# Problem Set #1

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1/1 points

1.

3-way-Merge Sort : Suppose that instead of dividing in half at each step of Merge Sort, you divide into thirds, sort each third, and finally combine all of them using a three-way merge subroutine. What is the overall asymptotic running time of this algorithm? (Hint: Note that the merge step can still be implemented in O(n) time.)

- $\bigcap n(\log(n))^2$
- $\bigcirc$  n
- $O \quad n^2 \log(n)$
- $\bigcap$   $n \log(n)$

# **Correct Response**

That's correct! There is still a logarithmic number of levels, and the overall amount of work at each level is still linear.

<b>~</b>	1 / 1 points
f(n) *	e given functions $f$ and $g$ such that $f(n) = O(g(n))$ . Is $log_2(f(n)^c) = O(g(n)*log_2(g(n)))$ ? (Here $c$ is some positive constant.) ould assume that $f$ and $g$ are nondecreasing and always bigger than 1.
0	Sometimes yes, sometimes no, depending on the functions $\boldsymbol{f}$ and $\boldsymbol{g}$
0	False
0	True
That loga	ect Response $c'$ 's correct! Roughly, because the constant $c'$ in the exponent is inside a rithm, it becomes part of the leading constant and gets suppressed the big-Oh notation.  Sometimes yes, sometimes no, depending on the constant $c'$
f(n) =	1/1 points e again two (positive) nondecreasing functions $f$ and $g$ such that $O(g(n))$ . Is $2^{f(n)}=O(2^{g(n)})$ ? (Multiple answers may be correct, you check all of those that apply.)
	Never
	ect Response example, what if f(n)=g(n)?

**Correct Response** 

Sometimes

Yes if  $f(n) \le g(n)$  for all sufficiently large n**Correct Response** Always **Correct Response** What if f(n) = 2n and g(n) = n? points 4. k-way-Merge Sort. Suppose you are given k sorted arrays, each with n elements, and you want to combine them into a single array of kn elements. Consider the following approach. Using the merge subroutine taught in lecture, you merge the first 2 arrays, then merge the  $3^{rd}$  given array with this merged version of the first two arrays, then merge the  $4^{th}$  given array with the merged version of the first three arrays, and so on until you merge in the final  $(k^{th})$  input array. What is the running time taken by this successive merging algorithm, as a function of k and n? (Optional: can you think of a faster way to do the k-way merge procedure?)  $\theta(nk)$  $\theta(n^2k)$  $\theta(nk^2)$ **Correct Response** That's correct! For the upper bound, the merged list size is always O(kn), merging is linear in the size of the larger array, and there are k iterations. For the lower bound, each of the last k/2 merges takes  $\Omega(kn)$  time.  $\theta(n \log(k))$ 

5.

Arrange the following functions in increasing order of growth rate (with g(n) following f(n) in your list if and only if f(n) = O(g(n))).

- a) $2^{\log(n)}$
- b) $2^{2^{\log(n)}}$
- c) $n^{5/2}$
- d) $2^{n^2}$
- $e)n^2 \log(n)$

Write your 5-letter answer, i.e., the sequence in lower case letters in the space provided. For example, if you feel that the answer is a->b->c->d->e (from smallest to largest), then type abcde in the space provided without any spaces before / after / in between the string.

You can assume that all logarithms are base 2 (though it actually doesn't matter).

WARNING: this question has multiple versions, you might see different ones on different attempts!

#### Preview

# eabcd

Please note: Each of the following will be interpreted as a single variable, not as a product of variables: eabcd. To multiply variables, please use \* (e.g. enter x\*y to multiply variables x and y).

## eabcd

#### **Incorrect Response**

One approach is to graph these functions for large values of n. Once in a while this can be misleading, however. Another useful trick is to take logarithms and see what happens (though again be careful, as in Question 3).

## Correct Answer: aecbd

One approach is to graph these functions for large values of n. Once in a while this can be misleading, however. Another useful trick is to take logarithms and see what happens (though again be careful, as in

Question 3).			

