

Lecture 13

State-action-reward-state-action (SARSA)

Q-learning:

Go through a number of episodes

start an episode with an S

Go through the episode step by step

Sarsa $Q = Q_{\text{new}}$ — give you policy

based on Q , choose an action a .

— ϵ -greedy

base on

$$V = \max_a (Q(s, a))$$

or
random

Take action a , get reward, get to a new state s'

$$Q_{\text{curr}} = r + \gamma \frac{V(s')}{\downarrow}$$

— Update

$$Q_{\text{new}}(s, a) = Q(s, a) + \alpha (Q_{\text{curr}}(s, a) - Q(s, a))$$

if $\alpha = 1$ \uparrow

$$S \leftarrow s'$$

continue until to the end of the episode.

Learn

Sarsa:

Go through a number of episode

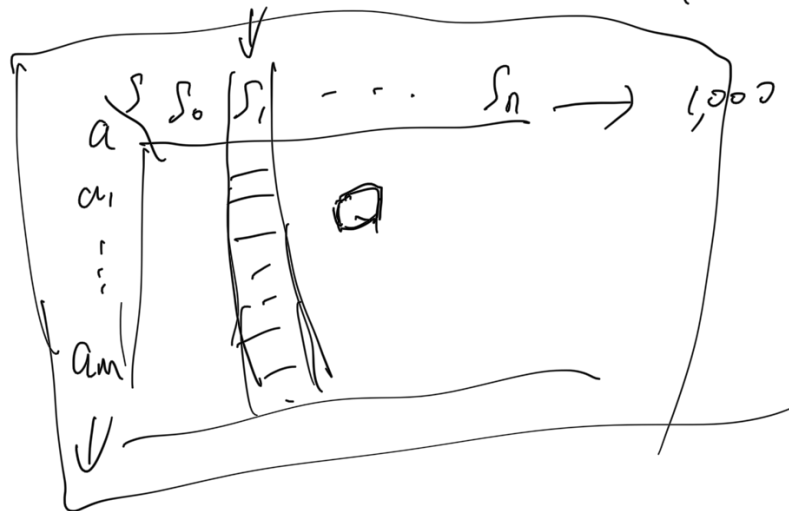
start with an S

→ choose actions use the current Q (ϵ -greedy)

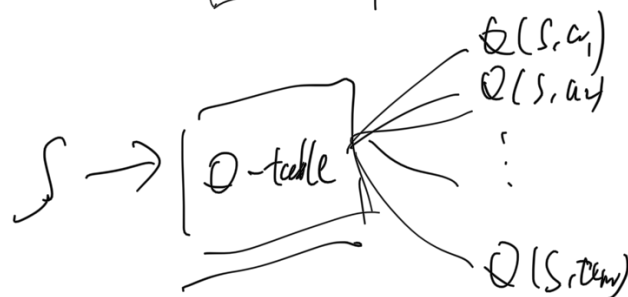
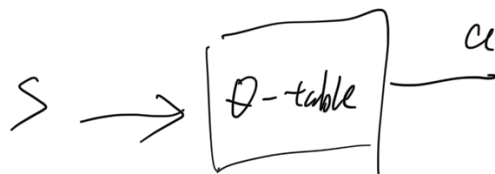
then carry out those chosen actions.

take one action at a time, get reward,
reach to a new state S'

$$Q_{\text{new}}(S, a) \leftarrow Q(S, a) + \alpha (R_{\text{current}}(S, a) - Q(S, a))$$



Q -learn

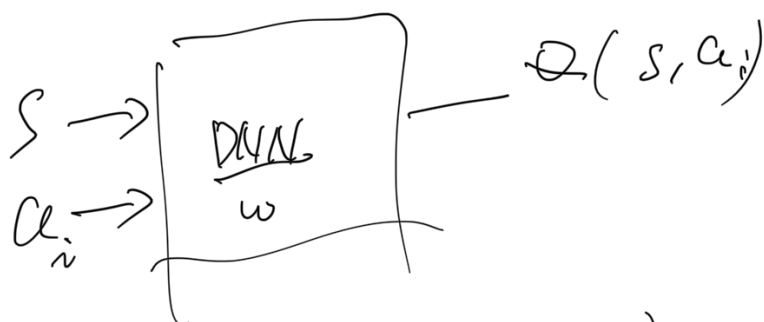


X	Y
x_1	y_1
x_2	y_2
\vdots	\vdots
x_n	y_n

$$\Rightarrow y = f(x)$$

look up table

regression



$$Q(s, a) \rightarrow Q(s, a, w)$$

neural network

if you know the ground truth $\hat{Q}(s, a)$

input: $(s, a)_k$, out is over $\hat{Q}(s, a)$

s	a	$\hat{Q}(s, a)$
x_1	x_2	y

$$L = \frac{1}{2} \sum (Q(s, a, w) - \hat{Q}(s, a))^2$$



$$\frac{\partial L}{\partial w}$$

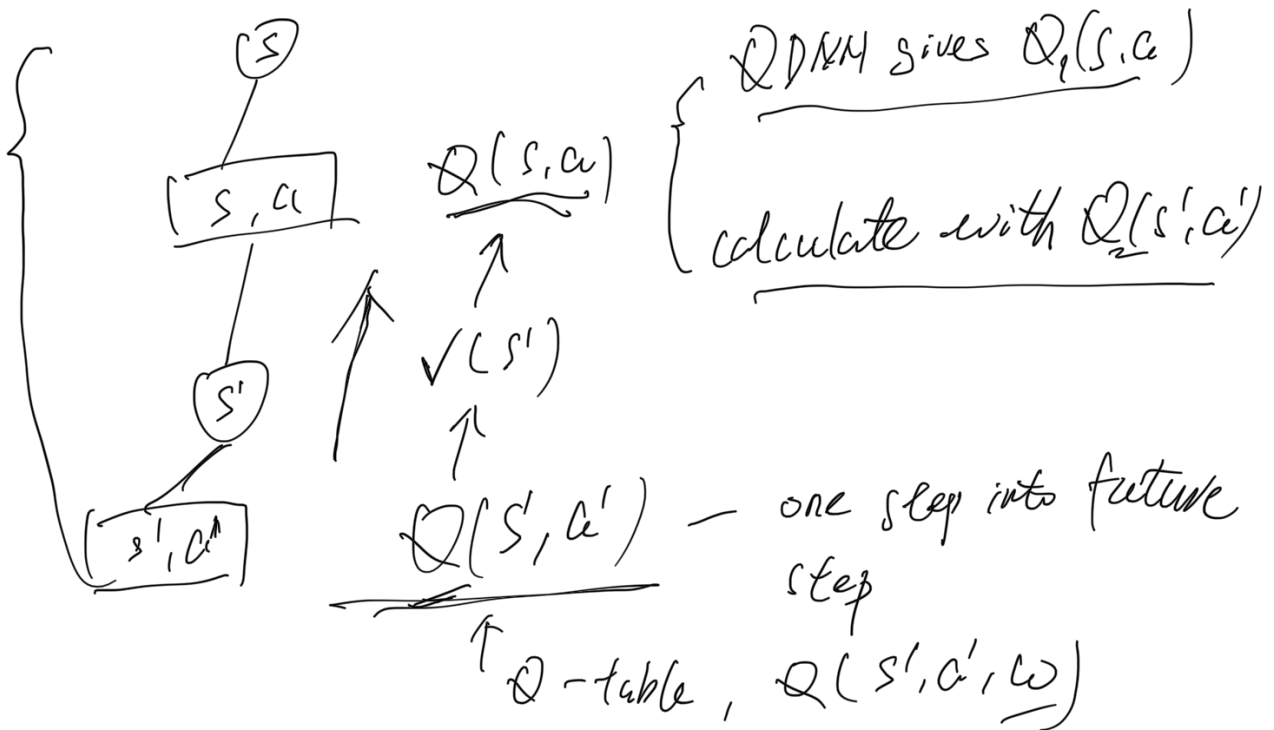


Q

Q-table

$$\begin{cases} Q(s, a, \omega) \text{ — current QNM} \\ Q_{\text{curr}}(s, a) = r + \lambda \max_{a'} Q(s', a', \omega) \end{cases}$$

s' is next state after take action a .



$$\begin{array}{cc} \begin{array}{c} s \\ a \end{array} \begin{array}{|c|} \hline \omega \\ \hline \end{array} \begin{array}{c} \leftarrow Q(s, a) \end{array} & \begin{array}{c} s' \\ a' \end{array} \begin{array}{|c|} \hline \omega \\ \hline \end{array} \begin{array}{c} \leftarrow Q(s', a') \end{array} \\ \hline \uparrow & \uparrow \\ (s, a, r, s') & \\ \hline L(\omega) = \left(\underbrace{Q_{\text{curr}}(s, a, \omega)}_{\substack{\uparrow \\ \text{current } r}} - \underbrace{Q(s, a, \omega)}_{\substack{\uparrow \\ \text{previous from NM}}} \right)^2 \end{array}$$

Loss

\uparrow
 Q_1

Q_2

$$\frac{\partial L(w)}{\partial w}$$

$$L = \sum_{i=1}^N (y_i - \hat{y}_i)^2, \quad N \text{ samples. for regular DNN}$$

for one (s_i, a_i, r_i, s_{i+1}) , we have on L_i

$$L = \sum_{i=1}^N L_i, \quad N \text{ could be very large.}$$

Get all (s_i, a_i, r_i, s_{i+1}) ,

sample, put into mini-batch,

calculate loss like mini-batch

Double Q -learning:

Train two Q 's, Q_1 and Q_2

Do Q -learning on both

$$\underline{Q_{1-w}}(s, a) = r + \gamma \max_{a'} (\underline{Q_2}(s', a'))$$

iterate

$$Q_{\pi}^w(s, a) = r + \gamma \max_{a'} (Q_{\pi}(s', a'))$$