

HOMEWORK 3

Guidelines:

- ② Attempt all questions by yourself before discussing with peers, this is practice to strengthen your concepts.
- ② For coding questions, try writing clean, readable code on paper.
- ② Since this homework is ungraded, focus on learning rather than using LLMs to generate codes and get answers.
- ② If you get stuck, you are encouraged to:
 - Post your doubts on the course Slack channel.
 - Visit the TAs during office hours for guidance.

Section A: Multiple Choice Questions (MCQs)

Q1. What is the worst-case time complexity of searching in a hash table with linear probing?

- a) $O(1)$
- b) $O(\log n)$
- c) $O(n)$
- d) $O(n \log n)$

Q2. Which of the following collision resolution strategies may lead to clustering?

- a) Linear Probing
- b) Quadratic Probing
- c) Separate Chaining
- d) Double Hashing

Q3. Which one of the following hash functions on integers will distribute keys most uniformly into 10 buckets (0–9) for keys ranging from 0 to 2020?

- a) $h(i) = i \bmod 10$
- b) $(i) = (7i+3) \bmod 8$
- c) $h(i) = (2i) \bmod 10$
- d) $h(i) = i \bmod 8$

Q4. Which of the following hash functions will distribute integers most uniformly into 12 buckets (0–11) for keys ranging from 0 to 5000?

- a) $h(k) = k \bmod 6$

- b) $h(k) = (7k+4) \bmod 12$
- c) $h(k) = (2k) \bmod 12$
- d) $h(k) = k \bmod 8$

Q5. Given the following input keys: 275, 123, 687, 543, 815, 927, 364, 482, and hash function $h(k) = k \bmod 10$, determine which keys hash to the same value.

Q6. A hash table of size 10 uses open addressing with hash function $h(k) = k \bmod 10$ and linear probing. After inserting 6 values, the table appears as follows:

Index	Value
0	
1	
2	42
3	52
4	34
5	33
6	23
7	46
8	—
9	—

Which of the following insertion orders could have resulted in this table?

- (a) 46, 33, 52, 23, 34, 42
- (b) 52, 46, 33, 42, 34, 46
- (c) 42, 52, 34, 33, 23, 46
- (d) 34, 33, 46, 52, 23, 42

Section B: Short Questions

Q1.. Insert the following keys into a hash table of size 10 using Linear Probing:

Keys = {12, 22, 42, 32, 52}

Show the final state of the table.

Q2. Given the following keys: 117, 124, 127, 155, 133, 144, 185, 186, 111

And hashing function: $K \bmod 9$

Construct the final hashed table of size 9, with open addressing and linear probing.

Q3. Given the same keys as before, but a hashing function: $2K \bmod 4$, use separate chaining on an array of pointers of size 4.

Q4.

20	17	10	22	31	4	15
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→ Determine the function that resulted in this table

→ Show the probing sequence for key 17

Q5. Write a C++ function that counts the frequency of elements in an array using an `unordered_map`

Q6. Consider a hash table with 100 slots. Collisions are resolved using chaining. Assuming simple uniform hashing, what is the probability that the first 3 slots are unfilled after the first 3 insertions?