



**Course: Compilers**  
**Duration: 1 hour**  
**Date: 19 November 2022**

Student ID: \_\_\_\_\_

## Question 2 (10 points)

Consider the grammar:

$$\langle S \rangle \rightarrow a\langle S \rangle b\langle S \rangle \mid b\langle S \rangle a\langle S \rangle \mid \varepsilon$$

- A. Is that grammar ambiguous ? **YES**
- B. IF the answer is Yes, Prove a string that shows such ambiguity and prove it through providing **two distinct leftmost derivations** for the match of the above string.

**YES: String example is abab**

**First derivation:**

$\langle S \rangle \longrightarrow a\langle S \rangle b\langle S \rangle$

$\langle S \rangle \longrightarrow ab\langle S \rangle$

$\langle S \rangle \longrightarrow aba\langle S \rangle b\langle S \rangle$

$\langle S \rangle \longrightarrow abab\langle S \rangle$

$\langle S \rangle \longrightarrow abab$

**Second derivation:**

$\langle S \rangle \longrightarrow a\langle S \rangle b\langle S \rangle$

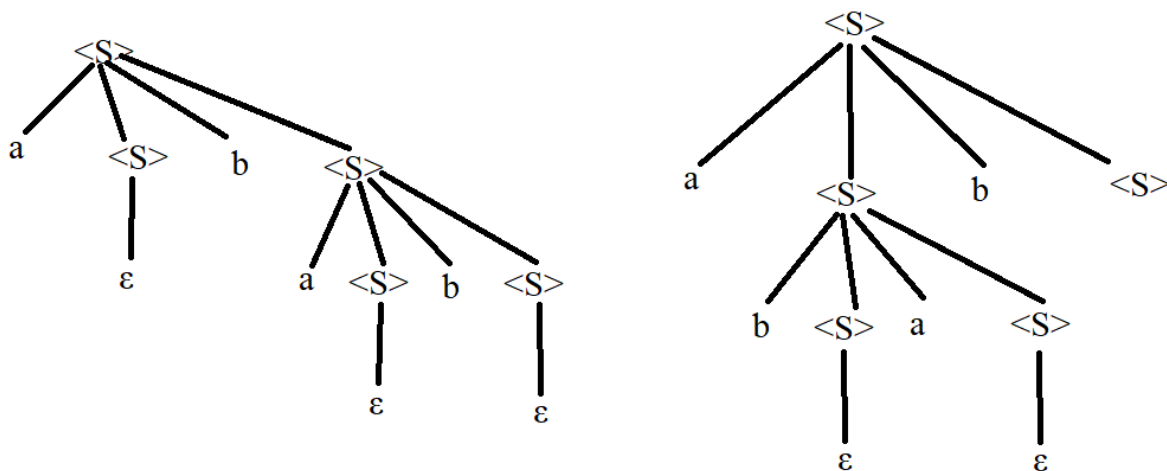
$\langle S \rangle \longrightarrow ab\langle S \rangle a\langle S \rangle b\langle S \rangle$

$\langle S \rangle \longrightarrow aba\langle S \rangle b\langle S \rangle$

$\langle S \rangle \longrightarrow abab\langle S \rangle$

$\langle S \rangle \longrightarrow abab$

- C. Draw the corresponding parse trees for your derivations.



### Question 3 (5 points)

Given  $\Sigma = \{a, b, c\}$  write a regular expression that matches the following language if possible and if not, Please explain why then suggest another way that could be used to match it:

**A. A set of all strings that contains at most one b.**

**$(a|c)^*(b|\epsilon)(a|c)^*$**

**B. A set of all strings that contains no two consecutive b's.**

**$(a|c|ba|bc)^*(b|\epsilon)$**

**C. A set of strings of two b's surrounded by the same number of a's.**

**It's not possible to express such language with regular expression since the regular expression couldn't count we could use BNF or Context free grammar to express it as follow:**

**$\langle G \rangle \longrightarrow a \langle G \rangle a \mid bb$**