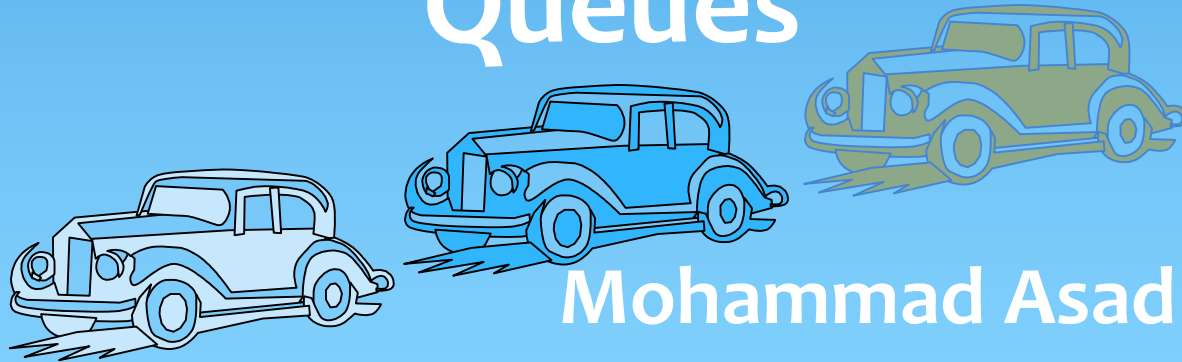


Queues



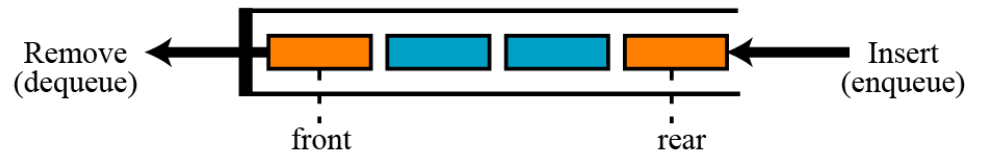
Mohammad Asad Abbasi
Lecture 5

Queues

- A data structure of ordered items such that items can be inserted only at one end and removed at the other end.
- A queue is called a FIFO (First in-First out) data structure.
- Insertions are at the rear of the queue and removals are at the front of the queue.



A queue of people



A computer queue

Application: Job scheduling

front	rear	Q[0]	Q[1]	Q[2]	Q[3]	Comments
-1	-1					queue is empty
-1	0	J1				Job 1 is added
-1	1	J1	J2			Job 2 is added
-1	2	J1	J2	J3		Job 3 is added
0	2		J2	J3		Job 1 is deleted
1	2			J3		Job 2 is deleted

Insertion and deletion from a sequential queue

Applications of Queues

➤ Direct applications

- Waiting lines
- Round-robin scheduling in processors
- Input/Output processing
- Queueing of packets for delivery in networks
- Access to shared resources (e.g., printer)
- Multiprogramming
- All types of customer service software (like Railway/Air ticket reservation) are designed using queue to give proper service to the customers.

➤ Indirect applications

- Auxiliary data structure for algorithms
- Component of other data structures

Main Queue Operations

➤ Main Queue Operations

- **enqueue(object):** inserts an element at the end of the queue
- **object dequeue():** removes and returns the element at the front of the queue

➤ Auxiliary queue operations:

- **object front():** returns the element at the front without removing it
- **integer size():** returns the number of elements stored
- **boolean isEmpty():** indicates whether no elements are stored

➤ Exceptions

- **Attempting the execution of dequeue or front on an empty queue throws an EmptyQueueException.**

Operations on queues

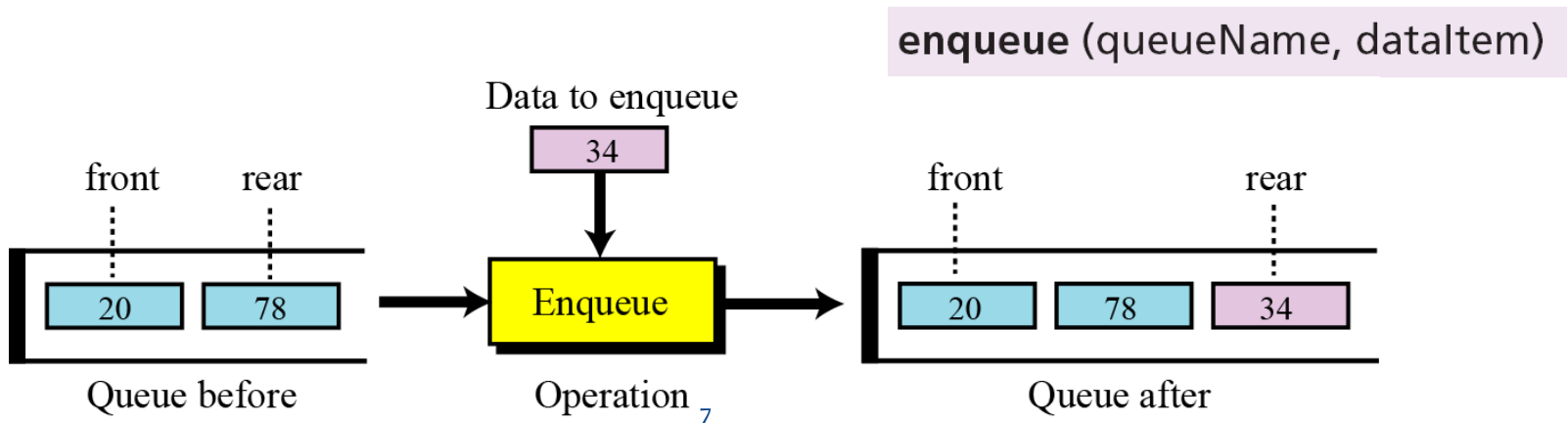
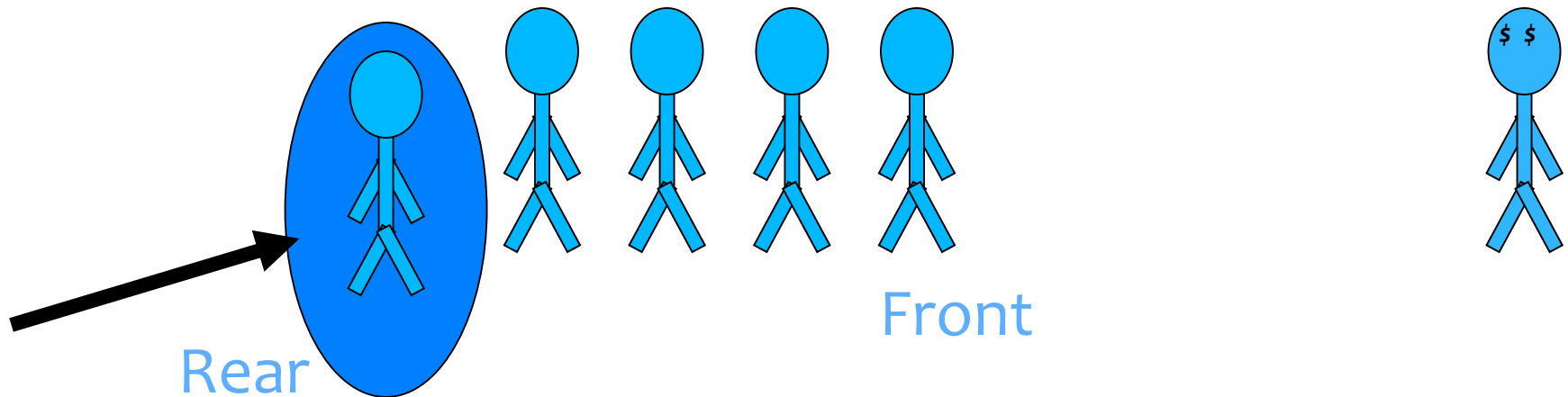
- The queue operation creates an empty queue.

`queue (queueName)`



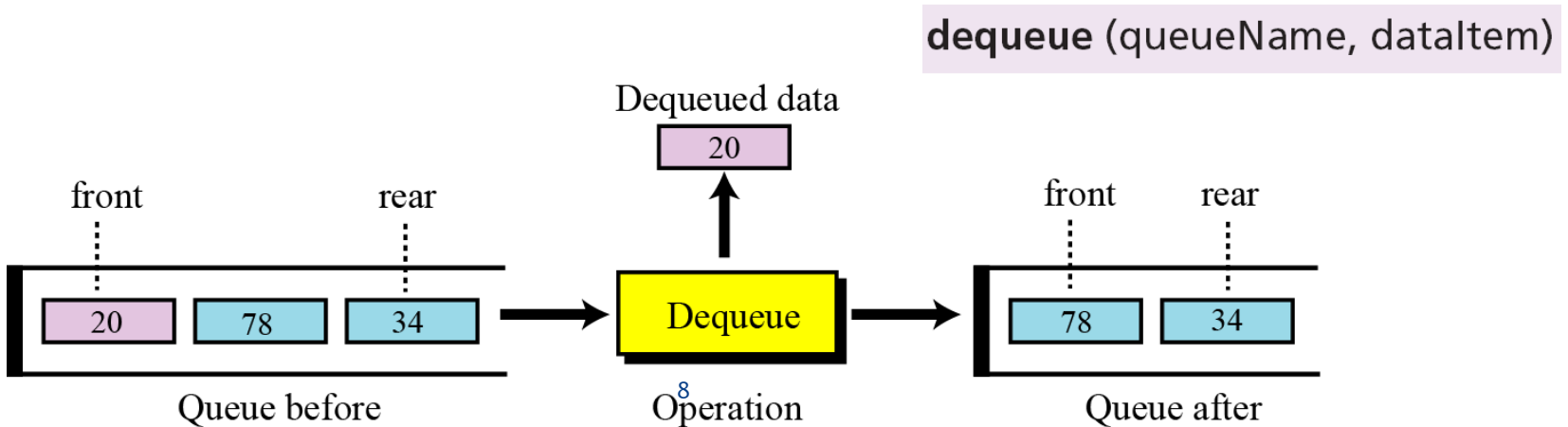
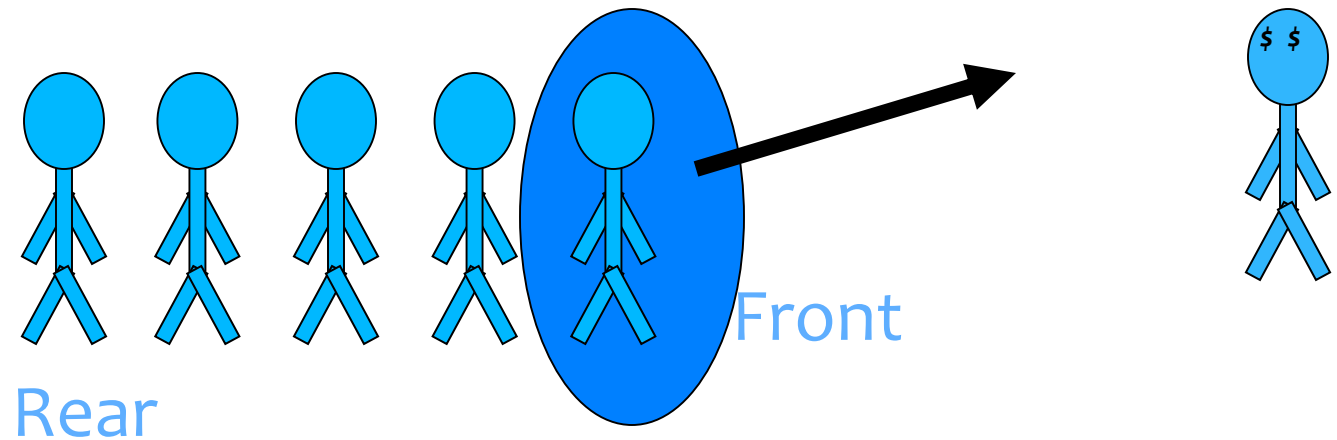
The enqueue operation

- The enqueue operation inserts an item at the rear of the queue.



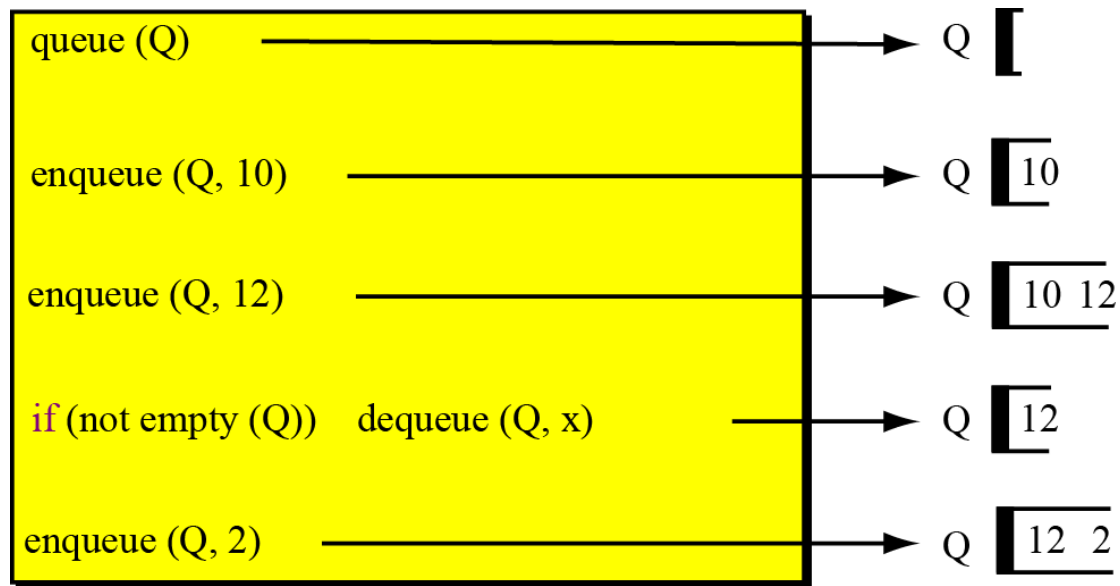
The dequeue operation

- The dequeue operation deletes the item at the front of the queue.



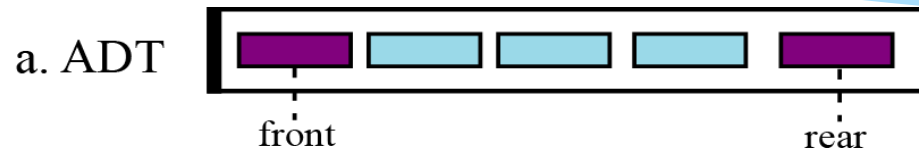
Example

- A segment of an algorithm that applies the previously defined operations on a queue Q.

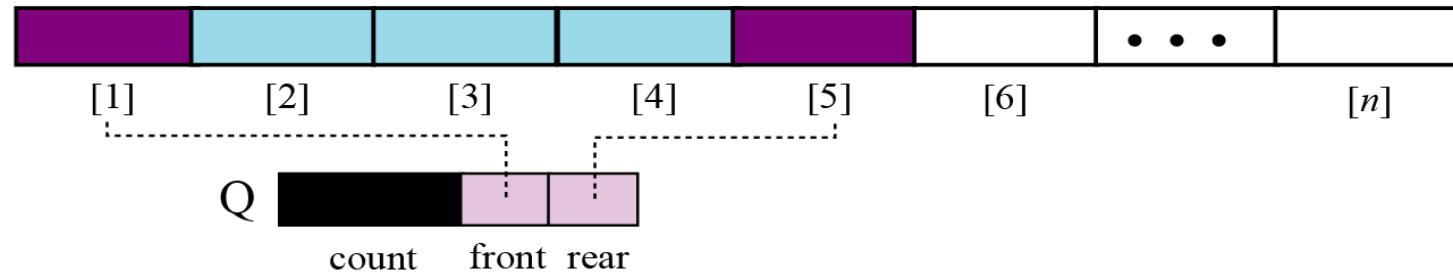


An algorithm segment

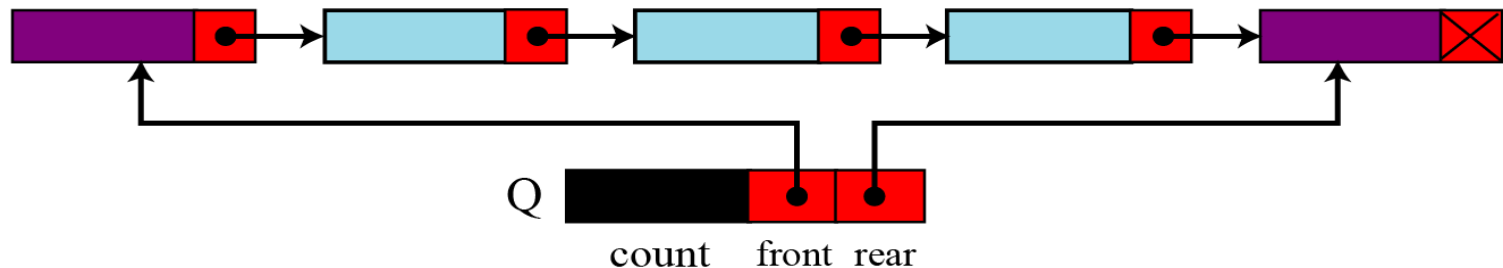
Implementing a Queue



b. Array
implementation



c. Linked list
implementation

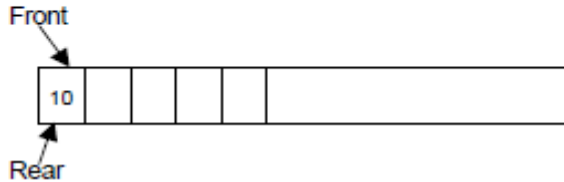


Example(Array Implementation)



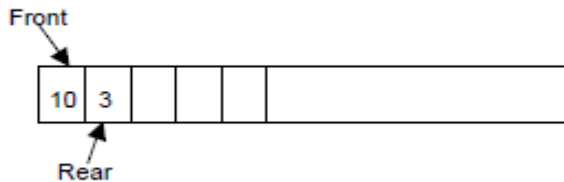
Rear = -1
Front = -1

Fig. 4.1. Queue is empty.



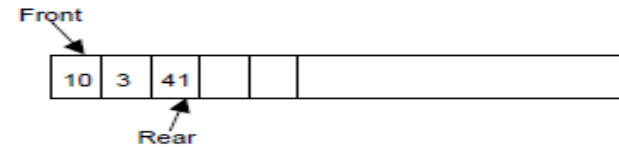
Rear = 0
Front = 0

Fig. 4.2. push(10)



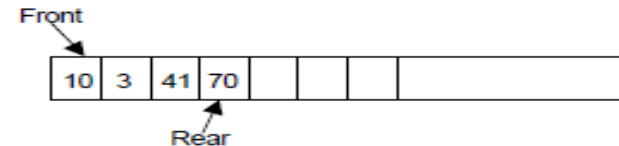
Rear = 1
Front = 0

Fig. 4.3. push(3)



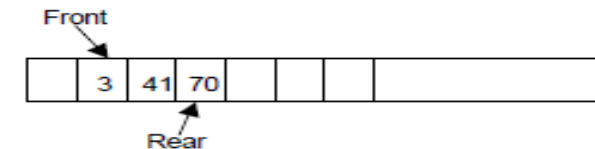
Rear = 2
Front = 0

Fig. 4.4. push(41)



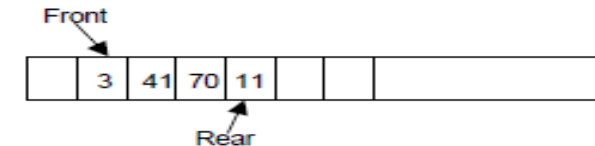
Rear = 3
Front = 0

Fig. 4.5. push(70)



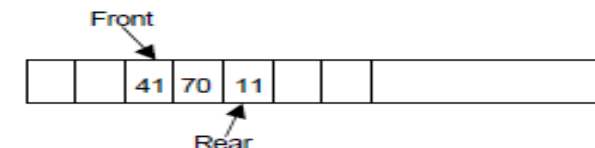
Rear = 3
Front = 1

Fig. 4.6. $x = \text{pop}()$ (i.e.; $x = 10$)



Rear = 4
Front = 1

Fig. 4.7. push(11)



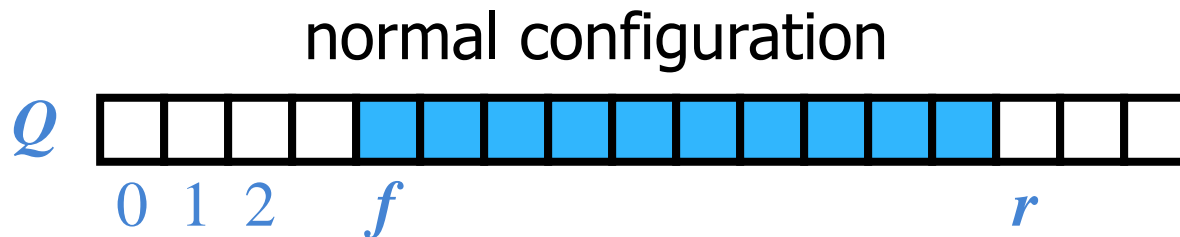
Rear = 4
Front = 2

Fig. 4.8. $x = \text{pop}()$ (i.e.; $x = 3$)

Implementation

Array-based Queue

- Use an array of size N in a circular fashion
- Two variables keep track of the front and rear
 - f index of the front element
 - r index immediately past the rear element
- Array location r is kept empty



INSERTING AN ELEMENT INTO THE QUEUE

1. Initialize front=0 & rear = -1
2. Input the value to be inserted and assign to variable “data”
3. If (rear >= SIZE)
 - (a) *Display “Queue overflow”*
 - (b) *Exit*
4. Else
 - (a) *Rear = rear +1*
5. $Q[\text{rear}] = \text{data}$
6. Exit

ENQUEUE()

```
1. //This function will insert an element to the queue
2. void insert ()
3. {
4.     int added_item;
5.     if (rear==MAX-1)
6.     {
7.         printf("\nQueue Overflow\n");
8.         getch();
9.         return;
10.    }
11.    else
12.    {
13.        if (front== -1)                /*If queue is initially empty */
14.        front=0;
15.        printf("\nInput the element for adding in queue: ");
16.        scanf("%d", &added_item);
17.        rear=rear+1;
18.        //Inserting the element
19.        queue_arr[rear] = added_item ;
20.    }
21. }/*End of insert()*/
```

ALGORITHM TO DELETE AN ELEMENT FROM QUEUE

1. If ($\text{rear} < \text{front}$)
 - (a) $\text{Front} = 0, \text{rear} = -1$
 - (b) Display “The queue is empty”
 - (c) Exit
2. Else
 - (a) $\text{Data} = \text{Q}[\text{front}]$
3. $\text{Front} = \text{front} + 1$
4. Exit

DEQUEUE()

```
1. //This function will delete (or pop) an element from the queue
2. void del()
3. {
4.     if (front == -1 || front > rear)
5.     {
6.         printf ("\nQueue Underflow\n");
7.         return;
8.     }
9.     else
10.    {                                     //deleteing the element
11.        printf ("\nElement deleted from queue is : %d\n",
12.            queue_arr[front]);
13.        front=front+1;
14.    }
15. }/*End of del()*/
```


PROGRAM TO DISPLAY ALL QUEUE ELEMENTS

```
1. //Displaying all the elements of the queue
2. void display()
3. {
4.     int i;
5.     if (front == -1 || front > rear)           //Checking whether the queue is empty or not
6.     {
7.         printf ("\nQueue is empty\n");
8.         return;
9.     }
10.    else
11.    {
12.        printf("\nQueue is :\n");
13.        for(i=front;i<= rear;i++)
14.            printf("%d ",queue_arr[i]);
15.        printf("\n");
16.    }
17. }/*End of display() */
```

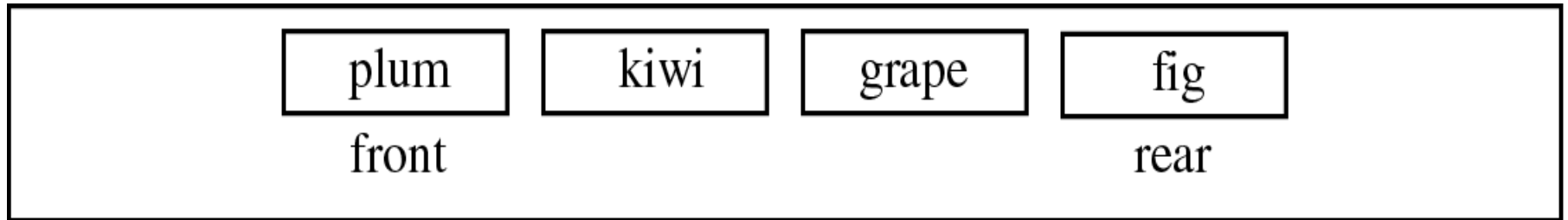
Linked-list implementation of queues

- In a queue, insertions occur at one end, deletions at the other end
- Operations at the front of a singly-linked list (SLL) are $O(1)$, but at the other end they are $O(n)$
 - Because you have to find the last element each time
- BUT: there is a simple way to use a singly-linked list to implement both insertions and deletions in $O(1)$ time
 - You always need a pointer to the first element in the list
 - You can keep an additional pointer to the *last* element in the list

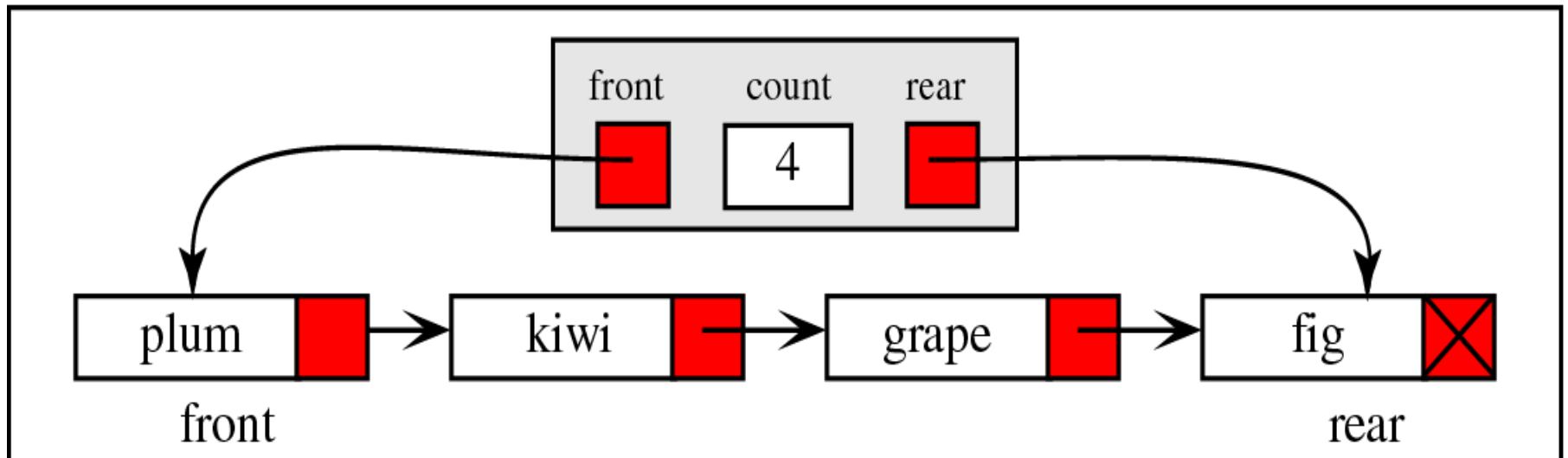
SLL implementation of queues

- In an SLL you can easily find the successor of a node, but not its predecessor
 - Remember, pointers (references) are one-way
- If you know where the *last* node in a list is, it's hard to remove that node, but it's easy to add a node after it
- Hence,
 - Use the *first* element in an SLL as the *front* of the queue
 - Use the *last* element in an SLL as the *rear* of the queue
 - Keep pointers to *both* the front and the rear of the SLL

Queue Linked List Design

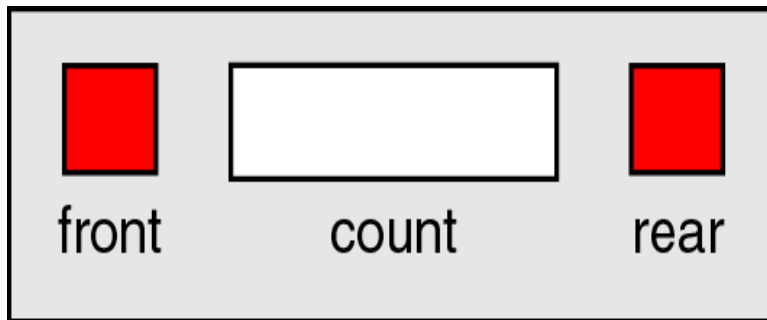


(a) Conceptual queue

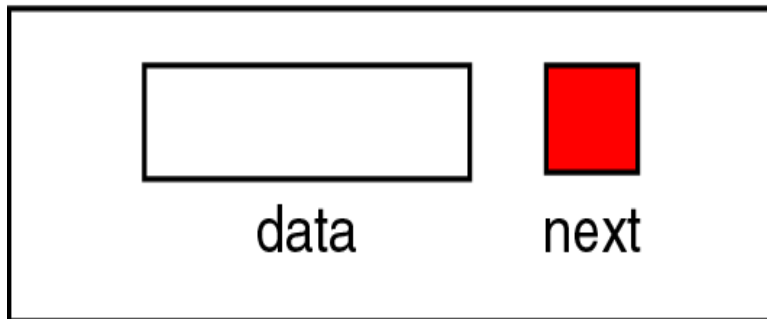


(b) Physical queue

Queue Data Structure



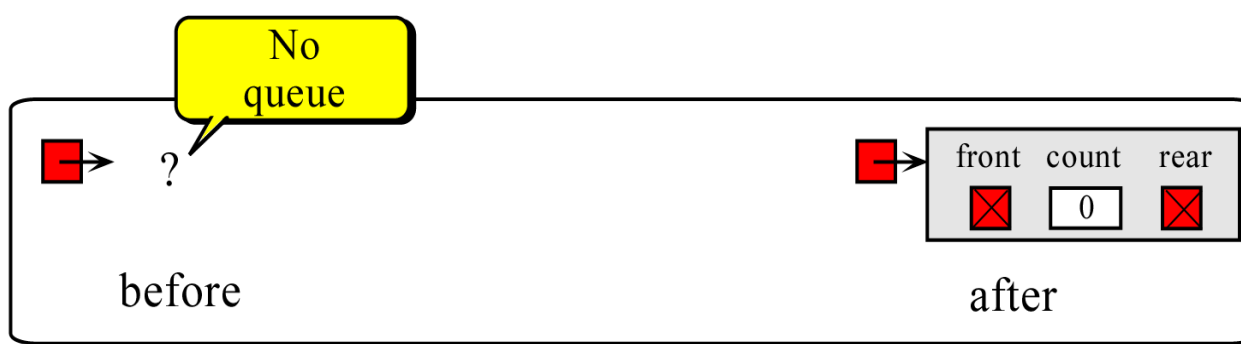
Head structure



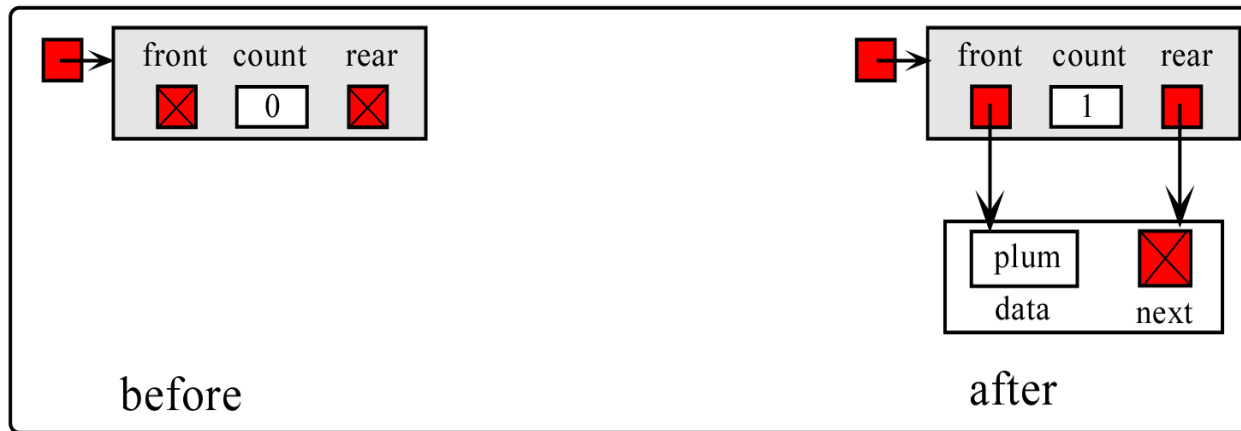
Node structure

```
queueHead  
  front    <node pointer>  
  count    <integer>  
  rear     <node pointer>  
end queueHead
```

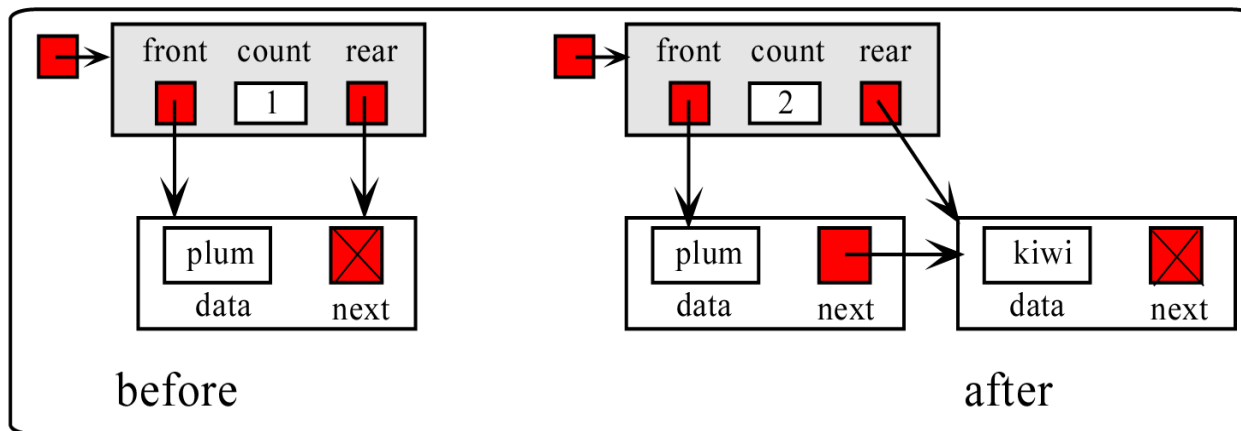
```
node  
  data     <dataType>  
  next     <node pointer>  
end node
```



create queue



enqueue

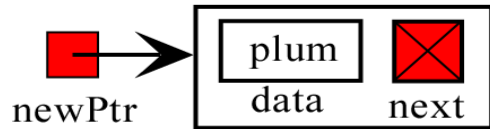
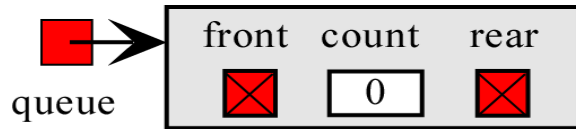


enqueue

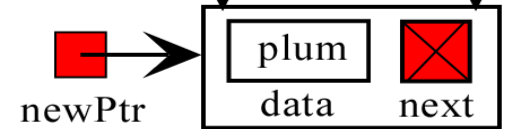
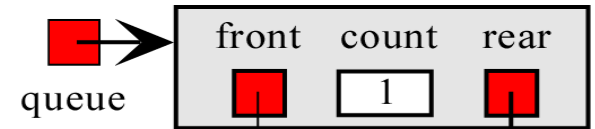
Queue Algorithms - Create Queue

- Algorithm createQueue
 - Allocates memory for a queue head node from dynamic memory and returns its address to the caller.
 - Pre Nothing
 - Post head has been allocated and initialized
 - Return head's address if successful, null if memory overflow.
1. if (memory available)
 - allocate (newPtr)
 - newPtr→front = null pointer
 - newPtr→rear = null pointer
 - newPtr→count = 0
 - return newPtr
 2. else
 - return null pointer
- end createQueue

Queue Algorithms - Enqueue

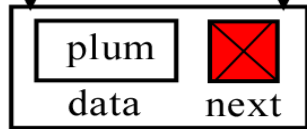
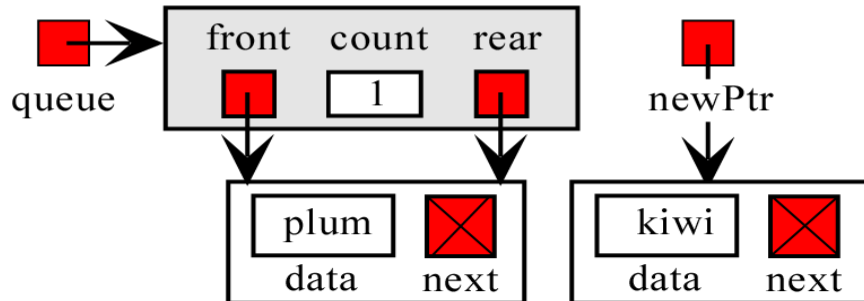


before

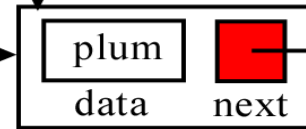
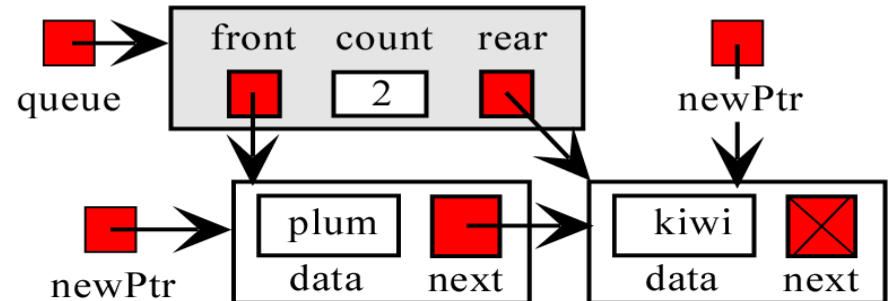


after

(a) Case 1: Insert into null queue



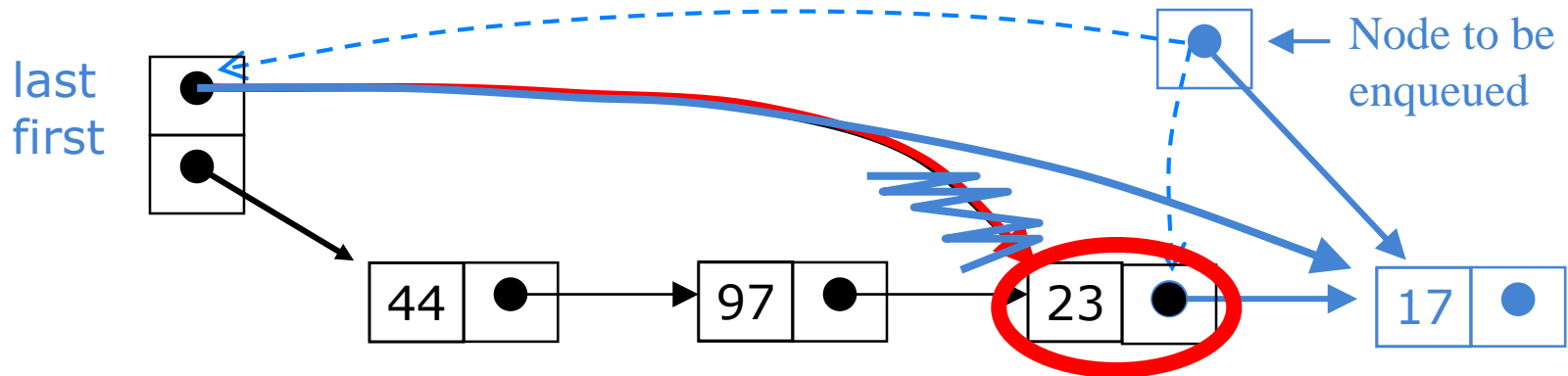
before



after

(b) Case 2: Insert into queue with data

Enqueueing a node



➤ To enqueue (add) a node:

- Find the current last node
- Change it to point to the new last node
- Change the last pointer in the list header

ALGORITHM FOR PUSHING AN ELEMENT TO A QUEUE

➤ REAR is a pointer in queue where the new elements are added. FRONT is a pointer, which is pointing to the queue where the elements are popped. DATA is an element to be pushed.

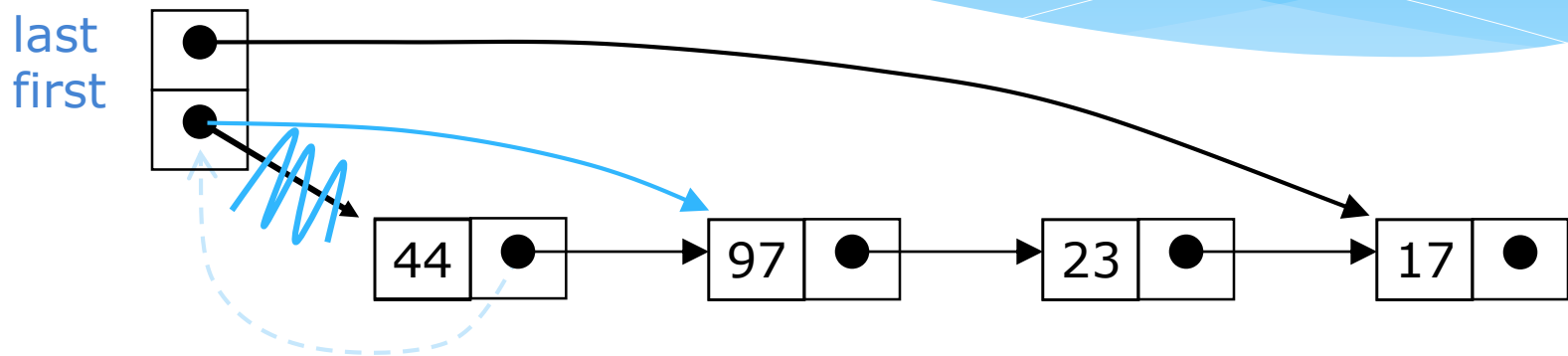
1. Input the DATA element to be pushed
2. Create a New Node
3. $\text{NewNode} \rightarrow \text{DATA} = \text{DATA}$
4. $\text{NewNode} \rightarrow \text{Next} = \text{NULL}$
5. If (REAR not equal to NULL)
(a) $\text{REAR} \rightarrow \text{next} = \text{NewNode};$
6. $\text{REAR} = \text{NewNode};$
7. Exit

PROGRAM FOR PUSHING AN ELEMENT TO A QUEUE

//This function will push an element into the queue

```
1.  NODE push(NODE rear)
2.  {
3.  NODE NewNode;           //New node is created to push the data
4.  printf ("\nEnter the no to be pushed = ");
5.  scanf ("%d",&NewNode->info);
6.  NewNode->next=NULL;
7.  if (rear != NULL)       //setting the rear pointer
    rear->next=NewNode;
8.  rear=NewNode;
9.  return(rear);
10. }
```

Dequeuing a node



- To dequeue (remove) a node:
 - Copy the pointer from the first node into the header

ALGORITHM FOR POPPING AN ELEMENT FROM A QUEUE

- REAR is a pointer in queue where the new elements are added. FRONT is a pointer, which is pointing to the queue where the elements are popped. DATA is an element popped from the queue.
- 1. If (FRONT is equal to NULL)
 - (a) Display “The Queue is empty”
- 2. Else
 - (a) Display “The popped element is FRONT → DATA”
 - (b) If(FRONT is not equal to REAR)
 - (i) FRONT = FRONT → Next
 - (c) Else
 - (d) FRONT = NULL;
- 3. Exit

OTHER QUEUES

- There are three major variations in a simple queue. They are
 1. Circular queue
 2. Double ended queue (de-queue)
 3. Priority queue

CIRCULAR QUEUE

- Suppose a queue Q has maximum size 5, say 5 elements pushed and 2 elements popped.

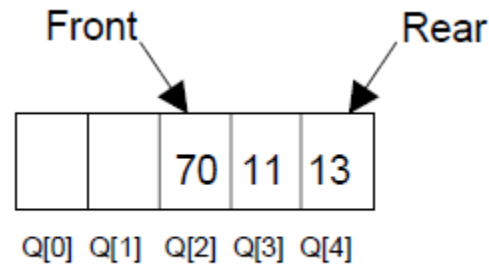


Fig. 4.10

- Rear is at last index
- New elements cannot be pushed

CIRCULAR QUEUE

- In circular queues the elements $Q[0], Q[1], Q[2] \dots Q[n - 1]$ is represented in a circular fashion with $Q[1]$ following $Q[n]$.
- A circular queue is one in which the insertion of a new element is done at the very first location of the queue if the last location at the queue is full.
- Suppose Q is a queue array of 6 elements. Push and pop operation can be performed on circular.

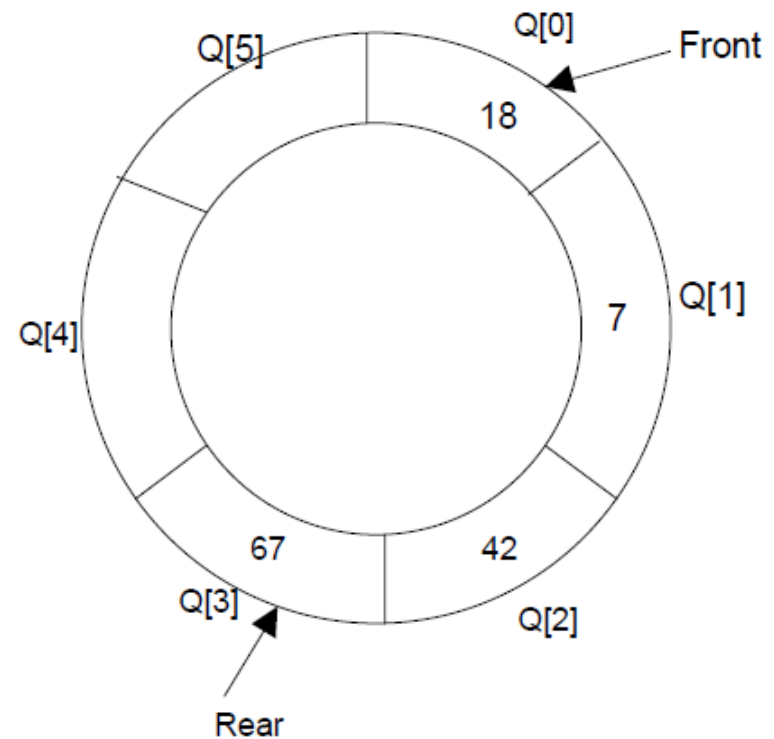


Fig. 4.11. A circular queue after inserting 18, 7, 42, 67.

CIRCULAR QUEUE

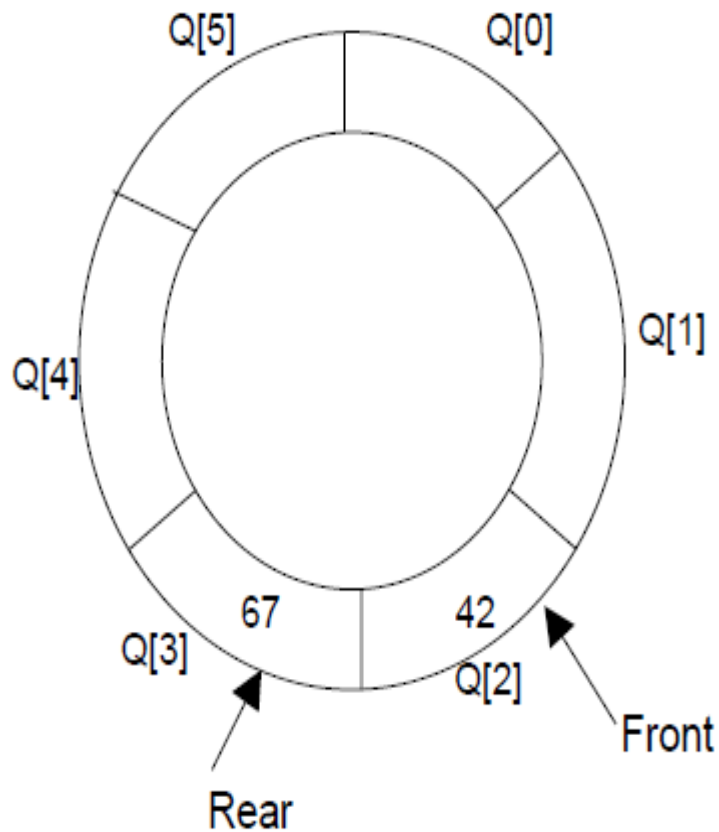


Fig. 4.12. A circular queue after popping 18, 7

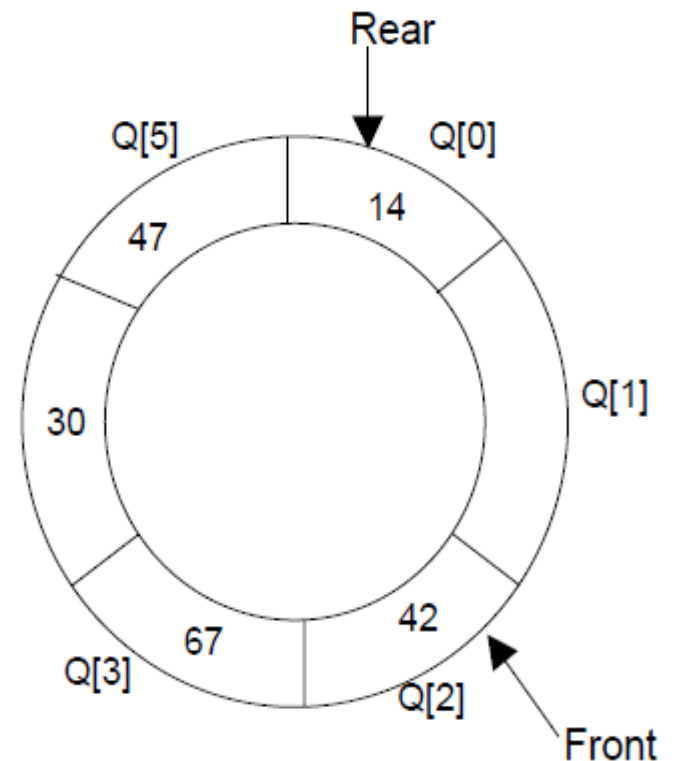


Fig. 4.13. A circular queue after pushing 30, 47, 14

CIRCULAR QUEUE

- At any time the position of the element to be inserted will be calculated by the relation **$\text{Rear} = (\text{Rear} + 1) \% \text{SIZE}$** .
- After deleting an element from circular queue the position of the front end is calculated by the relation **$\text{Front} = (\text{Front} + 1) \% \text{SIZE}$** .
- After locating the position of the new element to be inserted, *rear*, compare it with *front*. If **($\text{rear} = \text{front}$)**, the queue is full and cannot be inserted anymore.