

## CS1003 Mathematics, Taylor Series Tutorial Sheet

- Q1. Use the definition of a Taylor series to find the Taylor series about 2 for the function  $f(x) = x^{-1}$ . You are not expected to find the range of validity for this series.
- Q2. Use the binomial series to find the Taylor series about 0 for the function  $f(x) = (1+x)^5$ , and state a range of validity for the series.
- Q3. Use the binomial series to find the Taylor series about 0 for the function  $f(x) = \frac{1}{\sqrt[3]{1+x}}$ , simplifying each coefficient.
- Q4. By writing 1.25 as  $1 + 0.25$ , use the Taylor series for the function  $f(x) = \ln(1+x)$  about 0 to find a value for  $\ln(1.25)$  to three decimal places.
- Q5. Find the Taylor series about 0 for the function  $f(x) = \frac{1}{(1-4x^2)}$ . Determine a range of validity for this Taylor Series.
- Q6. By replacing  $x$  by  $x-2$  in the Taylor series about 0 for  $\ln(1+x)$ , find the Taylor series about 2 for the function  $\ln(x-1)$ . Determine a range of validity for this Taylor series.
- Q7. Find the quartic Taylor Polynomial about 0 for the function

$$f(x) = e^x \sin(-x)$$

evaluating each coefficient.

- Q8. Find the Taylor series about 0 for the function

$$\ln \frac{(1+x)}{(1-x)} = \ln(1+x) - \ln(1-x)$$

and determine the range of validity for this series.

- Q9. Find the value of  $x$  such that  $1.25 = \frac{(1+x)}{(1-x)}$ . Hence use the Taylor series found in Q8. to find a value for  $\ln(1.25)$  to three decimal places.
- Q10. Comment on whether the method of evaluating  $\ln(1.25)$  used in Q9. is better than the method used in Q4.