

# 1 What is Regularization?

- **Regularization** is a set of techniques used to reduce the complexity of a machine learning model and prevent it from overfitting the training data.
- Regularization adds a **penalty** to the model's **loss function**, discouraging it from fitting the training data too perfectly.
- Regularization works by adding a **regularization term** to the loss function (which the model tries to minimize).

## 1.1 Example

This is the original loss function (for example):

$$cost(W) = \frac{1}{2N} \sum_{i=1}^N (y(X^i, W) - t^i)^2 \quad (1)$$

After adding one of regularization types (ridge for example) it will be:

$$cost(W) = \frac{1}{2N} \sum_{i=1}^N (y(X^i, W) - t^i)^2 + \sum_{i=1}^M \left( \frac{\lambda}{2} \mathbf{w}_i^2 \right) \quad (2)$$

The new term is the **Regularization Term**.

Given one of the weights  $W_j$ , the partial derivative will be:

$$\frac{\partial cost(W)}{\partial W_j} = \frac{1}{N} \sum_{i=1}^N (y(X^i, W) - t^i)^2 * X_j^i + \lambda W_j \quad (3)$$

## 2 Ridge Regression

- We also call it L2 Regularization.
- Adds the squared magnitude of all weights to the loss function:

$$\text{Penalty} = \sum_{i=1}^M w_j^2 \quad (4)$$

- It encourages **smaller weights**.
- It keeps all features, but shrinks their influence.
- **Notice** that we started with  $i=1$ , which means we don't penalize the intercept at  $W_0$ .

### 3 Lasso Regression

- Adds the **absolute value** of weights to the loss function:

$$\text{Penalty} = \sum_j^M |w_j| \quad (5)$$

- Encourages **sparsity** — sets some weights to zero.
- Can be used for **feature selection**.