



SuperDataScience

# NEURAL NETWORKS IN PYTHON



# NEURAL NETWORKS IN PYTHON

1. Part 1
  - Biological fundamentals
  - Single layer perceptron
2. Part 2
  - Multi-layer perceptron
3. Part 3
  - Pybrain
  - Sklearn
  - TensorFlow
  - PyTorch



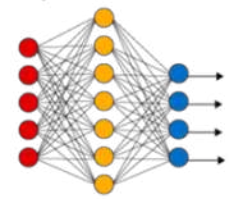
SuperDataScience

# NEURAL NETWORKS

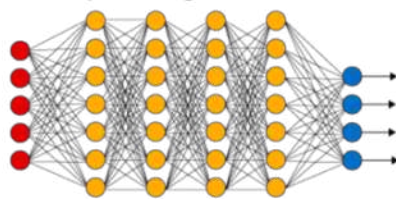


# 1. WHAT ARE NEURAL NETWORKS?

Simple Neural Network

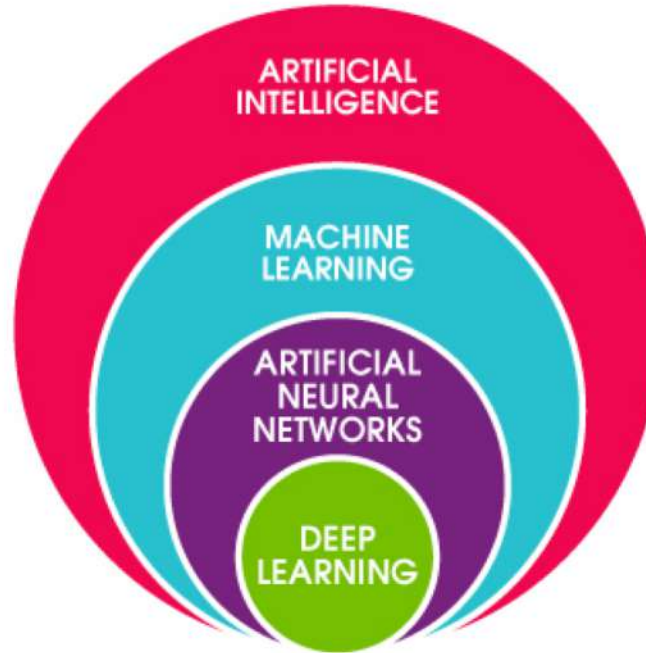


Deep Learning Neural Network



● Input Layer    ● Hidden Layer    ● Output Layer

Source: <https://www.meetup.com/pt-BR/Deep-Learning-for-Sciences-Engineering-and-Arts/events/257483663/>



Source: <https://elearningindustry.com/artificial-intelligence-will-shape-elearning>

## Artificial intelligence

- Expert systems
- Computer vision
- Genetic algorithms
- Natural language processing
- Fuzzy logic
- Case based reasoning
- Multi-agent systems
- Machine learning**

## Machine learning

- Naïve Bayes
- Decision trees
- SVM
- K-NN
- Rules

## Artificial neural networks





### 3. WHY STUDY NEURAL NETWORKS?



Google



amazon



NVIDIA®



python

# PLAN OF ATTACK – SINGLE LAYER PERCEPTRON

1. Neural networks applications
2. Biological fundamentals
3. Artificial neuron (perceptron)
4. Implementation of a perceptron from scratch using Python and Numpy

# NEURAL NETWORKS APPLICATIONS



Source: <https://www.livemint.com/Technology/T4C472fmWlWVnQ2P45mk7XouZ-free-can-unlock-your-smartphone-But-is-it-safe.html>



Source: <https://www.vepo.com.br/picardo-cancela-veiculos-autonomos-uma-realidade-para-impensavel-cockpit-de-autonomos-car-hud-head-up-display-and-digital-speedometer-self-driving-vehicle/>



Source: <https://www.biosciencetoday.co.uk/artificial-neural-networks-working-with-image-guided-therapies-to-improve-heart-disease-treatment/>



# NEURAL NETWORKS APPLICATIONS



Source: <https://howtobefinance.com/resources/engineering-in-stock-market-execution-quantifying-market-as-fundamentals-3895a9f911/>



Source: [https://www.endpoint-translation.com/blog/7d517851296268fbcd4d2wAR1dQufB73swWQIEVdmDrA5a4Nl\\_P6Z4N6\\_3uIMm4Ntd0Utre92uapX6](https://www.endpoint-translation.com/blog/7d517851296268fbcd4d2wAR1dQufB73swWQIEVdmDrA5a4Nl_P6Z4N6_3uIMm4Ntd0Utre92uapX6)



Source: <https://dreamdeeply.com/>



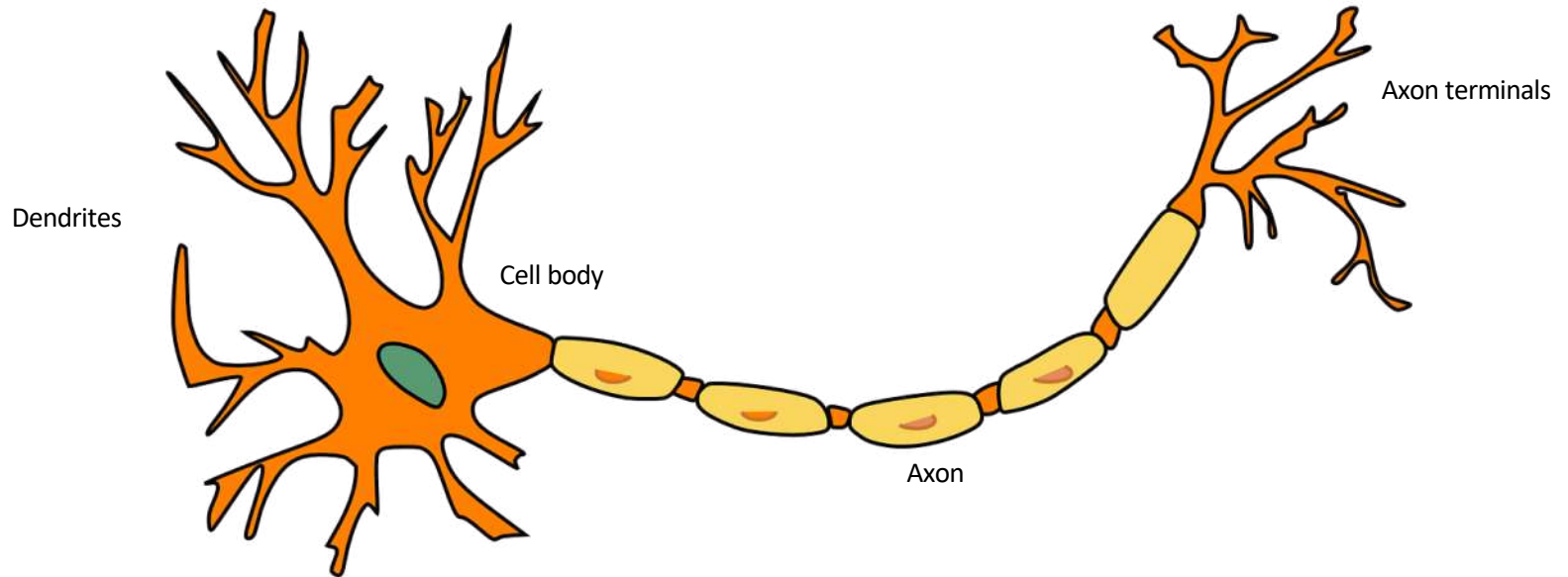
Source: <https://www.theverge.com/tldr/2019/7/15/18926095/ai-generated-fake-people-portraits-these-people-does-not-exist-style>



# BIOLOGICAL FUNDAMENTALS

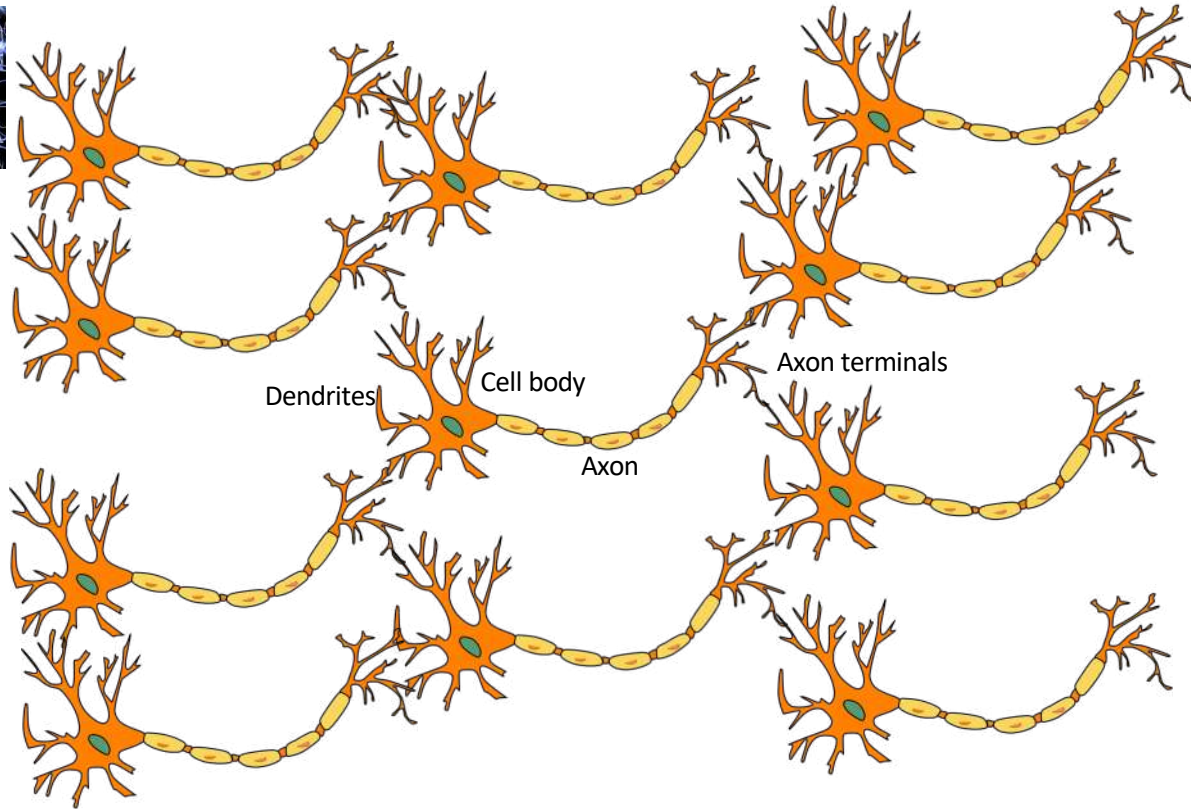


# BIOLOGICAL FUNDAMENTALS



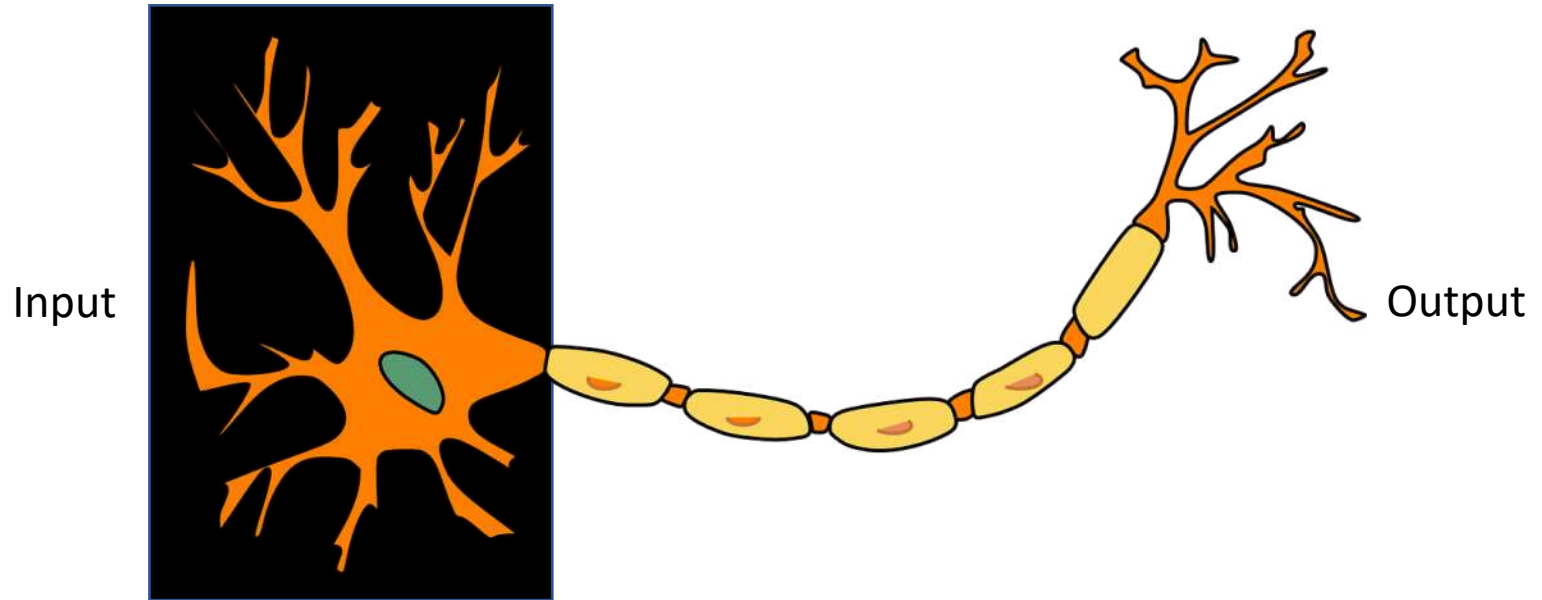


# BIOLOGICAL FUNDAMENTALS



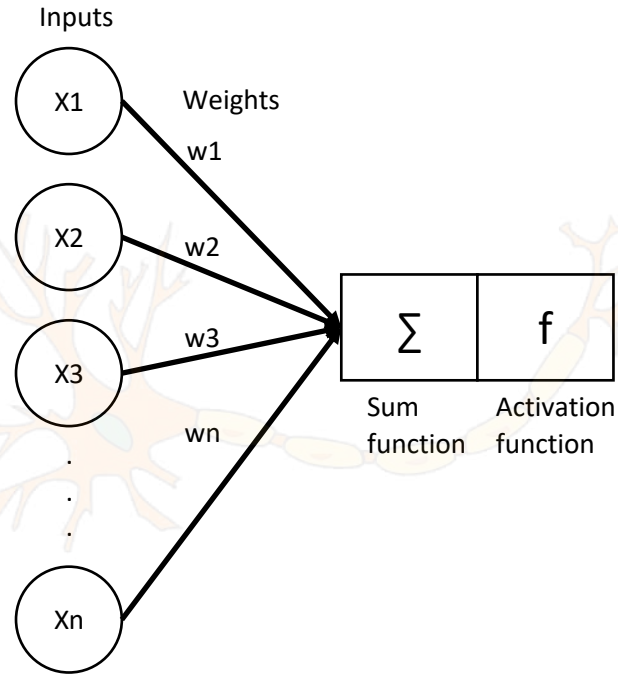
Synapse

# ARTIFICIAL NEURON





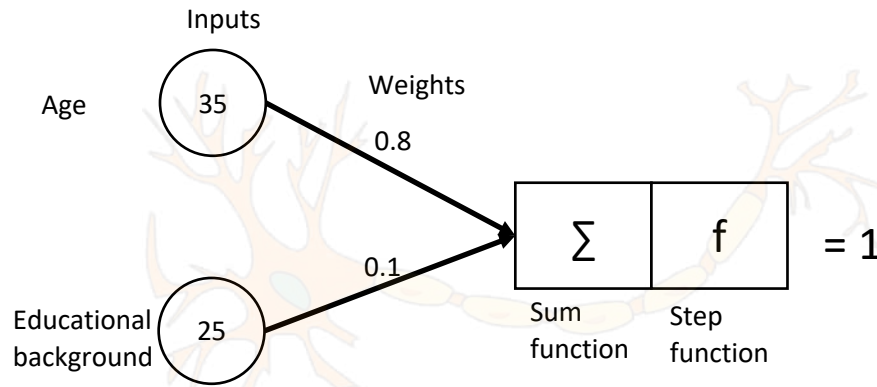
# ARTIFICIAL NEURON



$$sum = \sum_{i=1}^n x_i * w_i$$

$$x_1 * w_1 + x_2 * w_2 + x_3 * w_3$$

# PERCEPTRON



$$sum = \sum_{i=1}^n x_i * w_i$$

$$sum = (35 * 0.8) + (25 * 0.1)$$

$$sum = 28 + 2.5$$

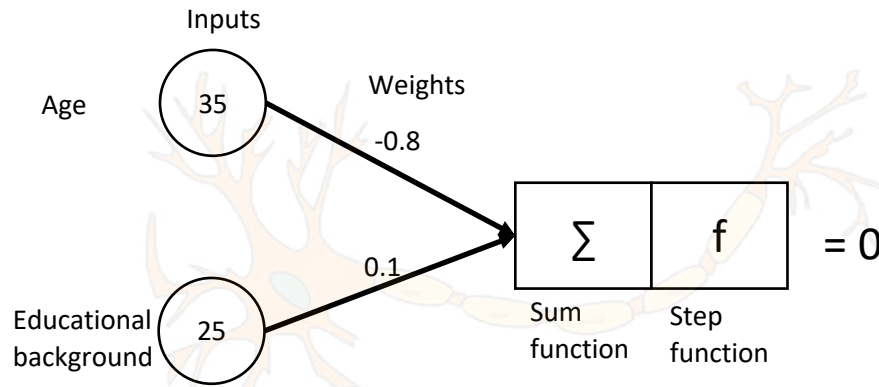
$$sum = 30.5$$

Greater or equal to 1 = 1

Otherwise = 0

“All or nothing” representation

# PERCEPTRON



$$sum = \sum_{i=1}^n x_i * w_i$$

$$sum = (35 * -0.8) + (25 * 0.1)$$

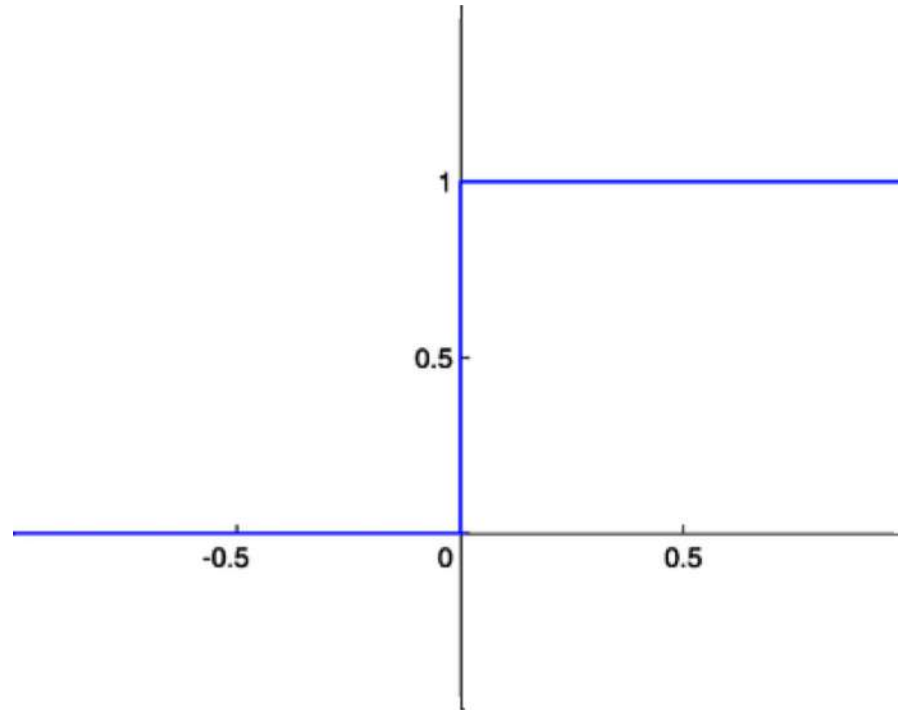
$$sum = -28 + 2.5$$

$$sum = -25.5$$

Greater or equal to 1 = 1

Otherwise = 0

# STEP FUNCTION



# PERCEPTRON

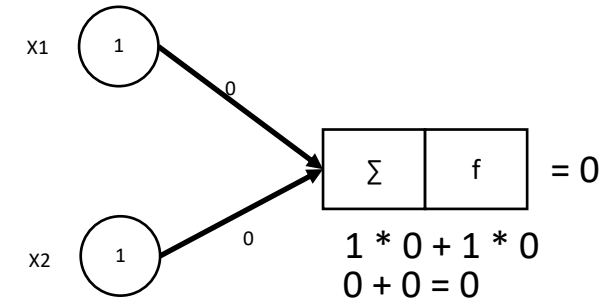
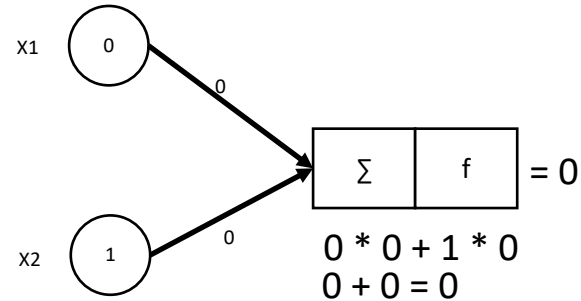
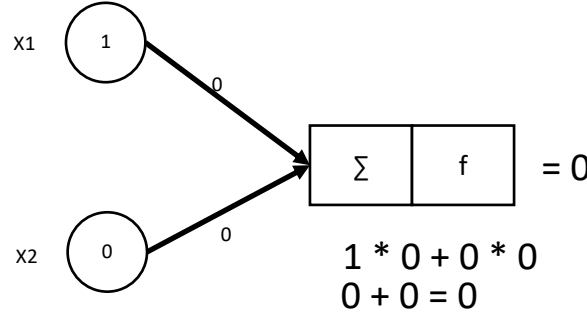
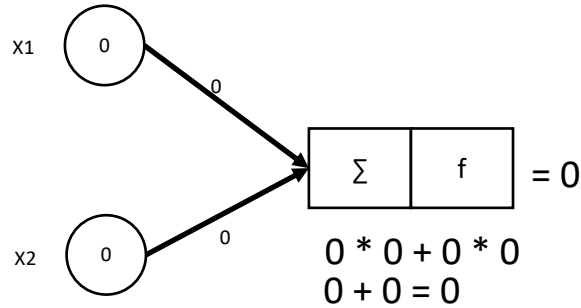
- Positive weight – exciting synapse
- Negative weight – inhibitory synapse
- Weights are the synapses
- Weights amplify or reduce the input signal
- The knowledge of a neural network is the weights



# "AND" OPERATOR

X1	X2	Class
0	0	0
0	1	0
1	0	0
1	1	1

# "AND" OPERATOR



X1	X2	Class
0	0	0
0	1	0
1	0	0
1	1	1

error = correct - prediction

Class	Prediction	Error
0	0	0
0	0	0
0	0	0
1	0	1

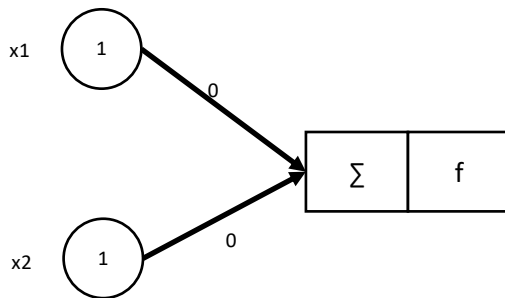
75%

$\text{weight}(n+1) = \text{weight}(n) + (\text{learning\_rate} * \text{input} * \text{error})$

# "AND" OPERATOR

error = correct - prediction

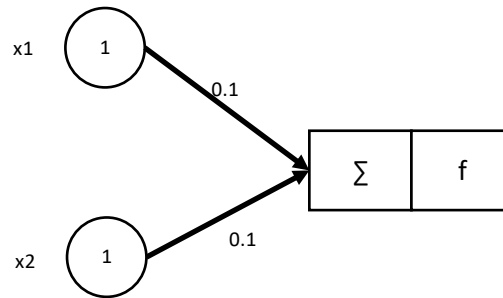
Class	Prediction	Error
0	0	0
0	0	0
0	0	0
1	0	1



$$\text{weight}(n+1) = \text{weight}(n) + (\text{learning\_rate} * \text{input} * \text{error})$$

$$\text{weight}(n+1) = 0 + (0.1 * 1 * 1)$$

$$\text{weight}(n+1) = 0.1$$

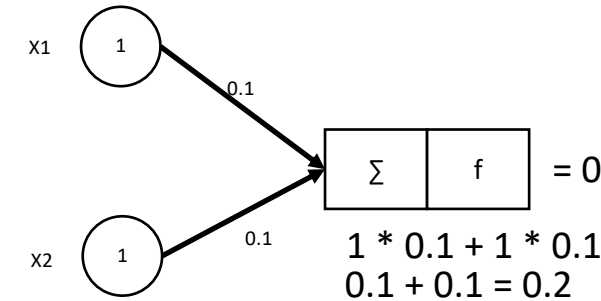
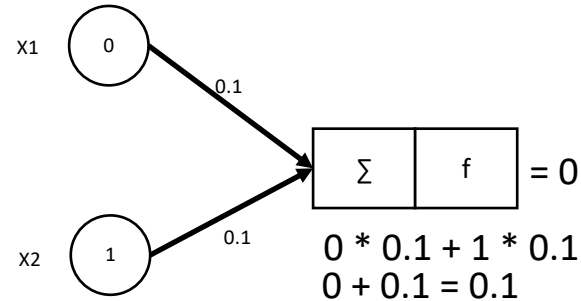
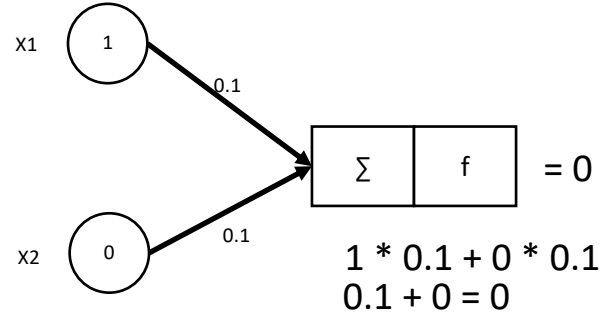
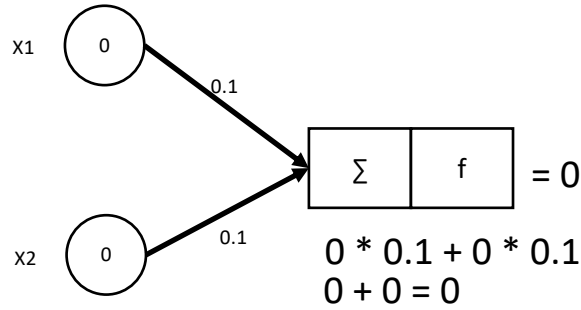


$$\text{weight}(n+1) = \text{weight}(n) + (\text{learning\_rate} * \text{input} * \text{error})$$

$$\text{weight}(n+1) = 0 + (0.1 * 1 * 1)$$

$$\text{weight}(n+1) = 0.1$$

# "AND" OPERATOR



X1	X2	Class
0	0	0
0	1	0
1	0	0
1	1	1

error = correct - prediction

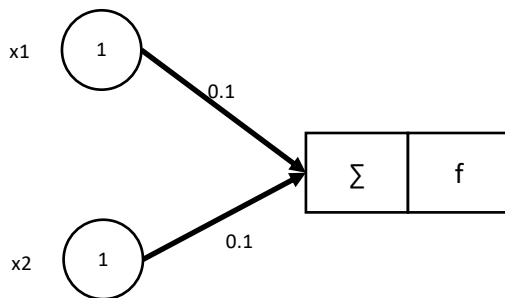
Class	Prediction	Error
0	0	0
0	0	0
0	0	0
1	0	1

75%

# "AND" OPERATOR

error = correct - prediction

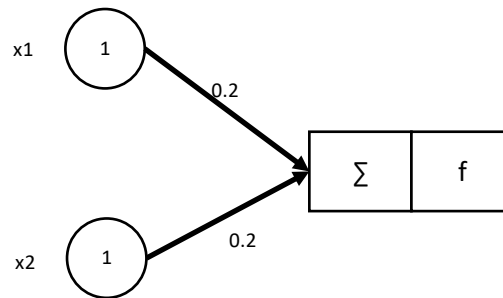
Class	Prediction	Error
0	0	0
0	0	0
0	0	0
1	0	1



$\text{weight}(n + 1) = \text{weight}(n) + (\text{learning\_rate} * \text{input} * \text{error})$

$\text{weight}(n + 1) = 0.1 + (0.1 * 1 * 1)$

$\text{weight}(n + 1) = 0.2$



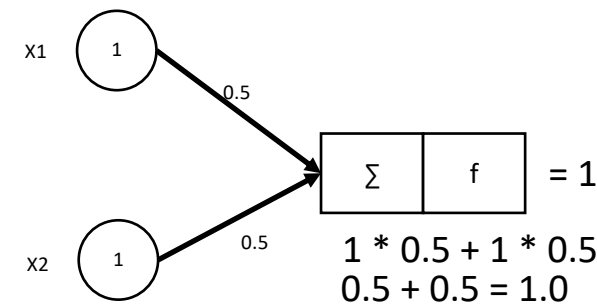
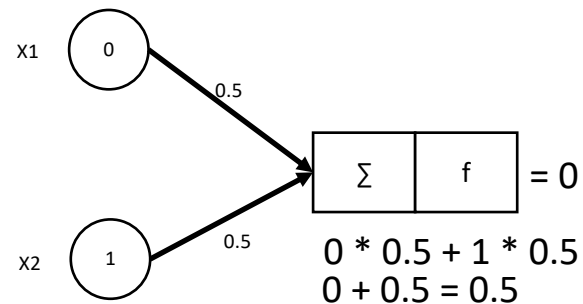
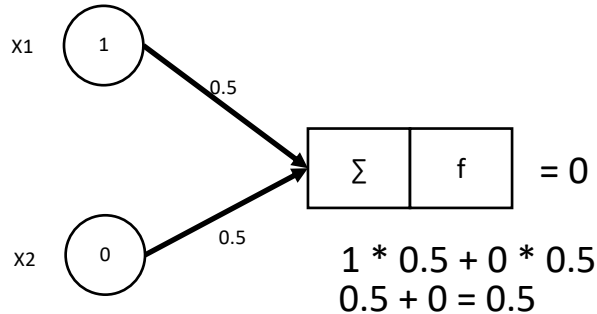
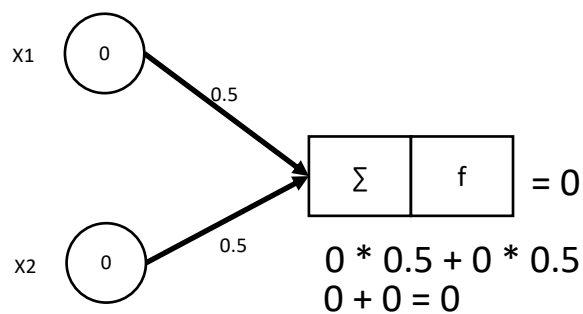
$\text{weight}(n + 1) = \text{weight}(n) + (\text{learning\_rate} * \text{input} * \text{error})$

$\text{weight}(n + 1) = 0.1 + (0.1 * 1 * 1)$

$\text{weight}(n + 1) = 0.2$



# "AND" OPERATOR



X1	X2	Class
0	0	0
0	1	0
1	0	0
1	1	1

error = correct - prediction

Class	Prediction	Error
0	0	0
0	0	0
0	0	0
1	1	0

100%

While error  $\neq 0$

- For each row

  - Calculate output

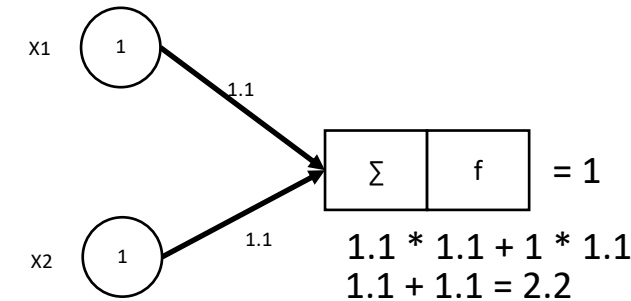
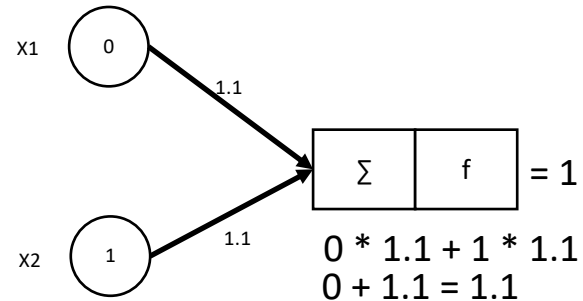
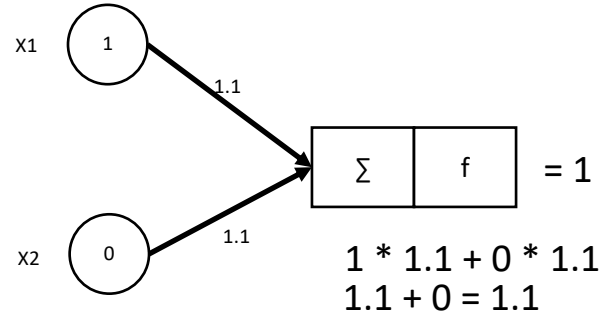
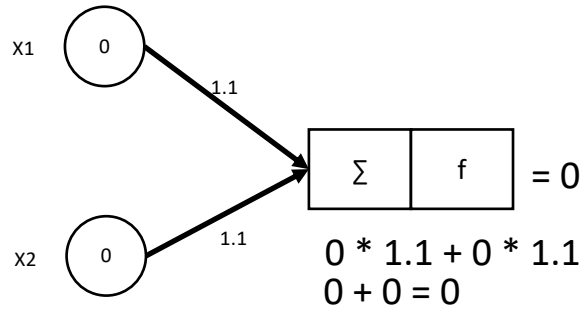
  - Calculate error (correct - prediction)

  - If error  $> 0$

    - For each weight

      - Update the weights

# "OR" OPERATOR



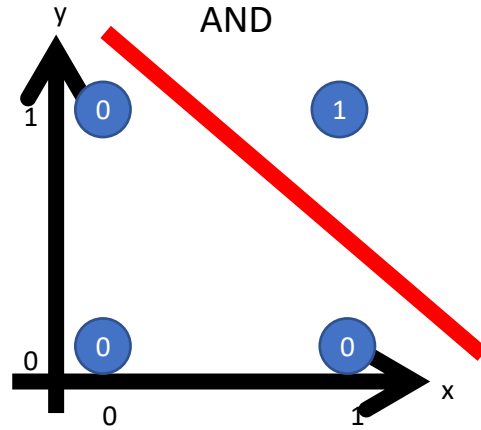
X1	X2	Class
0	0	0
0	1	1
1	0	1
1	1	1

error = correct - prediction

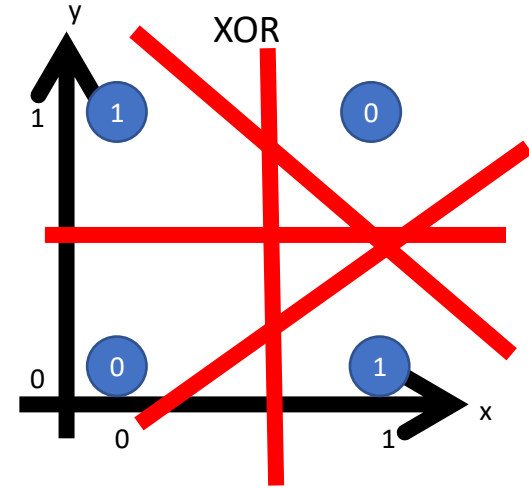
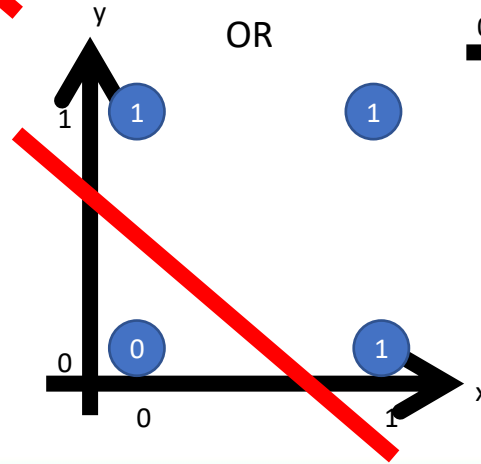
Class	Prediction	Error
0	0	0
1	1	0
1	1	0
1	1	0

100%

# "XOR" OPERATOR



Linearly separable



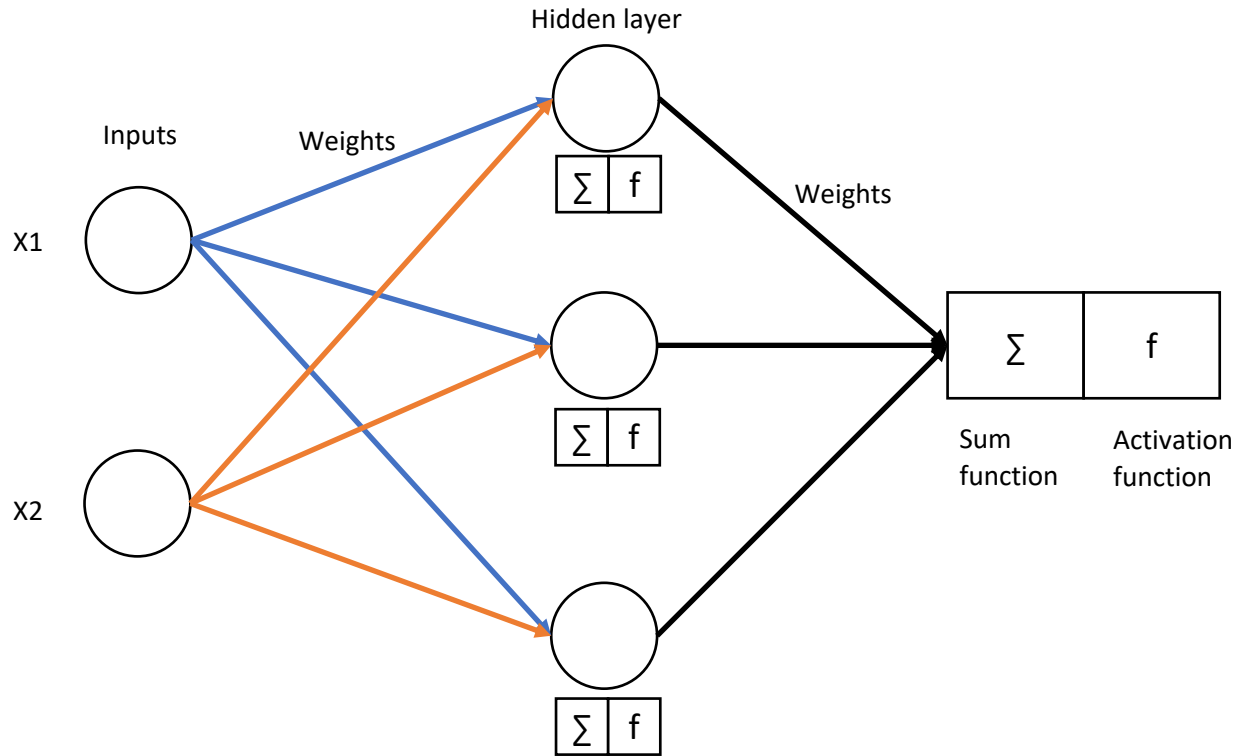
Non-linearly separable

# PLAN OF ATTACK – MULTI-LAYER PERCEPTRON

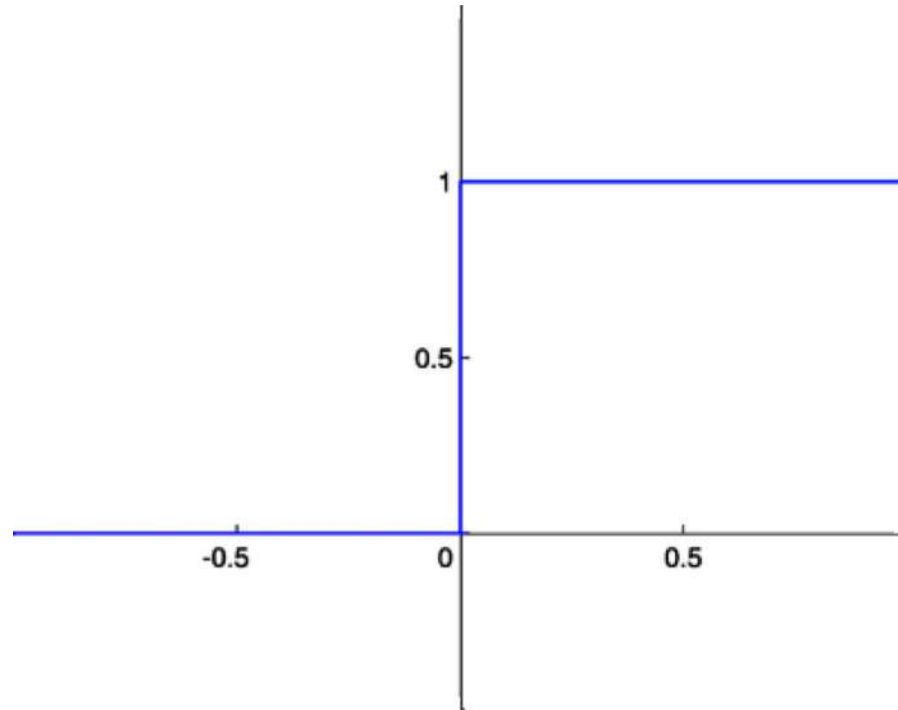
1. Single layer and multi-layer
2. Activation functions
3. Weight update (XOR operator)
4. Error functions
5. Gradient descent
6. Backpropagation
7. Implementation of a multi-layer perceptron from scratch using Python and Numpy



# MULTI-LAYER PERCEPTRON

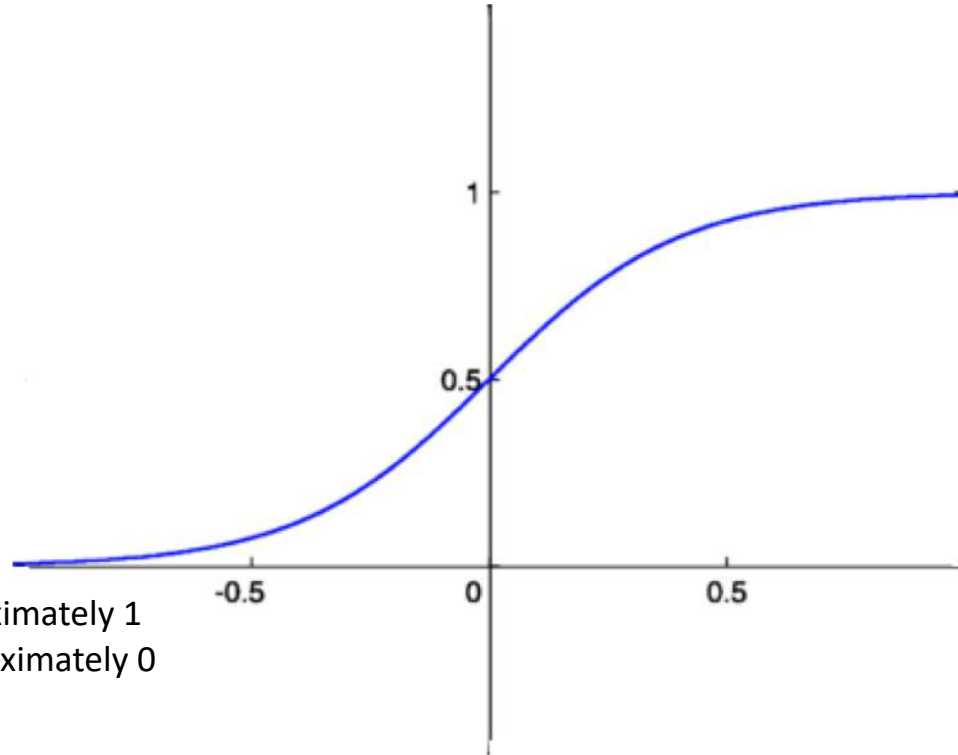


# STEP FUNCTION



# SIGMOID FUNCTION

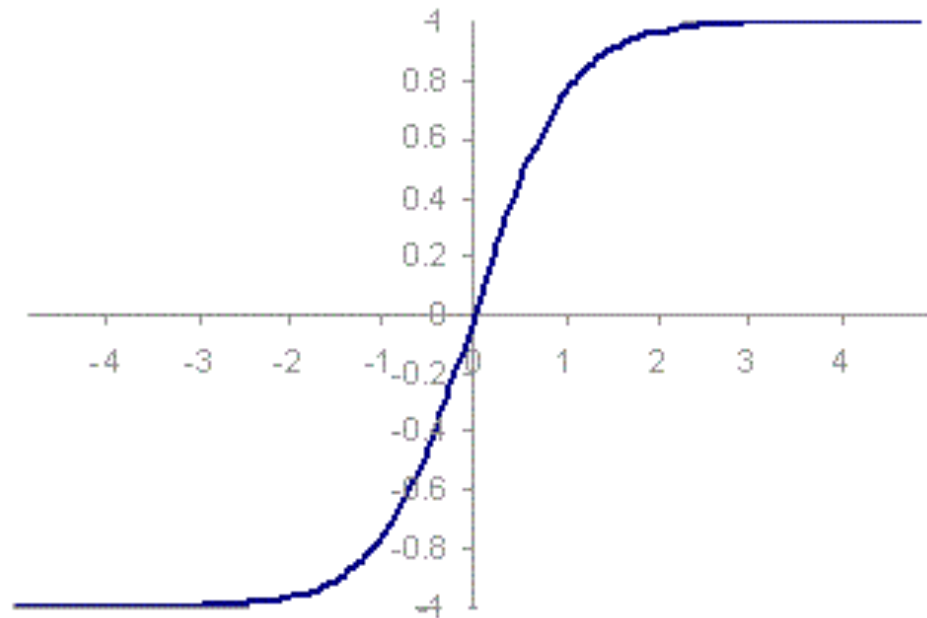
$$y = \frac{1}{1 + e^{-x}}$$



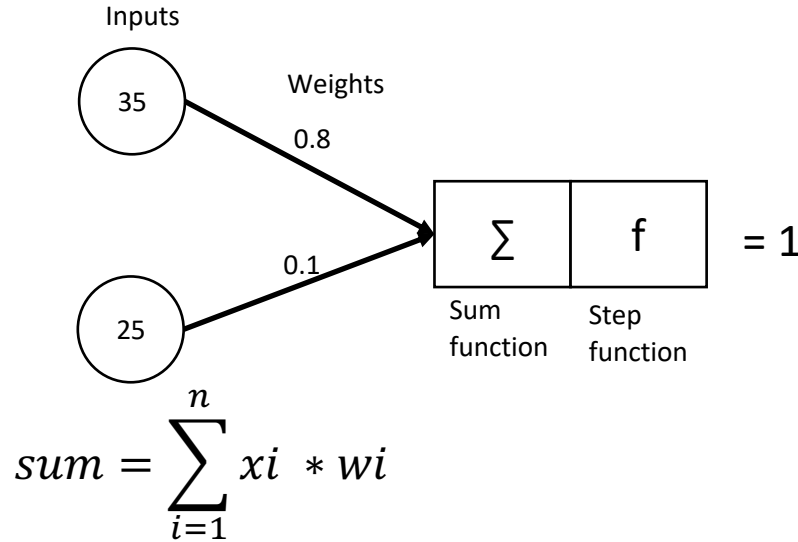
If X is high, the value is approximately 1  
If X is small, the value is approximately 0

# HYPERBOLIC TANGENT FUNCTION

$$Y = \frac{e^x - e^{-x}}{e^x + e^{-x}}$$



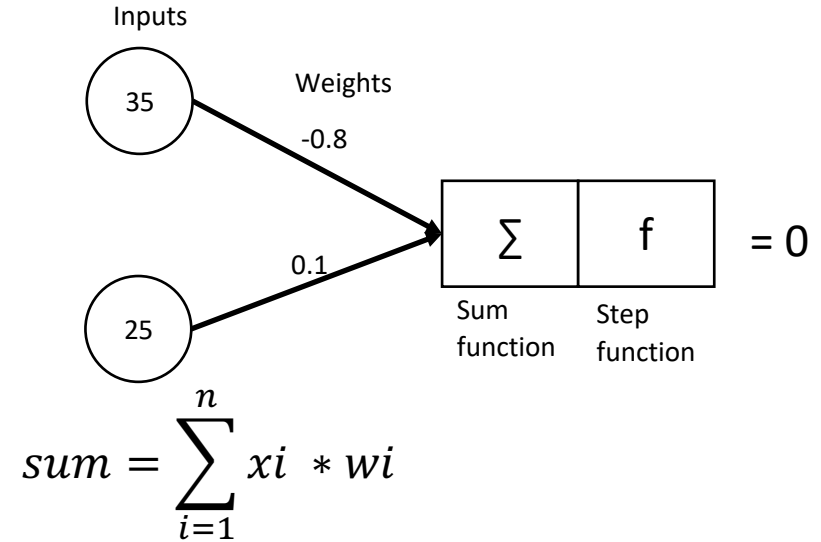
# STEP FUNCTION



$$sum = (35 * 0.8) + (25 * 0.1)$$

$$sum = 28 + 2.5$$

$$sum = 30.5$$



$$sum = (35 * -0.8) + (25 * 0.1)$$

$$sum = -28 + 2.5$$

$$sum = -25.5$$



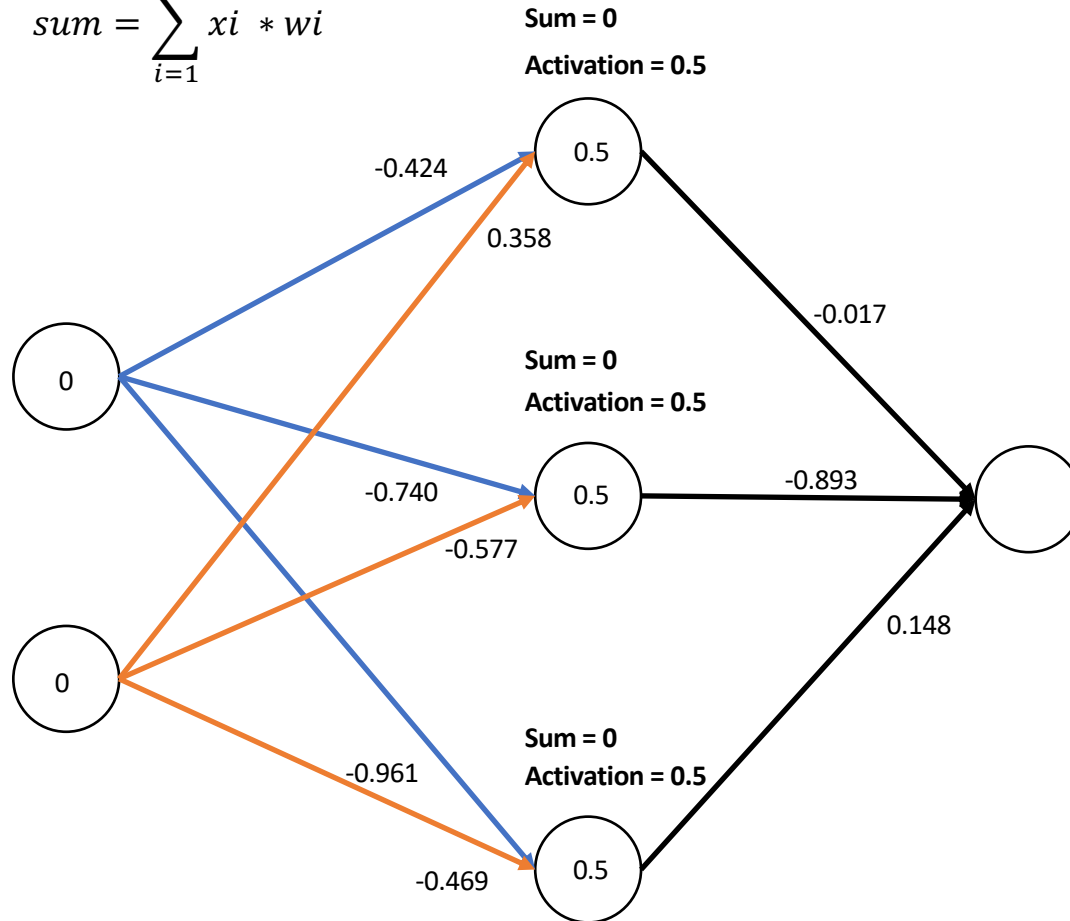
# "XOR" OPERATOR

X1	X2	Class
0	0	0
0	1	1
1	0	1
1	1	0

# INPUT LAYER TO HIDDEN LAYER



$$sum = \sum_{i=1}^n x_i * w_i$$



$$y = \frac{1}{1 + e^{-x}}$$

X1	X2	Class
0	0	0
0	1	1
1	0	1
1	1	0

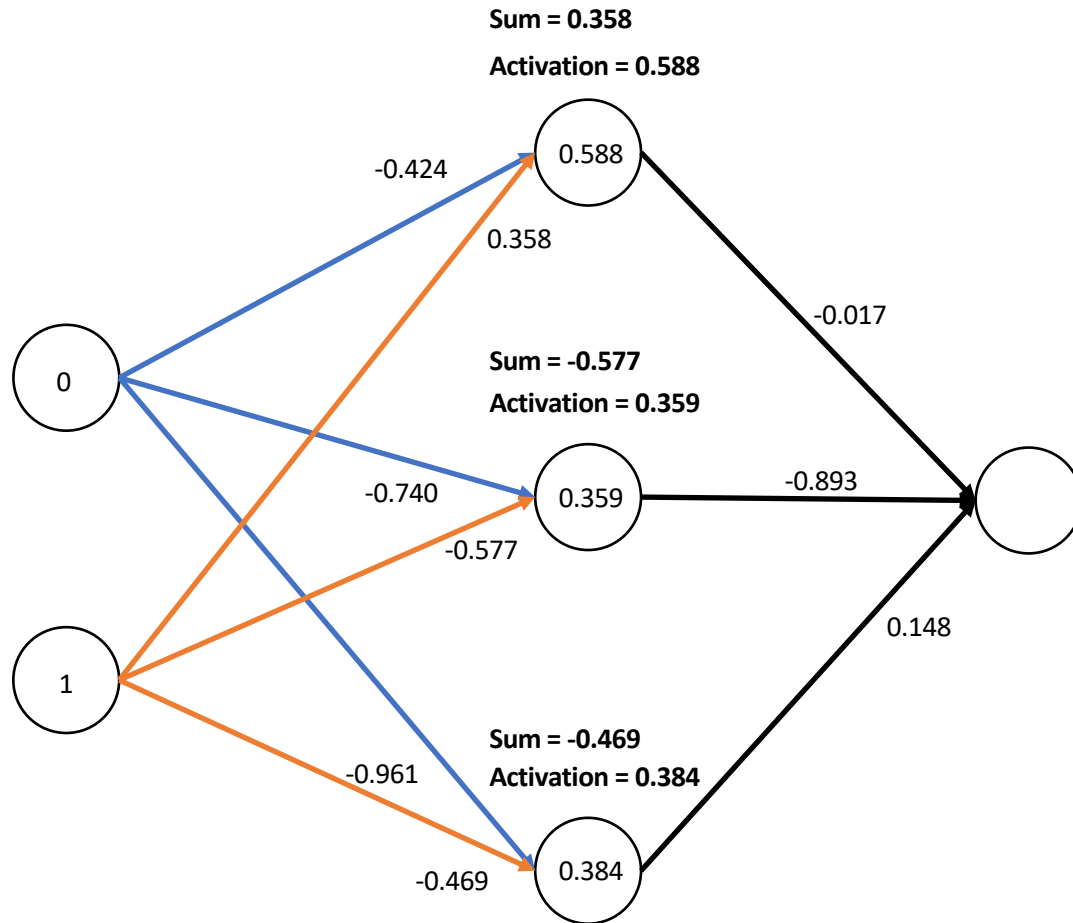
$$0 * (-0.424) + 0 * 0.358 = 0$$

$$0 * (-0.740) + 0 * (-0.577) = 0$$

$$0 * (-0.961) + 0 * (-0.469) = 0$$



# INPUT LAYER TO HIDDEN LAYER



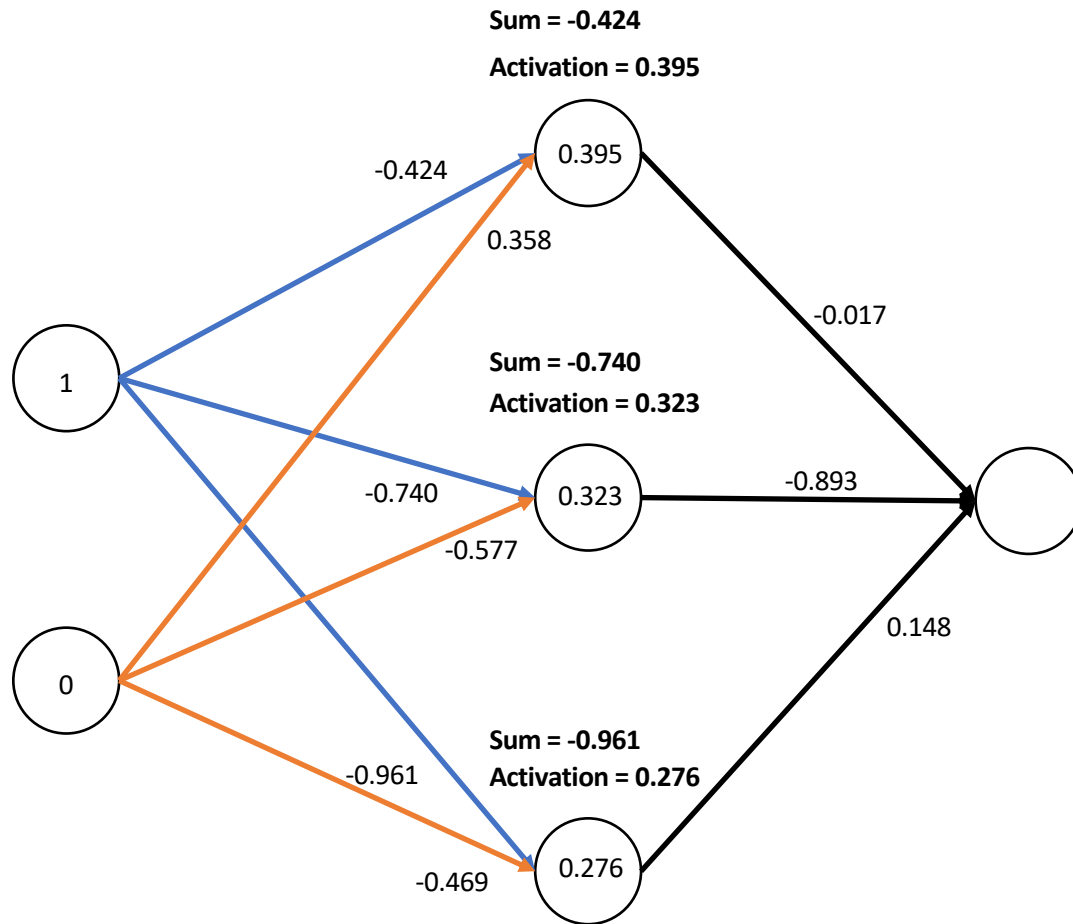
X1	X2	Class
0	0	0
0	1	1
1	0	1
1	1	0

$$0 * (-0.424) + 1 * 0.358 = 0.358$$

$$0 * (-0.740) + 1 * (-0.577) = -0.577$$

$$0 * (-0.961) + 1 * (-0.469) = -0.469$$

# INPUT LAYER TO HIDDEN LAYER



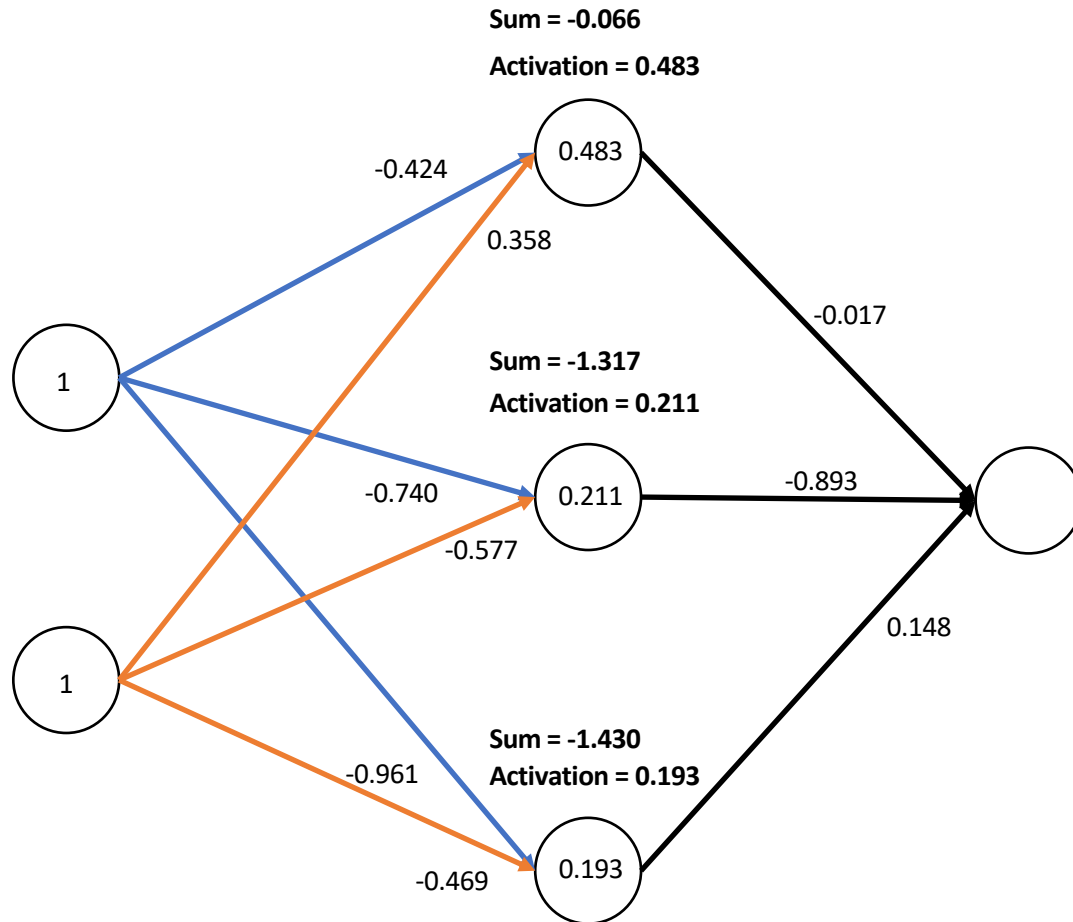
X1	X2	Class
0	0	0
0	1	1
1	0	1
1	1	0

$$1 * (-0.424) + 0 * 0.358 = -0.424$$

$$1 * (-0.740) + 0 * (-0.577) = -0.740$$

$$1 * (-0.961) + 0 * (-0.469) = -0.961$$

# INPUT LAYER TO HIDDEN LAYER



X1	X2	Class
0	0	0
0	1	1
1	0	1
1	1	0

$$1 * (-0.424) + 1 * 0.358 = -0.066$$

$$1 * (-0.740) + 1 * (-0.577) = -1.317$$

$$1 * (-0.961) + 1 * (-0.469) = -1.430$$

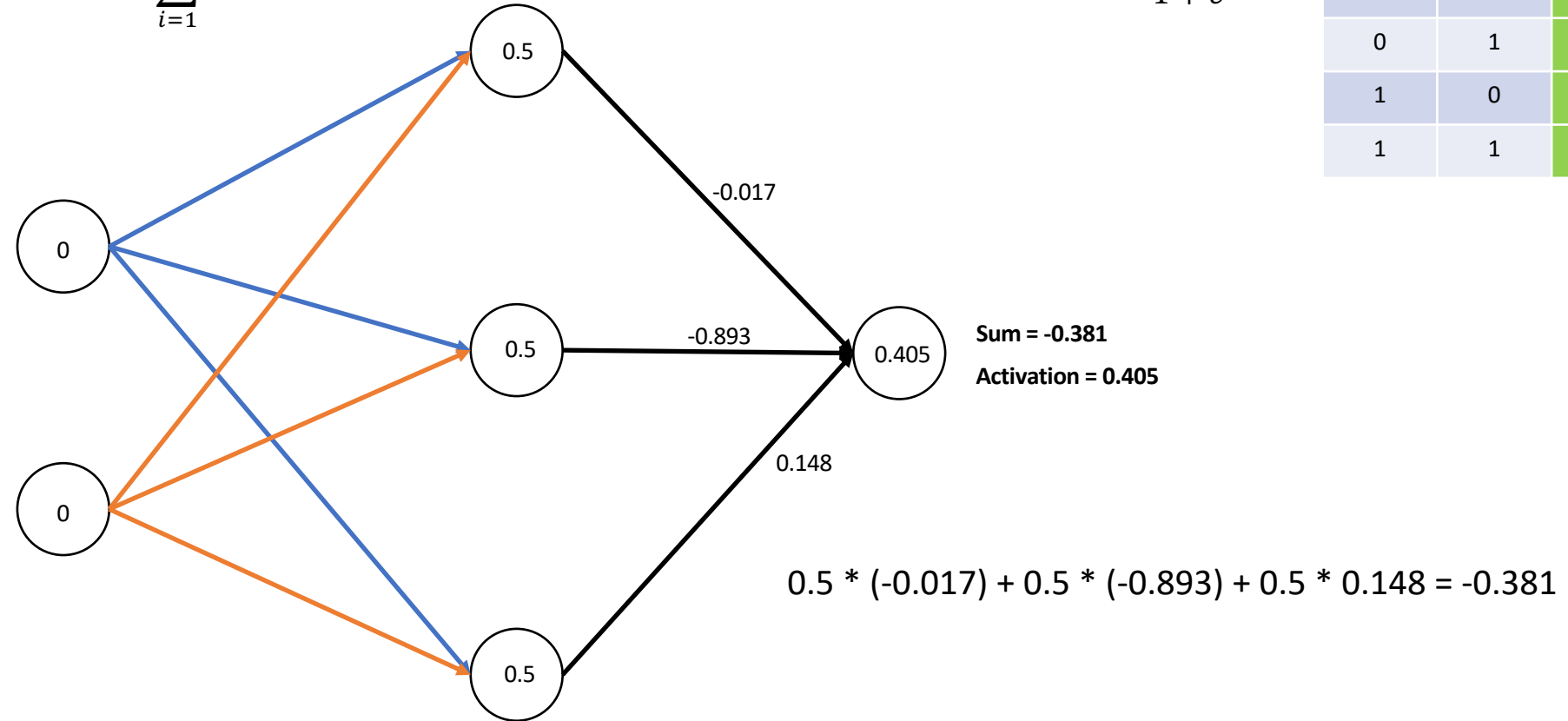
# HIDDEN LAYER TO OUTPUT LAYER



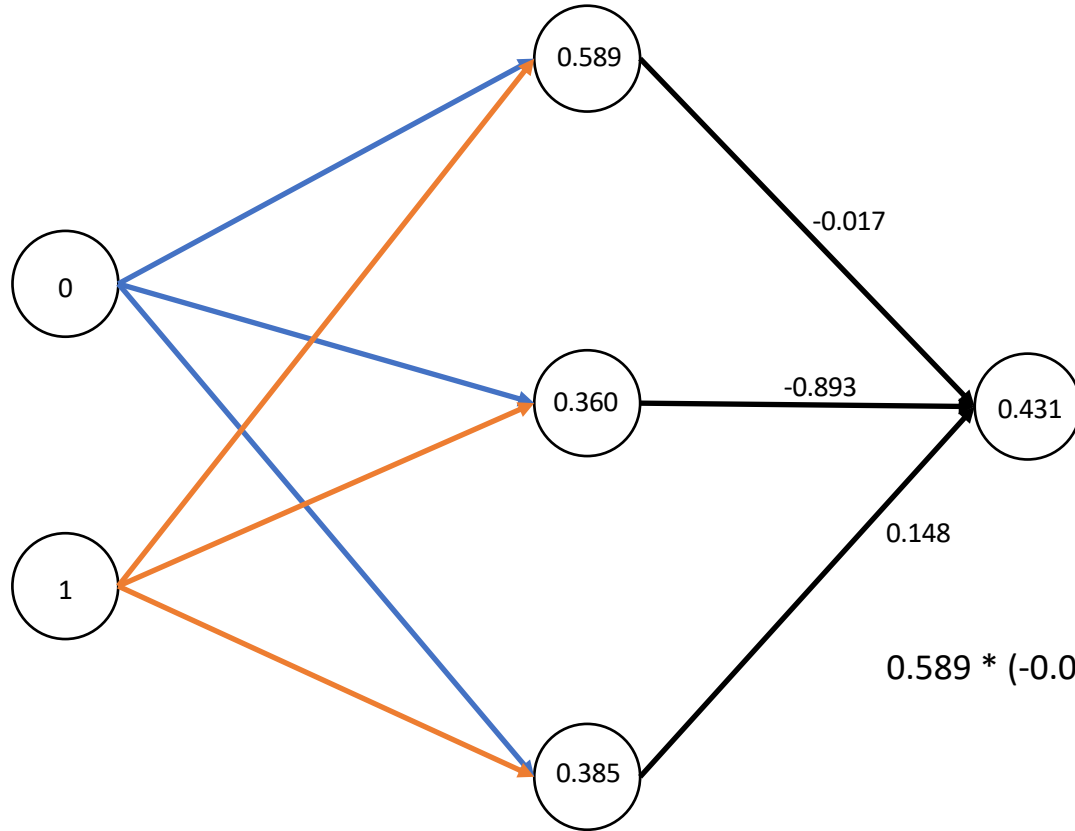
$$sum = \sum_{i=1}^n x_i * w_i$$

$$y = \frac{1}{1 + e^{-x}}$$

X1	X2	Class
0	0	0
0	1	1
1	0	1
1	1	0



# HIDDEN LAYER TO OUTPUT LAYER



**Sum = -0.274**

**Activation = 0.431**

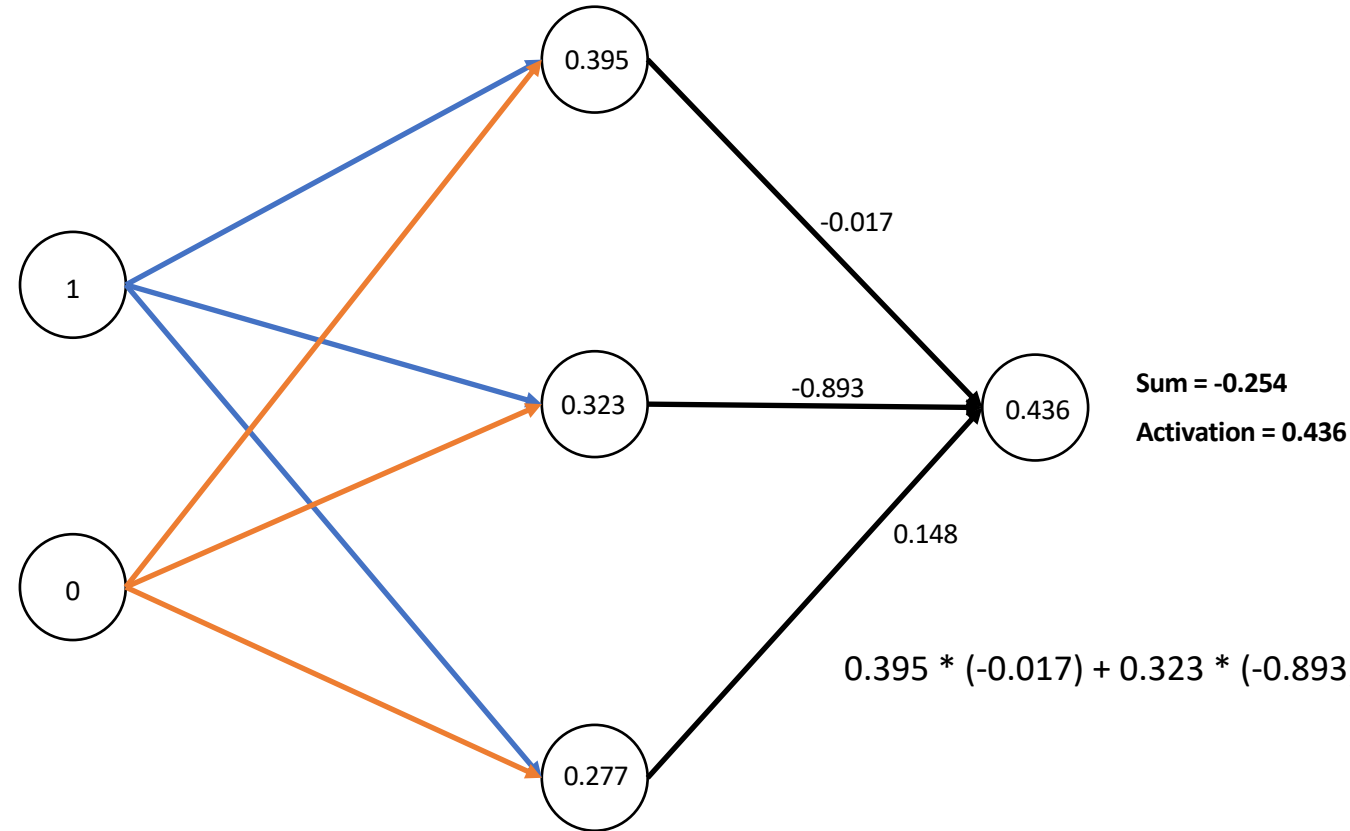
$$0.589 * (-0.017) + 0.360 * (-0.893) + 0.385 * 0.148 = -0.274$$

X1	X2	Class
0	0	0
0	1	1
1	0	1
1	1	0

# HIDDEN LAYER TO OUTPUT LAYER



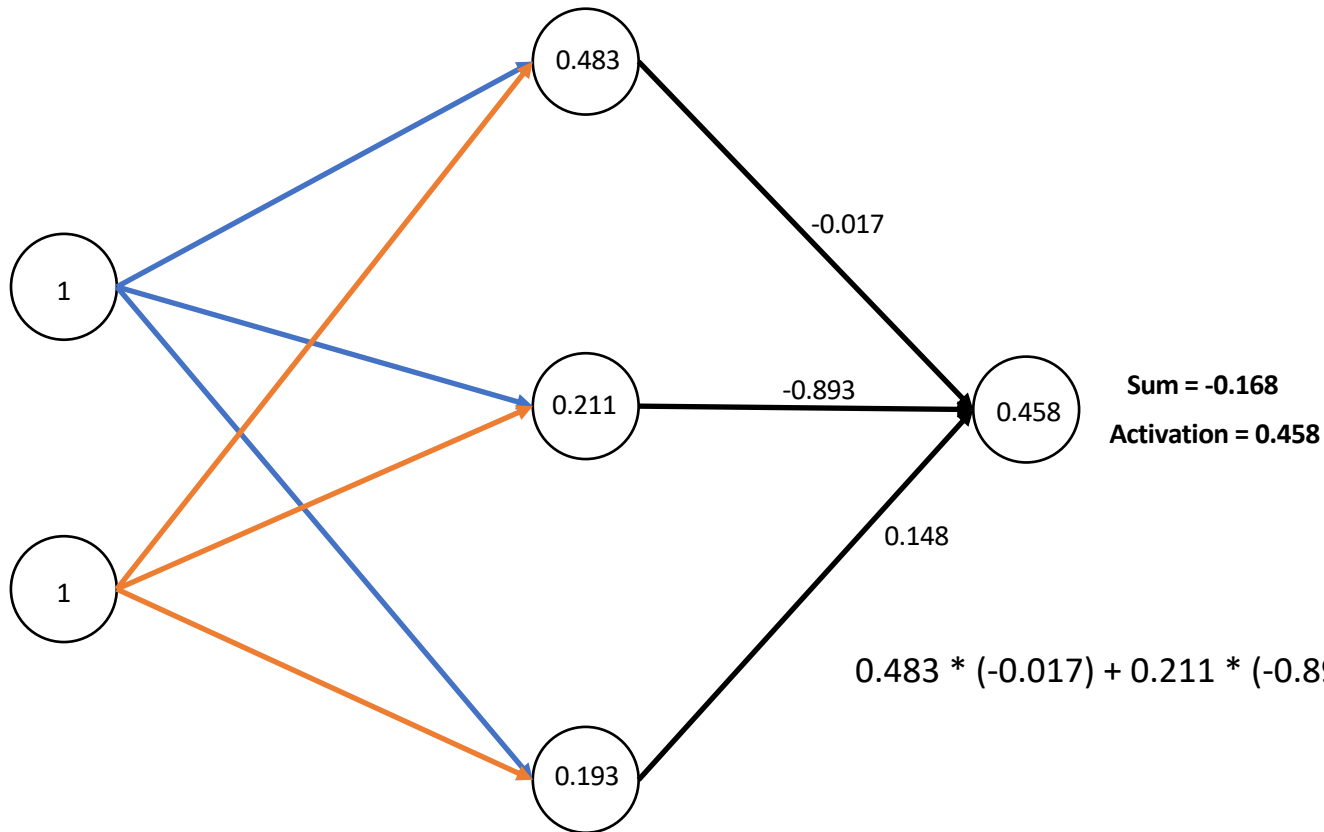
X1	X2	Class
0	0	0
0	1	1
1	0	1
1	1	0



# HIDDEN LAYER TO OUTPUT LAYER



X1	X2	Classe
0	0	0
0	1	1
1	0	1
1	1	0



$$0.483 * (-0.017) + 0.211 * (-0.893) + 0.193 * 0.148 = -0.168$$



# "XOR" OPERATOR – ERROR (LOSS FUNCTION)

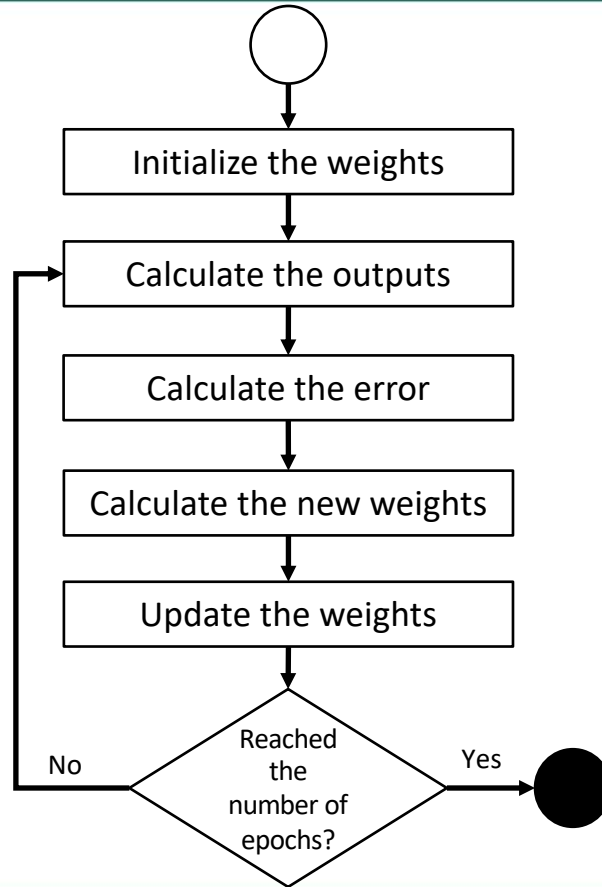
The simplest algorithm

error = correct – prediction

X1	X2	Class	Prediction	Error
0	0	0	0.405	-0.405
0	1	1	0.431	0.569
1	0	1	0.436	0.564
1	1	0	0.458	-0.458

Average = 0.499

# ALGORITHM



Cost function (loss function)

Gradient descent

Derivative

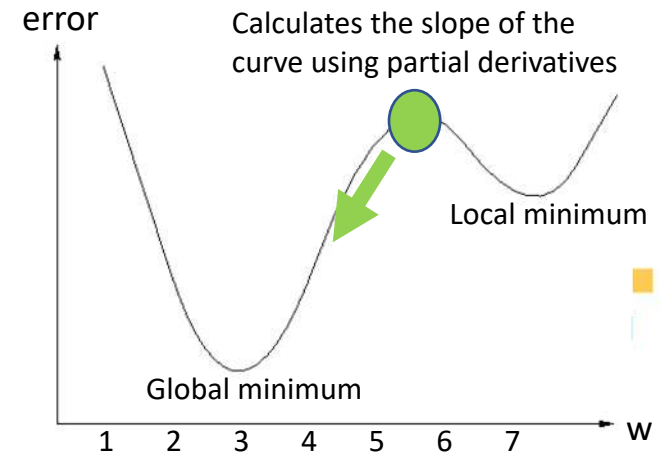
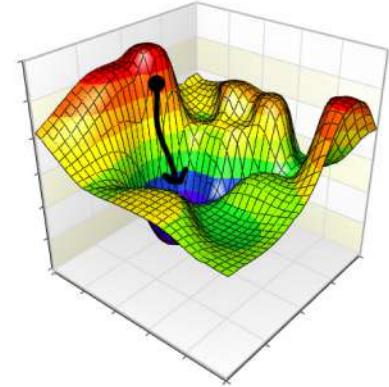
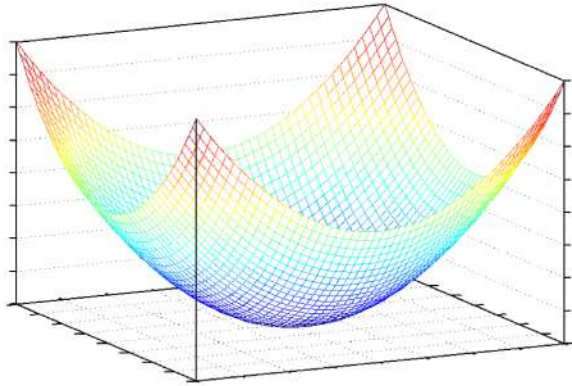
Delta

Backpropagation

# GRADIENT DESCENT

$$\min C(w_1, w_2 \dots w_n)$$

Calculate the partial derivative to move to the gradient direction



# GRADIENT DESCENT (DERIVATIVE)

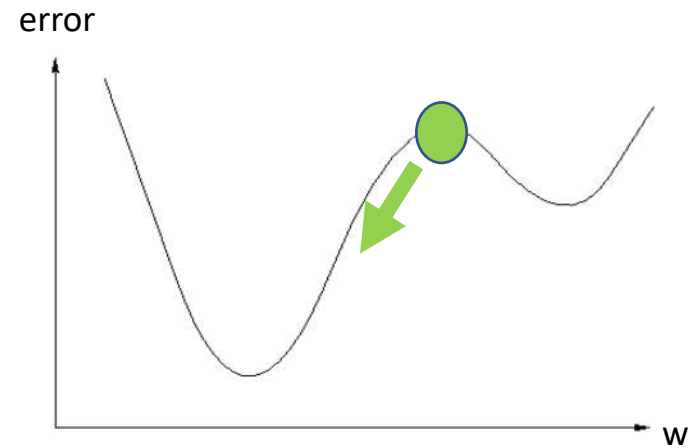
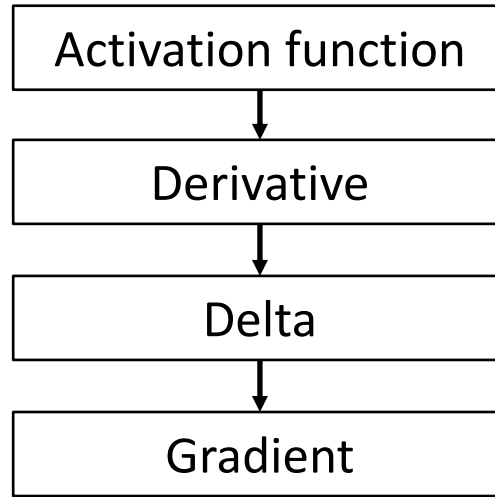
$$y = \frac{1}{1 + e^{-x}}$$



$$d = y * (1 - y)$$

$$d = 0.1 * (1 - 0.1)$$

# DELTA PARAMETER

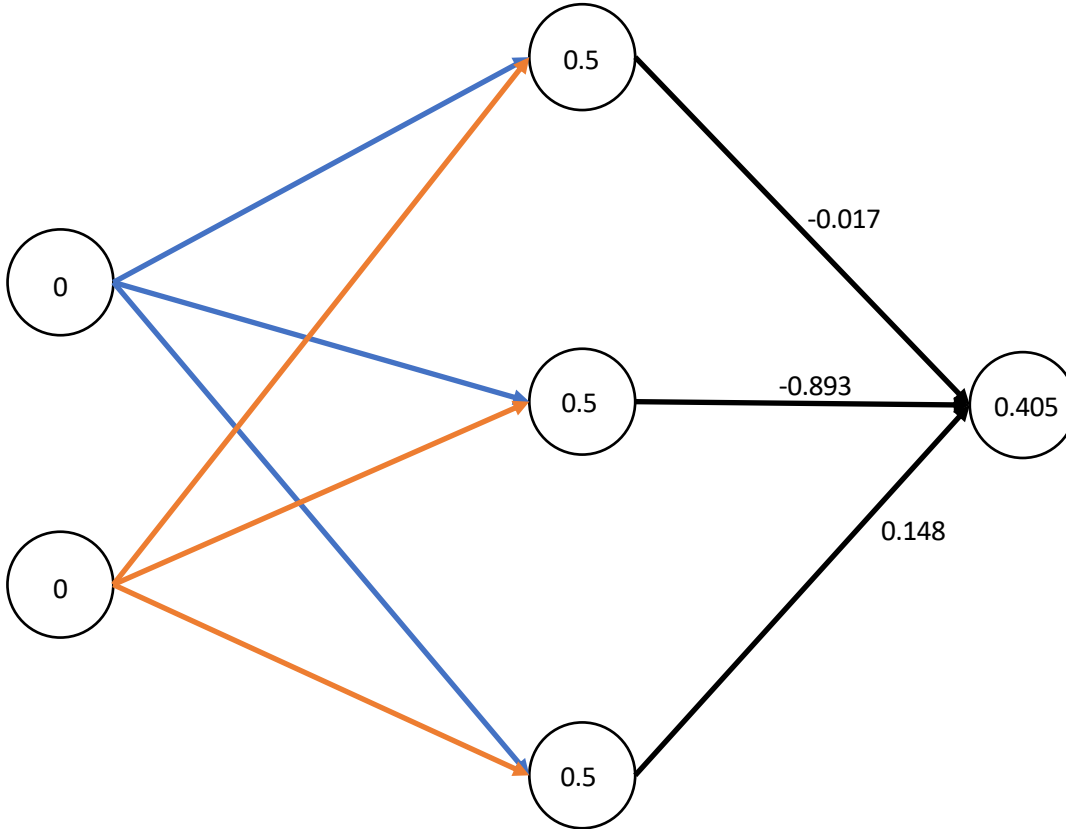


# OUTPUT LAYER – DELTA



$$\text{delta}_{\text{output}} = \text{error} * \text{sigmoid}_{\text{derivative}}$$

X1	X2	Class
0	0	0
0	1	1
1	0	1
1	1	0



Sum = -0.381

Activation = 0.405

Error = 0 - 0.405 = -0.405

Derivative activation (sigmoid) = 0.241

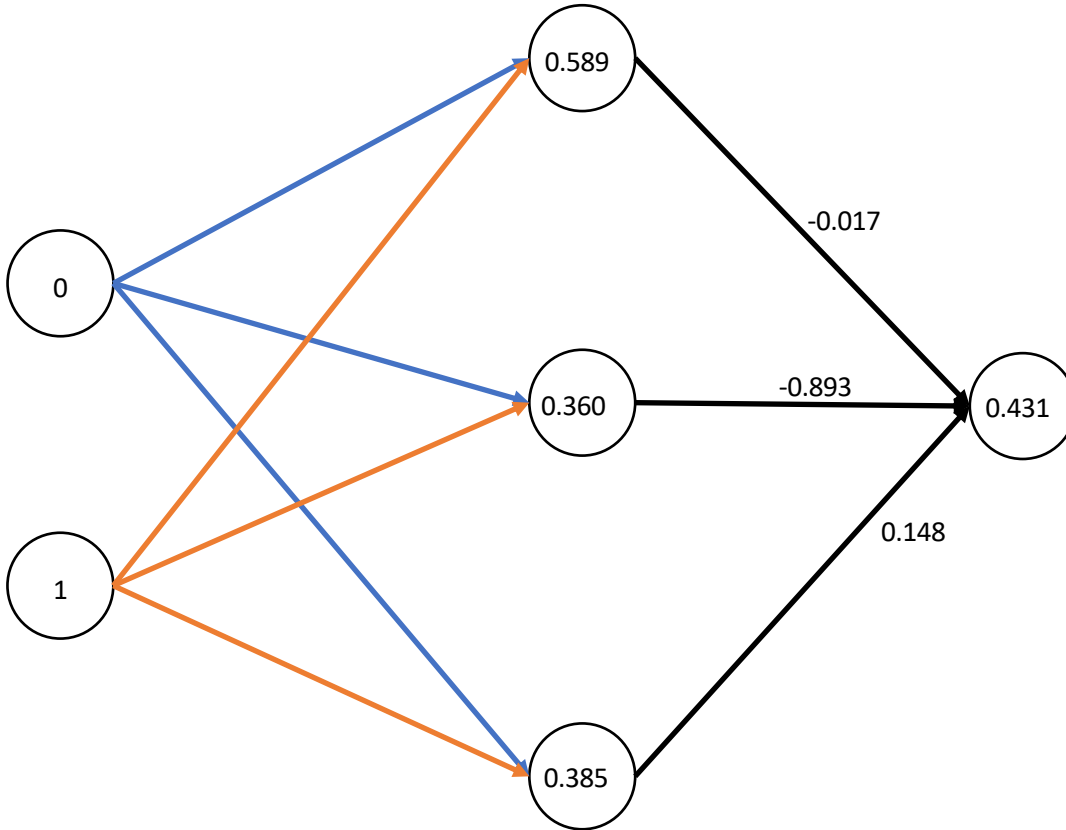
Delta (output) = -0.405 \* 0.241 = -0.097

# OUTPUT LAYER – DELTA



$$\delta_{output} = error * sigmoid_{derivative}$$

X1	X2	Class
0	0	0
0	1	1
1	0	1
1	1	0



**Sum = -0.274**

**Activation = 0.431**

**Error = 1 - 0.431 = 0.569**

**Derivative activation (sigmoid) = 0.245**

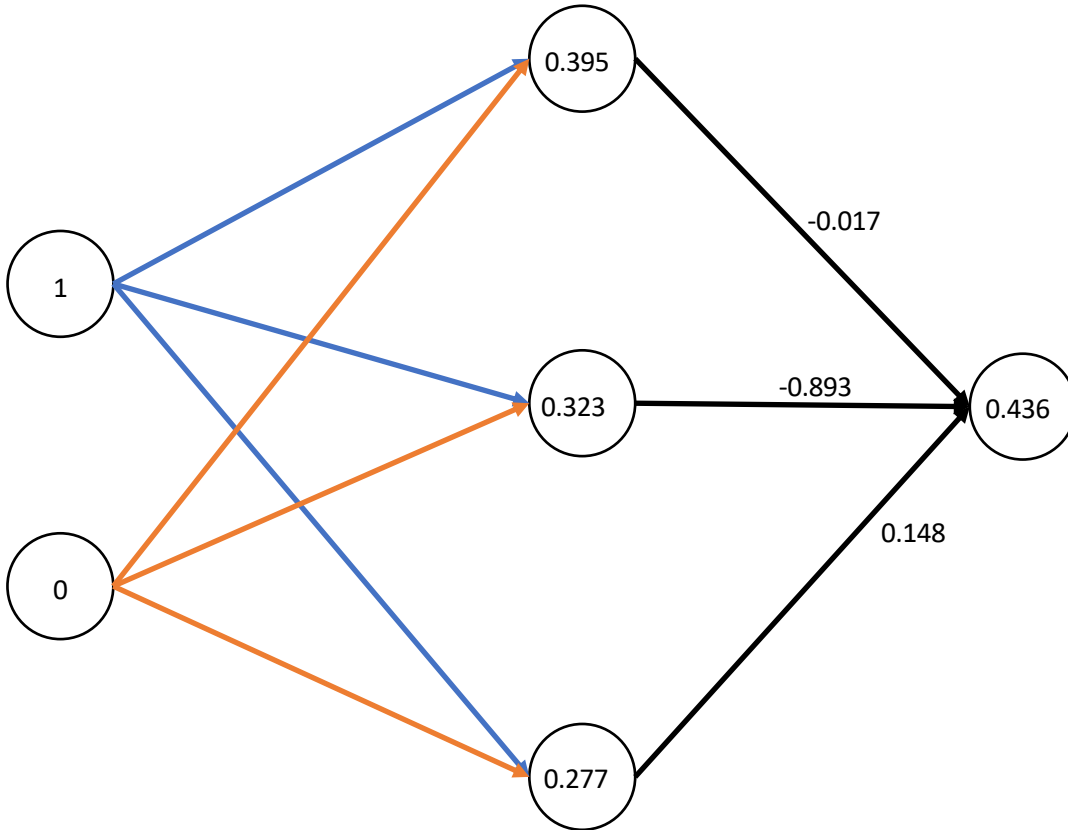
**Delta (output) = 0.569 \* 0.245 = 0.139**

# OUTPUT LAYER – DELTA



$$\text{delta}_{\text{output}} = \text{error} * \text{sigmoid}_{\text{derivative}}$$

X1	X2	Class
0	0	0
0	1	1
1	0	1
1	1	0



Sum = -0.254

Activation = 0.436

Error =  $1 - 0.436 = 0.564$

Derivative activation (sigmoid) = 0.246

Delta (output) =  $0.564 * 0.246 = 0.138$

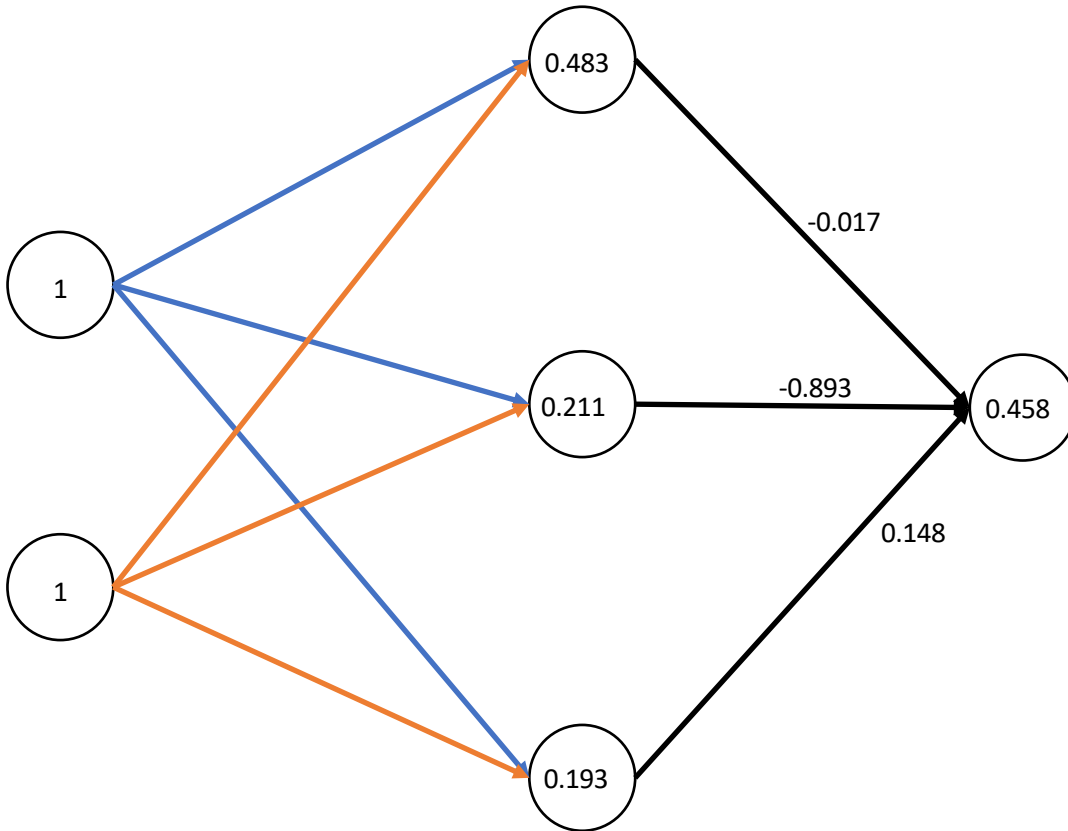


# OUTPUT LAYER – DELTA



$$\text{delta}_{\text{output}} = \text{error} * \text{sigmoid}_{\text{derivative}}$$

X1	X2	Class
0	0	0
0	1	1
1	0	1
1	1	0



Sum = -0.168

Activation = 0.458

Error = 0 - 0.458 = -0.458

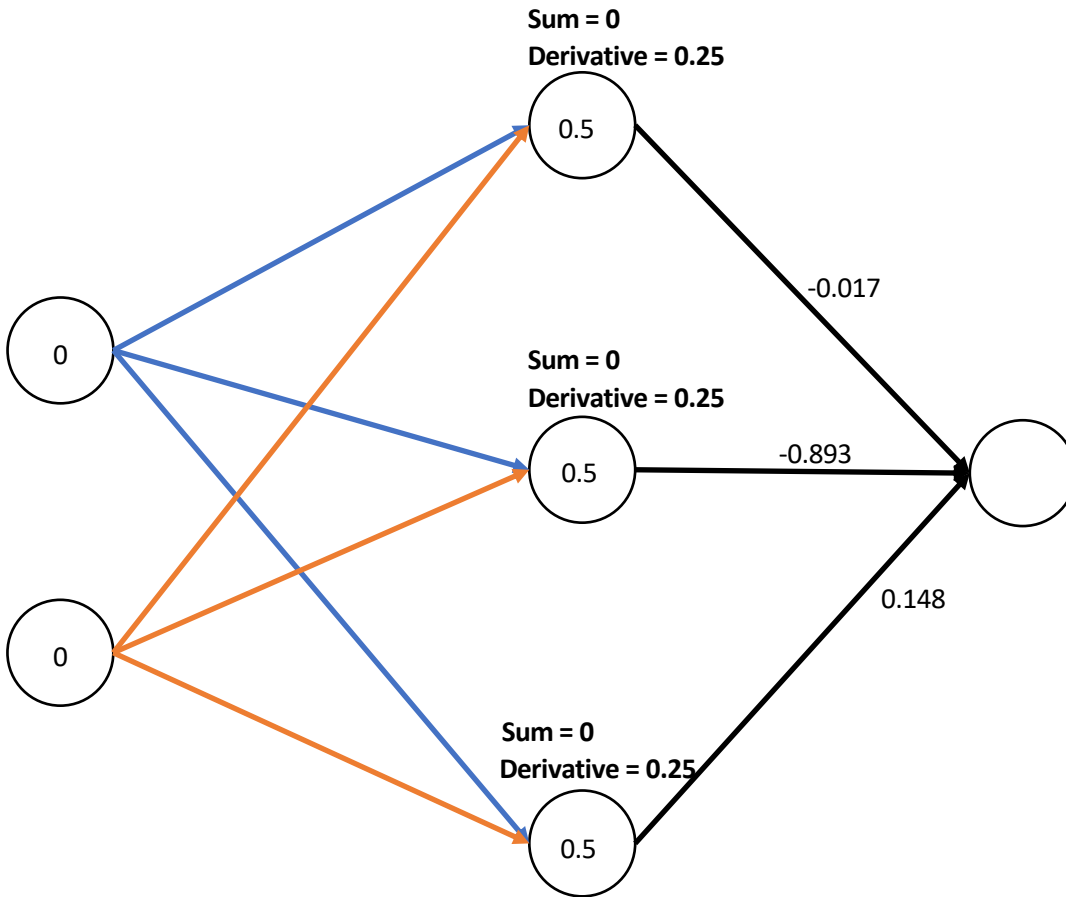
Derivative activation (sigmoid) = 0.248

Delta (output) = -0.458 \* 0.248 = -0.113

# HIDDEN LAYER – DELTA



$$\delta_{hidden} = \text{sigmoid}_{derivative} * \text{weight} * \delta_{output}$$



X1	X2	Class
0	0	0
0	1	1
1	0	1
1	1	0

Delta (output) = -0.097

$$0.25 * (-0.017) * (-0.097) = 0.000$$

$$0.25 * (-0.893) * (-0.097) = 0.021$$

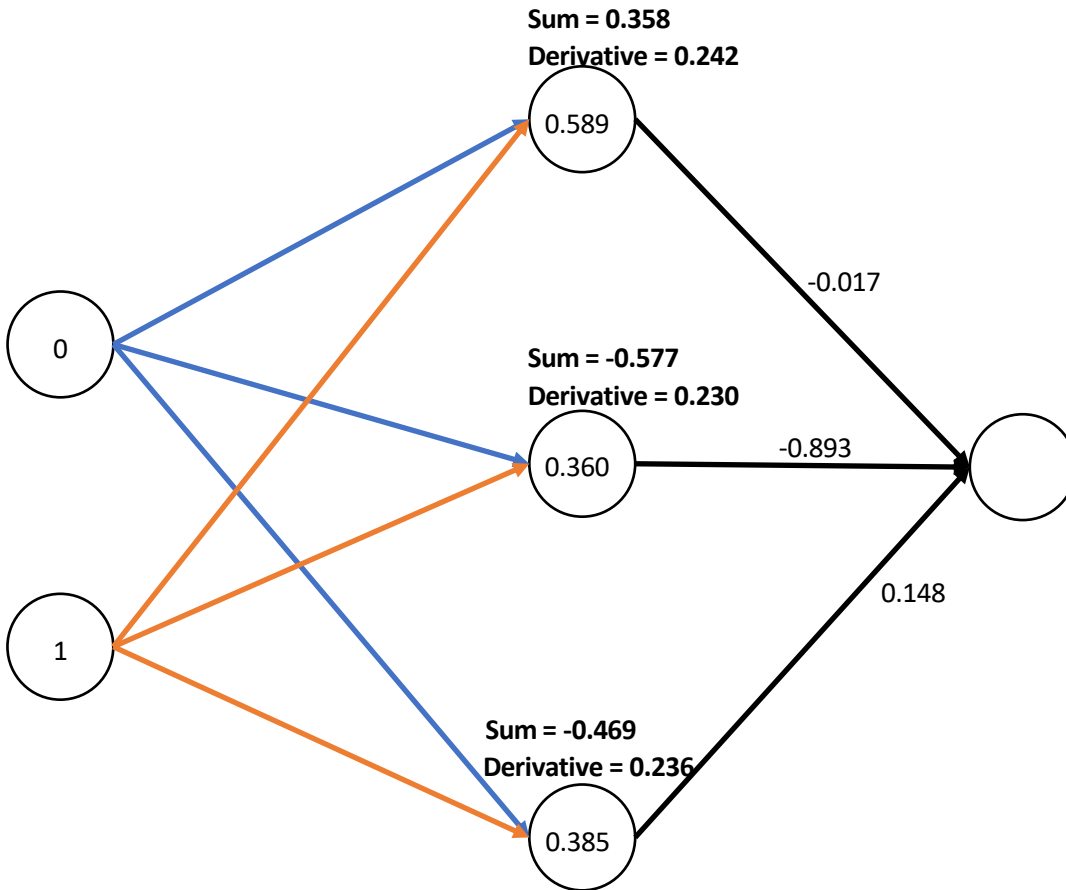
$$0.25 * 0.148 * (-0.097) = -0.003$$

# HIDDEN LAYER – DELTA



$$\delta_{hidden} = \text{sigmoid}_{derivative} * \text{weight} * \delta_{output}$$

X1	X2	Class
0	0	0
0	1	1
1	0	1
1	1	0



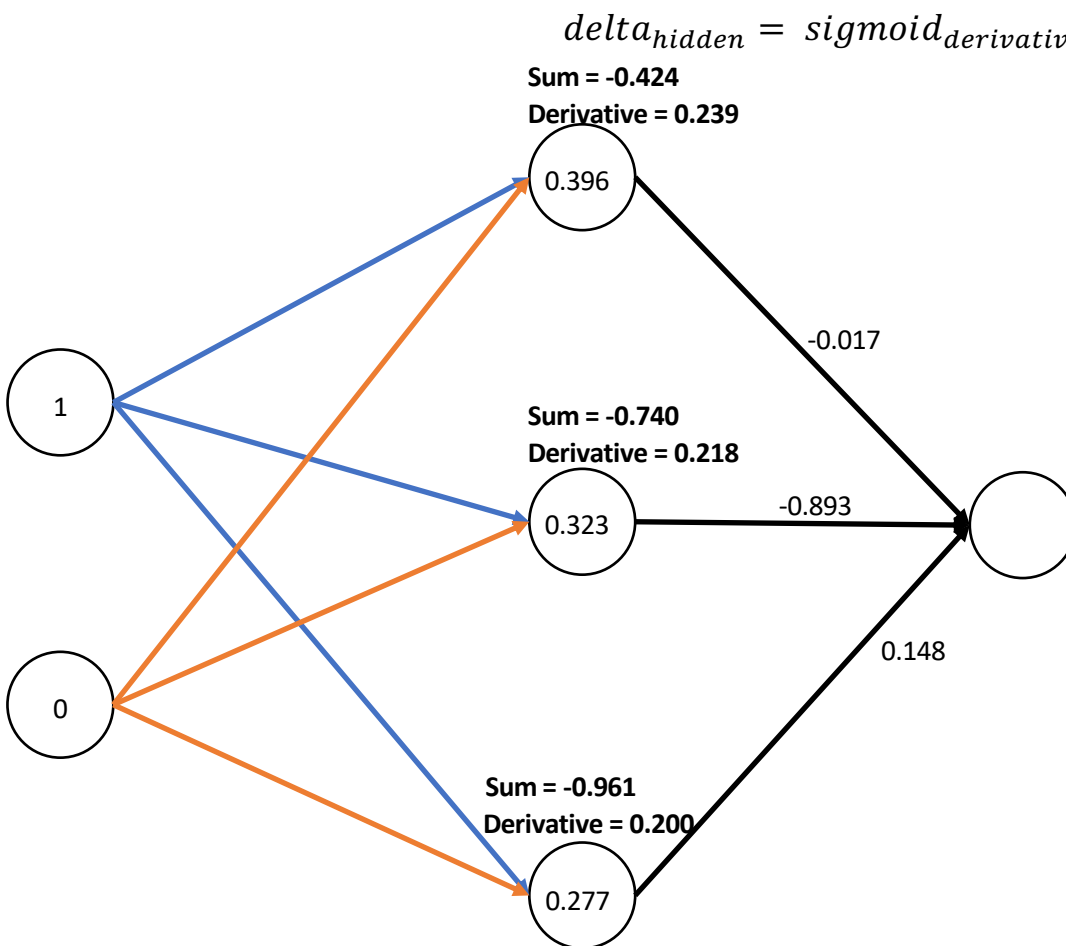
Delta (output) = 0.139

$$0.242 * (-0.017) * 0.139 = -0.000$$

$$0.230 * (-0.893) * 0.139 = -0.028$$

$$0.236 * 0.148 * 0.139 = 0.004$$

# HIDDEN LAYER – DELTA



X1	X2	Class
0	0	0
0	1	1
1	0	1
1	1	0

Delta (output) = 0.138

$$0.239 * (-0.017) * 0.138 = -0.000$$

$$0.218 * (-0.893) * 0.138 = -0.026$$

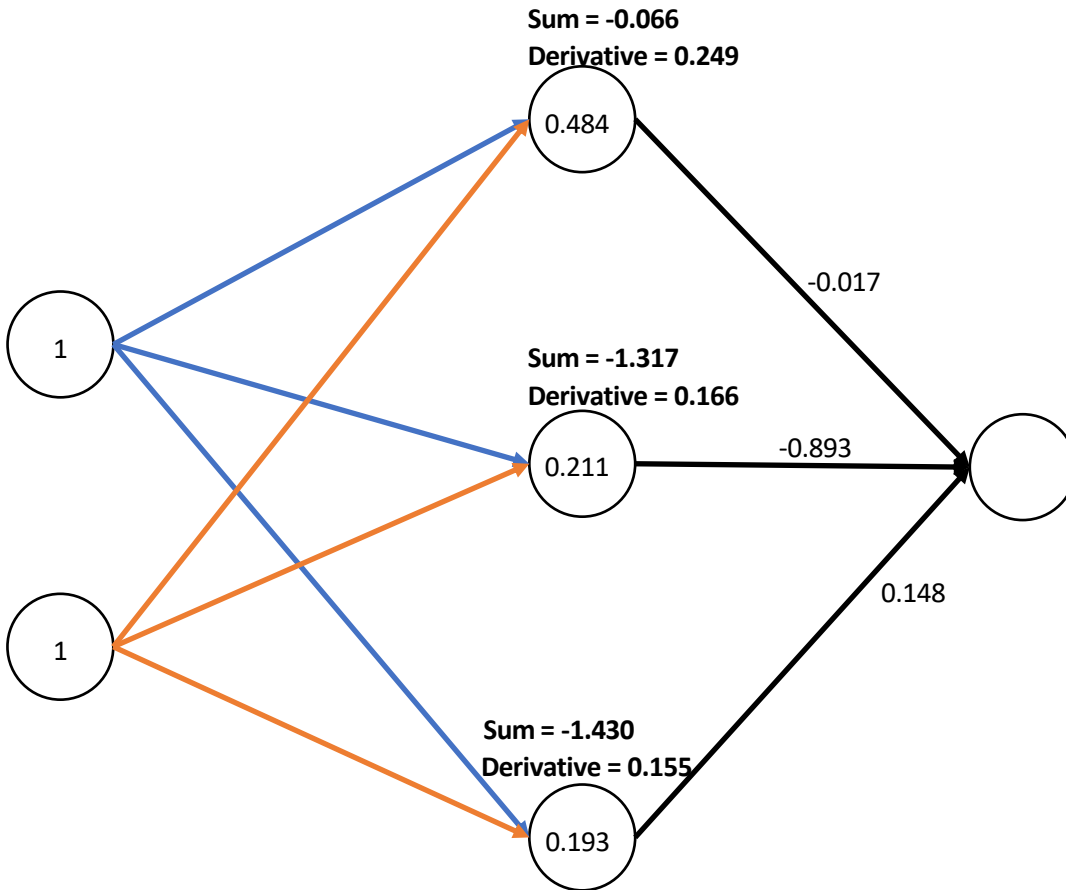
$$0.200 * 0.148 * 0.138 = 0.004$$

# HIDDEN LAYER – DELTA



$$\delta_{hidden} = \text{sigmoid}_{derivative} * \text{weight} * \delta_{output}$$

X1	X2	Class
0	0	0
0	1	1
1	0	1
1	1	0



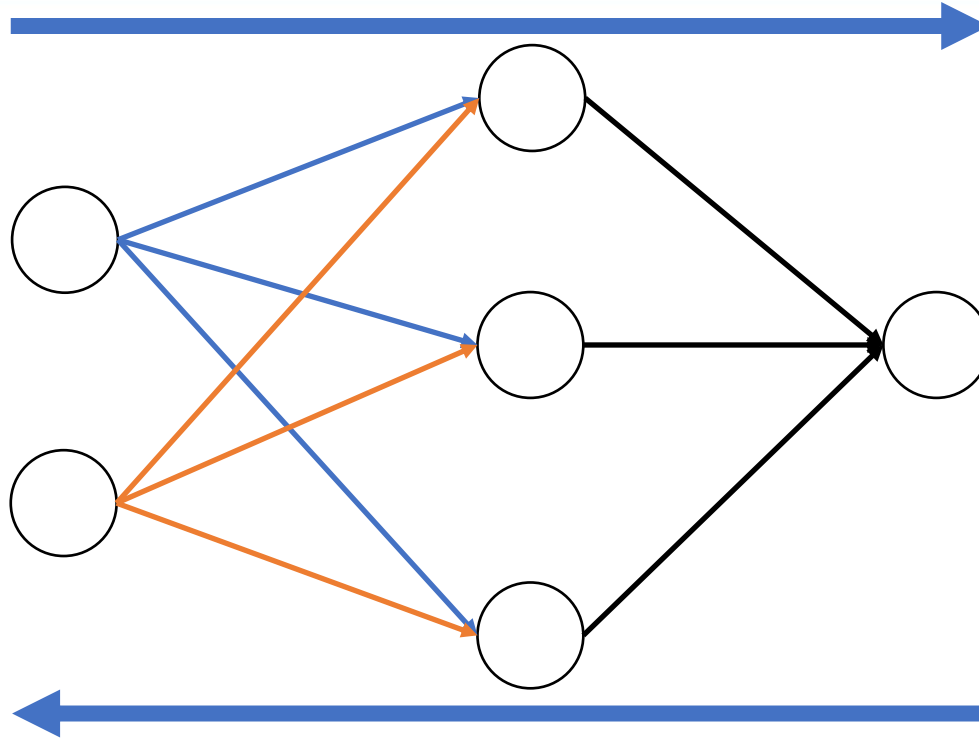
Delta (output) = -0.113

$$0.249 * (-0.017) * (-0.113) = 0.000$$

$$0.166 * (-0.893) * (-0.113) = 0.016$$

$$0.155 * 0.148 * (-0.113) = -0.002$$

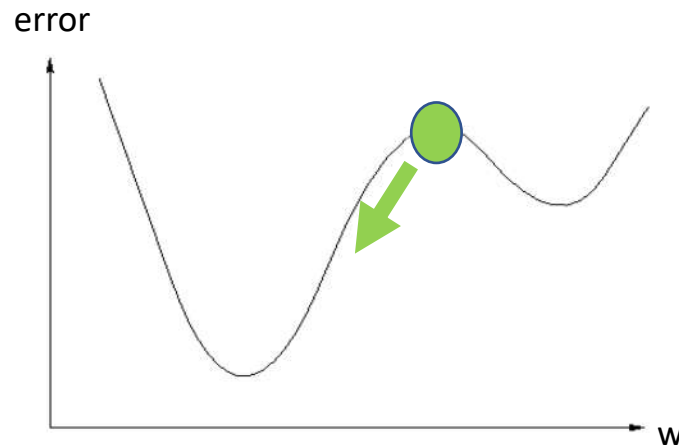
# WEIGHT UPDATE



$$weight_{n+1} = weight_n + (input * delta * learning\_rate)$$

# LEARNING RATE

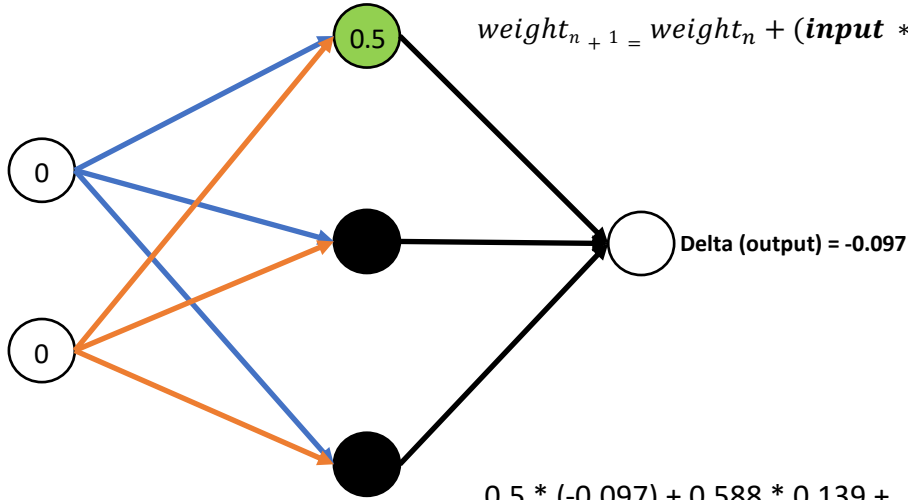
- Defines how fast the algorithm will learn
- High: the convergence is fast but may lose the global minimum
- Low: the convergence will be slower but more likely to reach the global minimum



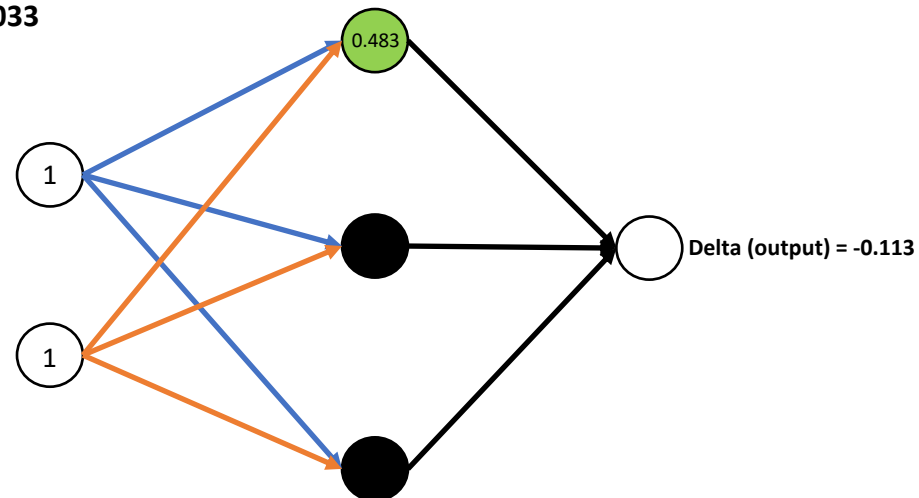
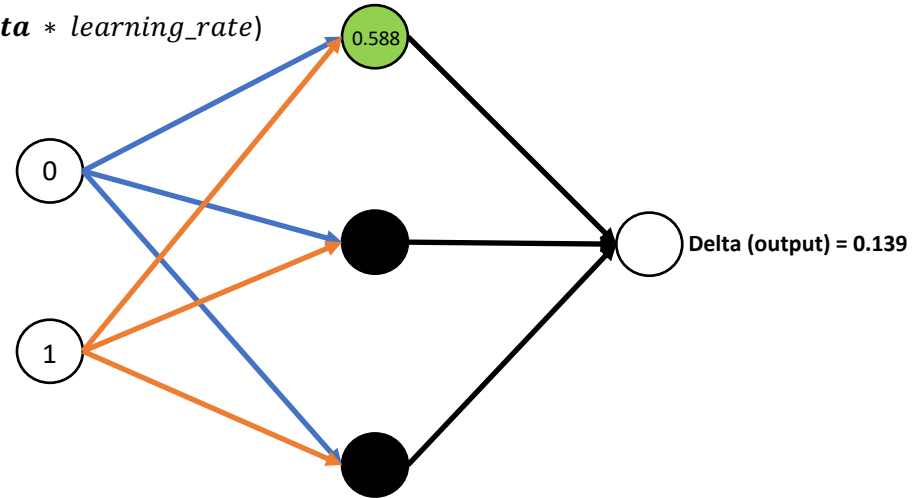
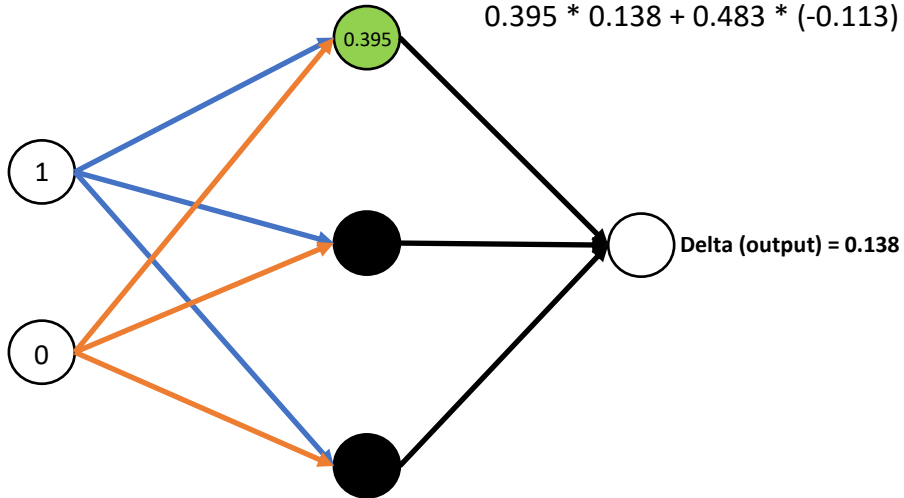
# WEIGHT UPDATE – OUTPUT LAYER TO HIDDEN LAYER



$$weight_{n+1} = weight_n + (input * delta * learning\_rate)$$



$$0.5 * (-0.097) + 0.588 * 0.139 + 0.395 * 0.138 + 0.483 * (-0.113) = 0.033$$

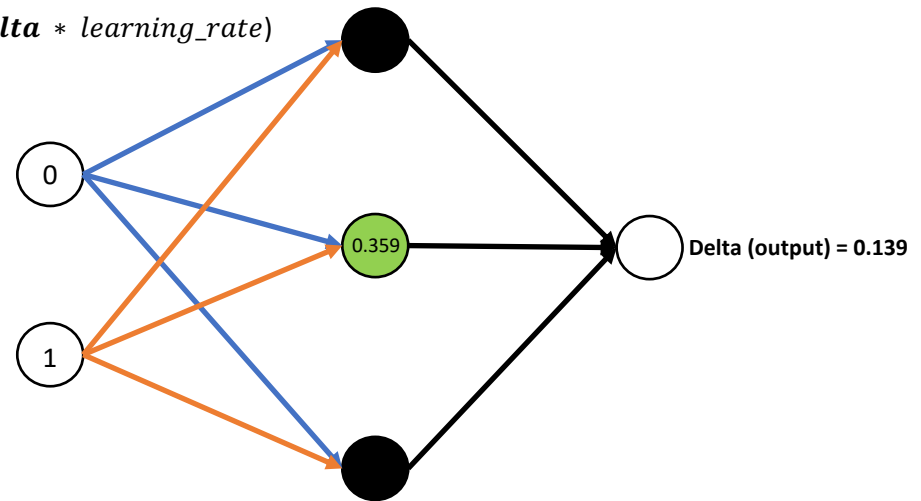
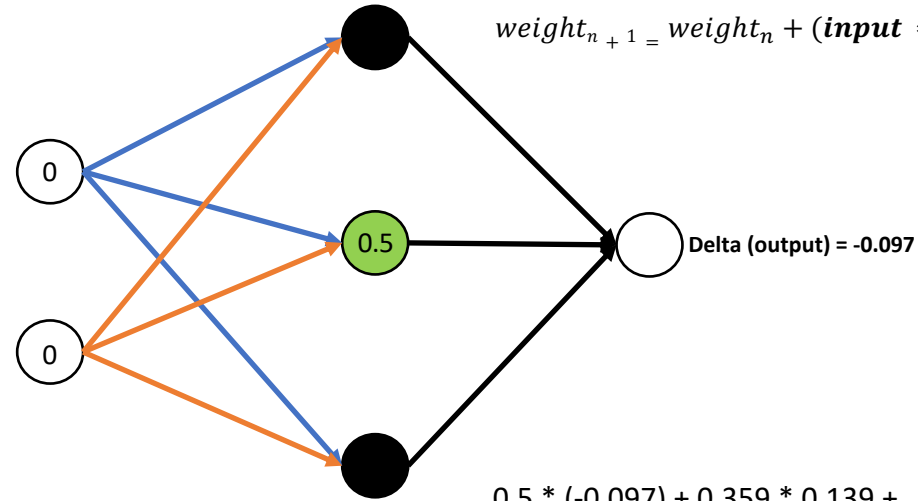




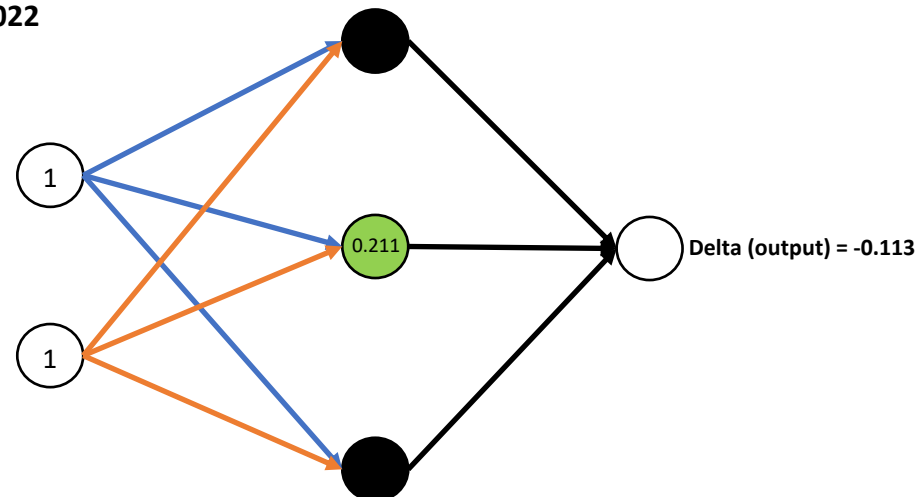
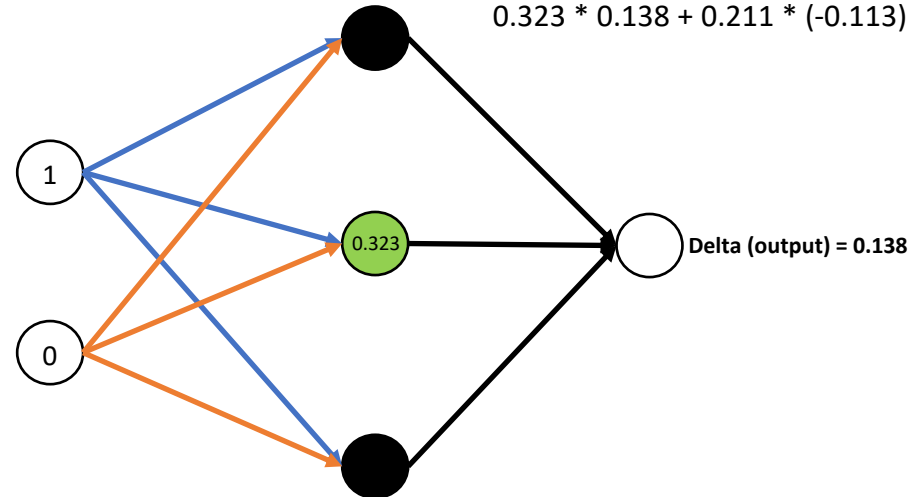
# WEIGHT UPDATE – OUTPUT LAYER TO HIDDEN LAYER



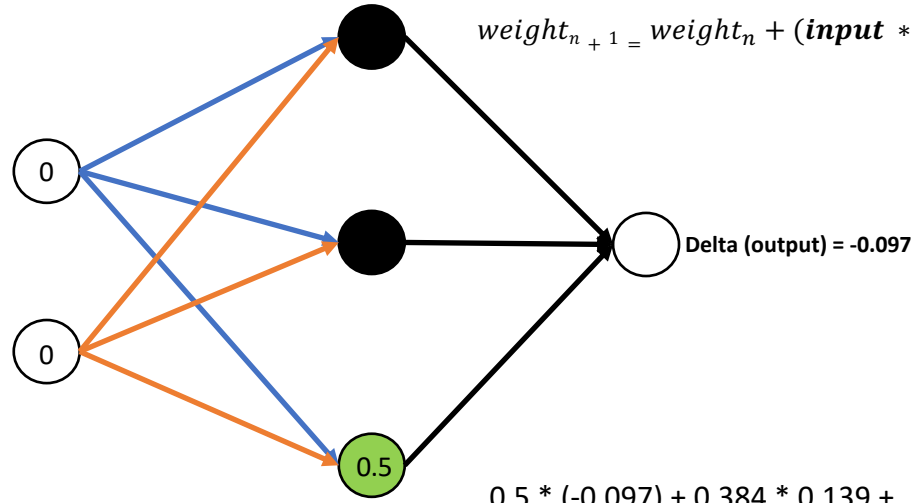
$$weight_{n+1} = weight_n + (input * delta * learning\_rate)$$



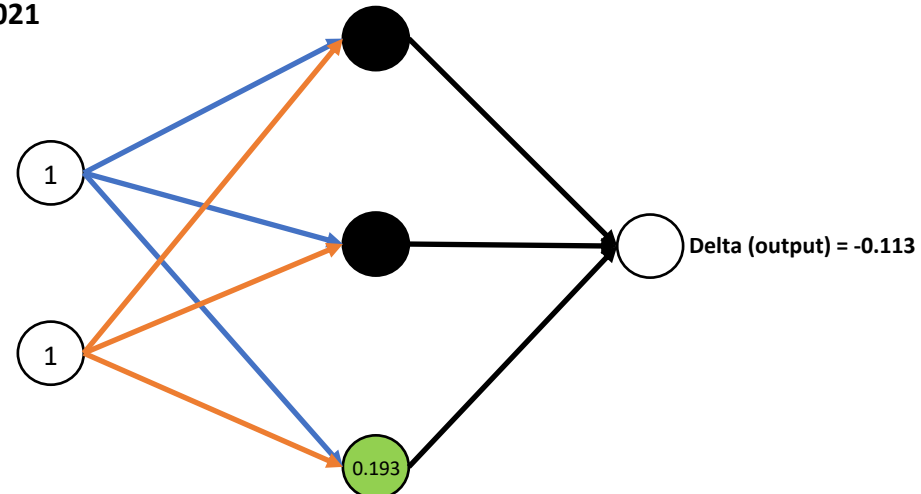
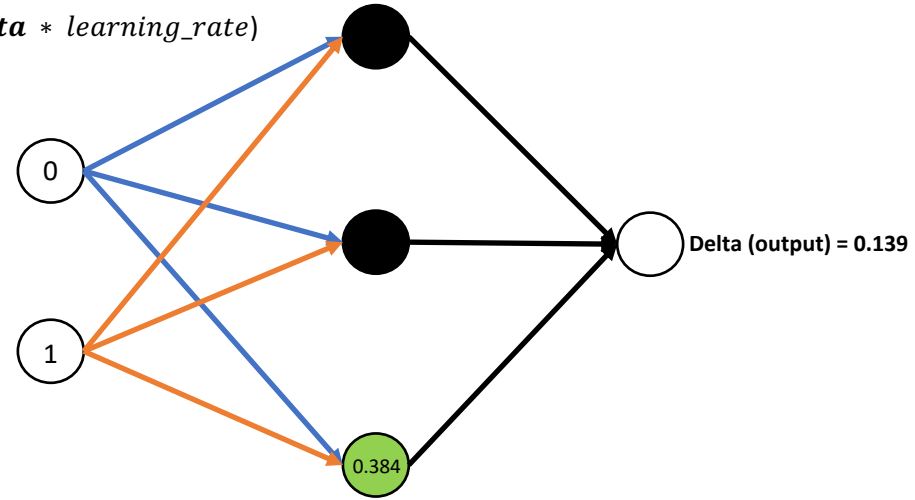
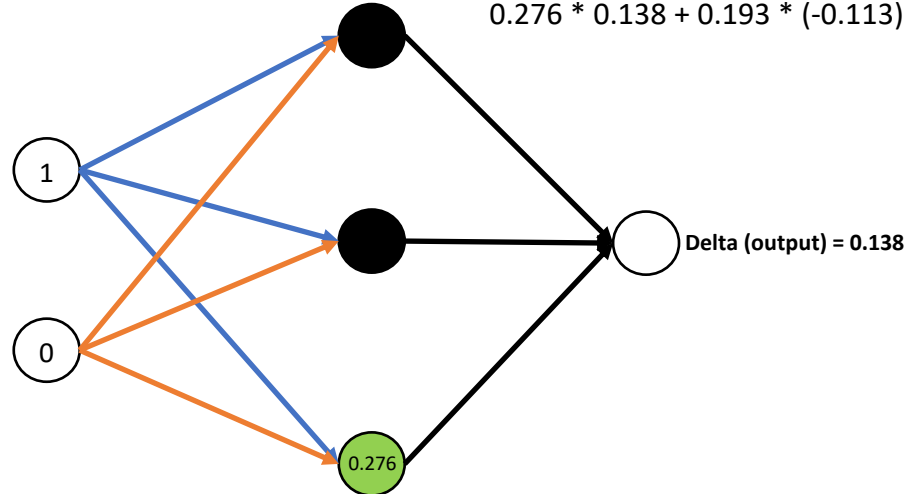
$$0.5 * (-0.097) + 0.359 * 0.139 + 0.323 * 0.138 + 0.211 * (-0.113) = \mathbf{0.022}$$



# WEIGHT UPDATE – OUTPUT LAYER TO HIDDEN LAYER



$$0.5 * (-0.097) + 0.384 * 0.139 + 0.276 * 0.138 + 0.193 * (-0.113) = \mathbf{0.021}$$



# WEIGHT UPDATE – OUTPUT LAYER TO HIDDEN LAYER

Learning rate = 0.3

**Input x delta**

0.033

0.022

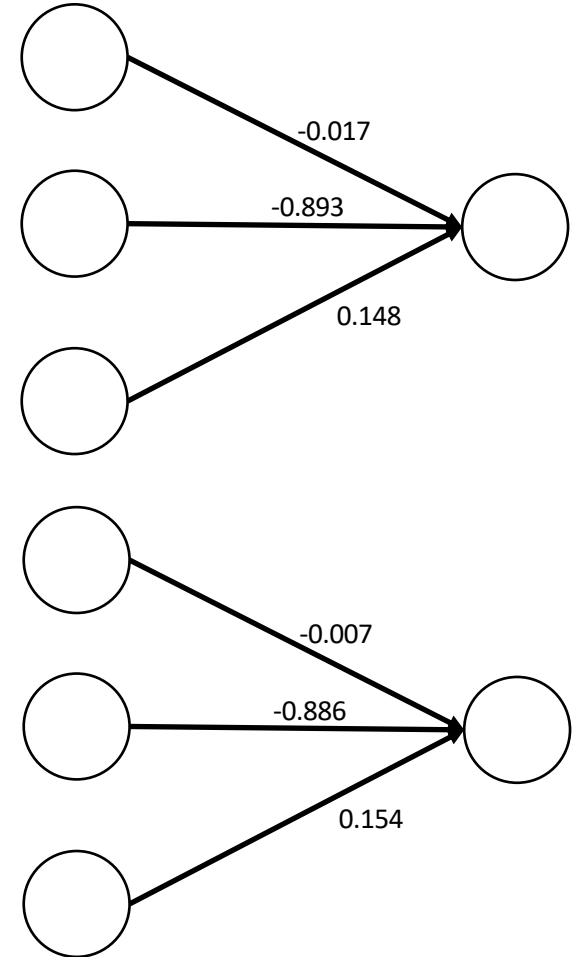
0.021

$$weight_{n+1} = weight_n + (input * delta * learning\_rate)$$

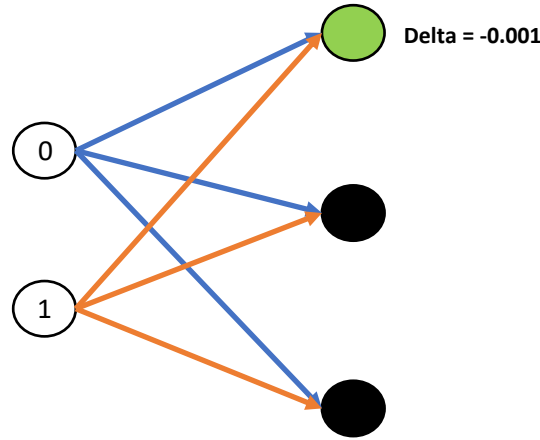
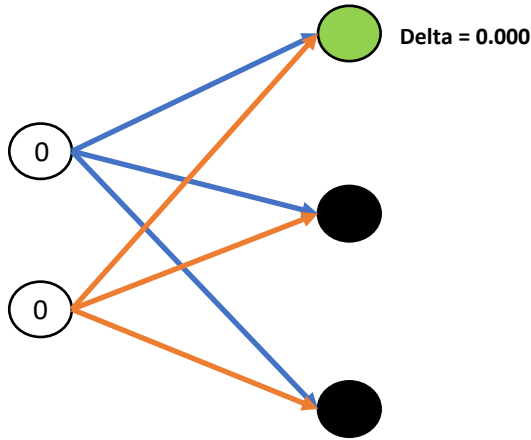
$$-0.017 + 0.033 * 0.3 = \mathbf{-0.007}$$

$$-0.893 + 0.022 * 0.3 = \mathbf{-0.886}$$

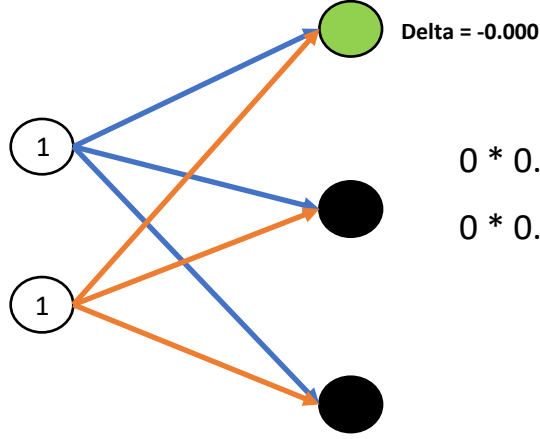
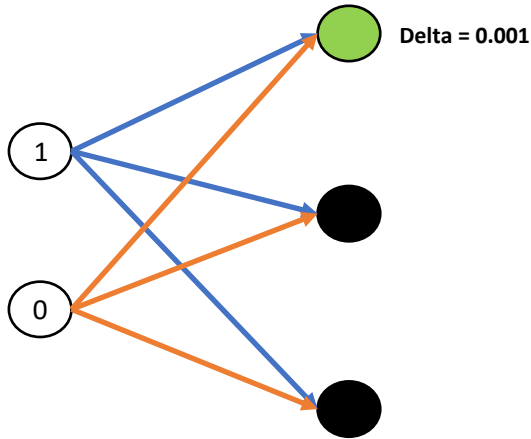
$$0.148 + 0.021 * 0.3 = \mathbf{0.154}$$



# WEIGHT UPDATE – HIDDEN LAYER TO INPUT LAYER



$$weight_{n+1} = weight_n + (input * delta * learning\_rate)$$



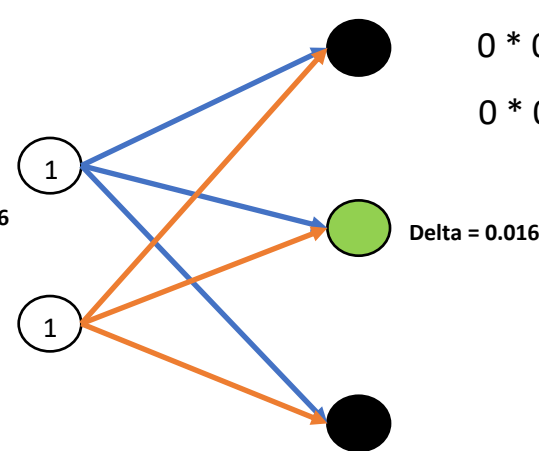
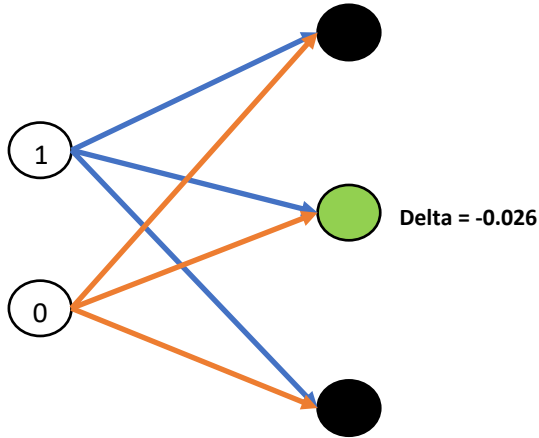
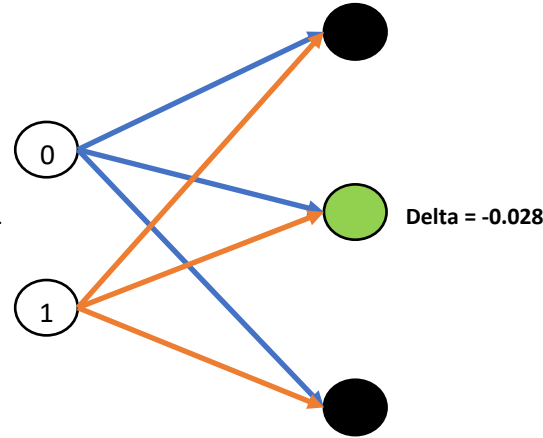
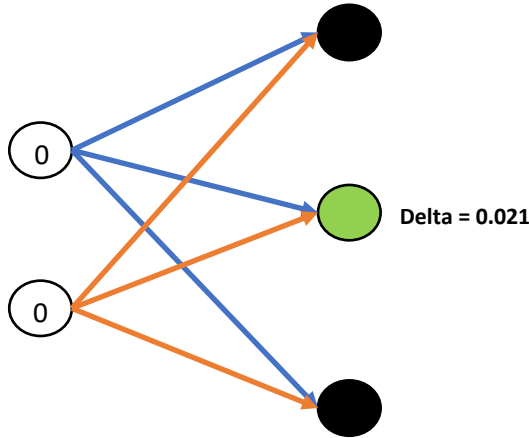
$$0 * 0.000 + 0 * (-0.001) + 1 * (0.001) + 1 * -0.000 = -0.000$$

$$0 * 0.000 + 1 * (-0.001) + 0 * (0.001) + 1 * -0.000 = -0.000$$

# WEIGHT UPDATE – HIDDEN LAYER TO INPUT LAYER



$$weight_{n+1} = weight_n + (input * delta * learning\_rate)$$



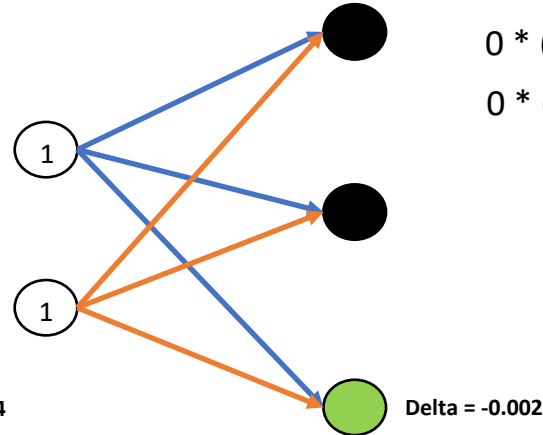
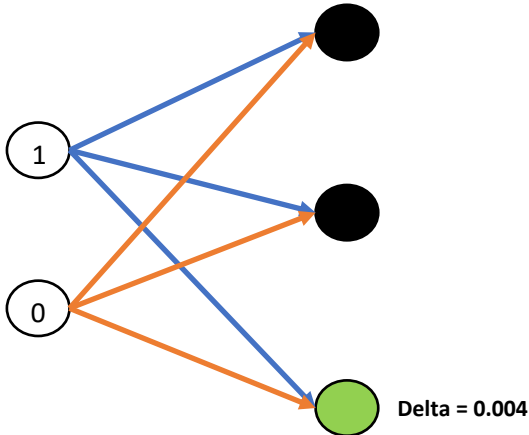
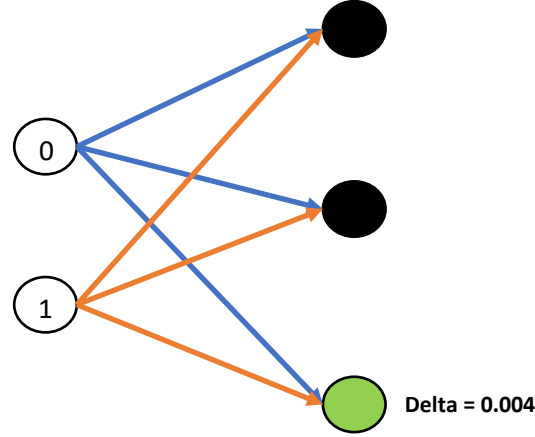
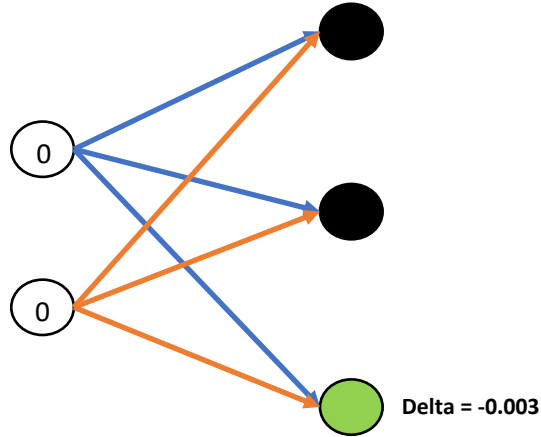
$$0 * 0.021 + 0 * (-0.028) + 1 * (-0.026) + 1 * 0.016 = -0.009$$

$$0 * 0.021 + 1 * (-0.028) + 0 * (-0.026) + 1 * 0.016 = -0.012$$

# WEIGHT UPDATE – HIDDEN LAYER TO INPUT LAYER



$$weight_{n+1} = weight_n + (input * delta * learning\_rate)$$



$$0 * (-0.003) + 0 * 0.004 + 1 * 0.004 + 1 * (-0.002) = 0.002$$

$$0 * (-0.003) + 1 * 0.004 + 0 * 0.004 + 1 * (-0.002) = 0.002$$

# WEIGHT UPDATE – HIDDEN LAYER TO INPUT LAYER



Learning rate = 0.3

**Input x delta**

-0.000 -0.009 0.002

-0.000 -0.012 0.002

$$weight_{n+1} = weight_n + (input * delta * learning\_rate)$$

$$-0.424 + (-0.000) * 0.3 = \mathbf{-0.424}$$

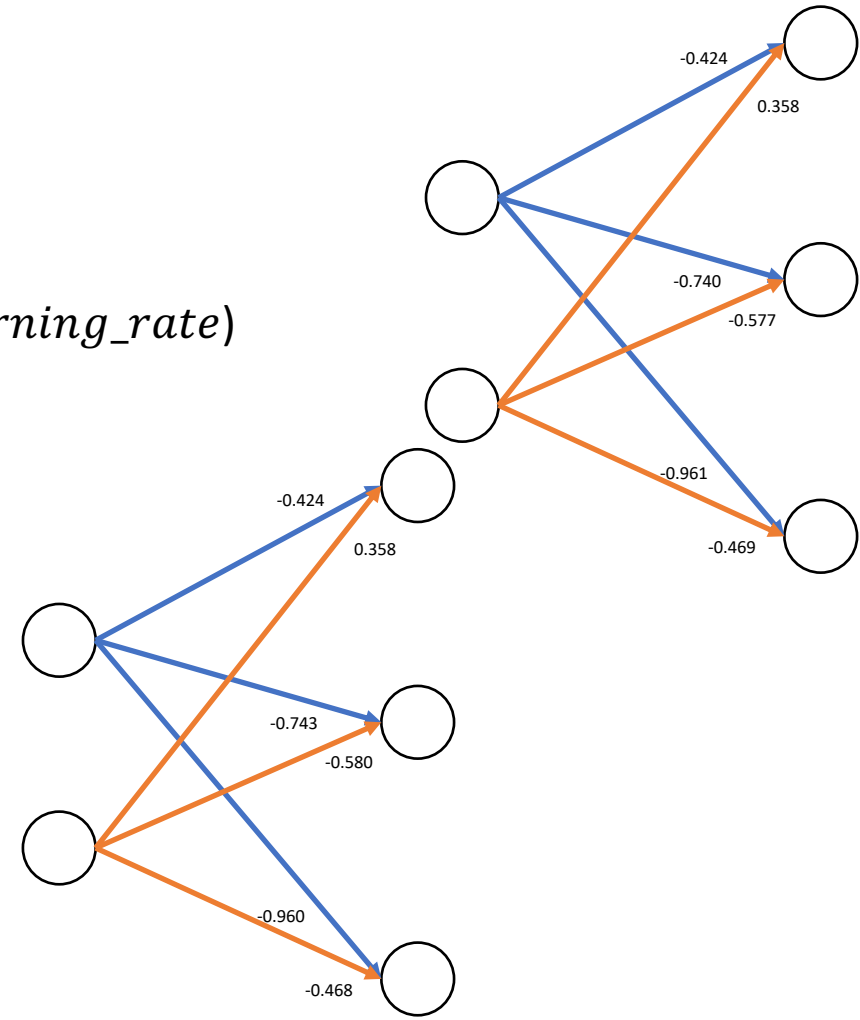
$$0.358 + (-0.000) * 0.3 = \mathbf{0.358}$$

$$-0.740 + (-0.009) * 0.3 = \mathbf{-0.743}$$

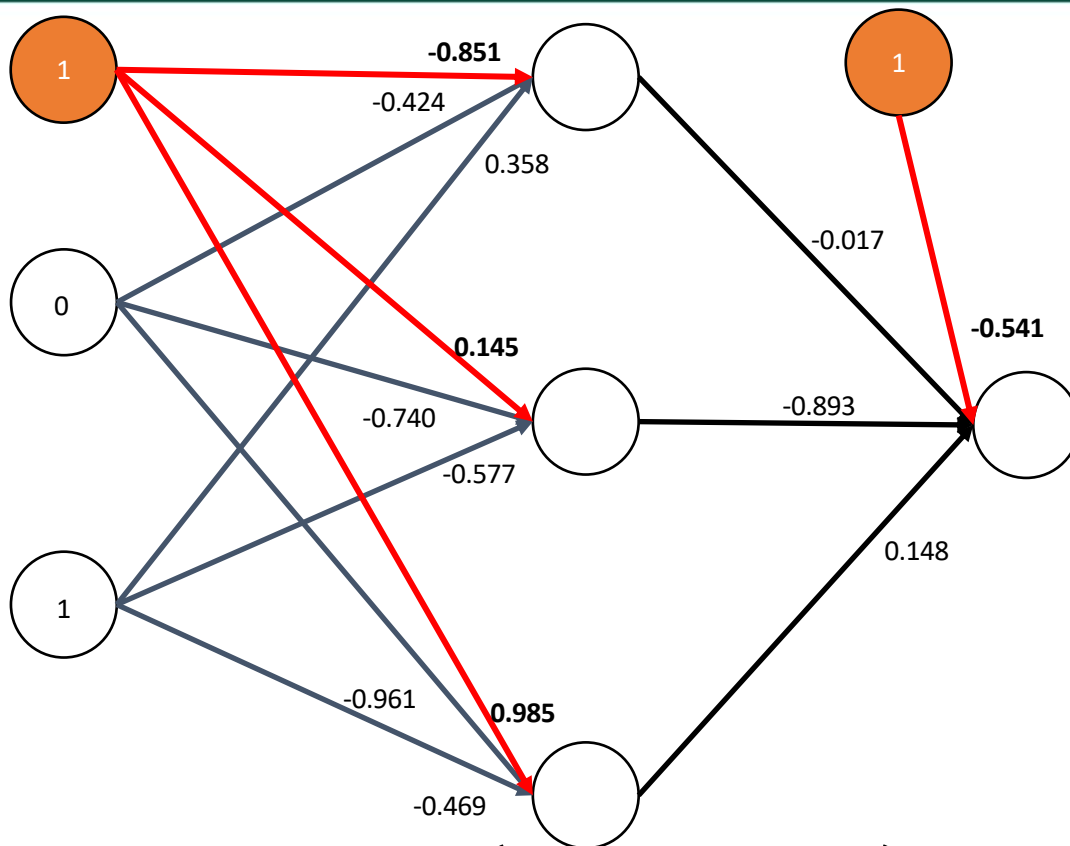
$$-0.577 + (-0.012) * 0.3 = \mathbf{-0.580}$$

$$-0.961 + 0.002 * 0.3 = \mathbf{-0.960}$$

$$-0.469 + 0.002 * 0.3 = \mathbf{-0.468}$$



# BIAS



$$\text{output} = \text{sum}(\text{inputs} * \text{weights}) + \text{bias}$$



# ERROR (LOSS FUNCTION)

The simplest algorithm

error = correct – prediction

X1	X2	Class	Prediction	Error
0	0	0	0.405	-0.405
0	1	1	0.431	0.569
1	0	1	0.436	0.564
1	1	0	0.458	-0.458

Average = 0.499

# MEAN SQUARED ERROR (MSE) AND ROOT MEAN SQUARED ERROR (RMSE)

$$MSE = \frac{1}{N} \sum_{i=1}^N (f_i - y_i)^2$$

$$RMSE = \sqrt{\frac{1}{N} \sum_{i=1}^N (f_i - o_i)^2}$$

X1	X2	Class	Prediction	Error
0	0	0	0.405	$(0 - 0.405)^2 = 0.164$
0	1	1	0.431	$(1 - 0.431)^2 = 0.322$
1	0	1	0.436	$(1 - 0.436)^2 = 0.316$
1	1	0	0.458	$(0 - 0.458)^2 = 0.209$

10 (expected) – 5 (prediction) = 5 ( $5^2 = 25$ )

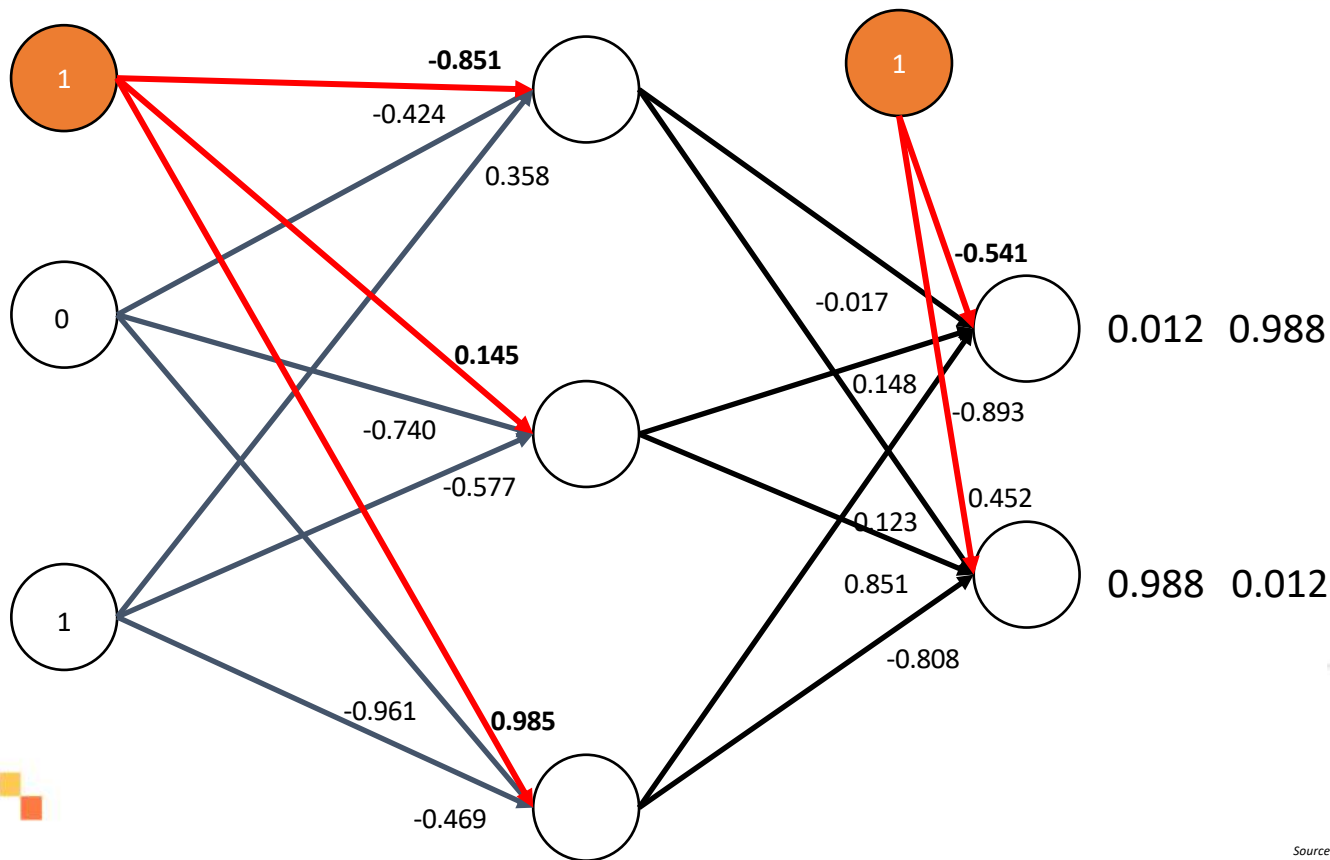
10 (expected) – 8 (prediction) = 2 ( $2^2 = 4$ )

Sum = 1.011

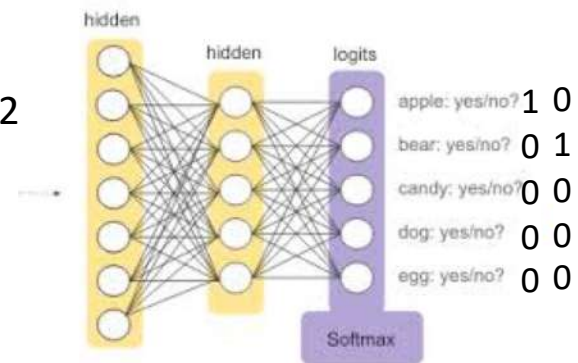
MSE = 1.011 / 4 = 0.252

RMSE = 0.501

# MULTIPLE OUTPUTS



X1	X2	Class
0	0	0
0	1	1
1	0	1
1	1	0



Source: <https://developers.google.com/machine-learning/crash-course/multi-class-neural-networks/softmax>



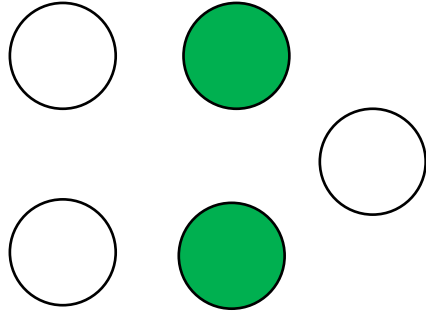
# HIDDEN LAYERS



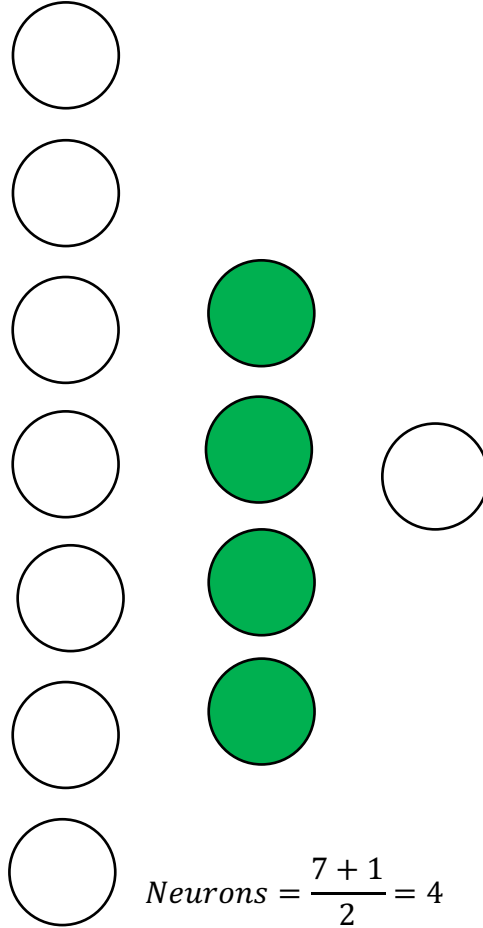
$$\text{Neurons} = \frac{\text{Inputs} + \text{Outputs}}{2}$$

Inputs

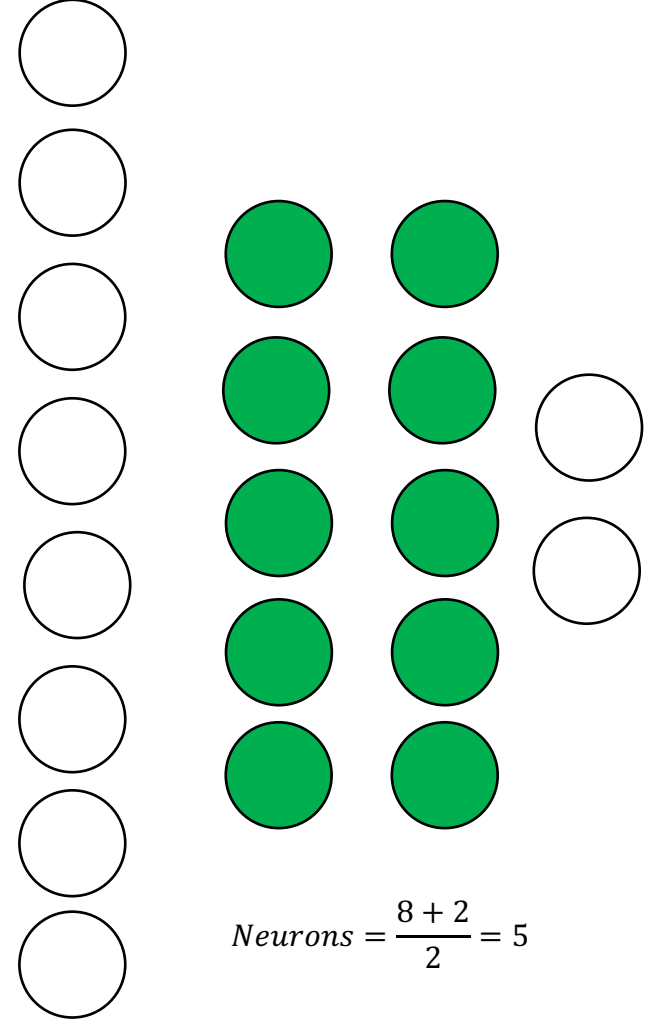
Output



$$\text{Neurons} = \frac{2 + 1}{2} = 1.5$$



$$\text{Neurons} = \frac{7 + 1}{2} = 4$$



$$\text{Neurons} = \frac{8 + 2}{2} = 5$$

# HIDDEN LAYERS

- Linearly separable problems do not require hidden layers
- In general, two layers work well
- Deep learning research shows that more layers are essential for more complex problems

# HIDDEN LAYERS

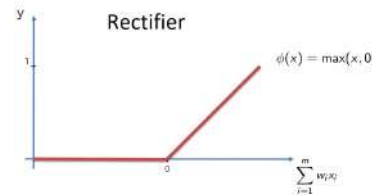
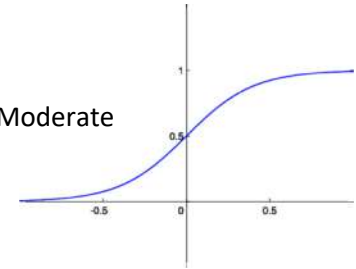
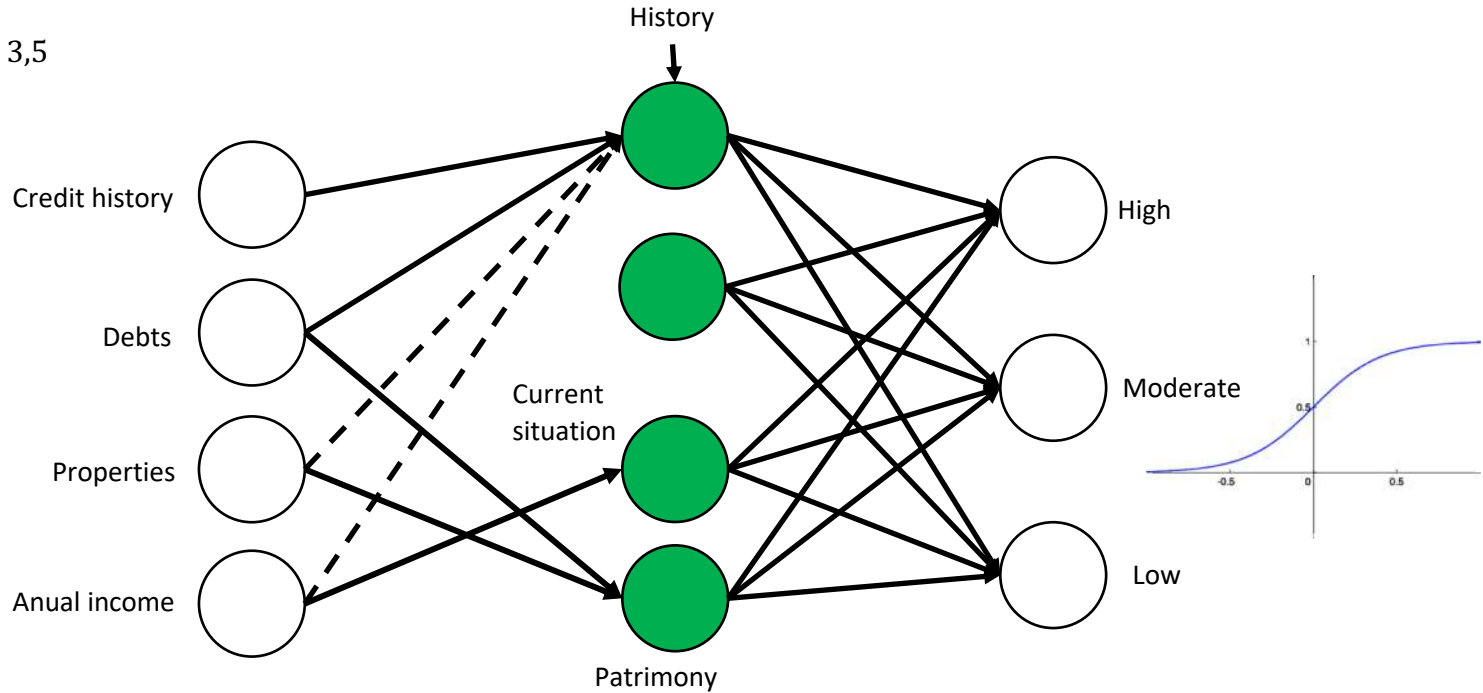


Credit history	Debts	Properties	Anual income	Risk
Bad	High	No	< 15.000	High
Unknown	High	No	>= 15.000 a <= 35.000	High
Unknown	Low	No	>= 15.000 a <= 35.000	Moderate
Unknown	Low	No	> 35.000	High
Unknown	Low	No	> 35.000	Low
Unknown	Low	Yes	> 35.000	Low
Bad	Low	No	< 15.000	High
Bad	Low	Yes	> 35.000	Moderate
Good	Low	No	> 35.000	Low
Good	High	Yes	> 35.000	Low
Good	High	No	< 15.000	High
Good	High	No	>= 15.000 a <= 35.000	Moderate
Good	High	No	> 35.0000	Low
Bad	High	No	>= 15.000 a <= 35.000	High

# HIDDEN LAYERS

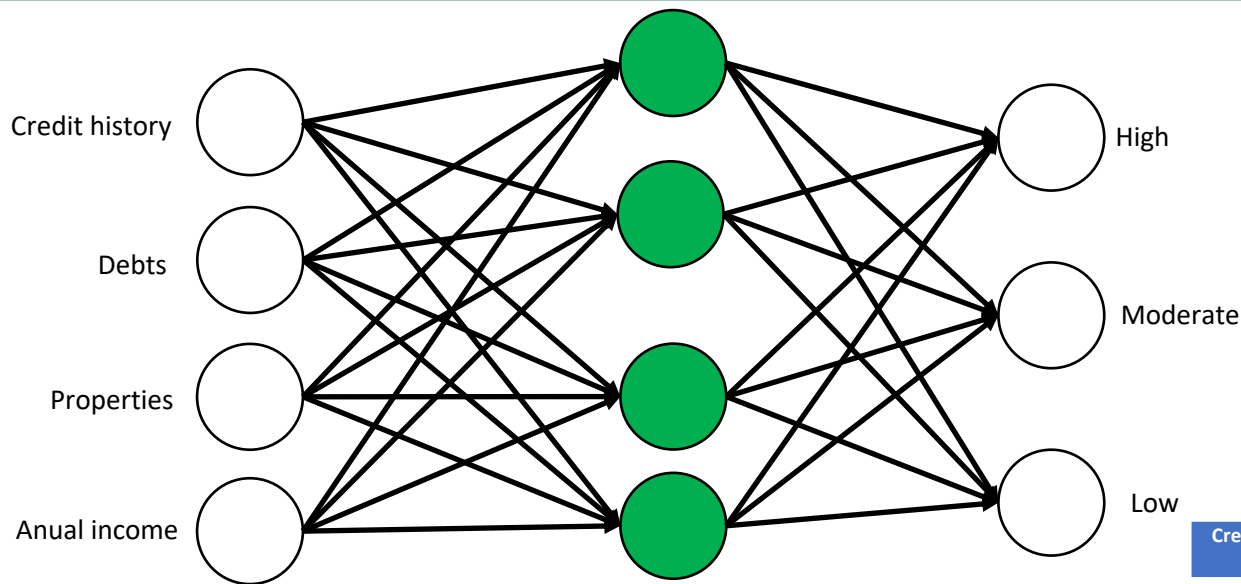


$$\text{Neurons} = \frac{4 + 3}{2} = 3,5$$



The higher the activation value,  
the more impact the neuron has

# OUTPUT LAYER WITH CATEGORICAL DATA



error = correct – prediction

expected output = 1 0 0

prediction = 0.95 0.02 0.03

error = (1 – 0.95) + (0 – 0.02) + (0 – 0.03)

error = 0.05 + 0.02 + 0.03 = 0.08

Credit history	Debts	Properties	Annual income	Risk
3	1	1	1	100
2	1	1	2	100
2	2	1	2	010
2	2	1	3	100
2	2	1	3	001
2	2	2	3	001
3	2	1	1	100
3	2	2	3	010
1	2	1	3	001
1	1	2	3	001
1	1	1	1	100
1	1	1	2	010
1	1	1	3	001
3	1	1	2	100



# STOCHASTIC GRADIENT DESCENT



Credit history	Debts	Properties	Anual income	Risk
3	1	1	1	100
2	1	1	2	100
2	2	1	2	010
2	2	1	3	100
2	2	1	3	001
2	2	2	3	001
3	2	1	1	100
3	2	2	3	010
1	2	1	3	001
1	1	2	3	001
1	1	1	1	100
1	1	1	2	010
1	1	1	3	001
3	1	1	2	100

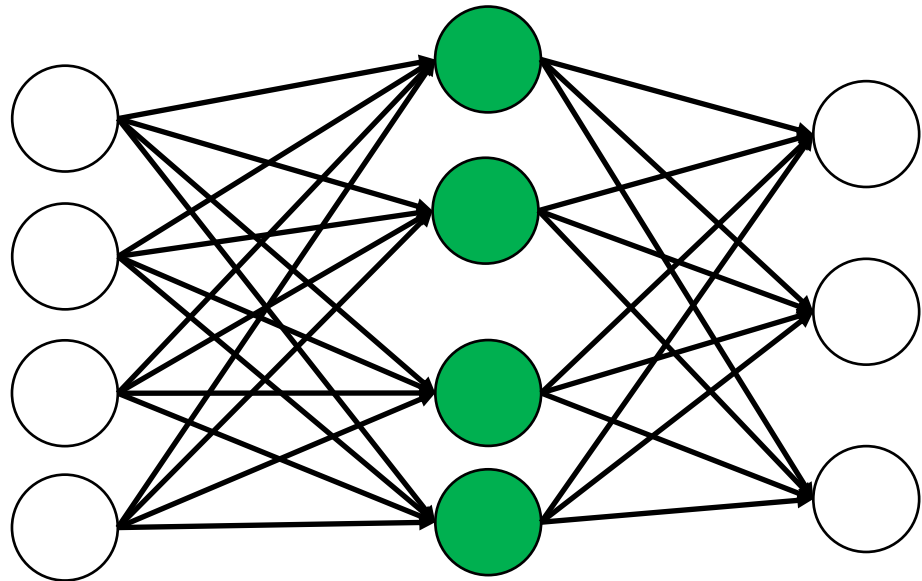
## Batch gradient descent

Calculate the error for all instances and then update the weights

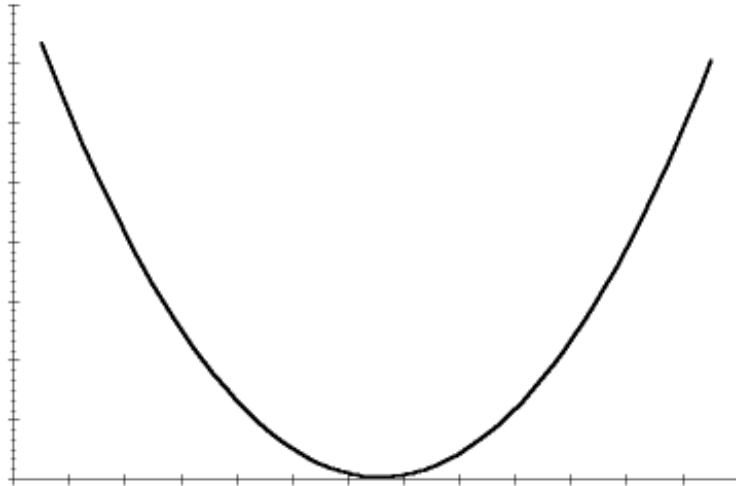
## Stochastic gradient descent

Calculate the error for each instance and then update the weights

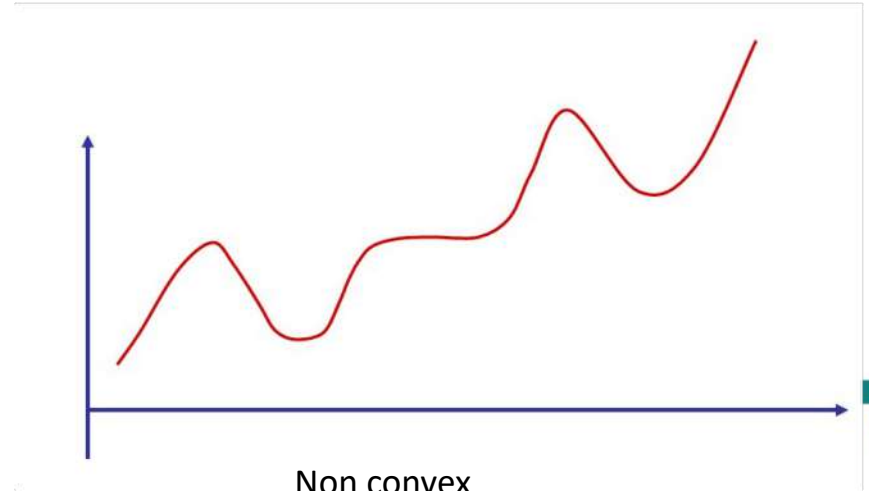
Credit history	Debts	Properties	Anual income	Risk
3	1	1	1	100
2	1	1	2	100
2	2	1	2	010
2	2	1	3	100
2	2	1	3	001
2	2	2	3	001
3	2	1	1	100
3	2	2	3	010
1	2	1	3	001
1	1	2	3	001
1	1	1	1	100
1	1	1	2	010
1	1	1	3	001
3	1	1	2	100



# CONVEX AND NON CONVEX



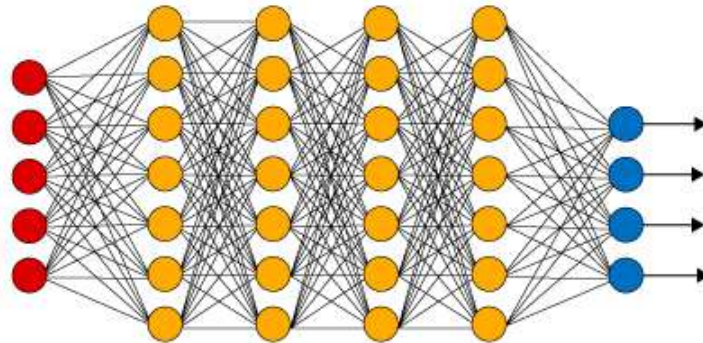
Convex



Non convex

- Stochastic gradient descent
  - Prevent local minimums (non convex)
  - Faster
- Mini batch gradient descent
  - Select a pre-defined number of instances in order to calculate the error and update the weights

- 90's: SVM (Support Vector Machines)
- From 2006, several algorithms were created for training neural networks
- Two or more hidden layers



- Convolutional neural networks
- Recurrent neural networks
- Autoencoders
- GANs (Generative adversarial networks)

# PLAN OF ATTACK – LIBRARIES FOR NEURAL NETWORKS

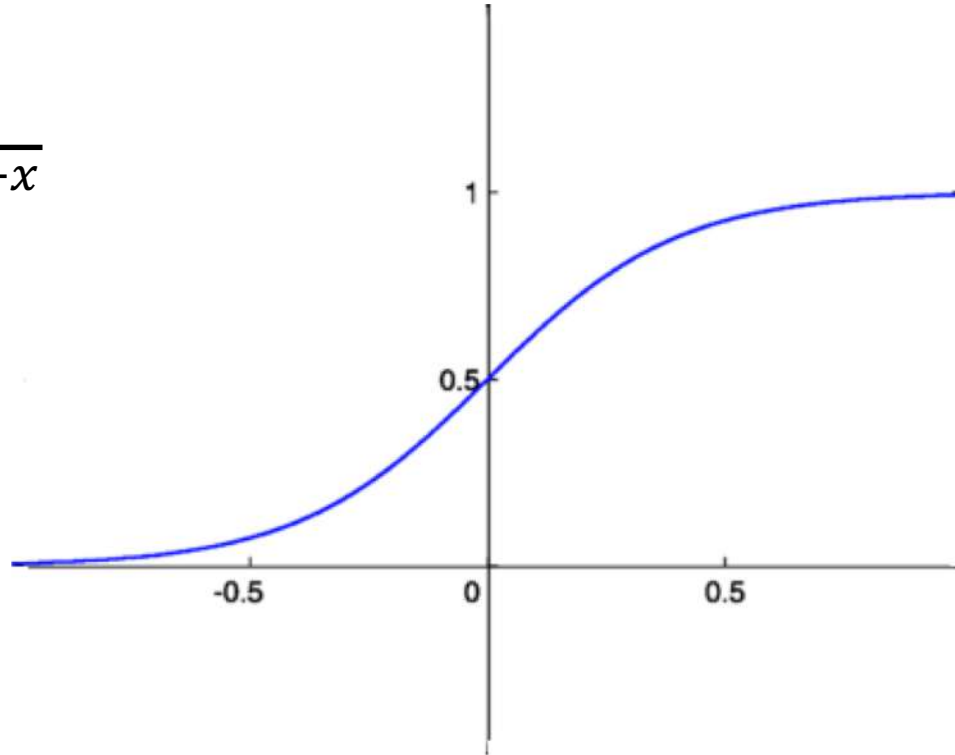
1. Pybrain
2. Sklearn (classification and regression)
3. TensorFlow (image classification)
4. PyTorch

# STEP FUNCTION



# SIGMOID FUNCTION

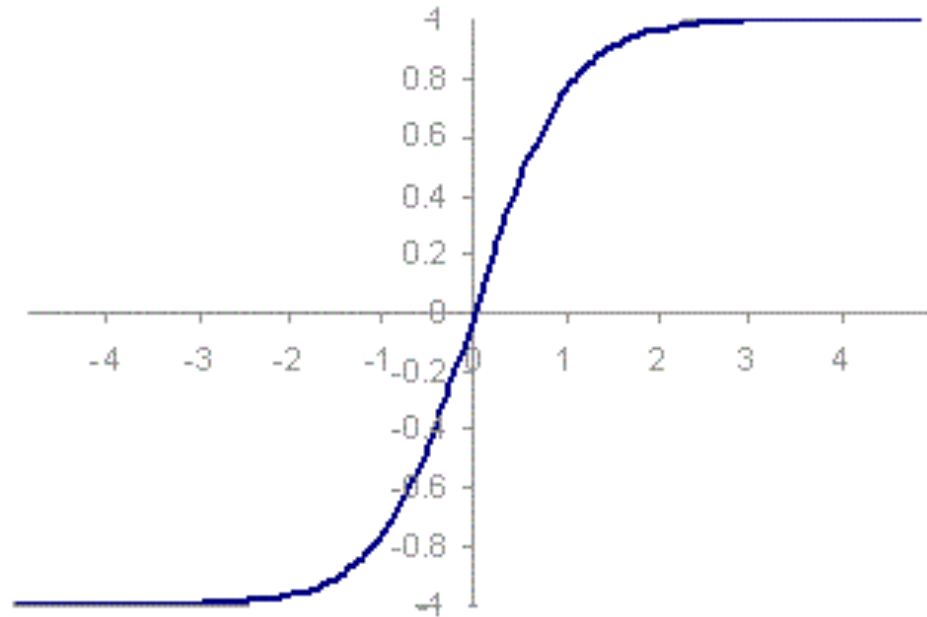
$$y = \frac{1}{1 + e^{-x}}$$





# HYPERBOLIC TANGENT

$$Y = \frac{e^x - e^{-x}}{e^x + e^{-x}}$$

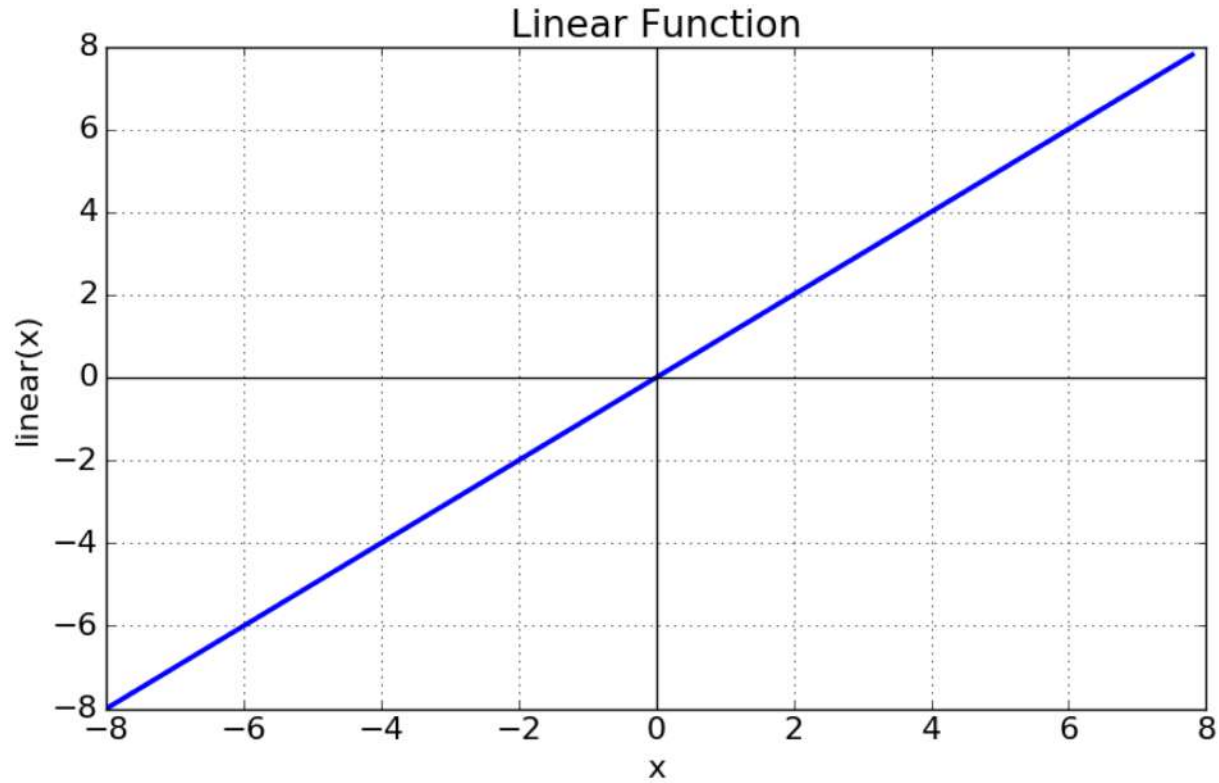


# ReLU (RECTIFIED LINEAR UNIT)

$$Y = \max(0, x)$$



# LINEAR



# SOFTMAX

$$Y = \frac{e(x)}{\sum e(x)}$$

