

CSE 221 (ALGORITHMS)

LAB 1

Submitted by Team: ALG0==FREAKS

Team Members:

Tasnia Zarin Shailee

ID: 19101145

sec: 01

Ishraq ahmed Esha

ID:19301261

sec: 01

Primality Testing

1. Naive approach:

```
bool prime [n]= {0};           // O(1)
void isPrime(int n)             // O(n²)
{
    for(int i=2;i<=n;i++){      // O(n²)
        int cnt = 0;
        for(int j=2;j<i;j++){
            if(i%j==0)cnt++;
        }
        if(cnt==0)prime[i]=1;
    }
    for(int i=2;i<=n;i++){      // O(n)
        if(prime[i])
            System.out.print(i+" ");
    }
}
```

Worst time complexity calculation:

$T(n)=O(1)+O(n^2)+O(n)$

$T(n)=O(n^2)$

[Answer]

2. Optimal Sieve

```
void sieveOfEratosthenes(int n)
{
    boolean prime[] = new boolean[n+1]; // O(1)
    for(int i=0;i<n;i++) //O(n)
        prime[i] = true;
    for(int p = 2; p<=sqrt(n); p++) //O(n log log n)
    {
        // If prime[p] is not changed, then it is a prime
        if(prime[p] == true)
        {
            // Update all multiples of p
            for(int i = p*p; i <= n; i += p)
                prime[i] = false;
        }
    }
    // Print all prime numbers
    for(int i = 2; i <= n; i++) //O(n)
    {
        if(prime[i] == true)
            System.out.print(i + " ");
    }
}
```

Worst time complexity calculation:

$T(n)=O(1)+O(n)+O(n \log \log n)O(n)$

$T(n)=O(n \log \log n)$

[Answer]

Recursion Tree Time Complexity

1. $T(n) = T(n/2) + n - 1, T(1) = 0$

We know Master Theorem, $T(n) = aT(n/b) + cn^k$

$$T(n) = T(n/2) + n - 1;$$

Here, $a=1, b=2, c=1, k=1$;

$$b^k = 2^1 = 2; a=1;$$

$$b^k > a$$

We know that if $b^k > a$,

Then time complexity = $O(n^k)$

$$\text{So, } O(n^1) = O(n)$$

Worst time Complexity = $O(n)$

2. $T(n) = T(n-1) + n - 1, T(1) = 0$

$$T(n) = T(n-1) + n - 1$$

$$= T(n-2) + (n-1) + (n-1)$$

$$= T(n-3) + (n-2) + (n-1) + (n-1)$$

$$= \dots$$

$$\text{So, } T(n) = 1 + 2 + 3 + \dots + (n-3) + (n-2) + (n-1)$$

$$= n(n+1)/2$$

$$= n^2 + n/2$$

$$= O(n^2)$$

Worst time Complexity = $O(n^2)$

3. $T(n)=T(n/3)+2T(n/3)+n$

$$=3T(n/3) + n$$

$$\text{Then, } 3T(n/3) = 3^2T(n/3^2) + 3(n/3)$$

$$3^2T(n/3^2) = 3^3T(n/3^3) + 3^2(n/3^2)$$

.....

$$3^kT(n/3^k) = 3^{k+1}T(n/3^{k+1}) + 3^k(n/3^k)$$

$$\text{Considering, } n/3^{k+1}=1$$

$$\text{So, } k+1 = \log_3 n$$

Adding,

$$T(n) = 3\log_3 n + (n + n + n + \dots + n)$$

$$T(n) = n + (n \cdot \log_3 n)$$

$$= O(n \log_3 n)$$

Worst time Complexity = $O(n \log_3 n)$

4. $T(n) = 2T(n/2) + n^2$

We know Master Theorem, $T(n) = aT(n/b) + cn^k$

$$T(n) = 2T(n/2) + n^2;$$

$$\text{Here, } a=2, b=2, c=1, k=2;$$

$$b^k = 2^2 = 4; a=2;$$

$$b^k > a$$

We know that if $b^k > a$,

$$\text{Then time complexity} = O(n^k)$$

$$\text{So, } O(n^2)$$

Worst time complexity = $O(n^2)$

Pseudocode to Coding

```
import java.util.Scanner;
public class Lab1{
    public static void main(String []args){
        Scanner sc= new Scanner(System.in);
        int n=sc.nextInt();
        int a=n;
        int sum=0;
        while (n>0){
            int r=n%10;
            sum=sum+r*r*r;
            n=n/10;
        }
        if(a==sum){
            System.out.println("Armstrong Number");
        }
        else{
            System.out.println("not an Armstrong Number");
        }
    }
}
```