Machine learning

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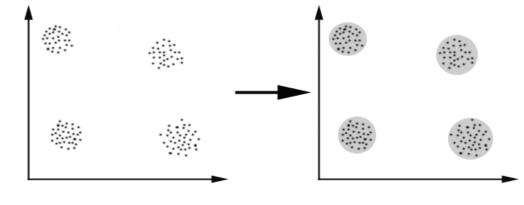


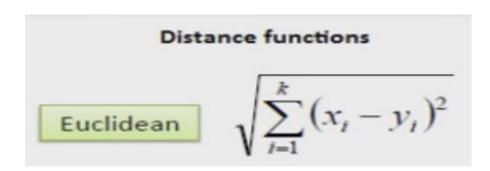
CLUSTERING

- Cluster Analysis is like Classification, but the class label of each object is not known.
- •Clustering can be considered the most <u>important unsupervised learning problem</u>; so, as every other problem of this kind, it deals with <u>finding a structure in a collection of unlabeled data</u>.
- Cluster is a subset of data which are similar
- **Clustering** is the *process of grouping the data into classes or clusters* so that objects within a cluster have high similarity in comparison to one another, but are very dissimilar to objects in other clusters.

SIMPLE GRAPHICAL EXAMPLE:

• In this case we easily identify the 4 clusters into which the data can be divided; the similarity criterion is *distance*: two or more objects belong to the same cluster if they are "close" according to a given distance. This is called *distance-based clustering*.





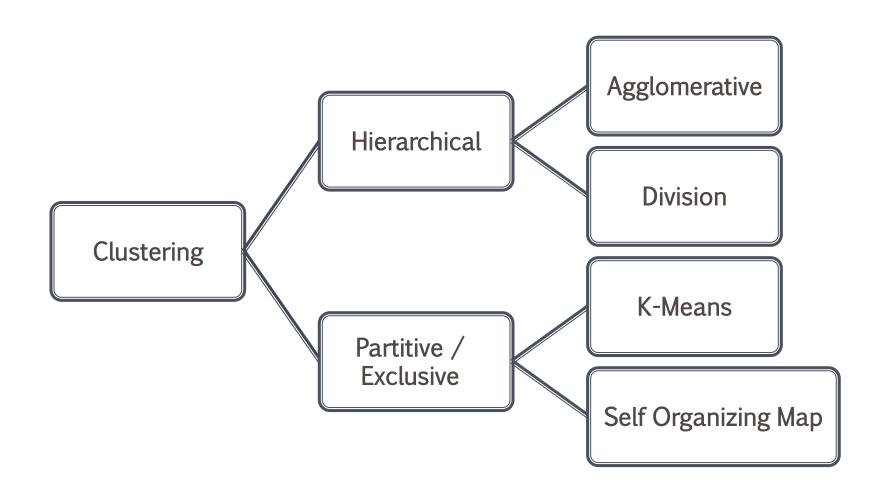
$$\sum_{i=1}^{k} |x_i - y_i|$$

Minkowski
$$\left(\sum_{i=1}^{k} (|x_i - y_i|)^q\right)^{1/q}$$

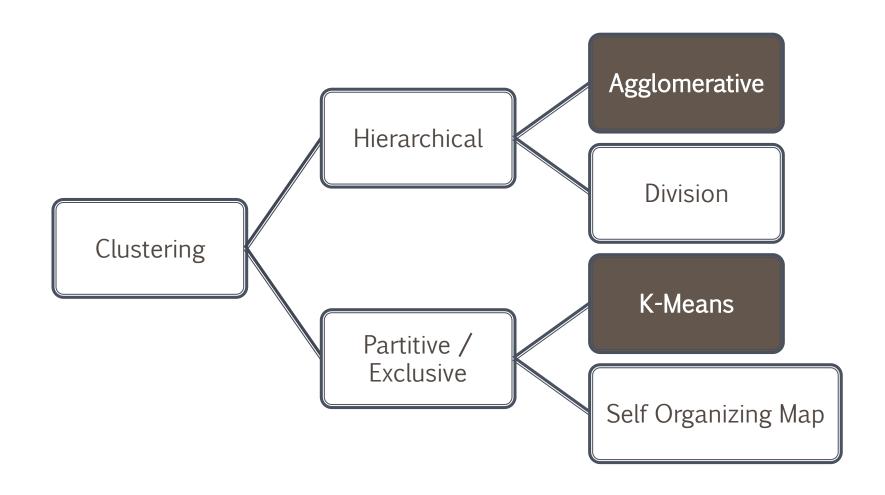
APPLICATIONS OF CLUSTERING

- Marketing: finding groups of customers with similar behavior given a large database of customer data containing their properties and past buying records;
- Biology: classification of plants and animals given their features;
- Libraries: book ordering;
- Insurance: identifying groups of motor insurance policy holders with a high average claim cost; identifying frauds;
- City-planning: identifying groups of houses according to their house type, value and geographical location;
- Earthquake studies: clustering observed earthquake epicenters to identify dangerous zones;
- WWW: document classification; clustering weblog data to discover groups of similar access patterns.

Two main groups of clustering algorithms



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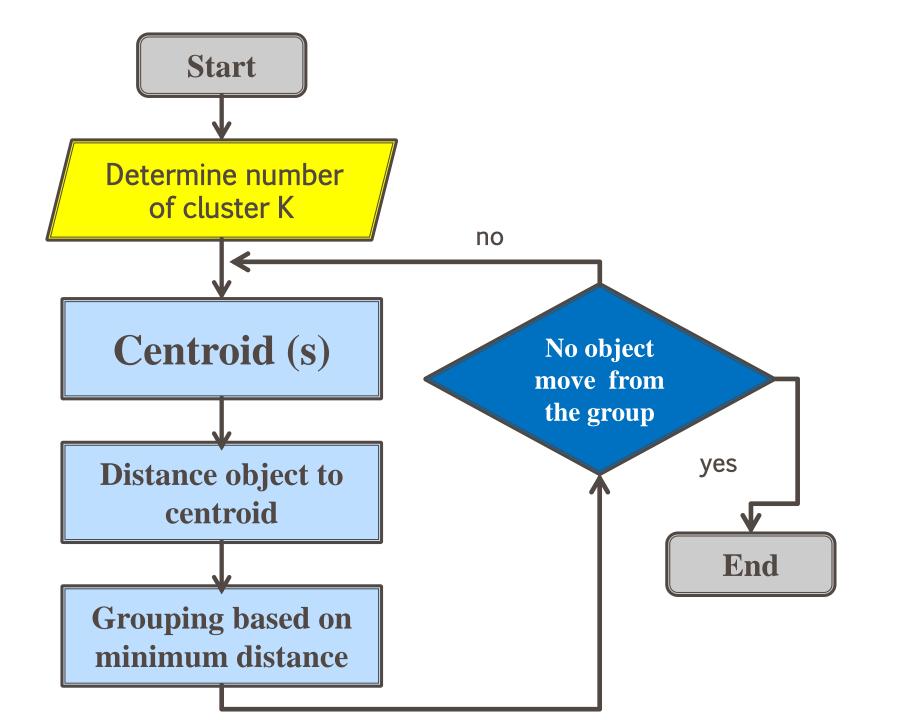
K-MEANS CLUSTERING

- Intends to partition n objects into k clusters in which <u>each</u> object belongs to the cluster with the nearest mean
- This method produces exactly k different clusters of greatest possible distinction
- The best number of clusters k leading to the greatest separation (distance) is not known as a priori and must be computed from the data

K-means Clustering algorithm

- Partitional clustering approach
- Each cluster is associated with a centroid (center point)
- Each point is assigned to the cluster with the closest centroid
- Number of clusters, K, must be specified
- The basic algorithm is very simple

- 1: Select K points as the initial centroids.
- 2: repeat
- 3: Form K clusters by assigning all points to the closest centroid.
- 4: Recompute the centroid of each cluster.
- 5: **until** The centroids don't change



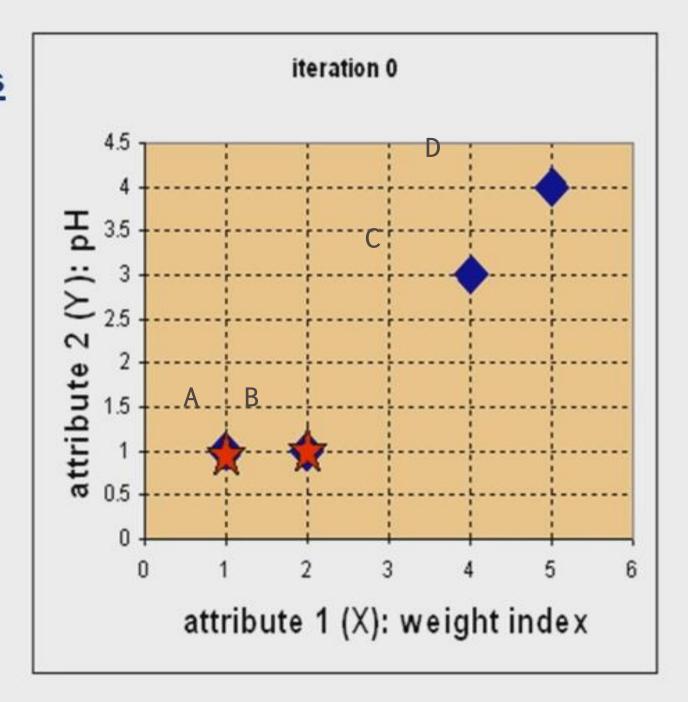
Real-Life Numerical Example of K-Means Clustering

We have 4 medicines as our training data points object and each medicine has 2 attributes. Each attribute represents coordinate of the object. We have to determine which medicines belong to cluster 1 and which medicines belong to the other cluster.

Object	Attribute1 (X): weight index	Attribute 2 (Y): pH	
Medicine A	1	1	
Medicine B	2	1	
Medicine C	4	3	
Medicine D	5	4	

Step 1:

- Initial value of centroids
 - : Suppose we use medicine A and medicine B as the first centroids.
- Let and c₁ and c₂ denote the coordinate of the centroids, then c₁=(1,1) and c₂=(2,1)



•Object Centroid distance: calculate the distance between each cluster centroid and each point using Euclidean distance

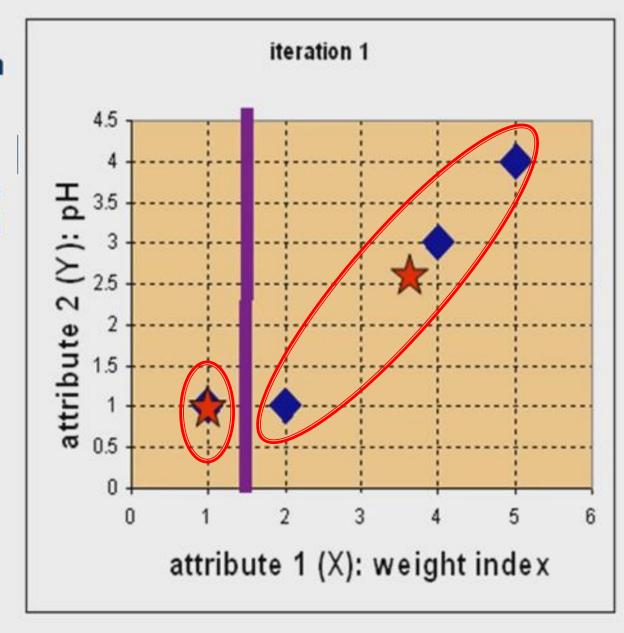
$$\sqrt{\sum_{i=1}^{k} (x_i - y_i)^2}$$

For example, distance from medicine C = (4, 3) to the first centroid $\epsilon_1 = (1,1)$ is $\sqrt{(4-1)^2 + (3-1)^2} = 3.61$ and its distance to the second centroid is, $\epsilon_2 = (2.1)$ is $\sqrt{(4-2)^2 + (3-1)^2} = 2.83$ etc.

Step 2:

- Objects clustering: We assign each object based on the minimum distance.
- Medicine A is assigned to group 1, medicine B to group 2, medicine C to group 2 and medicine D to group 2.
- The elements of Group matrix below is 1 if and only if the object is assigned to that group.

$$\mathbf{G}^{0} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 1 \end{bmatrix} \quad \begin{array}{c} group - 1 \\ group - 2 \end{array}$$



- Iteration-1, Objects-Centroids distances: The next step is to compute the distance of all objects to the new centroids.
- Similar to step 2, we have distance matrix at iteration 1 is

$$\mathbf{D}^{1} = \begin{bmatrix} 0 & 1 & 3.61 & 5 \\ 3.14 & 2.36 & 0.47 & 1.89 \end{bmatrix} \quad \mathbf{c}_{1} = (1,1) \quad group - 1 \\ \mathbf{c}_{2} = (\frac{11}{3}, \frac{8}{3}) \quad group - 2$$

A B C D

$$x \begin{bmatrix} 1 & 2 & 4 & 5 \\ 1 & 1 & 3 & 4 \end{bmatrix}$$
 $c_2 x = \frac{2+4+5}{3} = \frac{11}{3}$
 $c_2 y = \frac{1+3+4}{3} = \frac{8}{3}$

clustering: Based on the new distance matrix, we move the medicine B to Group 1 while all the other objects remain. The Group matrix is shown below

$$\mathbf{G}^{1} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix} \quad \begin{array}{c} group - 1 \\ group - 2 \end{array}$$

$$A \quad B \quad C \quad D$$

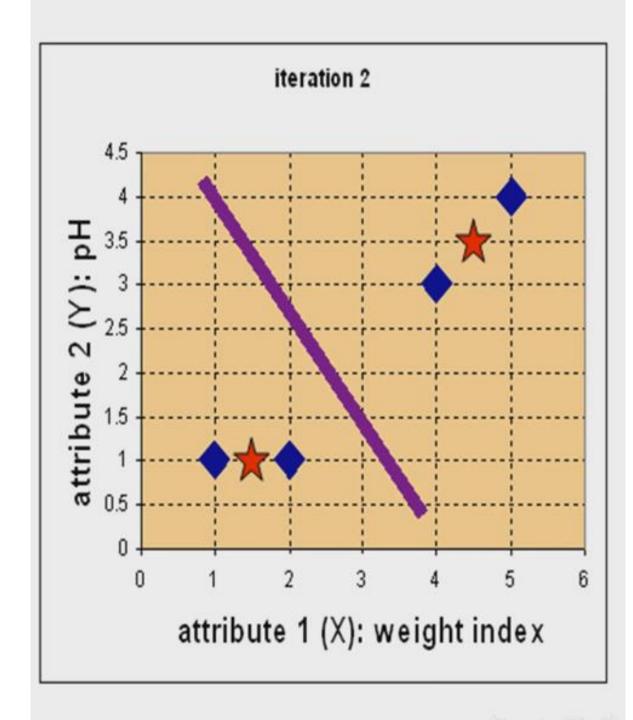
Compare

$$\mathbf{G}^{0} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 1 \end{bmatrix} \quad \begin{array}{c} group - 1 \\ group - 2 \end{array}$$

$$A \quad B \quad C \quad D$$

$$\mathbf{G}^{1} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix} \quad \begin{array}{c} group - 1 \\ group - 2 \end{array}$$

$$A \quad B \quad C \quad D$$

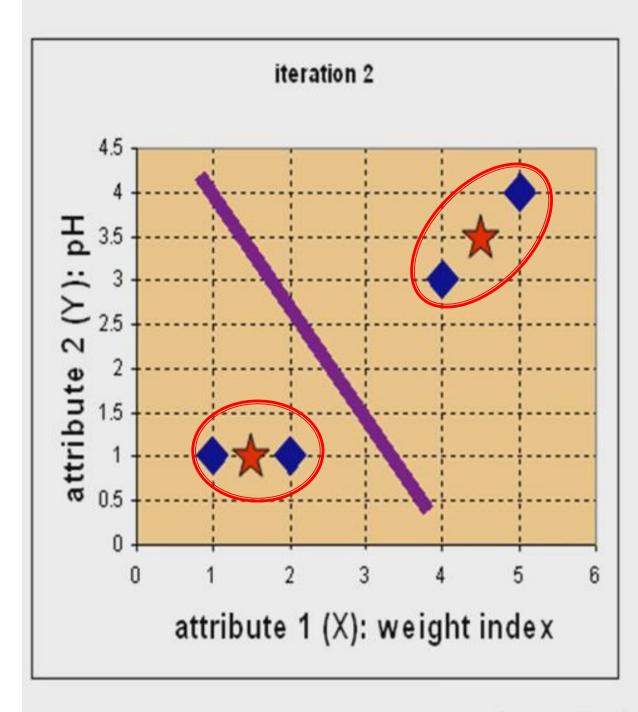


Iteration-1, Objects clustering: Based on the new distance matrix, we move the medicine B to Group 1 while all the other objects remain. The Group matrix is shown below

$$\mathbf{G}^{1} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix} \quad \begin{array}{c} group - 1 \\ group - 2 \end{array}$$

$$A \quad B \quad C \quad D$$

Now we repeat step 4 to calculate the new centroids coordinate based on the clustering of previous iteration. Group1 and group 2 both has two members, thus the new centroids are $c_1 = (\frac{1+2}{2}, \frac{1+1}{2}) = (1\frac{1}{2}, 1)$ and $c_2 = (\frac{4+5}{2}, \frac{3+4}{2}) = (4\frac{1}{2}, 3\frac{1}{2})$



•<u>Iteration-2:Object Centroid distance:</u> calculate the distance between each cluster centroid and each point

 Iteration-2, Objects clustering: Again, we assign each object based on the minimum distance.

$$\mathbf{G}^{2} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix} \quad \begin{array}{c} group - 1 \\ group - 2 \end{array}$$

$$A \quad B \quad C \quad D$$

Compare

$$\mathbf{G}^{1} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix} \quad \begin{array}{ccc} group - 1 \\ group - 2 \\ A & B & C & D \end{array}$$

$$\mathbf{G}^{2} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix} \quad \begin{array}{c} group - 1 \\ group - 2 \\ A & B & C & D \end{array}$$

- We obtain result that G² = G¹ Comparing the grouping of last iteration and this iteration reveals that the objects does not move group anymore.
- Thus, the computation of the k-mean clustering has reached its stability and no more iteration is needed...

We get the final grouping as the results as:

<u>Object</u>	Feature1(X): weight index	<u>Feature2</u> (Y): pH	<u>Group</u> (result)
Medicine A	1	1	1
Medicine B	2	1	1
Medicine C	4	3	2
Medicine D	5	4	2

K-means Clustering – Details

- Initial centroids are often chosen randomly.
 - Clusters produced vary from one run to another.
- The centroid is (typically) the mean of the points in the cluster.
- 'Closeness' is measured by Euclidean distance, cosine similarity, correlation, etc.
- K-means will converge for common similarity measures mentioned above.

K-means Clustering – Details

- Most of the convergence happens in the first few iterations.
 - Often the stopping condition is changed to 'Until relatively few points change clusters'
- Complexity is O(n * K * I * d)
 - n = number of points, K = number of clusters,
 I = number of iterations, d = number of attributes

COMPLEXITY

 In each round, we have to examine each input point exactly once to find closest centroid

Each round is O(kN) for N points, k clusters

 But the number of rounds to convergence can be very large!

The K-Means Clustering Method

<u>Strength</u>

- · Relatively efficient. O(tkn),
 - · *n* is # objects,
 - · k is # clusters
 - *t* is # iterations.

Normally, k, $t \ll n$.

<u>Weakness</u>

- · Applicable only when *mean* is defined (e.g., a vector space)
- · Need to specify *k*, the *number* of clusters, in advance.
- · It is sensitive to noisy data and *outliers* since a small number of such data can substantially influence the mean value.