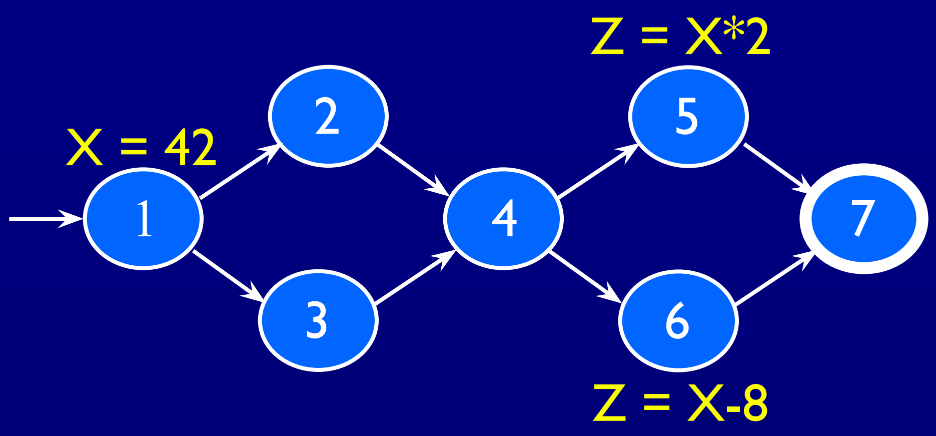
Data Flow Criteria

Goal : Ensure that values are computed and used correctly

- Definition (def) : A location where a value for a variable is stored into memory
- Use : A location where a variable's value is accessed



Defs: def (1) = { **X** }

def (5) = { **Z** }

def (6) = { **Z** }

Uses: use (5) = { **X** }

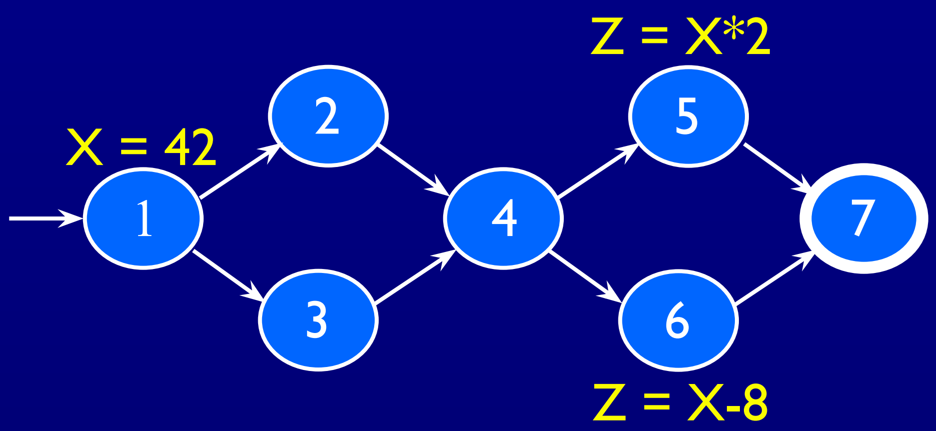
use (6) = { **X** }

Fill in these sets

The values given in defs should reach at least one, some, or all possible uses

Data Flow Criteria

- du-path : A simple subpath that is def-clear with respect to *v* from a def of *v* to a use of *v* -□ *{1,2,4,5} or {1,2,4,6}*
- du (n_i, n_j, v) – the set of du-paths from n_i to n_j □ *{ {1,2,4,5} , [1,2 4,6} }*
- du (n_i, v) – the set of du-paths that start at n_i



<u>Defs</u>: def (1) = { **X** }

def (5) = { **Z** }

def (6) = { **Z** }

<u>Uses</u>: use (5) = { **X** }

use (6) = { **X** }

Fill in these sets

The values given in defs should reach at least one, some, or all possible uses

DU Pairs and DU Paths

- def (n) or def (e) : The set of variables that are defined by node n or edge e
- use (n) or use (e) : The set of variables that are used by node n or edge e

- DU pair : A pair of locations (l_i, l_j) such that a variable *v* is defined at l_i and used at l_j

- Def-clear : A path from l_i to l_j is *def-clear* with respect to variable *v* if *v* is not given another value on any of the nodes or edges in the path
- Reach : If there is a def-clear path from l_i to l_j with respect to *v*, the def of *v* at l_i reaches the use at l_j

- du-path : A simple subpath that is def-clear with respect to *v* from a def of *v* to a use of *v*
- du (n_i, n_j, *v*) – the set of du-paths from n_i to n_j
- du (n_i, *v*) – the set of du-paths that start at n_i

Touring DU-Paths

- A test path *p* *du-tours* subpath *d* with respect to *v* if *p* tours *d* and the subpath taken is def-clear with respect to *v*
- Sidetrips can be used, just as with previous touring
- Three criteria
  - Use every def
  - Get to every use
  - Follow all du-paths

Data Flow Test Criteria

- First, we make sure every def reaches a use

<u>All-defs coverage (ADC)</u> : For each set of du-paths *S* = *du* (*n*, *v*), TR contains at least one path *d* in *S*.

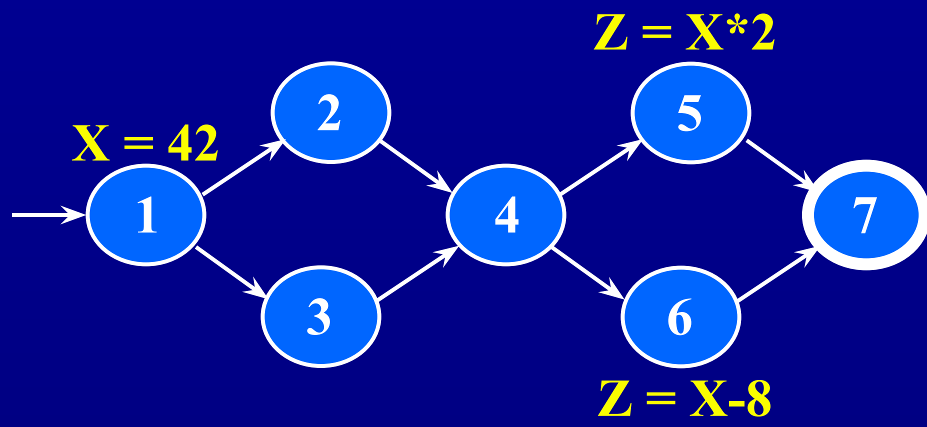
- Then we make sure that every def reaches all possible uses

<u>All-uses coverage (AUC)</u> : For each set of du-paths to uses *S* = *du* (n_i, n_j, *v*), TR contains at least one path *d* in *S*.

- Finally, we cover all the paths between defs and uses

<u>All-du-paths coverage (ADUPC)</u> : For each set *S* = *du* (*ni*, *nj*, *v*), TR contains every path *d* in *S*.

Data Flow Testing Example



All-defs for *X*

Write down paths to satisfy ADC

All-uses for *X*

[1, 2, 4, 5]

Write down paths to satisfy AUC

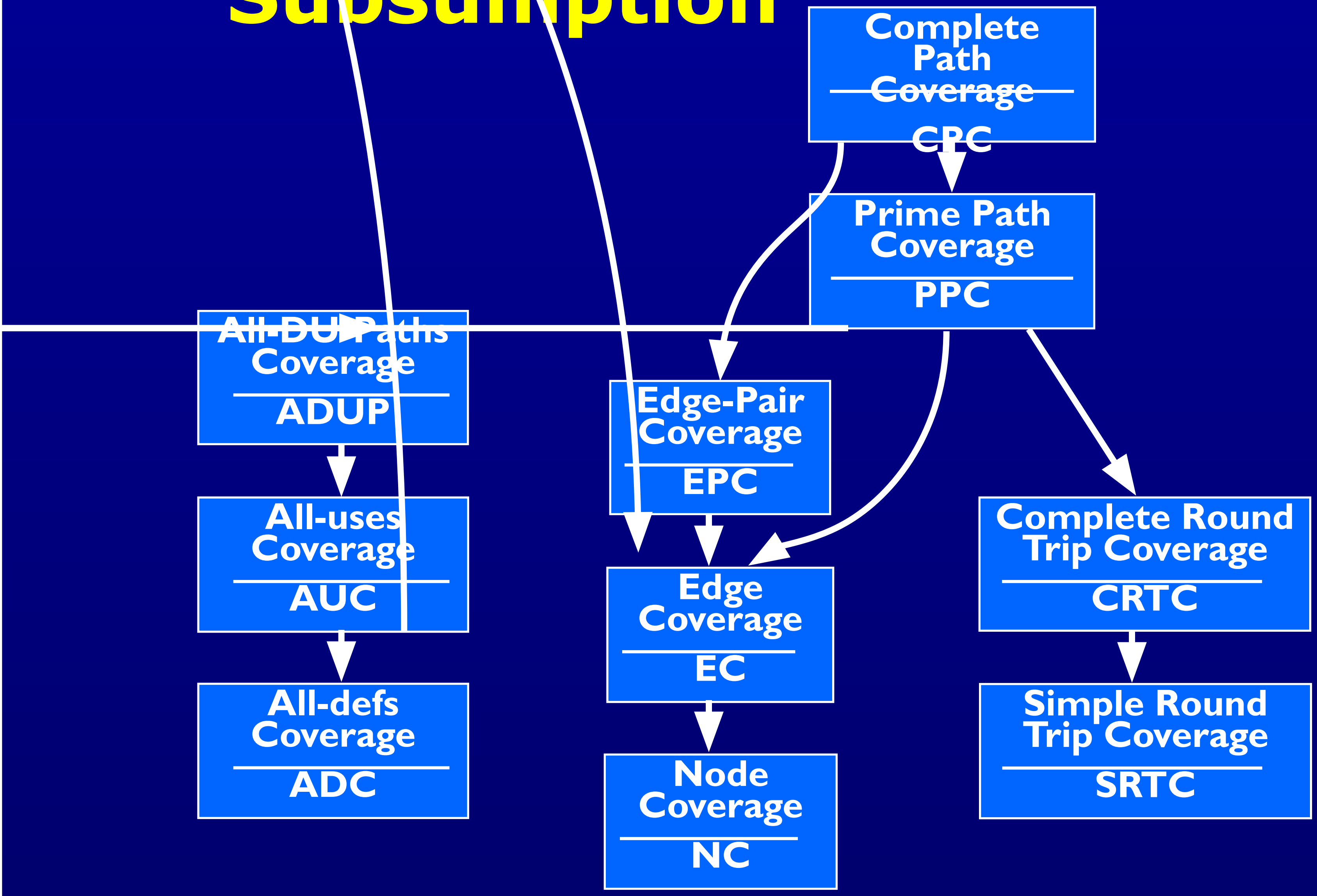
All-du-paths for *X*

[1, 2, 4, 5]

Write down paths to satisfy ADUPC

[1, 3, 4, 6]

Graph Coverage Criteria Subsumption



Summary 7.1-7.2

- Graphs are a very powerful abstraction for designing tests
- The various criteria allow lots of cost / benefit tradeoffs
- These two sections are entirely at the "design abstraction level" from chapter 2
- Graphs appear in many situations in software
  – As discussed in the rest of chapter 7

Introduction to Software Testing
Chapter 7.3
Graph Coverage for Source Code

Paul Ammann & Jeff Offutt

http://www.cs.gmu.edu/~offutt/softwaretest/

Update March 2016

Overview

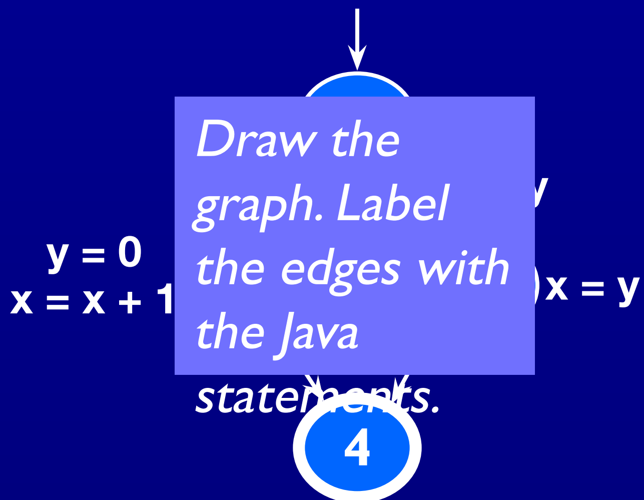
- A common application of graph criteria is to program source
- Graph : Usually the control flow graph (CFG)
- Node coverage : Execute every statement
- Edge coverage : Execute every branch
- Loops : Looping structures such as for loops, while loops, etc.
- Data flow coverage : Augment the CFG
  - defs are statements that assign values to variables
  - uses are statements that use variables

Control Flow Graphs

- A CFG models all executions of a method by describing control structures
- Nodes : Statements or sequences of statements (basic blocks)
- Edges : Transfers of control
- Basic Block : A sequence of statements such that if the first statement is executed, all statements will be (no branches)
- CFGs are sometimes annotated with extra information
  – branch predicates
  – defs
  – uses
- Rules for translating statements into graphs …

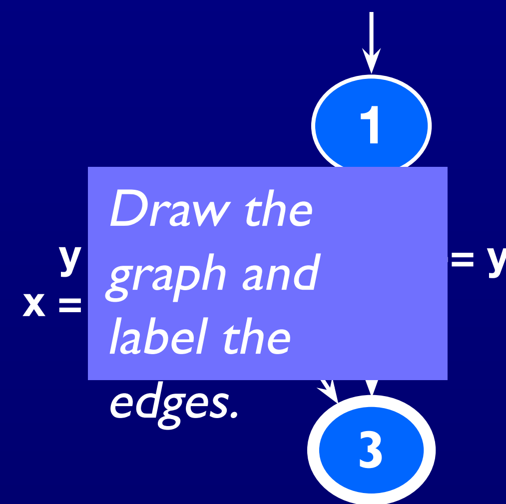
CFG : The if Statement

```
if (x < y)
{
   y = 0;
   x = x + 1;
}
else
{
   x = y;
}
```



Draw the graph. Label the edges with the Java statements.

```
if (x < y)
{
   y = 0;
   x = x + 1;
}
```

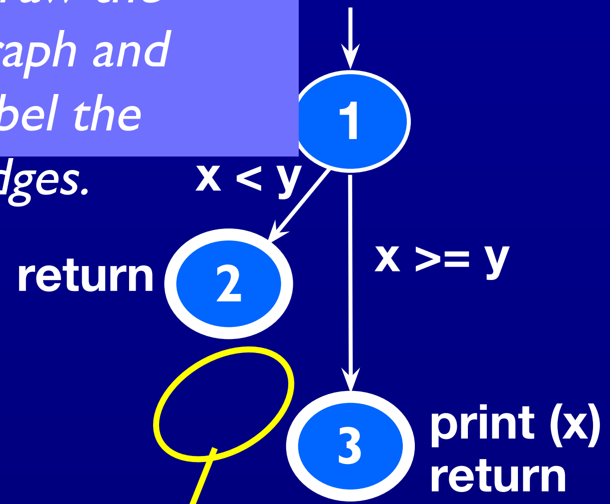


Draw the graph and label the edges.

CFG : The if-Return Statement

```
if (x < y)
{
   return;
}
print (x);
return;
```

Draw the graph and label the edges.



No edge from node 2 to 3.
The return nodes must be distinct.

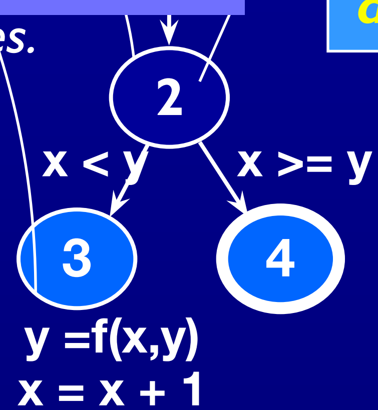
Loops

- Loops require "*extra*" nodes to be added
- Nodes that do not represent statements or basic blocks

CFG : while and for Loops

```
x = 0;
while (x < y)
{
   y = f (x, y);
   x = x + 1;
}
return (x);
```

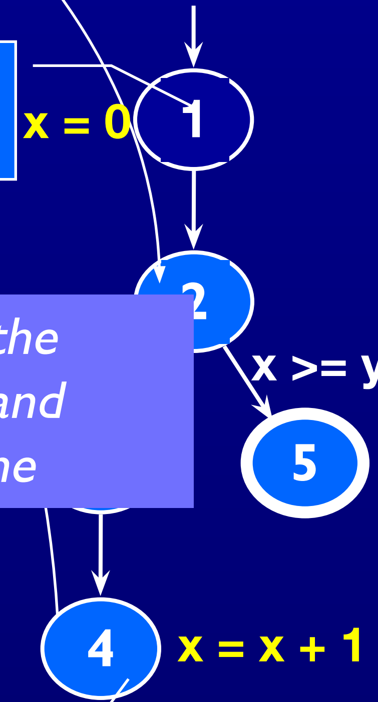
Draw the graph and label the edges.



dummy node

```
for (x = 0; x < y; x++)
{
   y = f (x, y);
}
return (x);
```

implicitly initializes loop

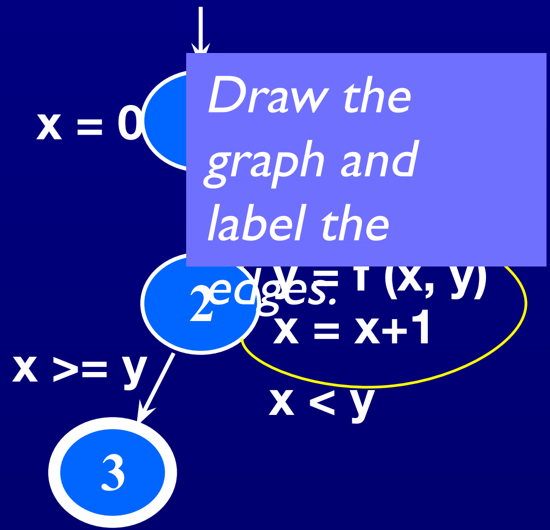


Draw the graph and label the edges.

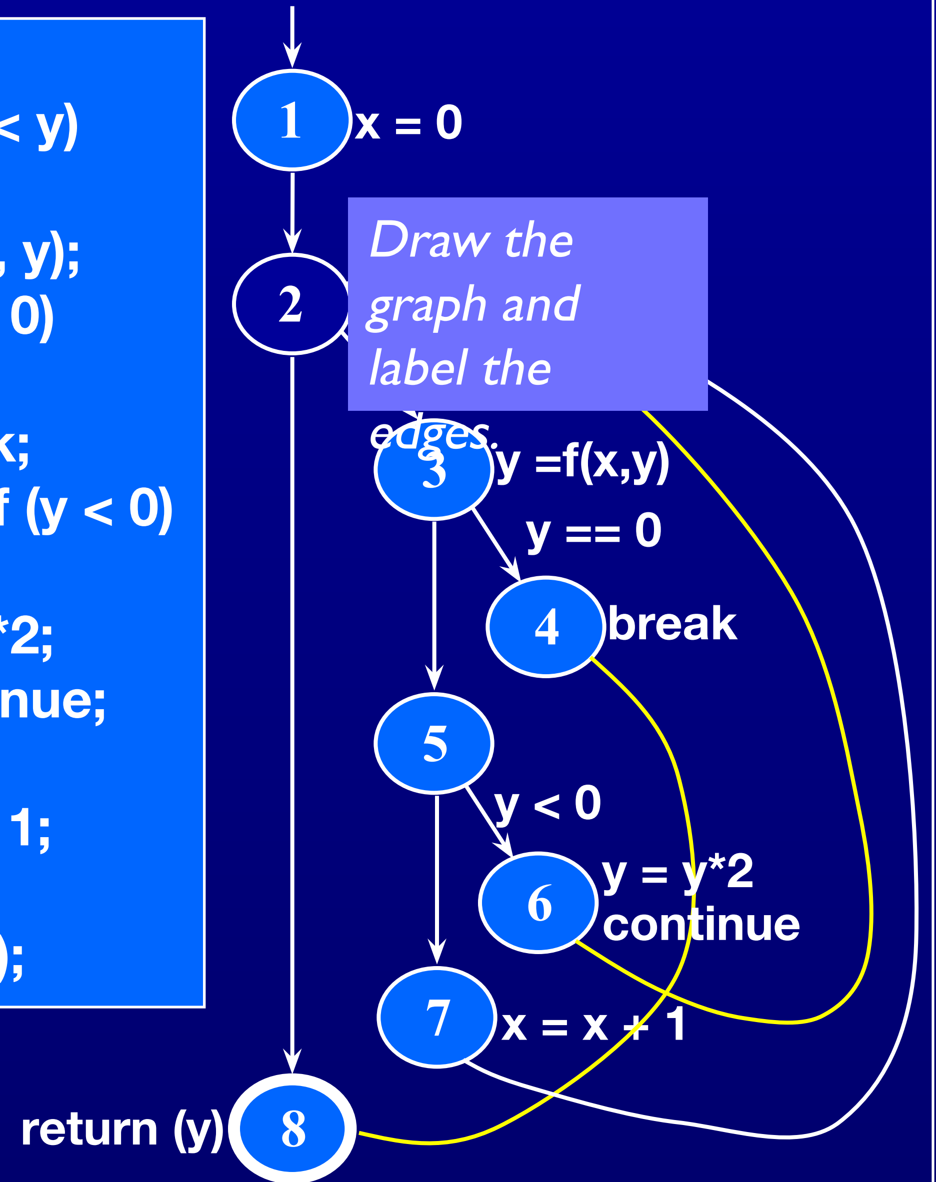
implicitly increments loop

CFG : do Loop, break and continue

```
x = 0;
do
{
   y = f (x, y);
   x = x + 1;
} while (x < y);
return (y);
```



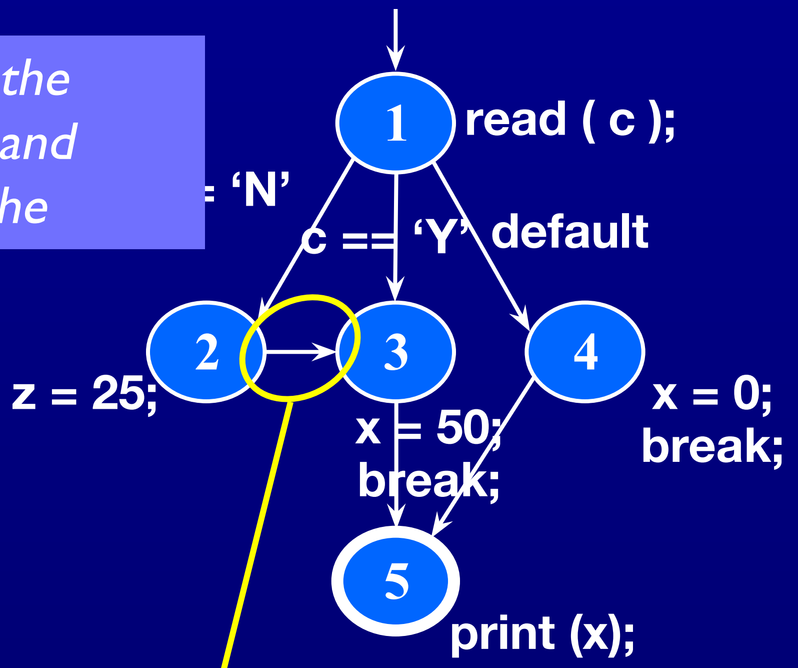

```
x = 0;
while (x < y)
{
   y = f (x, y);
   if (y == 0)
   {
      break;
   } else if (y < 0)
   {
      y = y*2;
      continue;
   }
   x = x + 1;
}
return (y);
```



CFG : The case (switch) Structure

```
read ( c) ;
switch ( c )
{
   case ‘N’:
      z = 25;
   case ‘Y’:
      x = 50;
      break;
   default:
      x = 0;
      break;
}
print (x);
```

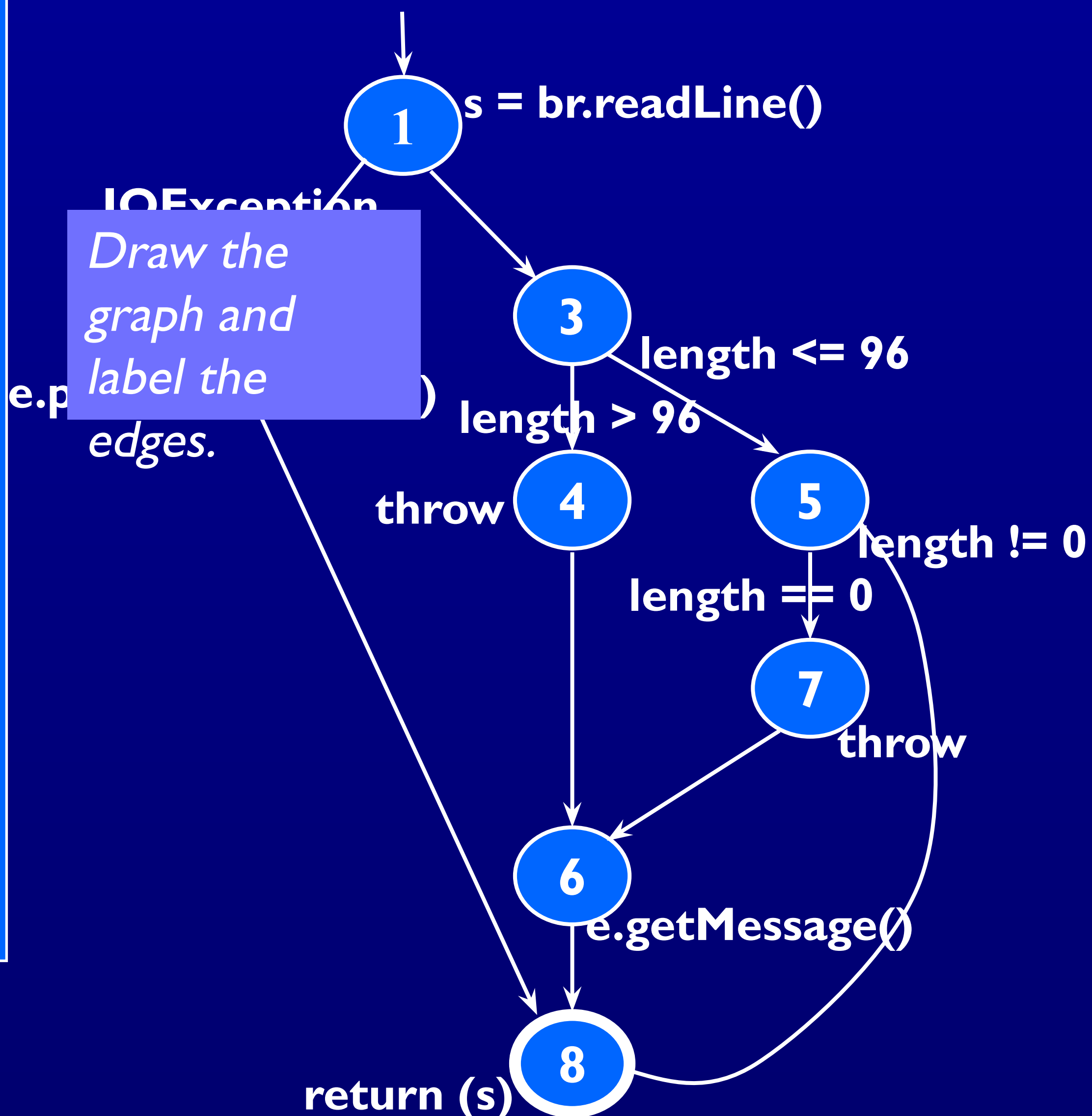
Draw the graph and label the edges.



Cases without breaks fall through to the next case

CFG : Exceptions (try-catch)

```
try
{
   s = br.readLine();
   if (s.length() > 96)
      throw new Exception
         ("too long");
   if (s.length() == 0)
      throw new Exception
         ("too short");
} (catch IOException e) {
   e.printStackTrace();
} (catch Exception e) {
   e.getMessage();
}
return (s);
```



Draw the graph and label the edges.

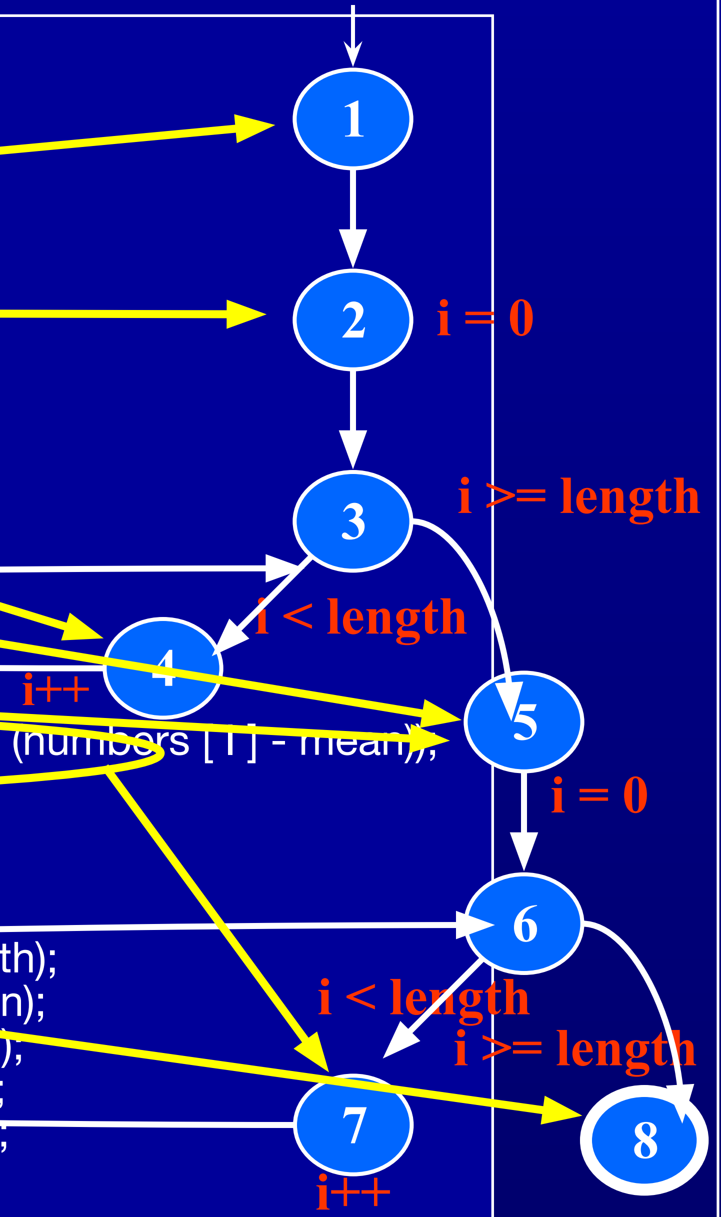
Example Control Flow – Stats

```
public static void computeStats (int [ ] numbers)
{
    int length = numbers.length;
    double med, var, sd, mean, sum, varsum;

    sum = 0;
    for (int i = 0; i < length; i++)
    {
        sum += numbers [ i ];
    }
    med   = numbers [ length / 2];
    mean = sum / (double) length;

    varsum = 0;
    for (int i = 0; i < length; i++)
    {
        varsum = varsum  + ((numbers [ i ] - mean) * (numbers [ i ] - mean));
    }
    var = varsum / ( length - 1.0 );
    sd  = Math.sqrt ( var );

    System.out.println ("length:                    " + length);
    System.out.println ("mean:                      " + mean);
    System.out.println ("median:                    " + med);
    System.out.println ("variance:                  " + var);
    System.out.println ("standard deviation: " + sd);
}
```

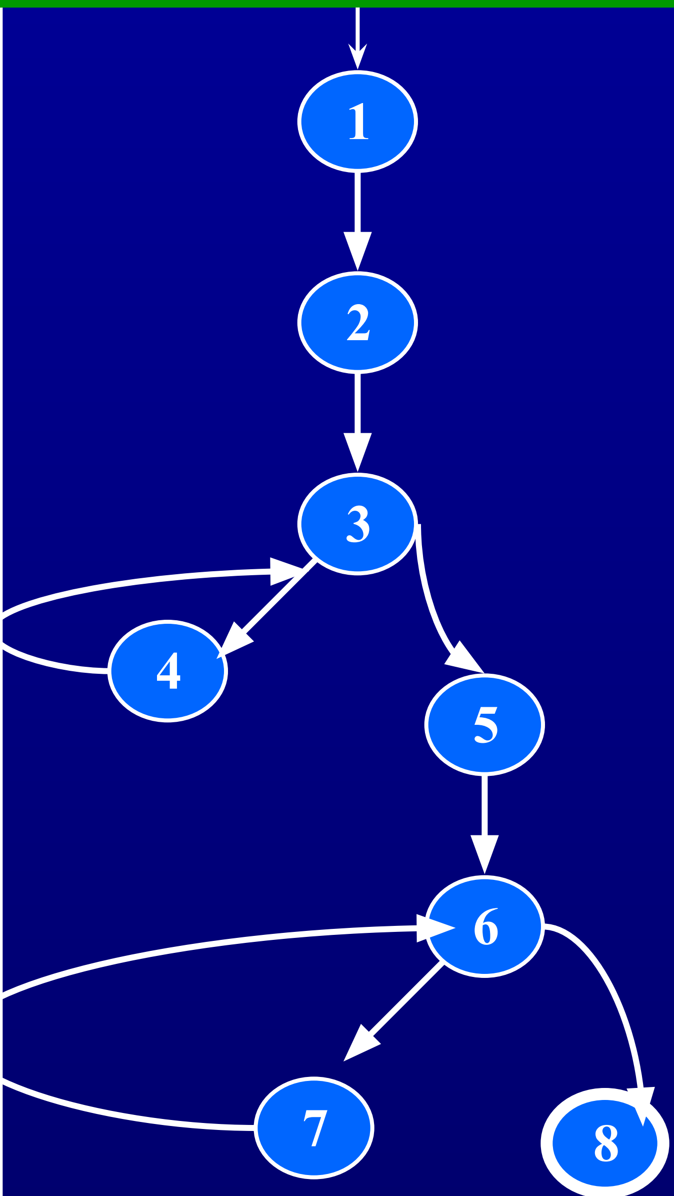
Draw the graph and label the edges.

Control Flow Graph for Stats

```
public static void computeStats (int [ ] numbers)
{
    int length = numbers.length;
    double med, var, sd, mean, sum, varsum;

    sum = 0;
    for (int i = 0; i < length; i++)
    {
        sum += numbers [ i ];
    }
    med   = numbers [ length / 2];
    mean = sum / (double) length;

    varsum = 0;
    for (int i = 0; i < length; i++)
    {
        varsum = varsum  + ((numbers [ I ] - mean) * (numbers [ I ] - mean));
    }
    var = varsum / ( length - 1.0 );
    sd  = Math.sqrt ( var );

    System.out.println ("length:                    " + length);
    System.out.println ("mean:                      " + mean);
    System.out.println ("median:                    " + med);
    System.out.println ("variance:                  " + var);
    System.out.println ("standard deviation: " + sd);
}
```



Control Flow TRs and Test Paths—EC

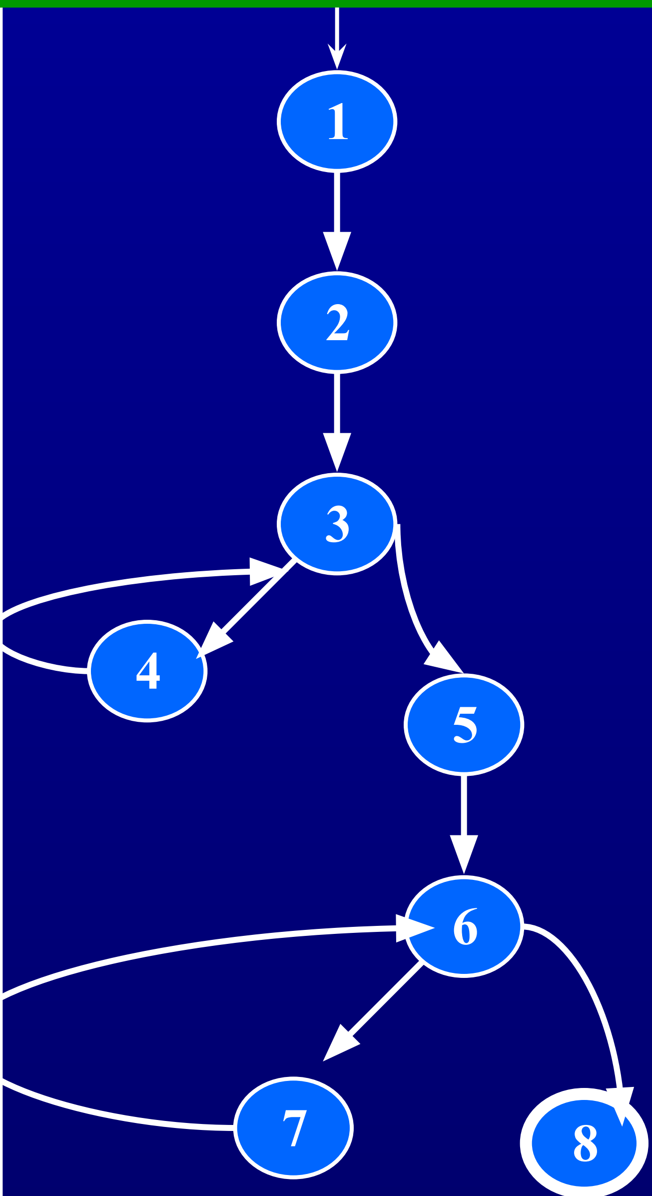


Edge Coverage	
TR	**Test Path**
A. [1, 2]	[1, 2, 6, 8]
D. [3, 5]	
E. [4, 3]	
F. [5, 6]	
G. [6, 7]	
H. [6, 8]	
I. [7, 6]	

Write down the TRs for EC

Write down test paths that tour all edges.

Control Flow TRs and Test Paths—EPC



Edge-Pair Coverage

TR

A. [1, 2, 3]

Write down TRs for EPC.

D. [3, 4, 3]
E. [3, 5, 6]
F. [4, 3, 5]
G. [5, 6, 7]
H. [5, 6, 8]
I. [6, 7, 6]
J. [7, 6, 8]
K. [4, 3, 4]
L. [7, 6, 7]

Test Paths

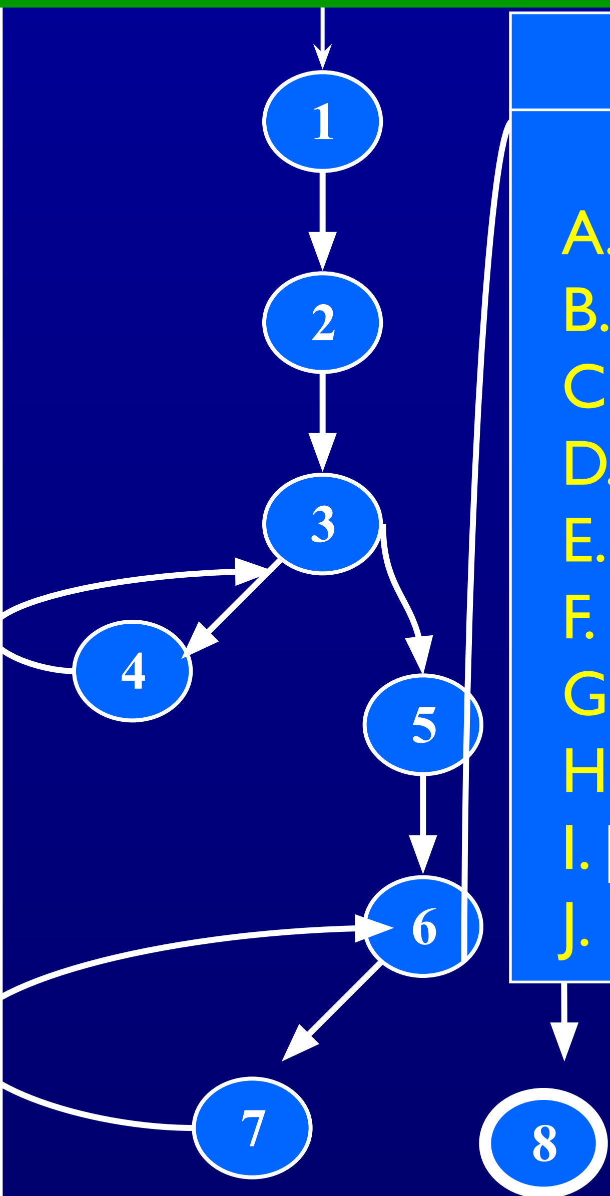
i. [1, 2, 3, 4, 3, 5, 6, 7, 6, 8]
ii. [1
iii. [1 … , 6, 7, 6, 7, 6, 8]

Write down test paths that tour all edge pairs.

TP	TRs toured	*sidetrips*
~~i~~	~~A, B, D, E, F, G, I, J~~	C, H
ii	A, C, E, H	
iii	A, B, D, E, F, G, I, J, K, L	C, H

TP iii makes TP i redundant. A *minimal* set of TPs is cheaper.

Control Flow TRs and Test Paths—PPC



Prime Path Coverage

TR

A. [3, 4, 3]
B. [4
C. [7
D. [7, 6, 8]
E. [6, 7, 6]
F. [1, 2, 3, 4]
G. [4, 3, 5, 6, 7]
H. [4, 3, 5, 6, 8]
I. [1, 2, 3, 5, 6, 7]
J. [1, 2, 3, 5, 6, 8]

Write down TRs for PPC.

Test Paths

i. [1, 2, 3, 4, 3, 5, 6, 7, 6, 8]
ii. [1
iii. [1, 2, 3, 4, 3, 5, 6, 8]
iv. [1, 2, 3, 5, 6, 7, 6, 8]
v. [1, 2, 3, 5, 6, 8]

Write down test paths that tour all prime paths.

TP	TRs toured	*sidetrips*
~~i~~	~~A, D, E, F, G~~	~~H, I, J~~
ii	A, B, C, D, E, F, G,	H, I, J
iii	A, F, H	J
iv	D, E, F, I	J
v	J	

TP ii makes TP i redundant.

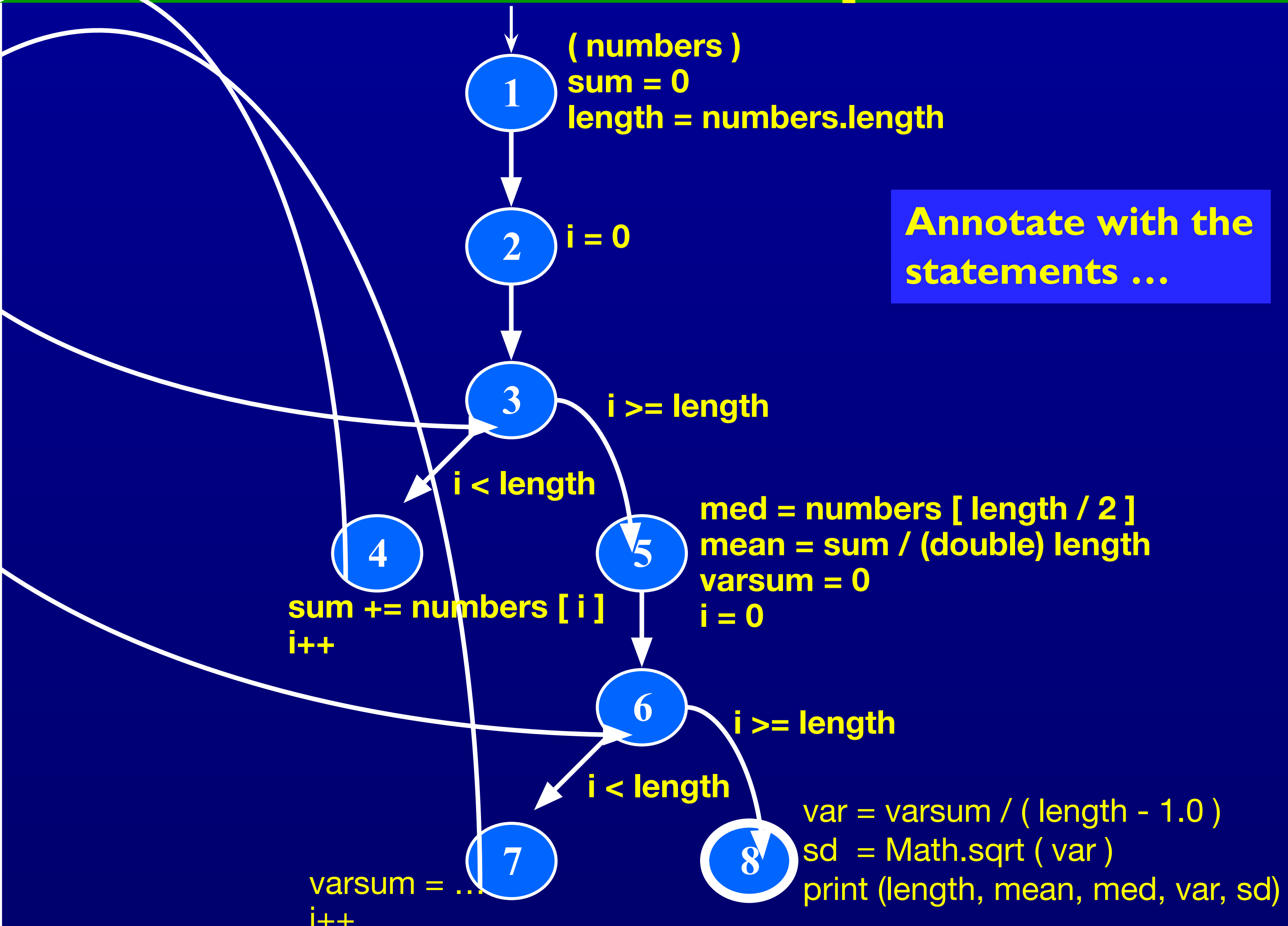
Data Flow Coverage for Source

- def : a location where a value is stored into memory
  - x appears on the left side of an assignment (x = 44;)
  - x is an actual parameter in a call and the method changes its value
  - x is a formal parameter of a method (implicit def when method starts)
  - x is an input to a program
- use : a location where variable's value is accessed
  - x appears on the right side of an assignment
  - x appears in a conditional test
  - x is an actual parameter to a method
  - x is an output of the program
  - x is an output of a method in a return statement
- If a def and a use appear on the same node, then it is only a DU-pair if the def occurs after the use and the node is in a loop

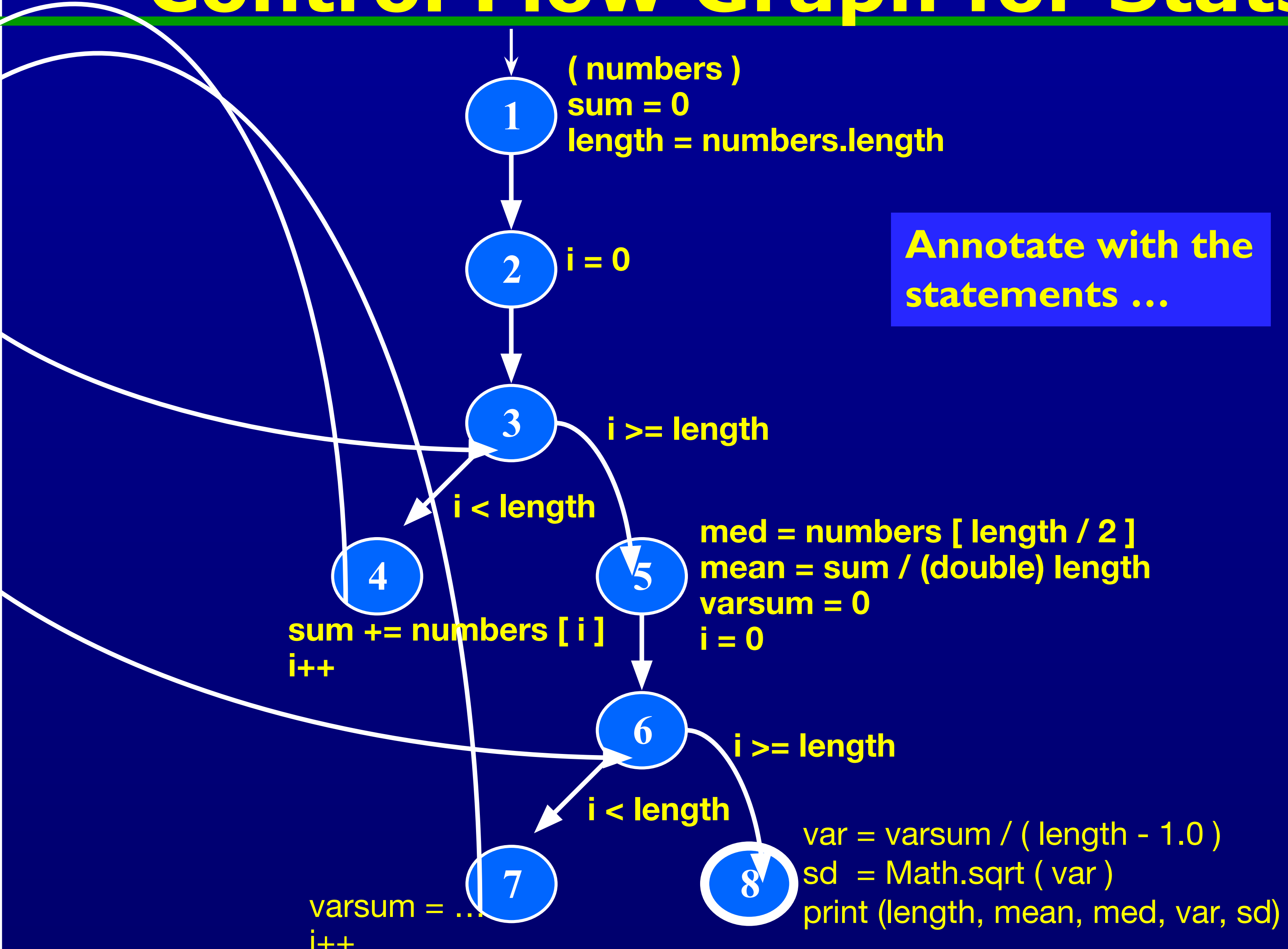
Example Data Flow – Stats

```
public static void computeStats (int [ ] numbers)
{
    int length = numbers.length;
    double med, var, sd, mean, sum, varsum;

    sum = 0.0;
    for (int i = 0; i < length; i++)
    {
        sum += numbers [ i ];
    }
    med   = numbers [ length / 2 ];
    mean = sum / (double) length;

    varsum = 0.o;
    for (int i = 0; i < length; i++)
    {
        varsum = varsum  + ((numbers [ i ] - mean) * (numbers [ i ] - mean));
    }
    var = varsum / ( length - 1 );
    sd  = Math.sqrt ( var );

    System.out.println ("length:                  " + length);
    System.out.println ("mean:                    " + mean);
    System.out.println ("median:                  " + med);
    System.out.println ("variance:                " + var);
    System.out.println ("standard deviation: " + sd);
}
```

Control Flow Graph for Stats

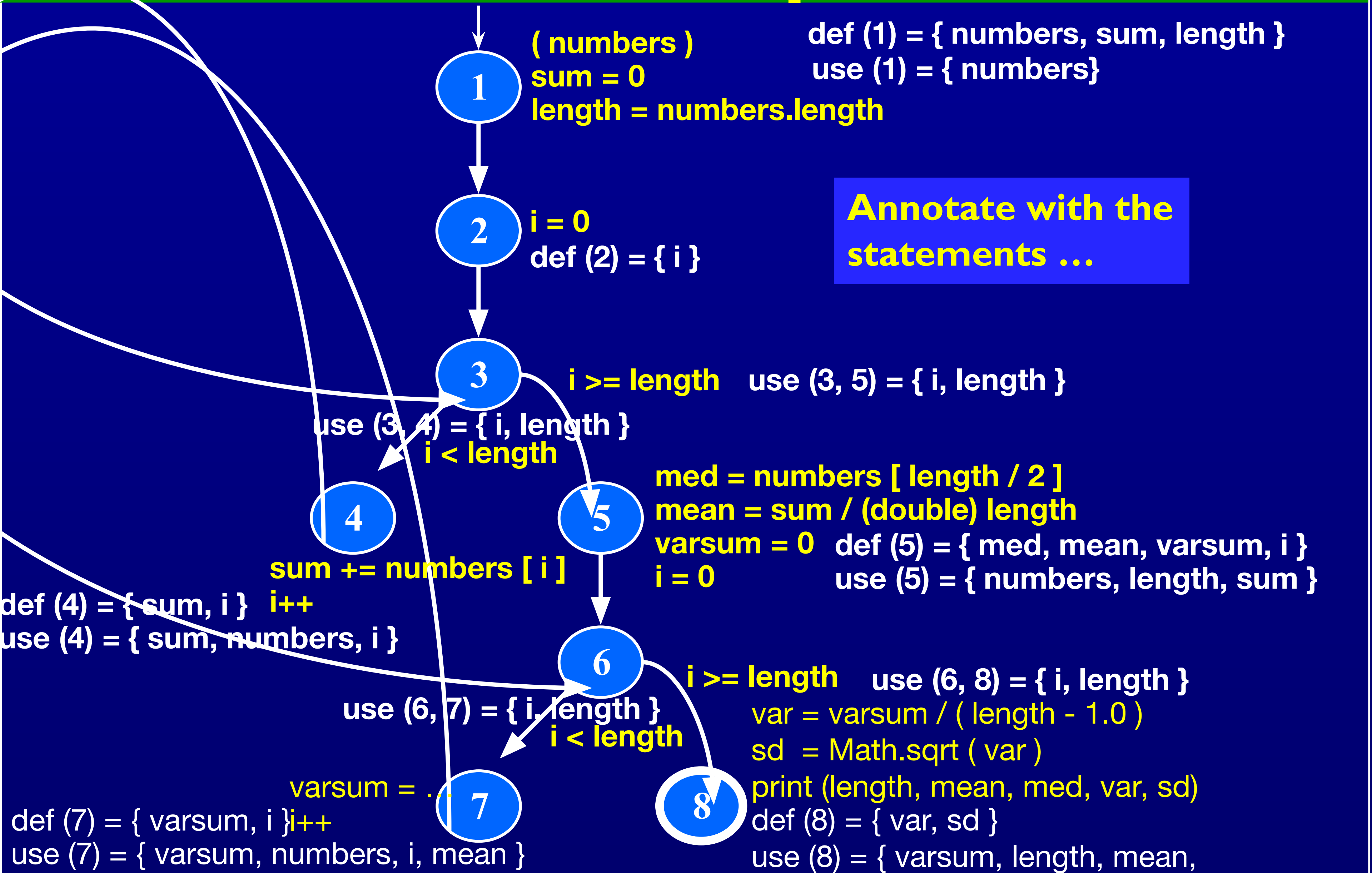


Control Flow Graph for Stats

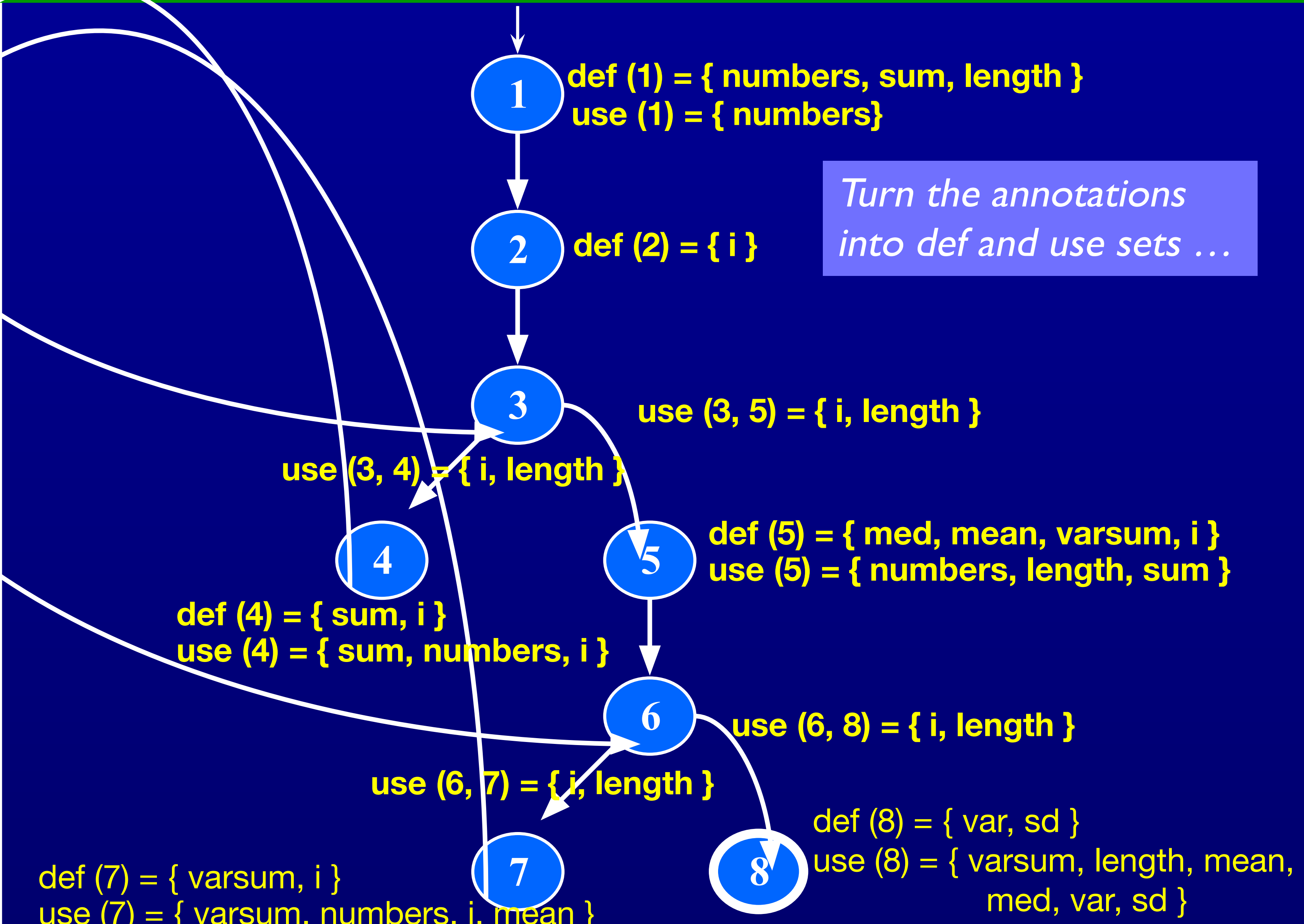


Annotate with the statements …

Control Flow Graph for Stats



CFG for Stats – With Defs & Uses



Turn the annotations into def and use sets …

Defs and Uses Tables for Stats

Node	Def	Use
1	{ numbers, sum, length }	{ numbers }
2	{ i }	
3		
4	{ sum, i }	{ numbers, i, sum }
5	{ med, mean, varsum, i }	{ numbers, length, sum }
6		
7	{ varsum, i }	{ varsum, numbers, i, mean }
8	{ var, sd }	{ varsum, length, var, mean, med, var, sd }

Edge	Use
(1, 2)	
(2, 3)	
(3, 4)	{ i, length }
(4, 3)	
(3, 5)	{ i, length }
(5, 6)	
(6, 7)	{ i, length }
(7, 6)	
(6, 8)	{ i, length }

DU Pairs for Stats

variable	DU Pairs
numbers	(1, 4) (1, 5) (1, 7)
length	(1, 5) (1, 8) (1, (3,4)) (1, (3,5)) (1, (6,7)) (1, (6,8))
med	(5, 8)
var	(8, 8)
sd	(8, 8)
mean	(5, 7) (5, 8)
sum	(1, 4) (1, 5) (4, 4) (4, 5)
varsum	(5, 7) (5, 8) (7, 7) (7, 8)
i	(2, 4) (2, (3,4)) (2, (3,5)) ~~(2, 7) (2, (6,7)) (2, (6,8))~~ (4, 4) (4, (3,4)) (4, (3,5)) ~~(4, 7) (4, (6,7)) (4, (6,8))~~ (5, 7) (5, (6,7)) (5, (6,8)) (7, 7) (7, (6,7)) (7, (6,8))

defs come <u>before</u> uses, do not count as DU pairs

defs <u>after</u> use in loop, these are valid DU pairs

No def-clear path … different scope for i

No path through graph from nodes 5 and 7 to 4 or 3

DU Paths for Stats

variable	DU Pairs	DU Paths
numbers	(1, 4) (1, 5) (1, 7)	[1, 2, 3, 4] [1, 2, 3, 5] [1, 2, 3, 5, 6, 7]
length	(1, 5) (1, 8) (1, (3,4)) (1, (3,5)) (1, (6,7)) (1, (6,8))	[1, 2, 3, 5] [1, 2, 3, 5, 6, 8] [1, 2, 3, 4] [1, 2, 3, 5] [1, 2, 3, 5, 6, 7] [1, 2, 3, 5, 6, 8]
med	(5, 8)	[5, 6, 8]
var	(8, 8)	*No path needed*
sd	(8, 8)	*No path needed*
sum	(1, 4) (1, 5) (4, 4) (4, 5)	[1, 2, 3, 4] [1, 2, 3, 5] [4, 3, 4] [4, 3, 5]

variable	DU Pairs	DU Paths
mean	(5, 7) (5, 8)	[5, 6, 7] [5, 6, 8]
varsum	(5, 7) (5, 8) (7, 7) (7, 8)	[5, 6, 7] [5, 6, 8] [7, 6, 7] [7, 6, 8]
i	(2, 4) (2, (3,4)) (2, (3,5)) (4, 4) (4, (3,4)) (4, (3,5)) (5, 7) (5, (6,7)) (5, (6,8)) (7, 7) (7, (6,7)) (7, (6,8))	[2, 3, 4] [2, 3, 4] [2, 3, 5] [4, 3, 4] [4, 3, 4] [4, 3, 5] [5, 6, 7] [5, 6, 7] [5, 6, 8] [7, 6, 7] [7, 6, 7] [7, 6, 8]

DU Paths for Stats—No Duplicates

There are 38 DU paths for Stats, but only 12 unique

[1, 2, 3, 4]	[4, 3, 4]
[1, 2, 3, 5]	[4, 3, 5]
[1, 2, 3, 5, 6, 7]	[5, 6, 7]
[1, 2, 3, 5, 6, 8]	[5, 6, 8]
[2, 3, 4]	[7, 6, 7]
[2, 3, 5]	[7, 6, 8]

4 expect a loop not to be "entered"

6 require at least one iteration of a loop

2 require at least two iterations of a loop

Test Cases and Test Paths

Test Case : numbers = (44) ; length = 1

Test Path : [1, 2, 3, 4, 3, 5, 6, 7, 6, 8]

Additional DU Paths covered (no sidetrips)

[1, 2, 3, 4]   [2, 3, 4]   [4, 3, 5]   [5, 6, 7]   [7, 6, 8]

The five stars ✦ that require at least one iteration of a loop

Test Case : numbers = (2, 10, 15) ; length = 3

Test Path : [1, 2, 3, 4, 3, 4, 3, 4, 3, 5, 6, 7, 6, 7, 6, 7, 6, 8]

DU Paths covered (no sidetrips)

[4, 3, 4]   [7, 6, 7]

The two stars that require at least two iterations of a loop

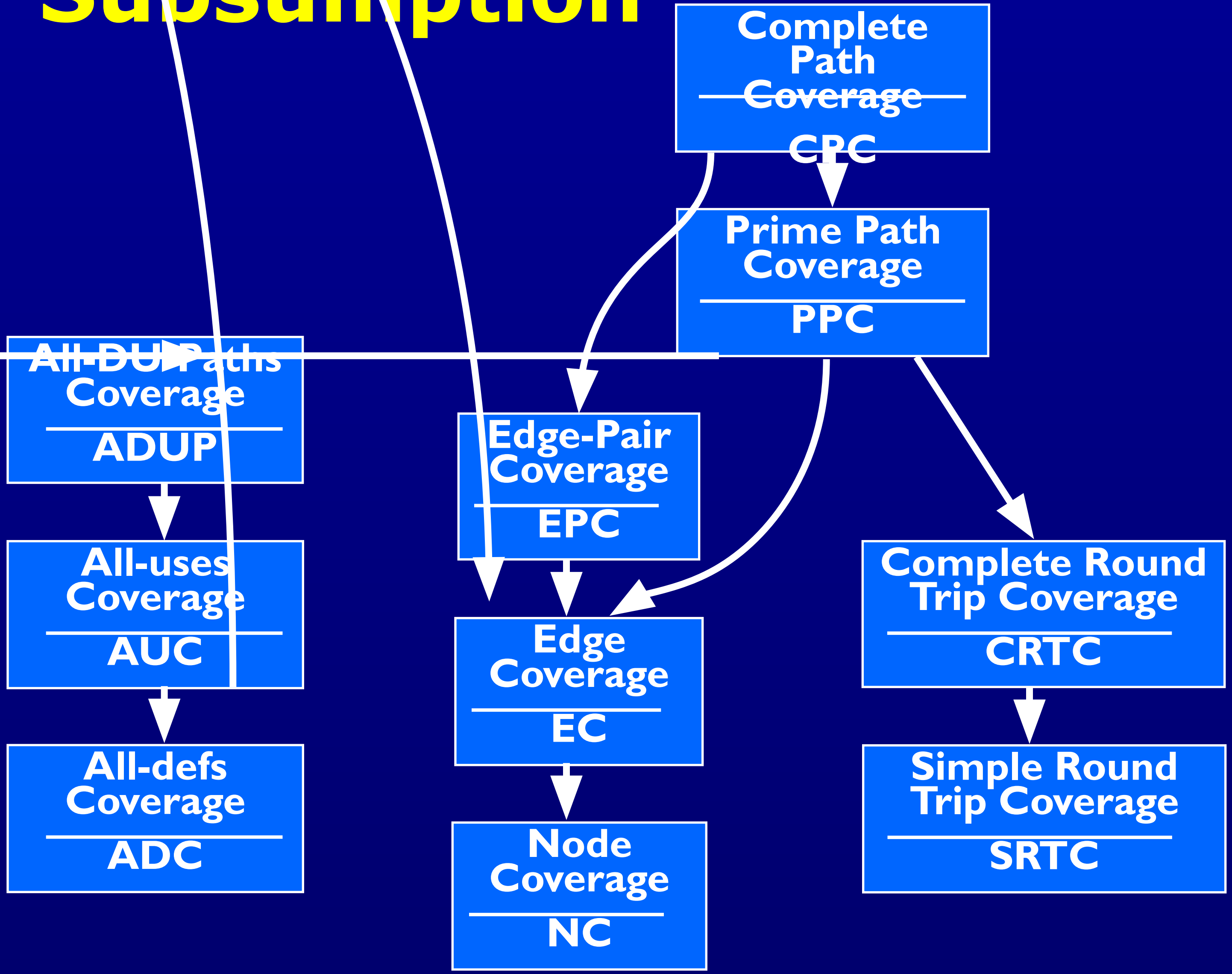
Other DU paths ★ require arrays with length 0 to skip loops

But the method fails with index out of bounds exception…

med = numbers [length / 2];

A fault was found

Graph Coverage Criteria Subsumption



Summary

- Applying the graph test criteria to control flow graphs is relatively straightforward
  - Most of the developmental research work was done with CFGs
- A few subtle decisions must be made to translate control structures into the graph
- Some tools will assign each statement to a unique node
  - These slides and the book uses basic blocks
  - Coverage is the same, although the bookkeeping will differ

Required Readings

- Sections 7.1, 7.2, and 7.3 from the textbook.