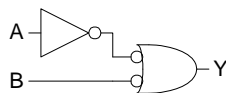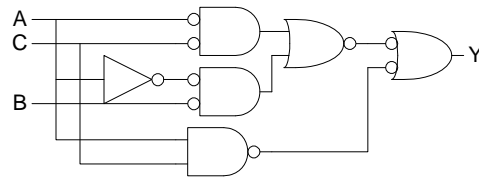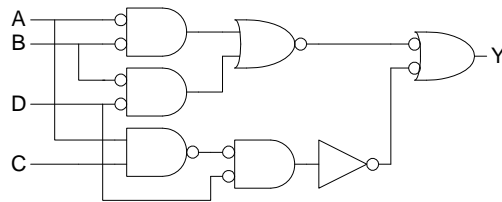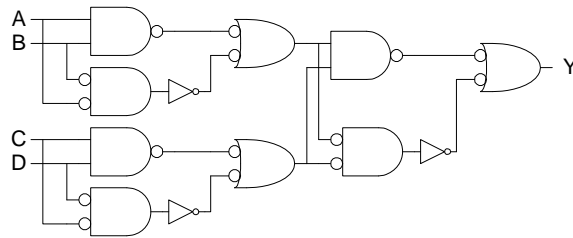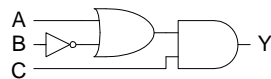## Exercise 2.15

(a)

(b)
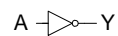
(c)
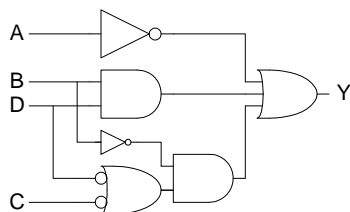
Exercise 2.17

(a) $Y = B + \overline{A}\,\overline{C}$

(b) $Y = \overline{A}B$
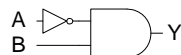
(c) $Y = A + \overline{B}\,\overline{C} + \overline{D}\,\overline{E}$
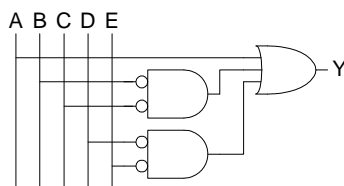
Exercise 2.19

4 gigarows = 4 x 2^{30} rows = 2^{32} rows, so the truth table has 32 inputs.

Exercise 2.21

Ben is correct. For example, the following function, shown as a K-map, has two possible minimal sum-of-products expressions. Thus, although $A\overline{C}\overline{D}$ and $\overline{B}\overline{C}\overline{D}$ are both prime implicants, the minimal sum-of-products expression does not have both of them.

$$Y = \overline{A}\overline{B}\overline{D} + AB\overline{C} + A\overline{C}\overline{D}$$

$$Y = \overline{A}\overline{B}\overline{D} + AB\overline{C} + \overline{B}\overline{C}\overline{D}$$
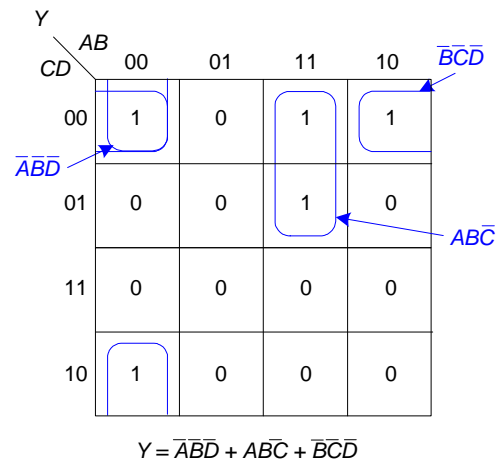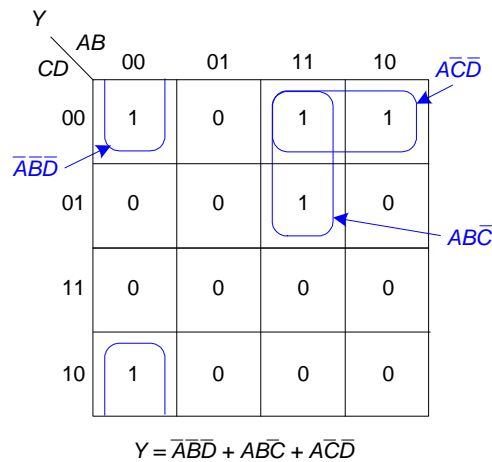
Exercise 2.23

B_2	B_1	B_0	$\overline{B_2 \bullet B_1 \bullet B_0}$	$\overline{B}_2 + \overline{B}_1 + \overline{B}_0$
0	0	0	1	1
0	0	1	1	1
0	1	0	1	1
0	1	1	1	1
1	0	0	1	1
1	0	1	1	1
1	1	0	1	1
1	1	1	0	0

Exercise 2.25

$$Y = A\bar{B}C + D$$

$$Z = A\bar{C}D + BD$$
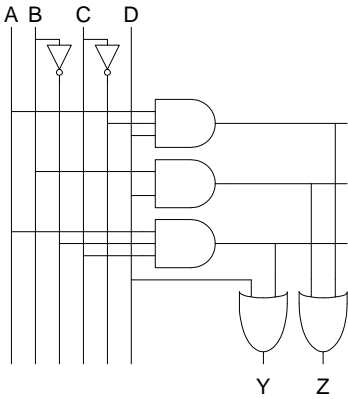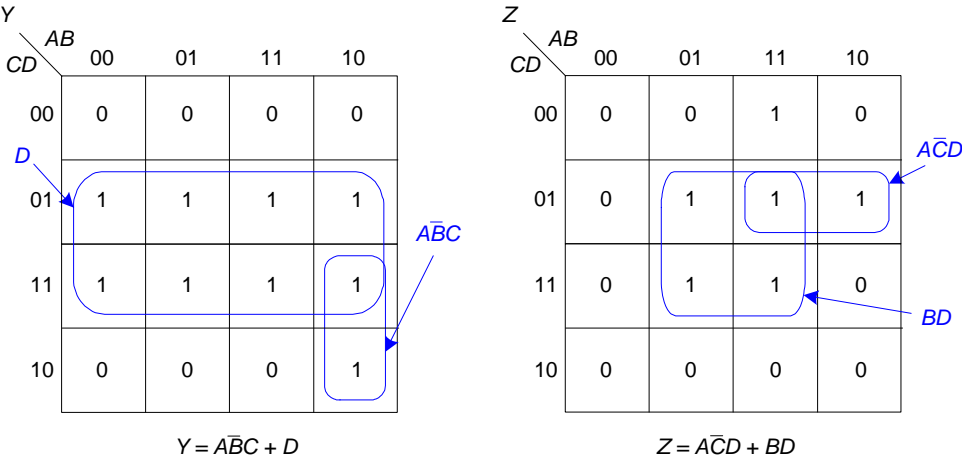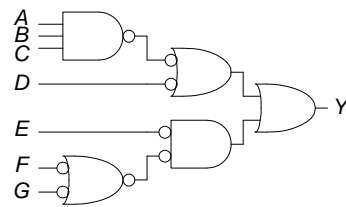
Exercise 2.27

$$Y = ABC + \overline{D} + (\overline{F} + \overline{G})\overline{E}$$
$$= ABC + \overline{D} + \overline{E}\,\overline{F} + \overline{E}\,\overline{G}$$

Exercise 2.29

Two possible options are shown below:

(a)   (b)
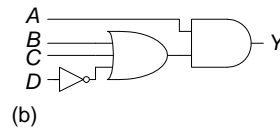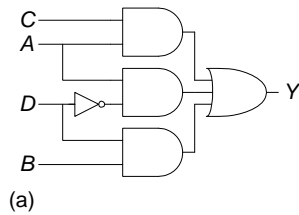
Exercise 2.31

$$Y = \overline{A}D + A\overline{B}\,\overline{C}\,\overline{D} + BD + CD = A\overline{B}\,\overline{C}\,\overline{D} + D(\overline{A} + B + C)$$

Exercise 2.33

The equation can be written directly from the description:

$$E = S\overline{A} + AL + H$$

Exercise 2.35

Decimal Value	A_3	A_2	A_1	A_0	D	P
0	0	0	0	0	0	0
1	0	0	0	1	0	0
2	0	0	1	0	0	1
3	0	0	1	1	1	1
4	0	1	0	0	0	0
5	0	1	0	1	0	1
6	0	1	1	0	1	0
7	0	1	1	1	0	1
8	1	0	0	0	0	0
9	1	0	0	1	1	0
10	1	0	1	0	0	0
11	1	0	1	1	0	1
12	1	1	0	0	1	0
13	1	1	0	1	0	1
14	1	1	1	0	0	0
15	1	1	1	1	1	0

P has two possible minimal solutions:

$$D = \bar{A_3}\bar{A_2}A_1A_0 + \bar{A_3}A_2A_1\bar{A_0} + A_3\bar{A_2}\bar{A_1}A_0$$
$$+ A_3A_2\bar{A_1}\bar{A_0} + A_3A_2A_1A_0$$

$$P = \bar{A_3}\bar{A_2}A_0 + \bar{A_3}A_1A_0 + \bar{A_3}\bar{A_2}A_1$$
$$+ \bar{A_2}A_1A_0$$
$$P = \bar{A_3}A_1A_0 + \bar{A_3}\bar{A_2}A_1 + \bar{A_2}A_1A_0$$
$$+ A_2\bar{A_1}A_0$$

Hardware implementations are below (implementing the first minimal equation given for *P*).
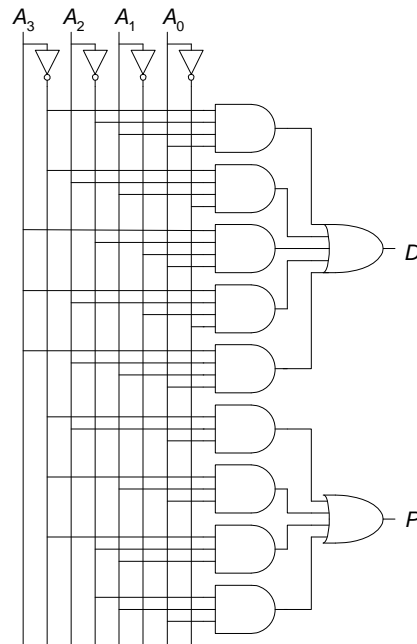
Exercise 2.37

The equations and circuit for $Y_{2:0}$ is the same as in Exercise 2.25, repeated here for convenience.

A_7	A_6	A_5	A_4	A_3	A_2	A_1	A_0	Y_2	Y_1	Y_0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	1	0	0	0
0	0	0	0	0	0	1	X	0	0	1
0	0	0	0	0	1	X	X	0	1	0
0	0	0	0	1	X	X	X	0	1	1
0	0	0	1	X	X	X	X	1	0	0
0	0	1	X	X	X	X	X	1	0	1
0	1	X	X	X	X	X	X	1	1	0
1	X	X	X	X	X	X	X	1	1	1

$$Y_2 = A_7 + A_6 + A_5 + A_4$$

$$Y_1 = A_7 + A_6 + \overline{A_5}\,\overline{A_4}A_3 + \overline{A_5}\,\overline{A_4}A_2$$

$$Y_0 = A_7 + \overline{A_6}A_5 + \overline{A_6}\,\overline{A_4}A_3 + \overline{A_6}\,\overline{A_4}\,\overline{A_2}A_1$$
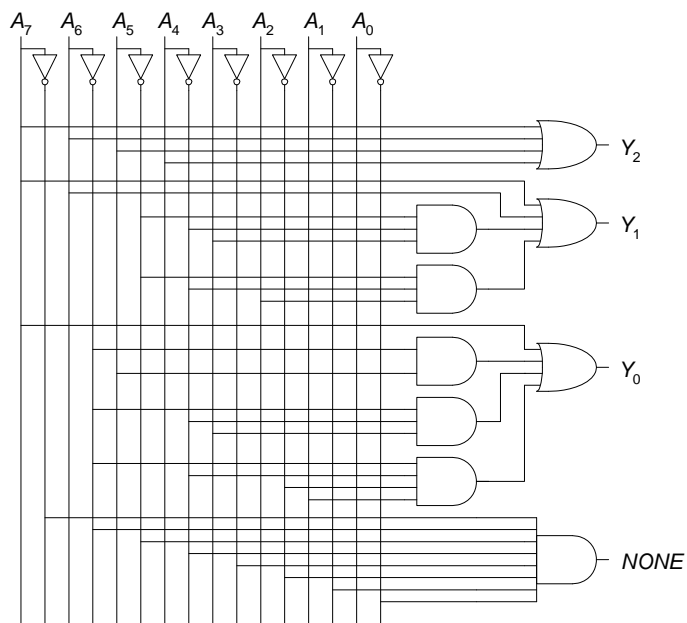
The truth table, equations, and circuit for $Z_{2:0}$ are as follows.

A_7	A_6	A_5	A_4	A_3	A_2	A_1	A_0	Z_2	Z_1	Z_0
0	0	0	0	0	0	1	1	0	0	0
0	0	0	0	0	1	0	1	0	0	0
0	0	0	0	1	0	0	1	0	0	0
0	0	0	1	0	0	0	1	0	0	0
0	0	1	0	0	0	0	1	0	0	0
0	1	0	0	0	0	0	1	0	0	0
1	0	0	0	0	0	0	1	0	0	0
0	0	0	0	0	1	1	X	0	0	1
0	0	0	0	1	0	1	X	0	0	1
0	0	0	1	0	0	1	X	0	0	1
0	0	1	0	0	0	1	X	0	0	1
0	1	0	0	0	0	1	X	0	0	1
1	0	0	0	0	0	1	X	0	0	1
0	0	0	0	1	1	X	X	0	1	0
0	0	0	1	0	1	X	X	0	1	0
0	0	1	0	0	1	X	X	0	1	0
0	1	0	0	0	1	X	X	0	1	0
1	0	0	0	0	1	X	X	0	1	0
0	0	0	1	1	X	X	X	0	1	1
0	0	1	0	1	X	X	X	0	1	1
0	1	0	0	1	X	X	X	0	1	1
1	0	0	0	1	X	X	X	0	1	1
0	0	1	1	X	X	X	X	1	0	0
0	1	0	1	X	X	X	X	1	0	0
1	0	0	1	X	X	X	X	1	0	0
0	1	1	X	X	X	X	X	1	0	1
1	0	1	X	X	X	X	X	1	0	1
1	1	X	X	X	X	X	X	1	1	0

$$Z_2 = A_4(A_5 + A_6 + A_7) + A_5(A_6 + A_7) + A_6 A_7$$

$$Z_1 = A_2(A_3 + A_4 + A_5 + A_6 + A_7) +$$
$$A_3(A_4 + A_5 + A_6 + A_7) + A_6 A_7$$

$$Z_0 = A_1(A_2 + A_3 + A_4 + A_5 + A_6 + A_7) +$$
$$A_3(A_4 + A_5 + A_6 + A_7) + A_5(A_6 + A_7)$$
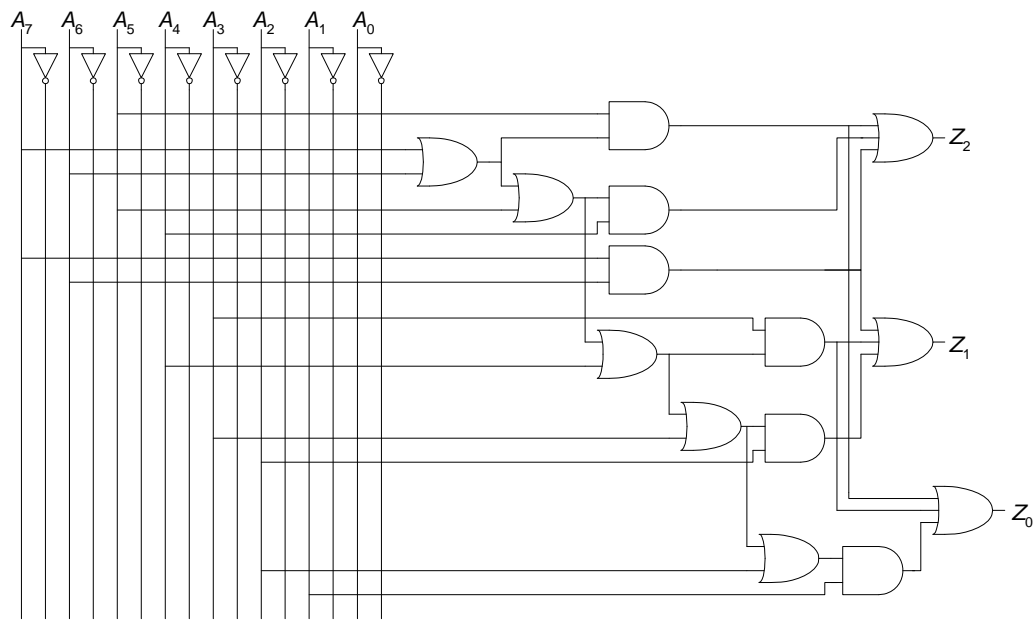
Exercise 2.39

$$Y = A + \overline{C \oplus D} = A + CD + \overline{C}\,\overline{D}$$

Exercise 2.41

A	B	C	Y
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1

(a)

A B C

- 000
- 001
- 010
- 011
- 100
- 101
- 110
- 111

Y

(b)

A	B	Y
0	0	$\overline{C}$
0	1	0
1	0	0
1	1	C

A B

C — 00
01
10
11

Y

A	Y
0	$\overline{BC}$
1	BC

B
C

A

0
1

Y

(c)

Exercise 2.43

$t_{pd} = 3t_{pd_NAND2} = $ **60 ps**
$t_{cd} = t_{cd_NAND2} = $ **15 ps**

Exercise 2.45

$t_{pd} = t_{pd\_NOT} + t_{pd\_AND3}$
$\quad = 15 \text{ ps} + 40 \text{ ps}$
$\quad = $ **55 ps**
$t_{cd} = t_{cd\_AND3}$
$\quad = $ **30 ps**
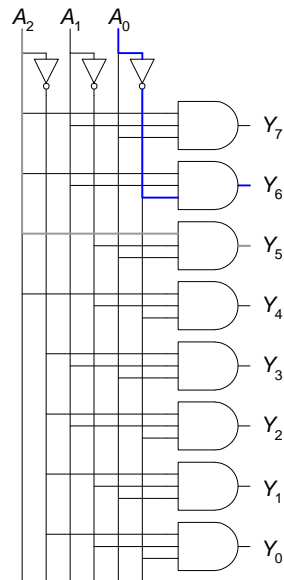
Exercise 2.47
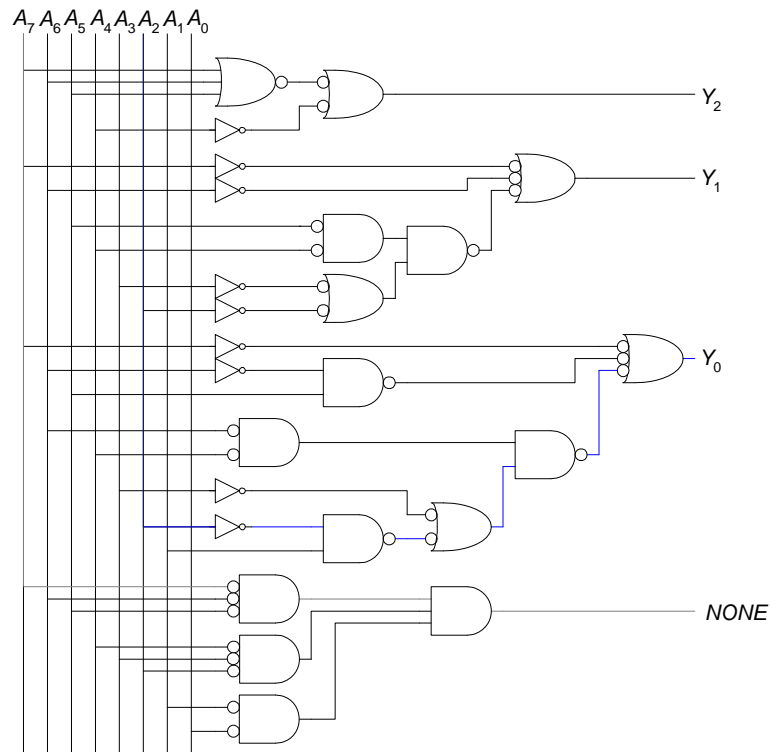
$$t_{pd} = t_{pd\_\text{INV}} + 3t_{pd\_\text{NAND2}} + t_{pd\_\text{NAND3}}$$
$$= [15 + 3\,(20) + 30]\text{ ps}$$
$$= \textbf{105 ps}$$
$$t_{cd} = t_{cd\_\text{NOT}} + t_{cd\_\text{NAND2}}$$
$$= [10 + 15]\text{ ps}$$
$$= \textbf{25 ps}$$
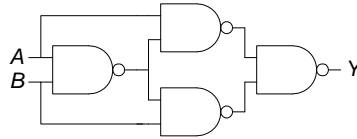
Question 2.1

Question 2.3

A tristate buffer has two inputs and three possible outputs: 0, 1, and Z. One of the inputs is the data input and the other input is a control input, often called the *enable* input. When the enable input is 1, the tristate buffer transfers the data input to the output; otherwise, the output is high impedance, Z. Tristate buffers are used when multiple sources drive a single output at different times. One and only one tristate buffer is enabled at any given time.

Question 2.5

A circuit's contamination delay might be less than its propagation delay because the circuit may operate over a range of temperatures and supply voltages, for example, 3-3.6 V for LVCMOS (low voltage CMOS) chips. As temperature increases and voltage decreases, circuit delay increases. Also, the circuit may have different paths (critical and short paths) from the input to the output. A gate itself may have varying delays between different inputs and the output, affecting the gate's critical and short paths. For example, for a two-input NAND gate, a HIGH to LOW transition requires two nMOS transistor delays, whereas a LOW to HIGH transition requires a single pMOS transistor delay.

CHAPTER 3

Exercise 3.1
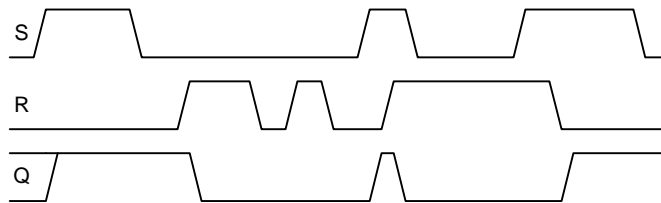
Exercise 3.3
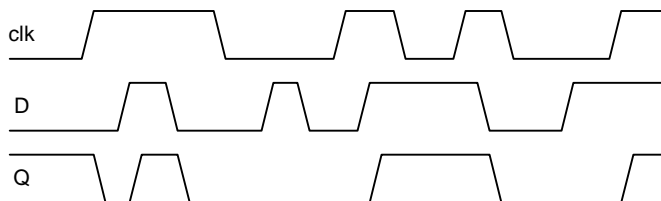
Exercise 3.5
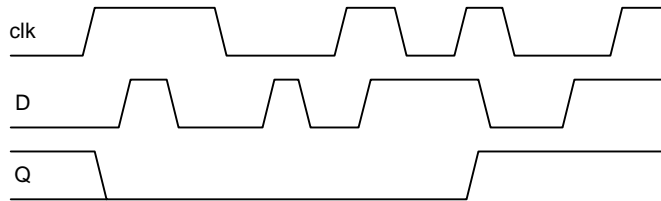
Exercise 3.7

The circuit is sequential because it involves feedback and the output depends on previous values of the inputs. This is a SR latch. When $\overline{S} = 0$ and $\overline{R} = 1$, the circuit sets Q to 1. When $\overline{S} = 1$ and $\overline{R} = 0$, the circuit resets Q to 0. When both $\overline{S}$ and $\overline{R}$ are 1, the circuit remembers the old value. And when both $\overline{S}$ and $\overline{R}$ are 0, the circuit drives both outputs to 1.

Exercise 3.9
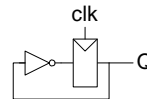
Exercise 3.11

If A and B have the same value, C takes on that value. Otherwise, C retains its old value.

Exercise 3.13
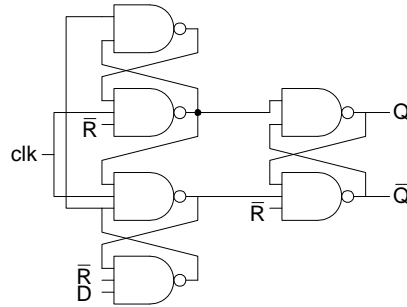
Exercise 3.15
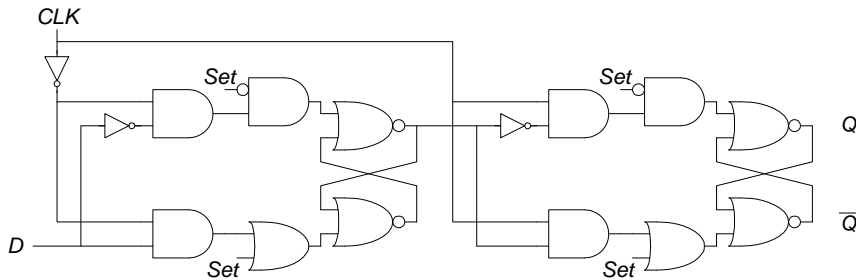
Exercise 3.17

If N is even, the circuit is stable and will not oscillate.

Exercise 3.19

The system has at least five bits of state to represent the 24 floors that the elevator might be on.

Exercise 3.21

The FSM could be factored into four independent state machines, one for each student. Each of these machines has five states and requires 3 bits, so at least 12 bits of state are required for the factored design.

Exercise 3.23

This finite state machine asserts the output Q when A AND B is TRUE.

state	encoding $s_{1:0}$
S0	00
S1	01
S2	10

TABLE 3.1 State encoding for Exercise 3.23

current state		inputs		next state		output
s_1	s_0	a	b	s'_1	s'_0	q
0	0	0	X	0	0	0
0	0	1	X	0	1	0
0	1	X	0	0	0	0
0	1	X	1	1	0	0
1	0	1	1	1	0	1
1	0	0	0	0	0	0
1	0	0	1	0	0	0
1	0	1	0	0	0	0

TABLE 3.2 Combined state transition and output table with binary encodings for Exercise 3.23

$$S'_1 = \overline{S_1}S_0B + S_1AB$$

$$S'_0 = \overline{S_1}\,\overline{S_0}A$$

$$Q' = S_1AB$$
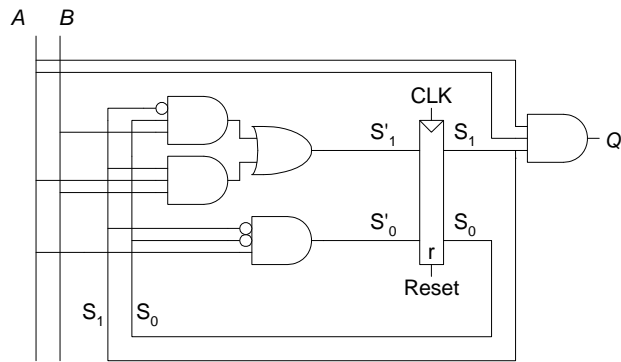
Exercise 3.25
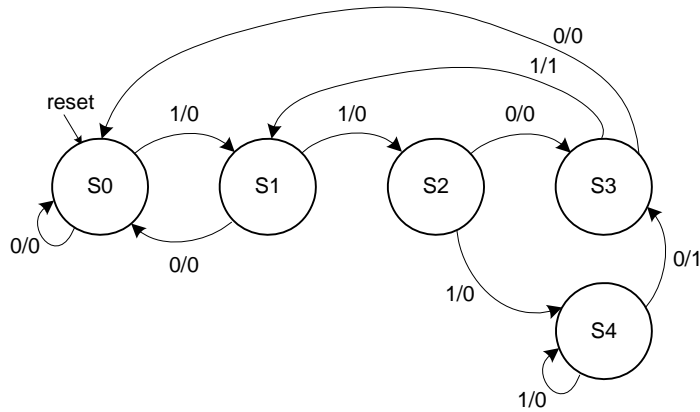
state	encoding $s_{1:0}$
S0	000
S1	001

TABLE 3.3 State encoding for Exercise 3.25

state	encoding $s_{1:0}$
S2	010
S3	100
S4	101

TABLE 3.3 State encoding for Exercise 3.25

current state			input	next state			output
s_2	s_1	s_0	a	s'_2	s'_1	s'_0	q
0	0	0	0	0	0	0	0
0	0	0	1	0	0	1	0
0	0	1	0	0	0	0	0
0	0	1	1	0	1	0	0
0	1	0	0	1	0	0	0
0	1	0	1	1	0	1	0
1	0	0	0	0	0	0	0
1	0	0	1	0	0	1	1
1	0	1	0	1	0	0	1
1	0	1	1	1	0	1	0

TABLE 3.4 Combined state transition and output table with binary encodings for Exercise 3.25

$$S'_2 = \overline{S_2}S_1\overline{S_0} + S_2\overline{S_1}S_0$$

$$S'_1 = \overline{S_2}\,\overline{S_1}S_0 A$$

$$S'_0 = A(\overline{S_2}\,\overline{S_0} + S_2\overline{S_1})$$

$$Q = S_2\overline{S_1}\,\overline{S_0}A + S_2\overline{S_1}S_0\overline{A}$$

Exercise 3.27

Reset

S000

S001

S011

S010

S110

S111

S101

S100
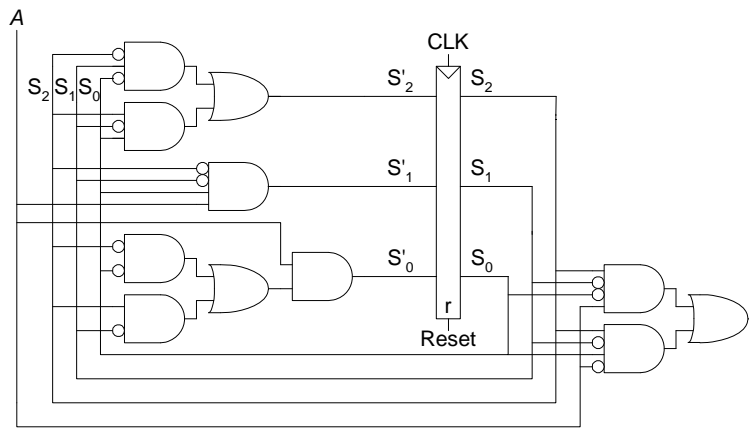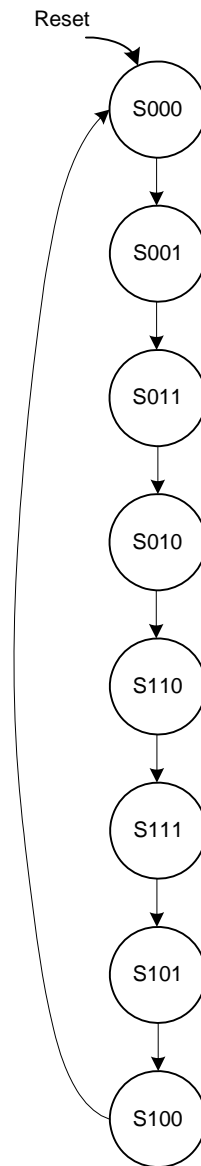
FIGURE 3.1 State transition diagram for Exercise 3.27

current state $S_{2:0}$	next state $S'_{2:0}$
000	001
001	011
011	010
010	110
110	111
111	101
101	100
100	000

TABLE 3.5 State transition table for Exercise 3.27

$$S'_2 = S_1\overline{S_0} + S_2 S_0$$

$$S'_1 = \overline{S_2}S_0 + S_1\overline{S_0}$$

$$S'_0 = \overline{S_2 \oplus S_1}$$

$$Q_2 = S_2$$

$$Q_1 = S_1$$

$$Q_0 = S_0$$
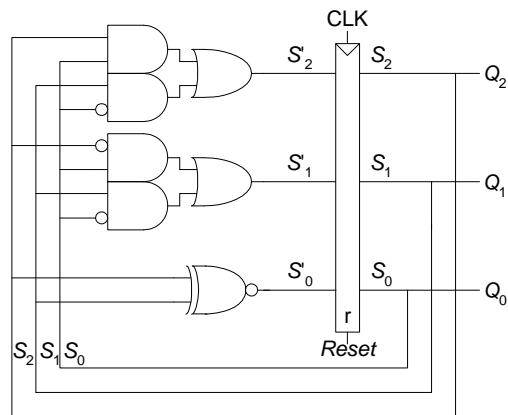
FIGURE 3.2 Hardware for Gray code counter FSM for Exercise 3.27

Exercise 3.29

(a)
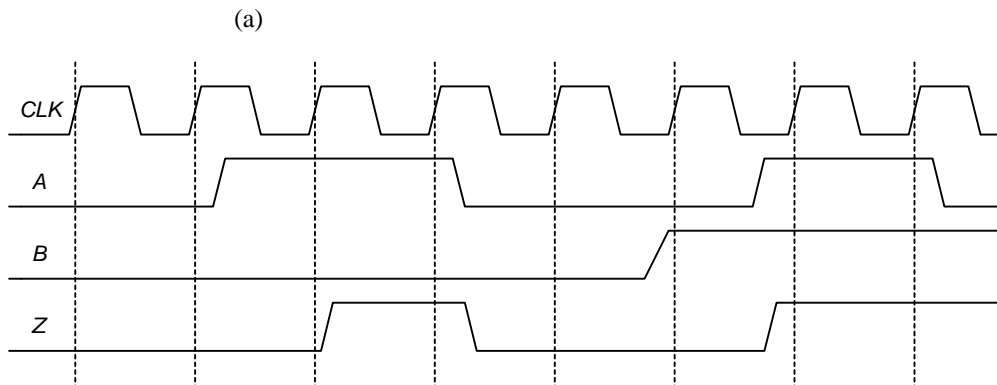
FIGURE 3.3 Waveform showing *Z* output for Exercise 3.29

(b) This FSM is a Mealy FSM because the output depends on the current value of the input as well as the current state.

(c)
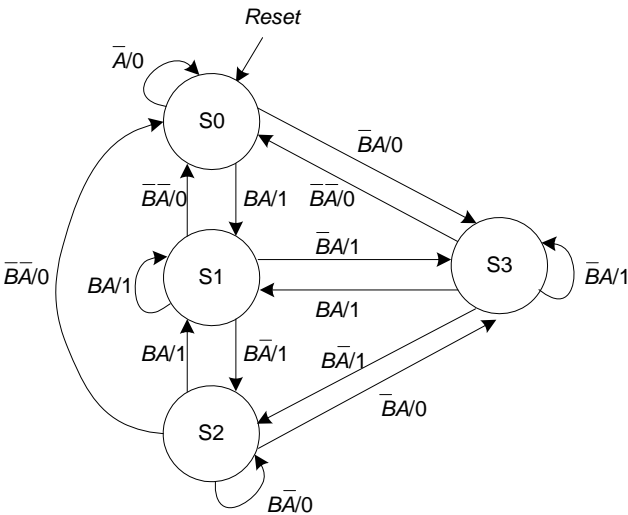
FIGURE 3.4 State transition diagram for Exercise 3.29

(Note: another viable solution would be to allow the state to transition from

S0 to S1 on $\overline{B}A/0$. The arrow from S0 to S0 would then be $\overline{B}\,\overline{A}/0$.)

current state $s_{1:0}$	inputs		next state $s'_{1:0}$	output z
	b	a		
00	X	0	00	0
00	0	1	11	0
00	1	1	01	1
01	0	0	00	0
01	0	1	11	1
01	1	0	10	1
01	1	1	01	1
10	0	X	00	0
10	1	0	10	0

TABLE 3.6 State transition table for Exercise 3.29

current state $s_{1:0}$	inputs		next state $s'_{1:0}$	output
	b	a		z
10	1	1	01	1
11	0	0	00	0
11	0	1	11	1
11	1	0	10	1
11	1	1	01	1

TABLE 3.6 State transition table for Exercise 3.29

$$S'_1 = \overline{B}A(\overline{S_1} + S_0) + B\overline{A}(S_1 + \overline{S_0})$$

$$S'_0 = A(\overline{S_1} + S_0 + B)$$

$$Z = BA + S_0(A + B)$$
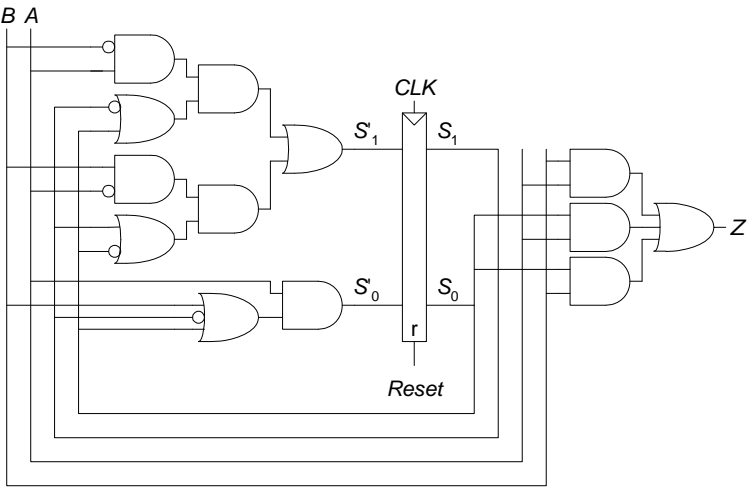
FIGURE 3.5 Hardware for FSM of Exercise 3.26

Note: One could also build this functionality by registering input *A*, pro-
ducing both the logical AND and OR of input *A* and its previous (registered)

value, and then muxing the two operations using B. The output of the mux is Z:
$Z = A A \text{prev}$ (if $B = 0$); $Z = A + A \text{prev}$ (if $B = 1$).

Exercise 3.31

This finite state machine is a divide-by-two counter (see Section 3.4.2) when $X = 0$. When $X = 1$, the output, Q, is HIGH.

current state		input	next state	
s_1	s_0	x	s'_1	s'_0
0	0	0	0	1
0	0	1	1	1
0	1	0	0	0
0	1	1	1	0
1	X	X	0	1

TABLE 3.7 State transition table with binary encodings for Exercise 3.31

current state		output
s_1	s_0	q
0	0	0
0	1	1
1	X	1

TABLE 3.8 Output table for Exercise 3.31
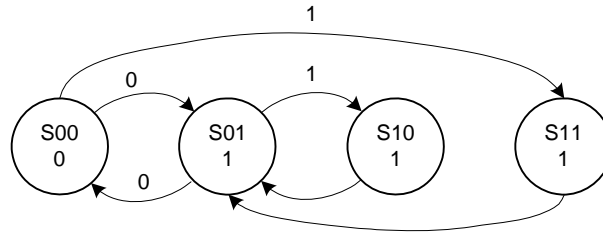
Exercise 3.33

(a) First, we calculate the propagation delay through the combinational logic:

$$t_{pd} = 3t_{pd\_XOR}$$
$$= 3 \times 100 \text{ ps}$$
$$= \textbf{300 ps}$$

Next, we calculate the cycle time:

$$T_c \geq t_{pcq} + t_{pd} + t_{setup}$$
$$\geq [70 + 300 + 60] \text{ ps}$$
$$= 430 \text{ ps}$$
$$f = 1 / 430 \text{ ps} = \textbf{2.33 GHz}$$

(b)
$$T_c \geq t_{pcq} + t_{pd} + t_{setup} + t_{skew}$$
Thus,
$$t_{skew} \leq T_c - (t_{pcq} + t_{pd} + t_{setup}), \text{ where } T_c = 1 / 2 \text{ GHz} = 500 \text{ ps}$$
$$\leq [500 - 430] \text{ ps} = \textbf{70 ps}$$

(c)
First, we calculate the contamination delay through the combinational logic:

$$t_{cd} = t_{cd\_XOR}$$
$$= 55 \text{ ps}$$

$$t_{ccq} + t_{cd} > t_{hold} + t_{skew}$$
Thus,
$$t_{skew} < (t_{ccq} + t_{cd}) - t_{hold}$$
$$< (50 + 55) - 20$$
$$< \textbf{85 ps}$$

(d)

FIGURE 3.6 Alyssa's improved circuit for Exercise 3.33

First, we calculate the propagation and contamination delays through the combinational logic:

$t_{pd} = 2t_{pd\_XOR}$
$\quad = 2 \times 100 \text{ ps}$
$\quad = \textbf{200 ps}$

$t_{cd} = 2t_{cd\_XOR}$
$\quad = 2 \times 55 \text{ ps}$
$\quad = \textbf{110 ps}$

Next, we calculate the cycle time:

$T_c \geq t_{pcq} + t_{pd} + t_{setup}$
$\quad \geq [70 + 200 + 60] \text{ ps}$
$\quad = 330 \text{ ps}$
$f \quad = 1 / 330 \text{ ps} = \textbf{3.03 GHz}$

$t_{skew} < (t_{ccq} + t_{cd}) - t_{hold}$
$\quad\quad < (50 + 110) - 20$
$\quad\quad \textbf{< 140 ps}$

Exercise 3.35

(a) $T_c = 1 / 40 \text{ MHz} = 25 \text{ ns}$

$T_c \quad \geq t_{pcq} + Nt_{CLB} + t_{setup}$
$25 \text{ ns} \geq [0.72 + N(0.61) + 0.53] \text{ ps}$
Thus, N < 38.9
N = 38

(b)

$$t_{skew} < (t_{ccq} + t_{cd\_CLB}) - t_{hold}$$
$$< [(0.5 + 0.3) - 0] \, ns$$
$$< 0.8 \, ns = 800 \, ps$$

Exercise 3.37

P(failure)/sec = 1/MTBF = 1/(50 years * 3.15 x 10^7 sec/year) = **6.34 x 10^{-10}** (EQ 3.26)

P(failure)/sec waiting for one clock cycle: $N*(T_0/T_c)*e^{-(Tc-tsetup)/Tau}$

$$= 0.5 * (110/1000) * e^{-(1000-70)/100} = 5.0 \times 10^{-6}$$

P(failure)/sec waiting for two clock cycles: $N*(T_0/T_c)*[e^{-(Tc-tsetup)/Tau}]^2$

$$= 0.5 * (110/1000) * [e^{-(1000-70)/100}]^2 = 4.6 \times 10^{-10}$$

This is just less than the required probability of failure (6.34 x 10^{-10}). Thus, **2 cycles** of waiting is just adequate to meet the MTBF.

Exercise 3.39

We assume a two flip-flop synchronizer. The most significant impact on the probability of failure comes from the exponential component. If we ignore the T_0/T_c term in the probability of failure equation, assuming it changes little with increases in cycle time, we get:

$$P(\text{failure}) = e^{-\frac{t}{\tau}}$$

$$MTBF = \frac{1}{P(failure)} = e^{\frac{T_c - t_{setup}}{\tau}}$$

$$\frac{MTBF_2}{MTBF_1} = 10 = e^{\frac{T_{c2} - T_{c1}}{30ps}}$$

Solving for $T_{c2} - T_{c1}$, we get:

$$T_{c2} - T_{c1} = 69ps$$

Thus, the clock cycle time must increase by **69 ps**. This holds true for cycle times much larger than T0 (20 ps) and the increased time (69 ps).

Question 3.1
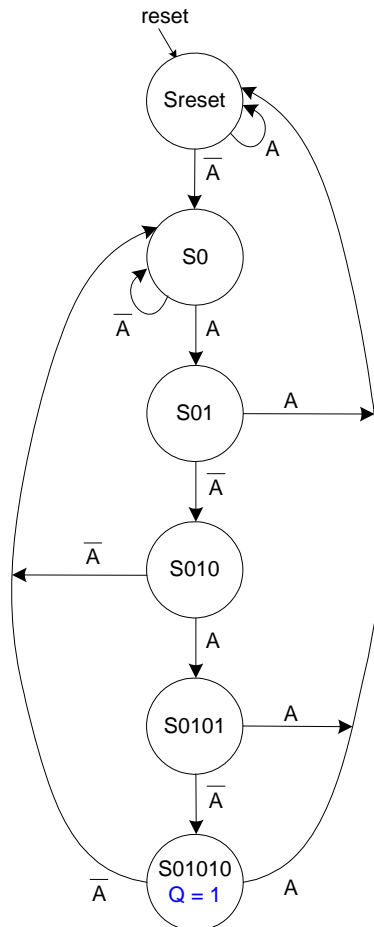
FIGURE 3.7 State transition diagram for Question 3.1

current state $s_{5:0}$	input a	next state $s'_{5:0}$
000001	0	000010
000001	1	000001
000010	0	000010
000010	1	000100
000100	0	001000
000100	1	000001
001000	0	000010
001000	1	010000
010000	0	100000
010000	1	000001
100000	0	000010
100000	1	000001

TABLE 3.9 State transition table for Question 3.1

$$S'_5 = S_4 A$$
$$S'_4 = S_3 A$$
$$S'_3 = S_2 A$$
$$S'_2 = S_1 A$$
$$S'_1 = A(S_1 + S_3 + S_5)$$
$$S'_0 = A(S_0 + S_2 + S_4 + S_5)$$
$$Q = S_5$$
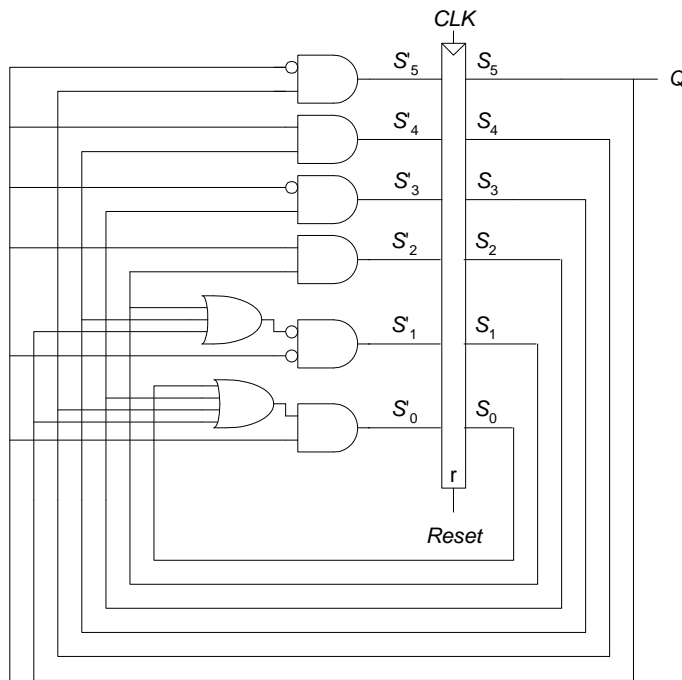
FIGURE 3.8 Finite state machine hardware for Question 3.1

Question 3.3

A latch allows input D to flow through to the output Q when the clock is HIGH. A flip-flop allows input D to flow through to the output Q at the clock edge. A flip-flop is preferable in systems with a single clock. Latches are preferable in *two-phase clocking* systems, with two clocks. The two clocks are used to eliminate system failure due to hold time violations. Both the phase and frequency of each clock can be modified independently.

Question 3.5
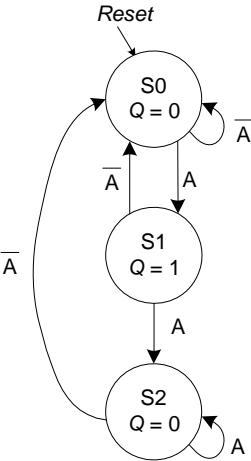
FIGURE 3.9 State transition diagram for edge detector circuit of Question 3.5

current state $s_{1:0}$	input a	next state $s'_{1:0}$
00	0	00
00	1	01
01	0	00
01	1	10
10	0	00
10	1	10

TABLE 3.10 State transition table for Question 3.5

$$S'_1 = AS_1$$

$$S'_0 = AS_1S_0$$

$Q = S_1$
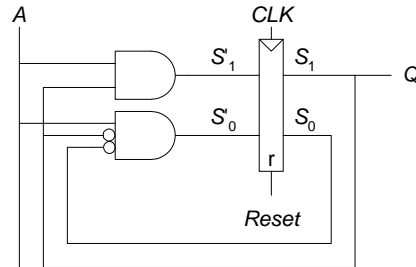
FIGURE 3.10 Finite state machine hardware for Question 3.5

Question 3.7

A flip-flop with a negative hold time allows *D* to start changing *before* the clock edge arrives.

Question 3.9

Without the added buffer, the propagation delay through the logic, t_{pd}, must be less than or equal to T_c - (t_{pcq} + t_{setup}). However, if you add a buffer to the clock input of the receiver, the clock arrives at the receiver later. The earliest that the clock edge arrives at the receiver is t_{cd_BUF} after the actual clock edge. Thus, the propagation delay through the logic is now given an extra t_{cd_BUF}. So, t_{pd} now must be less than T_c + t_{cd_BUF} - (t_{pcq} + t_{setup}).

CHAPTER 4

Note: the HDL files given in the following solutions are available on the textbook's companion website at:
    http://textbooks.elsevier.com/9780123704979
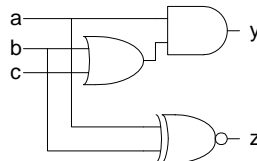
Exercise 4.1

Exercise 4.3

SystemVerilog

```
module xor_4(input logic [3:0] a,
             output logic      y);

   assign y = ^a;
endmodule
```

VHDL

```
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity xor_4 is
  port(a: in  STD_LOGIC_VECTOR(3 downto 0);
       y: out STD_LOGIC);
end;

architecture synth of xor_4 is
begin
  y <= a(3) xor a(2) xor a(1) xor a(0);
end;
```

Exercise 4.5

SystemVerilog

```
module minority(input  logic a, b, c
                output logic y);

   assign y = ~a & ~b | ~a & ~c | ~b & ~c;
endmodule
```

VHDL

```
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity minority is
  port(a, b, c:  in  STD_LOGIC;
       y:        out STD_LOGIC);
end;

architecture synth of minority is
begin
  y <= ((not a) and (not b)) or ((not a) and (not c))
       or ((not b) and (not c));
end;
```

Exercise 4.7

ex4_7.tv file:

```
0000_111_1110
0001_011_0000
0010_110_1101
0011_111_1001
0100_011_0011
0101_101_1011
0110_101_1111
0111_111_0000
1000_111_1111
1001_111_1011
1010_111_0111
1011_001_1111
1100_000_1101
1101_011_1101
1110_100_1111
1111_100_0111
```

Option 1:

SystemVerilog

```systemverilog
module ex4_7_testbench();
  logic        clk, reset;
  logic [3:0]  data;
  logic [6:0]  s_expected;
  logic [6:0]  s;
  logic [31:0] vectornum, errors;
  logic [10:0] testvectors[10000:0];

  // instantiate device under test
  sevenseg dut(data, s);

  // generate clock
  always
    begin
      clk = 1; #5; clk = 0; #5;
    end

  // at start of test, load vectors
  // and pulse reset
  initial
    begin
      $readmemb("ex4_7.tv", testvectors);
      vectornum = 0; errors = 0;
      reset = 1; #27; reset = 0;
    end

  // apply test vectors on rising edge of clk
  always @(posedge clk)
    begin
      #1; {data, s_expected} =
            testvectors[vectornum];
    end

  // check results on falling edge of clk
   always @(negedge clk)
    if (~reset) begin // skip during reset
      if (s !== s_expected) begin
        $display("Error: inputs = %h", data);
        $display("  outputs = %b (%b expected)",
                 s, s_expected);
        errors = errors + 1;
      end
      vectornum = vectornum + 1;
      if (testvectors[vectornum] === 11'bx) begin
       $display("%d tests completed with %d errors",
                vectornum, errors);
        $finish;
      end
    end
endmodule
```

VHDL

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;
use STD.TEXTIO.all;
use IEEE.STD_LOGIC_UNSIGNED.all;
use IEEE.STD_LOGIC_ARITH.all;

entity ex4_7_testbench is -- no inputs or outputs
end;

architecture sim of ex4_7_testbench is
  component seven_seg_decoder
  port(data:    in  STD_LOGIC_VECTOR(3 downto 0);
       segments: out STD_LOGIC_VECTOR(6 downto 0));
  end component;
  signal data: STD_LOGIC_VECTOR(3 downto 0);
  signal s:    STD_LOGIC_VECTOR(6 downto 0);
  signal clk, reset: STD_LOGIC;
  signal s_expected: STD_LOGIC_VECTOR(6 downto 0);
  constant MEMSIZE: integer := 10000;
  type tvarray is array(MEMSIZE downto 0) of
    STD_LOGIC_VECTOR(10 downto 0);
  signal testvectors: tvarray;
  shared variable vectornum, errors: integer;
begin
  -- instantiate device under test
  dut: seven_seg_decoder port map(data, s);

  -- generate clock
  process begin
    clk <= '1'; wait for 5 ns;
    clk <= '0'; wait for 5 ns;
  end process;

  -- at start of test, load vectors
  -- and pulse reset
  process is
    file tv: TEXT;
    variable i, j: integer;
    variable L: line;
    variable ch: character;
  begin
    -- read file of test vectors
    i := 0;
    FILE_OPEN(tv, "ex4_7.tv", READ_MODE);
    while not endfile(tv) loop
      readline(tv, L);
      for j in 10 downto 0 loop
        read(L, ch);
        if (ch = '_') then read(L, ch);
        end if;
        if (ch = '0') then
          testvectors(i)(j) <= '0';
        else testvectors(i)(j) <= '1';
        end if;
      end loop;
      i := i + 1;
    end loop;
```

(VHDL continued on next page)

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VHDL

```vhdl
    vectornum := 0; errors := 0;
    reset <= '1'; wait for 27 ns; reset <= '0';
    wait;
  end process;

  -- apply test vectors on rising edge of clk
  process (clk) begin
    if (clk'event and clk = '1') then

      data <= testvectors(vectornum)(10 downto 7)
        after 1 ns;
     s_expected <= testvectors(vectornum)(6 downto 0)
        after 1 ns;
    end if;
  end process;

  -- check results on falling edge of clk
  process (clk) begin
    if (clk'event and clk = '0' and reset = '0') then
      assert s = s_expected
        report "data = " &
          integer'image(CONV_INTEGER(data)) &
          "; s = " &
          integer'image(CONV_INTEGER(s)) &
          "; s_expected = " &
           integer'image(CONV_INTEGER(s_expected));
      if (s /= s_expected) then
        errors := errors + 1;
      end if;
      vectornum := vectornum + 1;
      if (is_x(testvectors(vectornum))) then
        if (errors = 0) then
          report "Just kidding -- " &
                 integer'image(vectornum) &
                 " tests completed successfully."
                 severity failure;
        else
          report integer'image(vectornum) &
                 " tests completed, errors = " &
                 integer'image(errors)
                 severity failure;
        end if;
      end if;
    end if;
  end process;
end;
```

Option 2 (VHDL only):

VHDL

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;
use STD.TEXTIO.all;
use work.txt_util.all;

entity ex4_7_testbench is -- no inputs or outputs
end;

architecture sim of ex4_7_testbench is
  component seven_seg_decoder
  port(data:     in  STD_LOGIC_VECTOR(3 downto 0);
       segments: out STD_LOGIC_VECTOR(6 downto 0));
  end component;
  signal data: STD_LOGIC_VECTOR(3 downto 0);
  signal s:    STD_LOGIC_VECTOR(6 downto 0);
  signal clk, reset: STD_LOGIC;
  signal s_expected: STD_LOGIC_VECTOR(6 downto 0);
  constant MEMSIZE: integer := 10000;
  type tvarray is array(MEMSIZE downto 0) of
    STD_LOGIC_VECTOR(10 downto 0);
  signal testvectors: tvarray;
  shared variable vectornum, errors: integer;
begin
  -- instantiate device under test
  dut: seven_seg_decoder port map(data, s);

  -- generate clock
  process begin
    clk <= '1'; wait for 5 ns;
    clk <= '0'; wait for 5 ns;
  end process;

  -- at start of test, load vectors
  -- and pulse reset
  process is
    file tv: TEXT;
    variable i, j: integer;
    variable L: line;
    variable ch: character;
  begin
    -- read file of test vectors
    i := 0;
    FILE_OPEN(tv, "ex4_7.tv", READ_MODE);
    while not endfile(tv) loop
      readline(tv, L);
      for j in 10 downto 0 loop
        read(L, ch);
        if (ch = '_') then read(L, ch);
        end if;
        if (ch = '0') then
          testvectors(i)(j) <= '0';
        else testvectors(i)(j) <= '1';
        end if;
      end loop;
      i := i + 1;
    end loop;

    vectornum := 0; errors := 0;
    reset <= '1'; wait for 27 ns; reset <= '0';
```

```vhdl
    wait;
  end process;

  -- apply test vectors on rising edge of clk
  process (clk) begin
    if (clk'event and clk = '1') then

      data <= testvectors(vectornum)(10 downto 7)
        after 1 ns;
      s_expected <= testvectors(vectornum)(6 downto 0)
        after 1 ns;
    end if;
  end process;

  -- check results on falling edge of clk
  process (clk) begin
    if (clk'event and clk = '0' and reset = '0') then
      assert s = s_expected
        report "data = " & str(data) &
          "; s = " & str(s) &
          "; s_expected = " & str(s_expected);
      if (s /= s_expected) then
        errors := errors + 1;
      end if;
      vectornum := vectornum + 1;
      if (is_x(testvectors(vectornum))) then
        if (errors = 0) then
          report "Just kidding -- " &
                 integer'image(vectornum) &
                 " tests completed successfully."
                 severity failure;
        else
          report integer'image(vectornum) &
                 " tests completed, errors = " &
                 integer'image(errors)
                 severity failure;
        end if;
      end if;
    end if;
  end process;
end;
```

(see Web site for file: txt_util.vhd)

Exercise 4.9

SystemVerilog

```
module ex4_9
   (input  logic a, b, c,
    output logic y);

   mux8 #(1) mux8_1(1'b1, 1'b0, 1'b0, 1'b1,
                    1'b1, 1'b1, 1'b0, 1'b0,
                    {a,b,c}, y);
endmodule
```

VHDL

```
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity ex4_9 is
  port(a,
       b,
       c: in  STD_LOGIC;
       y: out STD_LOGIC_VECTOR(0 downto 0));
end;

architecture struct of ex4_9 is
  component mux8
    generic(width: integer);
  port(d0, d1, d2, d3, d4, d5, d6,
       d7:  in  STD_LOGIC_VECTOR(width-1 downto 0);
       s:   in  STD_LOGIC_VECTOR(2 downto 0);
       y:   out STD_LOGIC_VECTOR(width-1 downto 0));
  end component;
  signal sel: STD_LOGIC_VECTOR(2 downto 0);
begin
  sel <= a & b & c;

  mux8_1: mux8 generic map(1)
              port map("1", "0", "0", "1",
                       "1", "1", "0", "0",
                       sel, y);
end;
```

Exercise 4.11

A shift register with feedback, shown below, cannot be correctly described with blocking assignments.

CLK
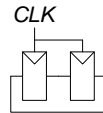
Exercise 4.13

SystemVerilog

```
module decoder2_4(input  logic [1:0] a,
                  output logic [3:0] y);
  always_comb
    case (a)
      2'b00: y = 4'b0001;
      2'b01: y = 4'b0010;
      2'b10: y = 4'b0100;
      2'b11: y = 4'b1000;
    endcase
endmodule
```

VHDL

```
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity decoder2_4 is
  port(a: in  STD_LOGIC_VECTOR(1 downto 0);
       y: out STD_LOGIC_VECTOR(3 downto 0));
end;

architecture synth of decoder2_4 is
begin
  process(all) begin
    case a is
      when "00"   => y <= "0001";
      when "01"   => y <= "0010";
      when "10"   => y <= "0100";
      when "11"   => y <= "1000";
      when others => y <= "0000";
    end case;
  end process;
end;
```

Exercise 4.15

(a) $Y = AC + \bar{A}\bar{B}C$

SystemVerilog

```
module ex4_15a(input  logic a, b, c,
               output logic y);

  assign y = (a & c) | (~a & ~b & c);
endmodule
```

VHDL

```
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity ex4_15a is
  port(a, b, c: in  STD_LOGIC;
           y:      out STD_LOGIC);
end;

architecture behave of ex4_15a is
begin
  y <= (not a and not b and c) or (not b and c);
end;
```

(b) $Y = \bar{A}\bar{B} + \bar{A}B\bar{C} + \overline{(A + \bar{C})}$

SystemVerilog

```
module ex4_15b(input  logic a, b, c,
               output logic y);

  assign y = (~a & ~b) | (~a & b & ~c) | ~(a | ~c);
endmodule
```

VHDL

```
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity ex4_15b is
  port(a, b, c: in  STD_LOGIC;
           y:      out STD_LOGIC);
end;

architecture behave of ex4_15b is
begin
  y <= ((not a) and (not b)) or ((not a) and b and
       (not c)) or (not(a or (not c)));
end;
```

(c) $Y = \bar{A}\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C} + A\bar{B}C\bar{D} + ABD + \bar{A}\bar{B}C\bar{D} + B\bar{C}D + \bar{A}$

SystemVerilog

```
module ex4_15c(input  logic a, b, c, d,
               output logic y);

  assign y = (~a & ~b & ~c & ~d) | (a & ~b & ~c) |
             (a & ~b & c & ~d) | (a & b & d) |
             (~a & ~b & c & ~d) | (b & ~c & d) | ~a;
endmodule
```

VHDL

```
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity ex4_15c is
  port(a, b, c, d: in  STD_LOGIC;
           y:      out STD_LOGIC);
end;

architecture behave of ex4_15c is
begin
  y <= ((not a) and (not b) and (not c) and (not d)) or
       (a and (not b) and (not c)) or
       (a and (not b) and c and (not d)) or
       (a and b and d) or
       ((not a) and (not b) and c and (not d)) or
       (b and (not c) and d) or (not a);
end;
```

Exercise 4.17

SystemVerilog

```
module ex4_17(input  logic a, b, c, d, e, f, g
              output logic y);

  logic n1, n2, n3, n4, n5;

  assign n1 = ~(a & b & c);
  assign n2 = ~(n1 & d);
  assign n3 = ~(f & g);
  assign n4 = ~(n3 | e);
  assign n5 = ~(n2 | n4);
  assign y = ~(n5 & n5);
endmodule
```

VHDL

```
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity ex4_17 is
  port(a, b, c, d, e, f, g: in  STD_LOGIC;
       y:             out STD_LOGIC);
end;

architecture synth of ex4_17 is
  signal n1, n2, n3, n4, n5: STD_LOGIC;
begin
  n1 <= not(a and b and c);
  n2 <= not(n1 and d);
  n3 <= not(f and g);
  n4 <= not(n3 or e);
  n5 <= not(n2 or n4);
  y <= not (n5 or n5);
end;
```

Exercise 4.19

SystemVerilog

```
module ex4_18(input  logic [3:0] a,
              output logic       p, d);

  always_comb
    case (a)
       0: {p, d} = 2'b00;
       1: {p, d} = 2'b00;
       2: {p, d} = 2'b10;
       3: {p, d} = 2'b11;
       4: {p, d} = 2'b00;
       5: {p, d} = 2'b10;
       6: {p, d} = 2'b01;
       7: {p, d} = 2'b10;
       8: {p, d} = 2'b00;
       9: {p, d} = 2'b01;
      10: {p, d} = 2'b00;
      11: {p, d} = 2'b10;
      12: {p, d} = 2'b01;
      13: {p, d} = 2'b10;
      14: {p, d} = 2'b00;
      15: {p, d} = 2'b01;
    endcase
endmodule
```

VHDL

```
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity ex4_18 is
  port(a:    in  STD_LOGIC_VECTOR(3 downto 0);
       p, d: out STD_LOGIC);
end;

architecture synth of ex4_18 is
signal vars: STD_LOGIC_VECTOR(1 downto 0);
begin
  p <= vars(1);
  d <= vars(0);
  process(all) begin
    case a is
      when X"0"   => vars <= "00";
      when X"1"   => vars <= "00";
      when X"2"   => vars <= "10";
      when X"3"   => vars <= "11";
      when X"4"   => vars <= "00";
      when X"5"   => vars <= "10";
      when X"6"   => vars <= "01";
      when X"7"   => vars <= "10";
      when X"8"   => vars <= "00";
      when X"9"   => vars <= "01";
      when X"A"   => vars <= "00";
      when X"B"   => vars <= "10";
      when X"C"   => vars <= "01";
      when X"D"   => vars <= "10";
      when X"E"   => vars <= "00";
      when X"F"   => vars <= "01";
      when others => vars <= "00";
    end case;
  end process;
end;
```

Exercise 4.21

SystemVerilog

```systemverilog
module priority_encoder2(input  logic [7:0] a,
                         output logic [2:0] y, z,
                         output logic       none);

  always_comb
  begin
    casez (a)
       8'b00000000: begin y = 3'd0; none = 1'b1; end
       8'b00000001: begin y = 3'd0; none = 1'b0; end
       8'b0000001?: begin y = 3'd1; none = 1'b0; end
       8'b000001??: begin y = 3'd2; none = 1'b0; end
       8'b00001???: begin y = 3'd3; none = 1'b0; end
       8'b0001????: begin y = 3'd4; none = 1'b0; end
       8'b001?????: begin y = 3'd5; none = 1'b0; end
       8'b01??????: begin y = 3'd6; none = 1'b0; end
       8'b1???????: begin y = 3'd7; none = 1'b0; end
    endcase

    casez (a)
       8'b00000011: z = 3'b000;
       8'b00000101: z = 3'b000;
       8'b00001001: z = 3'b000;
       8'b00010001: z = 3'b000;
       8'b00100001: z = 3'b000;
       8'b01000001: z = 3'b000;
       8'b10000001: z = 3'b000;
       8'b0000011?: z = 3'b001;
       8'b0000101?: z = 3'b001;
       8'b0001001?: z = 3'b001;
       8'b0010001?: z = 3'b001;
       8'b0100001?: z = 3'b001;
       8'b1000001?: z = 3'b001;
       8'b000011??: z = 3'b010;
       8'b000101??: z = 3'b010;
       8'b001001??: z = 3'b010;
       8'b010001??: z = 3'b010;
       8'b100001??: z = 3'b010;
       8'b00011???: z = 3'b011;
       8'b00101???: z = 3'b011;
       8'b01001???: z = 3'b011;
       8'b10001???: z = 3'b011;
       8'b0011????: z = 3'b100;
       8'b0101????: z = 3'b100;
       8'b1001????: z = 3'b100;
       8'b011?????: z = 3'b101;
       8'b101?????: z = 3'b101;
       8'b11??????: z = 3'b110;
       default:     z = 3'b000;
    end
  endmodule
```

VHDL

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity priority_encoder2 is
  port(a:    in  STD_LOGIC_VECTOR(7 downto 0);
       y, z: out STD_LOGIC_VECTOR(2 downto 0);
       none: out STD_LOGIC);
end;

architecture synth of priority_encoder is
begin
  process(all) begin
    case? a is
      when "00000000" => y <= "000"; none <= '1';
      when "00000001" => y <= "000"; none <= '0';
      when "0000001-" => y <= "001"; none <= '0';
      when "000001--" => y <= "010"; none <= '0';
      when "00001---" => y <= "011"; none <= '0';
      when "0001----" => y <= "100"; none <= '0';
      when "001-----" => y <= "101"; none <= '0';
      when "01------" => y <= "110"; none <= '0';
      when "1-------" => y <= "111"; none <= '0';
      when others     => y <= "000"; none <= '0';
    end case?;
    case? a is
      when "00000011" => z <= "000";
      when "00000101" => z <= "000";
      when "00001001" => z <= "000";
      when "00001001" => z <= "000";
      when "00010001" => z <= "000";
      when "00100001" => z <= "000";
      when "01000001" => z <= "000";
      when "10000001" => z <= "000";
      when "0000011-" => z <= "001";
      when "0000101-" => z <= "001";
      when "0001001-" => z <= "001";
      when "0010001-" => z <= "001";
      when "0100001-" => z <= "001";
      when "1000001-" => z <= "001";
      when "000011--" => z <= "010";
      when "000101--" => z <= "010";
      when "001001--" => z <= "010";
      when "010001--" => z <= "010";
      when "100001--" => z <= "010";
      when "00011---" => z <= "011";
      when "00101---" => z <= "011";
      when "01001---" => z <= "011";
      when "10001---" => z <= "011";
      when "0011----" => z <= "100";
      when "0101----" => z <= "100";
      when "1001----" => z <= "100";
      when "011-----" => z <= "101";
      when "101-----" => z <= "101";
      when "11------" => z <= "110";
      when others     => z <= "000";
    end case?;
  end process;
end;
```

Exercise 4.23

SystemVerilog

```
module month31days(input  logic [3:0] month,
                   output logic       y);

  always_comb
    casez (month)
        1:       y = 1'b1;
        2:       y = 1'b0;
        3:       y = 1'b1;
        4:       y = 1'b0;
        5:       y = 1'b1;
        6:       y = 1'b0;
        7:       y = 1'b1;
        8:       y = 1'b1;
        9:       y = 1'b0;
        10:      y = 1'b1;
        11:      y = 1'b0;
        12:      y = 1'b1;
        default: y = 1'b0;
    endcase
endmodule
```

VHDL

```
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity month31days is
  port(a:   in  STD_LOGIC_VECTOR(3 downto 0);
       y:   out STD_LOGIC);
end;

architecture synth of month31days is
begin
  process(all) begin
    case a is
      when X"1"   => y <= '1';
      when X"2"   => y <= '0';
      when X"3"   => y <= '1';
      when X"4"   => y <= '0';
      when X"5"   => y <= '1';
      when X"6"   => y <= '0';
      when X"7"   => y <= '1';
      when X"8"   => y <= '1';
      when X"9"   => y <= '0';
      when X"A"   => y <= '1';
      when X"B"   => y <= '0';
      when X"C"   => y <= '1';
      when others => y <= '0';
    end case;
  end process;
end;
```

Exercise 4.25
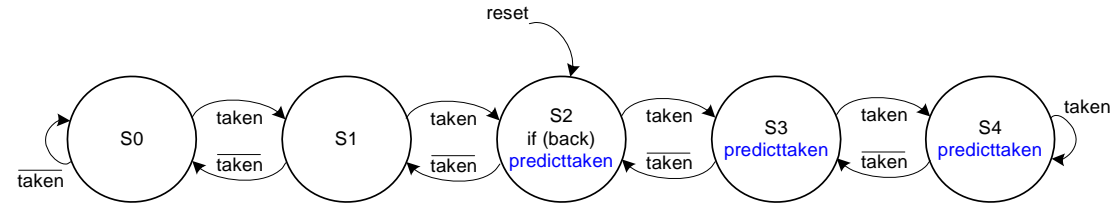
FIGURE 4.1 State transition diagram for Exercise 4.25

Exercise 4.27

SystemVerilog

```systemverilog
module jkflop(input  logic j, k, clk,
              output logic q);

  always @(posedge clk)
    case ({j,k})
      2'b01: q <= 1'b0;
      2'b10: q <= 1'b1;
      2'b11: q <= ~q;
    endcase
endmodule
```

VHDL

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity jkflop is
  port(j, k, clk: in    STD_LOGIC;
       q:            inout STD_LOGIC);
end;

architecture synth of jkflop is
signal jk: STD_LOGIC_VECTOR(1 downto 0);
begin
  jk <= j & k;
  process(clk) begin
    if rising_edge(clk) then
      if j = '1' and k = '0'
        then q <= '1';
      elsif j = '0' and k = '1'
        then q <= '0';
      elsif j = '1' and k = '1'
        then q <= not q;
      end if;
    end if;
  end process;
end;
```

Exercise 4.29

SystemVerilog

```systemverilog
module trafficFSM(input  logic clk, reset, ta, tb,
                  output logic [1:0] la, lb);

  typedef enum logic [1:0] {S0, S1, S2, S3}
    statetype;
  statetype [1:0] state, nextstate;

  parameter green  = 2'b00;
  parameter yellow = 2'b01;
  parameter red    = 2'b10;

  // State Register
  always_ff @(posedge clk, posedge reset)
    if (reset) state <= S0;
    else       state <= nextstate;

  // Next State Logic
  always_comb
    case (state)
      S0: if (ta) nextstate = S0;
          else    nextstate = S1;
      S1:         nextstate = S2;
      S2: if (tb) nextstate = S2;
          else    nextstate = S3;
      S3:         nextstate = S0;
    endcase

  // Output Logic
  always_comb
    case (state)
      S0: {la, lb} = {green, red};
      S1: {la, lb} = {yellow, red};
      S2: {la, lb} = {red, green};
      S3: {la, lb} = {red, yellow};
    endcase
endmodule
```

VHDL

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity trafficFSM is
  port(clk, reset, ta, tb: in  STD_LOGIC;
       la, lb: inout STD_LOGIC_VECTOR(1 downto 0));
end;

architecture behave of trafficFSM is
  type statetype is (S0, S1, S2, S3);
  signal state, nextstate: statetype;
  signal lalb: STD_LOGIC_VECTOR(3 downto 0);
begin
  -- state register
  process(clk, reset) begin
    if reset then state <= S0;
    elsif rising_edge(clk) then
      state <= nextstate;
    end if;
  end process;

 -- next state logic
 process(all) begin
    case state is
      when S0 => if ta then
                      nextstate <= S0;
                 else nextstate <= S1;
                 end if;
      when S1 => nextstate <= S2;
      when S2 => if tb then
                      nextstate <= S2;
                 else nextstate <= S3;
                 end if;
      when S3 => nextstate <= S0;
      when others =>  nextstate <= S0;
    end case;
  end process;

  -- output logic
  la <= lalb(3 downto 2);
  lb <= lalb(1 downto 0);
  process(all) begin
    case state is
      when S0 =>     lalb <= "0010";
      when S1 =>     lalb <= "0110";
      when S2 =>     lalb <= "1000";
      when S3 =>     lalb <= "1001";
      when others => lalb <= "1010";
    end case;
  end process;
end;
```

Exercise 4.31

SystemVerilog

```
module fig3_42(input  logic clk, a, b, c, d,
               output logic x, y);

  logic n1, n2;
  logic areg, breg, creg, dreg;

  always_ff @(posedge clk) begin
    areg <= a;
    breg <= b;
    creg <= c;
    dreg <= d;
    x <= n2;
    y <= ~(dreg | n2);
  end

  assign n1 = areg & breg;
  assign n2 = n1 | creg;
endmodule
```

VHDL

```
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity fig3_42 is
  port(clk, a, b, c, d: in  STD_LOGIC;
       x, y:            out STD_LOGIC);
end;

architecture synth of fig3_40 is
  signal n1, n2, areg, breg, creg, dreg: STD_LOGIC;
begin
  process(clk) begin
    if rising_edge(clk) then
      areg <= a;
      breg <= b;
      creg <= c;
      dreg <= d;
      x <= n2;
      y <= not (dreg or n2);
    end if;
  end process;

  n1 <= areg and breg;
  n2 <= n1 or creg;
end;
```

Exercise 4.33

SystemVerilog

```systemverilog
module fig3_70(input  logic clk, reset, a, b,
               output logic q);
  typedef enum logic [1:0] {S0, S1, S2} statetype;
  statetype [1:0] state, nextstate;

  // State Register
  always_ff @(posedge clk, posedge reset)
    if (reset) state <= S0;
    else       state <= nextstate;

  // Next State Logic
  always_comb
    case (state)
      S0: if (a)     nextstate = S1;
          else       nextstate = S0;
      S1: if (b)     nextstate = S2;
          else       nextstate = S0;
      S2: if (a & b) nextstate = S2;
          else       nextstate = S0;
      default:       nextstate = S0;
    endcase

  // Output Logic
  always_comb
    case (state)
      S0:          q = 0;
      S1:          q = 0;
      S2: if (a & b) q = 1;
          else     q = 0;
      default:     q = 0;
    endcase
endmodule
```

VHDL

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity fig3_70 is
  port(clk, reset, a, b: in  STD_LOGIC;
       q:                out STD_LOGIC);
end;

architecture synth of fig3_70 is
  type statetype is (S0, S1, S2);
  signal state, nextstate: statetype;
begin
  -- state register
  process(clk, reset) begin
    if reset then state <= S0;
    elsif rising_edge(clk) then
      state <= nextstate;
    end if;
  end process;

  -- next state logic
  process(all) begin
    case state is
      when S0 => if a then
                        nextstate <= S1;
                    else nextstate <= S0;
                    end if;
      when S1 => if b then
                        nextstate <= S2;
                    else nextstate <= S0;
                    end if;
      when S2 => if (a = '1' and b = '1') then
                        nextstate <= S2;
                    else nextstate <= S0;
                    end if;
      when others =>  nextstate <= S0;
    end case;
  end process;

  -- output logic
  q <= '1' when ( (state = S2) and
                  (a = '1' and b = '1'))
          else '0';
end;
```

Exercise 4.35

SystemVerilog

```systemverilog
module daughterfsm(input  logic clk, reset, a,
                   output logic smile);
  typedef enum logic [1:0] {S0, S1, S2, S3, S4}
    statetype;
  statetype [2:0] state, nextstate;

  // State Register
  always_ff @(posedge clk, posedge reset)
    if (reset) state <= S0;
    else       state <= nextstate;

  // Next State Logic
  always_comb
    case (state)
      S0: if (a) nextstate = S1;
          else   nextstate = S0;
      S1: if (a) nextstate = S2;
          else   nextstate = S0;
      S2: if (a) nextstate = S4;
          else   nextstate = S3;
      S3: if (a) nextstate = S1;
          else   nextstate = S0;
      S4: if (a) nextstate = S4;
          else   nextstate = S3;
      default:   nextstate = S0;
    endcase

  // Output Logic
  assign smile = ((state == S3) & a) |
                 ((state == S4) & ~a);
endmodule
```

VHDL

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity daughterfsm is
  port(clk, reset, a: in  STD_LOGIC;
       smile:         out STD_LOGIC);
end;

architecture synth of daughterfsm is
  type statetype is (S0, S1, S2, S3, S4);
  signal state, nextstate: statetype;
begin
  -- state register
  process(clk, reset) begin
    if reset then state <= S0;
    elsif rising_edge(clk) then
      state <= nextstate;
    end if;
  end process;

  -- next state logic
  process(all) begin
    case state is
      when S0 => if a then
                      nextstate <= S1;
                 else nextstate <= S0;
                 end if;
      when S1 => if a then
                      nextstate <= S2;
                 else nextstate <= S0;
                 end if;
      when S2 => if a then
                      nextstate <= S4;
                 else nextstate <= S3;
                 end if;
      when S3 => if a then
                      nextstate <= S1;
                 else nextstate <= S0;
                 end if;
      when S4 => if a then
                      nextstate <= S4;
                 else nextstate <= S3;
                 end if;
      when others =>  nextstate <= S0;
    end case;
  end process;

  -- output logic
  smile <= '1' when ( ((state = S3) and (a = '1')) or
                      ((state = S4) and (a = '0')) )
           else '0';
end;
```

Exercise 4.37

SystemVerilog

```systemverilog
module ex4_37(input  logic      clk, reset,
              output logic [2:0] q);
  typedef enum logic [2:0] {S0 = 3'b000,
                            S1 = 3'b001,
                            S2 = 3'b011,
                            S3 = 3'b010,
                            S4 = 3'b110,
                            S5 = 3'b111,
                            S6 = 3'b101,
                            S7 = 3'b100}
    statetype;

  statetype [2:0] state, nextstate;

  // State Register
  always_ff @(posedge clk, posedge reset)
    if (reset) state <= S0;
    else       state <= nextstate;

  // Next State Logic
  always_comb
    case (state)
      S0: nextstate = S1;
      S1: nextstate = S2;
      S2: nextstate = S3;
      S3: nextstate = S4;
      S4: nextstate = S5;
      S5: nextstate = S6;
      S6: nextstate = S7;
      S7: nextstate = S0;
    endcase

  // Output Logic
  assign q = state;
endmodule
```

VHDL

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity ex4_37 is
  port(clk:  in  STD_LOGIC;
       reset: in  STD_LOGIC;
       q:    out STD_LOGIC_VECTOR(2 downto 0));
end;

architecture synth of ex4_37 is
  signal state:    STD_LOGIC_VECTOR(2 downto 0);
  signal nextstate: STD_LOGIC_VECTOR(2 downto 0);
begin
  -- state register
  process(clk, reset) begin
    if reset then state <= "000";
    elsif rising_edge(clk) then
      state <= nextstate;
    end if;
  end process;

  -- next state logic
  process(all) begin
    case state is
      when "000"  => nextstate <= "001";
      when "001"  => nextstate <= "011";
      when "011"  => nextstate <= "010";
      when "010"  => nextstate <= "110";
      when "110"  => nextstate <= "111";
      when "111"  => nextstate <= "101";
      when "101"  => nextstate <= "100";
      when "100"  => nextstate <= "000";
      when others => nextstate <= "000";
    end case;
  end process;

  -- output logic
  q <= state;
end;
```

Exercise 4.39

Option 1

SystemVerilog

```systemverilog
module ex4_39(input  logic clk, reset, a, b,
              output logic z);
  typedef enum logic [1:0] {S0, S1, S2, S3}
    statetype;
  statetype [1:0] state, nextstate;

  // State Register
  always_ff @(posedge clk, posedge reset)
    if (reset) state <= S0;
    else       state <= nextstate;

  // Next State Logic
  always_comb
    case (state)
      S0: case ({b,a})
            2'b00: nextstate = S0;
            2'b01: nextstate = S3;
            2'b10: nextstate = S0;
            2'b11: nextstate = S1;
          endcase
      S1: case ({b,a})
            2'b00: nextstate = S0;
            2'b01: nextstate = S3;
            2'b10: nextstate = S2;
            2'b11: nextstate = S1;
          endcase
      S2: case ({b,a})
            2'b00: nextstate = S0;
            2'b01: nextstate = S3;
            2'b10: nextstate = S2;
            2'b11: nextstate = S1;
          endcase
      S3: case ({b,a})
            2'b00: nextstate = S0;
            2'b01: nextstate = S3;
            2'b10: nextstate = S2;
            2'b11: nextstate = S1;
          endcase
      default:   nextstate = S0;
    endcase

  // Output Logic
  always_comb
    case (state)
      S0:     z = a & b;
      S1:     z = a | b;
      S2:     z = a & b;
      S3:     z = a | b;
      default: z = 1'b0;
    endcase
endmodule
```

VHDL

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity ex4_39 is
  port(clk:   in  STD_LOGIC;
       reset: in  STD_LOGIC;
       a, b:  in  STD_LOGIC;
       z:     out STD_LOGIC);
end;

architecture synth of ex4_39 is
  type statetype is (S0, S1, S2, S3);
  signal state, nextstate: statetype;
  signal ba: STD_LOGIC_VECTOR(1 downto 0);
begin
  -- state register
  process(clk, reset) begin
    if reset then state <= S0;
    elsif rising_edge(clk) then
      state <= nextstate;
    end if;
  end process;

  -- next state logic
  ba <= b & a;
  process(all) begin
    case state is
      when S0  =>
        case (ba) is
          when "00"  => nextstate <= S0;
          when "01"  => nextstate <= S3;
          when "10"  => nextstate <= S0;
          when "11"  => nextstate <= S1;
          when others => nextstate <= S0;
        end case;
      when S1  =>
        case (ba) is
          when "00"  => nextstate <= S0;
          when "01"  => nextstate <= S3;
          when "10"  => nextstate <= S2;
          when "11"  => nextstate <= S1;
          when others => nextstate <= S0;
        end case;
      when S2  =>
        case (ba) is
          when "00"  => nextstate <= S0;
          when "01"  => nextstate <= S3;
          when "10"  => nextstate <= S2;
          when "11"  => nextstate <= S1;
          when others => nextstate <= S0;
        end case;
      when S3  =>
        case (ba) is
          when "00"  => nextstate <= S0;
          when "01"  => nextstate <= S3;
          when "10"  => nextstate <= S2;
          when "11"  => nextstate <= S1;
          when others => nextstate <= S0;
        end case;
      when others      =>   nextstate <= S0;
    end case;
  end process;
```

(continued from previous page)

VHDL

```vhdl
-- output logic
process(all) begin
  case state is
    when S0     => if (a = '1' and b = '1')
                     then z <= '1';
                     else z <= '0';
                   end if;
    when S1     => if (a = '1' or b = '1')
                     then z <= '1';
                     else z <= '0';
                   end if;
    when S2     => if (a = '1' and b = '1')
                     then z <= '1';
                     else z <= '0';
                   end if;
    when S3     => if (a = '1' or b = '1')
                     then z <= '1';
                     else z <= '0';
                   end if;
    when others => z <= '0';
  end case;
end process;
end;
```

Option 2

SystemVerilog

```systemverilog
module ex4_37(input  logic clk, a, b,
              output logic z);

  logic aprev;

  // State Register
  always_ff @(posedge clk)
    aprev <= a;

  assign z = b ? (aprev | a) : (aprev & a);
endmodule
```

VHDL

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity ex4_37 is
  port(clk:  in  STD_LOGIC;
       a, b: in  STD_LOGIC;
       z:    out STD_LOGIC);
end;

architecture synth of ex4_37 is
  signal aprev, n1and, n2or: STD_LOGIC;
begin
  -- state register
  process(clk) begin
    if rising_edge(clk) then
      aprev <= a;
    end if;
  end process;


  z <= (a or aprev) when b = '1' else
       (a and aprev);
end;
```

Exercise 4.41

SystemVerilog

```
module ex4_41(input  logic clk, start, a,
              output logic q);
  typedef enum logic [1:0] {S0, S1, S2, S3}
    statetype;
  statetype [1:0] state, nextstate;

  // State Register
  always_ff @(posedge clk, posedge start)
    if (start) state <= S0;
    else       state <= nextstate;

  // Next State Logic
  always_comb
    case (state)
      S0: if  (a) nextstate = S1;
          else    nextstate = S0;
      S1: if  (a) nextstate = S2;
          else    nextstate = S3;
      S2: if  (a) nextstate = S2;
          else    nextstate = S3;
      S3: if  (a) nextstate = S2;
          else    nextstate = S3;
    endcase

  // Output Logic
  assign q = state[0];
endmodule
```

VHDL

```
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity ex4_41 is
  port(clk, start, a: in  STD_LOGIC;
       q:             out STD_LOGIC);
end;

architecture synth of ex4_41 is
  type statetype is (S0, S1, S2, S3);
  signal state, nextstate: statetype;
begin
  -- state register
  process(clk, start) begin
    if start then state <= S0;
    elsif rising_edge(clk) then
      state <= nextstate;
    end if;
  end process;

 -- next state logic
  process(all) begin
    case state is
      when S0 =>  if a then
                       nextstate <= S1;
                  else nextstate <= S0;
                  end if;
      when S1 =>  if a then
                       nextstate <= S2;
                  else nextstate <= S3;
                  end if;
      when S2 =>  if a then
                       nextstate <= S2;
                  else nextstate <= S3;
                  end if;
      when S3 =>  if a then
                       nextstate <= S2;
                  else nextstate <= S3;
                  end if;
      when others =>   nextstate <= S0;
    end case;
  end process;

  -- output logic
  q <= '1' when ((state = S1) or (state = S3))
      else '0';
end;
```

Exercise 4.43

SystemVerilog

```
module ex4_43(input  clk, reset, a,
              output q);
  typedef enum logic [1:0] {S0, S1, S2} statetype;
  statetype [1:0] state, nextstate;

  // State Register
  always_ff @(posedge clk, posedge reset)
    if (reset) state <= S0;
    else       state <= nextstate;

  // Next State Logic
  always_comb
    case (state)
      S0: if (a) nextstate = S1;
          else   nextstate = S0;
      S1: if (a) nextstate = S2;
          else   nextstate = S0;
      S2: if (a) nextstate = S2;
          else   nextstate = S0;
      default:   nextstate = S0;
    endcase

  // Output Logic
  assign q = state[1];
endmodule
```

VHDL

```
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity ex4_43 is
  port(clk, reset, a: in  STD_LOGIC;
       q:             out STD_LOGIC);
end;

architecture synth of ex4_43 is
  type statetype is (S0, S1, S2);
  signal state, nextstate: statetype;
begin
  -- state register
  process(clk, reset) begin
    if reset then state <= S0;
    elsif rising_edge(clk) then
      state <= nextstate;
    end if;
  end process;

  -- next state logic
  process(all) begin
    case state is
      when S0 =>  if a then
                         nextstate <= S1;
                  else nextstate <= S0;
                  end if;
      when S1 =>  if a then
                         nextstate <= S2;
                  else nextstate <= S0;
                  end if;
      when S2 =>  if a then
                         nextstate <= S2;
                  else nextstate <= S0;
                  end if;
      when others =>   nextstate <= S0;
    end case;
  end process;

  -- output logic
  q <= '1' when (state = S2) else '0';
end;
```

Exercise 4.45

SystemVerilog

```
module ex4_45(input  logic        clk, c,
              input  logic [1:0] a, b,
              output logic [1:0] s);

  logic  [1:0] areg, breg;
  logic        creg;
  logic [1:0]  sum;
  logic        cout;

  always_ff @(posedge clk)
    {areg, breg, creg, s} <= {a, b, c, sum};

  fulladder fulladd1(areg[0], breg[0], creg,
                     sum[0], cout);
  fulladder fulladd2(areg[1], breg[1], cout,
                     sum[1], );
endmodule
```

VHDL

```
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity ex4_45 is
  port(clk, c: in  STD_LOGIC;
       a, b:   in  STD_LOGIC_VECTOR(1 downto 0);
       s:      out STD_LOGIC_VECTOR(1 downto 0));
end;

architecture synth of ex4_45 is
  component fulladder is
    port(a, b, cin: in  STD_LOGIC;
         s, cout:   out STD_LOGIC);
  end component;
  signal creg: STD_LOGIC;
  signal areg, breg, cout: STD_LOGIC_VECTOR(1 downto
0);
  signal sum:        STD_LOGIC_VECTOR(1 downto 0);
begin
  process(clk) begin
    if rising_edge(clk) then
      areg <= a;
      breg <= b;
      creg <= c;
      s <= sum;
    end if;
  end process;

  fulladd1: fulladder
   port map(areg(0), breg(0), creg, sum(0), cout(0));
  fulladd2: fulladder
      port map(areg(1), breg(1), cout(0), sum(1),
cout(1));
end;
```

Exercise 4.47

SystemVerilog

```
module syncbad(input  logic clk,
               input  logic d,
               output logic q);

  logic n1;

  always_ff @(posedge clk)
    begin
       q  <= n1;// nonblocking
       n1 <= d; // nonblocking
    end
endmodule
```

VHDL

```
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity syncbad is
  port(clk: in  STD_LOGIC;
        d:  in  STD_LOGIC;
        q:   out STD_LOGIC);
end;

architecture bad of syncbad is
begin
  process(clk)
     variable n1: STD_LOGIC;
  begin
    if rising_edge(clk) then
       q  <= n1; -- nonblocking
       n1 <= d;  -- nonblocking
    end if;
  end process;
end;
```

Exercise 4.49

They do not have the same function.
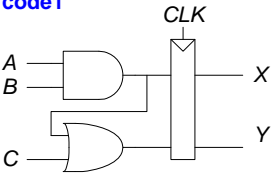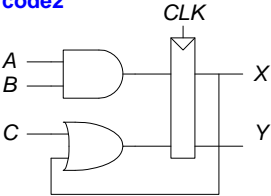
Exercise 4.51

It is necessary to write

```
q <= '1' when state = S0 else '0';
```

rather than simply

```
q <= (state = S0);
```

because the result of the comparison (state = S0) is of type Boolean (true and false) and q must be assigned a value of type STD_LOGIC ('1' and '0').

Question 4.1

SystemVerilog

```
assign result = sel ? data : 32'b0;
```

VHDL

```
result <= data when sel = '1' else X"00000000";
```

Question 4.3

The SystemVerilog statement performs the bit-wise AND of the 16 least significant bits of data with 0xC820. It then ORs these 16 bits to produce the 1-bit result.

CHAPTER 5

Exercise 5.1

(a) From Equation 5.1, we find the 64-bit ripple-carry adder delay to be:

$$t_{ripple} = Nt_{FA} = 64(450 \text{ ps}) = 28.8 \text{ ns}$$

(b) From Equation 5.6, we find the 64-bit carry-lookahead adder delay to be:

$$t_{CLA} = t_{pg} + t_{pg\_block} + \left(\frac{N}{k} - 1\right)t_{AND\_OR} + kt_{FA}$$

$$t_{CLA} = \left[150 + (6 \times 150) + \left(\frac{64}{4} - 1\right)300 + (4 \times 450)\right] = 7.35 \text{ ns}$$

(Note: the actual delay is only 7.2 ns because the first AND_OR gate only has a 150 ps delay.)

(c) From Equation 5.11, we find the 64-bit prefix adder delay to be:

$$t_{PA} = t_{pg} + \log_2 N(t_{pg\_prefix}) + t_{XOR}$$

$$t_{PA} = [150 + 6(300) + 150] = 2.1 \text{ ns}$$

Exercise 5.3

A designer might choose to use a ripple-carry adder instead of a carry-lookahead adder if chip area is the critical resource and delay is not the critical constraint.

Exercise 5.5
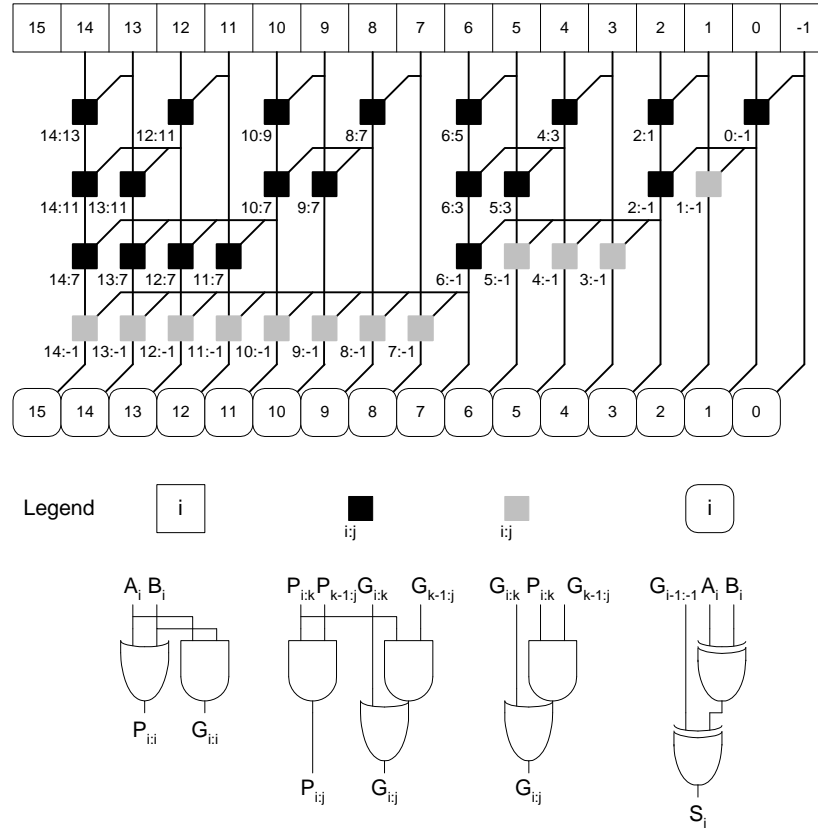
FIGURE 5.1 16-bit prefix adder with "gray cells"

Exercise 5.7

(a) We show an 8-bit priority circuit in Figure 5.2. In the figure $X_7 = \overline{A}_7$, $X_{7:6} = \overline{A}_7\overline{A}_6$, $X_{7:5} = \overline{A}_7\overline{A}_6\overline{A}_5$, and so on. The priority encoder's delay is $\log_2 N$ 2-input AND gates followed by a final row of 2-input AND gates. The final stage is an $(N/2)$-input OR gate. Thus, in general, the delay of an N-input priority encoder is:

$$t_{pd\_\text{priority}} = (\log_2 N + 1)t_{pd\_\text{AND2}} + t_{pd\_\text{OR}N/2}$$
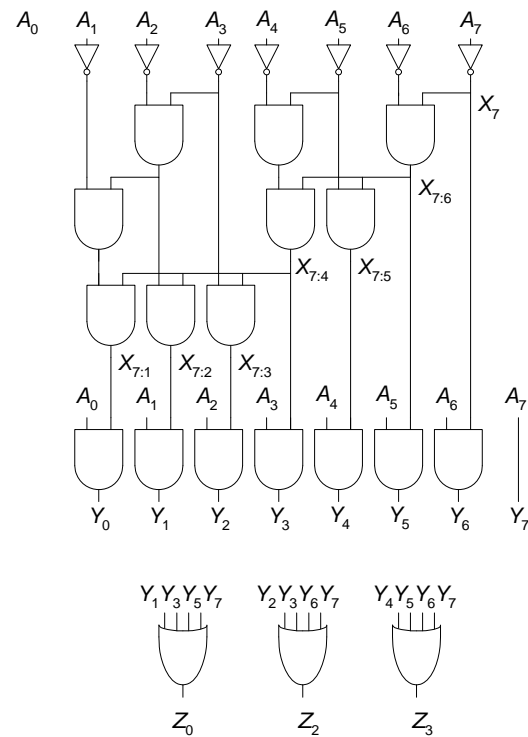
FIGURE 5.2 8-input priority encoder

SystemVerilog

```
module priorityckt(input  logic [7:0] a,
                  output logic [2:0] z);
  logic [7:0] y;
  logic       x7, x76, x75, x74, x73, x72, x71;
  logic       x32, x54, x31;
  logic [7:0] abar;

  // row of inverters
  assign abar = ~a;

  // first row of AND gates
  assign x7 = abar[7];
  assign x76 = abar[6] & x7;
  assign x54 = abar[4] & abar[5];
  assign x32 = abar[2] & abar[3];

  // second row of AND gates
  assign x75 = abar[5] & x76;
  assign x74 = x54 & x76;
  assign x31 = abar[1] & x32;

  // third row of AND gates
  assign x73 = abar[3] & x74;
  assign x72 = x32 & x74;
  assign x71 = x31 & x74;

  // fourth row of AND gates
  assign y = {a[7],        a[6] & x7,  a[5] & x76,
             a[4] & x75, a[3] & x74, a[2] & x73,
             a[1] & x72, a[0] & x71};

  // row of OR gates
  assign z = { |{y[7:4]},
               |{y[7:6], y[3:2]},
               |{y[1], y[3], y[5], y[7]} };
endmodule
```

VHDL

```
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity priorityckt is
  port(a: in  STD_LOGIC_VECTOR(7 downto 0);
       z: out STD_LOGIC_VECTOR(2 downto 0));
end;

architecture synth of priorityckt is
  signal y, abar:       STD_LOGIC_VECTOR(7 downto 0);
  signal x7, x76, x75, x74, x73, x72, x71,
         x32, x54, x31: STD_LOGIC;
begin
  -- row of inverters
  abar <= not a;

  -- first row of AND gates
  x7 <= abar(7);
  x76 <= abar(6) and x7;
  x54 <= abar(4) and abar(5);
  x32 <= abar(2) and abar(3);

  -- second row of AND gates
  x75 <= abar(5) and x76;
  x74 <= x54 and x76;
  x31 <= abar(1) and x32;

  -- third row of AND gates
  x73 <= abar(3) and x74;
  x72 <= x32 and x74;
  x71 <= x31 and x74;

  -- fourth row of AND gates
  y <= (a(7) & (a(6) and x7) & (a(5) and x76) &
       (a(4) and x75) & (a(3) and x74) & (a(2) and
x73) &
       (a(1) and x72) & (a(0) and x71));

  -- row of OR gates
  z <= ( (y(7) or y(6) or y(5) or y(4)) &
         (y(7) or y(6) or y(3) or y(2)) &
         (y(1) or y(3) or y(5) or y(7)) );

end;
```

Exercise 5.9

SystemVerilog

```systemverilog
module alu32(input  logic [31:0] A, B,
             input  logic [2:0]  F,
             output logic [31:0] Y);

  logic [31:0] S, Bout;

  assign Bout = F[2] ? ~B : B;
  assign S = A + Bout + F[2];

  always_comb
    case (F[1:0])
      2'b00: Y <= A & Bout;
      2'b01: Y <= A | Bout;
      2'b10: Y <= S;
      2'b11: Y <= S[31];
    endcase

endmodule
```

VHDL

```vhdl
library IEEE;
use IEEE.STD_LOGIC_1164.all;
use IEEE.std_logic_arith.all;
use ieee.std_logic_unsigned.all;

entity alu32 is
  port(A, B: in  STD_LOGIC_VECTOR(31 downto 0);
       F:    in  STD_LOGIC_VECTOR(2 downto 0);
       Y:    out STD_LOGIC_VECTOR(31 downto 0));
end;

architecture synth of alu32 is
  signal S, Bout:    STD_LOGIC_VECTOR(31 downto 0);
begin
  Bout <= (not B) when (F(2) = '1') else B;
  S <= A + Bout + F(2);

  process(all) begin
    case F(1 downto 0) is
      when "00" => Y <= A and Bout;
      when "01" => Y <= A or Bout;
      when "10" => Y <= S;
      when "11" => Y <=
      ("0000000000000000000000000000000" & S(31));
      when others => Y <= X"00000000";
    end case;
  end process;
end;
```

Exercise 5.11

SystemVerilog

```systemverilog
module alu32(input  logic [31:0] A, B,
             input  logic [2:0]  F,
             output logic [31:0] Y,
             output logic Zero, Overflow);
  logic [31:0] S, Bout;

  assign Bout = F[2] ? ~B : B;
  assign S = A + Bout + F[2];

  always_comb
    case (F[1:0])
      2'b00: Y <= A & Bout;
      2'b01: Y <= A | Bout;
      2'b10: Y <= S;
      2'b11: Y <= S[31];
    endcase

  assign Zero = (Y == 32'b0);

  always_comb
    case (F[2:1])
      2'b01: Overflow <= A[31] & B[31] & ~S[31] |
                         ~A[31] & ~B[31] & S[31];
      2'b11: Overflow <= ~A[31] & B[31] & S[31] |
                         A[31] & ~B[31] & ~S[31];
      default: Overflow <= 1'b0;
    endcase
endmodule
```

VHDL

```vhdl
library IEEE;
use IEEE.STD_LOGIC_1164.all;
use IEEE.std_logic_arith.all;
use ieee.std_logic_unsigned.all;

entity alu32 is
  port(A, B:    in   STD_LOGIC_VECTOR(31 downto 0);
       F:       in   STD_LOGIC_VECTOR(2 downto 0);
       Y:    inout STD_LOGIC_VECTOR(31 downto 0);
       Overflow: out  STD_LOGIC;
       Zero:    out  STD_LOGIC);
end;

architecture synth of alu32 is
  signal S, Bout:    STD_LOGIC_VECTOR(31 downto 0);
begin
  Bout <= (not B) when (F(2) = '1') else B;
  S <= A + Bout + F(2);

  -- alu function
  process(all) begin
    case F(1 downto 0) is
      when "00" => Y <= A and Bout;
      when "01" => Y <= A or Bout;
      when "10" => Y <= S;
      when "11" => Y <=
        ("0000000000000000000000000000000" & S(31));
      when others => Y <= X"00000000";
    end case;
  end process;

  Zero <= '1' when (Y = X"00000000") else '0';

  -- overflow circuit
  process(all) begin
    case F(2 downto 1) is
      when "01" => Overflow <=
        (A(31) and B(31) and (not (S(31)))) or
        ((not A(31)) and (not B(31)) and S(31));
      when "11" => Overflow <=
        ((not A(31)) and B(31) and S(31)) or
        (A(31) and (not B(31)) and (not S(31)));
      when others => Overflow <= '0';
    end case;
  end process;
end;
```

Exercise 5.13

A 2-bit left shifter creates the output by appending two zeros to the least significant bits of the input and dropping the two most significant bits.
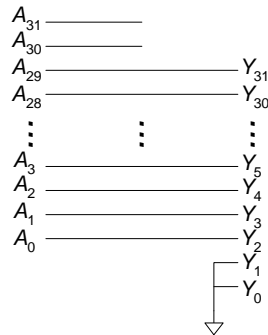
FIGURE 5.3 2-bit left shifter, 32-bit input and output

2-bit Left Shifter

SystemVerilog

```
module leftshift2_32(input  logic [31:0] a,
                     output logic [31:0] y);
  assign y = {a[29:0], 2'b0};

endmodule
```

VHDL

```
library IEEE;
use IEEE.STD_LOGIC_1164.all;

entity leftshift2_32 is
  port(a: in  STD_LOGIC_VECTOR(31 downto 0);
       y: out STD_LOGIC_VECTOR(31 downto 0));
end;

architecture synth of leftshift2_32 is
begin
  y <= a(29 downto 0) & "00";
end;
```

Exercise 5.15
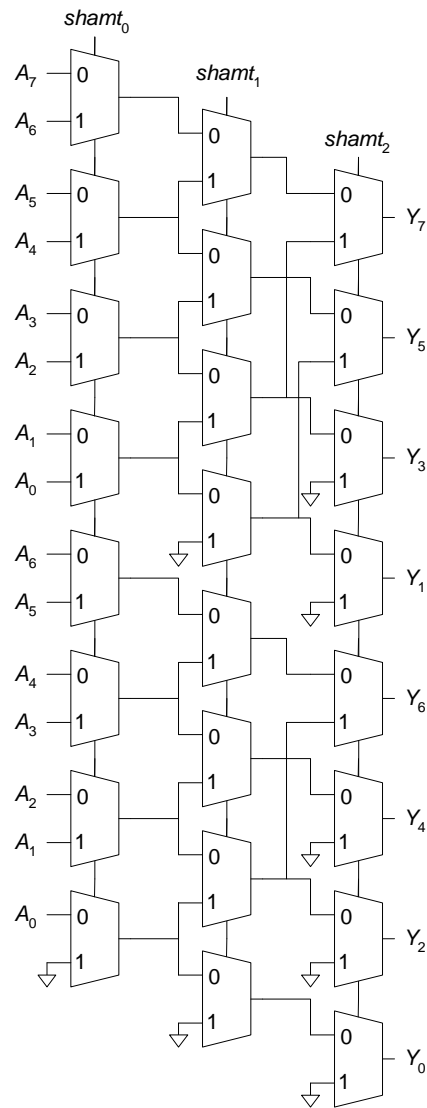
FIGURE 5.4 8-bit left shifter using 24 2:1 multiplexers

Exercise 5.17

(a) $B = 0$, $C = A$, $k = shamt$

(b) $B = A_{N-1}$ (the most significant bit of A), repeated N times to fill all N bits of B

(c) $B = A$, $C = 0$, $k = N$ - *shamt*
(d) $B = A$, $C = A$, $k =$ *shamt*
(e) $B = A$, $C = A$, $k = N$ - *shamt*

Exercise 5.19

$$t_{pd\_DIV4} = 4\,(4t_{FA} + t_{MUX}) = 16t_{FA} + 4t_{MUX}$$

$$t_{pd\_DIVN} = N^2 t_{FA} + N t_{MUX}$$

Exercise 5.21
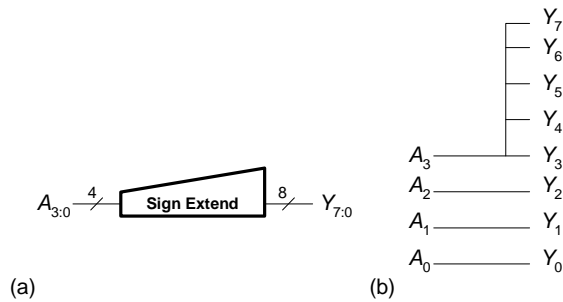
FIGURE 5.5 Sign extension unit (a) symbol, (b) underlying hardware

SystemVerilog

```
module signext4_8(input  logic [3:0] a,
                  output logic [7:0] y);

  assign y = { {4{a[3]}}, a};

endmodule
```

VHDL

```
library IEEE;
use IEEE.STD_LOGIC_1164.all;

entity signext4_8 is
  port(a: in  STD_LOGIC_VECTOR(3 downto 0);
       y: out STD_LOGIC_VECTOR(7 downto 0));
end;

architecture synth of signext4_8 is
begin
```

Exercise 5.23

```
                  100.110
          1100 │111001.000
              -1100↓↓ ↓│
               001001 0│
            -   110 0↓
                 11 00
            -    11 00
                    0
```

Exercise 5.25

(a) 1000 1101 . 1001 0000 = 0x8D90
(b) 0010 1010 . 0101 0000 = 0x2A50
(c) 1001 0001 . 0010 1000 = 0x9128

Exercise 5.27

(a) 1111 0010 . 0111 0000 = 0xF270
(b) 0010 1010 . 0101 0000 = 0x2A50
(c) 1110 1110 . 1101 1000 = 0xEED8

Exercise 5.29

(a) -1101.1001 = -1.1011001 $\times 2^3$
Thus, the biased exponent = 127 + 3 = 130 = 1000 0010$_2$
In IEEE 754 single-precision floating-point format:
1 1000 0010 101 1001 0000 0000 0000 0000 = **0xC1590000**

(b) 101010.0101 = 1.010100101 $\times 2^5$
Thus, the biased exponent = 127 + 5 = 132 = 1000 0100$_2$
In IEEE 754 single-precision floating-point format:
0 1000 0100 010 1001 0100 0000 0000 0000 = **0x42294000**

(c) -10001.00101 = -1.000100101 $\times 2^4$
Thus, the biased exponent = 127 + 4 = 131 = 1000 0011$_2$
In IEEE 754 single-precision floating-point format:
1 1000 0011 000 1001 0100 0000 0000 0000 = **0xC1894000**

Exercise 5.31

(a) 5.5

(b) $-0000.0001_2 = -0.0625$

(c) -8

Exercise 5.33

When adding two floating point numbers, the number with the smaller exponent is shifted to preserve the most significant bits. For example, suppose we were adding the two floating point numbers 1.0×2^0 and 1.0×2^{-27}. We make the two exponents equal by shifting the second number right by 27 bits. Because the mantissa is limited to 24 bits, the second number (1.000 0000 0000 0000 0000 $\times 2^{-27}$) becomes 0.000 0000 0000 0000 0000 $\times 2^0$, because the 1 is shifted off to the right. If we had shifted the number with the larger exponent (1.0×2^0) to the left, we would have shifted off the more significant bits (on the order of 2^0 instead of on the order of 2^{-27}).

Exercise 5.35

(a)
0xC0D20004 = 1 1000 0001 101 0010 0000 0000 0000 0100
$= -$ 1.101 0010 0000 0000 0000 01 $\times 2^2$
0x72407020 = 0 1110 0100 100 0000 0111 0000 0010 0000
$=$ 1.100 0000 0111 0000 001 $\times 2^{101}$

When adding these two numbers together, 0xC0D20004 becomes:

0×2^{101} because all of the significant bits shift off the right when making the exponents equal. Thus, the result of the addition is simply the second number:

0x72407020

(b)
0xC0D20004 = 1 1000 0001 101 0010 0000 0000 0000 0100
$= -$ 1.101 0010 0000 0000 0000 01 $\times 2^2$
0x40DC0004 = 0 1000 0001 101 1100 0000 0000 0000 0100
$=$ 1.101 1100 0000 0000 0000 01 $\times 2^2$

1.101 1100 0000 0000 0000 01 $\times 2^2$

$$- 1.101\ 0010\ 0000\ 0000\ 0000\ 01 \times 2^2$$
$$=\ 0.000\ 1010 \qquad\qquad\qquad \times 2^2$$
$$=\ 1.010 \times 2^{-2}$$

$$=\ 0\ 0111\ 1101\ 010\ 0000\ 0000\ 0000\ 0000\ 0000$$
$$=\ 0x3EA00000$$

(c)
$$0x5FBE4000 = 0\ 1011\ 1111\ 011\ 1110\ 0100\ 0000\ 0000\ 0000\ 0000$$
$$=\ 1.011\ 1110\ 01 \times 2^{64}$$
$$0x3FF80000 = 0\ 0111\ 1111\ 111\ 1000\ 0000\ 0000\ 0000\ 0000$$
$$=\ 1.111\ 1 \times 2^0$$
$$0xDFDE4000 = 1\ 1011\ 1111\ 101\ 1110\ 0100\ 0000\ 0000\ 0000\ 0000$$
$$=\ -\ 1.101\ 1110\ 01 \times 2^{64}$$

Thus, $(1.011\ 1110\ 01 \times 2^{64} + 1.111\ 1 \times 2^0) = 1.011\ 1110\ 01 \times 2^{64}$

And, $(1.011\ 1110\ 01 \times 2^{64} + 1.111\ 1 \times 2^0) - 1.101\ 1110\ 01 \times 2^{64} =$
$$-\ 0.01 \times 2^{64} = -1.0\ \times 2^{64}$$
$$=\ 1\ 1011\ 1101\ 000\ 0000\ 0000\ 0000\ 0000\ 0000$$
$$\mathbf{=\ 0xDE800000}$$

This is counterintuitive because the second number (0x3FF80000) does not affect the result because its order of magnitude is less than 2^{23} of the other numbers. This second number's significant bits are shifted off when the exponents are made equal.

Exercise 5.37

(a) $2(2^{31} - 1 - 2^{23}) = 2^{32} - 2 - 2^{24} = 4,278,190,078$
(b) $2(2^{31} - 1) = 2^{32} - 2 = 4,294,967,294$
(c) $\pm\infty$ and NaN are given special representations because they are often used in calculations and in representing results. These values also give useful information to the user as return values, instead of returning garbage upon overflow, underflow, or divide by zero.

Exercise 5.39
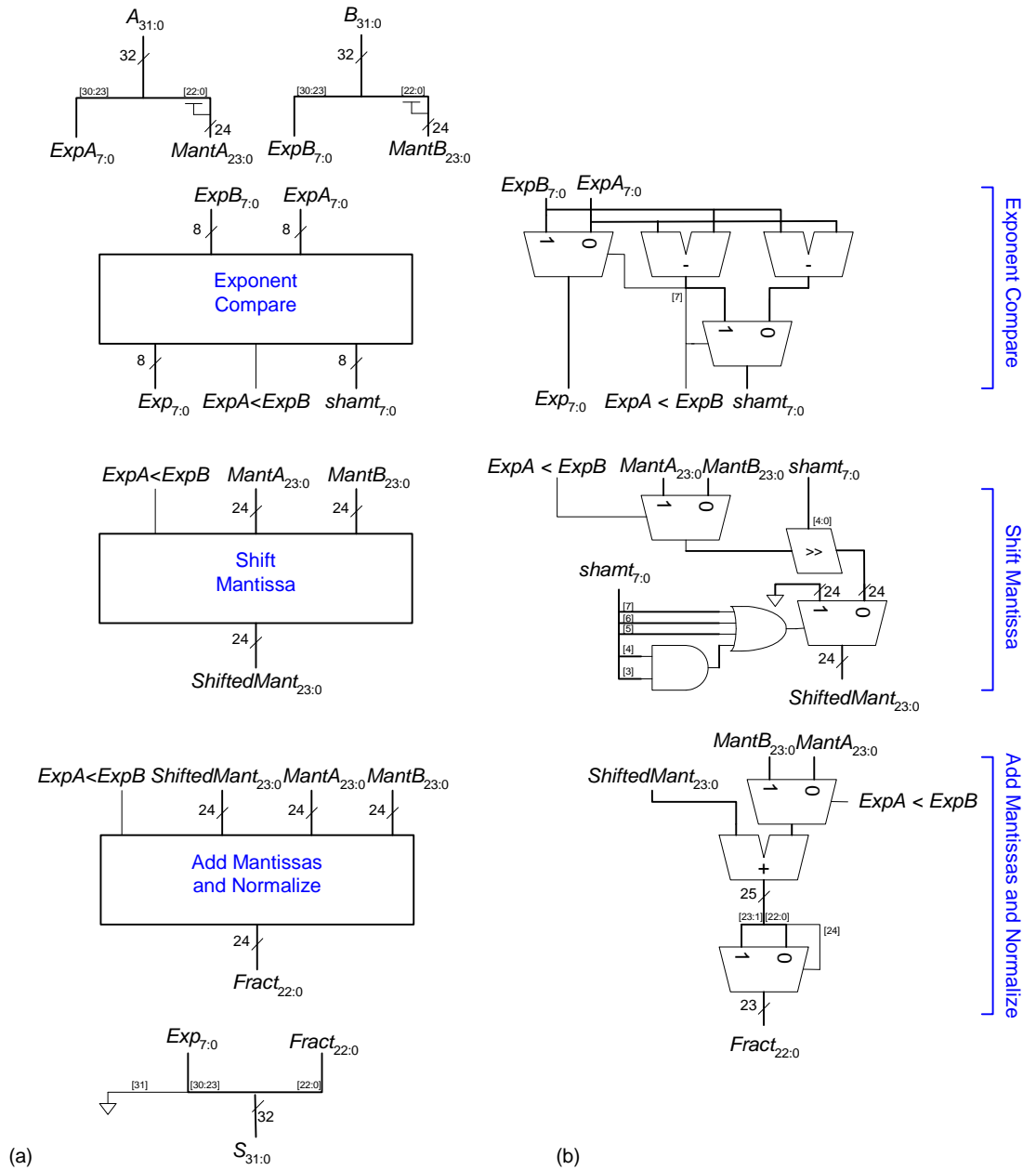
FIGURE 5.6 Floating-point adder hardware: (a) block diagram, (b) underlying hardware

SystemVerilog

```
module fpadd(input  logic [31:0] a, b,
             output logic [31:0] s);

  logic [7:0]  expa, expb, exp_pre, exp, shamt;
  logic        alessb;
  logic [23:0] manta, mantb, shmant;
  logic [22:0] fract;

  assign {expa, manta} = {a[30:23], 1'b1, a[22:0]};
  assign {expb, mantb} = {b[30:23], 1'b1, b[22:0]};
  assign s             = {1'b0, exp, fract};

  expcomp   expcomp1(expa, expb, alessb, exp_pre,
                     shamt);
  shiftmant shiftmant1(alessb, manta, mantb,
                       shamt, shmant);
  addmant   addmant1(alessb, manta, mantb,
                     shmant, exp_pre, fract, exp);

endmodule
```

VHDL

```
library IEEE; use IEEE.STD_LOGIC_1164.all;
use IEEE.STD_LOGIC_UNSIGNED.all;
use IEEE.STD_LOGIC_ARITH.all;

entity fpadd is
  port(a, b: in  STD_LOGIC_VECTOR(31 downto 0);
       s:    out STD_LOGIC_VECTOR(31 downto 0));
end;

architecture synth of fpadd is
  component expcomp
   port(expa, expb: in  STD_LOGIC_VECTOR(7 downto 0);
        alessb:     inout STD_LOGIC;
        exp,shamt:  out STD_LOGIC_VECTOR(7 downto 0));
  end component;

  component shiftmant
   port(alessb: in  STD_LOGIC;
        manta:  in  STD_LOGIC_VECTOR(23 downto 0);
        mantb:  in  STD_LOGIC_VECTOR(23 downto 0);
        shamt:  in  STD_LOGIC_VECTOR(7 downto 0);
        shmant: out STD_LOGIC_VECTOR(23 downto 0));
  end component;

  component addmant
   port(alessb:  in  STD_LOGIC;
        manta:   in  STD_LOGIC_VECTOR(23 downto 0);
        mantb:   in  STD_LOGIC_VECTOR(23 downto 0);
        shmant:  in  STD_LOGIC_VECTOR(23 downto 0);
        exp_pre: in  STD_LOGIC_VECTOR(7 downto 0);
        fract:   out STD_LOGIC_VECTOR(22 downto 0);
        exp:     out STD_LOGIC_VECTOR(7 downto 0));
  end component;

  signal expa, expb: STD_LOGIC_VECTOR(7 downto 0);
  signal exp_pre, exp: STD_LOGIC_VECTOR(7 downto 0);
  signal shamt: STD_LOGIC_VECTOR(7 downto 0);
  signal alessb: STD_LOGIC;
  signal manta: STD_LOGIC_VECTOR(23 downto 0);
  signal mantb: STD_LOGIC_VECTOR(23 downto 0);
  signal shmant: STD_LOGIC_VECTOR(23 downto 0);
  signal fract: STD_LOGIC_VECTOR(22 downto 0);
begin

  expa  <= a(30 downto 23);
  manta <= '1' & a(22 downto 0);
  expb  <= b(30 downto 23);
  mantb <= '1' & b(22 downto 0);

  s     <= '0' & exp & fract;

  expcomp1:  expcomp
    port map(expa, expb, alessb, exp_pre, shamt);
  shiftmant1: shiftmant
    port map(alessb, manta, mantb, shamt, shmant);
  addmant1: addmant
    port map(alessb, manta, mantb, shmant,
             exp_pre, fract, exp);

end;
```

(continued from previous page)

SystemVerilog

```
module expcomp(input  logic [7:0] expa, expb,
               output logic       alessb,
               output logic [7:0] exp, shamt);
  logic [7:0] aminusb, bminusa;

  assign aminusb = expa - expb;
  assign bminusa = expb - expa;
  assign alessb  = aminusb[7];

  always_comb
    if (alessb) begin
      exp = expb;
      shamt = bminusa;
    end
    else begin
      exp = expa;
      shamt = aminusb;
    end
endmodule
```

VHDL

```
library IEEE; use IEEE.STD_LOGIC_1164.all;
use IEEE.STD_LOGIC_UNSIGNED.all;
use IEEE.STD_LOGIC_ARITH.all;

entity expcomp is
  port(expa, expb: in  STD_LOGIC_VECTOR(7 downto 0);
       alessb:     inout STD_LOGIC;
       exp,shamt:  out STD_LOGIC_VECTOR(7 downto 0));
end;

architecture synth of expcomp is
  signal aminusb: STD_LOGIC_VECTOR(7 downto 0);
  signal bminusa: STD_LOGIC_VECTOR(7 downto 0);
begin
  aminusb <= expa - expb;
  bminusa <= expb - expa;
  alessb <= aminusb(7);

  exp <= expb when alessb = '1' else expa;
  shamt <= bminusa when alessb = '1' else aminusb;

end;
```

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SystemVerilog

```systemverilog
module shiftmant(input  logic alessb,
                 input  logic [23:0] manta, mantb,
                 input  logic [7:0] shamt,
                 output logic [23:0] shmant);

  logic [23:0] shiftedval;

  assign shiftedval = alessb ?
    (manta >> shamt) : (mantb >> shamt);

  always_comb
    if (shamt[7] | shamt[6] | shamt[5] |
        (shamt[4] & shamt[3]))
        shmant = 24'b0;
    else
        shmant = shiftedval;

endmodule


module addmant(input  logic        alessb,
               input  logic [23:0] manta,
                                   mantb, shmant,
               input  logic [7:0] exp_pre,
               output logic [22:0] fract,
               output logic [7:0]  exp);

  logic [24:0] addresult;
  logic [23:0] addval;

  assign addval    = alessb ? mantb : manta;
  assign addresult = shmant + addval;
  assign fract     = addresult[24] ?
                       addresult[23:1] :
                       addresult[22:0];

  assign exp       = addresult[24] ?
                       (exp_pre + 1) :
                       exp_pre;

endmodule
```

VHDL

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;
use ieee.numeric_std.all;
use IEEE.std_logic_unsigned.all;

entity shiftmant is
    port(alessb:  in  STD_LOGIC;
         manta:   in  STD_LOGIC_VECTOR(23 downto 0);
         mantb:   in  STD_LOGIC_VECTOR(23 downto 0);
         shamt:   in  STD_LOGIC_VECTOR(7 downto 0);
         shmant:  out STD_LOGIC_VECTOR(23 downto 0));
end;

architecture synth of shiftmant is
  signal shiftedval: unsigned (23 downto 0);
  signal shiftamt_vector: STD_LOGIC_VECTOR (7 downto
0);
begin

  shiftedval <= SHIFT_RIGHT( unsigned(manta), to_in-
teger(unsigned(shamt))) when alessb = '1'
          else SHIFT_RIGHT( unsigned(mantb), to_in-
teger(unsigned(shamt)));

  shmant <= X"000000" when (shamt > 22)
          else STD_LOGIC_VECTOR(shiftedval);
end;


library IEEE; use IEEE.STD_LOGIC_1164.all;
use IEEE.STD_LOGIC_UNSIGNED.all;
use IEEE.STD_LOGIC_ARITH.all;

entity addmant is
  port(alessb: in  STD_LOGIC;
       manta: in  STD_LOGIC_VECTOR(23 downto 0);
       mantb: in  STD_LOGIC_VECTOR(23 downto 0);
       shmant: in  STD_LOGIC_VECTOR(23 downto 0);
       exp_pre: in  STD_LOGIC_VECTOR(7 downto 0);
       fract: out STD_LOGIC_VECTOR(22 downto 0);
       exp: out  STD_LOGIC_VECTOR(7 downto 0));
end;

architecture synth of addmant is
  signal addresult: STD_LOGIC_VECTOR(24 downto 0);
  signal addval:    STD_LOGIC_VECTOR(23 downto 0);
begin
  addval <= mantb when alessb = '1' else manta;
  addresult <= ('0'&shmant) + addval;
  fract <= addresult(23 downto 1)
          when addresult(24) = '1'
          else addresult(22 downto 0);
  exp   <= (exp_pre + 1)
          when addresult(24) = '1'
          else exp_pre;

end;
```

Exercise 5.41

(a) Figure on next page
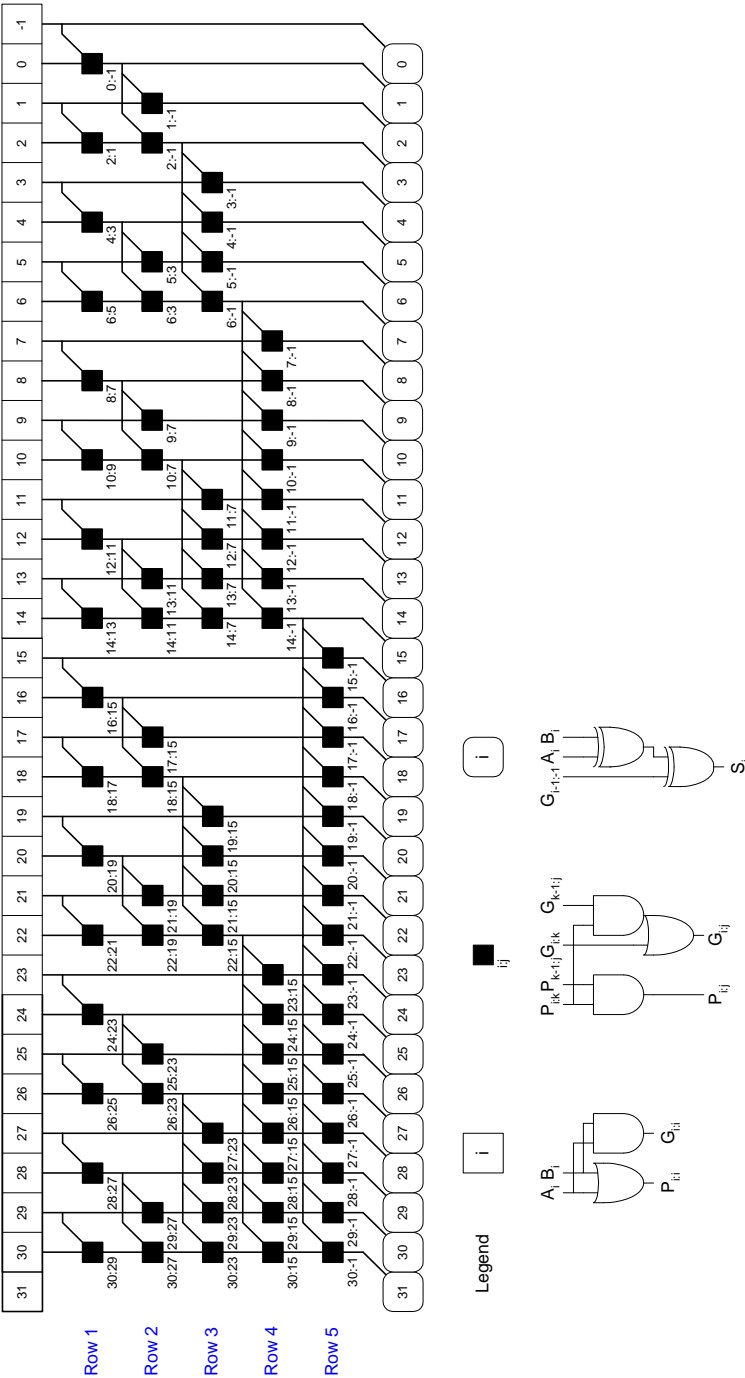
5.41 (b)

SystemVerilog

```systemverilog
module prefixadd(input  logic [31:0] a, b,
                 input  logic        cin,
                 output logic [31:0] s,
                 output logic        cout);

  logic [30:0] p, g;
  // p and g prefixes for rows 1 - 5
  logic [15:0] p1, p2, p3, p4, p5;
  logic [15:0] g1, g2, g3, g4, g5;

  pandg row0(a, b, p, g);
  blackbox row1({p[30],p[28],p[26],p[24],p[22],
                 p[20],p[18],p[16],p[14],p[12],
                 p[10],p[8],p[6],p[4],p[2],p[0]},
                {p[29],p[27],p[25],p[23],p[21],
                 p[19],p[17],p[15],p[13],p[11],
                 p[9],p[7],p[5],p[3],p[1],1'b0},
                {g[30],g[28],g[26],g[24],g[22],
                 g[20],g[18],g[16],g[14],g[12],
                 g[10],g[8],g[6],g[4],g[2],g[0]},
                {g[29],g[27],g[25],g[23],g[21],
                 g[19],g[17],g[15],g[13],g[11],
                 g[9],g[7],g[5],g[3],g[1],cin},
                 p1, g1);
```

VHDL

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity prefixadd is
  port(a, b: in  STD_LOGIC_VECTOR(31 downto 0);
       cin:  in  STD_LOGIC;
       s:    out STD_LOGIC_VECTOR(31 downto 0);
       cout: out STD_LOGIC);
end;

architecture synth of prefixadd is
  component pgblock
    port(a, b: in  STD_LOGIC_VECTOR(30 downto 0);
         p, g: out STD_LOGIC_VECTOR(30 downto 0));
  end component;

  component pgblackblock is
    port (pik, gik: in STD_LOGIC_VECTOR(15 downto 0);
          pkj, gkj: in STD_LOGIC_VECTOR(15 downto 0);
          pij: out STD_LOGIC_VECTOR(15 downto 0);
          gij: out STD_LOGIC_VECTOR(15 downto 0));
  end component;

  component sumblock is
    port (a, b, g: in  STD_LOGIC_VECTOR(31 downto 0);
          s:       out STD_LOGIC_VECTOR(31 downto 0));
  end component;

  signal p, g: STD_LOGIC_VECTOR(30 downto 0);
  signal pik_1, pik_2, pik_3, pik_4, pik_5,
         gik_1, gik_2, gik_3, gik_4, gik_5,
         pkj_1, pkj_2, pkj_3, pkj_4, pkj_5,
         gkj_1, gkj_2, gkj_3, gkj_4, gkj_5,
         p1, p2, p3, p4, p5,
         g1, g2, g3, g4, g5:
                 STD_LOGIC_VECTOR(15 downto 0);
  signal g6:   STD_LOGIC_VECTOR(31 downto 0);

begin
  row0: pgblock
    port map(a(30 downto 0), b(30 downto 0), p, g);

  pik_1 <=
   (p(30)&p(28)&p(26)&p(24)&p(22)&p(20)&p(18)&p(16)&
    p(14)&p(12)&p(10)&p(8)&p(6)&p(4)&p(2)&p(0));
  gik_1 <=
   (g(30)&g(28)&g(26)&g(24)&g(22)&g(20)&g(18)&g(16)&
    g(14)&g(12)&g(10)&g(8)&g(6)&g(4)&g(2)&g(0));
  pkj_1 <=
   (p(29)&p(27)&p(25)&p(23)&p(21)&p(19)&p(17)&p(15)&
    p(13)&p(11)&p(9)&p(7)&p(5)&p(3)&p(1)&'0');
  gkj_1 <=
   (g(29)&g(27)&g(25)&g(23)&g(21)&g(19)&g(17)&g(15)&
    g(13)&g(11)&g(9)&g(7)&g(5)& g(3)& g(1)& cin);

  row1: pgblackblock
        port map(pik_1, gik_1, pkj_1, gkj_1,
                 p1, g1);
```

(continued from previous page)

SystemVerilog   **VHDL**

```
blackbox row2({p1[15],p29],p1[13],p[25],p1[11],
              p[21],p1[9],p[17],p1[7],p[13],
              p1[5],p[9],p1[3],p[5],p1[1],p[1]},
             {{2{p1[14]}},{2{p1[12]}},{2{p1[10]}},
              {2{p1[8]}},{2{p1[6]}},{2{p1[4]}},
              {2{p1[2]}},{2{p1[0]}}},
             {g1[15],g29],g1[13],g[25],g1[11],
              g[21],g1[9],g[17],g1[7],g[13],
              g1[5],g[9],g1[3],g[5],g1[1],g[1]},
             {{2{g1[14]}},{2{g1[12]}},{2{g1[10]}},
              {2{g1[8]}},{2{g1[6]}},{2{g1[4]}},
              {2{g1[2]}},{2{g1[0]}}},
              p2, g2);

blackbox row3({p2[15],p2[14],p1[14],p[27],p2[11],
              p2[10],p1[10],p[19],p2[7],p2[6],
              p1[6],p[11],p2[3],p2[2],p1[2],p[3]},
             {{4{p2[13]}},{4{p2[9]}},{4{p2[5]}},
              {4{p2[1]}}},
             {g2[15],g2[14],g1[14],g[27],g2[11],
              g2[10],g1[10],g[19],g2[7],g2[6],
              g1[6],g[11],g2[3],g2[2],g1[2],g[3]},
             {{4{g2[13]}},{4{g2[9]}},{4{g2[5]}},
              {4{g2[1]}}},
              p3, g3);
```

```
pik_2 <= p1(15)&p(29)&p1(13)&p(25)&p1(11)&
         p(21)&p1(9)&p(17)&p1(7)&p(13)&
         p1(5)&p(9)&p1(3)&p(5)&p1(1)&p(1);

gik_2 <= g1(15)&g(29)&g1(13)&g(25)&g1(11)&
         g(21)&g1(9)&g(17)&g1(7)&g(13)&
         g1(5)&g(9)&g1(3)&g(5)&g1(1)&g(1);

pkj_2 <=
         p1(14)&p1(14)&p1(12)&p1(12)&p1(10)&p1(10)&
         p1(8)&p1(8)&p1(6)&p1(6)&p1(4)&p1(4)&
         p1(2)&p1(2)&p1(0)&p1(0);

gkj_2 <=
         g1(14)&g1(14)&g1(12)&g1(12)&g1(10)&g1(10)&
         g1(8)&g1(8)&g1(6)&g1(6)&g1(4)&g1(4)&
         g1(2)&g1(2)&g1(0)&g1(0);

row2: pgblackblock
      port map(pik_2, gik_2, pkj_2, gkj_2,
               p2, g2);

pik_3 <= p2(15)&p2(14)&p1(14)&p(27)&p2(11)&
         p2(10)&p1(10)&p(19)&p2(7)&p2(6)&
         p1(6)&p(11)&p2(3)&p2(2)&p1(2)&p(3);
gik_3 <= g2(15)&g2(14)&g1(14)&g(27)&g2(11)&
         g2(10)&g1(10)&g(19)&g2(7)&g2(6)&
         g1(6)&g(11)&g2(3)&g2(2)&g1(2)&g(3);
pkj_3 <= p2(13)&p2(13)&p2(13)&p2(13)&
         p2(9)&p2(9)&p2(9)&p2(9)&
         p2(5)&p2(5)&p2(5)&p2(5)&
         p2(1)&p2(1)&p2(1)&p2(1);
gkj_3 <= g2(13)&g2(13)&g2(13)&g2(13)&
         g2(9)&g2(9)&g2(9)&g2(9)&
         g2(5)&g2(5)&g2(5)&g2(5)&
         g2(1)&g2(1)&g2(1)&g2(1);

row3: pgblackblock
      port map(pik_3, gik_3, pkj_3, gkj_3, p3, g3);
```

SystemVerilog

```
blackbox row4({p3[15:12],p2[13:12],
              p1[12],p[23],p3[7:4],
              p2[5:4],p1[4],p[7]},
              {{8{p3[11]}},{8{p3[3]}}},
              {g3[15:12],g2[13:12],
              g1[12],g[23],g3[7:4],
              g2[5:4],g1[4],g[7]},
              {{8{g3[11]}},{8{g3[3]}}},
              p4, g4);

blackbox row5({p4[15:8],p3[11:8],p2[9:8],
              p1[8],p[15]},
              {{16{p4[7]}}},
              {g4[15:8],g3[11:8],g2[9:8],
              g1[8],g[15]},
              {{16{g4[7]}}},
              p5,g5);

sum row6({g5,g4[7:0],g3[3:0],g2[1:0],g1[0],cin},
         a, b, s);

// generate cout
assign cout = (a[31] & b[31]) |
              (g5[15] & (a[31] | b[31]));

endmodule
```

VHDL

```
pik_4 <= p3(15 downto 12)&p2(13 downto 12)&
         p1(12)&p(23)&p3(7 downto 4)&
         p2(5 downto 4)&p1(4)&p(7);
gik_4 <= g3(15 downto 12)&g2(13 downto 12)&
         g1(12)&g(23)&g3(7 downto 4)&
         g2(5 downto 4)&g1(4)&g(7);
pkj_4 <= p3(11)&p3(11)&p3(11)&p3(11)&
         p3(11)&p3(11)&p3(11)&p3(11)&
         p3(3)&p3(3)&p3(3)&p3(3)&
         p3(3)&p3(3)&p3(3)&p3(3);
gkj_4 <= g3(11)&g3(11)&g3(11)&g3(11)&
         g3(11)&g3(11)&g3(11)&g3(11)&
         g3(3)&g3(3)&g3(3)&g3(3)&
         g3(3)&g3(3)&g3(3)&g3(3);

row4: pgblackblock
     port map(pik_4, gik_4, pkj_4, gkj_4, p4, g4);

pik_5 <= p4(15 downto 8)&p3(11 downto 8)&
         p2(9 downto 8)&p1(8)&p(15);
gik_5 <= g4(15 downto 8)&g3(11 downto 8)&
         g2(9 downto 8)&g1(8)&g(15);
pkj_5 <= p4(7)&p4(7)&p4(7)&p4(7)&
         p4(7)&p4(7)&p4(7)&p4(7)&
         p4(7)&p4(7)&p4(7)&p4(7)&
         p4(7)&p4(7)&p4(7)&p4(7);
         gkj_5 <= g4(7)&g4(7)&g4(7)&g4(7)&
         g4(7)&g4(7)&g4(7)&g4(7)&
         g4(7)&g4(7)&g4(7)&g4(7)&
         g4(7)&g4(7)&g4(7)&g4(7);

row5: pgblackblock
     port map(pik_5, gik_5, pkj_5, gkj_5, p5, g5);

g6 <= (g5 & g4(7 downto 0) & g3(3 downto 0) &
      g2(1 downto 0) & g1(0) & cin);

row6: sumblock
     port map(g6, a, b, s);

-- generate cout
cout <= (a(31) and b(31)) or
        (g6(31) and (a(31) or b(31)));

end;
```

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(continued from previous page)

SystemVerilog

```systemverilog
module pandg(input  logic [30:0] a, b,
             output logic [30:0] p, g);

  assign p = a | b;
  assign g = a & b;

endmodule

module blackbox(input  logic [15:0] pleft, pright,
                                    gleft, gright,
                output logic [15:0] pnext, gnext);

  assign pnext = pleft & pright;
  assign gnext = pleft & gright | gleft;
endmodule


module sum(input  logic [31:0] g, a, b,
           output logic [31:0] s);

  assign s = a ^ b ^ g;

endmodule
```

VHDL

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity pgblock is
  port(a, b: in  STD_LOGIC_VECTOR(30 downto 0);
       p, g: out STD_LOGIC_VECTOR(30 downto 0));
end;

architecture synth of pgblock is
begin
  p <= a or b;
  g <= a and b;
end;


library IEEE; use IEEE.STD_LOGIC_1164.all;

entity pgblackblock is
  port(pik, gik, pkj, gkj:
         in  STD_LOGIC_VECTOR(15 downto 0);
       pij, gij:
         out STD_LOGIC_VECTOR(15 downto 0));
end;

architecture synth of pgblackblock is
begin
  pij <= pik and pkj;
  gij <= gik or (pik and gkj);
end;


library IEEE; use IEEE.STD_LOGIC_1164.all;

entity sumblock is
  port(g, a, b: in  STD_LOGIC_VECTOR(31 downto 0);
       s:       out STD_LOGIC_VECTOR(31 downto 0));
end;


architecture synth of sumblock is
begin
  s <= a xor b xor g;
end;
```

5.41 (c) Using Equation 5.11 to find the delay of the prefix adder:

$$t_{PA} = t_{pg} + \log_2 N(t_{pg\_prefix}) + t_{XOR}$$

We find the delays for each block:
$t_{pg} = 100$ ps
$t_{pg\_prefix} = 200$ ps
$t_{XOR} = 100$ ps

Thus,
$t_{PA} = [100 + 5(200) + 100]$ ps $= 1200$ ps $= \mathbf{1.2\ ns}$

5.41 (d) To make a pipelined prefix adder, add pipeline registers between each of the rows of the prefix adder. Now each stage will take 200 ps plus the

sequencing overhead, $t_{pq} + t_{setup}$= 80ps. Thus each cycle is 280 ps and the design can run at 3.57 GHz.
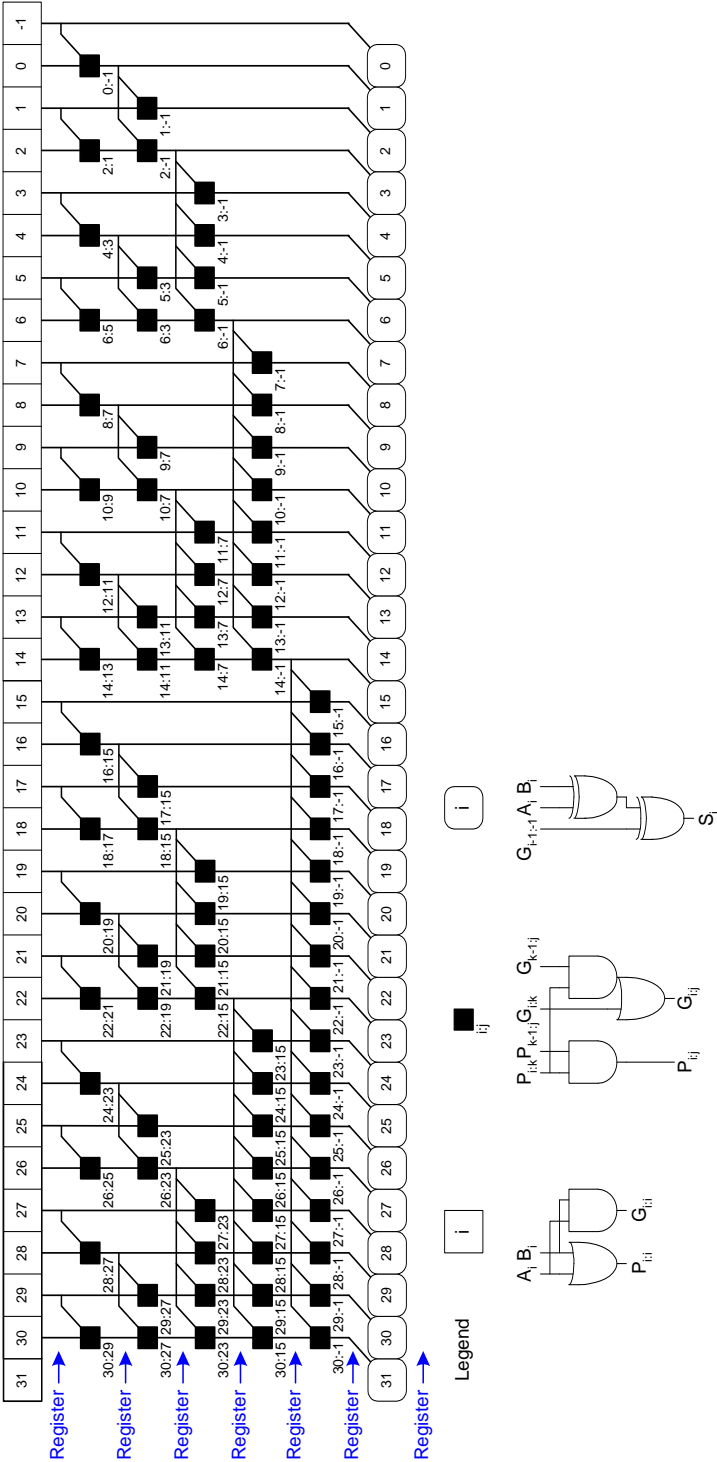
5.41 (e)

SystemVerilog

```
module prefixaddpipe(input  logic       clk, cin,
                     input  logic [31:0] a, b,
                     output logic [31:0] s, output cout);

  // p and g prefixes for rows 0 - 5
  logic [30:0] p0, p1, p2, p3, p4, p5;
  logic [30:0] g0, g1, g2, g3, g4, g5;
  logic p_1_0, p_1_1, p_1_2, p_1_3, p_1_4, p_1_5,
        g_1_0, g_1_1, g_1_2, g_1_3, g_1_4, g_1_5;

  // pipeline values for a and b
  logic [31:0] a0, a1, a2, a3, a4, a5,
               b0, b1, b2, b3, b4, b5;

  // row 0
  flop #(2) flop0_pg_1(clk, {1'b0,cin}, {p_1_0,g_1_0});
  pandg row0(clk, a[30:0], b[30:0], p0, g0);

  // row 1
  flop #(2)  flop1_pg_1(clk, {p_1_0,g_1_0}, {p_1_1,g_1_1});
                              flop          #(30)          flop1_pg(clk,
{p0[29],p0[27],p0[25],p0[23],p0[21],p0[19],p0[17],p0[15],
                              p0[13],p0[11],p0[9],p0[7],p0[5],p0[3],p0[1],

g0[29],g0[27],g0[25],g0[23],g0[21],g0[19],g0[17],g0[15],
                              g0[13],g0[11],g0[9],g0[7],g0[5],g0[3],g0[1]},
{p1[29],p1[27],p1[25],p1[23],p1[21],p1[19],p1[17],p1[15],
                              p1[13],p1[11],p1[9],p1[7],p1[5],p1[3],p1[1],

g1[29],g1[27],g1[25],g1[23],g1[21],g1[19],g1[17],g1[15],
                              g1[13],g1[11],g1[9],g1[7],g1[5],g1[3],g1[1]});

  blackbox row1(clk,
 {p0[30],p0[28],p0[26],p0[24],p0[22],
                 p0[20],p0[18],p0[16],p0[14],p0[12],
                 p0[10],p0[8],p0[6],p0[4],p0[2],p0[0]},

                {p0[29],p0[27],p0[25],p0[23],p0[21],
                 p0[19],p0[17],p0[15],p0[13],p0[11],
                 p0[9],p0[7],p0[5],p0[3],p0[1],1'b0},

                {g0[30],g0[28],g0[26],g0[24],g0[22],
                 g0[20],g0[18],g0[16],g0[14],g0[12],
                 g0[10],g0[8],g0[6],g0[4],g0[2],g0[0]},

                {g0[29],g0[27],g0[25],g0[23],g0[21],
                 g0[19],g0[17],g0[15],g0[13],g0[11],
                 g0[9],g0[7],g0[5],g0[3],g0[1],g_1_0},

                {p1[30],p1[28],p1[26],p1[24],p1[22],p1[20],
 p1[18],p1[16],p1[14],p1[12],p1[10],p1[8],
 p1[6],p1[4],p1[2],p1[0]},

                {g1[30],g1[28],g1[26],g1[24],g1[22],g1[20],
 g1[18],g1[16],g1[14],g1[12],g1[10],g1[8],
 g1[6],g1[4],g1[2],g1[0]});

  // row 2
  flop #(2)  flop2_pg_1(clk, {p_1_1,g_1_1}, {p_1_2,g_1_2});
                              flop              #(30)          flop2_pg(clk,
{p1[28:27],p1[24:23],p1[20:19],p1[16:15],p1[12:11],
```

```
                                   p1[8:7],p1[4:3],p1[0],
   g1[28:27],g1[24:23],g1[20:19],g1[16:15],g1[12:11],
   g1[8:7],g1[4:3],g1[0]},
    {p2[28:27],p2[24:23],p2[20:19],p2[16:15],p2[12:11],
                                   p2[8:7],p2[4:3],p2[0],
    g2[28:27],g2[24:23],g2[20:19],g2[16:15],g2[12:11],
    g2[8:7],g2[4:3],g2[0]}});
     blackbox row2(clk,

   {p1[30:29],p1[26:25],p1[22:21],p1[18:17],p1[14:13],p1[10:9],p1[6:5],p1[2:1]
   },

     {  {2{p1[28]}},  {2{p1[24]}},  {2{p1[20]}},  {2{p1[16]}},  {2{p1[12]}},
   {2{p1[8]}},
      {2{p1[4]}}, {2{p1[0]}} },


   {g1[30:29],g1[26:25],g1[22:21],g1[18:17],g1[14:13],g1[10:9],g1[6:5],g1[2:1]
   },

     {  {2{g1[28]}},  {2{g1[24]}},  {2{g1[20]}},  {2{g1[16]}},  {2{g1[12]}},
   {2{g1[8]}},
      {2{g1[4]}}, {2{g1[0]}} },


   {p2[30:29],p2[26:25],p2[22:21],p2[18:17],p2[14:13],p2[10:9],p2[6:5],p2[2:1]
   },


   {g2[30:29],g2[26:25],g2[22:21],g2[18:17],g2[14:13],g2[10:9],g2[6:5],g2[2:1]
   } );

     // row 3
     flop #(2)  flop3_pg_1(clk, {p_1_2,g_1_2}, {p_1_3,g_1_3});
     flop #(30) flop3_pg(clk, {p2[26:23],p2[18:15],p2[10:7],p2[2:0],
   g2[26:23],g2[18:15],g2[10:7],g2[2:0]},
   {p3[26:23],p3[18:15],p3[10:7],p3[2:0],
   g3[26:23],g3[18:15],g3[10:7],g3[2:0]});
     blackbox row3(clk,
               {p2[30:27],p2[22:19],p2[14:11],p2[6:3]},
   { {4{p2[26]}}, {4{p2[18]}}, {4{p2[10]}}, {4{p2[2]}} },
   {g2[30:27],g2[22:19],g2[14:11],g2[6:3]},
   { {4{g2[26]}}, {4{g2[18]}}, {4{g2[10]}}, {4{g2[2]}} },
   {p3[30:27],p3[22:19],p3[14:11],p3[6:3]},
   {g3[30:27],g3[22:19],g3[14:11],g3[6:3]});

     // row 4
     flop #(2)  flop4_pg_1(clk, {p_1_3,g_1_3}, {p_1_4,g_1_4});
     flop #(30) flop4_pg(clk, {p3[22:15],p3[6:0],
   g3[22:15],g3[6:0]},
                              {p4[22:15],p4[6:0],
   g4[22:15],g4[6:0]});

     blackbox row4(clk,
               {p3[30:23],p3[14:7]},
   { {8{p3[22]}}, {8{p3[6]}} },
               {g3[30:23],g3[14:7]},
   { {8{g3[22]}}, {8{g3[6]}} },
   {p4[30:23],p4[14:7]},
   {g4[30:23],g4[14:7]});

     // row 5
     flop #(2)  flop5_pg_1(clk, {p_1_4,g_1_4}, {p_1_5,g_1_5});
     flop #(30) flop5_pg(clk, {p4[14:0],g4[14:0]},
                              {p5[14:0],g5[14:0]});
```

```
  blackbox row5(clk,
                p4[30:15],
 {16{p4[14]}},
 g4[30:15],
 {16{g4[14]}},
 p5[30:15], g5[30:15]);

  // pipeline registers for a and b
  flop #(64) flop0_ab(clk, {a,b}, {a0,b0});
  flop #(64) flop1_ab(clk, {a0,b0}, {a1,b1});
  flop #(64) flop2_ab(clk, {a1,b1}, {a2,b2});
  flop #(64) flop3_ab(clk, {a2,b2}, {a3,b3});
  flop #(64) flop4_ab(clk, {a3,b3}, {a4,b4});
  flop #(64) flop5_ab(clk, {a4,b4}, {a5,b5});

  sum row6(clk, {g5,g_1_5}, a5, b5, s);
  // generate cout
  assign cout = (a5[31] & b5[31]) | (g5[30] & (a5[31] | b5[31]));
endmodule

// submodules
module pandg(input  logic       clk,
             input  logic [30:0] a, b,
             output logic [30:0] p, g);

  always_ff @(posedge clk)
  begin
    p <= a | b;
    g <= a & b;
  end

endmodule

module blackbox(input  logic clk,
                input  logic [15:0] pleft, pright, gleft, gright,
                output logic [15:0] pnext, gnext);

  always_ff @(posedge clk)
  begin
    pnext <= pleft & pright;
    gnext <= pleft & gright | gleft;
  end
endmodule


module sum(input  logic       clk,
           input  logic [31:0] g, a, b,
           output logic [31:0] s);

  always_ff @(posedge clk)
    s <= a ^ b ^ g;
endmodule

module flop
  #(parameter width = 8)
  (input  logic          clk,
   input  logic [width-1:0] d,
   output logic [width-1:0] q);

  always_ff @(posedge clk)
    q <= d;
endmodule
```

5.41 (e)

VHDL

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity prefixaddpipe is
  port(clk: in  STD_LOGIC;
       a, b: in  STD_LOGIC_VECTOR(31 downto 0);
       cin:  in  STD_LOGIC;
       s:    out STD_LOGIC_VECTOR(31 downto 0);
       cout: out STD_LOGIC);
end;

architecture synth of prefixaddpipe is
  component pgblock
    port(clk:  in  STD_LOGIC;
         a, b: in  STD_LOGIC_VECTOR(30 downto 0);
         p, g: out STD_LOGIC_VECTOR(30 downto 0));
  end component;
  component sumblock is
    port (clk:      in  STD_LOGIC;
          a, b, g: in  STD_LOGIC_VECTOR(31 downto 0);
          s:           out STD_LOGIC_VECTOR(31 downto 0));
  end component;
  component flop is generic(width: integer);
    port(clk: in  STD_LOGIC;
         d:   in  STD_LOGIC_VECTOR(width-1 downto 0);
         q:   out STD_LOGIC_VECTOR(width-1 downto 0));
  end component;
  component flop1 is
    port(clk:        in  STD_LOGIC;
         d:          in  STD_LOGIC;
         q:          out STD_LOGIC);
  end component;
  component row1 is
    port(clk:  in  STD_LOGIC;
         p0, g0: in  STD_LOGIC_VECTOR(30 downto 0);
         p_1_0, g_1_0: in STD_LOGIC;
         p1, g1: out STD_LOGIC_VECTOR(30 downto 0));
  end component;
  component row2 is
    port(clk:  in  STD_LOGIC;
         p1, g1: in  STD_LOGIC_VECTOR(30 downto 0);
         p2, g2: out STD_LOGIC_VECTOR(30 downto 0));
  end component;
  component row3 is
    port(clk:  in  STD_LOGIC;
         p2, g2: in  STD_LOGIC_VECTOR(30 downto 0);
         p3, g3: out STD_LOGIC_VECTOR(30 downto 0));
  end component;
  component row4 is
    port(clk:  in  STD_LOGIC;
         p3, g3: in  STD_LOGIC_VECTOR(30 downto 0);
         p4, g4: out STD_LOGIC_VECTOR(30 downto 0));
  end component;
  component row5 is
    port(clk:  in  STD_LOGIC;
         p4, g4: in  STD_LOGIC_VECTOR(30 downto 0);
         p5, g5: out STD_LOGIC_VECTOR(30 downto 0));
  end component;
```

```
  -- p and g prefixes for rows 0 - 5
  signal p0, p1, p2, p3, p4, p5: STD_LOGIC_VECTOR(30 downto 0);
  signal g0, g1, g2, g3, g4, g5: STD_LOGIC_VECTOR(30 downto 0);

  -- p and g prefixes for column -1, rows 0 - 5
  signal p_1_0, p_1_1, p_1_2, p_1_3, p_1_4, p_1_5,
         g_1_0, g_1_1, g_1_2, g_1_3, g_1_4, g_1_5: STD_LOGIC;

  -- pipeline values for a and b
  signal a0, a1, a2, a3, a4, a5,
         b0, b1, b2, b3, b4, b5: STD_LOGIC_VECTOR(31 downto 0);

  -- final generate signal
  signal g5_all: STD_LOGIC_VECTOR(31 downto 0);

begin

  -- p and g calculations
  row0_reg: pgblock port map(clk, a(30 downto 0), b(30 downto 0), p0, g0);
  row1_reg: row1 port map(clk, p0, g0, p_1_0, g_1_0, p1, g1);
  row2_reg: row2 port map(clk, p1, g1, p2, g2);
  row3_reg: row3 port map(clk, p2, g2, p3, g3);
  row4_reg: row4 port map(clk, p3, g3, p4, g4);
  row5_reg: row5 port map(clk, p4, g4, p5, g5);


  -- pipeline registers for a and b
  flop0_a: flop generic map(32) port map (clk, a, a0);
  flop0_b: flop generic map(32) port map (clk, b, b0);
  flop1_a: flop generic map(32) port map (clk, a0, a1);
  flop1_b: flop generic map(32) port map (clk, b0, b1);
  flop2_a: flop generic map(32) port map (clk, a1, a2);
  flop2_b: flop generic map(32) port map (clk, b1, b2);
  flop3_a: flop generic map(32) port map (clk, a2, a3);
  flop3_b: flop generic map(32) port map (clk, b2, b3);
  flop4_a: flop generic map(32) port map (clk, a3, a4);
  flop4_b: flop generic map(32) port map (clk, b3, b4);
  flop5_a: flop generic map(32) port map (clk, a4, a5);
  flop5_b: flop generic map(32) port map (clk, b4, b5);

  -- pipeline p and g for column -1
  p_1_0 <= '0'; flop_1_g0: flop1 port map (clk, cin, g_1_0);
  flop_1_p1: flop1 port map (clk, p_1_0, p_1_1);
  flop_1_g1: flop1 port map (clk, g_1_0, g_1_1);
  flop_1_p2: flop1 port map (clk, p_1_1, p_1_2);
  flop_1_g2: flop1 port map (clk, g_1_1, g_1_2);
  flop_1_p3: flop1 port map (clk, p_1_2, p_1_3); flop_1_g3:
  flop1 port map (clk, g_1_2, g_1_3);
  flop_1_p4: flop1 port map (clk, p_1_3, p_1_4);
  flop_1_g4: flop1 port map (clk, g_1_3, g_1_4);
  flop_1_p5: flop1 port map (clk, p_1_4, p_1_5);
  flop_1_g5: flop1 port map (clk, g_1_4, g_1_5);

  -- generate sum and cout
  g5_all <= (g5&g_1_5);
  row6: sumblock port map(clk, g5_all, a5, b5, s);

  -- generate cout
  cout <= (a5(31) and b5(31)) or (g5(30) and (a5(31) or b5(31)));
end;


library IEEE; use IEEE.STD_LOGIC_1164.all;
entity pgblock is
  port(clk:  in  STD_LOGIC;
```

```
          a, b: in  STD_LOGIC_VECTOR(30 downto 0);
          p, g: out STD_LOGIC_VECTOR(30 downto 0));
end;

architecture synth of pgblock is
begin
  process(clk) begin
    if rising_edge(clk) then
       p <= a or b;
       g <= a and b;
    end if;
  end process;
end;


library IEEE; use IEEE.STD_LOGIC_1164.all;

entity blackbox is
  port(clk:  in  STD_LOGIC;
       pik, pkj, gik, gkj:
             in  STD_LOGIC_VECTOR(15 downto 0);
       pij, gij:
             out STD_LOGIC_VECTOR(15 downto 0));
end;

architecture synth of blackbox is
begin
  process(clk) begin
    if rising_edge(clk) then
      pij <= pik and pkj;
      gij <= gik or (pik and gkj);
    end if;
  end process;
end;


library IEEE; use IEEE.STD_LOGIC_1164.all;

entity sumblock is
  port(clk:  in  STD_LOGIC;
       g, a, b: in  STD_LOGIC_VECTOR(31 downto 0);
       s:        out STD_LOGIC_VECTOR(31 downto 0));
end;

architecture synth of sumblock is
begin
  process(clk) begin
    if rising_edge(clk) then
      s <= a xor b xor g;
    end if;
  end process;
end;

library IEEE; use IEEE.STD_LOGIC_1164.all;  use IEEE.STD_LOGIC_ARITH.all;
entity flop is -- parameterizable flip flop
  generic(width: integer);
  port(clk:        in  STD_LOGIC;
       d:          in  STD_LOGIC_VECTOR(width-1 downto 0);
       q:          out STD_LOGIC_VECTOR(width-1 downto 0));
end;

architecture synth of flop is
begin
  process(clk) begin
    if rising_edge(clk) then
      q <= d;
```

```vhdl
    end if;
  end process;
end;


library IEEE; use IEEE.STD_LOGIC_1164.all;  use IEEE.STD_LOGIC_ARITH.all;
entity flop1 is -- 1-bit flip flop
  port(clk:        in  STD_LOGIC;
       d:          in  STD_LOGIC;
       q:          out STD_LOGIC);
end;


architecture synth of flop1 is
begin
  process(clk) begin
    if rising_edge(clk) then
      q <= d;
    end if;
  end process;
end;


library IEEE; use IEEE.STD_LOGIC_1164.all;

entity row1 is
  port(clk:    in STD_LOGIC;
       p0, g0: in  STD_LOGIC_VECTOR(30 downto 0);
       p_1_0, g_1_0: in STD_LOGIC;
       p1, g1: out STD_LOGIC_VECTOR(30 downto 0));
end;

architecture synth of row1 is
  component blackbox is
    port (clk:        in  STD_LOGIC;
          pik, pkj: in STD_LOGIC_VECTOR(15 downto 0);
          gik, gkj: in STD_LOGIC_VECTOR(15 downto 0);
          pij:        out STD_LOGIC_VECTOR(15 downto 0);
          gij:        out STD_LOGIC_VECTOR(15 downto 0));
  end component;
  component flop is generic(width: integer);
    port(clk: in  STD_LOGIC;
         d:   in  STD_LOGIC_VECTOR(width-1 downto 0);
         q:   out STD_LOGIC_VECTOR(width-1 downto 0));
  end component;

  -- internal signals for calculating p, g
  signal pik_0, gik_0, pkj_0, gkj_0,
         pij_0, gij_0: STD_LOGIC_VECTOR(15 downto 0);

  -- internal signals for pipeline registers
  signal pg0_in, pg1_out: STD_LOGIC_VECTOR(29 downto 0);

begin
  pg0_in <= (p0(29)&p0(27)&p0(25)&p0(23)&p0(21)&p0(19)&p0(17)&p0(15)&
                p0(13)&p0(11)&p0(9)&p0(7)&p0(5)&p0(3)&p0(1)&
                g0(29)&g0(27)&g0(25)&g0(23)&g0(21)&g0(19)&g0(17)&g0(15)&
                g0(13)&g0(11)&g0(9)&g0(7)&g0(5)&g0(3)&g0(1));
  flop1_pg: flop generic map(30) port map (clk, pg0_in, pg1_out);

  p1(29) <= pg1_out(29); p1(27)<= pg1_out(28); p1(25)<= pg1_out(27);
  p1(23) <= pg1_out(26);
  p1(21) <= pg1_out(25); p1(19) <= pg1_out(24); p1(17) <= pg1_out(23);
  p1(15) <= pg1_out(22); p1(13) <= pg1_out(21); p1(11) <= pg1_out(20);
  p1(9) <= pg1_out(19); p1(7) <= pg1_out(18); p1(5) <= pg1_out(17);
  p1(3) <= pg1_out(16); p1(1) <= pg1_out(15);
  g1(29) <= pg1_out(14); g1(27) <= pg1_out(13); g1(25) <= pg1_out(12);
  g1(23) <= pg1_out(11); g1(21) <= pg1_out(10); g1(19) <= pg1_out(9);
  g1(17) <= pg1_out(8); g1(15) <= pg1_out(7); g1(13) <= pg1_out(6);
```

```
            g1(11) <= pg1_out(5); g1(9) <= pg1_out(4); g1(7) <= pg1_out(3);
            g1(5) <= pg1_out(2); g1(3) <= pg1_out(1); g1(1) <= pg1_out(0);

            -- pg calculations
            pik_0 <= (p0(30)&p0(28)&p0(26)&p0(24)&p0(22)&p0(20)&p0(18)&p0(16)&
                      p0(14)&p0(12)&p0(10)&p0(8)&p0(6)&p0(4)&p0(2)&p0(0));
            gik_0 <= (g0(30)&g0(28)&g0(26)&g0(24)&g0(22)&g0(20)&g0(18)&g0(16)&
                      g0(14)&g0(12)&g0(10)&g0(8)&g0(6)&g0(4)&g0(2)&g0(0));
            pkj_0 <= (p0(29)&p0(27)&p0(25)&p0(23)&p0(21)& p0(19)& p0(17)&p0(15)&
                      p0(13)&p0(11)&p0(9)&p0(7)&p0(5)&p0(3)&p0(1)&p_1_0);
            gkj_0 <= (g0(29)&g0(27)&g0(25)&g0(23)&g0(21)&g0(19)&g0(17)&g0(15)&
                      g0(13)&g0(11)&g0(9)&g0(7)&g0(5)& g0(3)&g0(1)&g_1_0);

            row1: blackbox port map(clk, pik_0, pkj_0, gik_0, gkj_0, pij_0, gij_0);

            p1(30) <= pij_0(15); p1(28) <= pij_0(14); p1(26) <= pij_0(13);
            p1(24) <= pij_0(12); p1(22) <= pij_0(11); p1(20) <= pij_0(10);
            p1(18) <= pij_0(9); p1(16) <= pij_0(8); p1(14) <= pij_0(7);
            p1(12) <= pij_0(6); p1(10) <= pij_0(5); p1(8) <= pij_0(4);
           p1(6) <= pij_0(3); p1(4) <= pij_0(2); p1(2) <= pij_0(1); p1(0) <= pij_0(0);

            g1(30) <= gij_0(15); g1(28) <= gij_0(14); g1(26) <= gij_0(13);
            g1(24) <= gij_0(12); g1(22) <= gij_0(11); g1(20) <= gij_0(10);
            g1(18) <= gij_0(9); g1(16) <= gij_0(8); g1(14) <= gij_0(7);
            g1(12) <= gij_0(6); g1(10) <= gij_0(5); g1(8) <= gij_0(4);
           g1(6) <= gij_0(3); g1(4) <= gij_0(2); g1(2) <= gij_0(1); g1(0) <= gij_0(0);
        end;

        library IEEE; use IEEE.STD_LOGIC_1164.all;

        entity row2 is
          port(clk:    in STD_LOGIC;
               p1, g1: in  STD_LOGIC_VECTOR(30 downto 0);
               p2, g2: out STD_LOGIC_VECTOR(30 downto 0));
        end;

        architecture synth of row2 is
          component blackbox is
            port (clk:       in  STD_LOGIC;
                  pik, pkj: in STD_LOGIC_VECTOR(15 downto 0);
                  gik, gkj: in STD_LOGIC_VECTOR(15 downto 0);
                  pij:       out STD_LOGIC_VECTOR(15 downto 0);
                  gij:       out STD_LOGIC_VECTOR(15 downto 0));
          end component;
          component flop is generic(width: integer);
            port(clk: in  STD_LOGIC;
                 d:   in  STD_LOGIC_VECTOR(width-1 downto 0);
                 q:   out STD_LOGIC_VECTOR(width-1 downto 0));
          end component;

          -- internal signals for calculating p, g
          signal pik_1, gik_1, pkj_1, gkj_1,
                 pij_1, gij_1: STD_LOGIC_VECTOR(15 downto 0);

          -- internal signals for pipeline registers
          signal pg1_in, pg2_out: STD_LOGIC_VECTOR(29 downto 0);

        begin
          pg1_in <= (p1(28 downto 27)&p1(24 downto 23)&p1(20 downto 19)&
                     p1(16 downto 15)&
                     p1(12 downto 11)&p1(8 downto 7)&p1(4 downto 3)&p1(0)&
                     g1(28 downto 27)&g1(24 downto 23)&g1(20 downto 19)&
                     g1(16 downto 15)&
                     g1(12 downto 11)&g1(8 downto 7)&g1(4 downto 3)&g1(0));
          flop2_pg: flop generic map(30) port map (clk, pg1_in, pg2_out);
```

```
  p2(28 downto 27) <= pg2_out(29 downto 28);
  p2(24 downto 23) <= pg2_out(27 downto 26);
  p2(20 downto 19) <= pg2_out( 25 downto 24);
  p2(16 downto 15) <= pg2_out(23 downto 22);
  p2(12 downto 11) <= pg2_out(21 downto 20);
  p2(8 downto 7) <= pg2_out(19 downto 18);
  p2(4 downto 3) <= pg2_out(17 downto 16);
  p2(0) <= pg2_out(15);
  g2(28 downto 27) <= pg2_out(14 downto 13);
  g2(24 downto 23) <= pg2_out(12 downto 11);
  g2(20 downto 19) <= pg2_out(10 downto 9);
  g2(16 downto 15) <= pg2_out(8 downto 7);
  g2(12 downto 11) <= pg2_out(6 downto 5);
  g2(8 downto 7) <= pg2_out(4 downto 3);
  g2(4 downto 3) <= pg2_out(2 downto 1); g2(0) <= pg2_out(0);

  -- pg calculations
  pik_1 <= (p1(30 downto 29)&p1(26 downto 25)&p1(22 downto 21)&
            p1(18 downto 17)&p1(14 downto 13)&p1(10 downto 9)&
            p1(6 downto 5)&p1(2 downto 1));
  gik_1 <= (g1(30 downto 29)&g1(26 downto 25)&g1(22 downto 21)&
            g1(18 downto 17)&g1(14 downto 13)&g1(10 downto 9)&
            g1(6 downto 5)&g1(2 downto 1));
  pkj_1 <= (p1(28)&p1(28)&p1(24)&p1(24)&p1(20)&p1(20)&p1(16)&p1(16)&
            p1(12)&p1(12)&p1(8)&p1(8)&p1(4)&p1(4)&p1(0)&p1(0));
  gkj_1 <= (g1(28)&g1(28)&g1(24)&g1(24)&g1(20)&g1(20)&g1(16)&g1(16)&
            g1(12)&g1(12)&g1(8)&g1(8)&g1(4)&g1(4)&g1(0)&g1(0));

  row2: blackbox
        port map(clk, pik_1, pkj_1, gik_1, gkj_1, pij_1, gij_1);

  p2(30 downto 29) <= pij_1(15 downto 14);
  p2(26 downto 25) <= pij_1(13 downto 12);
  p2(22 downto 21) <= pij_1(11 downto 10);
  p2(18 downto 17) <= pij_1(9 downto 8);
 p2(14 downto 13) <= pij_1(7 downto 6); p2(10 downto 9) <= pij_1(5 downto 4);
 p2(6 downto 5) <= pij_1(3 downto 2); p2(2 downto 1) <= pij_1(1 downto 0);

  g2(30 downto 29) <= gij_1(15 downto 14);
  g2(26 downto 25) <= gij_1(13 downto 12);
  g2(22 downto 21) <= gij_1(11 downto 10);
  g2(18 downto 17) <= gij_1(9 downto 8);
 g2(14 downto 13) <= gij_1(7 downto 6); g2(10 downto 9) <= gij_1(5 downto 4);
 g2(6 downto 5) <= gij_1(3 downto 2); g2(2 downto 1) <= gij_1(1 downto 0);

end;


library IEEE; use IEEE.STD_LOGIC_1164.all;

entity row3 is
  port(clk:   in STD_LOGIC;
       p2, g2: in  STD_LOGIC_VECTOR(30 downto 0);
       p3, g3: out STD_LOGIC_VECTOR(30 downto 0));
end;

architecture synth of row3 is
  component blackbox is
    port (clk:      in  STD_LOGIC;
          pik, pkj: in STD_LOGIC_VECTOR(15 downto 0);
          gik, gkj: in STD_LOGIC_VECTOR(15 downto 0);
          pij:      out STD_LOGIC_VECTOR(15 downto 0);
          gij:      out STD_LOGIC_VECTOR(15 downto 0));
  end component;
  component flop is generic(width: integer);
    port(clk: in  STD_LOGIC;
         d:   in  STD_LOGIC_VECTOR(width-1 downto 0);
```

```
                          q:    out STD_LOGIC_VECTOR(width-1 downto 0));
              end component;

              -- internal signals for calculating p, g
              signal pik_2, gik_2, pkj_2, gkj_2,
                     pij_2, gij_2: STD_LOGIC_VECTOR(15 downto 0);

              -- internal signals for pipeline registers
              signal pg2_in, pg3_out: STD_LOGIC_VECTOR(29 downto 0);

            begin
              pg2_in <= (p2(26 downto 23)&p2(18 downto 15)&p2(10 downto 7)&
                          p2(2 downto 0)&
                        g2(26 downto 23)&g2(18 downto 15)&g2(10 downto 7)&g2(2 downto 0));
              flop3_pg: flop generic map(30) port map (clk, pg2_in, pg3_out);
              p3(26 downto 23) <= pg3_out(29 downto 26);
              p3(18 downto 15) <= pg3_out(25 downto 22);
              p3(10 downto 7) <= pg3_out(21 downto 18);
              p3(2 downto 0) <= pg3_out(17 downto 15);
              g3(26 downto 23) <= pg3_out(14 downto 11);
              g3(18 downto 15) <= pg3_out(10 downto 7);
              g3(10 downto 7) <= pg3_out(6 downto 3);
              g3(2 downto 0) <= pg3_out(2 downto 0);

              -- pg calculations
              pik_2 <= (p2(30 downto 27)&p2(22 downto 19)&
                        p2(14 downto 11)&p2(6 downto 3));
              gik_2 <= (g2(30 downto 27)&g2(22 downto 19)&
                        g2(14 downto 11)&g2(6 downto 3));
              pkj_2 <= (p2(26)&p2(26)&p2(26)&p2(26)&
                        p2(18)&p2(18)&p2(18)&p2(18)&
                        p2(10)&p2(10)&p2(10)&p2(10)&
                        p2(2)&p2(2)&p2(2)&p2(2));
              gkj_2 <= (g2(26)&g2(26)&g2(26)&g2(26)&
                        g2(18)&g2(18)&g2(18)&g2(18)&
                        g2(10)&g2(10)&g2(10)&g2(10)&
                        g2(2)&g2(2)&g2(2)&g2(2));

              row3: blackbox
                    port map(clk, pik_2, pkj_2, gik_2, gkj_2, pij_2, gij_2);

              p3(30 downto 27) <= pij_2(15 downto 12);
              p3(22 downto 19) <= pij_2(11 downto 8);
              p3(14 downto 11) <= pij_2(7 downto 4); p3(6 downto 3) <= pij_2(3 downto 0);
              g3(30 downto 27) <= gij_2(15 downto 12);
              g3(22 downto 19) <= gij_2(11 downto 8);
              g3(14 downto 11) <= gij_2(7 downto 4); g3(6 downto 3) <= gij_2(3 downto 0);

            end;

            library IEEE; use IEEE.STD_LOGIC_1164.all;

            entity row4 is
              port(clk:    in STD_LOGIC;
                   p3, g3: in  STD_LOGIC_VECTOR(30 downto 0);
                   p4, g4: out STD_LOGIC_VECTOR(30 downto 0));
            end;

            architecture synth of row4 is
              component blackbox is
                port (clk:       in  STD_LOGIC;
                      pik, pkj: in STD_LOGIC_VECTOR(15 downto 0);
                      gik, gkj: in STD_LOGIC_VECTOR(15 downto 0);
                      pij:      out STD_LOGIC_VECTOR(15 downto 0);
                      gij:      out STD_LOGIC_VECTOR(15 downto 0));
              end component;
```

```
    component flop is generic(width: integer);
      port(clk: in  STD_LOGIC;
            d:   in  STD_LOGIC_VECTOR(width-1 downto 0);
            q:   out STD_LOGIC_VECTOR(width-1 downto 0));
    end component;

    -- internal signals for calculating p, g
    signal pik_3, gik_3, pkj_3, gkj_3,
           pij_3, gij_3: STD_LOGIC_VECTOR(15 downto 0);

    -- internal signals for pipeline registers
    signal pg3_in, pg4_out: STD_LOGIC_VECTOR(29 downto 0);

begin
  pg3_in <= (p3(22 downto 15)&p3(6 downto 0)&g3(22 downto 15)&g3(6 downto 0));
  flop4_pg: flop generic map(30) port map (clk, pg3_in, pg4_out);
  p4(22 downto 15) <= pg4_out(29 downto 22);
  p4(6 downto 0) <= pg4_out(21 downto 15);
  g4(22 downto 15) <= pg4_out(14 downto 7);
  g4(6 downto 0) <= pg4_out(6 downto 0);

    -- pg calculations
    pik_3 <= (p3(30 downto 23)&p3(14 downto 7));
    gik_3 <= (g3(30 downto 23)&g3(14 downto 7));
    pkj_3 <= (p3(22)&p3(22)&p3(22)&p3(22)&p3(22)&p3(22)&p3(22)&p3(22)&
             p3(6)&p3(6)&p3(6)&p3(6)&p3(6)&p3(6)&p3(6)&p3(6));
    gkj_3 <= (g3(22)&g3(22)&g3(22)&g3(22)&g3(22)&g3(22)&g3(22)&g3(22)&
             g3(6)&g3(6)&g3(6)&g3(6)&g3(6)&g3(6)&g3(6)&g3(6));

    row4: blackbox
         port map(clk, pik_3, pkj_3, gik_3, gkj_3, pij_3, gij_3);

    p4(30 downto 23) <= pij_3(15 downto 8);
    p4(14 downto 7) <= pij_3(7 downto 0);
    g4(30 downto 23) <= gij_3(15 downto 8);
    g4(14 downto 7) <= gij_3(7 downto 0);

end;


library IEEE; use IEEE.STD_LOGIC_1164.all;

entity row5 is
  port(clk:    in STD_LOGIC;
       p4, g4: in  STD_LOGIC_VECTOR(30 downto 0);
       p5, g5: out STD_LOGIC_VECTOR(30 downto 0));
end;
architecture synth of row5 is
  component blackbox is
    port (clk:       in  STD_LOGIC;
        pik, pkj: in STD_LOGIC_VECTOR(15 downto 0);
          gik, gkj: in STD_LOGIC_VECTOR(15 downto 0);
          pij:      out STD_LOGIC_VECTOR(15 downto 0);
          gij:      out STD_LOGIC_VECTOR(15 downto 0));
  end component;
  component flop is generic(width: integer);
    port(clk: in  STD_LOGIC;
          d:   in  STD_LOGIC_VECTOR(width-1 downto 0);
          q:   out STD_LOGIC_VECTOR(width-1 downto 0));
  end component;

  -- internal signals for calculating p, g
  signal pik_4, gik_4, pkj_4, gkj_4,
         pij_4, gij_4: STD_LOGIC_VECTOR(15 downto 0);

  -- internal signals for pipeline registers
  signal pg4_in, pg5_out: STD_LOGIC_VECTOR(29 downto 0);
```

```
begin

  pg4_in <= (p4(14 downto 0)&g4(14 downto 0));
  flop4_pg: flop generic map(30) port map (clk, pg4_in, pg5_out);
  p5(14 downto 0) <= pg5_out(29 downto 15); g5(14 downto 0) <= pg5_out(14
downto 0);

  -- pg calculations
  pik_4 <= p4(30 downto 15);
  gik_4 <= g4(30 downto 15);
  pkj_4 <= p4(14)&p4(14)&p4(14)&p4(14)&
          p4(14)&p4(14)&p4(14)&p4(14)&
          p4(14)&p4(14)&p4(14)&p4(14)&
          p4(14)&p4(14)&p4(14)&p4(14);
  gkj_4 <= g4(14)&g4(14)&g4(14)&g4(14)&
          g4(14)&g4(14)&g4(14)&g4(14)&
          g4(14)&g4(14)&g4(14)&g4(14)&
          g4(14)&g4(14)&g4(14)&g4(14);

  row5: blackbox
        port map(clk, pik_4, gik_4, pkj_4, gkj_4, pij_4, gij_4);
                p5(30 downto 15) <= pij_4; g5(30 downto 15) <= gij_4;

end;
```

Exercise 5.43
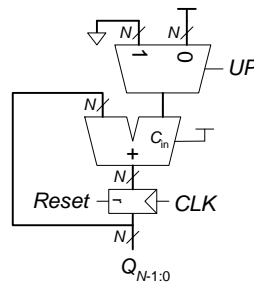
FIGURE 5.7 Up/Down counter

Exercise 5.45
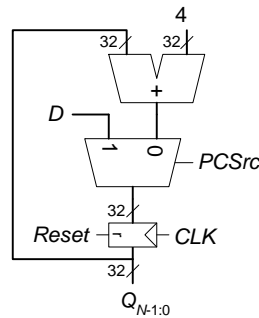
FIGURE 5.8 32-bit counter that increments by 4 or loads a new value, *D*

Exercise 5.47

SystemVerilog

```
module scanflop4(input  logic        clk, test, sin,
                 input  logic [3:0] d,
                 output logic [3:0] q,
                 output logic        sout);

  always_ff @(posedge clk)
    if (test)
      q <= d;
    else
      q <= {q[2:0], sin};

  assign sout = q[3];

endmodule
```

VHDL

```
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity scanflop4 is
  port(clk, test, sin:  in  STD_LOGIC;
       d:   in     STD_LOGIC_VECTOR(3 downto 0);
       q:   inout STD_LOGIC_VECTOR(3 downto 0);
       sout:          out STD_LOGIC);
end;

architecture synth of scanflop4 is
begin
  process(clk, test) begin
    if rising_edge(clk) then
      if test then
        q <= d;
      else
        q <= q(2 downto 0) & sin;
      end if;
    end if;
  end process;

  sout <= q(3);

end;
```

Exercise 5.49

http://www.intel.com/design/flash/articles/what.htm

Flash memory is a nonvolatile memory because it retains its contents after power is turned off. Flash memory allows the user to electrically program and erase information. Flash memory uses memory cells similar to an EEPROM, but with a much thinner, precisely grown oxide between a floating gate and the substrate (see Figure 5.9).

Flash programming occurs when electrons are placed on the floating gate. This is done by forcing a large voltage (usually 10 to 12 volts) on the control gate. Electrons quantum-mechanically tunnel from the source through the thin oxide onto the control gate. Because the floating gate is completely insulated by oxide, the charges are trapped on the floating gate during normal operation. If electrons are stored on the floating gate, it blocks the effect of the control gate. The electrons on the floating gate can be removed by reversing the procedure, i.e., by placing a large negative voltage on the control gate.

The default state of a flash bitcell (when there are no electrons on the floating gate) is ON, because the channel will conduct when the wordline is HIGH. After the bitcell is programmed (i.e., when there are electrons on the floating gate), the state of the bitcell is OFF, because the floating gate blocks the effect of the control gate. Flash memory is a key element in thumb drives, cell phones, digital cameras, Blackberries, and other low-power devices that must retain their memory when turned off.
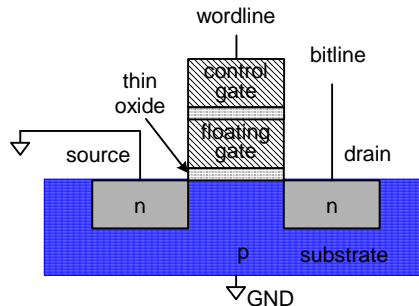
FIGURE 5.9 Flash EEPROM

Exercise 5.51
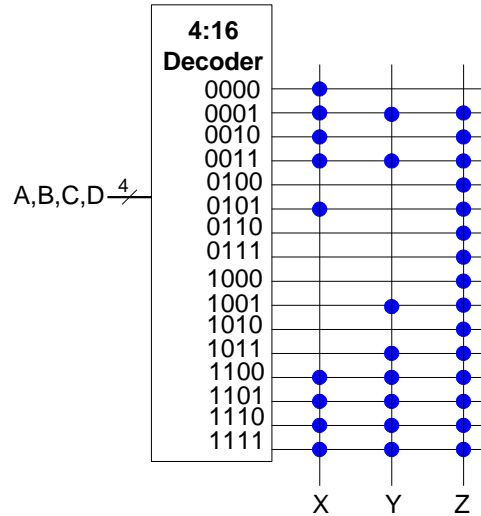
Exercise 5.53

(a) Number of inputs = $2 \times 16 + 1 = 33$
Number of outputs = $16 + 1 = 17$

Thus, this would require a 2^{33} x 17-bit ROM.

(b) Number of inputs = 16
Number of outputs = 16

Thus, this would require a 2^{16} x 16-bit ROM.

(c) Number of inputs = 16
Number of outputs = 4

Thus, this would require a 2^{16} x 4-bit ROM.

All of these implementations are not good design choices. They could all be implemented in a smaller amount of hardware using discrete gates.

Exercise 5.55

(a) 1 LE

(A) data 1	(B) data 2	(C) data 3	(D) data 4	(Y) LUT output
0	0	0	0	1
0	0	0	1	1
0	0	1	0	1
0	0	1	1	1
0	1	0	0	1
0	1	0	1	1
0	1	1	0	1
0	1	1	1	1
1	0	0	0	1
1	0	0	1	1
1	0	1	0	1
1	0	1	1	0
1	1	0	0	0
1	1	0	1	1
1	1	1	0	0
1	1	1	1	1
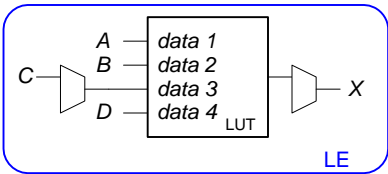
(b) 2 LEs

(B) data 1	(C) data 2	(D) data 3	(E) data 4	(X) LUT output
0	0	0	0	1
0	0	0	1	1
0	0	1	0	1
0	0	1	1	1
0	1	0	0	1
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	1
1	0	0	1	0
1	0	1	0	0
1	0	1	1	0
1	1	0	0	1
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0

(A) data 1	(X) data 2	data 3	data 4	(Y) LUT output
0	0	X	X	0
0	1	X	X	1
1	0	X	X	1
1	1	X	X	1
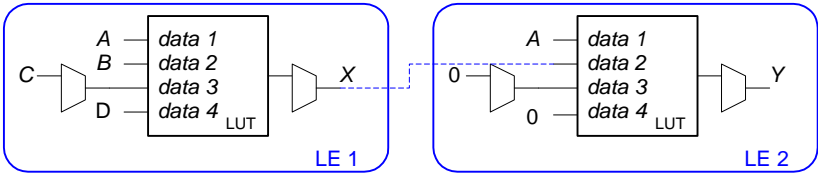
(c) 2 LEs

(A) data 1	(B) data 2	(C) data 3	(D) data 4	(Y) LUT output
0	0	0	0	0
0	0	0	1	1
0	0	1	0	0
0	0	1	1	1
0	1	0	0	0
0	1	0	1	1
0	1	1	0	0
0	1	1	1	1
1	0	0	0	0
1	0	0	1	1
1	0	1	0	1
1	0	1	1	1
1	1	0	0	0
1	1	0	1	1
1	1	1	0	0
1	1	1	1	1

(A) data 1	(B) data 2	(C) data 3	(D) data 4	(Z) LUT output
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	1
0	1	1	0	0
0	1	1	1	1
1	0	0	0	0
1	0	0	1	1
1	0	1	0	0
1	0	1	1	0
1	1	0	0	0
1	1	0	1	1
1	1	1	0	0
1	1	1	1	1

(d) 2 LEs

(A_3) data 1	(A_2) data 2	(A_1) data 3	(A_0) data 4	(D) LUT output		(A_3) data 1	(A_2) data 2	(A_1) data 3	(A_0) data 4	(P) LUT output
0	0	0	0	0		0	0	0	0	0
0	0	0	1	0		0	0	0	1	0
0	0	1	0	0		0	0	1	0	1
0	0	1	1	1		0	0	1	1	1
0	1	0	0	0		0	1	0	0	0
0	1	0	1	0		0	1	0	1	1
0	1	1	0	1		0	1	1	0	0
0	1	1	1	0		0	1	1	1	1
1	0	0	0	0		1	0	0	0	0
1	0	0	1	1		1	0	0	1	0
1	0	1	0	0		1	0	1	0	0
1	0	1	1	0		1	0	1	1	1
1	1	0	0	1		1	1	0	0	0
1	1	0	1	0		1	1	0	1	1
1	1	1	0	0		1	1	1	0	0
1	1	1	1	1		1	1	1	1	0

LE 1

LE 2

(e) 2 LEs

(A_3) data 1	(A_2) data 2	(A_1) data 3	(A_0) data 4	(Y_0) LUT output
0	0	0	0	0
0	0	0	1	0
0	0	1	0	1
0	0	1	1	1
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	1
1	0	0	1	1
1	0	1	0	1
1	0	1	1	1
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	1

(A_3) data 1	(A_2) data 2	(A_1) data 3	(A_0) data 4	(Y_1) LUT output
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	1
0	1	0	1	1
0	1	1	0	1
0	1	1	1	1
1	0	0	0	1
1	0	0	1	1
1	0	1	0	1
1	0	1	1	1
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	1

Exercise 5.57

(a) 5 LEs (2 for next state logic and state registers, 3 for output logic)

(b)

$t_{pd} = t_{pd\_LE} + t_{wire}$
$\quad = (381+246)$ ps
$\quad = 627$ ps

$T_c \geq t_{pcq} + t_{pd} + t_{setup}$
$\quad \geq [199 + 627 + 76]$ ps
$\quad = 902$ ps

$f \quad = 1 / 902$ ps = **1.1 GHz**

(c)

First, we check that there is no hold time violation with this amount of clock skew.

$t_{cd\_LE} = t_{pd\_LE} = 381$ ps
$t_{cd} = t_{cd\_LE} + t_{wire} = 627$ ps

$t_{skew} < (t_{ccq} + t_{cd}) - t_{hold}$

$< [(199 + 627) - 0]$ ps

< 826 ps

3 ns is less than 826 ps, so there is no hold time violation.

Now we find the fastest frequency at which it can run.

$T_c \geq t_{pcq} + t_{pd} + t_{setup} + t_{skew}$

$\geq [0.902 + 3]$ ns

$= 3.902$ ns

$f = 1 / 3.902$ ns $= $ **256 MHz**

Exercise 5.59

First, we find the cycle time:

$T_c = 1/f = 1/100$ MHz $= 10$ ns

$T_c \geq t_{pcq} + Nt_{LE+wire} + t_{setup}$

10 ns $\geq [0.199 + N(0.627) + 0.076]$ ns

Thus, $N \leq 15.5$

The maximum number of LEs on the critical path is **15**.

With at most one LE on the critical path and no clock skew, the fastest the FSM will run is:

$T_c \geq [0.199 + 0.627 + 0.076]$ ns

≥ 0.902 ns

$f = 1 / 0.902$ ns $= $ **1.1 GHz**

Question 5.1

$(2^N-1)(2^N-1) = 2^{2N} - 2^{N+1} +1$

Question 5.3
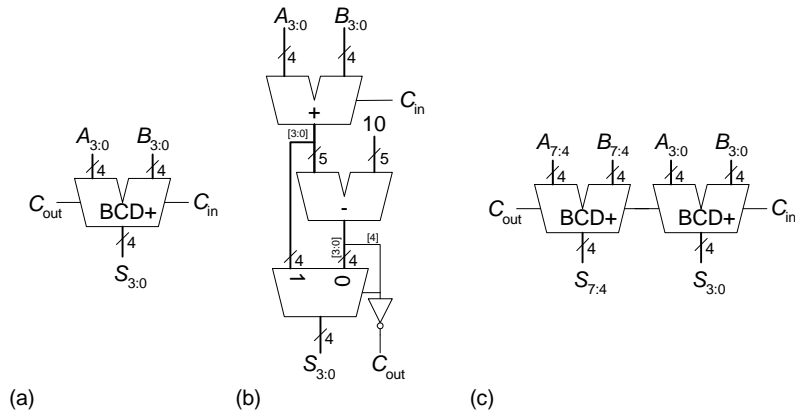
FIGURE 5.10 BCD adder: (a) 4-bit block, (b) underlying hardware, (c) 8-bit BCD adder

(continued from previous page)

SystemVerilog

```
module bcdadd_8(input  logic [7:0] a, b,
                input  logic       cin,
                output logic [7:0] s,
                output logic       cout);

  logic c0;

  bcdadd_4 bcd0(a[3:0], b[3:0], cin, s[3:0], c0);
  bcdadd_4 bcd1(a[7:4], b[7:4], c0, s[7:4], cout);

endmodule


module bcdadd_4(input  logic [3:0] a, b,
                input  logic       cin,
                output logic [3:0] s,
                output logic       cout);

  logic [4:0] result, sub10;

  assign result = a + b + cin;
  assign sub10 = result - 10;

  assign cout = ~sub10[4];
  assign s = sub10[4] ? result[3:0] : sub10[3:0];

endmodule
```

VHDL

```
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity bcdadd_8 is
  port(a, b: in  STD_LOGIC_VECTOR(7 downto 0);
       cin:  in  STD_LOGIC;
       s:    out STD_LOGIC_VECTOR(7 downto 0);
       cout: out STD_LOGIC);
end;

architecture synth of bcdadd_8 is
  component bcdadd_4
  port(a, b: in  STD_LOGIC_VECTOR(3 downto 0);
       cin:  in  STD_LOGIC;
       s:    out STD_LOGIC_VECTOR(3 downto 0);
       cout: out STD_LOGIC);
  end component;
  signal c0: STD_LOGIC;
begin

  bcd0: bcdadd_4
    port map(a(3 downto 0), b(3 downto 0), cin, s(3
downto 0), c0);
  bcd1: bcdadd_4
    port map(a(7 downto 4), b(7 downto 4), c0, s(7
downto 4), cout);

end;


library IEEE; use IEEE.STD_LOGIC_1164.all;
use IEEE.STD_LOGIC_UNSIGNED.all;
use IEEE.STD_LOGIC_ARITH.all;

entity bcdadd_4 is
  port(a, b: in  STD_LOGIC_VECTOR(3 downto 0);
       cin:  in  STD_LOGIC;
       s:    out STD_LOGIC_VECTOR(3 downto 0);
       cout: out STD_LOGIC);
end;

architecture synth of bcdadd_4 is
signal  result,  sub10,  a5,  b5:  STD_LOGIC_VECTOR(4
downto 0);
begin
  a5 <= '0' & a;
  b5 <= '0' & b;
  result <= a5 + b5 + cin;
  sub10 <= result - "01010";

  cout <= not (sub10(4));
  s <= result(3 downto 0) when sub10(4) = '1'
       else sub10(3 downto 0);

end;
```

CHAPTER 6

Exercise 6.1

(1) Simplicity favors regularity:

- Each instruction has a 6-bit opcode.

- MIPS has only 3 instruction formats (R-Type, I-Type, J-Type).

- Each instruction format has the same number and order of operands (they differ only in the opcode).

- Each instruction is the same size, making decoding hardware simple.

(2) Make the common case fast.

- Registers make the access to most recently accessed variables fast.

- The RISC (reduced instruction set computer) architecture, makes the common/simple instructions fast because the computer must handle only a small number of simple instructions.

- Most instructions require all 32 bits of an instruction, so all instructions are 32 bits (even though some would have an advantage of a larger instruction size and others a smaller instruction size). The instruction size is chosen to make the common instructions fast.

(3) Smaller is faster.

- The register file has only 32 registers.

- The ISA (instruction set architecture) includes only a small number of commonly used instructions. This keeps the hardware small and, thus, fast.

- The instruction size is kept small to make instruction fetch fast.

  (4) Good design demands good compromises.

- MIPS uses three instruction formats (instead of just one).

- Ideally all accesses would be as fast as a register access, but MIPS architecture also supports main memory accesses to allow for a compromise between fast access time and a large amount of memory.

- Because MIPS is a RISC architecture, it includes only a set of simple instructions, it provides pseudocode to the user and compiler for commonly used operations, like moving data from one register to another (`move`) and loading a 32-bit immediate (`li`).

Exercise 6.3

(a) $42 \times 4 = 42 \times 2^2 = 101010_2 << 2 = 10101000_2 = 0xA8$

(b) 0xA8 through 0xAB

(c)
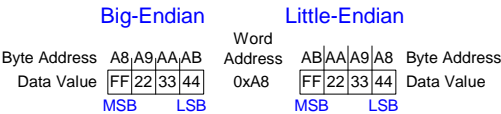
Exercise 6.5

```
# Big-endian
    li    $t0, 0xABCD9876
    sw    $t0, 100($0)
    lb    $s5, 101($0)  # the LSB of $s5 = 0xCD

# Little-endian
    li    $t0, 0xABCD9876
    sw    $t0, 100($0)
    lb    $s5, 101($0)  # the LSB of $s5 = 0x98
```

In big-endian format, the bytes are numbered from 100 to 103 from left to right. In little-endian format, the bytes are numbered from 100 to 103 from right to left. Thus, the final load byte (`lb`) instruction returns a different value depending on the endianness of the machine.

Exercise 6.7

(a) 0x68 6F 77 64 79 00
(b) 0x6C 69 6F 6E 73 00
(c) 0x54 6F 20 74 68 65 20 72 65 73 63 75 65 21 00

Exercise 6.9

Little-Endian Memory

Word Address	Data			
⋮	⋮			
10001010			00	79
1000100C	64	77	6F	68
⋮	Byte 3	⋮		Byte 0

(a)

Word Address	Data			
⋮	⋮			
10001010			00	73
1000100C	6E	6F	69	6C
⋮	Byte 3	⋮		Byte 0

(b)

Word Address	Data			
⋮	⋮			
10001018		00	21	65
10001014	75	63	73	65
10001010	72	20	65	68
1000100C	74	20	6F	54
⋮	Byte 3	⋮		Byte 0

(c)

Big-Endian Memory

Word Address	Data			
⋮	⋮			
10001010	79	00		
1000100C	68	6F	77	64
⋮	Byte 0	⋮		Byte 3

(a)

Word Address	Data			
⋮	⋮			
10001010	73	00		
1000100C	6C	69	6F	6E
⋮	Byte 0	⋮		Byte 3

(b)

Word Address	Data			
⋮	⋮			
10001018	65	21	00	
10001014	65	73	63	75
10001010	68	65	20	72
1000100C	54	6F	20	74
⋮	Byte 0	⋮		Byte 3

(c)

Exercise 6.11

0x20100049
0xad49fff9
0x02f24822

Exercise 6.13

(a)
```
addi $s0, $0, 73
sw   $t1, -7($t2)
```

(b)
0x20100049 (addi)
0xad49fff9 (sw)

Exercise 6.15

```
  addi $t0, $0, 31
L1:
  srlv $t1, $a0, $t0
  andi $t1, $t1, 1
  slt $t1, $0, $t1
  sb $t1, 0($a1)
  addi $a1, $a1, 1
  addi $t0, $t0, -1
  bgez $t0, L1
  jr $ra
```

(a) This program converts a number ($a0) from decimal to binary and stores it in an array pointed to by $a1.

```
void convert2bin(int num, char binarray[])
{
  int i;
  char tmp, val = 31;

  for (i=0; i<32; i++) {
    tmp = (num >> val) & 1;
    binarray[i] = tmp;
    val--;
  }
}
```

Exercise 6.17

(a)
```
# $s0 = g, $s1 = h
slt $t0, $s1, $s0      # if h < g, $t0 = 1
beq $t0, $0, else      # if $t0 == 0, do else
add $s0, $s0, $s1      # g = g + h
j done                 # jump past else block
else:sub $s0, $s0, $s1 # g = g - h
done:
```

(b)

```
slt  $t0, $s0, $s1 # if g < h, $t0 = 1
bne  $t0, $0, else # if $t0 != 0, do else
addi $s0, $s0, 1   # g = g + 1
j    done          # jump past else block
else:  addi $s1, $s1, -1  # h = h - 1
done:
```

(c)
```
slt $t0, $s1, $s0  # if h < g, $t0 = 1
bne $t0, $0, else  # if $t0 != 0, do else
add $s0, $0, $0    # g = 0
j   done           # jump past else block
else:   sub $s1, $0, $0    # h = 0
done:
```

Exercise 6.19

(a)
```
# MIPS assembly code
# base address of array dst = $a0
# base address of array src = $a1
# i = $s0

strcpy:
  addi $sp, $sp, -4
  sw   $s0, 0($sp)   # save $s0 on the stack
  add  $s0, $0, $0   # i = 0

loop:
  add  $t1, $a1, $s0 # $t1 = address of src[i]
  lb   $t2, 0($t1)   # $t2 = src[i]
  add  $t3, $a0, $s0 # $t3 = address of dst[i]
  sb   $t2, 0($t3)   # dst[i] = src[i]
  beq  $t2, $0, done # check for null character
  addi $s0, $s0, 1   # i++
  j    loop

done:
  lw   $s0, 0($sp)   # restore $s0 from stack
  addi $sp, $sp, 4   # restore stack pointer
  jr   $ra           # return
```

(b) The stack (i) before, (ii) during, and (iii) after the strcpy procedure call.
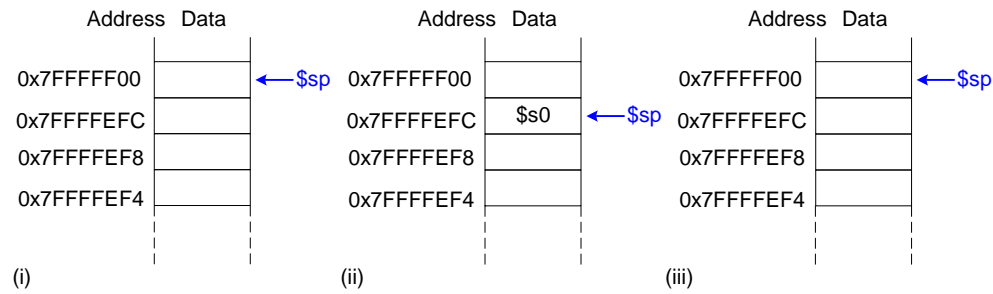
Exercise 6.21

(a) The stack frames of each procedure are:

proc1: 3 words deep (for $s0 - $s1, $ra)

proc2: 7 words deep (for $s2 - $s7, $ra)

proc3: 4 words deep (for $s1 - $s3, $ra)

proc4: 0 words deep (doesn't use any saved registers or call other procedures)

(b) Note: we arbitrarily chose to make the initial value of the stack pointer 0x7FFFFF04 just before the procedure calls.

Address		Data	
	⋮	⋮	
7FFF FF00		$ra	
7FFF FEFC		$s0	
7FFF FEF8		$s1	
7FFF FEF4		$ra = 0x00401024	
7FFF FEF0		$s2	
7FFF FEEC		$s3	
7FFF FEE8		$s4	
7FFF FEE4		$s5	
7FFF FEE0		$s6	
7FFF FEDC		$s7	
7FFF FED8		$ra = 0x00401180	
7FFF FED4		$s1	
7FFF FED0		$s2	
7FFF FECC		$s3	←$sp
	⋮	⋮	

(stack frame proc1: 7FFF FF00 – 7FFF FEF8)
(stack frame proc2: 7FFF FEF4 – 7FFF FEDC)
(stack frame proc3: 7FFF FED8 – 7FFF FECC)

Exercise 6.23

(a) 120
(b) 2
(c)
 (i) 3 - returned value is 1
 (ii) 2 (depending on what's stored on the stack frame of the callee's stack)
 (iii) 4

Exercise 6.25

(a) 000100 01000 10001 0000 0000 0000 0010
   = **0x11110002**
(b) 000100 01111 10100 0000 0100 0000 1111
   = **0x11F4040F**
(c) 000100 11001 10111 1111 1000 0100 0010
   = **0x1337F842**
(d) 000011 0000 0100 0001 0001 0100 0111 11
   = **0x0C10451F**

(e) 000010 00 0001 0000 0000 1100 0000 0001
   = 0x08100C01

Exercise 6.27

(a)
```
set_array:  addi $sp,$sp,-52   # move stack pointer
            sw   $ra,48($sp)   # save return address
            sw   $s0,44($sp)   # save $s0
            sw   $s1,40($sp)   # save $s1

            add  $s0,$0,$0     # i = 0
            addi $s1,$0,10     # max iterations = 10
     loop:  add  $a1,$s0,$0    # pass i as parameter
            jal  compare       # call compare(num, i)
            sll  $t1,$s0,2     # $t1 = i*4
            add  $t2,$sp,$t1   # $t2 = address of array[i]
            sw   $v0,0($t2)    # array[i] = compare(num, i);
            addi $s0,$s0,1     # i++
            bne  $s0,$s1,loop  # if i<10, goto loop

            lw   $s1,40($sp)   # restore $s1
            lw   $s0,44($sp)   # restore $s0
            lw   $ra,48($sp)   # restore return address
            addi $sp,$sp,52    # restore stack pointer
            jr   $ra           # return to point of call


  compare:  addi $sp,$sp,-4    # move stack pointer
            sw   $ra,0($sp)    # save return address on the stack
            jal  subtract      # input parameters already in $a0,$a1
            slt  $v0,$v0,$0    # $v0=1 if sub(a,b) < 0 (return 0)
            slti $v0,$v0,1     # $v0=1 if sub(a,b)>=0, else $v0 = 0
            lw   $ra,0($sp)    # restore return address
            addi $sp,$sp,4     # restore stack pointer
            jr   $ra           # return to point of call

 subtract:  sub  $v0,$a0,$a1   # return a-b
            jr   $ra           # return to point of call
```

6.27 (b)

Before set_array:	During set_array:	During compare/sub:
	$ra	$ra
	$s0	$s0
	$s1	$s1
	array[9]	array[9]
	array[8]	array[8]
	array[7]	array[7]
	array[6]	array[6]
	array[5]	array[5]
	array[4]	array[4]
	array[3]	array[3]
	array[2]	array[2]
	array[1]	array[1]
	array[0]	array[0]
		$ra

$sp → (Before set_array, upper division)

$sp → array[0] (During set_array)

$sp → $ra (During compare/sub)
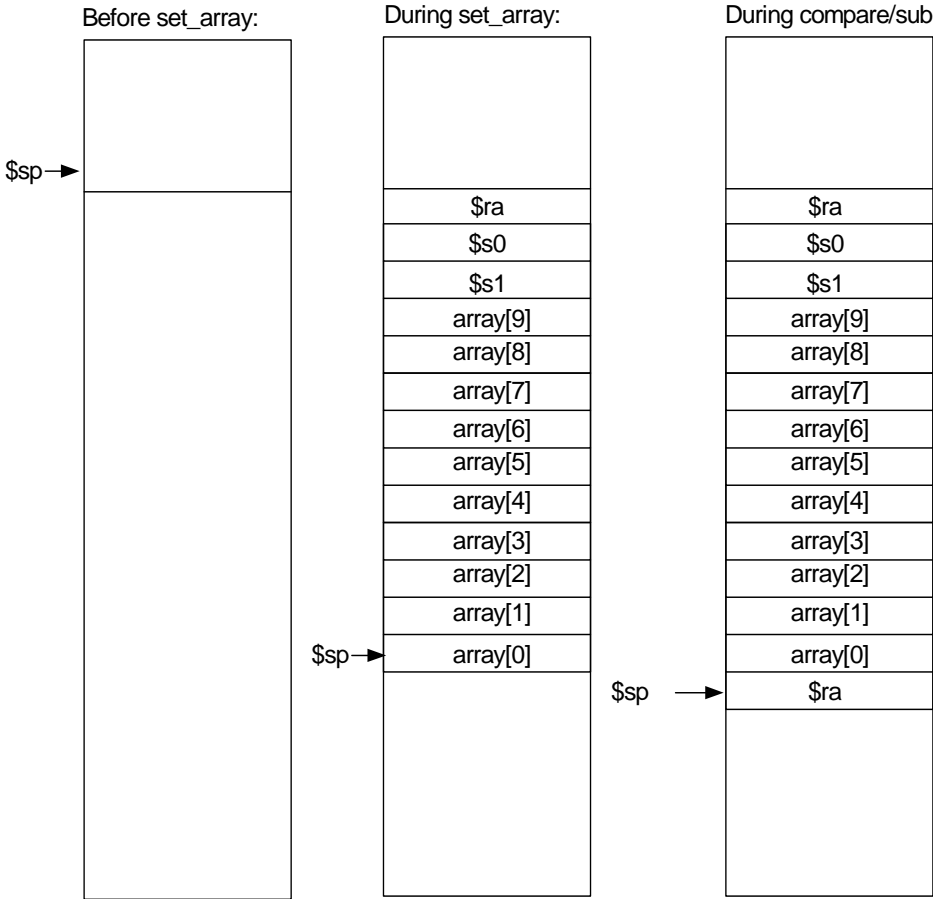
(c) If $ra were never stored on the stack, the compare function would re-turn to the instruction after the call to subtract (slt $v0,$v0,$0) in-stead of returning to the set_array function. The program would enter an infinite loop in the compare function between jr $ra and slt $v0, $v0, $0. It would increment the stack during that loop until the stack space was exceeded and the program would likely crash.

Exercise 6.29

Instructions (32 K - 1) words before the branch to instructions 32 K words after the branch instruction.

Exercise 6.31

It is advantageous to have a large address field in the machine format for jump instructions to increase the range of instruction addresses to which the instruction can jump.

Exercise 6.33

```
# high-level code
void little2big(int[] array)
{
  int i;

  for (i = 0; i < 10; i = i + 1) {
    array[i] = ((array[i] & 0xFF) << 24) ||
               (array[i] & 0xFF00) << 8) ||
               (array[i] & 0xFF0000) >> 8) ||
               ((array[i] >> 24) & 0xFF));
  }
}


# MIPS assembly code
# $a0 = base address of array
little2big:
          addi $t5, $0, 10  # $t5 = i = 10 (loop counter)
    loop: lb   $t0, 0($a0)  # $t0 = array[i] byte 0
          lb   $t1, 1($a0)  # $t1 = array[i] byte 1
          lb   $t2, 2($a0)  # $t2 = array[i] byte 2
          lb   $t3, 3($a0)  # $t3 = array[i] byte 3
          sb   $t3, 0($a0)  # array[i] byte 0 = previous byte 3
          sb   $t2, 1($a0)  # array[i] byte 1 = previous byte 2
          sb   $t1, 2($a0)  # array[i] byte 2 = previous byte 1
          sb   $t0, 3($a0)  # array[i] byte 3 = previous byte 0
          addi $a0, $a0, 4  # increment index into array
          addi $t5, $t5, -1 # decrement loop counter
          beq  $t5, $0, done
          j    loop
    done:
```

Exercise 6.35

```
# define the masks in the global data segment
        .data
mmask:  .word 0x007FFFFF
emask:  .word 0x7F800000
ibit:   .word 0x00800000
obit:   .word 0x01000000

        .text

flpadd: lw $t4,mmask          # load mantissa mask
        and $t0,$s0,$t4        # extract mantissa from $s0 (a)
        and $t1,$s1,$t4        # extract mantissa from $s1 (b)
        lw $t4,ibit           # load implicit leading 1
        or $t0,$t0,$t4         # add the implicit leading 1 to mantissa
        or $t1,$t1,$t4         # add the implicit leading 1 to mantissa
```

```
        lw $t4,emask          # load exponent mask
        and $t2,$s0,$t4       # extract exponent from $s0 (a)
        srl $t2,$t2,23        # shift exponent right
        and $t3,$s1,$t4       # extract exponent from $s1 (b)
        srl $t3,$t3,23        # shift exponent right
match:  beq $t2,$t3,addsig    # check whether the exponents match
        bgeu $t2,$t3,shiftb   # determine which exponent is larger
shifta: sub $t4,$t3,$t2       # calculate difference in exponents
        srav $t0,$t0,$t4      # shift a by calculated difference
        add $t2,$t2,$t4       # update a's exponent
        j addsig              # skip to the add
shiftb: sub $t4,$t2,$t3       # calculate difference in exponents
        srav $t1,$t1,$t4      # shift b by calculated difference
        add $t3,$t3,$t4       # update b's exponent (not necessary)
addsig: add $t5,$t0,$t1       # add the mantissas
norm:   lw $t4,obit           # load mask for bit 24 (overflow bit)
        and $t4,$t5,$t4       # mask bit 24
        beq $t4,$0,done       # right shift not needed because bit 24=0
        srl $t5,$t5,1         # shift right once by 1 bit
        addi $t2,$t2,1        # increment exponent
done:   lw $t4,mmask          # load mask
        and $t5,$t5,$t4       # mask mantissa
        sll $t2,$t2,23        # shift exponent into place
        lw $t4,emask          # load mask
        and $t2,$t2,$t4       # mask exponent
        or $v0,$t5,$t2        # place mantissa and exponent into $v0
        jr $ra                # return to caller
```

Exercise 6.37

(a)
```
0x00400000  main:    addi $sp, $sp, -4
0x00400004           sw   $ra, 0($sp)
0x00400008           addi $t0, $0, 15
0x0040000C           sw   $t0, 0x8000($gp)
0x00400010           addi $a1, $0, 27
0x00400014           sw   $a1, 0x8004($gp)
0x00400018           lw   $a0, 0x8000($gp)
0x0040001C           jal  greater
0x00400020           lw   $ra, 0($sp)
0x00400024           addi $sp, $sp, 4
0x00400028           jr   $ra

0x0040002C  greater: slt  $v0, $a1, $a0
0x00400030           jr   $ra
```

(b)

symbol	address
a	0x10000000
b	0x10000004
main	0x00400000
greater	0x0040002C

TABLE 6.1 Symbol table

(c)

Executable file header	Text Size	Data Size	
	0x34 (52 bytes)	0x8 (8 bytes)	
Text segment	**Address**	**Instruction**	
	0x00400000	0x23BDFFFC	addi $sp, $sp, -4
	0x00400004	0xAFBF0000	sw $ra, 0($sp)
	0x00400008	0x2008000F	addi $t0, $0, 15
	0x0040000C	0xAF888000	sw $t0, 0x8000($gp)
	0x00400010	0x2005001B	addi $a1, $0, 27
	0x00400014	0xAF858004	sw $a1, 0x8004($gp)
	0x00400018	0x8F848000	lw $a0, 0x8000($gp)
	0x0040001C	0x0C10000B	jal greater
	0x00400020	0x8FBF0000	lw $ra, 0($sp)
	0x00400024	0x23BD0004	addi $sp, $sp, 4
	0x00400028	0x03E00008	jr $ra
	0x0040002C	0x00A4102A	slt $v0, $a1, $a0
	0x00400030	0x03E00008	jr $ra
Data segment	**Address**	**Data**	
	0x10000000	a	
	0x10000004	b	

(d)
The data segment is 8 bytes and the text segment is 52 (0x34) bytes.

(e)

	Address	Memory	
		Reserved	
	0x7FFFFFFC	Stack	← $sp = 0x7FFFFFFC
		↓	
		↑	
	0x10010000	Heap	
		⋮	← $gp = 0x10008000
		b	
	0x10000000	a	
		⋮	
		0x03E00008	
		0x00A4102A	
		0x03E00008	
		0x23BD0004	
		0x8FBF0000	
		0x0C10000B	
		0x8f848000	
		0xAF850004	
		0x2005001B	
		0xAF888000	
		0x2008000F	
		0xAFBF0000	
	0x00400000	0x23BDFFFC	← PC = 0x00400000
		Reserved	
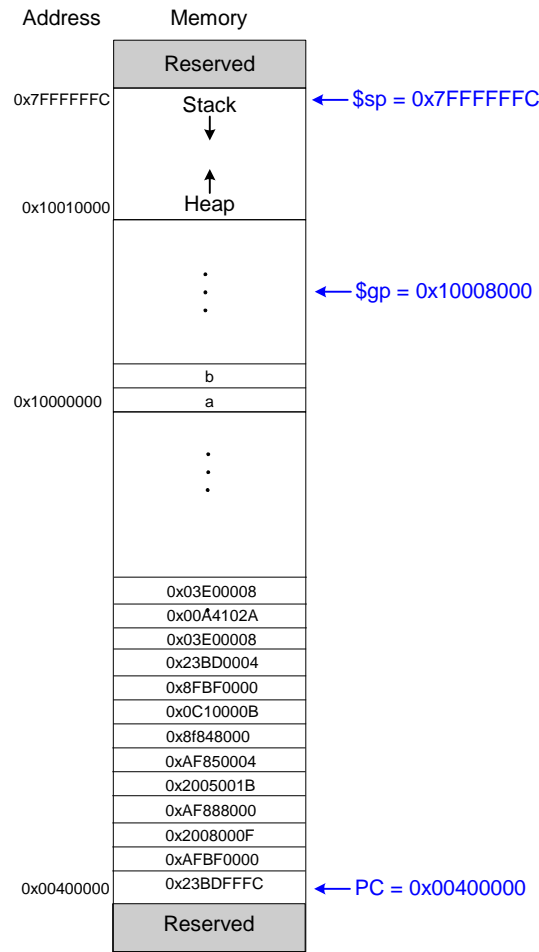
Exercise 6.39

(a)
```
beq $t1, imm31:0, L

lui $at, imm31:16
ori $at, $at, imm15:0
beq $t1, $at, L
```

(b)
```
ble $t3, $t5, L

slt $at, $t5, $t3
beq $at, $0, L
```

(c)
```
bgt $t3, $t5, L

slt $at, $t5, $t3
bne $at, $0, L
```
(d)
```
bge $t3, $t5, L

slt $at, $t3, $t5
beq $at, $0, L
```

Question 6.1

```
xor $t0, $t0, $t1  # $t0 = $t0 XOR $t1
xor $t1, $t0, $t1  # $t1 = original value of $t0
xor $t0, $t0, $t1  # $t0 = original value of $t1
```

Question 6.3

High-Level Code

```
// high-level algorithm
void reversewords(char[] array) {
  int i, j, length;



  // find length of string
  for (i = 0; array[i] != 0; i = i + 1) ;




  length = i;

  // reverse characters in string
  reverse(array, length-1, 0);

// reverse words in string
  i = 0; j = 0;

  // check for spaces
  while (i <= length) {
    if ( (i != length) || (array[i] != 0x20) ) {
      i = i + 1;



    else {
      reverse(array, i-1, j);
      i = i + 1; // j and i at start of next word
      j = i;
    }
  }
}








void reverse(char[] array, int i, int j)
{
  char tmp;
  while (i > j) {
    tmp = array[i];
    array[i] = array[j];
    array[j] = tmp;
    i = i-1;
    j = j+1;
  }
}
```

MIPS Assembly Code

```
# $s2 = i, $s3 = j, $s1 = length
reversewords:
        addi $sp, $sp, -16    # make room on stack
        sw   $ra, 12($sp)     # store regs on stack
        sw   $s1, 8($sp)
        sw   $s2, 4($sp)
        sw   $s3, 0($sp)

        addi $s2, $0, 0       # i = 0
length: add  $t4, $a0, $s2    # $t4 = &array[i]
        lb   $t3, 0($t4)      # $t3 = array[i]
        beq  $t3, $0, done    # end of string?
        addi $s2, $s2, 1      # i++
        j    length

done:   addi $s1, $s2, 0      # length = i
        addi $a1, $s1, -1     # $a1 = length - 1
        addi $a2, $0, 0       # $a2 = 0
        jal  reverse          # call reverse

        addi $s2, $0, 0       # i = 0
        addi $s3, $0, 0       # j = 0
        addi $t5, $0, 0x20    # $t5 = "space"
word:   slt  $t4, $s1, $s2    # $t4 = 1 if length<i
        bne  $t4, $0, return  # return if length<i
        beq  $s2, $s1, else   # if i==length, else
        add  $t4, $a0, $s2    # $t4 = &array[i]
        lb   $t4, 0($t4)      # $t4 = array[i]
        beq  $t4, $t5, else   # if $t4==0x20,else
        addi $s2, $s2, 1      # i = i + 1
        j    word
else:   addi $a1, $s2, -1     # $a1 = i - 1
        addi $a2, $s3, 0      # $a2 = j
        jal  reverse
        addi $s2, $s2, 1      # i = i + 1
        addi $s3, $s2, 0      # j = i
        j    word

return: lw   $ra, 12($sp)     # restore regs
        lw   $s1, 8($sp)
        lw   $s2, 4($sp)
        lw   $s3, 0($sp)
        addi $sp, $sp, 16     # restore $sp
        jr   $ra              # return



reverse:
        slt  $t0, $a2, $a1    # $t0 = 1 if j < i
        beq  $t0, $0,  exit   # if j < i, return
        add  $t1, $a0, $a1    # $t1 = &array[i]
        lb   $t2, 0($t1)      # $t2 = array[i]
        add  $t3, $a0, $a2    # $t3 = &array[j]
        lb   $t4, 0($t3)      # $t4 = array[j]
        sb   $t4, 0($t1)      # array[i] =array[j]
        sb   $t2, 0($t3)      # array[j] =array[i]
        addi $a1, $a1, -1     # i = i-1
        addi $a2, $a2, 1      # j = j+1
        j    reverse
exit:   jr   $ra
```

Question 6.5

High-Level Code

```
num = swap(num, 1, 0x55555555);  // swap bits
num = swap(num, 2, 0x33333333);  // swap pairs
num = swap(num, 4, 0x0F0F0F0F);  // swap nibbles
num = swap(num, 8, 0x00FF00FF);  // swap bytes
num = swap(num, 16, 0xFFFFFFFF); // swap halves

// swap masked bits
int swap(int num, int shamt, unsigned int mask) {
  return ((num >> shamt) & mask) |
         ((num & mask) << shamt);
}
```

MIPS Assembly Code

```
# $t3 = num
addi $a0, $t3, 0      # set up args
addi $a1, $0, 1
li   $a2, 0x55555555
jal  swap             # swap bits
addi $a0, $v0, 0      # num = return value

addi $a1, $0, 2       # set up args
li   $a2, 0x33333333
jal  swap             # swap pairs
addi $a0, $v0, 0      # num = return value

addi $a1, $0, 4       # set up args
li   $a2, 0x0F0F0F0F
jal  swap             # swap nibbles
addi $a0, $v0, 0      # num = return value

addi $a1, $0, 8       # set up args
li   $a2, 0x00FF00FF
jal  swap             # swap bytes
addi $a0, $v0, 0      # num = return value

addi $a1, $0, 16      # set up args
li   $a2, 0xFFFFFFFF
jal  swap             # swap halves
addi $t3, $v0, 0      # num = return value

done: j done

swap:
  srlv $v0, $a0, $a1  # $v0 = num >> shamt
  and  $v0, $v0, $a2  # $v0 = $v0 & mask
  and  $t0, $a0, $a2  # $t0 = num & mask
  sllv $t0, $t0, $a1  # $t0 = $t0 << shamt
  or   $v0, $v0, $t0  # $v0 = $v0 | $t0
  jr   $ra            # return
```

Question 6.7

High-Level Code

```
bool palindrome(char* array) {
  int i, j; // array indices
  // find length of string
  for (j = 0; array[j] != 0; j=j+1) ;



  j = j-1; // j is index of last char

  int i = 0;
  while (j > i) {
    tmp = array[i];
    if (array[i] != array[j])
      return false;
    j = j-1;
    i = i+1;
  }


  return true;
}
```

MIPS Assembly Code

```
# $t0 = j, $t1 = i, $a0 = base address of string
palindrome:
        addi $t0, $0, 0     # j = 0
length: add  $t2, $a0, $t0  # $t2 = &array[j]
        lb   $t2, 0($t2)    # $t2 = array[j]
        beq  $t2, $0, done  # end of string?
        addi $t0, $t0, 1    # j = j+1
        j    length
done:   addi $t0, $t0, -1   # j = j-1

        addi $t1, $0, 0     # i = 0
loop:   slt  $t2, $t1, $t0  # $t2 = 1 if i < j
        beq  $t2, $0,  yes  # if !(i < j) return
        add  $t2, $a0, $t1  # $t2 = &array[i]
        lb   $t2, 0($t2)    # $t2 = array[i]
        add  $t3, $a0, $t0  # $t3 = &array[j]
        lb   $t3, 0($t3)    # $t3 = array[j]
        bne  $t2, $t3, no   # is palindrome?
        addi $t0, $t0, -1   # j = j-1
        addi $t1, $t1, 1    # i = i+1
        j    loop

yes:    # yes a palindrome
        addi $v0, $0, 1
        j yes
        jr   $ra

no:     # not a palindrome
        addi $v0, $0, 0
        j no
        jr   $ra
```

CHAPTER 7

Exercise 7.1

(a) R-type, `lw`, `addi`
(b) R-type
(c) `sw`

Exercise 7.3

(a) `sll`

First, we modify the ALU.
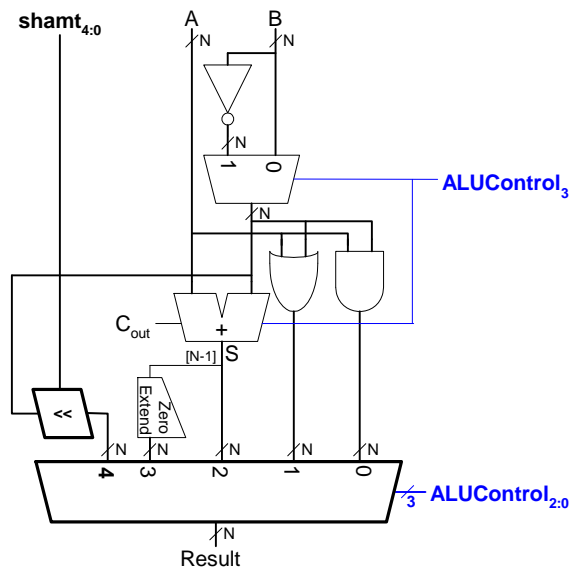
FIGURE 7.1 Modified ALU to support `sll`

ALUControl$_{3:0}$	Function
0000	A AND B
0001	A OR B
0010	A + B
0011	not used
1000	A AND $\overline{B}$
1001	A OR $\overline{B}$
1010	A - B
1011	SLT
0100	SLL

TABLE 7.1 Modified ALU operations to support `sll`

ALUOp	Funct	ALUControl
00	X	0010 (add)
X1	X	1010 (subtract)
1X	100000 (add)	0010 (add)
1X	100010 (sub)	1010 (subtract)
1X	100100 (and)	0000 (and)
1X	100101 (or)	0001 (or)
1X	101010 (slt)	1011 (set less than)
1X	000000 (sll)	0100 (shift left logical)

TABLE 7.2 ALU decoder truth table

Then we modify the datapath.
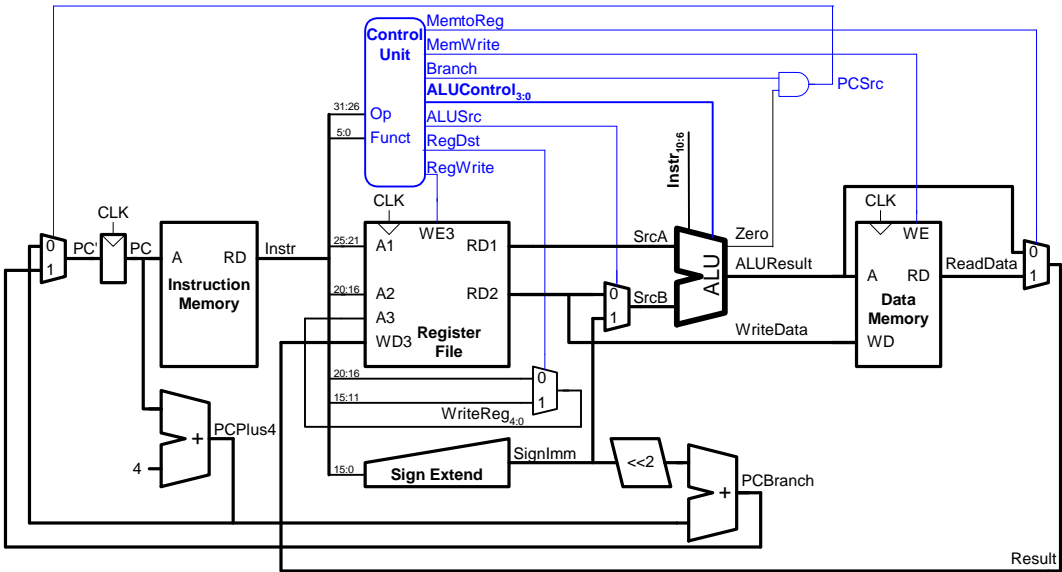
FIGURE 7.2 Modified single-cycle MIPS processor extended to run `sll`

7.3 (b) lui

Note: the 5-bit rs field of the lui instruction is 0.

Instruction	opcode	RegWrite	RegDst	ALUSrc	Branch	MemWrite	MemtoReg	ALUOp
R-type	000000	1	1	00	0	0	0	10
lw	100011	1	0	01	0	0	1	00
sw	101011	0	X	01	0	1	X	00
beq	000100	0	X	00	1	0	X	01
lui	001111	1	0	10	0	0	0	00

TABLE 7.3 Main decoder truth table enhanced to support lui
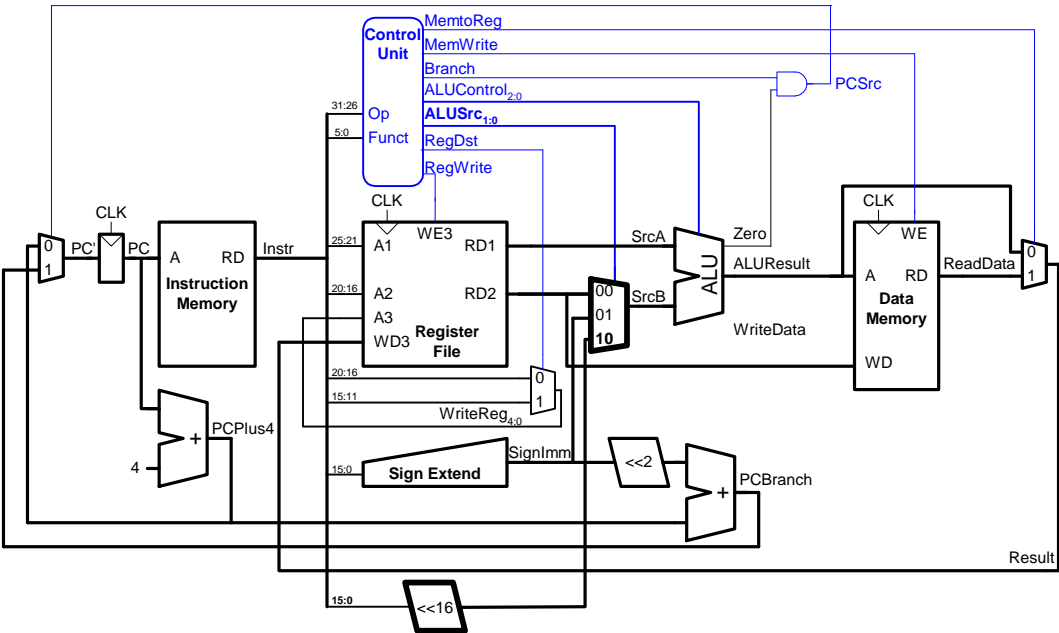
FIGURE 7.3 Modified single-cycle datapath to support lui

7.3 (c) slti

The datapath doesn't change. Only the controller changes, as shown in Table 7.4 and Table 7.5.

ALUOp	Funct	ALUControl
00	X	010 (add)
01	X	110 (subtract)
10	100000 (add)	010 (add)
10	100010 (sub)	110 (subtract)
10	100100 (and)	000 (and)
10	100101 (or)	001 (or)
10	101010 (slt)	111 (set less than)
11	**X**	**111 (set less than)**

TABLE 7.4 ALU decoder truth table

Instruction	opcode	RegWrite	RegDst	ALUSrc	Branch	MemWrite	MemtoReg	ALUOp
R-type	000000	1	1	0	0	0	0	10
lw	100011	1	0	1	0	0	1	00
sw	101011	0	X	1	0	1	X	00
beq	000100	0	X	0	1	0	X	01
slti	**001010**	**1**	**0**	**1**	**0**	**0**	**0**	**11**

TABLE 7.5 Main decoder truth table enhanced to support slti

7.3 (d) `blez`

First, we modify the ALU
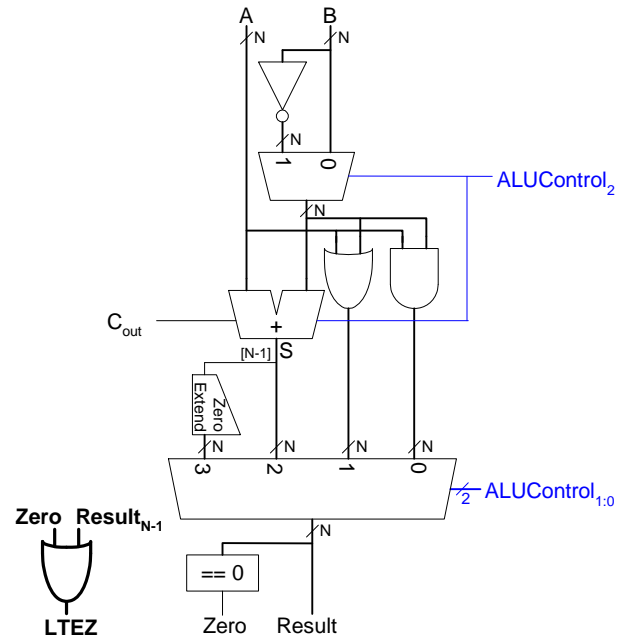
Then, we modify the datapath

.
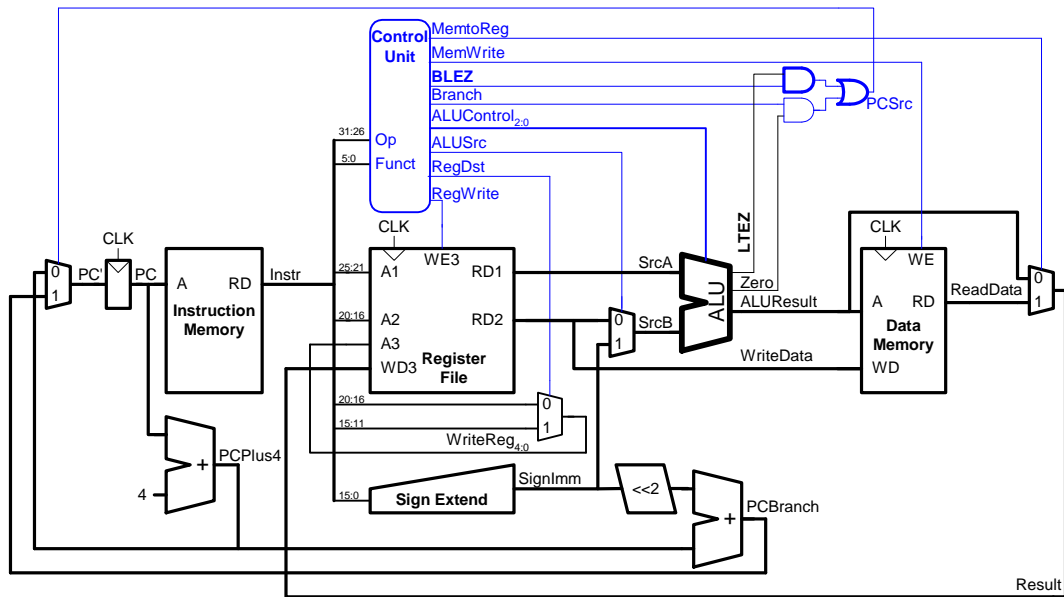
Instruction	opcode	RegWrite	RegDst	ALUSrc	Branch	MemWrite	MemtoReg	ALUOp	BLEZ
R-type	000000	1	1	0	0	0	0	10	0
lw	100011	1	0	1	0	0	1	00	0
sw	101011	0	X	1	0	1	X	00	0
beq	000100	0	X	0	1	0	X	01	0
blez	000110	0	X	0	0	0	X	01	1

TABLE 7.6 Main decoder truth table enhanced to support blez

Exercise 7.5

It is not possible to implement this instruction without either modifying the register file (adding another write port) or making the instruction take two cycles to execute.

We modify the register file and datapath as shown in Figure 7.4.
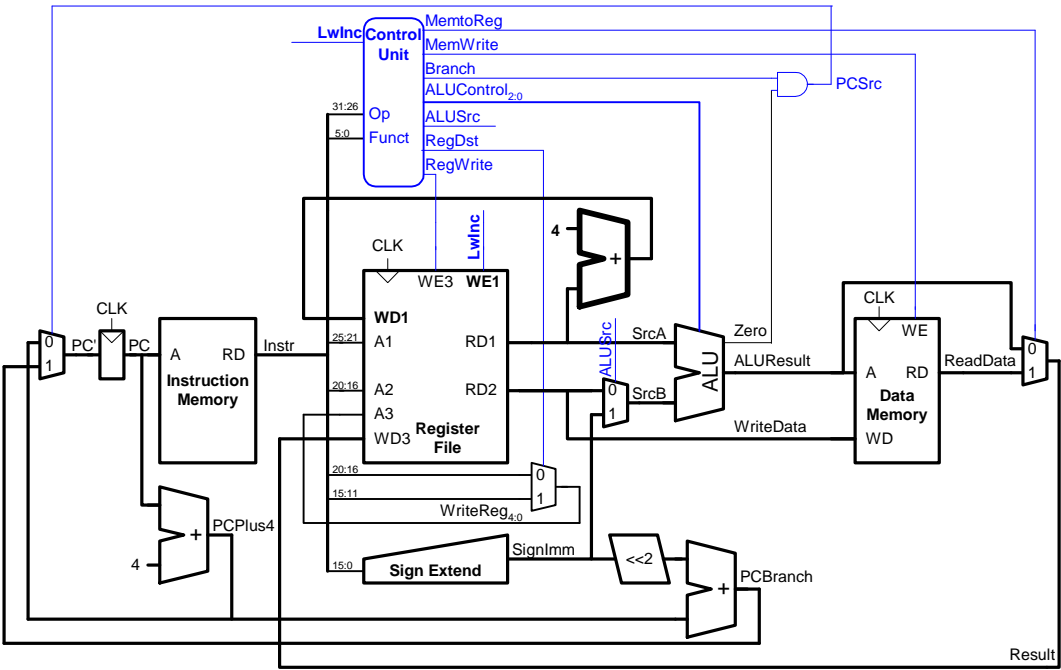
FIGURE 7.4 Modified datapath

Instruction	opcode	RegWrite	RegDst	ALUSrc	Branch	MemWrite	MemtoReg	ALUOp	**Lwinc**
R-type	000000	1	1	0	0	0	0	10	**0**
lw	100011	1	0	1	0	0	1	00	**0**
sw	101011	0	X	1	0	1	X	00	**0**
beq	000100	0	X	0	1	0	X	01	**0**
lwinc		**1**	**0**	**1**	**0**	**0**	**1**	**00**	**1**

TABLE 7.7 Main decoder truth table enhanced to support lwinc

Exercise 7.7

Before the enhancement (see Equation 7.3, page 380 in the text, also Errata):

$T_c = t_{pcq\_PC} + 2t_{mem} + t_{RFread} + t_{mux} + t_{ALU} + t_{RFsetup}$
$= 30 + 2(250) + 150 + 25 + 200 + 20 = $ **925ps**

The unit that your friend could speed up that would make the largest reduction in cycle time would be the memory unit. So tmem_new = 125ps, and the new cycle time is:

$T_c = $ **675 ps**

Exercise 7.9

(a) `lw`
(b) `beq`
(c) `beq, j`

Exercise 7.11

SystemVerilog

```
module top(input  logic        clk, reset,
           output logic [31:0] writedata, dataadr,
           output logic        memwrite);

  logic [31:0] pc, instr, readdata;

  // instantiate processor and memories
  mips mips(clk, reset, pc, instr, memwrite, dataadr,
            writedata, readdata);
  imem imem(pc[7:2], instr);
  dmem dmem(clk, memwrite, dataadr, writedata, readdata);
endmodule

module dmem(input  logic        clk, we,
            input  logic [31:0] a, wd,
            output logic [31:0] rd);

  logic [31:0] RAM[63:0];

  assign rd = RAM[a[31:2]]; // word aligned

  always_ff @(posedge clk)
    if (we) RAM[a[31:2]] <= wd;
endmodule

module imem(input  logic [5:0] a,
```

```
                  output logic [31:0] rd);

   logic [31:0] RAM[63:0];

   initial
       $readmemh("memfile.dat",RAM);

   assign rd = RAM[a]; // word aligned
endmodule



module mipssingle(input  logic         clk, reset,
                  output logic [31:0] pc,
                  input  logic [31:0] instr,
                  output logic         memwrite,
                  output logic [31:0] aluresult,
                                      writedata,
                  input  logic [31:0] readdata);

   logic         memtoreg;
   logic [1:0]  alusrc;  // LUI
   logic         regdst;
   logic         regwrite, jump, pcsrc, zero;
   logic [3:0]  alucontrol;  // SLL
   logic         ltez;  // BLEZ

   controller c(instr[31:26], instr[5:0], zero,
                memtoreg, memwrite, pcsrc,
                alusrc, regdst, regwrite, jump,
                alucontrol,
                ltez);  // BLEZ

   datapath dp(clk, reset, memtoreg, pcsrc,
                alusrc, regdst, regwrite, jump,
                alucontrol,
                zero, pc, instr,
                aluresult, writedata, readdata,
                ltez);  // BLEZ
endmodule

module controller(input  logic [5:0] op, funct,
                  input  logic        zero,
                  output logic        memtoreg, memwrite,
                  output logic        pcsrc,
                  output logic [1:0] alusrc,     // LUI
                  output logic        regdst,
                  output logic        regwrite,
                  output logic        jump,
                  output logic [3:0] alucontrol,  // SLL
                  input  logic        ltez);       // BLEZ

   logic [1:0] aluop;
```

```
   logic         branch;
   logic         blez;  // BLEZ

   maindec md(op, memtoreg, memwrite, branch,
              alusrc, regdst, regwrite, jump,
              aluop, blez);  // BLEZ
   aludec  ad(funct, aluop, alucontrol);

   // BLEZ
   assign pcsrc = (branch & zero) | (blez & ltez);

endmodule

module maindec(input  logic [5:0] op,
               output logic       memtoreg, memwrite,
               output logic       branch,
               output logic [1:0] alusrc, // LUI
               output logic       regdst,
               output logic       regwrite,
               output logic       jump,
               output logic [1:0] aluop,
               output logic       blez);   // BLEZ

   // increase control width for LUI, BLEZ
   logic [10:0] controls;

   assign {regwrite, regdst, alusrc, branch, memwrite,
           memtoreg, aluop, jump, blez} = controls;

   always_comb
     case(op)
       6'b000000: controls = 11'b11000001000; //Rtype
       6'b100011: controls = 11'b10010010000; //LW
       6'b101011: controls = 11'b00010100000; //SW
       6'b000100: controls = 11'b00001000100; //BEQ
       6'b001000: controls = 11'b10010000000; //ADDI
       6'b000010: controls = 11'b00000000010; //J
       6'b001010: controls = 11'b10010001100; //SLTI
       6'b001111: controls = 11'b10100000000; //LUI
       6'b000110: controls = 11'b00000000101; //BLEZ
       default:   controls = 11'bxxxxxxxxxxx; //???
     endcase
endmodule

module aludec(input  logic [5:0] funct,
              input  logic [1:0] aluop,
              output logic [3:0] alucontrol);
                    // increase to 4 bits for SLL

   always_comb
     case(aluop)
       2'b00: alucontrol = 4'b0010;  // add
       2'b01: alucontrol = 4'b1010;  // sub
```

```
            2'b11: alucontrol = 4'b1011;  // slt
            default: case(funct)          // RTYPE
                6'b100000: alucontrol = 4'b0010; // ADD
                6'b100010: alucontrol = 4'b1010; // SUB
                6'b100100: alucontrol = 4'b0000; // AND
                6'b100101: alucontrol = 4'b0001; // OR
                6'b101010: alucontrol = 4'b1011; // SLT
                6'b000000: alucontrol = 4'b0100; // SLL
                default:   alucontrol = 4'bxxxx; // ???
            endcase
        endcase
    endmodule

    module datapath(input  logic        clk, reset,
                    input  logic        memtoreg, pcsrc,
                    input  logic [1:0]  alusrc,    // LUI
                    input  logic        regdst,
                    input  logic        regwrite, jump,
                    input  logic [3:0]  alucontrol, // SLL
                    output logic        zero,
                    output logic [31:0] pc,
                    input  logic [31:0] instr,
                    output logic [31:0] aluresult, writedata,
                    input  logic [31:0] readdata,
                    output logic        ltez);   // LTEZ

        logic [4:0]  writereg;
        logic [31:0] pcnext, pcnextbr, pcplus4, pcbranch;
        logic [31:0] signimm, signimmsh;
        logic [31:0] upperimm;  // LUI
        logic [31:0] srca, srcb;
        logic [31:0] result;
        logic [31:0] memdata;

        // next PC logic
        flopr #(32) pcreg(clk, reset, pcnext, pc);
        adder       pcadd1(pc, 32'b100, pcplus4);
        sl2         immsh(signimm, signimmsh);
        adder       pcadd2(pcplus4, signimmsh, pcbranch);
        mux2 #(32)  pcbrmux(pcplus4, pcbranch, pcsrc,
                            pcnextbr);
        mux2 #(32)  pcmux(pcnextbr, {pcplus4[31:28],
                          instr[25:0], 2'b00},
                          jump, pcnext);

        // register file logic
        regfile     rf(clk, regwrite, instr[25:21],
                       instr[20:16], writereg,
                       writeresult, srca, writedata);

        mux2 #(5)   wrmux(instr[20:16], instr[15:11],
                          regdst, writereg);
```

```
  signext      se(instr[15:0], signimm);
  upimm        ui(instr[15:0], upperimm);  // LUI

  // ALU logic
  mux3 #(32)  srcbmux(writedata, signimm,
                      upperimm, alusrc,
                      srcb);       // LUI
  alu          alu(srca, srcb, alucontrol,
                   instr[10:6],  // SLL
                   aluresult, zero,
                   ltez); // BLEZ
  mux2 #(32)  rdmux(aluresult, readdata,
                    memtoreg, result);

endmodule


// upimm module needed for LUI
module upimm(input  logic [15:0] a,
             output logic [31:0] y);

  assign y = {a, 16'b0};
endmodule

// mux3 needed for LUI
module mux3 #(parameter WIDTH = 8)
             (input  logic [WIDTH-1:0] d0, d1, d2,
              input  logic [1:0]       s,
              output logic [WIDTH-1:0] y);

  assign #1 y = s[1] ? d2 : (s[0] ? d1 : d0);
endmodule

module alu(input  logic [31:0] A, B,
           input  logic [3:0]  F,
           input  logic [4:0]  shamt, // SLL
           output logic [31:0] Y,
           output logic        Zero,
           output logic        ltez);  // BLEZ

  logic [31:0] S, Bout;

  assign Bout = F[3] ? ~B : B;
  assign S = A + Bout + F[3];  // SLL

  always_comb
    case (F[2:0])
      3'b000: Y = A & Bout;
      3'b001: Y = A | Bout;
      3'b010: Y = S;
      3'b011: Y = S[31];
      3'b100: Y = (Bout << shamt);  // SLL
    endcase
```

```
assign Zero = (Y == 32'b0);
assign ltez = Zero | S[31];  // BLEZ

endmodule


module regfile(input  logic        clk,
               input  logic        we3,
               input  logic [4:0]  ra1, ra2, wa3,
               input  logic [31:0] wd3,
               output logic [31:0] rd1, rd2);

  logic [31:0] rf[31:0];

  // three ported register file
  // read two ports combinationally
  // write third port on rising edge of clk
  // register 0 hardwired to 0
  always_ff @(posedge clk)
    if (we3) rf[wa3] <= wd3;

  assign rd1 = (ra1 != 0) ? rf[ra1] : 0;
  assign rd2 = (ra2 != 0) ? rf[ra2] : 0;
endmodule

module adder(input  logic [31:0] a, b,
             output logic [31:0] y);

  assign y = a + b;
endmodule

module sl2(input  logic [31:0] a,
           output logic [31:0] y);

  // shift left by 2
  assign y = {a[29:0], 2'b00};
endmodule

module signext(input  logic [15:0] a,
               output logic [31:0] y);

  assign y = {{16{a[15]}}, a};
endmodule

module flopr #(parameter WIDTH = 8)
              (input  logic            clk, reset,
               input  logic [WIDTH-1:0] d,
               output logic [WIDTH-1:0] q);

  always_ff @(posedge clk, posedge reset)
    if (reset) q <= 0;
    else       q <= d;
```

```
    endmodule

    module mux2 #(parameter WIDTH = 8)
                 (input  logic [WIDTH-1:0] d0, d1,
                  input  logic             s,
                  output logic [WIDTH-1:0] y);

      assign y = s ? d1 : d0;
    endmodule
```

VHDL

```
    -- mips.vhd

    library IEEE;
    use    IEEE.STD_LOGIC_1164.all;    use    IEEE.NUMERIC_STD_UN-
SIGNED.all;

    entity testbench is
    end;

    architecture test of testbench is
      component top
        port(clk, reset:            in  STD_LOGIC;
             writedata, dataadr:  out STD_LOGIC_VECTOR(31 downto 0);
              memwrite:              out STD_LOGIC);
      end component;
      signal writedata, dataadr:    STD_LOGIC_VECTOR(31 downto 0);
      signal clk, reset,  memwrite: STD_LOGIC;
    begin

      -- instantiate device to be tested
      dut: top port map(clk, reset, writedata, dataadr, memwrite);

      -- Generate clock with 10 ns period
      process begin
        clk <= '1';
        wait for 5 ns;
        clk <= '0';
        wait for 5 ns;
      end process;

      -- Generate reset for first two clock cycles
      process begin
        reset <= '1';
        wait for 22 ns;
        reset <= '0';
        wait;
      end process;

      -- check that 7 gets written to address 84 at end of program
```

```
            process (clk) begin
               if (clk'event and clk = '0' and memwrite = '1') then
                  if (to_integer(dataadr) = 84 and to_integer(writedata) =
7) then
                     report "NO ERRORS: Simulation succeeded" severity fail-
ure;
                  elsif (dataadr /= 80) then
                     report "Simulation failed" severity failure;
                  end if;
               end if;
            end process;
         end;

         library IEEE;
         use    IEEE.STD_LOGIC_1164.all;    use    IEEE.NUMERIC_STD_UN-
SIGNED.all;

         entity top is -- top-level design for testing
           port(clk, reset:            in     STD_LOGIC;
                writedata, dataadr:   buffer STD_LOGIC_VECTOR(31 downto
0);
                memwrite:              buffer STD_LOGIC);
         end;

         architecture test of top is
           component mips
             port(clk, reset:          in  STD_LOGIC;
                  pc:                   out STD_LOGIC_VECTOR(31 downto 0);
                  instr:                in  STD_LOGIC_VECTOR(31 downto 0);
                  memwrite:             out STD_LOGIC;
                  aluresult:            out STD_LOGIC_VECTOR(31 downto 0);
                  writedata:            out STD_LOGIC_VECTOR(31 downto 0);
                  readdata:             in  STD_LOGIC_VECTOR(31 downto 0));
           end component;
           component imem
             port(a:  in  STD_LOGIC_VECTOR(5 downto 0);
                  rd: out STD_LOGIC_VECTOR(31 downto 0));
           end component;
           component dmem
             port(clk, we:  in STD_LOGIC;
                  a, wd:    in STD_LOGIC_VECTOR(31 downto 0);
                  rd:       out STD_LOGIC_VECTOR(31 downto 0));
           end component;
           signal pc, instr,
                  readdata: STD_LOGIC_VECTOR(31 downto 0);
         begin
           -- instantiate processor and memories
            mips1: mips port map(clk, reset, pc, instr, memwrite, dataadr,
                                 writedata, readdata);
            imem1: imem port map(pc(7 downto 2), instr);
            dmem1: dmem port map(clk, memwrite, dataadr, writedata, re-
addata);
         end;
```

```
library IEEE;
use IEEE.STD_LOGIC_1164.all; use STD.TEXTIO.all;
use IEEE.NUMERIC_STD_UNSIGNED.all;

entity dmem is -- data memory
  port(clk, we:  in STD_LOGIC;
       a, wd:    in STD_LOGIC_VECTOR(31 downto 0);
       rd:       out STD_LOGIC_VECTOR(31 downto 0));
end;

architecture behave of dmem is
begin
  process is
    type ramtype is array (63 downto 0) of STD_LOGIC_VECTOR(31
downto 0);
    variable mem: ramtype;
  begin
    -- read or write memory
    loop
      if clk'event and clk = '1' then
        if (we = '1') then mem(to_integer(a(7 downto 2))) := wd;
          end if;
      end if;
      rd <= mem(to_integer(a(7 downto 2)));
      wait on clk, a;
    end loop;

  end process;
end;

library IEEE;
use IEEE.STD_LOGIC_1164.all; use STD.TEXTIO.all;
use IEEE.NUMERIC_STD_UNSIGNED.all;

entity imem is -- instruction memory
  port(a:  in  STD_LOGIC_VECTOR(5 downto 0);
       rd: out STD_LOGIC_VECTOR(31 downto 0));
end;

architecture behave of imem is
begin
  process is
    file mem_file: TEXT;
    variable L: line;
    variable ch: character;
    variable i, index, result: integer;
    type ramtype is array (63 downto 0) of STD_LOGIC_VECTOR(31
downto 0);
    variable mem: ramtype;
  begin
    -- initialize memory from file
    for i in 0 to 63 loop -- set all contents low
```

```vhdl
            mem(i) := (others => '0');
        end loop;
        index := 0;
          FILE_OPEN(mem_file,  "C:/docs/DDCA2e/hdl/memfile.dat",
READ_MODE);
        while not endfile(mem_file) loop
          readline(mem_file, L);
          result := 0;
          for i in 1 to 8 loop
            read(L, ch);
            if '0' <= ch and ch <= '9' then
                result := character'pos(ch) - character'pos('0');
            elsif 'a' <= ch and ch <= 'f' then
              result := character'pos(ch) - character'pos('a')+10;
            else report "Format error on line " & integer'image(in-
dex)
                  severity error;
            end if;
             mem(index)(35-i*4 downto 32-i*4) :=to_std_logic_vec-
tor(result,4);
          end loop;
          index := index + 1;
        end loop;

        -- read memory
        loop
          rd <= mem(to_integer(a));
          wait on a;
        end loop;
      end process;
    end;

    library IEEE; use IEEE.STD_LOGIC_1164.all;

    entity mips is -- single cycle MIPS processor
      port(clk, reset:        in  STD_LOGIC;
          pc:                 out STD_LOGIC_VECTOR(31 downto 0);
          instr:              in  STD_LOGIC_VECTOR(31 downto 0);
          memwrite:           out STD_LOGIC;
          aluresult:          out STD_LOGIC_VECTOR(31 downto 0);
          writedata:          out STD_LOGIC_VECTOR(31 downto 0);
          readdata:           in  STD_LOGIC_VECTOR(31 downto 0));
    end;

    architecture struct of mips is
      component controller
        port(op, funct:          in  STD_LOGIC_VECTOR(5 downto 0);
            zero:                in  STD_LOGIC;
            memtoreg, memwrite:  out STD_LOGIC;
            pcsrc:               out STD_LOGIC;
          alusrc:            out STD_LOGIC_VECTOR(1 downto 0);  -- LUI
            regdst, regwrite:  out STD_LOGIC;
            jump:              out STD_LOGIC;
```

```vhdl
        alucontrol:           out STD_LOGIC_VECTOR(3 downto 0);  -
- SLL
        ltez:                 out STD_LOGIC);                    -- BLEZ
    end component;
    component datapath
      port(clk, reset:        in  STD_LOGIC;
           memtoreg, pcsrc:   in  STD_LOGIC;
           alusrc, regdst:    in  STD_LOGIC;
           regwrite, jump:    in  STD_LOGIC;
           alucontrol:        in  STD_LOGIC_VECTOR(2 downto 0);
           zero:              out STD_LOGIC;
          pc:                 buffer STD_LOGIC_VECTOR(31 downto 0);
           instr:             in STD_LOGIC_VECTOR(31 downto 0);
         aluresult:           buffer STD_LOGIC_VECTOR(31 downto 0);
          writedata:          buffer STD_LOGIC_VECTOR(31 downto 0);
           readdata:          in  STD_LOGIC_VECTOR(31 downto 0));
    end component;
    signal memtoreg: STD_LOGIC;
    signal alusrc: STD_LOGIC_VECTOR(1 downto 0);     -- LUI
    signal regdst, regwrite, jump, pcsrc: STD_LOGIC;
    signal zero: STD_LOGIC;
    signal alucontrol: STD_LOGIC_VECTOR(3 downto 0); -- SLL
    signal ltez: STD_LOGIC;                          -- BLEZ
  begin
    cont: controller port map(instr(31 downto 26), instr(5 downto
0),
                       zero, memtoreg, memwrite, pcsrc, alusrc,
                          regdst, regwrite, jump, alucontrol,
                            ltez);  -- BLEZ
      dp: datapath port map(clk, reset, memtoreg, pcsrc, alusrc,
regdst,
                     regwrite, jump, alucontrol, zero, pc, instr,
                         aluresult, writedata, readdata,
                         ltez);  -- BLEZ
    end;

    library IEEE; use IEEE.STD_LOGIC_1164.all;

    entity controller is -- single cycle control decoder
      port(op, funct:          in  STD_LOGIC_VECTOR(5 downto 0);
           zero:               in  STD_LOGIC;
           memtoreg, memwrite: out STD_LOGIC;
           pcsrc:              out STD_LOGIC;
         alusrc:               out STD_LOGIC_VECTOR(1 downto 0); -- LUI
           regdst, regwrite:   out STD_LOGIC;
           jump:               out STD_LOGIC;
           alucontrol:         out STD_LOGIC_VECTOR(3 downto 0);  -
- SLL
           ltez:               out STD_LOGIC);                    -- BLEZ
    end;

    architecture struct of controller is
      component maindec
```

```vhdl
                    port(op:                     in  STD_LOGIC_VECTOR(5 downto 0);
                         memtoreg, memwrite: out STD_LOGIC;
                         branch:                 out STD_LOGIC;
                         alusrc:                 out STD_LOGIC_VECTOR(1 downto 0);
-- LUI
                         regdst, regwrite:   out STD_LOGIC;
                         jump:                   out STD_LOGIC;
                         aluop:                  out STD_LOGIC_VECTOR(1 downto 0);
                         blez:                   out STD_LOGIC);
          end component;
          component aludec
            port(funct:     in  STD_LOGIC_VECTOR(5 downto 0);
                 aluop:     in  STD_LOGIC_VECTOR(1 downto 0);
                 alucontrol: out STD_LOGIC_VECTOR(3 downto 0));  -- SLL
          end component;
          signal aluop:  STD_LOGIC_VECTOR(1 downto 0);
          signal branch: STD_LOGIC;
          signal blez:   STD_LOGIC; --BLEZ
        begin
          md: maindec port map(op, memtoreg, memwrite, branch,
                            alusrc, regdst, regwrite, jump, aluop, blez);
          ad: aludec port map(funct, aluop, alucontrol);

          --BLEZ
          pcsrc <= (branch and zero) or (blez and ltez);
        end;

        library IEEE; use IEEE.STD_LOGIC_1164.all;

        entity maindec is -- main control decoder
          port(op:                     in  STD_LOGIC_VECTOR(5 downto 0);
               memtoreg, memwrite: out STD_LOGIC;
               branch:                 out STD_LOGIC;
             alusrc:                out STD_LOGIC_VECTOR(1 downto 0);  -- LUI
               regdst, regwrite:   out STD_LOGIC;
               jump:                   out STD_LOGIC;
               aluop:                  out STD_LOGIC_VECTOR(1 downto 0);
               blez:                   out STD_LOGIC);
        end;

        architecture behave of maindec is
          signal controls: STD_LOGIC_VECTOR(10 downto 0);
        begin
          process(all) begin
            case op is
              when "000000" => controls <= "11000001000"; -- RTYPE
              when "100011" => controls <= "10010010000"; -- LW
              when "101011" => controls <= "00010100000"; -- SW
              when "000100" => controls <= "00001000100"; -- BEQ
              when "001000" => controls <= "10010000000"; -- ADDI
              when "000010" => controls <= "00000000010"; -- J
              when "001010" => controls <= "10010001100"; -- SLTI
              when "001111" => controls <= "10100000000"; -- LUI
```

```
         when "000110" => controls <= "00000000101"; -- BLEZ
           when others   => controls <= "-----------"; -- illegal op
         end case;
      end process;

      (regwrite, regdst, alusrc, branch, memwrite,
       memtoreg, aluop(1 downto 0), jump, blez) <= controls;
    end;

    library IEEE; use IEEE.STD_LOGIC_1164.all;

    entity aludec is -- ALU control decoder
      port(funct:      in  STD_LOGIC_VECTOR(5 downto 0);
           aluop:      in  STD_LOGIC_VECTOR(1 downto 0);
           alucontrol: out STD_LOGIC_VECTOR(3 downto 0));  -- SLL
    end;

    architecture behave of aludec is
    begin
      process(all) begin
        case aluop is
          when "00" => alucontrol <= "0010"; -- add
          when "01" => alucontrol <= "1010"; -- sub
          when "11" => alucontrol <= "1011"; -- slt
         when others => case funct is       -- R-type instructions
                          when "100000" => alucontrol <= "0010";
-- add
                          when "100010" => alucontrol <= "1010";
-- sub
                          when "100100" => alucontrol <= "0000";
-- and
                        when "100101" => alucontrol <= "0001"; -- or
                          when "101010" => alucontrol <= "1011";
-- slt
                          when "000000" => alucontrol <= "0100";
-- sll
                        when others   => alucontrol <= "----"; -- ???
                          end case;
        end case;
      end process;
    end;

    library IEEE; use IEEE.STD_LOGIC_1164.all; use IEEE.STD_LOG-
IC_ARITH.all;

    entity datapath is  -- MIPS datapath
      port(clk, reset:       in  STD_LOGIC;
           memtoreg, pcsrc:  in  STD_LOGIC;
          alusrc:           in STD_LOGIC_VECTOR(1 downto 0);  -- LUI
           alusrc, regdst:   in  STD_LOGIC;
           regwrite, jump:   in  STD_LOGIC;
           alucontrol:       in  STD_LOGIC_VECTOR(3 downto 0);   -
- SLL
```

```
                              zero:                out STD_LOGIC;
                              pc:                  buffer STD_LOGIC_VECTOR(31 downto 0);
                              instr:               in  STD_LOGIC_VECTOR(31 downto 0);
                              aluresult:           buffer STD_LOGIC_VECTOR(31 downto 0);
                              writedata:           buffer STD_LOGIC_VECTOR(31 downto 0);
                              readdata:            in  STD_LOGIC_VECTOR(31 downto 0);
                              ltez:              out STD_LOGIC);                       -- LTEZ
                   end;

                   architecture struct of datapath is
                     component alu
                       port(a, b:       in  STD_LOGIC_VECTOR(31 downto 0);
                            alucontrol: in  STD_LOGIC_VECTOR(3 downto 0);   --SLL
                            shamt:      in  STD_LOGIC_VECTOR(4 downto 0);   --SLL
                            result:     buffer STD_LOGIC_VECTOR(31 downto 0);
                            zero:       buffer STD_LOGIC;                   --BLEZ
                            ltez:       out STD_LOGIC);                     --BLEZ
                     end component;
                     component regfile
                       port(clk:            in  STD_LOGIC;
                            we3:            in  STD_LOGIC;
                            ra1, ra2, wa3: in  STD_LOGIC_VECTOR(4 downto 0);
                            wd3:            in  STD_LOGIC_VECTOR(31 downto 0);
                            rd1, rd2:       out STD_LOGIC_VECTOR(31 downto 0));
                     end component;
                     component adder
                       port(a, b: in  STD_LOGIC_VECTOR(31 downto 0);
                            y:    out STD_LOGIC_VECTOR(31 downto 0));
                     end component;
                     component sl2
                       port(a: in  STD_LOGIC_VECTOR(31 downto 0);
                            y: out STD_LOGIC_VECTOR(31 downto 0));
                     end component;
                     component signext
                       port(a: in  STD_LOGIC_VECTOR(15 downto 0);
                            y: out STD_LOGIC_VECTOR(31 downto 0));
                     end component;
                     component upimm
                       port(a: in  STD_LOGIC_VECTOR(15 downto 0);
                            y: out STD_LOGIC_VECTOR(31 downto 0));
                     end component;
                     component flopr generic(width: integer);
                       port(clk, reset: in  STD_LOGIC;
                            d:              in  STD_LOGIC_VECTOR(width-1 downto 0);
                            q:              out STD_LOGIC_VECTOR(width-1 downto 0));
                     end component;
                     component mux2 generic(width: integer);
                       port(d0, d1: in  STD_LOGIC_VECTOR(width-1 downto 0);
                            s:      in  STD_LOGIC;
                            y:      out STD_LOGIC_VECTOR(width-1 downto 0));
                     end component;
                     component mux3 generic(width: integer);
                       port(d0, d1, d2: in  STD_LOGIC_VECTOR(width-1 downto 0);
```

```vhdl
            s:             in  STD_LOGIC_VECTOR(1 downto 0);
            y:             out STD_LOGIC_VECTOR(width-1 downto 0));
    end component;
    signal writereg:           STD_LOGIC_VECTOR(4 downto 0);
    signal pcjump, pcnext,
           pcnextbr, pcplus4,
           pcbranch:            STD_LOGIC_VECTOR(31 downto 0);
    signal upperimm:           STD_LOGIC_VECTOR(31 downto 0);   -
- LUI
    signal signimm, signimmsh: STD_LOGIC_VECTOR(31 downto 0);
    signal srca, srcb, result: STD_LOGIC_VECTOR(31 downto 0);
  begin
    -- next PC logic
    pcjump <= pcplus4(31 downto 28) & instr(25 downto 0) & "00";
   pcreg: flopr generic map(32) port map(clk, reset, pcnext, pc);
    pcadd1: adder port map(pc, X"00000004", pcplus4);
    immsh: sl2 port map(signimm, signimmsh);
    pcadd2: adder port map(pcplus4, signimmsh, pcbranch);
    pcbrmux: mux2 generic map(32) port map(pcplus4, pcbranch,
                                              pcsrc, pcnextbr);
    pcmux: mux2 generic map(32) port map(pcnextbr, pcjump, jump,
pcnext);

    -- register file logic
    rf: regfile port map(clk, regwrite, instr(25 downto 21),
                  instr(20 downto 16), writereg, result, srca,
   writedata);
    wrmux: mux2 generic map(5) port map(instr(20 downto 16),
                                        instr(15 downto 11),
                                        regdst, writereg);
    resmux: mux2 generic map(32) port map(aluresult, readdata,
                                          memtoreg, result);
    se: signext port map(instr(15 downto 0), signimm);
    ui: upimm port map(instr(15 downto 0), upperimm);  --LUI

    -- ALU logic
     srcbmux: mux3 generic map(32) port map(writedata, signimm,
upperimm,
                                          alusrc, srcb); -- LUI
    mainalu: alu port map(srca, srcb, alucontrol, instr(10 downto
6), --SLL
                          aluresult, zero, ltez);  --BLEZ

    end;

    library IEEE; use IEEE.STD_LOGIC_1164.all;
    use IEEE.NUMERIC_STD_UNSIGNED.all;

    entity regfile is -- three-port register file
      port(clk:             in  STD_LOGIC;
           we3:             in  STD_LOGIC;
           ra1, ra2, wa3:   in  STD_LOGIC_VECTOR(4 downto 0);
           wd3:             in  STD_LOGIC_VECTOR(31 downto 0);
```

```vhdl
                        rd1, rd2:     out STD_LOGIC_VECTOR(31 downto 0));
end;

architecture behave of regfile is
    type ramtype is array (31 downto 0) of STD_LOGIC_VECTOR(31
downto 0);
   signal mem: ramtype;
begin
  -- three-ported register file
  -- read two ports combinationally
  -- write third port on rising edge of clock
  -- register 0 hardwired to 0
  process(clk) begin
    if rising_edge(clk) then
       if we3 = '1' then mem(to_integer(wa3)) <= wd3;
       end if;
    end if;
  end process;
  process(all) begin
   if (to_integer(ra1) = 0) then rd1 <= X"00000000"; -- register
0 holds 0
      else rd1 <= mem(to_integer(ra1));
      end if;
      if (to_integer(ra2) = 0) then rd2 <= X"00000000";
      else rd2 <= mem(to_integer(ra2));
      end if;
  end process;
end;

library IEEE; use IEEE.STD_LOGIC_1164.all;
use IEEE.NUMERIC_STD_UNSIGNED.all;

entity adder is -- adder
  port(a, b: in  STD_LOGIC_VECTOR(31 downto 0);
       y:    out STD_LOGIC_VECTOR(31 downto 0));
end;

architecture behave of adder is
begin
  y <= a + b;
end;


library IEEE; use IEEE.STD_LOGIC_1164.all;

entity sl2 is -- shift left by 2
  port(a: in  STD_LOGIC_VECTOR(31 downto 0);
       y: out STD_LOGIC_VECTOR(31 downto 0));
end;

architecture behave of sl2 is
begin
  y <= a(29 downto 0) & "00";
```

```
end;

library IEEE; use IEEE.STD_LOGIC_1164.all;

entity signext is -- sign extender
  port(a: in  STD_LOGIC_VECTOR(15 downto 0);
       y: out STD_LOGIC_VECTOR(31 downto 0));
end;

architecture behave of signext is
begin
  y <= X"ffff" & a when a(15) else X"0000" & a;
end;


library IEEE; use IEEE.STD_LOGIC_1164.all;
entity upimm is -- create upper immediate for LUI
  port(a: in  STD_LOGIC_VECTOR(15 downto 0);
       y: out STD_LOGIC_VECTOR(31 downto 0));
end;

architecture behave of upimm is
begin
  y <= a & X"0000";
end;

library IEEE; use IEEE.STD_LOGIC_1164.all;  use IEEE.STD_LOG-
IC_ARITH.all;

entity flopr is -- flip-flop with synchronous reset
  generic(width: integer);
  port(clk, reset: in  STD_LOGIC;
       d:          in  STD_LOGIC_VECTOR(width-1 downto 0);
       q:          out STD_LOGIC_VECTOR(width-1 downto 0));
end;

architecture asynchronous of flopr is
begin
  process(clk, reset) begin
    if reset then  q <= (others => '0');
    elsif rising_edge(clk) then
      q <= d;
    end if;
  end process;
end;

library IEEE; use IEEE.STD_LOGIC_1164.all;
entity mux2 is -- two-input multiplexer
  generic(width: integer);
  port(d0, d1: in  STD_LOGIC_VECTOR(width-1 downto 0);
       s:      in  STD_LOGIC;
       y:      out STD_LOGIC_VECTOR(width-1 downto 0));
end;
```

```vhdl
architecture behave of mux2 is
begin
  y <= d1 when s else d0;
end;

-- 3:1 mux needed for LUI
library IEEE; use IEEE.STD_LOGIC_1164.all;
entity mux3 is -- three-input multiplexer
  generic(width: integer);
  port(d0, d1, d2: in  STD_LOGIC_VECTOR(width-1 downto 0);
       s:          in  STD_LOGIC_VECTOR(1 downto 0);
       y:          out STD_LOGIC_VECTOR(width-1 downto 0));
end;

architecture behave of mux3 is
begin
  y <= d1 when s(1) else (d1 when s(0) else d0);
end;


library IEEE; use IEEE.STD_LOGIC_1164.all;
use IEEE.NUMERIC_STD_UNSIGNED.all;

entity alu is
  port(a, b:      in  STD_LOGIC_VECTOR(31 downto 0);
       alucontrol: in  STD_LOGIC_VECTOR(3 downto 0);   --SLL
       shamt:     in  STD_LOGIC_VECTOR(4 downto 0);   --SLL
       result:    buffer STD_LOGIC_VECTOR(31 downto 0);
       zero:      buffer STD_LOGIC;                     --BLEZ
       ltez:      out STD_LOGIC);                       --BLEZ
end;

architecture behave of alu is
  signal condinvb, sum: STD_LOGIC_VECTOR(31 downto 0);
begin
  condinvb <= not b when alucontrol(3) else b;
  sum <= a + condinvb + alucontrol(3);

  process(all) begin
    case alucontrol(2 downto 0) is
      when "000"  => result <= a and b;
      when "001"  => result <= a or b;
      when "010"  => result <= sum;
      when "011"  => result <= (0 => sum(31), others => '0');
      when "100"  => result <= (condinvb << shamt);   --SLL
      when others => result <= (others => 'X');
    end case;
  end process;

  zero <= '1' when result = X"00000000" else '0';
  ltez <= zero or sum(31);
end;
```

Exercise 7.13

(a) `srlv`

First, we show the modifications to the ALU.
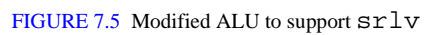
FIGURE 7.5 Modified ALU to support `srlv`

Next, we show the modifications to the ALU decoder.

ALUControl$_{3:0}$	Function
0000	A AND B
0001	A OR B
0010	A + B
0011	not used
1000	A AND $\overline{B}$
1001	A OR $\overline{B}$
1010	A - B
1011	SLT
0100	**SRLV**

FIGURE 7.6 Modified ALU operations to support `srlv`

ALUOp	Funct	ALUControl
00	X	0010 (add)
X1	X	1010 (subtract)
1X	100000 (`add`)	0010 (add)
1X	100010 (`sub`)	1010 (subtract)
1X	100100 (`and`)	0000 (and)
1X	100101 (`or`)	0001 (or)
1X	101010 (`slt`)	1011 (set less than)
1X	**000110 (`srlv`)**	**0100 (shift right logical variable)**

TABLE 7.8 ALU decoder truth table

Next, we show the changes to the datapath.   The only modification is the width of *ALUControl*. No changes are made to the datapath main control FSM.
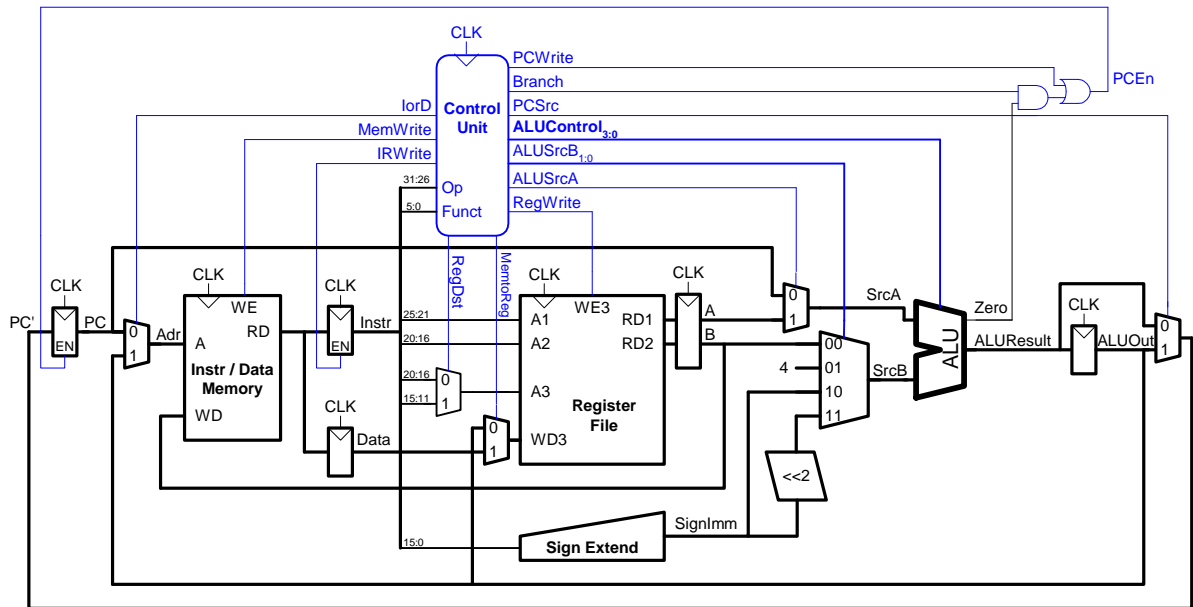
FIGURE 7.7 Modified multicycle MIPS datapath to support `sll`

(b) `ori`

We add a zero extension unit to the datapath, extend the *ALUSrcB* signal from 2 bits to 3 bits, and extend the SrcB multiplexer from 4 inputs to 5 inputs. We also modify the ALU decoder and main control FSM.
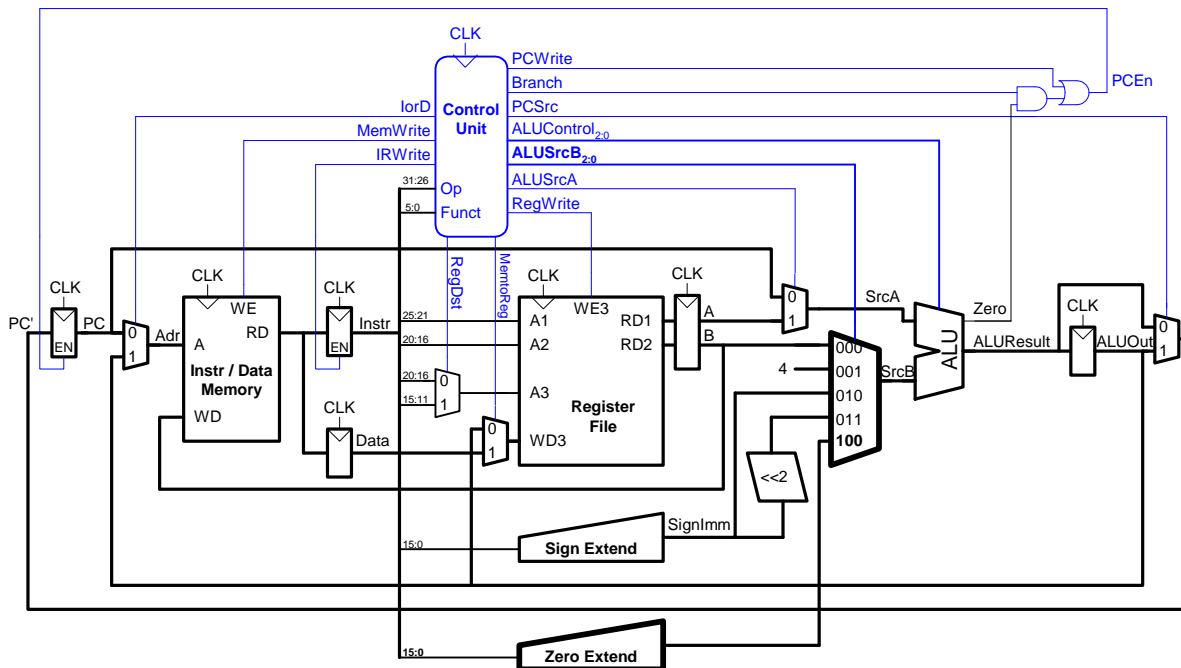
FIGURE 7.8 Modified datapath for `ori`

A L U O p	F u n c t	A L U C o n t r o l
00	X	010 (add)
01	X	110 (subtract)
11	**X**	**001 (or)**
10	100000 (`add`)	010 (add)
10	100010 (`sub`)	110 (subtract)
10	100100 (`and`)	000 (and)

TABLE 7.9 ALU decoder truth table

ALUOp	Funct	ALUControl
10	100101 (or)	001 (or)
10	101010 (slt)	111 (set less than)

TABLE 7.9 ALU decoder truth table
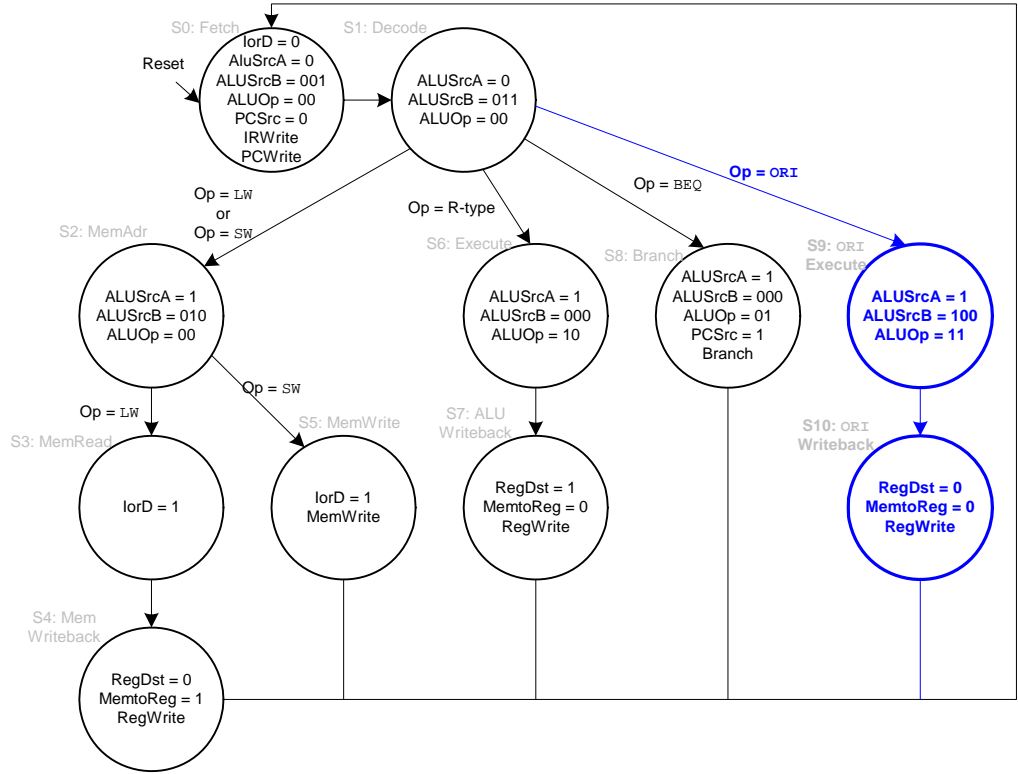
(c) `xori`

First, we modify the ALU and the ALU decoder.
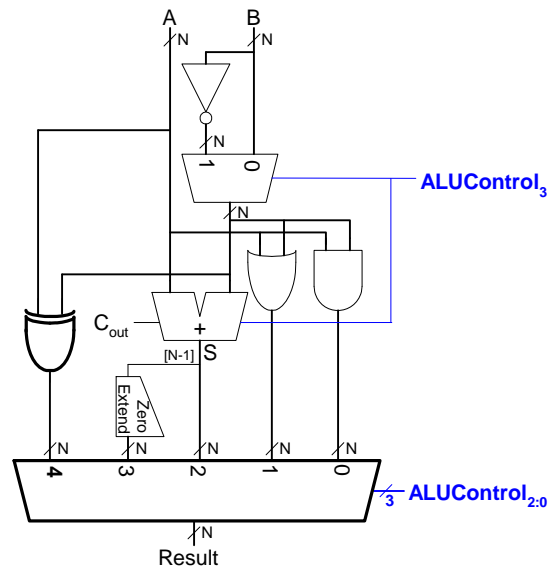
l

ALUControl$_{3:0}$	Function
0000	A AND B
0001	A OR B
0010	A + B
0011	not used
1000	A AND $\overline{B}$
1001	A OR $\overline{B}$
1010	A - B
1011	SLT
0100	**A XOR B**

ALUOp	Funct	ALUControl
00	X	0010 (add)
01	X	1010 (subtract)
11	**X**	**0100 (xor)**
10	100000 (`add`)	0010 (add)
10	100010 (`sub`)	1010 (subtract)
10	100100 (`and`)	0000 (and)
10	100101 (`or`)	0001 (or)
10	101010 (`slt`)	1011 (set less than)

TABLE 7.10 ALU decoder truth table for `xori`

Next, we modify the datapath. We change the buswidth of the *ALUControl* signal from 3 bits to 4 bits and the *ALUSrcB* signal from 2 bits to 3 bits. We also extend the SrcB mux and add a zero-extension unit.

And finally, we modify the main control FSM.
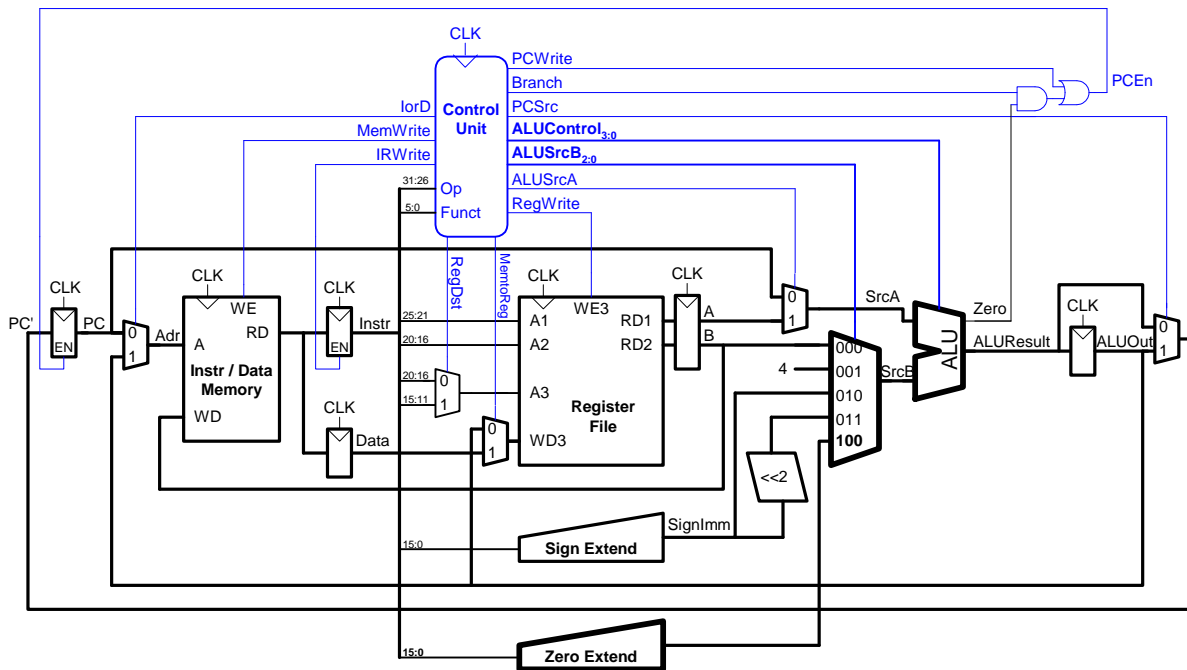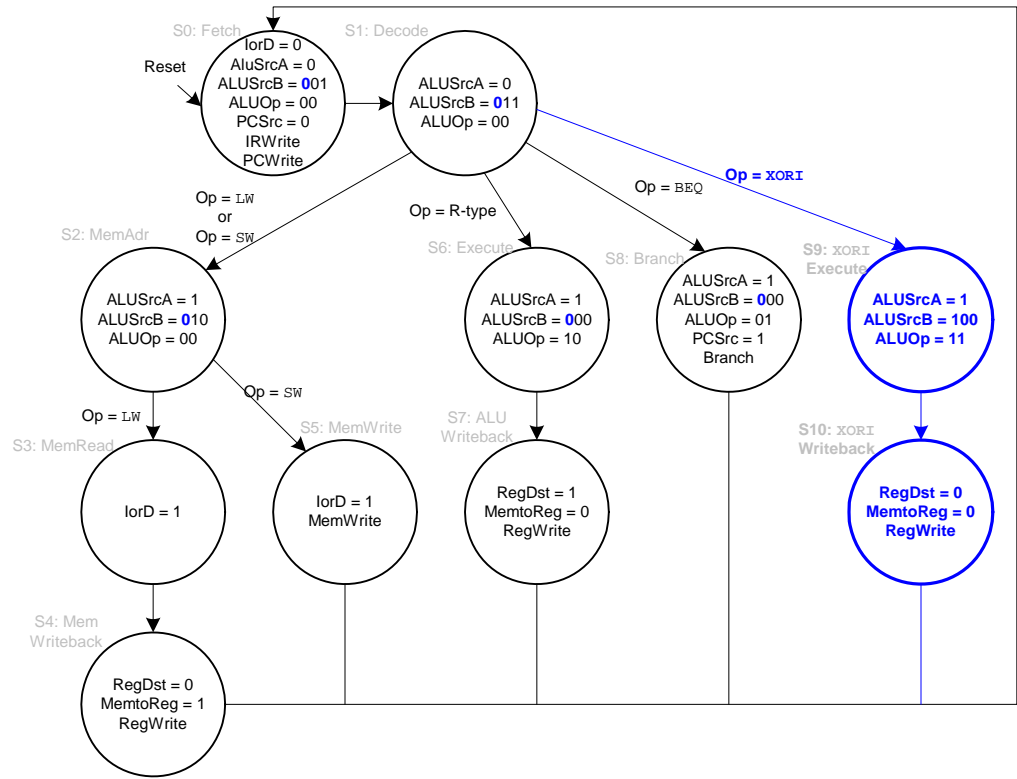
(d) jr

First, we extend the ALU Decoder for jr.

ALUOp	Funct	ALUControl
00	X	010 (add)
X1	X	110 (subtract)
1X	100000 (add)	010 (add)
1X	100010 (sub)	110 (subtract)
1X	100100 (and)	000 (and)
1X	100101 (or)	001 (or)

TABLE 7.11 ALU decoder truth table with jr

A L U O p	F u n c t	A L U C o n t r o l
1X	101010 (slt)	111 (set less than)
1X	001000 (jr)	010 (add)

TABLE 7.11 ALU decoder truth table with jr

Next, we modify the main controller. The datapath requires no modification.
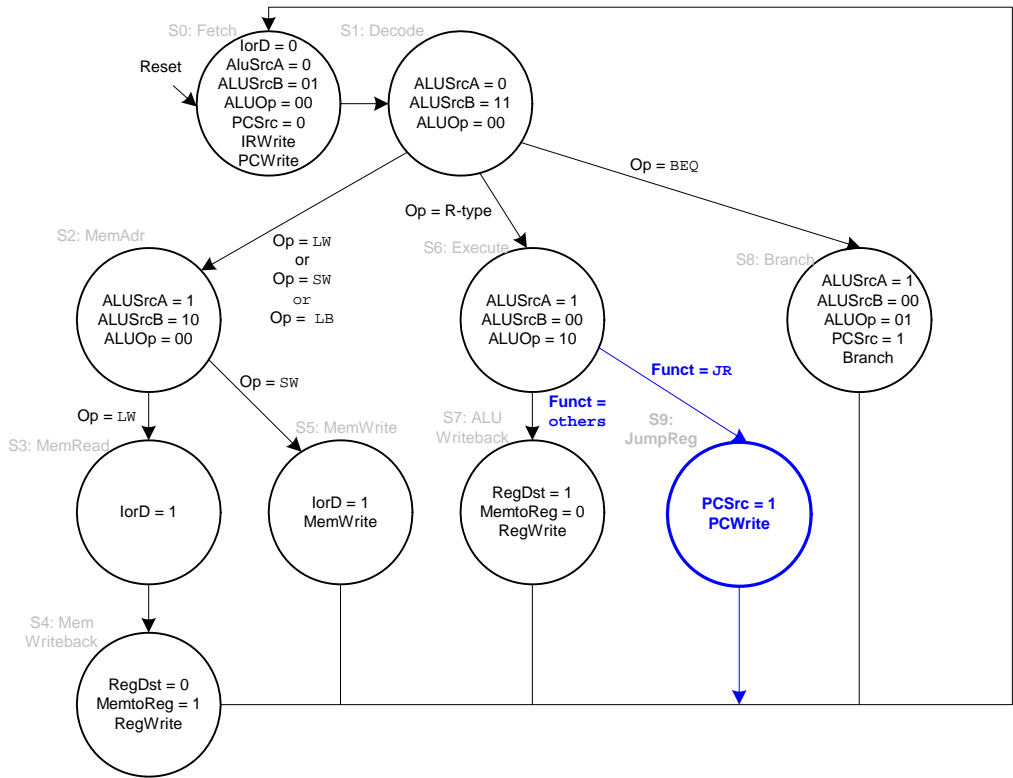
Exercise 7.15

Yes, it is possible to add this instruction without modifying the register file. First we show the modifications to the datapath. The only modification is adding the rs field of the instruction (*Instruction*$_{25:21}$) to the input of the write address mux of the register file. *RegDst* must be expanded to two bits.
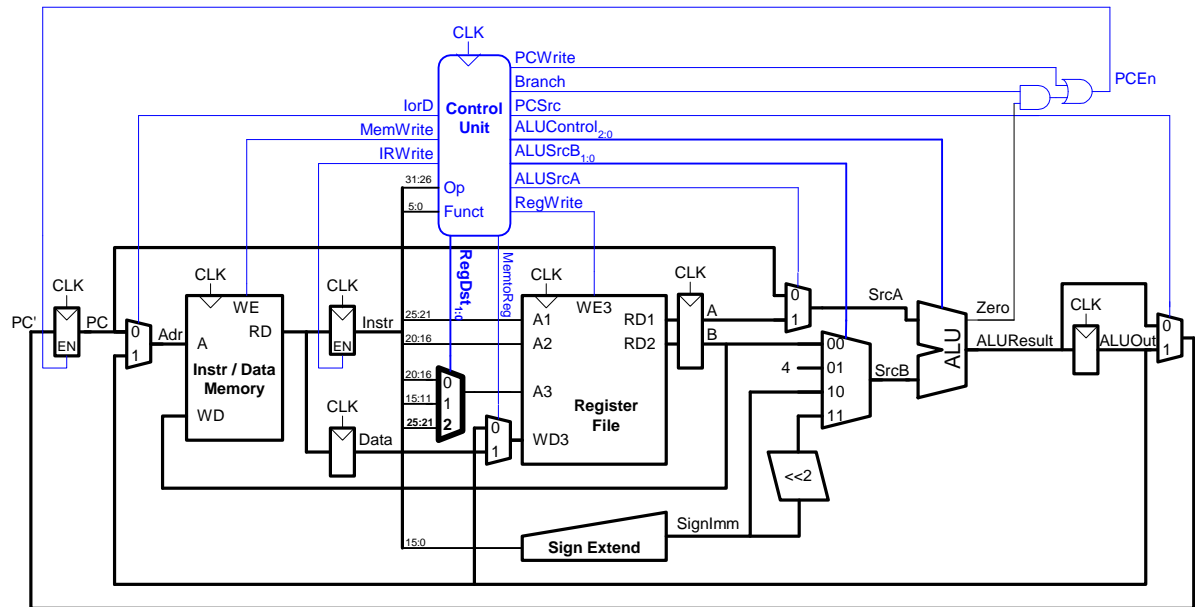
The finite state machine requires another state to write the `rs` register. If execution time is critical, another adder could be placed just after the A/B register to add 4 to A. Then in State 3, as memory is read, the register file could be written back with the incremented `rs`. In that case, `lwinc` would require the same number of cycles as `lw`. The penalty, however, would be chip area, and thus power and cost.
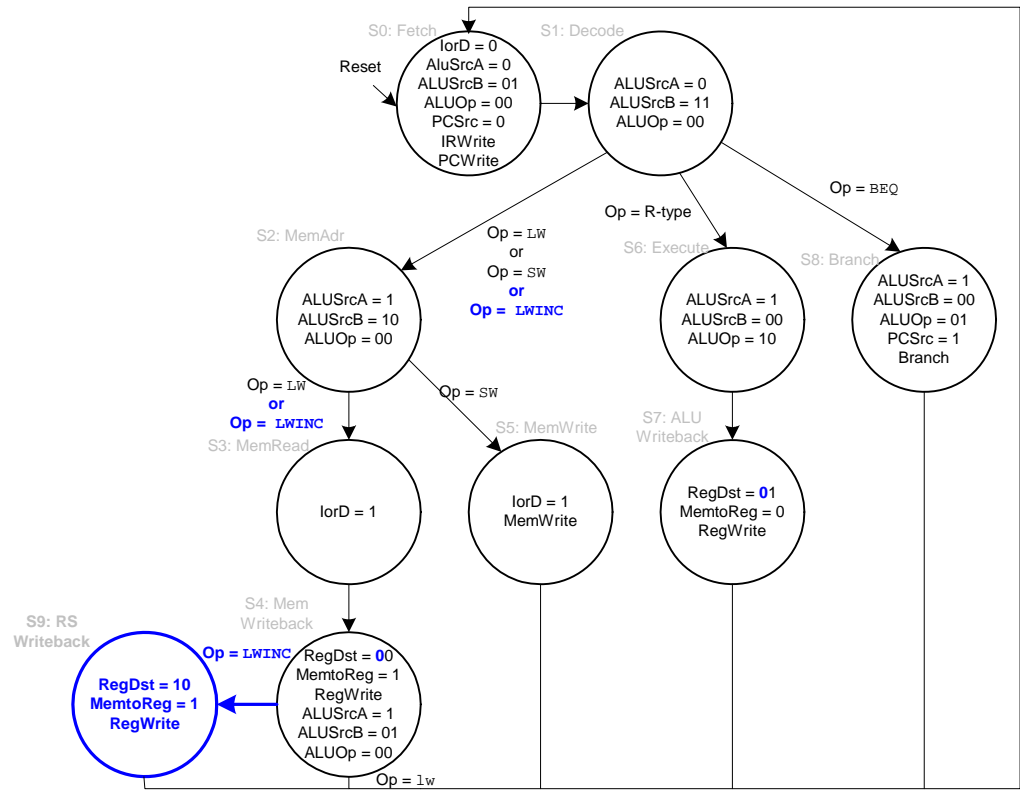
Exercise 7.17

We add an enable signal, *FlPtEn*, to the result register.
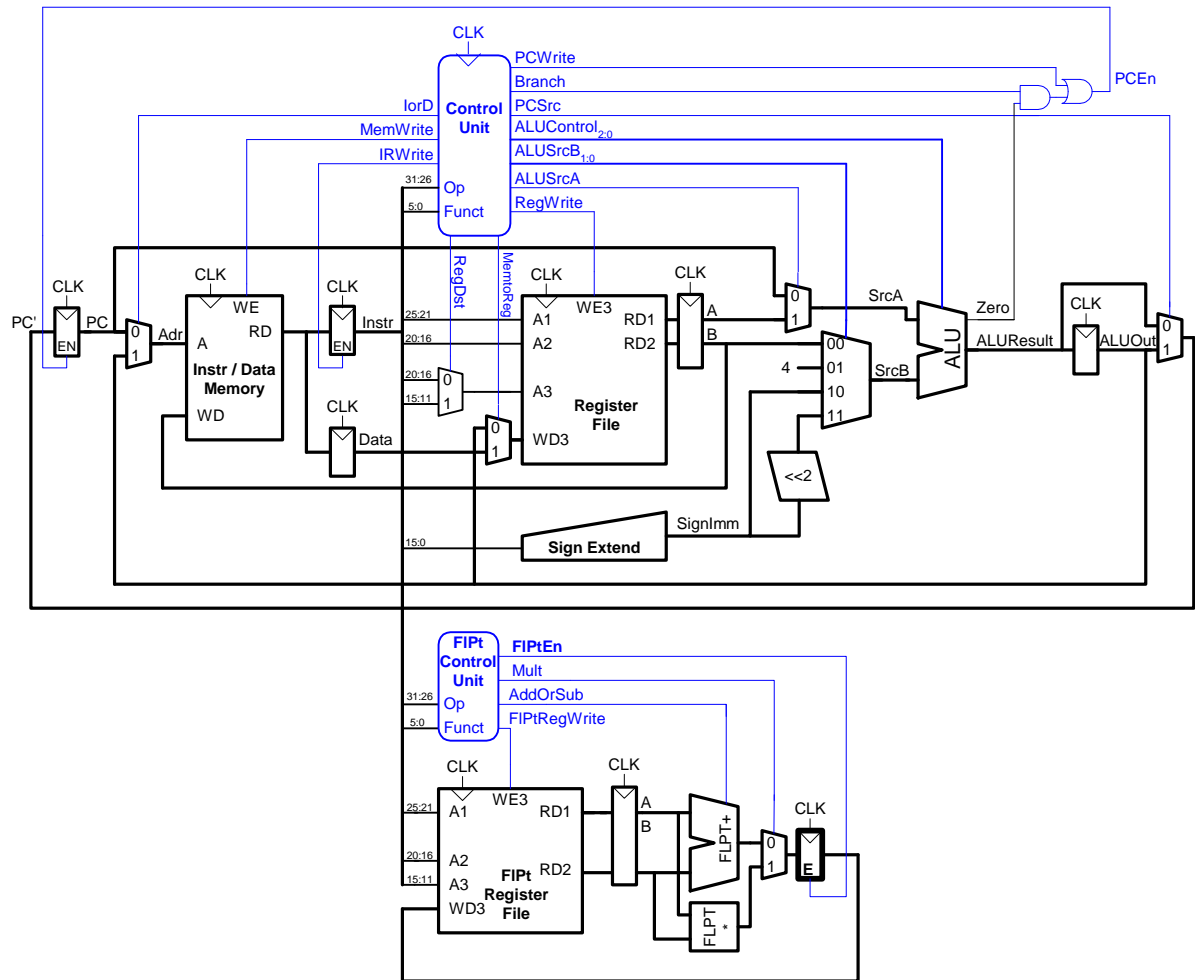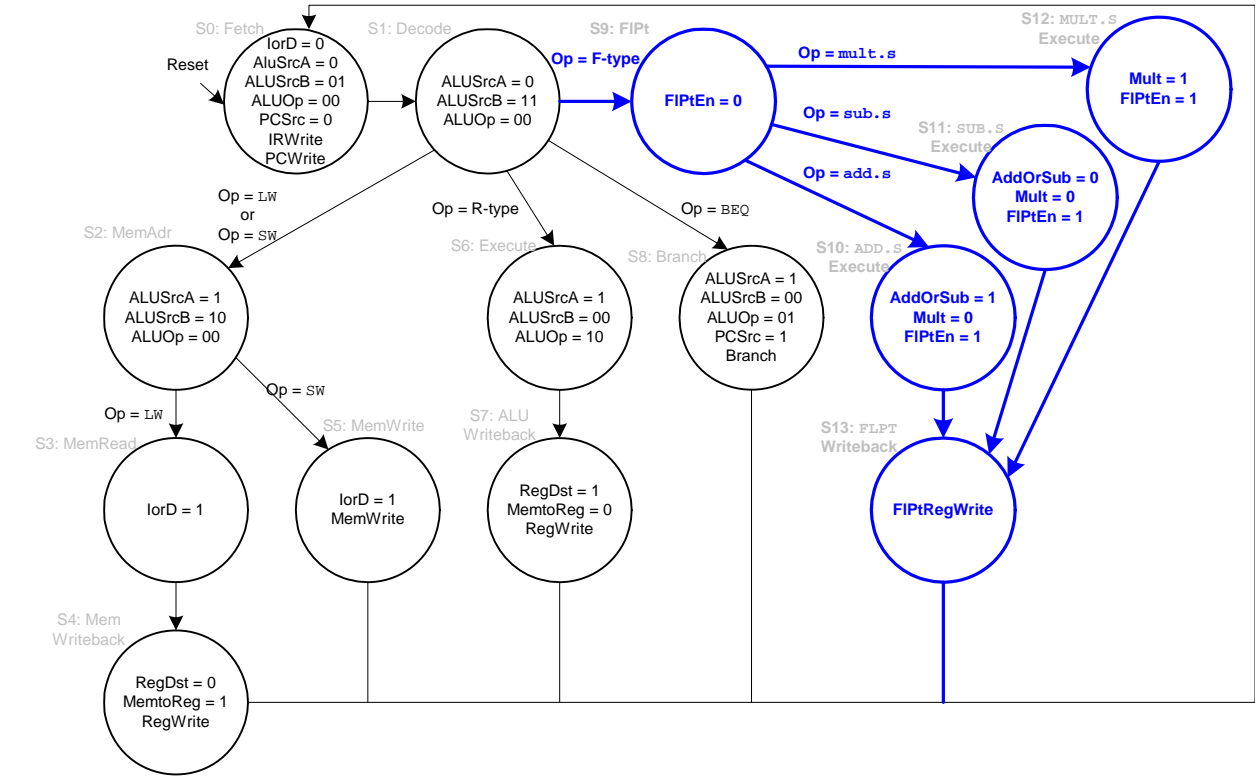
Exercise 7.19

Because the ALU is not on the critical path, the speedup in performance of the ALU does not affect the cycle time. Thus, the cycle time, given in Example 7.8, is still 325 ps. Given the instruction mix in Example 7.7, the overall execution time for 100 billion instructions is still 133.9 seconds.

Exercise 7.21
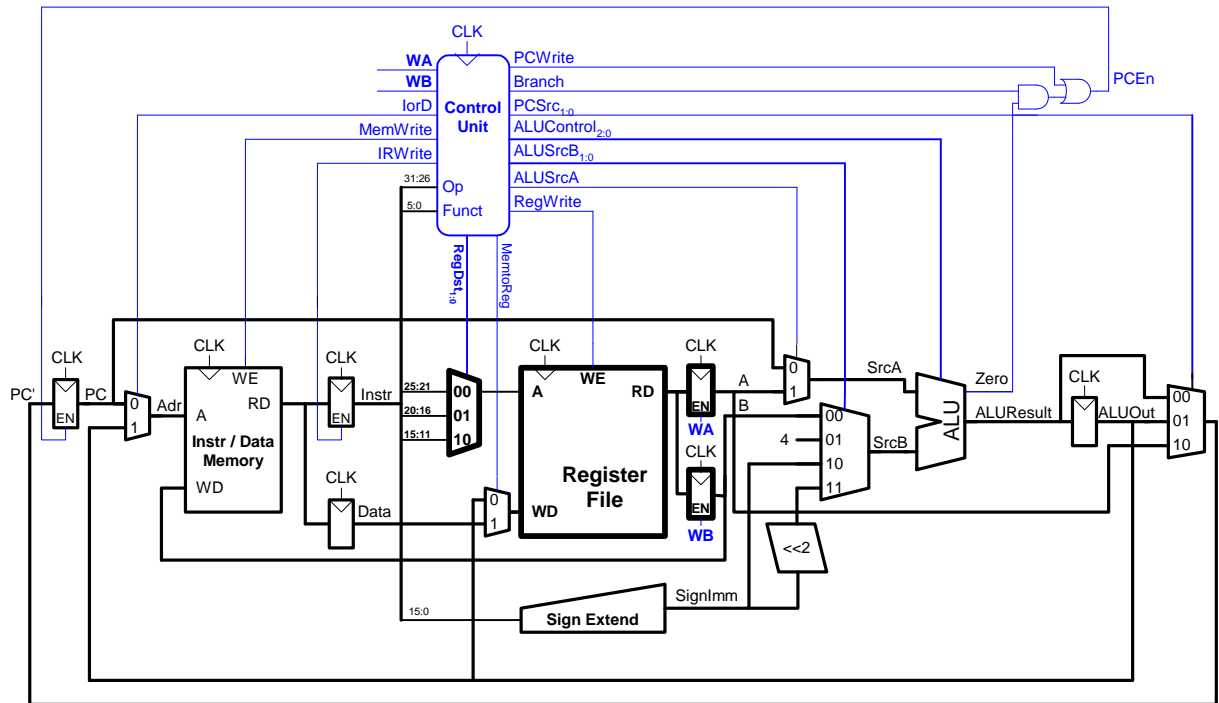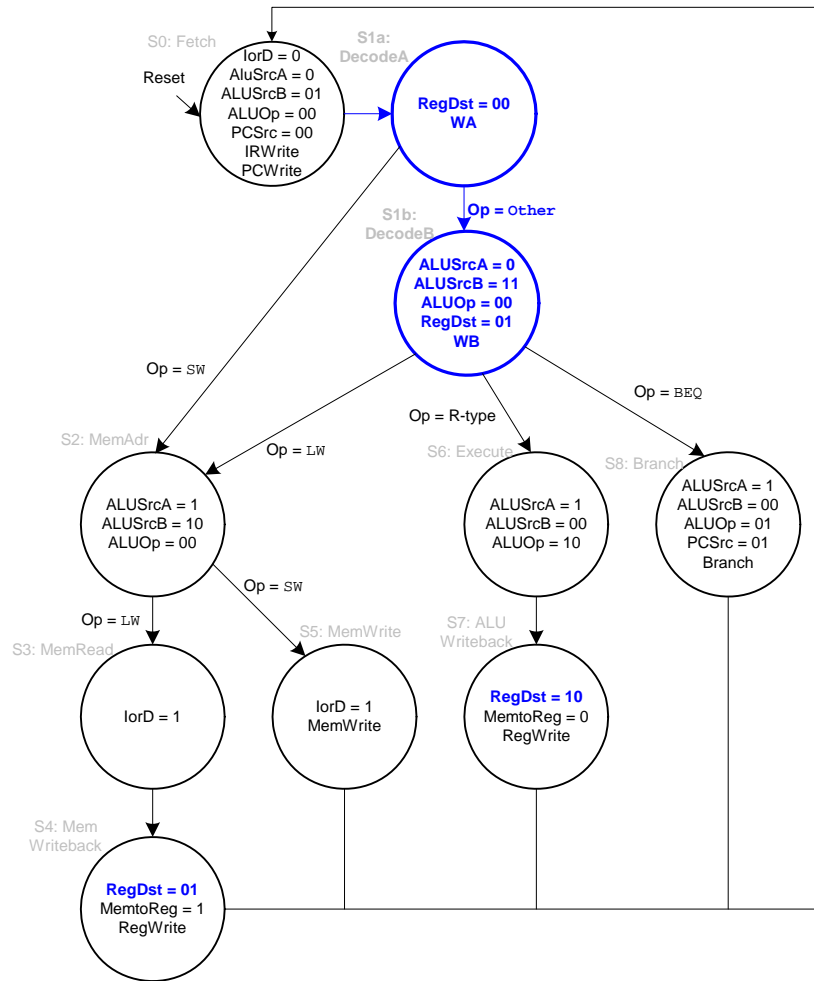
Exercise 7.23

$4 + (3 + 4 + 3) \times 5 + 3 =$ **57 clock cycles**

The number of instructions executed is $1 + (3 \times 5) + 1 = 17$. Thus, the CPI $= 57$ clock cycles / 17 instructions = **3.35 CPI**

Exercise 7.25

MIPS Multicycle Processor

SystemVerilog

```
module mips(input  logic        clk, reset,
            output logic [31:0] adr, writedata,
            output logic        memwrite,
            input  logic [31:0] readdata);

  logic        zero, pcen, irwrite, regwrite,
               alusrca, iord, memtoreg, regdst;
  logic [1:0]  alusrcb, pcsrc;
  logic [2:0]  alucontrol;
  logic [5:0]  op, funct;

  controller c(clk, reset, op, funct, zero,
               pcen, memwrite, irwrite, regwrite,
               alusrca, iord, memtoreg, regdst,
               alusrcb, pcsrc, alucontrol);
  datapath dp(clk, reset,
               pcen, irwrite, regwrite,
               alusrca, iord, memtoreg, regdst,
               alusrcb, pcsrc, alucontrol,
               op, funct, zero,
               adr, writedata, readdata);
endmodule
```

VHDL

```
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity mips is -- multicycle MIPS processor
  port(clk, reset:        in  STD_LOGIC;
       adr:               out STD_LOGIC_VECTOR(31 downto 0);
  writedata:          inout STD_LOGIC_VECTOR(31 downto 0);
       memwrite:          out STD_LOGIC;
  readdata:           in  STD_LOGIC_VECTOR(31 downto 0));
end;

architecture struct of mips is
  component controller
    port(clk, reset:        in  STD_LOGIC;
         op, funct:         in  STD_LOGIC_VECTOR(5 downto 0);
         zero:              in  STD_LOGIC;
         pcen, memwrite:    out STD_LOGIC;
         irwrite, regwrite: out STD_LOGIC;
         alusrca, iord:     out STD_LOGIC;
         memtoreg, regdst:  out STD_LOGIC;
         alusrcb, pcsrc:    out STD_LOGIC_VECTOR(1 downto 0);
         alucontrol:        out STD_LOGIC_VECTOR(2 downto 0));
  end component;
  component datapath
  port(clk, reset:        in  STD_LOGIC;
       pcen, irwrite:     in  STD_LOGIC;
       regwrite, alusrca: in  STD_LOGIC;
       iord, memtoreg:    in  STD_LOGIC;
       regdst:            in  STD_LOGIC;
       alusrcb, pcsrc:    in  STD_LOGIC_VECTOR(1 downto 0);
       alucontrol:        in  STD_LOGIC_VECTOR(2 downto 0);
       readdata:          in  STD_LOGIC_VECTOR(31 downto 0);
       op, funct:         out STD_LOGIC_VECTOR(5 downto 0);
       zero:              out STD_LOGIC;
       adr:               out STD_LOGIC_VECTOR(31 downto 0);
       writedata:         inout STD_LOGIC_VECTOR(31 downto 0));
  end component;
  signal zero, pcen, irwrite, regwrite, alusrca, iord, memtoreg,
         regdst: STD_LOGIC;
  signal alusrcb, pcsrc: STD_LOGIC_VECTOR(1 downto 0);
  signal alucontrol: STD_LOGIC_VECTOR(2 downto 0);
  signal op, funct: STD_LOGIC_VECTOR(5 downto 0);
begin
  c: controller port map(clk, reset, op, funct, zero,
                         pcen, memwrite, irwrite, regwrite,
                         alusrca, iord, memtoreg, regdst,
                         alusrcb, pcsrc, alucontrol);
  dp: datapath port map(clk, reset,
                        pcen, irwrite, regwrite,
                        alusrca, iord, memtoreg, regdst,
                        alusrcb, pcsrc, alucontrol,
                        readdata, op, funct, zero,
                        adr, writedata);
end;
```

MIPS Multicycle Control

SystemVerilog

```systemverilog
module controller(input  logic        clk, reset,
                  input  logic [5:0] op, funct,
                  input  logic        zero,
                  output logic        pcen, memwrite,
                                      irwrite, regwrite,
                  output logic        alusrca, iord,
                                      memtoreg, regdst,
                  output logic [1:0] alusrcb, pcsrc,
                  output logic [2:0] alucontrol);

  logic [1:0] aluop;
  logic       branch, pcwrite;

  // Main Decoder and ALU Decoder subunits.
  maindec md(clk, reset, op,
             pcwrite, memwrite, irwrite, regwrite,
             alusrca, branch, iord, memtoreg, regdst,
             alusrcb, pcsrc, aluop);
  aludec  ad(funct, aluop, alucontrol);

  assign pcen = pcwrite | (branch & zero);

endmodule
```

VHDL

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;
entity controller is -- multicycle control decoder
  port(clk, reset:        in  STD_LOGIC;
       op, funct:         in  STD_LOGIC_VECTOR(5 downto 0);
       zero:              in  STD_LOGIC;
       pcen, memwrite:    out STD_LOGIC;
       irwrite, regwrite: out STD_LOGIC;
       alusrca, iord:     out STD_LOGIC;
       memtoreg, regdst:  out STD_LOGIC;
       alusrcb, pcsrc:    out STD_LOGIC_VECTOR(1 downto 0);
       alucontrol:        out STD_LOGIC_VECTOR(2 downto 0));
end;

architecture struct of controller is
  component maindec
    port(clk, reset:        in  STD_LOGIC;
         op:                in  STD_LOGIC_VECTOR(5 downto 0);
         pcwrite, memwrite: out STD_LOGIC;
         irwrite, regwrite: out STD_LOGIC;
         alusrca, branch:   out STD_LOGIC;
         iord, memtoreg:    out STD_LOGIC;
         regdst:            out STD_LOGIC;
         alusrcb, pcsrc:    out STD_LOGIC_VECTOR(1 downto 0);
         aluop:             out STD_LOGIC_VECTOR(1 downto 0));
  end component;
  component aludec
    port(funct:     in  STD_LOGIC_VECTOR(5 downto 0);
         aluop:     in  STD_LOGIC_VECTOR(1 downto 0);
         alucontrol: out STD_LOGIC_VECTOR(2 downto 0));
  end component;
  signal aluop: STD_LOGIC_VECTOR(1 downto 0);
  signal branch, pcwrite: STD_LOGIC;
begin
  md: maindec port map(clk, reset, op,
                       pcwrite, memwrite, irwrite, regwrite,
                       alusrca, branch, iord, memtoreg, regdst,
                       alusrcb, pcsrc, aluop);
  ad: aludec port map(funct, aluop, alucontrol);

  pcen <= pcwrite or (branch and zero);

end;
```

MIPS Multicycle Main Decoder FSM

SystemVerilog

```systemverilog
module maindec(input  logic       clk, reset,
               input  logic [5:0] op,
               output logic       pcwrite, memwrite,
                                  irwrite, regwrite,
               output logic       alusrca, branch, iord,
                                  memtoreg, regdst,
               output logic [1:0] alusrcb, pcsrc,
               output logic [1:0] aluop);

  typedef enum logic [3:0] {FETCH, DECODE, MEMADR,
                            MEMRD, MEMWB, MEMWR, RTYPEEX,
                            RTYPEWB, BEQEX, ADDIEX,
                            ADDIWB, JEX} statetype;
  statetype [3:0] state, nextstate;

  parameter   LW     = 6'b100011;// Opcode for lw
  parameter   SW     = 6'b101011;// Opcode for sw
  parameter   RTYPE  = 6'b000000;// Opcode for R-type
  parameter   BEQ    = 6'b000100;// Opcode for beq
  parameter   ADDI   = 6'b001000;// Opcode for addi
  parameter   J      = 6'b000010;// Opcode for j

  reg [3:0]  state, nextstate;
  reg [14:0] controls;

  // state register
  always_ff @(posedge clk or posedge reset)
    if (reset) state <= FETCH;
    else state <= nextstate;
```

VHDL

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;
entity maindec is -- main control decoder
  port(clk, reset:        in  STD_LOGIC;
       op:                in  STD_LOGIC_VECTOR(5 downto 0);
       pcwrite, memwrite: out STD_LOGIC;
       irwrite, regwrite: out STD_LOGIC;
       alusrca, branch:   out STD_LOGIC;
       iord, memtoreg:    out STD_LOGIC;
       regdst:            out STD_LOGIC;
    alusrcb, pcsrc:    out STD_LOGIC_VECTOR(1 downto 0);
  aluop:               out STD_LOGIC_VECTOR(1 downto 0));
end;

architecture behave of maindec is
  type statetype is (FETCH, DECODE, MEMADR, MEMRD, MEMWB, MEMWR,
             RTYPEEX, RTYPEWB, BEQEX, ADDIEX, ADDIWB, JEX);
  signal state, nextstate: statetype;
  signal controls: STD_LOGIC_VECTOR(14 downto 0);
begin
  --state register
  process(clk, reset) begin
    if reset then state <= FETCH;
    elsif rising_edge(clk) then
      state <= nextstate;
    end if;
  end process;

  -- next state logic
  process(all) begin
    case state is
      when FETCH =>        nextstate <= DECODE;
      when DECODE =>
          case op is
            when "100011" => nextstate <= MEMADR;
            when "101011" => nextstate <= MEMADR;
            when "000000" => nextstate <= RTYPEEX;
            when "000100" => nextstate <= BEQEX;
            when "001000" => nextstate <= ADDIEX;
            when "000010" => nextstate <= JEX;
            when others   => nextstate <= FETCH; -- should never happen
          end case;
      when MEMADR =>
          case op is
            when "100011" =>  nextstate <= MEMRD;
            when "101011" =>  nextstate <= MEMWR;
            when others   => nextstate <= FETCH; -- should never happen
          end case;
      when MEMRD =>        nextstate <= MEMWB;
      when MEMWB =>        nextstate <= FETCH;
      when MEMWR =>        nextstate <= FETCH;
      when RTYPEEX =>      nextstate <= RTYPEWB;
      when RTYPEWB =>      nextstate <= FETCH;
      when BEQEX =>        nextstate <= FETCH;
      when ADDIEX =>       nextstate <= ADDIWB;
      when JEX =>          nextstate <= FETCH;
      when others =>       nextstate <= FETCH; -- should never happen
    end case;
  end process;
```

SystemVerilog

```systemverilog
    // next state logic
  always_comb
    case(state)
      FETCH:    nextstate <= DECODE;
      DECODE:   case(op)
                  LW:       nextstate <= MEMADR;
                  SW:       nextstate <= MEMADR;
                  RTYPE:    nextstate <= RTYPEEX;
                  BEQ:      nextstate <= BEQEX;
                  ADDI:     nextstate <= ADDIEX;
                  J:        nextstate <= JEX;
                  default: nextstate <= FETCH;
                    // default should never happen
                endcase
      MEMADR:   case(op)
                  LW:       nextstate <= MEMRD;
                  SW:       nextstate <= MEMWR;
                  default: nextstate <= FETCH;
                    // default should never happen
                endcase
      MEMRD:    nextstate <= MEMWB;
      MEMWB:    nextstate <= FETCH;
      MEMWR:    nextstate <= FETCH;
      RTYPEEX: nextstate <= RTYPEWB;
      RTYPEWB: nextstate <= FETCH;
      BEQEX:    nextstate <= FETCH;
      ADDIEX:  nextstate <= ADDIWB;
      ADDIWB:  nextstate <= FETCH;
      JEX:      nextstate <= FETCH;
      default: nextstate <= FETCH;
                    // default should never happen
    endcase

  // output logic
  assign {pcwrite, memwrite, irwrite, regwrite,
          alusrca, branch, iord, memtoreg, regdst,
          alusrcb, pcsrc, aluop} = controls;

    always_comb
    case (state)
      FETCH:    controls <= 15'b1010_00000_0100_00;
      DECODE:   controls <= 15'b0000_00000_1100_00;
      MEMADR:   controls <= 15'b0000_10000_1000_00;
      MEMRD:    controls <= 15'b0000_00100_0000_00;
      MEMWB:    controls <= 15'b0001_00010_0000_00;
      MEMWR:    controls <= 15'b0100_00100_0000_00;
      RTYPEEX: controls <= 15'b0000_10000_0000_10;
      RTYPEWB: controls <= 15'b0001_00001_0000_00;
      BEQEX:    controls <= 15'b0000_11000_0001_01;
      ADDIEX:  controls <= 15'b0000_10000_1000_00;
      ADDIWB:  controls <= 15'b0001_00000_0000_00;
     JEX:      controls <= 15'b1000_00000_0010_00;
      default: controls <= 15'b0000_xxxxx_xxxx_xx;
    endcase
endmodule
```

VHDL

```vhdl
    -- output logic
    process(all) begin
      case state is
        when FETCH   => controls <= "101000000010000";
        when DECODE  => controls <= "000000000110000";
        when MEMADR  => controls <= "000010000100000";
        when MEMRD   => controls <= "000000100000000";
        when MEMWB   => controls <= "000100010000000";
        when MEMWR   => controls <= "010000100000000";
        when RTYPEEX => controls <= "000010000000010";
        when RTYPEWB => controls <= "000100001000000";
        when BEQEX   => controls <= "000011000000101";
        when ADDIEX  => controls <= "000010000100000";
        when ADDIWB  => controls <= "000100000000000";
        when JEX     => controls <= "100000000001000";
        when others  => controls <= "---------------"; --illegal op
      end case;
    end process;

    pcwrite  <= controls(14);
    memwrite <= controls(13);
    irwrite  <= controls(12);
    regwrite <= controls(11);
    alusrca  <= controls(10);
    branch   <= controls(9);
    iord     <= controls(8);
    memtoreg <= controls(7);
    regdst   <= controls(6);
    alusrcb  <= controls(5 downto 4);
    pcsrc    <= controls(3 downto 2);
    aluop    <= controls(1 downto 0);

end;
```

MIPS Multicycle ALU Decoder

SystemVerilog

```systemverilog
module aludec(input  logic [5:0] funct,
              input  logic [1:0] aluop,
              output logic [2:0] alucontrol);

    always_comb
    case(aluop)
      2'b00: alucontrol <= 3'b010;  // add
      2'b01: alucontrol <= 3'b110;  // sub
      default: case(funct)          // RTYPE
          6'b100000: alucontrol <= 3'b010; // ADD
          6'b100010: alucontrol <= 3'b110; // SUB
          6'b100100: alucontrol <= 3'b000; // AND
          6'b100101: alucontrol <= 3'b001; // OR
          6'b101010: alucontrol <= 3'b111; // SLT
          default:   alucontrol <= 3'bxxx; // ???
        endcase
    endcase

endmodule
```

VHDL

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;
entity aludec is -- ALU control decoder
  port(funct:     in  STD_LOGIC_VECTOR(5 downto 0);
       aluop:     in  STD_LOGIC_VECTOR(1 downto 0);
       alucontrol: out STD_LOGIC_VECTOR(2 downto 0));
end;

architecture behave of aludec is
begin
  process(all) begin
    case aluop is
      when "00" => alucontrol <= "010"; -- add (for lb/sb/addi)
      when "01" => alucontrol <= "110"; -- sub (for beq)
      when "11" => alucontrol <= "111"; -- slt (for slti)
      when others => case funct is        -- R-type instructions
                       when "100000" => alucontrol <= "010"; -- add
                       when "100010" => alucontrol <= "110"; -- sub
                       when "100100" => alucontrol <= "000"; -- and
                       when "100101" => alucontrol <= "001"; -- or
                       when "101010" => alucontrol <= "111"; -- slt
                       when others  => alucontrol <= "---"; -- ???
                     end case;
    end case;
  end process;
end;
```

MIPS Multicycle Datapath

SystemVerilog

```systemverilog
module datapath(input logic         clk, reset,
                input logic         pcen, irwrite,
                input logic         regwrite,
                input logic         alusrca, iord,
                                    memtoreg, regdst,
                input  logic [1:0]  alusrcb, pcsrc,
                input  logic [2:0]  alucontrol,
                output logic [5:0]  op, funct,
                output logic        zero,
                output logic [31:0] adr, writedata,
                input  logic [31:0] readdata);

  // Internal signals of the datapath module.

  logic [4:0]  writereg;
  logic [31:0] pcnext, pc;
  logic [31:0] instr, data, srca, srcb;
  logic [31:0] a;
  logic [31:0] aluresult, aluout;
  logic [31:0] signimm;    // sign-extended immediate
  logic [31:0] signimmsh;  // sign-extended immediate
                           // shifted left by 2
  logic [31:0] wd3, rd1, rd2;

  // op and funct fields to controller
  assign op = instr[31:26];
  assign funct = instr[5:0];

  // datapath
  flopenr #(32) pcreg(clk, reset, pcen, pcnext, pc);
  mux2    #(32) adrmux(pc, aluout, iord, adr);
  flopenr #(32) instrreg(clk, reset, irwrite,
                         readdata, instr);
  flopr   #(32) datareg(clk, reset, readdata, data);
  mux2    #(5)  regdstmux(instr[20:16], instr[15:11],
                         regdst, writereg);
  mux2    #(32) wdmux(aluout, data, memtoreg, wd3);
  regfile       rf(clk, regwrite, instr[25:21],
                   instr[20:16],
                   writereg, wd3, rd1, rd2);
  signext       se(instr[15:0], signimm);
  sl2           immsh(signimm, signimmsh);
  flopr   #(32) areg(clk, reset, rd1, a);
  flopr   #(32) breg(clk, reset, rd2, writedata);
  mux2    #(32) srcamux(pc, a, alusrca, srca);
  mux4    #(32) srcbmux(writedata, 32'b100,
                        signimm, signimmsh,
                        alusrcb, srcb);
  alu           alu(srca, srcb, alucontrol,
                    aluresult, zero);
  flopr   #(32) alureg(clk, reset, aluresult, aluout);
  mux3    #(32) pcmux(aluresult, aluout,
                      {pc[31:28], instr[25:0], 2'b00},
                      pcsrc, pcnext);

endmodule
```

VHDL

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all; use IEEE.STD_LOGIC_ARITH.all;
entity datapath is  -- MIPS datapath
  port(clk, reset:       in  STD_LOGIC;
       pcen, irwrite:    in  STD_LOGIC;
       regwrite, alusrca: in STD_LOGIC;
       iord, memtoreg:   in  STD_LOGIC;
       regdst:           in  STD_LOGIC;
       alusrcb, pcsrc:   in  STD_LOGIC_VECTOR(1 downto 0);
       alucontrol:       in  STD_LOGIC_VECTOR(2 downto 0);
       readdata:         in  STD_LOGIC_VECTOR(31 downto 0);
       op, funct:        out STD_LOGIC_VECTOR(5 downto 0);
       zero:             out STD_LOGIC;
       adr:              out STD_LOGIC_VECTOR(31 downto 0);
       writedata:        inout STD_LOGIC_VECTOR(31 downto 0));
end;

architecture struct of datapath is
  component alu
    port(A, B: in    STD_LOGIC_VECTOR(31 downto 0);
         F:    in    STD_LOGIC_VECTOR(2 downto 0);
         Y:    buffer STD_LOGIC_VECTOR(31 downto 0);
         Zero: out   STD_LOGIC);
  end component;
  component regfile
    port(clk:           in  STD_LOGIC;
         we3:           in  STD_LOGIC;
         ra1, ra2, wa3: in  STD_LOGIC_VECTOR(4 downto 0);
         wd3:           in  STD_LOGIC_VECTOR(31 downto 0);
         rd1, rd2:      out STD_LOGIC_VECTOR(31 downto 0));
  end component;
  component adder
    port(a, b: in  STD_LOGIC_VECTOR(31 downto 0);
         y:    out STD_LOGIC_VECTOR(31 downto 0));
  end component;
  component sl2
    port(a: in  STD_LOGIC_VECTOR(31 downto 0);
         y: out STD_LOGIC_VECTOR(31 downto 0));
  end component;
  component signext
    port(a: in  STD_LOGIC_VECTOR(15 downto 0);
         y: out STD_LOGIC_VECTOR(31 downto 0));
  end component;
  component flopr generic(width: integer);
    port(clk, reset: in  STD_LOGIC;
         d:          in  STD_LOGIC_VECTOR(width-1 downto 0);
         q:          out STD_LOGIC_VECTOR(width-1 downto 0));
  end component;
  component flopenr generic(width: integer);
    port(clk, reset: in  STD_LOGIC;
         en:         in  STD_LOGIC;
         d:          in  STD_LOGIC_VECTOR(width-1 downto 0);
         q:          out STD_LOGIC_VECTOR(width-1 downto 0));
  end component;
  component mux2 generic(width: integer);
    port(d0, d1: in  STD_LOGIC_VECTOR(width-1 downto 0);
         s:      in  STD_LOGIC;
         y:      out STD_LOGIC_VECTOR(width-1 downto 0));
  end component;
  component mux3 generic(width: integer);
    port(d0, d1, d2: in  STD_LOGIC_VECTOR(width-1 downto 0);
         s:          in  STD_LOGIC_VECTOR(1 downto 0);
         y:          out STD_LOGIC_VECTOR(width-1 downto 0));
  end component;
  component mux4 generic(width: integer);
    port(d0, d1, d2, d3: in  STD_LOGIC_VECTOR(width-1 downto 0);
         s:              in  STD_LOGIC_VECTOR(1 downto 0);
         y:              out STD_LOGIC_VECTOR(width-1 downto 0));
  end component;
  signal writereg: STD_LOGIC_VECTOR(4 downto 0);
  signal pcnext, pc, instr, data, srca, srcb, a,
         aluresult, aluout, signimm, signimmsh, wd3, rd1, rd2, pcjump:
                STD_LOGIC_VECTOR(31 downto 0);
```

(continued from previous page)

VHDL

```
begin
  -- op and funct fields to controller
  op <= instr(31 downto 26);
  funct <= instr(5 downto 0);

  -- datapath
  pcreg: flopenr generic map(32) port map(clk, reset, pcen, pcnext, pc);
  adrmux: mux2 generic map(32) port map(pc, aluout, iord, adr);
  instrreg: flopenr generic map(32) port map(clk, reset, irwrite,
                                             readdata, instr);
  datareg: flopr generic map(32) port map(clk, reset, readdata, data);
  regdstmux: mux2 generic map(5) port map(instr(20 downto 16),
                                          instr(15 downto 11),
                                          regdst, writereg);
  wdmux: mux2 generic map(32) port map(aluout, data, memtoreg, wd3);
  rf: regfile port map(clk, regwrite, instr(25 downto 21),
                       instr(20 downto 16),
                       writereg, wd3, rd1, rd2);
  se: signext port map(instr(15 downto 0), signimm);
  immsh: sl2 port map(signimm, signimmsh);
  areg: flopr generic map(32) port map(clk, reset, rd1, a);
  breg: flopr generic map(32) port map(clk, reset, rd2, writedata);
  srcamux: mux2 generic map(32) port map(pc, a, alusrca, srca);
  srcbmux: mux4 generic map(32) port map(writedata,
                   "00000000000000000000000000000100",
                   signimm, signimmsh, alusrcb, srcb);
  alu32: alu port map(srca, srcb, alucontrol, aluresult, zero);
  alureg: flopr generic map(32) port map(clk, reset, aluresult, aluout);
  pcjump <= pc(31 downto 28)&instr(25 downto 0)&"00";
  pcmux: mux3 generic map(32) port map(aluresult, aluout,
                                       pcjump, pcsrc, pcnext);
end;
```

The following HDL describes the building blocks that are used in the MIPS
multicycle processor that are not found in Section 7.6.2.

MIPS Multicycle Building Blocks

SystemVerilog

```systemverilog
module flopenr #(parameter WIDTH = 8)
               (input  logic              clk, reset,
                input  logic              en,
                input  logic [WIDTH-1:0] d,
                output logic [WIDTH-1:0] q);

  always_ff @(posedge clk, posedge reset)
    if      (reset) q <= 0;
    else if (en)    q <= d;
endmodule

module mux3 #(parameter WIDTH = 8)
            (input  logic [WIDTH-1:0] d0, d1, d2,
             input  logic [1:0]       s,
             output logic [WIDTH-1:0] y);

  assign #1 y = s[1] ? d2 : (s[0] ? d1 : d0);
endmodule

module mux4 #(parameter WIDTH = 8)
            (input  logic [WIDTH-1:0] d0, d1, d2, d3,
             input  logic [1:0]       s,
             output logic [WIDTH-1:0] y);

  always_comb
    case(s)
      2'b00: y <= d0;
      2'b01: y <= d1;
      2'b10: y <= d2;
      2'b11: y <= d3;
    endcase
endmodule
```

VHDL

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;  use IEEE.STD_LOGIC_ARITH.all;
entity flopenr is -- flip-flop with asynchronous reset
  generic(width: integer);
  port(clk, reset: in  STD_LOGIC;
       en:         in  STD_LOGIC;
       d:          in  STD_LOGIC_VECTOR(width-1 downto 0);
       q:          out STD_LOGIC_VECTOR(width-1 downto 0));
end;

architecture asynchronous of flopenr is
begin
  process(clk, reset) begin
    if reset then q <= CONV_STD_LOGIC_VECTOR(0, width);
    elsif rising_edge(clk) and en = '1' then
      q <= d;
    end if;
  end process;
end;


library IEEE; use IEEE.STD_LOGIC_1164.all;
entity mux3 is -- three-input multiplexer
  generic(width: integer);
  port(d0, d1, d2: in  STD_LOGIC_VECTOR(width-1 downto 0);
       s:          in  STD_LOGIC_VECTOR(1 downto 0);
       y:          out STD_LOGIC_VECTOR(width-1 downto 0));
end;

architecture behave of mux3 is
begin
  process(all) begin
    case s is
      when "00" =>  y <= d0;
      when "01" =>  y <= d1;
      when "10" =>  y <= d2;
      when others => y <= d0;
    end case;
  end process;
end;


library IEEE; use IEEE.STD_LOGIC_1164.all;
entity mux4 is -- four-input multiplexer
  generic(width: integer);
  port(d0, d1, d2, d3: in  STD_LOGIC_VECTOR(width-1 downto 0);
       s:              in  STD_LOGIC_VECTOR(1 downto 0);
       y:              out STD_LOGIC_VECTOR(width-1 downto 0));
end;

architecture behave of mux4 is
begin
  process(all) begin
    case s is
      when "00" =>  y <= d0;
      when "01" =>  y <= d1;
      when "10" =>  y <= d2;
      when "11" =>  y <= d3;
      when others => y <= d0; -- should never happen
    end case;
  end process;
end;
```

Exercise 7.27

We modify the MIPS multicycle processor to implement all instructions
from Exercise 7.14.

SystemVerilog

```
module top(input  logic        clk, reset,
           output logic [31:0] writedata, dataadr,
           output logic        memwrite);

  logic [31:0] pc, instr, readdata;

  // instantiate processor and memories
  mips mips(clk, reset, pc, instr, memwrite, dataadr,
            writedata, readdata);
  imem imem(pc[7:2], instr);
  dmem dmem(clk, memwrite, dataadr, writedata, readdata);
endmodule

module dmem(input  logic        clk, we,
            input  logic [31:0] a, wd,
            output logic [31:0] rd);

  logic [31:0] RAM[63:0];

  assign rd = RAM[a[31:2]]; // word aligned

  always_ff @(posedge clk)
    if (we) RAM[a[31:2]] <= wd;
endmodule

module imem(input  logic [5:0] a,
            output logic [31:0] rd);

  logic [31:0] RAM[63:0];

  initial
      $readmemh("memfile.dat",RAM);

  assign rd = RAM[a]; // word aligned
endmodule


module top(input  logic        clk, reset,
           output logic [31:0] writedata, adr,
           output logic        memwrite);

  logic [31:0] readdata;

  // instantiate processor and memory
  mips mips(clk, reset, adr, writedata, memwrite,
            readdata);
  mem mem(clk, memwrite, adr, writedata,
            readdata);

endmodule


module mips(input  logic        clk, reset,
           output logic [31:0] adr, writedata,
           output logic        memwrite,
           input  logic [31:0] readdata);
```

```
            logic zero, pcen, irwrite, regwrite,
                  alusrca, iord, memtoreg, regdst;
            logic [2:0]  alusrcb;  // ANDI
            logic [1:0]  pcsrc;
            logic [2:0]  alucontrol;
            logic [5:0]  op, funct;
            logic [1:0]  lb;          // LB/LBU

            controller c(clk, reset, op, funct, zero,
                         pcen, memwrite, irwrite, regwrite,
                         alusrca, iord, memtoreg, regdst,
                         alusrcb, pcsrc, alucontrol, lb);  // LB/LBU
            datapath dp(clk, reset,
                         pcen, irwrite, regwrite,
                         alusrca, iord, memtoreg, regdst,
                         alusrcb, pcsrc, alucontrol,
                         lb,                           // LB/LBU
                         op, funct, zero,
                         adr, writedata, readdata);
         endmodule

         module controller(input  logic       clk, reset,
                           input  logic [5:0] op, funct,
                           input  logic       zero,
                           output logic       pcen, memwrite,
                                              irwrite, regwrite,
                           output logic       alusrca, iord,
                           output logic       memtoreg, regdst,
                           output logic [2:0] alusrcb,   // ANDI
                           output logic [1:0] pcsrc,
                           output logic [2:0] alucontrol,
                           output logic [1:0] lb);       // LB/LBU

           logic [1:0] aluop;
           logic       branch, pcwrite;
           logic       bne;  // BNE

           // Main Decoder and ALU Decoder subunits.
           maindec md(clk, reset, op,
                      pcwrite, memwrite, irwrite, regwrite,
                      alusrca, branch, iord, memtoreg, regdst,
                      alusrcb, pcsrc, aluop, bne, lb); //BNE, LBU
           aludec  ad(funct, aluop, alucontrol);

           assign pcen = pcwrite | (branch & zero) |
                           (bne & ~zero);  // BNE

         endmodule

         module maindec(input        clk, reset,
                        input  [5:0] op,
                        output       pcwrite, memwrite,
                                     irwrite, regwrite,
                        output       alusrca, branch,
                                     iord, memtoreg, regdst,
                        output [2:0] alusrcb, // ANDI
                        output [1:0] pcsrc,
                        output [1:0] aluop,
                        output       bne,     // BNE
                        output [1:0] lb);     // LB/LBU

           typedef enum logic [4:0] {FETCH, DECODE, MEMADR,
             MEMRD, MEMWB, MEMWR, RTYPEEX, RTYPEWB, BEQEX,
             ADDIEX, ADDIWB, JEX, ANDIEX, ANDIWB,
             BNEEX, LBURD, LBRD} statetype;
```

```
            statetype [4:0] state, nextstate;

parameter RTYPE = 6'b000000;
parameter LW =    6'b100011;
parameter SW =    6'b101011;
parameter BEQ =   6'b000100;
parameter ADDI =  6'b001000;
parameter J =     6'b000010;
parameter BNE =   6'b000101;
parameter LBU =   6'b100100;
parameter LB =    6'b100000;
parameter ANDI =  6'b001100;

logic [18:0] controls;  // ANDI, BNE, LBU

// state register
always_ff @(posedge clk or posedge reset)
  if(reset) state <= FETCH;
  else state <= nextstate;


// next state logic
always_comb
  case(state)
    FETCH:    nextstate <= DECODE;
    DECODE:   case(op)
                LW:      nextstate <= MEMADR;
                SW:      nextstate <= MEMADR;
                LB:      nextstate <= MEMADR; // LB
                LBU:     nextstate <= MEMADR; // LBU
                RTYPE:   nextstate <= RTYPEEX;
                BEQ:     nextstate <= BEQEX;
                ADDI:    nextstate <= ADDIEX;
                J:       nextstate <= JEX;
                BNE:     nextstate <= BNEEX;  // BNE
                ANDI:    nextstate <= ADDIEX; // ANDI
                default: nextstate <= FETCH;
                      // should never happen
              endcase
    MEMADR:   case(op)
                LW:      nextstate <= MEMRD;
                SW:      nextstate <= MEMWR;
                LBU:     nextstate <= LBURD; // LBU
                LB:      nextstate <= LBRD;  // LB
                default: nextstate <= FETCH;
                      // should never happen
              endcase
    MEMRD:    nextstate <= MEMWB;
    MEMWB:    nextstate <= FETCH;
    MEMWR:    nextstate <= FETCH;
    RTYPEEX:  nextstate <= RTYPEWB;
    RTYPEWB:  nextstate <= FETCH;
    BEQEX:    nextstate <= FETCH;
    ADDIEX:   nextstate <= ADDIWB;
    ADDIWB:   nextstate <= FETCH;
    JEX:      nextstate <= FETCH;
    ANDIEX:   nextstate <= ANDIWB; // ANDI
    ANDIWB:   nextstate <= FETCH;  // ANDI
    BNEEX:    nextstate <= FETCH;  // BNE
    LBURD:    nextstate <= MEMWB;  // LBU
    LBRD:     nextstate <= MEMWB;  // LB
    default: nextstate <= FETCH;
          // should never happen
  endcase

// output logic
```

```
            assign {pcwrite, memwrite, irwrite, regwrite,
                    alusrca, branch, iord, memtoreg, regdst,
                    bne, // BNE
                    alusrcb, pcsrc,
                    aluop,
                    lb} = controls;  // LBU

        always_comb
          case(state)
            FETCH:   controls <= 19'b1010_00000_0_00100_00_00;
            DECODE:  controls <= 19'b0000_00000_0_01100_00_00;
            MEMADR:  controls <= 19'b0000_10000_0_01000_00_00;
            MEMRD:   controls <= 19'b0000_00100_0_00000_00_00;
            MEMWB:   controls <= 19'b0001_00010_0_00000_00_00;
            MEMWR:   controls <= 19'b0100_00100_0_00000_00_00;
            RTYPEEX: controls <= 19'b0000_10000_0_00000_10_00;
            RTYPEWB: controls <= 19'b0001_00001_0_00000_00_00;
            BEQEX:   controls <= 19'b0000_11000_0_00001_01_00;
            ADDIEX:  controls <= 19'b0000_10000_0_01000_00_00;
            ADDIWB:  controls <= 19'b0001_00000_0_00000_00_00;
            JEX:     controls <= 19'b1000_00000_0_00010_00_00;
            ANDIEX:  controls <= 19'b0000_10000_0_10000_11_00; // ANDI
            ANDIWB:  controls <= 19'b0001_00000_0_00000_00_00; // ANDI
            BNEEX:   controls <= 19'b0000_10000_1_00001_01_00; // BNE
            LBURD:   controls <= 19'b0000_00100_0_00000_00_01; // LBU
            LBRD:    controls <= 19'b0000_00100_0_00000_00_10; // LB
            default: controls <= 19'b0000_xxxxx_x_xxxxx_xx_xx;
                              // should never happen
          endcase
      endmodule

      module aludec(input  logic [5:0] funct,
                    input  logic [1:0] aluop,
                    output logic [2:0] alucontrol);

        always_comb
        case(aluop)
          2'b00: alucontrol <= 3'b010;  // add
          2'b01: alucontrol <= 3'b110;  // sub
          2'b11: alucontrol <= 3'b000;  // and
          2'b10: case(funct)            // RTYPE
              6'b100000: alucontrol <= 3'b010; // ADD
              6'b100010: alucontrol <= 3'b110; // SUB
              6'b100100: alucontrol <= 3'b000; // AND
              6'b100101: alucontrol <= 3'b001; // OR
              6'b101010: alucontrol <= 3'b111; // SLT
              default:   alucontrol <= 3'bxxx; // ???
            endcase
          default: alucontrol <= 3'bxxx;       // ???
        endcase
      endmodule


      module datapath(input  logic        clk, reset,
                      input  logic        pcen, irwrite,
                      input  logic        regwrite,
                      input  logic        alusrca, iord,
                                          memtoreg, regdst,
                      input  logic [2:0]  alusrcb, // ANDI
                      input  logic [1:0]  pcsrc,
                      input  logic [2:0]  alucontrol,
                      input  logic [1:0]  lb,        // LB/LBU
                      output logic [5:0]  op, funct,
                      output logic        zero,
                      output logic [31:0] adr, writedata,
                      input  logic [31:0] readdata);
```

```
    // Internal signals of the datapath module

    logic [4:0]  writereg;
    logic [31:0] pcnext, pc;
    logic [31:0] instr, data, srca, srcb;
    logic [31:0] a;
    logic [31:0] aluresult, aluout;
    logic [31:0] signimm;   // the sign-extended imm
    logic [31:0] zeroimm;   // the zero-extended imm
                            // ANDI
    logic [31:0] signimmsh; // the sign-extended imm << 2
    logic [31:0] wd3, rd1, rd2;
    logic [31:0] memdata, membytezext, membytesext; // LB / LBU
    logic [7:0]  membyte; // LB / LBU

    // op and funct fields to controller
    assign op = instr[31:26];
    assign funct = instr[5:0];

    // datapath
    flopenr #(32) pcreg(clk, reset, pcen, pcnext, pc);
    mux2    #(32) adrmux(pc, aluout, iord, adr);
    flopenr #(32) instrreg(clk, reset, irwrite,
                           readdata, instr);

    // changes for LB / LBU
    flopr   #(32) datareg(clk, reset, memdata, data);
    mux4    #(8)  lbmux(readdata[31:24],
                       readdata[23:16], readdata[15:8],
                       readdata[7:0], aluout[1:0],
                       membyte);
    zeroext8_32   lbze(membyte, membytezext);
    signext8_32   lbse(membyte, membytesext);
    mux3    #(32) datamux(readdata, membytezext, membytesext,
                         lb, memdata);


    mux2    #(5)  regdstmux(instr[20:16],
                           instr[15:11], regdst, writereg);
    mux2    #(32) wdmux(aluout, data, memtoreg, wd3);
    regfile       rf(clk, regwrite, instr[25:21],
                    instr[20:16],
                    writereg, wd3, rd1, rd2);
    signext       se(instr[15:0], signimm);
    zeroext       ze(instr[15:0], zeroimm);   // ANDI
    sl2           immsh(signimm, signimmsh);
    flopr   #(32) areg(clk, reset, rd1, a);
    flopr   #(32) breg(clk, reset, rd2, writedata);
    mux2    #(32) srcamux(pc, a, alusrca, srca);
    mux5    #(32) srcbmux(writedata, 32'b100,
                         signimm, signimmsh,
                         zeroimm,  // ANDI
                         alusrcb, srcb);

    alu           alu(srca, srcb, alucontrol,aluresult, zero);
    flopr   #(32) alureg(clk, reset, aluresult, aluout);
    mux3    #(32) pcmux(aluresult, aluout,
                       {pc[31:28], instr[25:0], 2'b00},
                       pcsrc, pcnext);

endmodule

module alu(input  logic [31:0] A, B,
           input  logic [2:0]  F,
           output logic [31:0] Y, output Zero);
```

```
    logic [31:0] S, Bout;

    assign Bout = F[2] ? ~B : B;
    assign S = A + Bout + F[2];

    always_comb
      case (F[1:0])
        3'b00: Y <= A & Bout;
        3'b01: Y <= A | Bout;
        3'b10: Y <= S;
        3'b11: Y <= S[31];
      endcase

    assign Zero = (Y == 32'b0);
endmodule


// mux5 is needed for ANDI
module mux5 #(parameter WIDTH = 8)
             (input      [WIDTH-1:0] d0, d1, d2, d3, d4,
              input      [2:0]       s,
              output reg [WIDTH-1:0] y);

    always_comb
      case(s)
        3'b000: y <= d0;
        3'b001: y <= d1;
        3'b010: y <= d2;
        3'b011: y <= d3;
        3'b100: y <= d4;
      endcase
endmodule

// zeroext is needed for ANDI
module zeroext(input  [15:0] a,
               output [31:0] y);

  assign y = {16'b0, a};
endmodule

// zeroext8_32 is needed for LBU
module zeroext8_32(input  logic [7:0] a,
                   output logic [31:0] y);

  assign y = {24'b0, a};
endmodule

// signext8_32 is needed for LB
module signext8_32(input  logic [7:0] a,
                   output logic [31:0] y);

  assign y = {{24{a[7]}}, a};
endmodule

module alu(input  logic [31:0] A, B,
           input  logic [3:0]  F,
           input  logic [4:0]  shamt, // SRL
           output logic [31:0] Y,
           output logic        Zero);

  logic [31:0] S, Bout;

  assign Bout = F[3] ? ~B : B;
  assign S = A + Bout + F[3];  // SRL
```

```
  always_comb
    case (F[2:0])
      3'b000: Y = A & Bout;
      3'b001: Y = A | Bout;
      3'b010: Y = S;
      3'b011: Y = S[31];
      3'b100: Y = (Bout >> shamt);  // SRL
    endcase

  assign Zero = (Y == 32'b0);

endmodule

module regfile(input  logic        clk,
               input  logic        we3,
               input  logic [4:0]  ra1, ra2, wa3,
               input  logic [31:0] wd3,
               output logic [31:0] rd1, rd2);

  logic [31:0] rf[31:0];

  // three ported register file
  // read two ports combinationally
  // write third port on rising edge of clk
  // register 0 hardwired to 0
  always_ff @(posedge clk)
    if (we3) rf[wa3] <= wd3;

  assign rd1 = (ra1 != 0) ? rf[ra1] : 0;
  assign rd2 = (ra2 != 0) ? rf[ra2] : 0;
endmodule

module adder(input  logic [31:0] a, b,
             output logic [31:0] y);

  assign y = a + b;
endmodule

module sl2(input  logic [31:0] a,
           output logic [31:0] y);

  // shift left by 2
  assign y = {a[29:0], 2'b00};
endmodule

module signext(input  logic [15:0] a,
               output logic [31:0] y);

  assign y = {{16{a[15]}}, a};
endmodule

module flopr #(parameter WIDTH = 8)
             (input  logic            clk, reset,
              input  logic [WIDTH-1:0] d,
              output logic [WIDTH-1:0] q);

  always_ff @(posedge clk, posedge reset)
    if (reset) q <= 0;
    else       q <= d;
endmodule

module mux2 #(parameter WIDTH = 8)
            (input  logic [WIDTH-1:0] d0, d1,
             input  logic            s,
             output logic [WIDTH-1:0] y);
```

```
    assign y = s ? d1 : d0;
endmodule
```

VHDL

```
library IEEE; use IEEE.STD_LOGIC_1164.all;

entity mips is -- multicycle MIPS processor
  port(clk, reset:         in  STD_LOGIC;
       adr:                out STD_LOGIC_VECTOR(31 downto 0);
  writedata:          inout STD_LOGIC_VECTOR(31 downto 0);
       memwrite:           out STD_LOGIC;
  readdata:           in  STD_LOGIC_VECTOR(31 downto 0));
end;

architecture struct of mips is
  component controller
    port(clk, reset:        in  STD_LOGIC;
         op, funct:         in  STD_LOGIC_VECTOR(5 downto 0);
         zero:              in  STD_LOGIC;
         pcen, memwrite:    out STD_LOGIC;
         irwrite, regwrite: out STD_LOGIC;
         alusrca, iord:     out STD_LOGIC;
         memtoreg, regdst:  out STD_LOGIC;
         alusrcb:           out STD_LOGIC_VECTOR(2 downto 0); --andi
         pcsrc:             out STD_LOGIC_VECTOR(1 downto 0);
         alucontrol:        out STD_LOGIC_VECTOR(2 downto 0);
         lb:                out STD_LOGIC_VECTOR(1 downto 0));--lb, lbu
  end component;
  component datapath
    port(clk, reset:      in  STD_LOGIC;
         pcen, irwrite:    in  STD_LOGIC;
         regwrite, alusrca: in  STD_LOGIC;
         iord, memtoreg:   in  STD_LOGIC;
         regdst:           in  STD_LOGIC;
         alusrcb:          in  STD_LOGIC_VECTOR(2 downto 0); --andi
         pcsrc:            in  STD_LOGIC_VECTOR(1 downto 0);
         alucontrol:       in  STD_LOGIC_VECTOR(2 downto 0);
         lb:               in  STD_LOGIC_VECTOR(1 downto 0); --lb / lbu
         readdata:         in  STD_LOGIC_VECTOR(31 downto 0);
         op, funct:        out STD_LOGIC_VECTOR(5 downto 0);
         zero:             out STD_LOGIC;
         adr:              out STD_LOGIC_VECTOR(31 downto 0);
         writedata:        inout STD_LOGIC_VECTOR(31 downto 0));
  end component;
  signal zero, pcen, irwrite, regwrite, alusrca, iord, memtoreg,
         regdst:      STD_LOGIC;
  signal alusrcb:     STD_LOGIC_VECTOR(2 downto 0);  --andi
  signal pcsrc:       STD_LOGIC_VECTOR(1 downto 0);
  signal alucontrol: STD_LOGIC_VECTOR(2 downto 0);
  signal op, funct:  STD_LOGIC_VECTOR(5 downto 0);
  signal lb:          STD_LOGIC_VECTOR(1 downto 0);  --lb / lbu
begin
  c: controller port map(clk, reset, op, funct, zero,
                         pcen, memwrite, irwrite, regwrite,
                         alusrca, iord, memtoreg, regdst,
                         alusrcb, pcsrc, alucontrol, lb);  --lb /lbu
  dp: datapath port map(clk, reset,
                        pcen, irwrite, regwrite,
                        alusrca, iord, memtoreg, regdst,
                        alusrcb, pcsrc, alucontrol,
                   lb,                     --lb / lbu
                        readdata, op, funct, zero,
                        adr, writedata, readdata);
end;
```

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;
entity controller is -- multicycle control decoder
  port(clk, reset:        in  STD_LOGIC;
       op, funct:         in  STD_LOGIC_VECTOR(5 downto 0);
       zero:              in  STD_LOGIC;
       pcen, memwrite:    out STD_LOGIC;
       irwrite, regwrite: out STD_LOGIC;
       alusrca, iord:     out STD_LOGIC;
       memtoreg, regdst:  out STD_LOGIC;
       alusrcb:           out STD_LOGIC_VECTOR(2 downto 0); --andi
       pcsrc:             out STD_LOGIC_VECTOR(1 downto 0);
       alucontrol:        out STD_LOGIC_VECTOR(2 downto 0);
       lb:                out STD_LOGIC_VECTOR(1 downto 0));--lb, lbu
end;
architecture struct of controller is
  component maindec
    port(clk, reset:        in  STD_LOGIC;
         op:                in  STD_LOGIC_VECTOR(5 downto 0);
         pcwrite, memwrite: out STD_LOGIC;
         irwrite, regwrite: out STD_LOGIC;
         alusrca, branch:   out STD_LOGIC;
         iord, memtoreg:    out STD_LOGIC;
         regdst:            out STD_LOGIC;
    alusrcb:            out STD_LOGIC_VECTOR(2 downto 0); --andi
    pcsrc:              out STD_LOGIC_VECTOR(1 downto 0);
    aluop:              out STD_LOGIC_VECTOR(1 downto 0);
         lb:                out STD_LOGIC_VECTOR(1 downto 0));  --lb / lbu
  end component;
  component aludec
    port(funct:     in  STD_LOGIC_VECTOR(5 downto 0);
         aluop:     in  STD_LOGIC_VECTOR(1 downto 0);
         alucontrol: out STD_LOGIC_VECTOR(2 downto 0));
  end component;
  signal aluop: STD_LOGIC_VECTOR(1 downto 0);
  signal branch, pcwrite, bne: STD_LOGIC;  --bne
begin
  md: maindec port map(clk, reset, op,
                       pcwrite, memwrite, irwrite, regwrite,
                       alusrca, branch, iord, memtoreg, regdst,
                       alusrcb, pcsrc, aluop, bne, lb);  --bne, lb
  ad: aludec port map(funct, aluop, alucontrol);

  pcen <= pcwrite or (branch and zero) or (bne and (not zero));  --bne
end;


library IEEE; use IEEE.STD_LOGIC_1164.all;
entity maindec is -- main control decoder
  port(clk, reset:        in  STD_LOGIC;
       op:                in  STD_LOGIC_VECTOR(5 downto 0);
       pcwrite, memwrite: out STD_LOGIC;
       irwrite, regwrite: out STD_LOGIC;
       alusrca, branch:   out STD_LOGIC;
       iord, memtoreg:    out STD_LOGIC;
       regdst:            out STD_LOGIC;
 alusrcb:           out STD_LOGIC_VECTOR(2 downto 0); --andi
 pcsrc:             out STD_LOGIC_VECTOR(1 downto 0);
 aluop:             out STD_LOGIC_VECTOR(1 downto 0);
 bne:               out STD_LOGIC;                        --bne
 aluop:             out STD_LOGIC_VECTOR(1 downto 0));--lb / lbu
end;

architecture behave of maindec is
  type statetype is (FETCH, DECODE, MEMADR, MEMRD, MEMWB, MEMWR,
                     RTYPEEX, RTYPEWB, BEQEX, ADDIEX, ADDIWB, JEX,
```

```
                            ANDIEX, ANDIWB,BNEEX, LBURD, LBRD);
    signal state, nextstate: statetype;
    signal controls: STD_LOGIC_VECTOR(18 downto 0);
begin
  --state register
  process(clk, reset) begin
    if reset then state <= FETCH;
    elsif rising_edge(clk) then
      state <= nextstate;
    end if;
  end process;

  -- next state logic
  process(all) begin
    case state is
      when FETCH  =>           nextstate <= DECODE;
      when DECODE =>
          case op is
            when "100011" =>  nextstate <= MEMADR; --LW
            when "101011" =>  nextstate <= MEMADR; --SW
            when "100000" =>  nextstate <= MEMADR; --LB
            when "100100" =>  nextstate <= MEMADR; --LBU
            when "000000" =>  nextstate <= RTYPEEX;--RTYPE
            when "000100" =>  nextstate <= BEQEX;  --BEQ
            when "001000" =>  nextstate <= ADDIEX; --ADDI
            when "000010" =>  nextstate <= JEX;    --J
            when "000101" =>  nextstate <= ORIEX;  --BNE
            when "001100" =>  nextstate <= ORIEX;  --ANDI
            when others    => nextstate <= FETCH;  -- should never happen
          end case;
      when MEMADR =>
          case op is
            when "100011" =>  nextstate <= MEMRD;
            when "101011" =>  nextstate <= MEMWR;
            when "100000" =>  nextstate <= LBRD;  --LB
            when "100100" =>  nextstate <= LBURD; --LBU
            when others   =>  nextstate <= FETCH; -- should never happen
          end case;
      when MEMRD =>            nextstate <= MEMWB;
      when MEMWB =>            nextstate <= FETCH;
      when MEMWR =>            nextstate <= FETCH;
      when RTYPEEX =>          nextstate <= RTYPEWB;
      when RTYPEWB =>          nextstate <= FETCH;
      when BEQEX =>            nextstate <= FETCH;
      when ADDIEX =>           nextstate <= ADDIWB;
      when JEX =>              nextstate <= FETCH;
      when ANDIEX =>           nextstate <= ANDIWB; // ANDI
      when ANDIWB =>           nextstate <= FETCH;  // ANDI
      when BNEEX  =>           nextstate <= FETCH;  // BNE
      when LBURD  =>           nextstate <= MEMWB;  // LBU
      when LBRD   =>           nextstate <= MEMWB;  // LB
      when others =>           nextstate <= FETCH; -- should never happen
    end case;
  end process;

  -- output logic
  process(all) begin
    case state is
      when FETCH   => controls <= "1010_00000_0_00100_00_00";
      when DECODE  => controls <= "0000_00000_0_01100_00_00";
      when MEMADR  => controls <= "0000_10000_0_01100_00_00";
      when MEMRD   => controls <= "0000_00100_0_00000_00_00";
      when MEMWB   => controls <= "0001_00010_0_00000_00_00";
      when MEMWR   => controls <= "0100_00100_0_00000_00_00";
      when RTYPEEX => controls <= "0000_10000_0_00000_10_00";
      when RTYPEWB => controls <= "0001_00001_0_00000_00_00";
```

```
      when BEQEX   => controls <= "0000_11000_0_00001_01_00";
      when ADDIEX  => controls <= "0000_10000_0_01000_00_00";
      when ADDIWB  => controls <= "0001_00000_0_00000_00_00";
      when JEX     => controls <= "1000_00000_0_00010_00_00";
      when ANDIEX  => controls <= "0000_10000_0_10000_11_00";
      when ANDIWB  => controls <= "0001_00000_0_00000_00_00";
      when BNEEX   => controls <= "0000_10000_1_00001_01_00";
      when LBURD   => controls <= "0000_00100_0_00000_00_01";
      when LBRD    => controls <= "0000_00100_0_00000_00_10";
      when others  => controls <= "0000_-----_-_-----_--_--";
                                                      --illegal op
    end case;
  end process;

  pcwrite  <= controls(18);
  memwrite <= controls(17);
  irwrite  <= controls(16);
  regwrite <= controls(15);
  alusrca  <= controls(14);
  branch   <= controls(13);
  iord     <= controls(12);
  memtoreg <= controls(11);
  regdst   <= controls(10);
  bne      <= controls(9);
  alusrcb  <= controls(8 downto 6);
  pcsrc    <= controls(5 downto 4);
  aluop    <= controls(3 downto 1);
  lb       <= controls(0);

end;


library IEEE; use IEEE.STD_LOGIC_1164.all;
entity aludec is -- ALU control decoder
  port(funct:     in  STD_LOGIC_VECTOR(5 downto 0);
       aluop:     in  STD_LOGIC_VECTOR(1 downto 0);
       alucontrol: out STD_LOGIC_VECTOR(2 downto 0));
end;

architecture behave of aludec is
begin
  process(all) begin
    case aluop is
      when "00" => alucontrol <= "010"; -- add (for lb/sb/addi)
      when "01" => alucontrol <= "110"; -- sub (for beq)
      when "11" => alucontrol <= "000"; -- and (for andi)
      when others => case funct is          -- R-type instructions
                       when "100000" => alucontrol <= "010"; -- add
                       when "100010" => alucontrol <= "110"; -- sub
                       when "100100" => alucontrol <= "000"; -- and
                       when "100101" => alucontrol <= "001"; -- or
                       when "101010" => alucontrol <= "111"; -- slt
                       when others   => alucontrol <= "---"; -- ???
                     end case;
    end case;
  end process;
end;


library IEEE; use IEEE.STD_LOGIC_1164.all; use IEEE.STD_LOGIC_ARITH.all;
entity datapath is  -- MIPS datapath
  port(clk, reset:      in  STD_LOGIC;
       pcen, irwrite:   in  STD_LOGIC;
       regwrite, alusrca: in  STD_LOGIC;
       iord, memtoreg:  in  STD_LOGIC;
       regdst:          in  STD_LOGIC;
```

```
        alusrcb:            in  STD_LOGIC_VECTOR(2 downto 0); --andi
        pcsrc:             in  STD_LOGIC_VECTOR(1 downto 0);
        alucontrol:        in  STD_LOGIC_VECTOR(2 downto 0);
        lb:                in  STD_LOGIC_VECTOR(1 downto 0); --lb / lbu
        readdata:          in  STD_LOGIC_VECTOR(31 downto 0);
        op, funct:         out STD_LOGIC_VECTOR(5 downto 0);
        zero:              out STD_LOGIC;
        adr:               out STD_LOGIC_VECTOR(31 downto 0);
        writedata:         inout STD_LOGIC_VECTOR(31 downto 0));
end;

architecture struct of datapath is
  component alu
    port(A, B:    in  STD_LOGIC_VECTOR(31 downto 0);
         F:       in  STD_LOGIC_VECTOR(2 downto 0);
         Y:       out STD_LOGIC_VECTOR(31 downto 0);
         Zero:    out STD_LOGIC);
  end component;
  component regfile
    port(clk:             in  STD_LOGIC;
         we3:             in  STD_LOGIC;
         ra1, ra2, wa3: in  STD_LOGIC_VECTOR(4 downto 0);
         wd3:             in  STD_LOGIC_VECTOR(31 downto 0);
         rd1, rd2:        out STD_LOGIC_VECTOR(31 downto 0));
  end component;
  component adder
    port(a, b: in  STD_LOGIC_VECTOR(31 downto 0);
         y:     out STD_LOGIC_VECTOR(31 downto 0));
  end component;
  component sl2
    port(a: in  STD_LOGIC_VECTOR(31 downto 0);
         y: out STD_LOGIC_VECTOR(31 downto 0));
  end component;
  component signext
    port(a: in  STD_LOGIC_VECTOR(15 downto 0);
         y: out STD_LOGIC_VECTOR(31 downto 0));
  end component;
  component zeroext
    port(a: in  STD_LOGIC_VECTOR(15 downto 0);
         y: out STD_LOGIC_VECTOR(31 downto 0));
  end component;
  component flopr generic(width: integer);
    port(clk, reset: in  STD_LOGIC;
         d:              in  STD_LOGIC_VECTOR(width-1 downto 0);
         q:              out STD_LOGIC_VECTOR(width-1 downto 0));
  end component;
  component flopenr generic(width: integer);
    port(clk, reset: in  STD_LOGIC;
         en:             in  STD_LOGIC;
         d:              in  STD_LOGIC_VECTOR(width-1 downto 0);
         q:              out STD_LOGIC_VECTOR(width-1 downto 0));
  end component;
  component mux2 generic(width: integer);
    port(d0, d1: in  STD_LOGIC_VECTOR(width-1 downto 0);
         s:       in  STD_LOGIC;
         y:       out STD_LOGIC_VECTOR(width-1 downto 0));
  end component;
  component mux3 generic(width: integer);
    port(d0, d1, d2: in  STD_LOGIC_VECTOR(width-1 downto 0);
         s:              in  STD_LOGIC_VECTOR(1 downto 0);
         y:              out STD_LOGIC_VECTOR(width-1 downto 0));
  end component;
  component mux4 generic(width: integer);
    port(d0, d1, d2, d3: in  STD_LOGIC_VECTOR(width-1 downto 0);
         s:                 in  STD_LOGIC_VECTOR(1 downto 0);
         y:                 out STD_LOGIC_VECTOR(width-1 downto 0));
```

```
    end component;
    component mux5 generic(width: integer);
      port(d0, d1, d2, d3, d4: in  STD_LOGIC_VECTOR(width-1 downto 0);
           s:                  in  STD_LOGIC_VECTOR(2 downto 0);
           y:                  out STD_LOGIC_VECTOR(width-1 downto 0));
    end component;
    -- lb / lbu
    component zeroext8_32
      port(a: in  STD_LOGIC_VECTOR(7 downto 0);
           y: out STD_LOGIC_VECTOR(31 downto 0));
    end component;
    component signext8_32
      port(a: in  STD_LOGIC_VECTOR(7 downto 0);
           y: out STD_LOGIC_VECTOR(31 downto 0));
    end component;

    signal writereg: STD_LOGIC_VECTOR(4 downto 0);
    signal pcnext, pc, instr, data, srca, srcb, a,
           aluresult, aluout, signimm, signimmsh, wd3, rd1, rd2, pcjump:
                    STD_LOGIC_VECTOR(31 downto 0);
    -- lb / lbu
    signal memdata, membytezext, membytesext: STD_LOGIC_VECTOR(31 downto 0);
    signal membyte: STD_LOGIC_VECTOR(7 downto 0);


begin
  -- op and funct fields to controller
  op <= instr(31 downto 26);
  funct <= instr(5 downto 0);

  -- datapath
  pcreg: flopenr generic map(32) port map(clk, reset, pcen, pcnext, pc);
  adrmux: mux2 generic map(32) port map(pc, aluout, iord, adr);
  instrreg: flopenr generic map(32) port map(clk, reset, irwrite,
                                                 readdata, instr);
  -- changes for lb / lbu
  datareg: flopr generic map(32) port map(clk, reset, memdata, data);
  lbmux:   mux4 generic map(8) port map(readdata(31 downto 24),
                                        readdata(23 downto 16),
                                        readdata(15 downto 8),
                                        readdata(7 downto 0),
                                        aluout(1 downto 0), membyte);
  lbze: zeroext8_32 port map(membyte, membytezext);
  lbse: signext8_32 port map(membyte, membytesext);
  datamux: mux3 generic map(32) port map(readdata, membytezext, membytesext,
                                         lb, memdata);

  datareg: flopr generic map(32) port map(clk, reset, readdata, data);
  regdstmux: mux2 generic map(5) port map(instr(20 downto 16),
                                          instr(15 downto 11),
                                          regdst, writereg);
  wdmux: mux2 generic map(32) port map(aluout, data, memtoreg, wd3);
  rf: regfile port map(clk, regwrite, instr(25 downto 21),
                       instr(20 downto 16),
                       writereg, wd3, rd1, rd2);
  se: signext port map(instr(15 downto 0), signimm);
  ze: zeroext port map(instr(15 downto 0), zeroimm);  --andi
  immsh: sl2 port map(signimm, signimmsh);
  areg: flopr generic map(32) port map(clk, reset, rd1, a);
  breg: flopr generic map(32) port map(clk, reset, rd2, writedata);
  srcamux: mux2 generic map(32) port map(pc, a, alusrca, srca);
  srcbmux: mux5 generic map(32) port map(writedata,
                 "00000000000000000000000000000100",
                 signimm, signimmsh, zeroimm, alusrcb, srcb); --andi
  alu32: alu port map(srca, srcb, alucontrol, aluresult, zero);
  alureg: flopr generic map(32) port map(clk, reset, aluresult, aluout);
```

```
                        pcjump <= pc(31 downto 28)&instr(25 downto 0)&"00";
                        pcmux: mux3 generic map(32) port map(aluresult, aluout,
                                                             pcjump, pcsrc, pcnext);
                      end;


                      library IEEE; use IEEE.STD_LOGIC_1164.all;  use IEEE.STD_LOGIC_ARITH.all;
                      entity flopenr is -- flip-flop with asynchronous reset
                        generic(width: integer);
                        port(clk, reset: in  STD_LOGIC;
                             en:          in  STD_LOGIC;
                             d:           in  STD_LOGIC_VECTOR(width-1 downto 0);
                             q:           out STD_LOGIC_VECTOR(width-1 downto 0));
                      end;

                      architecture asynchronous of flopenr is
                      begin
                        process(clk, reset) begin
                          if reset then  q <= CONV_STD_LOGIC_VECTOR(0, width);
                          elsif rising_edge(clk) and en = '1' then
                            q <= d;
                          end if;
                        end process;
                      end;


                      library IEEE; use IEEE.STD_LOGIC_1164.all;
                      entity mux3 is -- three-input multiplexer
                        generic(width: integer);
                        port(d0, d1, d2: in  STD_LOGIC_VECTOR(width-1 downto 0);
                             s:          in  STD_LOGIC_VECTOR(1 downto 0);
                             y:          out STD_LOGIC_VECTOR(width-1 downto 0));
                      end;

                      architecture behave of mux3 is
                      begin
                        process(all) begin
                          case s is
                            when "00" =>  y <= d0;
                            when "01" =>  y <= d1;
                            when "10" =>  y <= d2;
                            when others => y <= d0;
                          end case;
                        end process;
                      end;


                      library IEEE; use IEEE.STD_LOGIC_1164.all;
                      entity mux4 is -- four-input multiplexer
                        generic(width: integer);
                        port(d0, d1, d2, d3: in  STD_LOGIC_VECTOR(width-1 downto 0);
                             s:              in  STD_LOGIC_VECTOR(1 downto 0);
                             y:              out STD_LOGIC_VECTOR(width-1 downto 0));
                      end;

                      architecture behave of mux4 is
                      begin
                        process(all) begin
                          case s is
                            when "00" =>  y <= d0;
                            when "01" =>  y <= d1;
                            when "10" =>  y <= d2;
                            when "11" =>  y <= d3;
                            when others => y <= d0; -- should never happen
                          end case;
                        end process;
```

```
end;



library IEEE; use IEEE.STD_LOGIC_1164.all;
entity mux5 is -- five-input multiplexer
  generic(width: integer);
  port(d0, d1, d2, d3, d4: in  STD_LOGIC_VECTOR(width-1 downto 0);
       s:                  in  STD_LOGIC_VECTOR(2 downto 0);
       y:                  out STD_LOGIC_VECTOR(width-1 downto 0));
end;
architecture behave of mux5 is
begin
  process(all) begin
    case s is
      when "000" =>  y <= d0;
      when "001" =>  y <= d1;
      when "010" =>  y <= d2;
      when "011" =>  y <= d3;
      when "100" =>  y <= d4;
      when others => y <= d0; -- should never happen
    end case;
  end process;
end;



library IEEE;
use IEEE.STD_LOGIC_1164.all;
use IEEE.std_logic_arith.all;
use ieee.std_logic_unsigned.all;

entity alu is
  port(A, B:     in  STD_LOGIC_VECTOR(31 downto 0);
       F:        in  STD_LOGIC_VECTOR(2 downto 0);
       Y:        out STD_LOGIC_VECTOR(31 downto 0);
       Zero:     out STD_LOGIC);
end;

architecture synth of alu is
  signal S, Bout:     STD_LOGIC_VECTOR(31 downto 0);
begin
  Bout <= (not B) when (F(3) = '1') else B;
  S <= A + Bout + F(3);
  Zero <= '1' when (Y = X"00000000") else '0';

  process(all) begin
    case F(1 downto 0) is
      when "00" => Y <= A and Bout;
      when "01" => Y <= A or Bout;
      when "10" => Y <= S;
      when "11" => Y <=
      ("0000000000000000000000000000000" & S(31));
      when others => Y <= X"00000000";
    end case;
  end process;
end;

library IEEE;
use IEEE.STD_LOGIC_1164.all;
use ieee.std_logic_unsigned.all;

entity signext is
  port(A:     in  STD_LOGIC_VECTOR(15 downto 0);
       Y:     out STD_LOGIC_VECTOR(31 downto 0));
end;
```

```vhdl
architecture synth of signext is
begin
  Y <= (15 downto 0 => a, others => a(15));
end;

library IEEE;
use IEEE.STD_LOGIC_1164.all;
use ieee.std_logic_unsigned.all;

entity zeroext is
  port(A:      in  STD_LOGIC_VECTOR(15 downto 0);
       Y:      out STD_LOGIC_VECTOR(31 downto 0));
end;
architecture synth of zeroext is
begin
  Y <= (15 downto 0 => a, others => '0');
end;

-- for lb / lbu
library IEEE;
use IEEE.STD_LOGIC_1164.all;
use ieee.std_logic_unsigned.all;

entity signext8_32 is
  port(A:     in  STD_LOGIC_VECTOR(7 downto 0);
       Y:     out STD_LOGIC_VECTOR(31 downto 0));
end;
architecture synth of signext8_32 is
begin
  Y <= (7 downto 0 => a, others => a(7));
end;


-- for lb / lbu
library IEEE;
use IEEE.STD_LOGIC_1164.all;
use ieee.std_logic_unsigned.all;

entity zeroext8_32 is
  port(A:     in  STD_LOGIC_VECTOR(7 downto 0);
       Y:     out STD_LOGIC_VECTOR(31 downto 0));
end;
architecture synth of zeroext8_32 is
begin
  Y <= (7 downto 0 => a, others =>'0');
end;
```

Exercise 7.29

$s0 is written, $t4 and $t5 are read in cycle 5.

Exercise 7.31
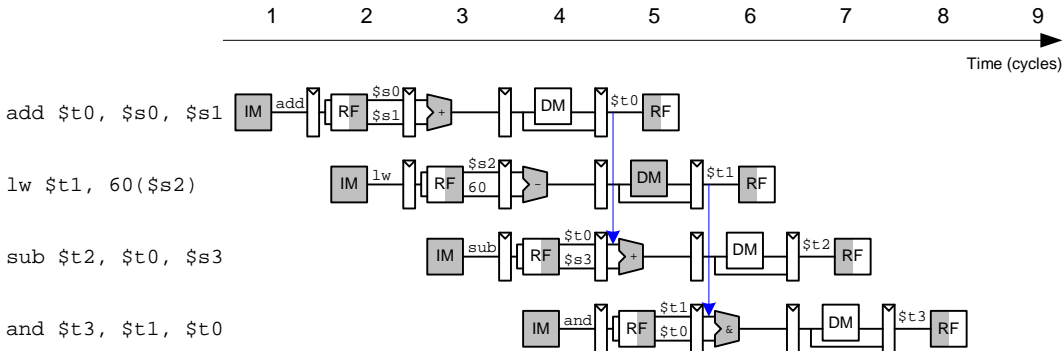
FIGURE 7.9 Abstract pipeline for Exercise 7.31

Exercise 7.33

It takes $3 + 6(10) + 3 =$ **66 clock cycles** to issue all the instructions.

instructions $= 3 + 5(10) + 2 = 55$

CPI $= 66$ clock cycles / 55 instructions $=$ **1.2.**

Exercise 7.35
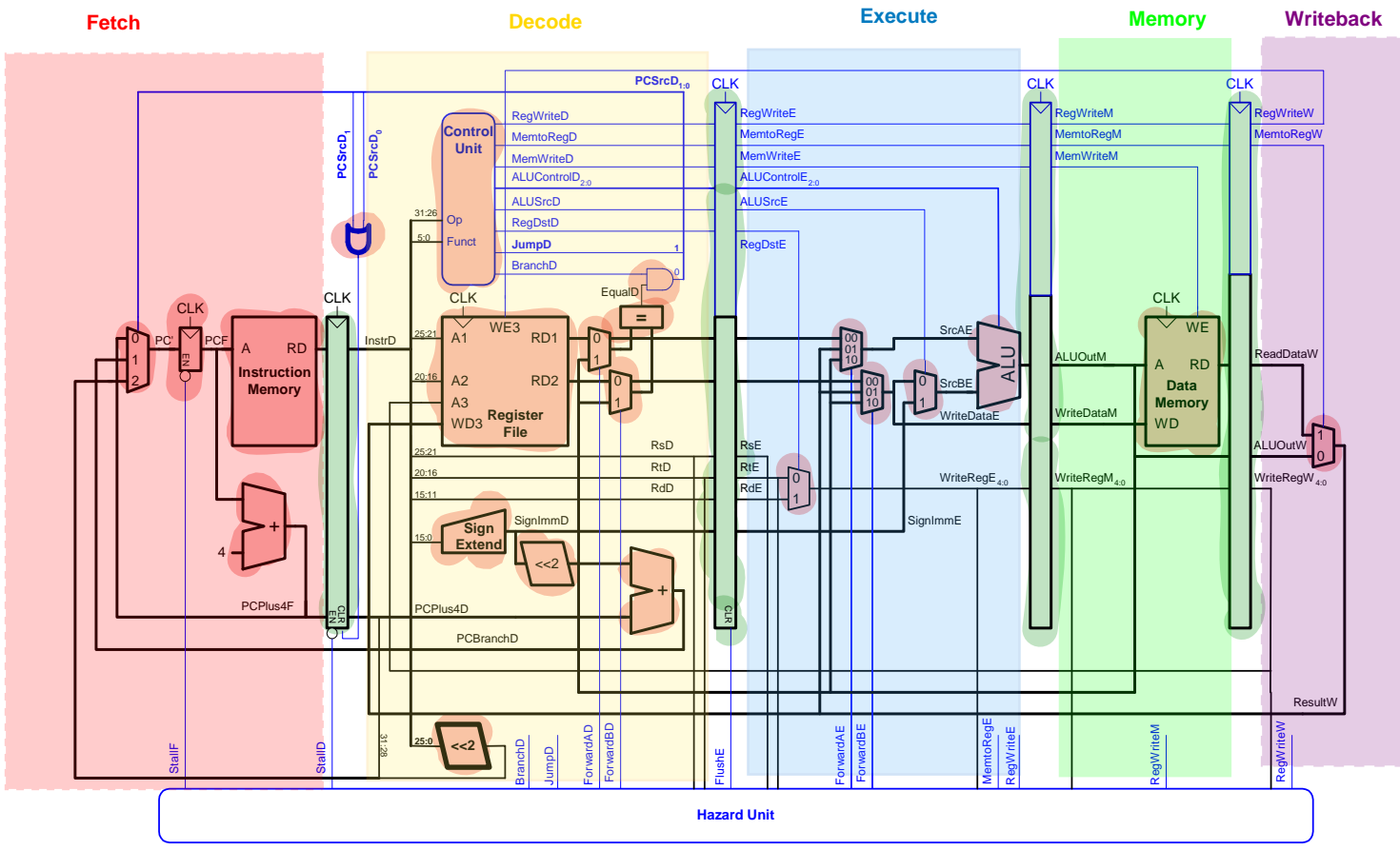
Instruction	opcode	RegWrite	RegDst	ALUSrc	Branch	MemWrite	MemtoReg	ALUOp	**JumpD**
R-type	000000	1	1	0	0	0	0	10	**0**
lw	100011	1	0	1	0	0	1	00	**0**
sw	101011	0	X	1	0	1	X	00	**0**
beq	000100	0	X	0	1	0	X	01	**0**
j	**000010**	**0**	**X**	**X**	**0**	**0**	**X**	**XX**	**1**

TABLE 7.12 Main decoder truth table enhanced to support j

We must also write new equations for the flush signal, *FlushE*.
```
FlushE = lwstall OR branchstall OR JumpD
```

Exercise 7.37

The critical path is the Decode stage, according to Equation 7.5:

T_{c3} = max(30 + 250 + 20, 2(150 + 25 + 40 + 15 + 25 + 20), 30 + 25 + 25 + 200 + 20, 30 + 220 + 20, 2(30 + 25 + 100)) = max(300, 550, 300, 270, 310) = 550 ps. The next slowest stage is 310 ps for the writeback stage, so it doesn't make sense to make the Decode stage any faster than that.

The slowest unit in the Decode stage is the register file read (150 ps). We need to reduce the cycle time by 550 - 310 = 240 ps. Thus, we need to reduce the register file read delay by 240/2 = 120 ps to (150 - 120) = **30 ps**.

The new cycle time is **310 ps**.

Exercise 7.39

CPI = 0.25(1+0.5*6) + 0.1(1) + 0.11(1+0.3*1)+0.02(2)+0.52(1) = 1.8

Execution Time = (100 x 10^9 instructions)(1.8 cycles/instruction)(400 x 10^{-12} s/cycle) = 72s

Exercise 7.41

MIPS Pipelined Processor Hazard Unit

SystemVerilog

```systemverilog
module hazard(input  logic [4:0] rsD, rtD, rsE, rtE,
              input  logic [4:0] writeregE,
                                 writeregM, writeregW,
              input  logic       regwriteE, regwriteM,
                                 regwriteW,
              input  logic       memtoregE, memtoregM,
              input  logic       branchD,
              output logic       forwardaD, forwardbD,
              output logic [1:0] forwardaE, forwardbE,
              output logic       stallF, stallD,
                                 flushE);

  logic lwstallD, branchstallD;

  // forwarding sources to D stage (branch equality)
  assign forwardaD = (rsD !=0 & rsD == writeregM &
                                        regwriteM);
  assign forwardbD = (rtD !=0 & rtD == writeregM &
                                        regwriteM);

  // forwarding sources to E stage (ALU)
  always_comb
    begin
      forwardaE = 2'b00; forwardbE = 2'b00;
      if (rsE != 0)
        if (rsE == writeregM & regwriteM)
          forwardaE = 2'b10;
        else if (rsE == writeregW & regwriteW)
          forwardaE = 2'b01;
      if (rtE != 0)
        if (rtE == writeregM & regwriteM)
          forwardbE = 2'b10;
        else if (rtE == writeregW & regwriteW)
          forwardbE = 2'b01;
    end

  // stalls
  assign #1 lwstallD = memtoregE &
                        (rtE == rsD | rtE == rtD);
  assign #1 branchstallD = branchD &
            (regwriteE &
            (writeregE == rsD | writeregE == rtD) |
             memtoregM &
            (writeregM == rsD | writeregM == rtD));

  assign #1 stallD = lwstallD | branchstallD;
  assign #1 stallF = stallD;
    // stalling D stalls all previous stages
  assign #1 flushE = stallD;
    // stalling D flushes next stage

  // Note: not necessary to stall D stage on store
  //       if source comes from load;
  //       instead, another bypass network could
  //       be added from W to M
endmodule
```

VHDL

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;
entity hazard is -- hazard unit
  port(rsD, rtD, rsE, rtE:            in STD_LOGIC_VECTOR(4 downto 0);
       writeregE, writeregM, writeregW: in STD_LOGIC_VECTOR(4 downto 0);
       regwriteE, regwriteM, regwriteW: in STD_LOGIC;
       memtoregE, memtoregM, branchD:  in STD_LOGIC;
       forwardaD, forwardbD:          out STD_LOGIC;
       forwardaE, forwardbE:          out STD_LOGIC_VECTOR(1 downto 0);
       stallF, flushE:                out STD_LOGIC;
       stallD:                        inout STD_LOGIC);
  end;

architecture behave of hazard is
  signal lwstallD, branchstallD: STD_LOGIC;
begin

  -- forwarding sources to D stage (branch equality)
  forwardaD <= '1' when ((rsD /= "00000") and (rsD = writeregM) and
                         (regwriteM = '1'))
               else '0';
  forwardbD <= '1' when ((rtD /= "00000") and (rtD = writeregM) and
                         (regwriteM = '1'))
               else '0';

  -- forwarding sources to E stage (ALU)
  process(all) begin
    forwardaE <= "00"; forwardbE <= "00";
    if (rsE /= "00000") then
      if ((rsE = writeregM) and (regwriteM = '1')) then
        forwardaE <= "10";
      elsif ((rsE = writeregW) and (regwriteW = '1')) then
        forwardaE <= "01";
      end if;
    end if;
    if (rtE /= "00000") then
      if ((rtE = writeregM) and (regwriteM = '1')) then
        forwardbE <= "10";
      elsif ((rtE = writeregW) and (regwriteW = '1')) then
        forwardbE <= "01";
      end if;
    end if;
  end process;

  -- stalls
  lwstallD <= '1' when ((memtoregE = '1') and ((rtE = rsD) or (rtE = rtD)))
              else '0';
  branchstallD <= '1' when ((branchD = '1') and
           (((regwriteE = '1') and
            ((writeregE = rsD) or (writeregE = rtD))) or
            ((memtoregM = '1') and
            ((writeregM = rsD) or (writeregM = rtD)))))
              else '0';
  stallD <= (lwstallD or branchstallD) after 1 ns;
  stallF <= stallD after 1 ns; -- stalling D stalls all previous stages
  flushE <= stallD after 1 ns; -- stalling D flushes next stage

  -- not necessary to stall D stage on store if source comes from load;
  -- instead, another bypass network could be added from W to M
end;
```
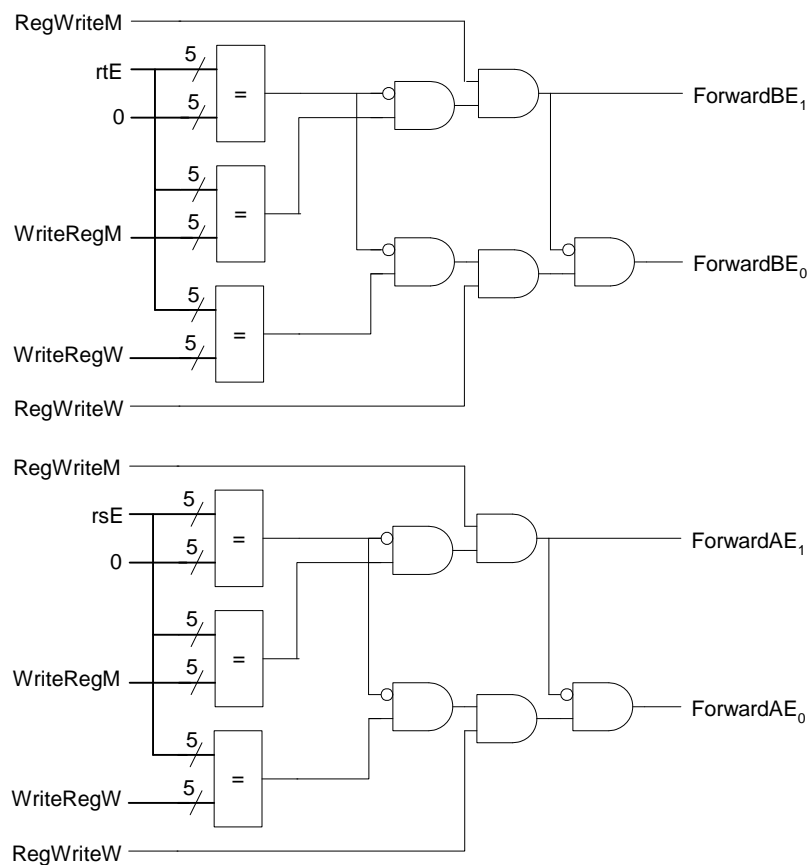
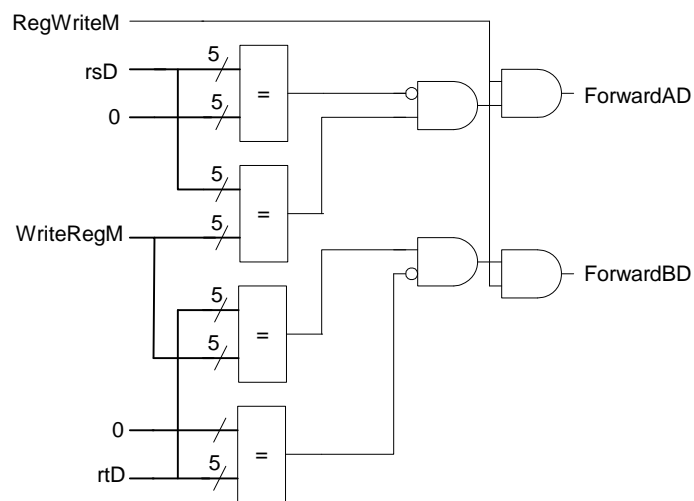FIGURE 7.10 Hazard unit hardware for forwarding to the Execution stage

FIGURE 7.11 Hazard unit hardware for forwarding to the Decode stage
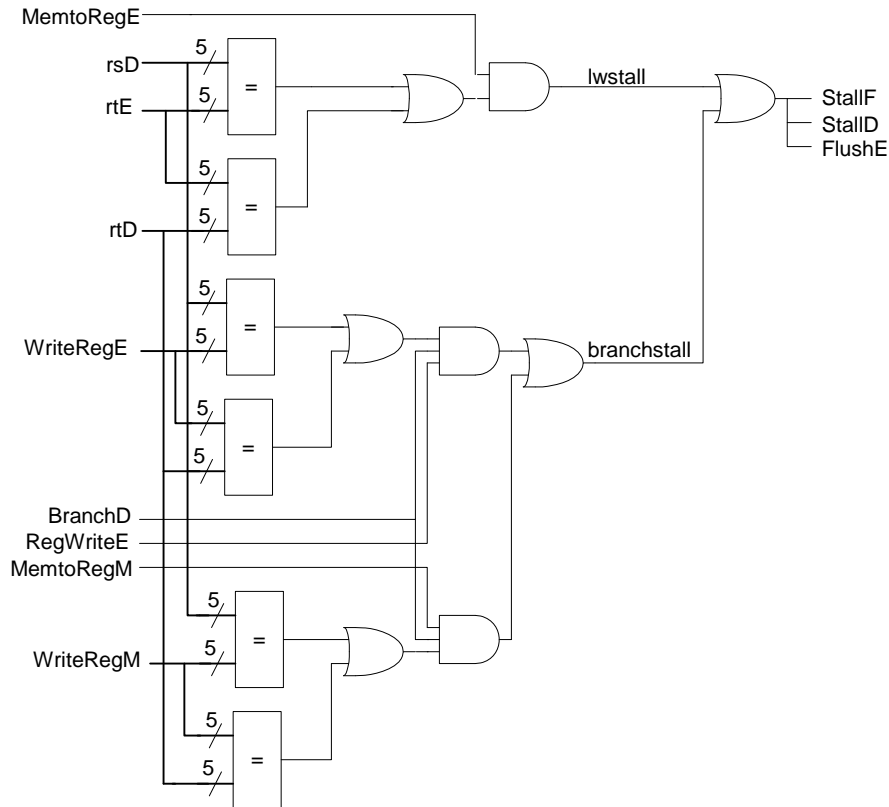
FIGURE 7.12 Hazard unit hardware for stalling/flushing in the Fetch, Decode, and Execute stages

Question 7.1

A pipelined microprocessors with *N* stages offers an ideal speedup of *N* over nonpipelined microprocessor. This speedup comes at the cost of little extra hardware: pipeline registers and possibly a hazard unit.

Question 7.3

A hazard in a pipelined microprocessor occurs when the execution of an instruction depends on the result of a previously issued instruction that has not completed executing. Some options for dealing with hazards are: (1) to have the compiler insert nops to prevent dependencies, (2) to have the compiler reorder the code to eliminate dependencies (inserting nops when this is impossible), (3) to have the hardware stall (or flush the pipeline) when there is a dependency, (4)

to have the hardware forward results to earlier stages in the pipeline or stall when that is impossible.

Options (1 and 2): Advantages of the first two methods are that no added hardware is required, so area and, thus, cost and power is minimized. However, performance is not maximized in cases where nops are inserted.

Option 3: The advantage of having the hardware flush or stall the pipeline as needed is that the compiler can be simpler and, thus, likely faster to run and develop. Also, because there is no forwarding hardware, the added hardware is minimal. However, again, performance is not maximized in cases where forwarding could have been used instead of stalling.

Option 4: This option offers the greatest performance advantage but also costs the most hardware for forwarding, stalling, and flushing the pipeline as necessary because of dependencies.

A combination of options 2 and 4 offers the greatest performance advantage at the cost of more hardware and a more sophisticated compiler.

CHAPTER 8

Exercise 8.1

Answers to this question will vary.

Temporal locality: (1) making phone calls (if you called someone recently, you're likely to call them again soon). (2) using a textbook (if you used a textbook recently, you will likely use it again soon).

Spatial locality: (1) reading a magazine (if you looked at one page of the magazine, you're likely to look at next page soon). (2) walking to locations on campus - if a student is visiting a professor in the engineering department, she or he is likely to visit another professor in the engineering department soon.

Exercise 8.3

Repeat data accesses to the following addresses:
0x0 0x10 0x20 0x30 0x40

The miss rate for the fully associative cache is: 100%. Miss rate for direct-mapped cache is $2/5 = 40\%$.

Exercise 8.5

(a) Increasing block size will increase the cache's ability to take advantage of spatial locality. This will reduce the miss rate for applications with spatial locality. However, it also decreases the number of locations to map an address, possibly increasing conflict misses. Also, the miss penalty (the amount of time it takes to fetch the cache block from memory) increases.

(b) Increasing the associativity increases the amount of necessary hardware but in most cases decreases the miss rate. Associativities above 8 usually show only incremental decreases in miss rate.

(c) Increasing the cache size will decrease capacity misses and could decrease conflict misses. It could also, however, increase access time.

Exercise 8.7

(a) **False.**
Counterexample: A 2-word cache with block size of 1 and access pattern:
    0 4 8
has a 50% miss rate with a direct-mapped cache, and a100% miss rate with a 2-way set associative cache.

(b) **True.**
The 16KB cache is a superset of the 8KB cache. (Note: it's possible that they have the *same* miss rate.)

(c) **Usually true.**
Instruction memory accesses display great spatial locality, so a large block size reduces the miss rate.

Exercise 8.9

Figure 8.1 shows where each address maps for each cache configuration.

Set 15	7C
	78
	74
	70

	20

Set 7	9C 1C
	98 18
	94 14
	90 10
	4C 8C C
	48 88 8
	44 84 4
Set 0	40 80 0

(a) Direct Mapped

| 7C 9C 1C |
| 78 98 18 |
| 74 94 14 |
| 70 90 10 |
| 4C 8C C |
| 48 88 8 |
| 44 84 4 |
| 40 80 0 20 |

(c) 2-way assoc

| 78-7C |
| 70-74 |
| |
| 20-24 |
| 98-9C 18-1C |
| 90-94 10-14 |
| 48-4C 88-8C 8-C |
| 40-44 80-84 0-4 |

(d) direct mapped b=2
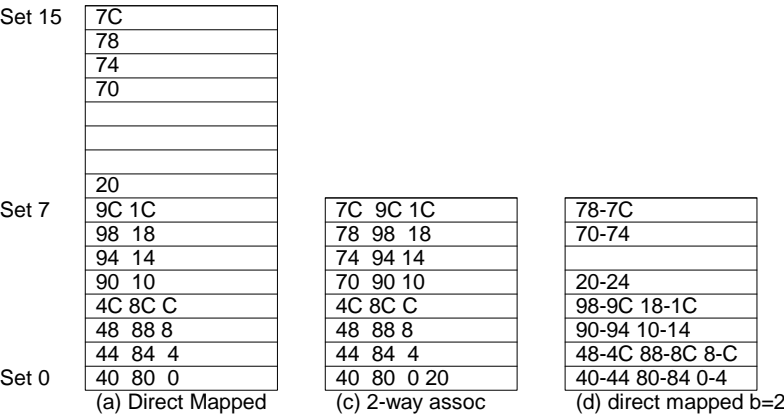
FIGURE 8.1 Address mappings for Exercise 8.9

(a) **80% miss rate**. Addresses 70-7C and 20 use unique cache blocks and are not removed once placed into the cache. Miss rate is 20/25 = 80%.

(b) **100% miss rate**. A repeated sequence of length greater than the cache size produces no hits for a fully-associative cache using LRU.

(c) **100% miss rate**. The repeated sequence makes at least three accesses to each set during each pass. Using LRU replacement, each value must be replaced each pass through.

(d) **40% miss rate**. Data words from consecutive locations are stored in each cache block. The larger block size is advantageous since accesses in the given sequence are made primarily to consecutive word addresses. A block size of two cuts the number of block fetches in half since two words are obtained per block fetch. The address of the second word in the block will always hit in this type of scheme (e.g. address 44 of the 40-44 address pair). Thus, the second consecutive word accesses always hit: 44, 4C, 74, 7C, 84, 8C, 94, 9C, 4, C, 14, 1C. Tracing block accesses (see Figure 8.1) shows that three of the eight blocks (70-74, 78-7C, 20-24) also remain in memory. Thus, the hit rate is: 15/25 = 60% and miss rate is 40%.

Exercise 8.11

(a) 128
(b) 100%
(c) ii

Exercise 8.13

(a)
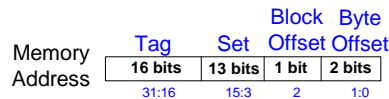
(b) Each tag is 16 bits. There are 32Kwords / (2 words / block) = 16K blocks and each block needs a tag: $16 \times 16K = 2^{18} = 256$ Kbits of tags.

(c) Each cache block requires: 2 status bits, 16 bits of tag, and 64 data bits, thus each set is 2×82 bits = **164 bits**.

(d) The design must use enough RAM chips to handle both the total capacity and the number of bits that must be read on each cycle. For the data, the SRAM must provide a capacity of 128 KB and must read 64 bits per cycle (one 32-bit word from each way). Thus the design needs at least 128KB / (8KB/RAM) = 16 RAMs to hold the data and 64 bits / (4 pins/RAM) = 16 RAMs to supply the number of bits. These are equal, so the design needs exactly 16 RAMs for the data.

For the tags, the total capacity is 32 KB, from which 32 bits (two 16-bit tags) must be read each cycle. Therefore, only 4 RAMs are necessary to meet the capacity, but 8 RAMs are needed to supply 32 bits per cycle. Therefore, the design will need 8 RAMs, each of which is being used at half capacity.

With 8Ksets, the status bits require another 8K × 4-bit RAM. We use a 16K × 4-bit RAM, using only half of the entries.
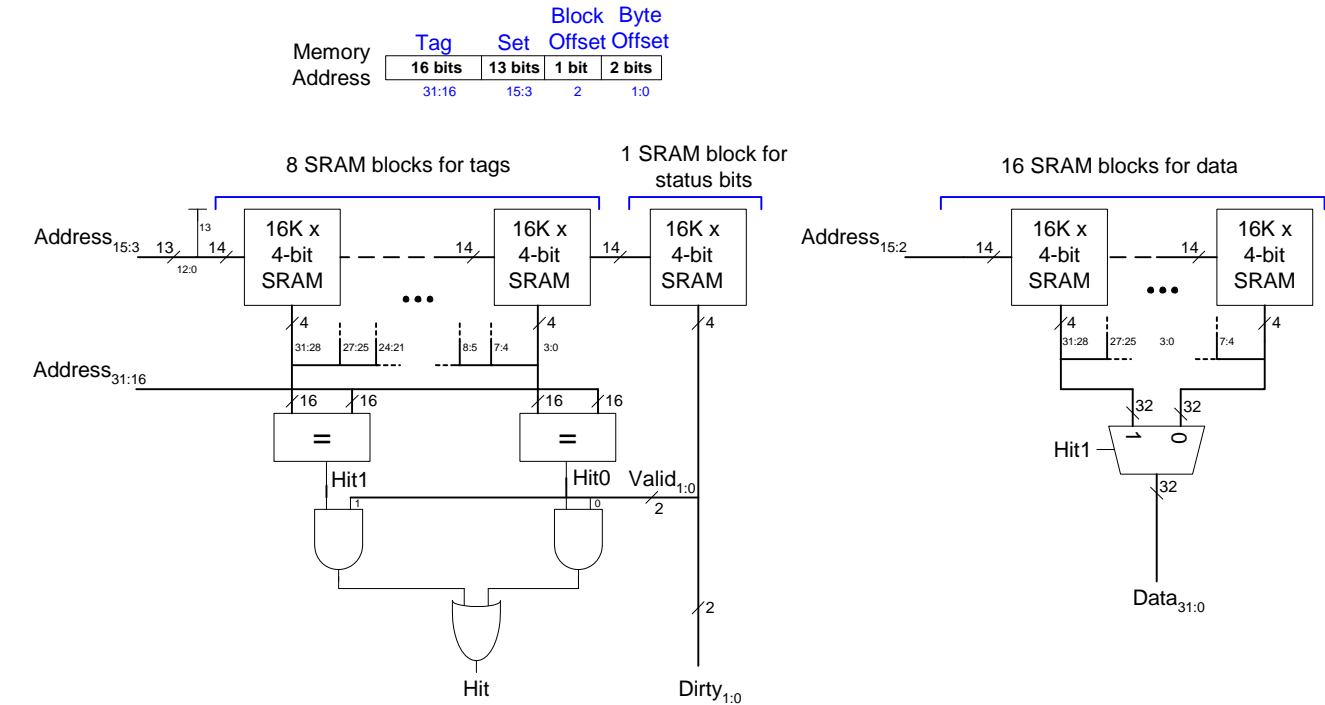
FIGURE 8.2 Cache design for Exercise 8.13

Bits 15:2 of the address select the word within a set and block. Bits 15-3 select the set. Bits 31:16 of the address are matched against the tags to find a hit in one (or none) of the two blocks with each set.

Exercise 8.15

(a)
FIFO:
FIFO replacement approximates LRU replacement by discarding data that has been in the cache longest (and is thus least likely to be used again). A FIFO cache can be stored as a queue, so the cache need not keep track of the least recently used way in an *N*-way set-associative cache. It simply loads a new cache block into the next way upon a new access. FIFO replacement doesn't work well when the *least recently used* data is not also the data fetched *longest ago*.
Random:

Random replacement requires less overhead (storage and hardware to update status bits). However, a random replacement policy might randomly evict recently used data. In practice random replacement works quite well.

(b)
FIFO replacement would work well for an application that accesses a first set of data, then the second set, then the first set again. It then accesses a third set of data and finally goes back to access the second set of data. In this case, FIFO would replace the first set with the third set, but LRU would replace the second set. The LRU replacement would require the cache to pull in the second set of data twice.

Exercise 8.17

(a)
$$AMAT = t_{\text{cache}} + MR_{\text{cache}}\, t_{\text{MM}}$$

With a cycle time of $1/1$ GHz $= 1$ ns,

$$AMAT = 1\text{ ns} + 0.15(200\text{ ns}) = 31\text{ ns}$$

(b) CPI $= 31 + 4 = $ **35 cycles** (for a load)
    CPI $= 31 + 3 = $ **34 cyles** (for a store)
(c) Average CPI $= (0.11 + 0.02)(3) + (0.52)(4) + (0.1)(34) + (0.25)(35) = $ **14.6**
(d) Average CPI $= 14.6 + 0.1(200) = $ **34.6**

Exercise 8.19

1 million gigabytes of hard disk $\approx 2^{20} \times 2^{30} = 2^{50}$ bytes $= 1$ petabytes

10,000 gigabytes of hard disk $\approx 2^{14} \times 2^{30} = 2^{44}$ bytes $= 16$ terabytes

Thus, the system would need **44 bits** for the physical address and **50 bits** for the virtual address.

Exercise 8.21

(a) **31 bits**
(b) $2^{50}/2^{12} = $ **2^{38} virtual pages**
(c) 2 GB / 4 KB $= 2^{31}/2^{12} = $ **2^{19} physical pages**
(d) virtual page number: **38 bits**; physical page number $= $ **19 bits**
(e) **2^{38}** page table entries (one for each virtual page).

(f) Each entry uses 19 bits of physical page number and 2 bits of status information. Thus, **3 bytes** are needed for each entry (rounding 21 bits up to the nearest number of bytes).

(h)The total table size is **3 x 2^{38} bytes**.

Exercise 8.23

(a) 1 valid bit + 19 data bits (PPN) + 38 tag bits (VPN) x 128 entries = 58 * 128 bits = 7424 bits

(b)
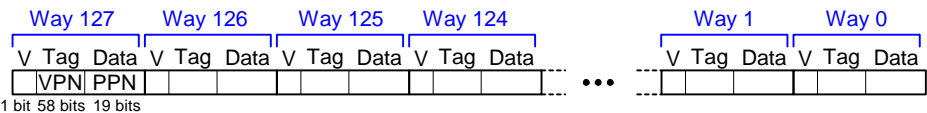
(c) 128 x 58-bit SRAM

Exercise 8.25

(a) Each entry in the page table has 2 status bits (*V* and *D*), and a physical page number (22-16 = 6 bits). The page table has $2^{25 - 16} = 2^9$ entries.

Thus, the total page table size is $2^9 \times 8$ bits = **4096 bits**

(b)

This would increase the virtual page number to 25 - 14 = 11 bits, and the physical page number to 22 - 14 = 8 bits. This would increase the page table size to:

$2^{11} \times 10$ bits = **20480 bits**

This increases the page table by 5 times, wasted valuable hardware to store the extra page table bits.

(c)

Yes, this is possible. In order for concurrent access to take place, the number of set + block offset + byte offset bits must be less than the page offset bits.

(d) It is impossible to perform the tag comparison in the on-chip cache concurrently with the page table access because the upper (most significant) bits of the physical address are unknown until after the page table lookup (address translation) completes.

Exercise 8.27

(a) 2^{32} bytes = 4 gigabytes

(b) The amount of the hard disk devoted to virtual memory determines how many applications can run and how much virtual memory can be devoted to each application.

(c) The amount of physical memory affects how many physical pages can be accessed at once. With a small main memory, if many applications run at once or a single application accesses addresses from many different pages, thrashing can occur. This can make the applications dreadfully slow.

Exercise 8.29

(a)

```
#  MIPS code for Traffic Light FSM
       addi $t0, $0,  0xC     # $t0 = green / red
       addi $t1, $0,  0x14    # $t1 = yellow / red
       addi $t2, $0,  0x21    # $t2 = red / green
       addi $t3, $0,  0x22    # $t3 = red / yellow

Start: sw   $t2, 0xF004($0)  # lights = red / green
S0:    lw   $t4, 0xF000($0)  # $t4 = sensor values
       andi $t4, $t4, 0x2    # $t4 = TA
       bne  $t4, $0,  S0     # if TA == 1, loop back to S0

S1:    sw   $t3, 0xF004($0)  # lights = red / yellow

       sw   $t0, 0xF004($0)  # lights = green / red
S2:    lw   $t4, 0xF000($0)  # $t4 = sensor values
       andi $t4, $t4, 0x1    # $t4 = TB
       bne  $t4, $0,  S2     # if TB == 1, loop back to S2

S3:    sw   $t1, 0xF004($0)  # lights = yellow / red
       j    Start
```

(b)

(c) **Address Decoder for Exercise 8.29**

SystemVerilog

```systemverilog
module addrdec(input  logic [31:0] addr,
               input  logic        memwrite,
               output logic        WELights, Mwrite,
               output logic        rdselect);

  parameter  T      = 16'hF000; // traffic sensors
  parameter  Lights = 16'hF004; // traffic lights

  logic [15:0] addressbits;

  assign addressbits = addr[15:0];

  always_comb
    if (addr[31:16] == 16'hFFFF) begin
      // writedata control
      if (memwrite)
        if (addressbits == Lights)
          {WELights, Mwrite, rdselect} = 3'b100;
        else
          {WELights, Mwrite, rdselect} = 3'b010;

      // readdata control
      else
  if ( addressbits == T )
          {WELights, Mwrite, rdselect} = 3'b001;
        else
          {WELights, Mwrite, rdselect} = 3'b000;
    end
    else
      {WELights, Mwrite, rdselect} =
  {1'b0, memwrite, 1'b0};
endmodule
```

VHDL

```vhdl
library IEEE; use IEEE.STD_LOGIC_1164.all;
entity addrdec is -- address decoder
  port(addr:                      in STD_LOGIC_VECTOR(31 downto 0);
       memwrite:                  in STD_LOGIC;
       WELights, Mwrite, rdselect: out STD_LOGIC);
end;

architecture struct of addrdec is
begin

  process(all) begin
    if (addr(31 downto 16) = X"FFFF") then
      -- writedata control
      if (memwrite = '1') then
        if (addr(15 downto 0) = X"F004") then    -- traffic lights
          WELights <= '1'; Mwrite <= '0'; rdselect <= '0';
        else
          WELights <= '0'; Mwrite <= '1'; rdselect <= '0';
        end if;

      -- readdata control
      else
        if ( addr(15 downto 0) = X"F000" ) then  -- traffic sensors
          WELights <= '0'; Mwrite <= '0'; rdselect <= '1';
        else
          WELights <= '0'; Mwrite <= '0'; rdselect <= '0';
        end if;
      end if;

    -- not a memory-mapped address
    else
      WELights <= '0'; Mwrite <= memwrite; rdselect <= '0';
    end if;
  end process;
end;
```

Question 8.1

Caches are categorized based on the number of blocks (B) in a set. In a direct mapped cache, each set contains exactly one block, so the cache has S = B sets. Thus a particular main memory address maps to a unique block in the cache. In an N-way set associative cache, each set contains N blocks. The address still maps to a unique set, with S = B / N sets. But the data from that address can go in any of the N blocks in the set. A fully associative cache has only S = 1 set. Data can go in any of the B blocks in the set. Hence, a fully associative cache is another name for a B-way set associative cache.

A **direct mapped cache** performs better than the other two when the data access pattern is to sequential cache blocks in memory with a repeat length one greater than the number of blocks in the cache.

An *N-way set-associative cache* performs better than the other two when N sequential block accesses map to the same set in the set-associative *and* di-

rect-mapped caches. The last set has $N+1$ blocks that map to it. This access pattern then repeats.

In the direct-mapped cache, the accesses to the same set conflict, causing a 100% miss rate. But in the set-associative cache all accesses (except the last one) don't conflict. Because the number of block accesses in the repeated pattern is one more than the number of blocks in the cache, the fully associative cache also has a 100% miss rate.

A **fully associative cache** performs better than the other two when the direct-mapped and set-associative accesses conflict and the fully associative accesses don't. Thus, the repeated pattern must access at most B blocks that map to conflicting sets in the direct and set-associative caches.

Question 8.3

The advantages of using a virtual memory system are the illusion of a larger memory without the expense of expanding the physical memory, easy relocation of programs and data, and protection between concurrently running processes.

The disadvantages are a more complex memory system and the sacrifice of some physical and possibly virtual memory to store the page table.

Question 8.5

No, addresses used for memory-mapped I/O may not be cached. Otherwise, repeated reads to the I/O device would read the old (cached) value. Likewise, repeated writes would write to the cache instead of the I/O device.